

# Module Interface Specification for Attitude Check

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# 1 Revision History

Date	Version	Notes
March 16, 2024	1.0	Initial document

## 2 Symbols, Abbreviations and Acronyms

See SRS Documentation at [https://github.com/adrian-soch/attitude\\_check/blob/main/docs/SRS/SRS.pdf](https://github.com/adrian-soch/attitude_check/blob/main/docs/SRS/SRS.pdf).

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### 3 Introduction

The following document details the Module Interface Specifications for Attitude Check.

Complementary documents include the System Requirement Specifications and Module Guide. The full documentation and implementation can be found at [https://github.com/adrian-soch/attitude\\_check](https://github.com/adrian-soch/attitude_check).

### 4 Notation

The structure of the MIS for modules comes from Hoffman and Strooper (1995), with the addition that template modules have been adapted from Ghezzi et al. (2003). The mathematical notation comes from Chapter 3 of Hoffman and Strooper (1995). For instance, the symbol  $:=$  is used for a multiple assignment statement and conditional rules follow the form  $(c_1 \Rightarrow r_1 | c_2 \Rightarrow r_2 | \dots | c_n \Rightarrow r_n)$ .

The following table summarizes the primitive data types used by Attitude Check.

Data Type	Notation	Description
real	$\mathbb{R}$	any number in $(-\infty, \infty)$
boolean	$\mathbb{B}$	value in $[\text{false} = 0, \text{true} = 1]$
matrix	$\mathbb{R}^{m \times n}$	matrix of any number in $(-\infty, \infty)$
vector	$\mathbb{R}^m$	column vector of any number in $(-\infty, \infty)$
quaternion	$\mathbf{q}$	a quaternion $\in \mathbb{R}^4$ , see SRS for details

The specification of Attitude Check uses some derived data types: sequences, strings, and tuples. Sequences are lists filled with elements of the same data type. Strings are sequences of characters. Tuples contain a list of values, potentially of different types. In addition, Attitude Check uses functions, which are defined by the data types of their inputs and outputs. Local functions are described by giving their type signature followed by their specification.

### 5 Module Decomposition

The following table is taken directly from the Module Guide document for this project.

Level 1	Level 2
Behaviour-Hiding Module	Control Module
	Input Verification Module
	Accel To Quat Module
	Mag To Quat Module
	Estimate w/o Mag Module
	Estimate w Mag Module
Software Decision Module	Matrix Math Module
	Quaternion Module

Table 1: Module Hierarchy



## 6 MIS of Control Module

### 6.1 Module

control

### 6.2 Uses

Input Verification Module  
Accel To Quat Module  
Mag To Quat Module  
Estimate w/o Mag Module  
Estimate w Mag Module  
Quaternion Module  
Math Module  
Matrix Math Module

### 6.3 Syntax

#### 6.3.1 Exported Access Programs

Name	In	Out	Exceptions
	-	-	-

### 6.4 Semantics

#### 6.4.1 State Variables

#### 6.4.2 Access Routine Semantics

():

- transition:
- output:
- exception:

## 7 MIS of Estimate w/o Mag Module

### 7.1 Module

estimate\_wo\_mag

### 7.2 Uses

Accel To Quat Module

Quaternion Module

Math Module

Matrix Math Module

### 7.3 Syntax

#### 7.3.1 Exported Constants

#### 7.3.2 Exported Access Programs

Name	In	Out	Exceptions
	-	-	-

### 7.4 Semantics

#### 7.4.1 State Variables

#### 7.4.2 Access Routine Semantics

():

- transition:
- output:
- exception:

## 8 MIS of Estimate w Mag Module

### 8.1 Module

estimate\_w\_mag

### 8.2 Uses

Mag To Quat Module

Quaternion Module

Math Module

Matrix Math Module

### 8.3 Syntax

#### 8.3.1 Exported Access Programs

Name	In	Out	Exceptions
	-	-	-

### 8.4 Semantics

#### 8.4.1 State Variables

#### 8.4.2 Access Routine Semantics

():

- transition:
- output:
- exception:

## 9 MIS of Accel To Quat Module

### 9.1 Module

acc2quat

### 9.2 Uses

Quaternion Module

Math Module

Matrix Math Module

### 9.3 Syntax

#### 9.3.1 Exported Access Programs

Name	In	Out	Exceptions
acc_to_quat	$\mathbf{a} := \mathbb{R}^3$	$q_{\text{out}} := \mathbf{q}$	-

### 9.4 Semantics

#### 9.4.1 Access Routine Semantics

mag\_to\_quat( $\mathbf{a} := \mathbb{R}^3$ ):

- output:  $q_{\text{out}} := \text{euler\_to\_quat}(\theta, \phi, \psi)$  given

$$\theta = \text{atan2}(a_y, a_z)$$

$$\phi = \text{atan2}(-a_x, \sqrt{a_y^2 + a_z^2})$$

$$\psi = 0$$

$$\text{where } [a_x, a_y, a_z] = \frac{\mathbf{a}}{|\mathbf{a}|}$$

- exception: none

## 10 MIS of Mag To Quat Module

### 10.1 Module

mag2quat

### 10.2 Uses

Quaternion Module  
Matrix Math Module  
Math Module

### 10.3 Syntax

#### 10.3.1 Exported Access Programs

Name	In	Out	Exceptions
mag_to_quat	$\mathbf{m} := \mathbb{R}^3, \mathbf{a} := \mathbb{R}^3$	$q_{\text{out}} := \mathbf{q}$	ValueError

### 10.4 Semantics

#### 10.4.1 Access Routine Semantics

mag\_to\_quat( $\mathbf{m} := \mathbb{R}^3, \mathbf{a} := \mathbb{R}^3$ ):

- output:  $q_{\text{out}} := \text{euler\_to\_quat}(\theta, \phi, \psi)$  given

$$\theta = \text{atan2}(a_y, a_z)$$

$$\phi = \text{atan2}(-a_x, \sqrt{a_y^2 + a_z^2})$$

$$\psi = \text{atan2}(m_z \sin \phi - m_y \cos \phi, m_x \cos \theta + \sin \theta (m_y \sin \phi + m_z \cos \phi))$$

where  $[a_x, a_y, a_z] = \frac{\mathbf{a}}{|\mathbf{a}|}$  and  $[m_x, m_y, m_z] = \frac{\mathbf{m}}{|\mathbf{m}|}$

- exception: ValueError

## 11 MIS of Input Verification Module

### 11.1 Module

input

### 11.2 Uses

None

### 11.3 Syntax

#### 11.3.1 Exported Access Programs

Name	In	Out	Exceptions
input_checker	$q := \mathbf{q}, \text{gyr} := \mathbb{R}^3, \text{acc} := \mathbb{R}^3, \text{mag} := \mathbb{R}^3, \text{dt} := \mathbb{R}$	$y := \mathbb{B}$	ValueError
input_checker	$q := \mathbf{q}, \text{gyr} := \mathbb{R}^3, \text{acc} := \mathbb{R}^3, \text{dt} := \mathbb{R}$	$y := \mathbb{B}$	ValueError

### 11.4 Semantics

#### 11.4.1 Access Routine Semantics

$\text{input\_checker}(q := \mathbf{q}, \text{gyr} := \mathbb{R}^3, \text{acc} := \mathbb{R}^3, \text{mag} := \mathbb{R}^3, \text{dt} := \mathbb{R})$ :

- output:  $y := \text{true}$ , if input values are within the bounds specified in Section 4.2.8 Input Data Constraints of the SRS.
- exception: ValueError

$\text{input\_checker}(q := \mathbf{q}, \text{gyr} := \mathbb{R}^3, \text{acc} := \mathbb{R}^3, \text{dt} := \mathbb{R})$ :

- output:  $y := \text{true}$ , if input values are within the bounds specified in Section 4.2.8 Input Data Constraints of the SRS.
- exception: ValueError

## 12 MIS of Quaternion Module

### 12.1 Module

quaternion

### 12.2 Uses

Matrix Math Module

Math Module

### 12.3 Syntax

#### 12.3.1 Exported Access Programs

Name	In	Out	Exceptions
create_quat	$w := \mathbb{R}, x := \mathbb{R}, y := \mathbb{R}, z := \mathbb{R}$	-	ValueError
quat_prod	$p := \mathbf{q}, q := \mathbf{q}$	$q_{\text{out}} := \mathbf{q}$	ValueError
normalize	-	-	ValueError
assert_is_norm	$w := \mathbb{R}, x := \mathbb{R}, y := \mathbb{R}, z := \mathbb{R}$	$\text{out} := \mathbb{B}$	ValueError
quat_to_euler	-	$\mathbf{e} := \mathbb{R}^3$	ValueError
quat_to_rot	-	$\mathbf{R} := \mathbb{R}^{3 \times 3}$	ValueError

### 12.4 Semantics

#### 12.4.1 State Variables

$\text{quat} : \mathbf{q}$

#### 12.4.2 Access Routine Semantics

$\text{create\_quat}(w, x, y, z):$

- transition:  $\text{quat} := \mathbf{q}$  where  $\mathbf{q} = [w, x, y, z]$
- exception: ValueError when  $|\text{quat}| \neq 1$

$\text{quat\_prod}(p, q):$

- output:

$$q_{\text{out}} := \begin{bmatrix} p_w q_w - p_x q_x - p_y q_y - p_z q_z \\ p_w q_x + p_x q_w + p_y q_z - p_z q_y \\ p_w q_y - p_x q_z + p_y q_w + p_z q_x \\ p_w q_z + p_x q_y - p_y q_x + p_z q_w \end{bmatrix}$$

- exception: ValueError

normalize():

- transition:  $\text{quat} := \left[ \frac{\text{quat}_w}{d}, \frac{\text{quat}_x}{d}, \frac{\text{quat}_y}{d}, \frac{\text{quat}_z}{d} \right]$  where  $d = \sqrt{\text{quat}_w^2 + \text{quat}_x^2 + \text{quat}_y^2 + \text{quat}_z^2}$

- exception: ValueError

assert\_is\_norm():

- output:  $\text{out} := (1 == \sqrt{w^2 + x^2 + y^2 + z^2})$
- exception: ValueError

quat\_to\_euler():

- output:

$$\mathbf{e} := \begin{bmatrix} \text{yaw} \\ \text{pitch} \\ \text{roll} \end{bmatrix} = \begin{bmatrix} \text{atan2}(2q_yq_w - 2q_xq_z, 1 - 2q_y^2 - 2q_z^2) \\ \text{asin}(2q_xq_y + 2q_zq_w) \\ \text{atan2}(2q_xq_w - 2q_yq_z, 1 - 2q_x^2 - 2q_z^2) \end{bmatrix}$$

See <https://www.euclideanspace.com/maths/geometry/rotations/conversions/quaternionToEuler/index.htm> for 2 special cases.

- exception: ValueError

quat\_to\_rot():

- output:

$$\mathbf{R} := \begin{bmatrix} 1 - 2q_y^2 - 2q_z^2 & 2q_xq_y - 2q_zq_w & 2q_xq_z + 2q_yq_w \\ 2q_xq_y + 2q_zq_w & 1 - 2q_x^2 - 2q_z^2 & 2q_yq_z - 2q_xq_w \\ 2q_xq_z - 2q_yq_w & 2q_yq_z + 2q_xq_w & 1 - 2q_x^2 - 2q_y^2 \end{bmatrix}$$

- exception: ValueError



## 13 MIS of Matrix Math Module

### 13.1 Module

matrix

### 13.2 Uses

N/A

### 13.3 Syntax

#### 13.3.1 Exported Access Programs

Name	In	Out	Exceptions
*	$\mathbb{R}^{m \times n} \times \mathbb{R}^{n \times m}$	$m := \mathbb{R}^{n \times n}$	ValueError
*	$\mathbb{R}^{m \times n} \times \mathbb{R}$	$m := \mathbb{R}^{m \times n}$	ValueError
+	$\mathbb{R}^{m \times n} \times \mathbb{R}^{m \times n}$	$m := \mathbb{R}^{m \times n}$	ValueError
transpose	$\mathbb{R}^{m \times n}$	$m := \mathbb{R}^{n \times m}$	ValueError
norm	$\mathbf{x} := \mathbb{R}^n$	$\mathbf{y} := \mathbb{R}^n$	ValueError

### 13.4 Semantics

#### 13.4.1 Access Routine Semantics

transpose( $\mathbb{R}^{m \times n}$ ):

- output:  $m := \mathbb{R}^{m \times n}$
- exception: ValueError

$$[\mathbf{A}^T]_{i,j} = [\mathbf{A}]_{j,i}$$

$\mathbb{R}^{m \times n} * \mathbb{R}^{n \times m}$ :

- output:  $m := \mathbb{R}^{n \times n}$
- exception: ValueError

Let  $\mathbf{A} = [a_{i,j}]_{m \times n}$  and  $\mathbf{B} = [b_{i,j}]_{n \times m}$ . Then  $\mathbf{C} = \mathbf{A} * \mathbf{B}$  with  $c_{i,j} = a_{i,0}b_{0,j} + a_{i,1}b_{1,j} \dots a_{i,n}b_{n,j}$ .

$\mathbb{R}^{m \times n} * \mathbb{R}$ :

- output:  $m := \mathbb{R}^{m \times n}$
- exception: ValueError

Let  $\mathbf{A} = [a_{i,j}]_{m \times n}$  and  $k = \mathbb{R}$ . Then  $\mathbf{C} = \mathbf{A} * k$  with  $c_{i,j} = ka_{i,j}$ .

$\mathbb{R}^{m \times n} + \mathbb{R}^{m \times n}$ :

- output:  $m := \mathbb{R}^{m \times n}$
- exception: ValueError

Let  $\mathbf{A} = [a_{i,j}]_{m \times n}$  and  $\mathbf{B} = [b_{i,j}]_{m \times n}$ . Then  $\mathbf{A} + \mathbf{B} = [a_{i,j} + b_{i,j}]_{m \times n}$ .

$\text{norm}(\mathbf{x} := \mathbb{R}^n)$ :

- output:  $y := \mathbb{R}^n$  where  $y = \frac{\mathbf{x}}{|\mathbf{x}|}$
- exception: ValueError

## 14 MIS of Math Module

### 14.1 Module

math

### 14.2 Uses

None

### 14.3 Syntax

#### 14.3.1 Exported Constants

PI := 3.141592654

RAD2DEG :=  $\frac{180}{\text{PI}}$

DEG2RAD :=  $\frac{\text{PI}}{180}$

#### 14.3.2 Exported Access Programs

Name	In	Out	Exceptions
sin	$x := \mathbb{R}$	$\text{out} := \mathbb{R}$	ValueError
cos	$x := \mathbb{R}$	$\text{out} := \mathbb{R}$	ValueError
asin	$x := \mathbb{R}$	$\text{out} := \mathbb{R}$	ValueError
atan2	$x := \mathbb{R}, y := \mathbb{R}$	$\text{out} := \mathbb{R}$	ValueError
euler_to_quat	$\mathbf{e} := \mathbb{R}^3$	$y := \mathbf{q}$	ValueError
rot_to_quat	$\mathbf{R} := \mathbb{R}^{3 \times 3}$	$y := \mathbf{q}$	ValueError

### 14.4 Semantics

#### 14.4.1 Access Routine Semantics

$\text{sin}(x := \mathbb{R})$ :

- output:  $y = \sin(x)$
- exception: ValueError

$\text{cos}(x := \mathbb{R})$ :

- output:  $y = \cos(x)$
- exception: ValueError

`asin(x:= $\mathbb{R}$ ):`

- output:  $y = \sin(x)$
- exception: `ValueError`

`atan2(y:= $\mathbb{R}$ , x:= $\mathbb{R}$ ):`

- output: See [https://en.wikipedia.org/wiki/Atan2#Definition\\_and\\_computation](https://en.wikipedia.org/wiki/Atan2#Definition_and_computation)
- exception: `ValueError` if  $x = 0, y = 0$

`euler_to_quat(e :=  $\mathbb{R}^3$ ):`

- output: See <https://www.euclideanspace.com/maths/geometry/rotations/conversions/eulerToQuaternion/index.htm>
- exception: `ValueError`

`rot_to_quat(R :=  $\mathbb{R}^{3 \times 3}$ ):`

- output: See <https://www.euclideanspace.com/maths/geometry/rotations/conversions/matrixToQuaternion/>
- exception: `ValueError`

## References

- Carlo Ghezzi, Mehdi Jazayeri, and Dino Mandrioli. *Fundamentals of Software Engineering*. Prentice Hall, Upper Saddle River, NJ, USA, 2nd edition, 2003.
- Daniel M. Hoffman and Paul A. Strooper. *Software Design, Automated Testing, and Maintenance: A Practical Approach*. International Thomson Computer Press, New York, NY, USA, 1995. URL <http://citeseer.ist.psu.edu/428727.html>.