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Exercise #7

		A	B	C
$P(A) = 0.5$	wrong size, $P(w)$	$\frac{3}{5}$	$\frac{1}{3}$	$\frac{3}{8}$
$P(B) = 0.3$	defects, $P(d)$	$\frac{1}{10}$	$\frac{1}{2}$	$\frac{1}{4}$
$P(C) = 0.2$	change mind, $P(m)$	$\frac{3}{10}$	$\frac{1}{6}$	$\frac{3}{8}$

$$\begin{aligned}
 \text{i) Find } P(A|m) &= \frac{P(m|A) P(A)}{P(m|A) P(A) + P(m|B) P(B) + P(m|C) P(C)} \\
 &= \frac{(\frac{3}{10})(0.5)}{(\frac{3}{10})(0.5) + (\frac{1}{6})(0.3) + (\frac{3}{8})(0.2)} \\
 &= 0.545
 \end{aligned}$$

$$\begin{aligned}
 \text{ii) Find } P(C|w) &= \frac{P(w|C) P(C)}{P(w|A) P(A) + P(w|B) P(B) + P(w|C) P(C)} \\
 &= \frac{(\frac{3}{8})(0.2)}{(\frac{3}{5})(0.5) + (\frac{1}{3})(0.3) + (\frac{3}{8})(0.2)} \\
 &= 0.158
 \end{aligned}$$

$$\begin{aligned}
 \text{iii) Find } P(B|d) &= \frac{P(d|B) P(B)}{P(d|A) P(A) + P(d|B) P(B) + P(d|C) P(C)} \\
 &= \frac{(\frac{1}{2})(0.3)}{(\frac{1}{10})(0.5) + (\frac{1}{2})(0.3) + (\frac{1}{4})(0.2)} \\
 &= 0.6
 \end{aligned}$$

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Exercise #8

a) find female adults = $1 - 0.51$

$$\left. \begin{array}{l} \text{adults (male)} = 0.51 \\ \text{adults (female)} = 0.49 \end{array} \right\} \text{in rural}$$
 $= 0.49$ $\approx 49\%$ b) given $P(r|m) = 0.095$ } $P(r|f) = 0.017$ } voters onlyi) find $P(r|m) = 0.095$

$$\begin{aligned} \text{ii) find } P(m|r) &= \frac{P(r|m)P(m)}{P(r|m)P(m) + P(r|f)P(f)} \\ &= \frac{(0.095)(0.51)}{(0.095)(0.51) + (0.017)(0.49)} \\ &= 0.835 \end{aligned}$$

iii) find $P(f|f) = 0.983$

$$= 0.983 \times 100000$$

$$= 98300 \text{ people}$$

	male	female
rural (R)	0.095	0.017
urban (\bar{R})	0.905	0.983

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Exercise #9

$$P(P) = 0.45$$

$$\text{i) find } P(P') = 1 - 0.45$$

$$P(G|P) = 0.40$$

$$= 0.55$$

$$P(G|P') = 0.55$$

$$\begin{aligned}\text{ii) find } (P|G) &= \frac{P(G|P) P(P)}{P(G|P) P(P) + P(G|P') P(P')} \\ &= \frac{(0.40)(0.45)}{(0.40)(0.45) + (0.55)(0.55)} \\ &= 0.373\end{aligned}$$

$$\begin{aligned}\text{iii) find } (P'|G) &= \frac{P(G|P') P(P')}{P(G|P) P(P) + P(G|P') P(P')} \\ &= \frac{(0.55)(0.55)}{(0.40)(0.45) + (0.55)(0.55)} \\ &= 0.627\end{aligned}$$

$$\begin{aligned}\text{iv) And } P(G) &= P(G|P) P(P) + P(G|P') P(P') \\ &= (0.40 \times 0.45) + (0.55 \times 0.55) \\ &= 0.4825\end{aligned}$$