Documentation: `recommendx`

Installation

`recommendx` has the following dependencies:

- Python (>=3.5)
- NumPy (>=1.10)
- Pandas (>=0.18)

The easiest way to install `recommendx` is using `pip`:

```
pip install recommendx
```

Alternatively, the package can be accessed from Github.

The package contains two related prediction algorirthms: `RWR` and `RWT`. These are discussed below.

Here is some test. We will see if this exports properly. Here is β

Recommendation with Regressors (RWR)

`RWR` implements a slightly modified version of what we might call the "classic" SVD algorithm. This is often attributed to Simon Funk, who famously used it during the Netflix Prize competition. The classic SVD approach relies upon latent item attributes. `RWR` extends this framework by allowing the researcher to specify observed item attributes, as well.

We can define $\hat{r}_{ui}$ as user u's predicted rating for item i:

$$\hat{r}_{ui} = \mu + b_u + X_i\beta_u + Z_i\alpha_u$$

In this specification,

- μ is the average rating in the data

- b_u is the bias for user u
- X_i is a vector of **observed** attributes for item i
- Z_i is a vector of **latent** attributes for item i
- β_u and α_u are user u's preferences for observed and latent item attributes, respectively

This specification is similar to the usual matrix factorization set-up, with the standard item bias term (b_i) replaced by observed attributes.

Defining R as the set of all observed user-item ratings and imposing L2-regularization on our parameters, we seek to minimize the following objective function:

$$\sum_{r_{ui} \in R} = (r_{ui} - \hat{r}_{ui})^2 + \lambda(b_u^2 + ||\beta_u||^2 + ||Z_i||^2 + ||\alpha_u||^2)$$

The minimization is done using stochastic gradient descent (SGD). The relevant gradients, which can easily be obtained by hand, lead to the following update rules:

- $b_u \Longleftarrow b_u + \gamma(e_{ui} - \lambda b_u)$
- $\beta_u \Longleftarrow \beta_u + \gamma(e_{ui} X_i - \lambda \beta_u)$
- $\alpha_u \Longleftarrow \alpha_u + \gamma(e_{ui} Z_i - \lambda \alpha_u)$
- $Z_i \Longleftarrow Z_i + \gamma(e_{ui} \alpha_u - \lambda Z_i)$

where $e_{ui} = r_{ui} - \hat{r}_{ui}$, λ is the regularization penalty term, and γ is the SGD learning rate. The learning rate determines how large of a "step" to take when we update parameters.

Parameters

Note: I have purposely chosen the parameter names to be similar to this in Surprise in order to facilitate easy movement between packages.

- **n_factors** - The number of latent factors in Z. Default is `50`.
- **n_epochs** - The number of iterations of the SGD procedure. Default is `50`.
- **init_mean** - The mean of the normal distribution used to initialize parameter values. Default value is `0`.
- **init_std_dev** - The standard deviation of the normal distribution used to initialize parameter values. Default is `0.1`.
- **reg** - The regularization penalty term used for all parameters (λ). Default is `0.02`.
- **lr** - The learning rate for all parameters (γ). Default is `0.005`.

Attributes

Once an `RWR` instance is `fit()`, the resulting parameter values are returned as attributes of the instance.

- `intercept_` (μ)
    - Scalar intercept term
- `bu` (b_u)
    - NumPy array with shape (`n_users` ,1)
- `B` (β_u)
    - If X_i is provided to `fit()` (see below), `B` is a NumPy array with shape (`n_users` , `n_Xs`)
- `alpha_` (α_u)
    - NumPy array with shape (`n_users` , `n_factors`)
- `Z` (Z_i)
    - NumPy array with shape (`u_items` , `n_factors`)

Methods

- `fit(self,df,Xi=None)`
    - Fits the recommender system model
    - `df` must be a NumPy array
        - Each row corresponds to a rating (r_{ui})
        - Columns **must** be ordered: [`user` , `item` , `rating`]
        - `user` and `item` may be strings or integers
    - `Xi` (if supplied) must be a NumPy array
        - If no observed item attributes are supplied, `fit()` returns the same results as SVD
        - First column of `Xi` must be item identifier that corresponds with item labels used in `df`
        - Shape of array is (`n_items` , 1+ `n_Xs`)
    - `accuracy(self,df,Xi=None)`
        - Returns the mean squared prediction error
        - Requires the recommender system be fit first
        - All provided values must be in the same format as supplied to `fit()`
    - `predict(self,u_p,i_p)`
        - Returns predicted ratings
        - `u_p` is a user value

- `i_p` is an item value
- Both `u_p` and `i_p` must be provided in the same format as `fit()`

Sample Syntax

If we assume that `dat` is a NumPy array of ratings data and `att` is a NumPy array of observed item attributes, we can use the following code:

```
from recommendx import RWR
rwr = RWR(n_factors = 5)
rwr.fit(dat,att)
rwr.accuracy(dat,att)
rwr.predict('userA','item1')
```

Recommendation with Time (RWT)

`RWT` implements the same basic model as `RWR` but allows for time-varying taste parameters.

Our main ratings prediction equation becomes:

$$\hat{r}_{uit} = \mu + b_u + X_i\beta_{u,t} + Z_i\alpha_{u,t}$$

Neither observed (X_i) nor latent (Z_i) item attributes vary with time, although one could "trick" the model into allowing that by creating items that are time-specific.

User taste parameters $\beta_{u,t}$ and $\alpha_{u,t}$ are assumed to vary by time period. This allows for the possibility, for example, that a Netflix viewer might be more inclined to enjoy a horror movie at night. Or a coffee drinker may prefer espresso drinks more in the morning than in the evening.

`RWT` requires that time be defined categorically. A simple example might be that time takes the values ["Morning","Afternoon","Night"]. These categorical labels must be assigned by the researcher prior to fitting the recommender.

The model is fit using SGD. The equations are identical to those for `RWR` with the exception that the β and α parameters are now subscripted with time, as well.

Parameters

`RWT` has the same model parameters as `RWR`. Parameter arrays $\beta_{u,t}$ and $\alpha_{u,t}$ are identified only using ratings observations for each specific time period. To account for this, the default value of **n_epochs** has been increased to `100`.

Attributes

Once an `RWT` instance is `fit()`, the resulting parameter values are returned as attributes of the instance.

- `intercept_` (μ)
    - Scalar intercept term
- `bu` (b_u)
    - NumPy array with shape (`n_users` ,1)
- `B` ($\beta_{u,t}$)
    - If X_i is provided to `fit()` (see below), `B` is a 3-dimensional NumPy array with shape (`n_times` , `n_users` , `n_Xs`)
- `alpha_` ($\alpha_{u,t}$)
    - A 3-dimensional NumPy array with shape (`n_times` , `n_users` , `n_factors`)
- `Z` (Z_i)
    - NumPy array with shape (`u_items` , `n_factors`)

Methods

- `fit(self,df,Xi=None)`
    - Fits the recommender system model
    - `df` must be a NumPy array
        - Each row corresponds to a rating (r_{ui})
        - Columns **must** be ordered: [`user` , `item` , `rating` , `time`]
        - `user` and `item` may be strings or integers

        - `time` should be the time label for r_{uit}. Can be string or integer but is treated as categorical
    - `Xi` (if supplied) must be a NumPy array
        - If no observed item attributes are supplied, `fit()` returns the results for SVD withe time-varying parameters
        - First column of `Xi` must be item identifier that corresponds with item labels used in `df`
        - Shape of array is (`n_items` , 1+ `n_Xs`)
    - `accuracy(self,df,Xi=None)`
        - Returns the mean squared prediction error
        - Requires the recommender system be fit first
        - All provided values must be in the same format as supplied to `fit()`
    - `predict(self,u_p,i_p,tee)`
        - Returns predicted ratings
        - `u_p` is a user value
        - `i_p` is an item value
        - `tee` is a time value
        - Both `u_p` , `i_p` , and `tee` must be provided in the same format as `fit()`

Sample Syntax

If we assume that `dat` is a NumPy array of ratings data (with time label) and `att` is a NumPy array of observed item attributes, we can use the following code:

```
from recommendx import RWT
rwt = RWT(n_factors = 3)
rwt.fit(dat,att)
rwt.accuracy(dat,att)
rwt.predict('userA','item1','AM')
rwt.predict('userA','item1','PM')
```