

Anthony Poerio (adp59@pitt.edu)

CS1674: Homework 10 - Written

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QUESTIONS

1) Why do we say neural networks are not linear classifiers?

A neural network is more specifically a “non-linear classifier.” This is because a neural network can model *any arbitrarily complex* function—as long as it is continuous. And in fact, when there are very many “layers” in a neural network, this is exactly what happens. So, to call a neural network a ‘linear’ classifier would be inaccurate.

The function that a complicated multi-layered neural network approximates would be hard to approximate linearly.

2) Briefly describe one way in which artificial neurons resemble brain neurons.

In a neural network, we use artificial neurons called ‘perceptrons’. These are much more simplistic than brain neurons--BUT, both are objects are similar in that:

1. They essentially form a ‘graph’ of sorts, connecting themselves with other neurons in their respective systems.
2. Each kind of neuron can have some arbitrary number of inputs.
3. Information can flow OUT of the neuron and into other neurons (as input) if the output function reaches some set threshold (we call this ‘firing’).
4. In this way, both structures can be used to transfer information in a complex way across graph.

- 3) Say a vision system predicts the following scores for a cat image: 10 for the category "cat," 5 for the category "dog," and 3 for the category "cow." Another system predicts scores 8, 6 and 1 for the same categories. Is the SVM loss the same or different for these two systems? What about the softmax loss? Why?

SVM Loss (assuming we use the loss function on slides 41-45 in the neural net slide set):

- System 1 calculation
 - $\text{Max}(0, 5-10 +1) + \text{Max}(0, 3-10 +1) = 0$
- System 2 Calculation
 - $\text{Max}(0, 6-8 +1) + \text{Max}(0, 1-8 +1) = 0$
 - Therefore, SVM Loss is *same* for both systems, **because we are taking a max with 0**, and therefore the lowest possible value is 0.
 - If we allowed for a negative value, however → then the SVM Losses would be different.

Softmax Loss:

- Softmax Loss would very likely be different for both systems, because its output is **an exact probability**, as a Real Number in the range [0,1). Moreover, we aren't using a max, in this function. So, there's no operation by which we would have an 'artificial cutoff' of sorts, like we do when taking the max calculations of the SVM Loss function.

4) Briefly, how does gradient descent work?

Essentially, gradient descent works by iteratively looking for the vector with the steepest downward slope from any given point in some arbitrary high-dimensional space.

Then, we take a 'step' of some specified distance in the direction of that steepest downward slope, and repeat.

We repeat this until we find what is likely the 'bottom' or minimum point in that space. Often it is useful to find minimizing functions/values/vectors/distances (i.e. – for matching), and this is an efficient way to do so.

5) What is mini-batch?

Mini batch is a gradient descent algorithm that works *by only taking a subset of the entire data-set into account at each step*.

Practically, this often yields similar results to a full gradient descent algorithm where *all* values are exhaustively checked, and it can be executed much more quickly.

6) How can we prevent overfitting in a neural network?

Speaking generally, overfitting in a neural network is the **result of two things**:

1. **Running too many epochs** on the training data
 - When this happens we fit *too tightly* against the training data itself, and can't generalize effectively
2. **Having too many hidden units** in our model
 - In this case, we are essentially creating a very high-degree polynomial function as our model, which—again—can't generalize well, because it is fit too tightly against our training data. And hence it will match those training data points alone, at the expense of all others.