## a ranked alphabet

arity 2

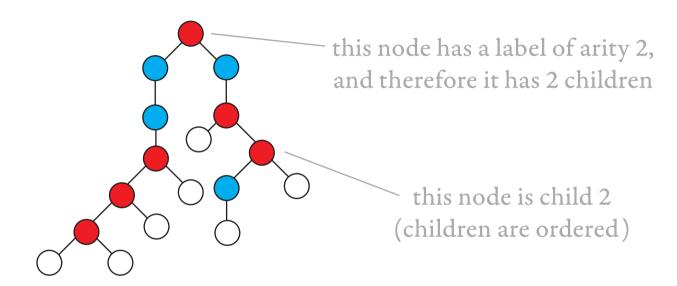


arity 1



arity 0

a tree







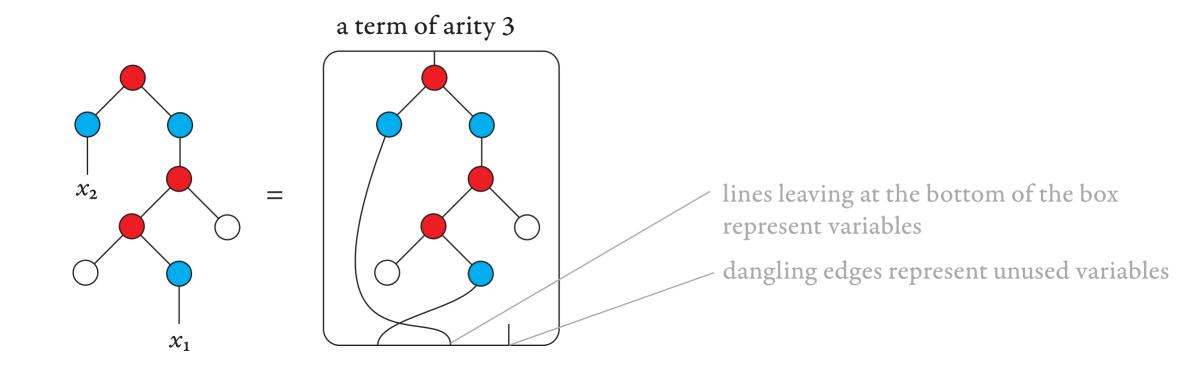


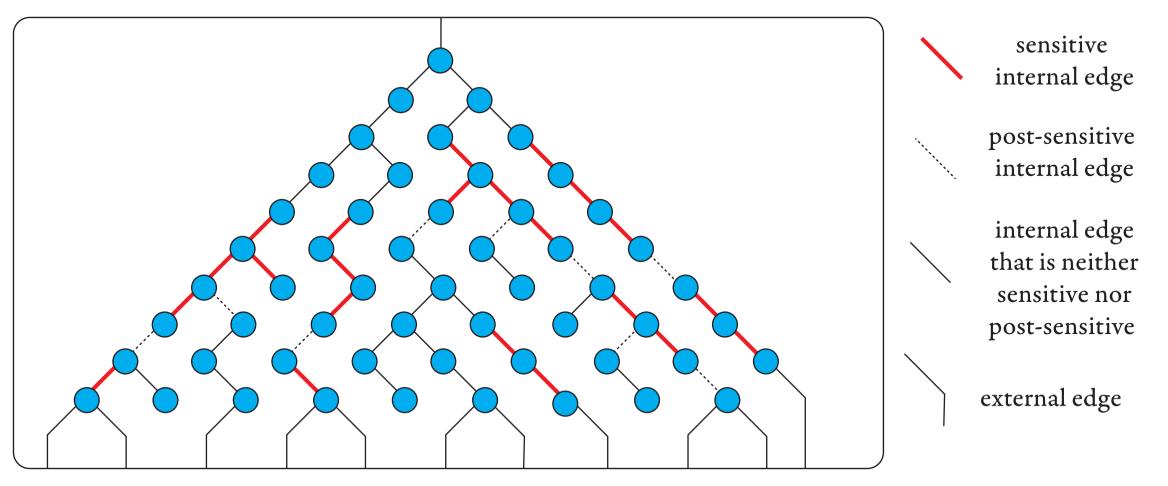


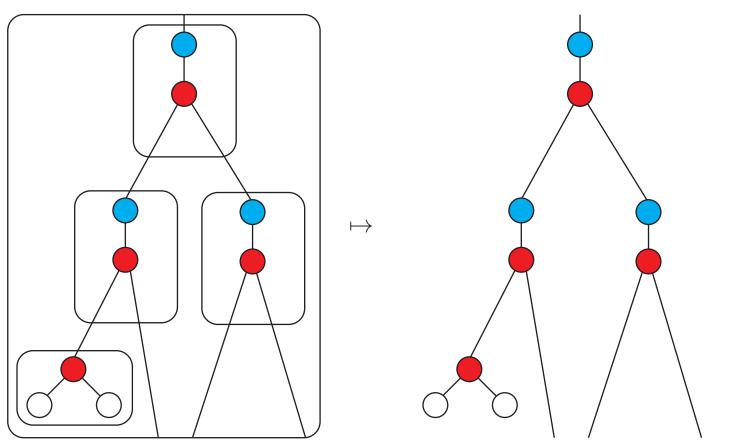
## substitute(t)







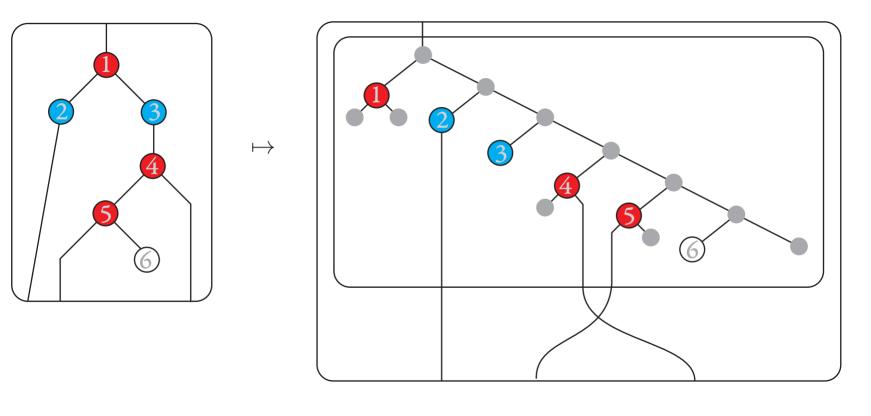






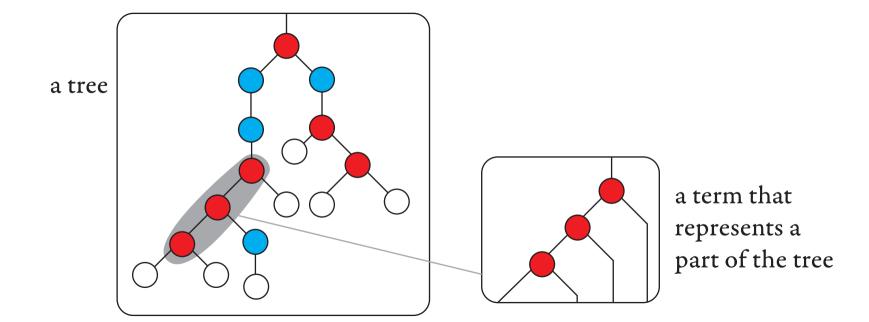




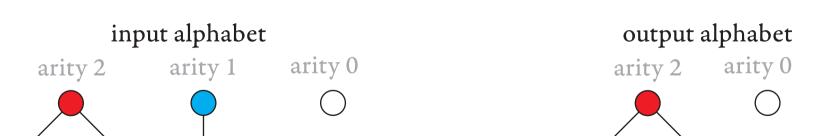


a factorisation equivalence































If the root has arity n, and  $1 \le i < j \le n$ , then all ports of the *j*-th subterm of the root are after all ports of the *i*-th subterm of the root



satisfies (\*)

violates (\*)

a register update

its dual

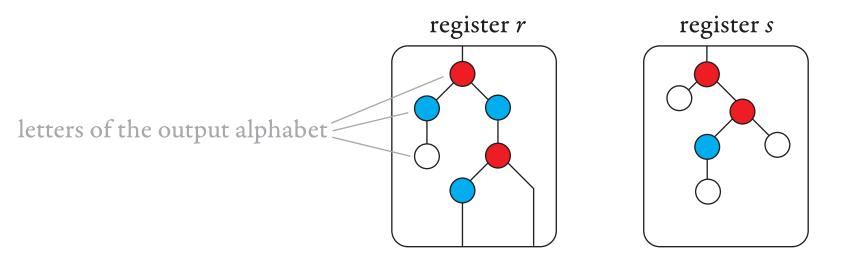


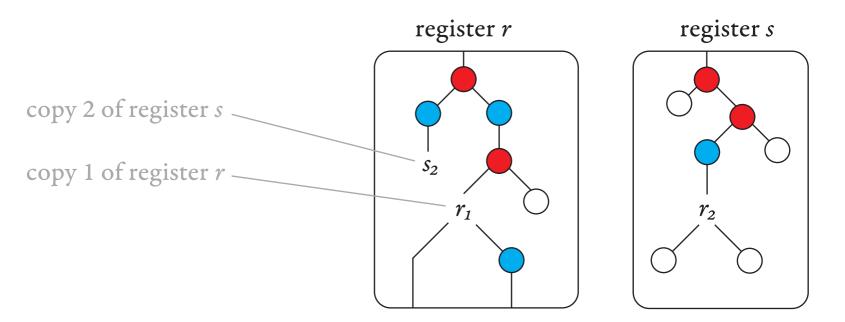
Variable *i.j* represents register *i* in the *j*-th argument of the reigster update.

In the dual, this variable is mapped to the *i*-th edge which enters the *j*-th port of the reducer.

















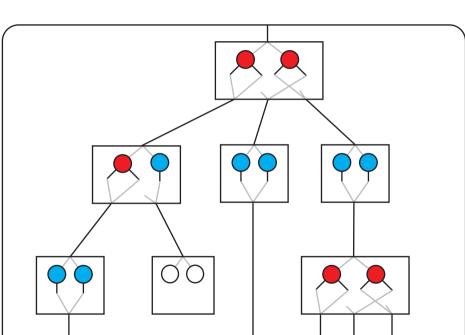


factors with branching nodes

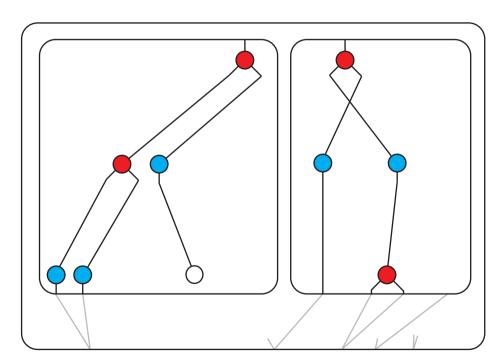


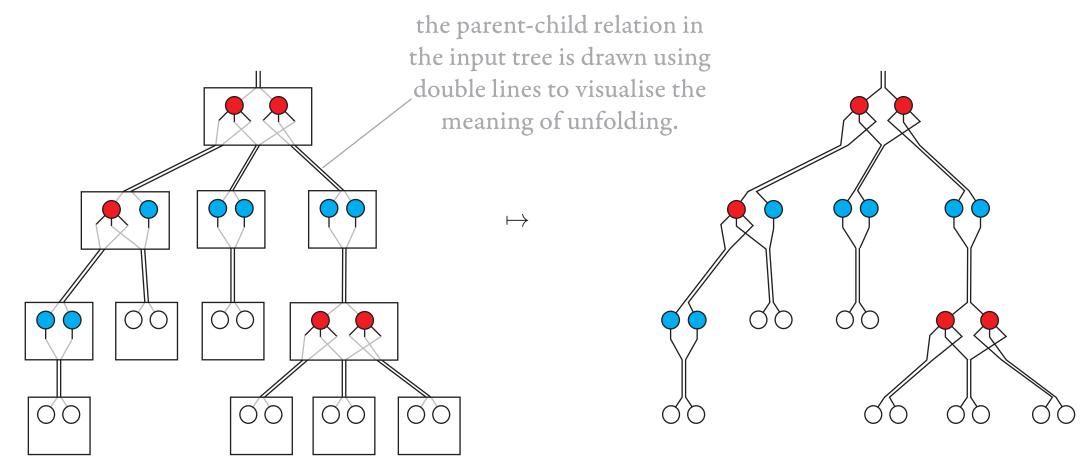


a term of matrix powers



its term unfolding















λ-term of type *o* 



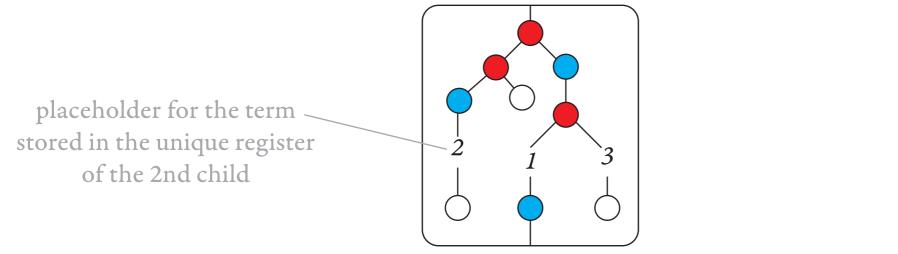




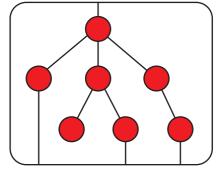
 $\lambda x$ .

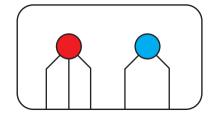


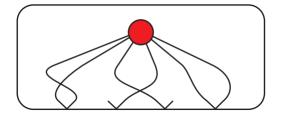




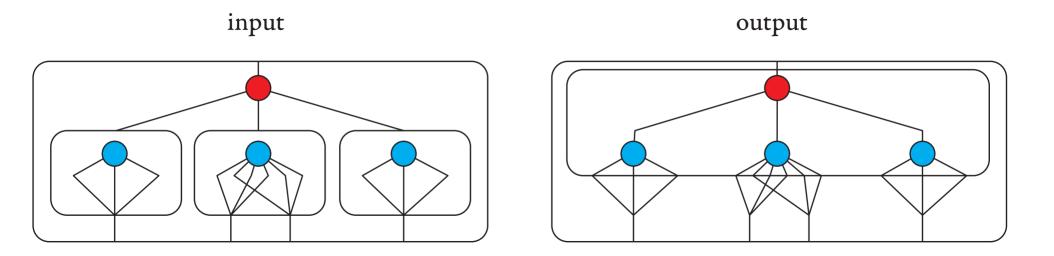


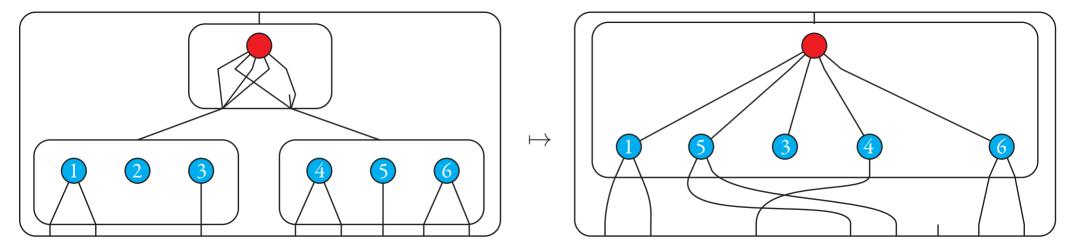
















its representation as a  $\lambda$ -term





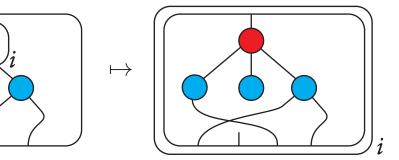


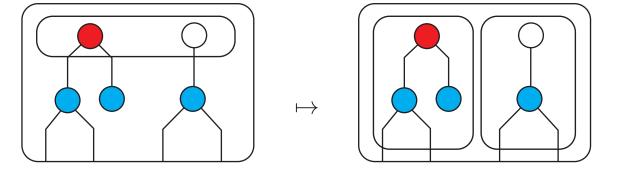


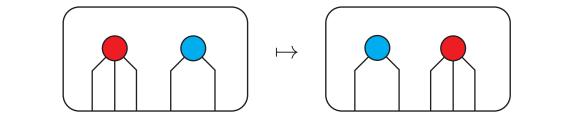






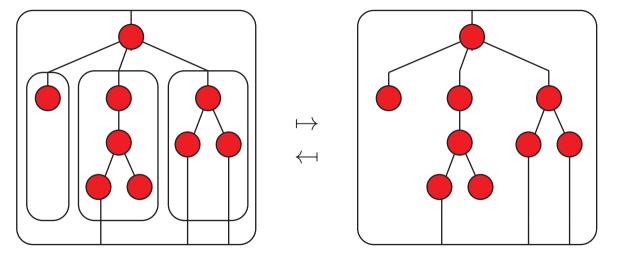


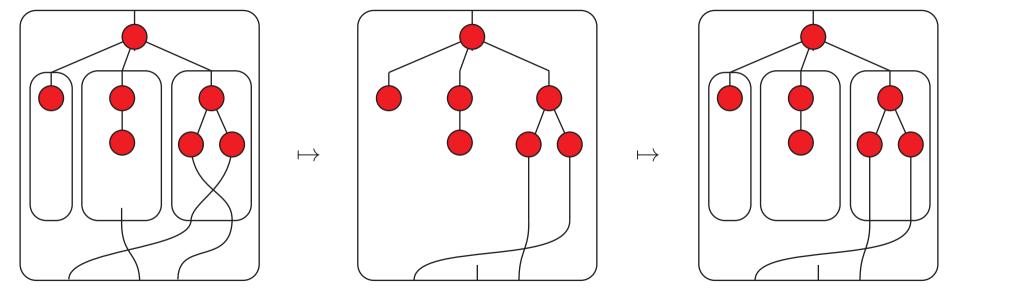










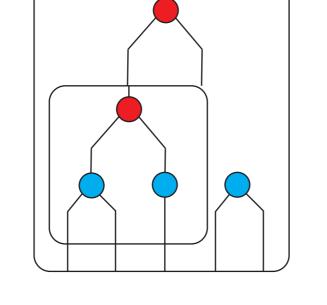


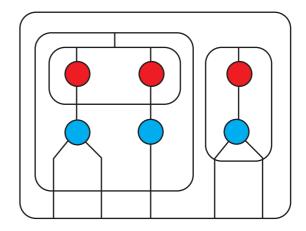


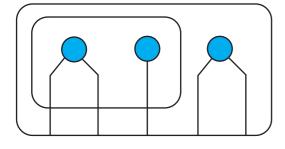






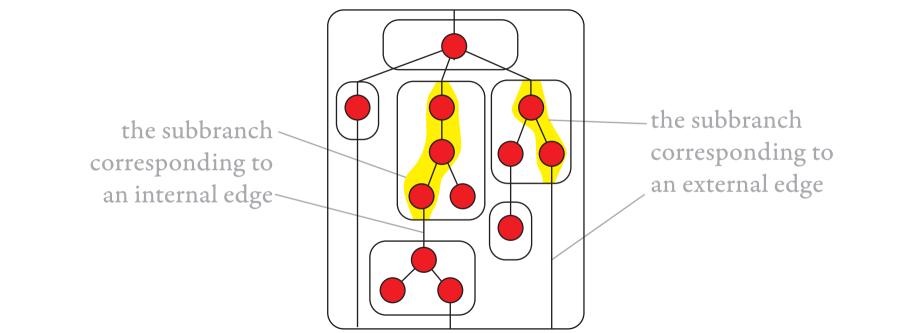


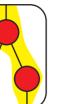






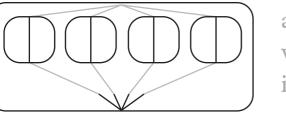






a branch can be visualised as a term with a distinguished root-to-port path





a tuple of *k* identity terms with all their ports folded into one

$$\Sigma = \{ \bigcirc, \bigcirc, \bigcirc \}$$
  $a \in \Sigma^{[2]}$   $b \in \Sigma^{[2]}$ 

