Documentation for C++ model

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1 Parameter Values:

- Tau= τ : τ measures the timestep for the model and is currently $\frac{1}{4000}$ minutes.
- Contact Length: This measures the length of time that an MT attached to the Cortex remains attached. It is currently $400*Tau = \frac{1}{10}$ minutes.
- $Vg = V_q$: This measures the growth velocity of an MT and is currently $40\mu m/\text{min}$.
- $Vs = V_s$: This measures the shrinking velocity of an MT and is currently $120\mu m/\text{min}$.
- $Vs_c = V_{sc}$: This measures the shrinking velocity of an MT post contact and is currently $120\mu m/\text{min}$.
- $kc = k_c$: This measures the catastrophe frequency of an MT and is currently $.1 \cdot 601/\text{min}$.
- $kr = k_r$: This measures the catastrophe frequency of an MT and is currently $.4 \cdot 601/\text{min}$.
- R1_max= R_1 : This measures the maximum length of the ellipsoidal cell body along the x-axis and is currently $50\mu m$.
- R2_max= R_2 : This measures the maximum length of the ellipsoidal cell body along the y-axis and is currently $30\mu m$.
- Prad= P_{rad} : This measures the radius of the pronucleus and is currently $5\mu m$.
- Eta= η : This measures the translational drag coefficient of the pronucleus and is currently $1\frac{pN}{\mu m min}$.
- Mu= μ : This measures the translational drag coefficient of the pronucleus and is currently $5\eta=5\frac{pN}{\mu m min}$.

2 Usage Instructions:

The three basic steps to to use this code are: **To Compile:** Run make on the command line.

To Run: After compilation, run

./mtKineticModel <Number of Runs> <Output File> [temp/all]

on the command line. Here, <Number of Runs> denotes the number of runs of the given system the model should produce and <Output File> specifies the file to which the results should be written. Note that this file will be placed in the directory nuclearKineticsModelling/data. The final parameter, [temp/all], is an optional parameter. If omitted, the system will only store the final configuration of the system in the result file. If given as temp, it will store 30 second time slices in the result system for each model run, in sequence (i.e. it will list various parameters for 30 second slices for the first run, then those for the second, and so on and so forth). If given as all, it will write data for every timestep in the result file, in sequence, for each model run.

To View: There are a variety of matlab scripts in the plottingCode folder to visualize the results. Several key scripts are outlined below. All are run by setting, either in the matlab console or via the matlab -r command line flag, the variables dataDir and dataFile to the directory containing the data file and the name of the data file (without the extension), respectively, then running the script (to run the script, either type run [SCRIPT NAME].m in the matlab console, or at the end of the variable declarations in the -r command line flag).

positionHeatRotationRose.m This script produces a heat map of the pronucleus' final position and a rose plot (angular histogram) of the pronucleus' final orientation. In addition to specifying the data directory and the data file via matlab variables dataDir and dataFile in this script, you can also specify the number of runs for which the simulation was computed. Note that this script only works & is meaningful for many simulations of the model that only output the default amount of data each iteration (i.e. run with ./mtKineticModel [NUMBER OF RUNS] [OUTPUT FILENAME], not ./mtKineticModel [NUMBER OF RUNS] [OUTPUT FILENAME] all.

movieMaker.m This script produces a visualization of an individual run, by animating the motion of the pronucleus and MTs. It also writes these images to the plottingCode/figs/ folder, which can then be translated into a movie using other utilities. Note that it also erases this figs/ folder prior to running, so don't expect those images to stay around if you are running this script multiple times. In addition to dataDir and dataFile, you can also set the variables visible and step to control whether or not the frames are shown on the screen while it is being rendered and what the step size is between frames, respectively. Note that this script only

works with single simulation runs that output all their data (i.e. run with ./mtKineticModel [NUMBER OF RUNS] [OUTPUT FILENAME] all).

Of particular note are the histogram scripts, positionRotationHist.m and positionRotationHistCompare.m, the single-run visualization tool, readData.m, and the movie-frame making scripts movieMaker*.m. All of these scripts are run with the following basic premise: Open MATLAB, set values dataDir and dataFile (and/or dataFile2) in the MATLAB console, then run the script. dataDir stands for the directory (as a sub-directory of nuclearKineticsModelling/data/) and dataFile stands for the dataFile in question.

2.1 Basic Usage:

For basic usage, the only additional step beyond simple compilation and running is parameter modification. Here is a short description of some of the parameters we change most frequently (All found in the parameters.cpp file).

- springsOn This boolean value controls whether the centrosomes are connected to the pronucleus rigidly (and thus not allowed to translate relative to the pronucleus) or via springs (of spring constant given later in the file).
- translation This boolean value controls whether the pronucleus is allowed to translate. If it is true, the system proceeds in full generality. If it is false, the pronucleus center is fixed in the cortex (though it is allowed to rotate). If the springs are on, the centrosomes are also allowed to translate (and thus provide force via the springs to the pronucleus).
- kM/kD These parameters control the relative spring constants for the springs connecting the mother (M) centrosome and daughter (D) centrosome to the pronucleus, respectively. If springs are off, then these parameters do nothing. We do not yet have good values for these constants.
- startX This parameter controls the starting x coordinate of the pronucleus, with 0 being the center of the cell. We typically test starting at 0 and starting at $7.5\mu m$.
- startPsi This parameter controls the starting angular position of the pronucleus, in radians, with 0 being *horizontal*. For on-angle runs, we use $\frac{\pi}{2}$. To test the effects of angular variations, we typically use $\frac{\pi}{2} + k\frac{\pi}{8}$, with $1 \le k \le 4$, though it might be sensible to test larger k and finer gradations.
- numRegions/regionAngles/regionProbabilities These are the band parameters, and control the number of uniform probability regions, the angular endpoints of those regions, and the associated probabilities with those regions.

2.2 Advanced Usage:

There are a variety of other parameters one may wish to modify, all of which found in the parameters.cpp file. For these modifications, the same procedure is used: modify the parameter, re-compile, and run.

2.3 Major Experiments:

For running a long form experiment, with many runs of many different parameter variations required to collect all the requisite data, manually changing the parameter file each time is tedious and slow. To combat this, there is also a script experiment.sh inside of modelCode which automates this process for you. Currently, experiment.sh only supports running experiments on the translation, envWidthM, envWidthD, and width parameters, which correspond to the translation status, mother allowed-growth envelope width, daughter allowed-growth envelope width, and the push band width, respectively. To use this script, decide what values of these parameters you would like tested. The script will then run all possible combinations of these values, and write the data to file names based on specified parameter-specific portions. Be warned, should the user-specified parameter naming scheme be ambiguous, then the script will potentially overwrite other files it has produced on a later model run. However, with a sensible naming style, this should not happen. To specify the parameter values and naming schema used, simply modify the values specified in the file (lines 15-18, currently) and the associated file path/name variables (lines 25, 27, 29, and 31, currently). Values are stored in space separated lists and encoded as strings currently. Each string in this list is then used to overwrite the current parameter in the parameters.cpp file, before the file is made, then run, with the associated file passed as input. Note that, as these values are simply passed directly into the parameters.cpp file, they must be valid C++ syntax. Furthermore, the initial values must be known to the shell script. In other words, the values specified on lines 34 through 37 must match the current values in the parameters.cpp file, character for character. Unfortunately, currently this script is rather hacked together, and not especially elegant so it may be hard to understand. Feel free to reach out to me at mattmcdermott8@gmail.com in case of confusion.

3 Current Algorithm

3.1 High Level Description

The current algorithm is very straightforward. In particular, for each step in time, stepping by a set parameter tau through Duration minutes, the algorithm computes the net force and torque on the pronucleus and then uses an eulerian approximation of the solution to the DE inspired by friction dominated domain conditions to update the position and angle of rotation of the body. The algorithm also maintains a list of endpoints of a set number of MTs, updating these

through growth, shortening, and respawning when necessary. It also uses the same risk formulas for catastrophe and rescue as did the previous matlab model. The only real differences are that several bugs are corrected, force and torque are calculated upon every iteration directly, and the implementation outputs final data to a file for another program to read in. It is worth noting that the current implementation has a separate, abstracted Vector class to handle vector addition, scalar multiplication, taking projections and finding the norm. This makes the code more readable, but also enables a much easier switch from 2D to 3D. In fact, the Vector class itself is dimension independent (as in, it is set Vector.hpp but can be changed without consequence) so moving to a 3D model really only amounts to modifying the cortex positioning code.

3.2 Implementation Details

3.2.1 MT Envelope Restriction:

In this code, there is a parameter which specifies the allowed envelope of growth for MTs from either the mother MTOC or the daughter MTOC (separately). This is accessed via the variable envWidthM(D) and envelopeM(D). For standard envelopes, simply setting the width should be sufficient (as this actually is used in the envelope parameter) but for stranger cases, it is also possible to just modify the envelope parameter directly and set the envelope that way. We have tried and discussed a number of ways to use this parameter, but have finally settled upon the idea that the envelope merely limits growth. In particular, a new MT can only be spawned within the allowed envelope (meaning spawned at an angle contained in the range specified by the envelope parameter, with 0 degrees being the angle of rotation of the MTOC anchor point relative to the pronucleus) but an MT that falls outside of this envelope as the pronucleus rotates is allowed to continue to grow, connect, and catastrophe as normal. If this needs to be changed, see line 604 of main.cpp, near the comment beginning with MT-ENV, which is just before the length-based respawning code.

3.2.2 Spring Implementations:

Currently there is built in spring capabilities that can be activated with or without pushing forces on either MTOC separately that do account for potential contact and resulting force transfer with the pronucleus. The springs are turned on or off in the two boolean parameters motherSpringOn and daughterSpringOn in the file parameters.cpp. If a spring is on, then the motion of that MTOC is governed by three things: the forces from the associated MTs, the spring force between the MTOC and its anchor point (using current displacement), and a random displacement term. Note that this is altered slightly if the MTOC is close enough to the pronucleus. In that case, the spring force directed towards the pronucleus is reflected by the pronucleus, inducing a force on the MTOC away from the pronucleus and on the pronucleus away from the MTOC. Note, however, that this does not imply that the MTOC experiences a net force away

from the pronucleus. This is not a reflection collision event; rather, the force from the MTOC towards the pronucleus is effectively just transferred to the pronucleus. The force induced by the pronucleus on the MTOC is completely balanced out by the initial force towards the pronucleus on the MTOC in the first place, resulting in only net tangential forces on the MTOC after contact. Similarly, in this case, the random displacement is only allowed to occur tangentially. Note that when the spring is enabled, there is no direct action on the pronucleus by the MTs. Rather, the MTs induce a force on the MTOC, which moves, thus inducing a spring force on the pronucleus (and itself, in opposite magnitude) the next timestep. Thus, the pronucleus is only ever directly moved by the spring with this model.

3.2.3 Boundary Checking:

The current system checks for a cortex pronucleus collision and a MTOC pronucleus collision using slightly different methods. For the MTOC pronucleus collision, the system simply determines if the MTOC is within Prad + 0.1 of the pronucleus position, using simple vector arithmetic. For the pronucleus cortex collision, the system must do something slightly stranger. Here, the system determines if the center of the pronucleus has impacted a slightly smaller ellipse than the cortex. This doesn't give exactly the desired behavior, as the curvature makes this slightly inaccurate, but in practice it is quite effective.

3.2.4 MT Connection Density Limitation:

The system maintains a collection of windows, within each is only allowed one contact. The contact windows are computed in mathematica, and stored in the parameters.cpp file as plain values. There is another, finer set of windows which is commented out in this file as well.

3.2.5 Band Specification:

The band specification is very straightforward. A list of fixed cortex angles are stored, beginning with 0 and ending with 2π . These specify the endpoints of all "cortex pieces," which are angular, uniform sectors of the cortex. This is stored in regionAngles. The probability of contact in these areas and force multipliers scaling contacts in these areas are stored in regionProbabilities and regionForceMultipliers, respectively. These are each one component shorter than regionAngles, as index i of the probability and multiplier vectors describe the effect on the region between angles regionAngles[i] and regionAngles[i+1].

3.2.6 Other Miscellaneous Notes:

• It is important to the current implementation that mt_numb is a constant value, as otherwise fixed-size arrays could not be used to store all the codes data.

- The parameters.cpp file defines not only fixed constants for the program, but also initializes global variables, a few import typedefs, and an enum that defines the centrosome options. The first typedef sets up a new float_T type, which is used so that precision of the model can be altered painlessly, and the second wraps the separate Vector class type with a vec_T type, which is actually not needed anymore and could be removed, so long as all the code was updated to use Vector instead of vec_T.
- The two operator functions at the top of main.cpp are merely to aid in file output.
- The net force calc function is simple; It merely sums up the all the force directions for the MTs, then multiplies that sum by the force for any given MT. This will give the net force on that centrosome.
- The net force function is just a wrapper around net force calc.
- The updatePNPos() function is an extraction of the code to update the position of the pronucleus from the main loop. The actual mechanics of the function are very straightforward currently, and simply translate the components of the force into torque and motion inspiring forces, respectively.
- advanceMT is simply an encapsulation of some messy code from the loop. It grows or shrinks MTs.
- respawnMT creates a new MT.
- The main loop appropriately orders these functions, updates contact statistics, growth statistics, and growth velocities. It also checks for rescue and catastrophe and writes the data to the file.
- Note here that a major implementation detail between this algorithm and the matlab one is that as this algorithm computes the force on every iteration, not just on a new contact, the MT_touch array must be active every second, which in particular means that it cannot be used to distinguish between shortening velocities as it is in the matlab model. So, instead, an additional array is maintained, MT_GrowthVel_*, where * is either M or D. This stores the current growth velocity of the given MT.

4 Future Work

- 1. Add generic, extendable cortex positioning code. This would ensure a smooth change from 2D to 3D. Test and optimize the code. No performance testing or benchmarking has been done to date.
- 2. Test Stability