Machine Learning I Group Work

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1	Packages	
	<pre>brary(gridExtra) brary(tree)</pre>	

```
library(dplyr)
library(readr)
library(randomForest)
library(e1071)
                   # for SVM
library(ISLR)
library(tibble)
library(MASS)
library(gbm)
library(ipred)
library(neuralnet) # for NN
library(h2o)
               # for NN
library(bit64)
                 # for NN
library(h2o)
                   # for NN
library(ggplot2)
library(tidyverse) # inclued qqplot2
library(mgcv)
```

2 Import and data cleaning

```
#qetwd()
#setwd("~/GitHub/machinelearning/machinelearning/03 rmarkdown") #adrianas extrawurst
insurance <- read.csv("../01_data/insurance.csv", header=TRUE)</pre>
str(insurance)
## 'data.frame':
                     1338 obs. of 7 variables:
           : int 19 18 28 33 32 31 46 37 37 60 ...
## $ sex
              : Factor w/ 2 levels "female", "male": 1 2 2 2 2 1 1 1 2 1 ...
             : num 27.9 33.8 33 22.7 28.9 ...
## $ children: int 0 1 3 0 0 0 1 3 2 0 ...
## $ smoker : Factor w/ 2 levels "no", "yes": 2 1 1 1 1 1 1 1 1 1 ...
## $ region : Factor w/ 4 levels "northeast", "northwest", ..: 4 3 3 2 2 3 3 2 1 2 ...
## $ charges : num 16885 1726 4449 21984 3867 ...
# smoker = 1 / nonsmoker = 0
insurance$smoker <- as.character(insurance$smoker)</pre>
insurance$smoker[insurance$smoker == "yes"] <- "1"</pre>
insurance$smoker[insurance$smoker == "no"] <- "0"</pre>
insurance$smoker <- as.factor(insurance$smoker)</pre>
# female = 1 / male = 0
insurance$sex <- as.character(insurance$sex)</pre>
insurance$sex[insurance$sex == "female"] <- "1"</pre>
insurance$sex[insurance$sex == "male"] <- "0"</pre>
insurance$sex <- as.factor(insurance$sex)</pre>
\# region / SE = 1 / SW = 0 / NE = 2 / NW = 3
insurance$region <- as.character(insurance$region)</pre>
insurance$region[insurance$region == "southwest"] <- "1"</pre>
insurance$region[insurance$region == "southeast"] <- "0"</pre>
insurance$region[insurance$region == "northeast"] <- "2"</pre>
insurance$region[insurance$region == "northwest"] <- "3"</pre>
insurance$region <- as.factor(insurance$region)</pre>
head(insurance)
```

age sex bmi children smoker region charges

```
## 1
      19
            1 27.900
                                              1 16884.924
##
   2
      18
                              1
                                      0
                                                  1725.552
            0 33.770
       28
            0 33.000
                              3
                                      0
                                                  4449.462
                              0
                                      0
                                                21984.471
      33
            0 22.705
                                              3
##
##
      32
            0 28.880
                              0
                                      0
                                              3
                                                  3866.855
                                                  3756.622
      31
            1 25.740
                              0
                                      0
```

3 Linear models -> Christina

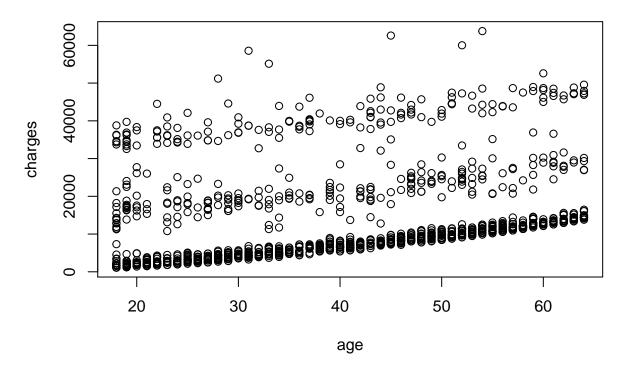
The data set used for this project contains 1338 observations and seven variables containing the age, sex, bmi, children, smoker, region and charges. Those variables are covering continuous and categorical variables. The region as an categorical variable is covering four different levels.

3.1 Basic analysis of continuous variables

Here we will begin with a graphical analysis. Therefore we will plot the response variable against the given predictors to gather first relationships, which can be used later in the modelling process.

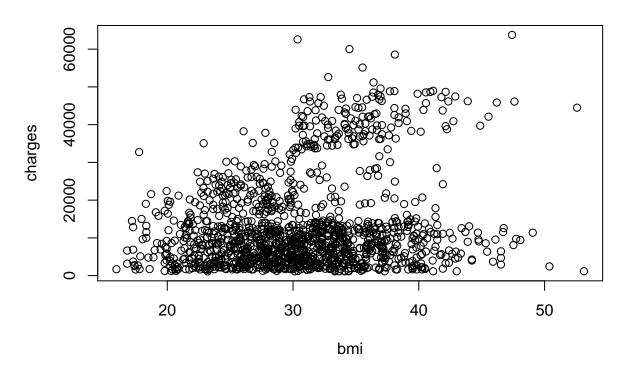
```
plot(charges ~ age, data =insurance, main = 'Charges against age')
```

Charges against age



There seems to be a positive relationship between age and charges.

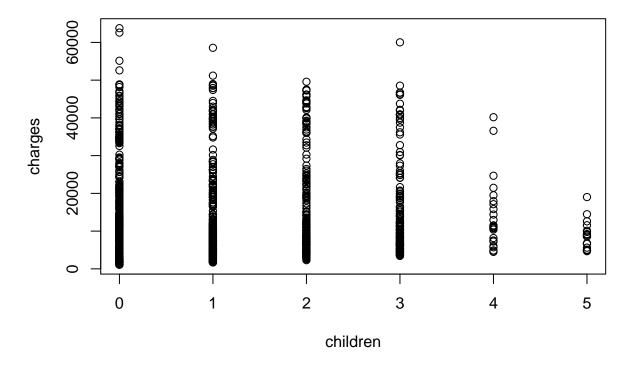
Charges against bmi



The above plot is not showing a clear relationship between bmi and the corresponding charges.

plot(charges ~ children, data =insurance, main = 'Charges against children')

Charges against children



There might be an affect between the number of children and the charges. As shown above it might be possible to interpret that with a rising number of children the charges a decreasing. Still this is not a clear relationship, more a wide interpretation of the plot.

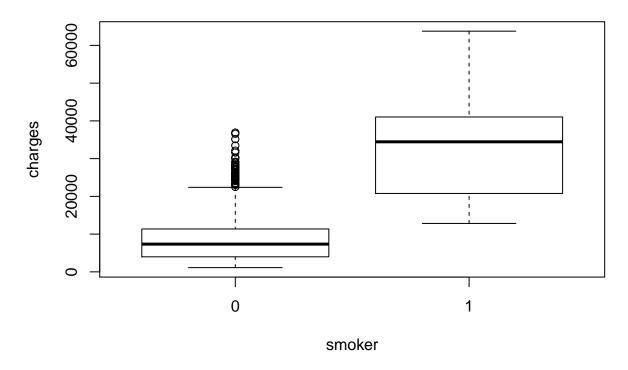
3.2 Basic analysis of categorical variables

```
##plot(charges ~ sex, data =insurance, main = 'Charges against sex')
```

As shown above there are some differences in the charges, comparing the boxplot for the two given genders. It seems that the range for 50% of the obersavation is bigger than the one for the female group. Also the 95% quantile is about 10'000 lower than the same quantile for the male group.

```
plot(charges ~ smoker, data =insurance, main = 'Charges against smoker')
```

Charges against smoker



This plot is showing a clear affect of smoking on the charges. As you can see persons who are not smoking having mean charges that are three times less as the one of people who are smoking. even the outliers of the smokers are still in the range where only 50% of the smokers are located.

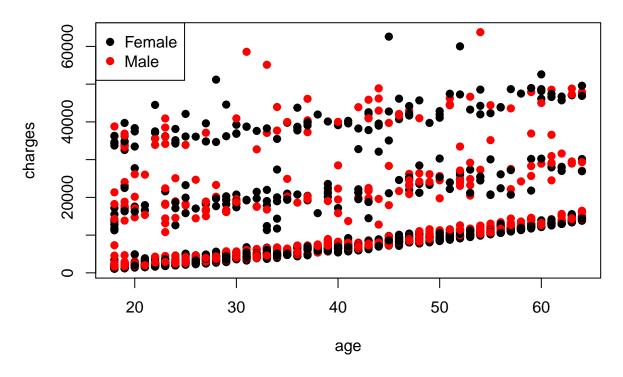
```
##plot(charges ~ region, data =insurance, main = 'Charges against region')
```

In this case there isn't any clear realtionship or trend visible between the region and the corresponding charges. Comparing the four regions together seems that there are slightly small differences in the width of the box, distribution of 50% of the observation as well the setting of the 95% quantile. Those differences will be analysed later.

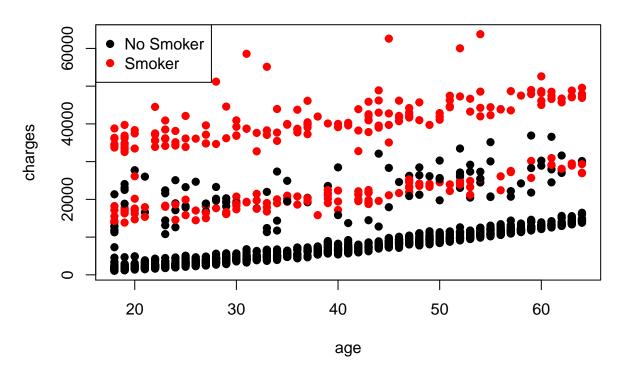
3.3 Basic analysis of categorical and continous variables

In this part we want to show exemplary how the relationship between charges and the age can be affected by adding additionally a categorical variable. This can be used for further data explorations and as well be adapted on all other variables. For this section we will just perform this enlargement for the case of the age to illustrate some possible relationships, which also can be helpful for the following modeling process.

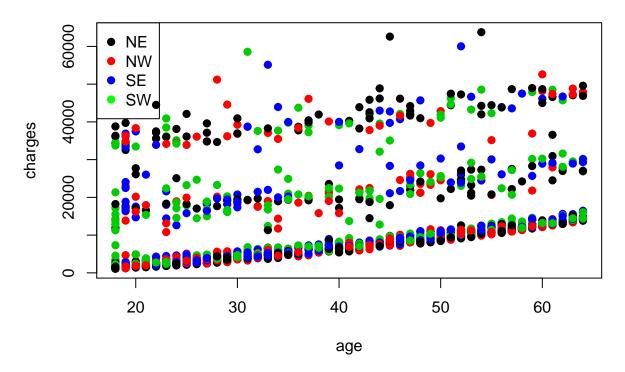
Charges against age (sex)



Charges against age (smoker)

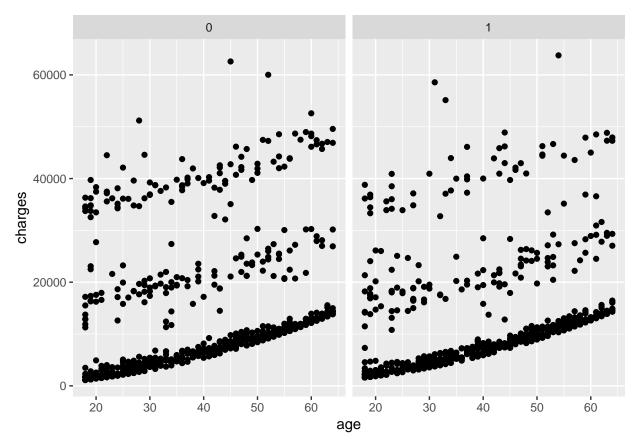


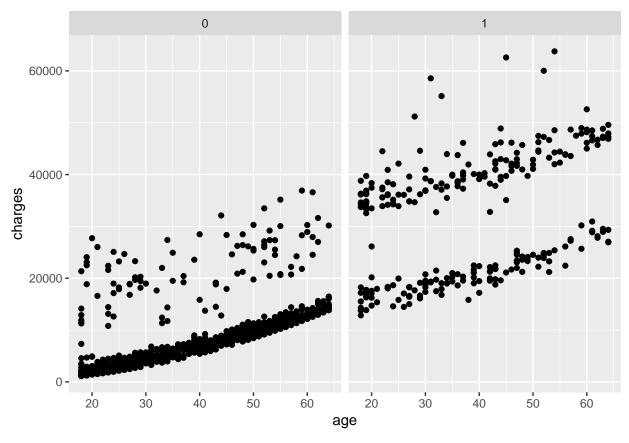
Charges against age (region)

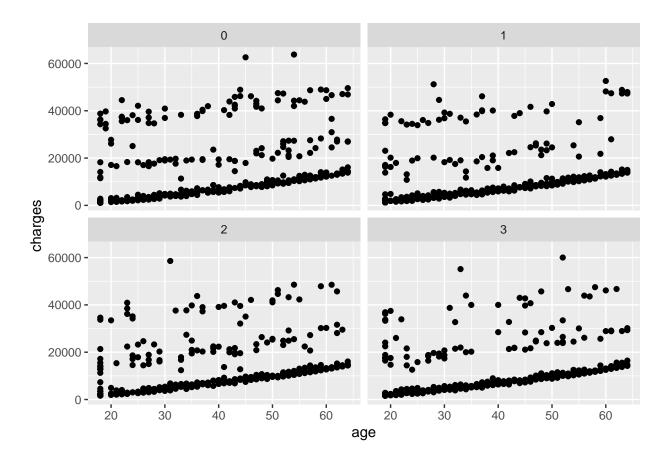


Since it is possible to have overlapping observations, we will plot the same set-up using the qplot. Having separate facets will avoid overlapping and therefore might serve different results as already seen above.

```
qplot(y=charges, x=age,
    data = insurance,
    facets = ~ sex)
```







3.4 Fitting a first Linear Model

As usually we will start by fitting a simple regression model to the insurance dataset. Therfore we will start with one variable and add additional complexity in each following subset. This step-by-step approach helps to explore the data slightly better and will simplify the final modelling.

3.4.1 Linear Model with one variable

For the first simple regression model we will use the age.

```
lm.insurance <- lm(charges ~ age, data = insurance)
summary(lm.insurance)</pre>
```

```
##
## lm(formula = charges ~ age, data = insurance)
##
## Residuals:
##
      Min
              1Q Median
                            30
                                  Max
    -8059 -6671 -5939
                          5440
                                47829
##
##
## Coefficients:
##
              Estimate Std. Error t value Pr(>|t|)
## (Intercept)
                 3165.9
                             937.1
                                     3.378 0.000751 ***
                  257.7
                              22.5 11.453 < 2e-16 ***
## age
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
```

```
##
## Residual standard error: 11560 on 1336 degrees of freedom
## Multiple R-squared: 0.08941, Adjusted R-squared: 0.08872
## F-statistic: 131.2 on 1 and 1336 DF, p-value: < 2.2e-16</pre>
```

3.4.1.1 Coefficent and Interpretation

As shown in the R Output a person with the age of 0 will have a base charge of 3165.885. This intercept and its interpretation seems to be nonsensical. With each year the charges are increasing by 257.7226, which is the slope for this regressionline

3.4.1.2 P-values

With a value of 2e-16 the age seesm to have a very strong effect on the charges. This means that the slope of the chages is not flat, not zero, so the hypothesisi has to be thrown away.

3.4.1.3 Including the gender as a second variable

In this subsest we will consider also the sex for modelling a simple regression model.

```
lm.insurance.2 <- lm(charges ~ age + sex, data = insurance)
summary(lm.insurance.2)</pre>
```

```
##
## Call:
## lm(formula = charges ~ age + sex, data = insurance)
## Residuals:
##
     Min
             1Q Median
                           30
                                 Max
   -8821 -6947 -5511
##
                         5443
                               48203
##
## Coefficients:
##
              Estimate Std. Error t value Pr(>|t|)
                                    3.960 7.9e-05 ***
## (Intercept) 3882.46
                           980.49
                258.87
                            22.47 11.523 < 2e-16 ***
## age
              -1538.83
                           631.08 -2.438
                                            0.0149 *
## sex1
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
## Residual standard error: 11540 on 1335 degrees of freedom
## Multiple R-squared: 0.09344,
                                   Adjusted R-squared: 0.09209
## F-statistic: 68.8 on 2 and 1335 DF, p-value: < 2.2e-16
```

3.4.1.4 Including interaction

1Q Median

3Q

Max

##

##

Residuals:

Min

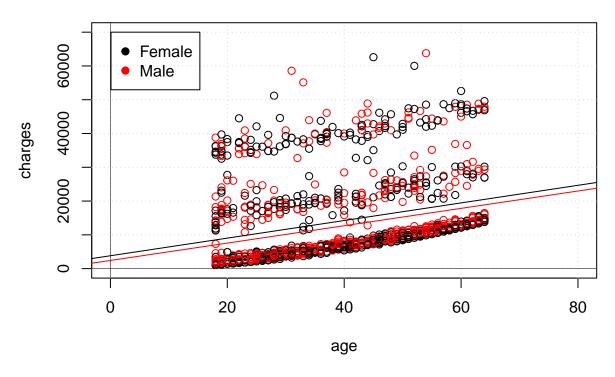
Since a second variable was added we want to explore if there might be significant interaction between age and sex, that might have to be considered for the modeling process.

```
lm.insurance.3 <-lm(charges ~ age * sex, data =insurance)
summary(lm.insurance.3)

##
## Call:
## lm(formula = charges ~ age * sex, data = insurance)</pre>
```

```
## -8823 -6936 -5500 5456 48187
##
## Coefficients:
             Estimate Std. Error t value Pr(>|t|)
##
## (Intercept) 3811.77
                          1308.29
                                  2.914 0.00363 **
               260.68
                            31.62 8.244 3.96e-16 ***
## age
## sex1
              -1394.92
                          1872.30 -0.745 0.45638
                            44.95 -0.082 0.93494
                 -3.67
## age:sex1
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
## Residual standard error: 11540 on 1334 degrees of freedom
## Multiple R-squared: 0.09345, Adjusted R-squared: 0.09141
## F-statistic: 45.84 on 3 and 1334 DF, p-value: < 2.2e-16
plot(charges ~ age, data =insurance,
    main = "Model 'lm.insurance.3'",
    xlim = c(0, 80),
    ylim = c(0, 70000),
    col = sex)
##
grid()
##
abline(h = 0, lwd = 0.5)
abline(v = 0, lwd = 0.5)
abline(a = coef(lm.insurance.3)[1],
      b = coef(lm.insurance.3)["age"])
abline(a = coef(lm.insurance.3)[1] + coef(lm.insurance.3)["sex1"],
      b = coef(lm.insurance.3)["age"] + coef(lm.insurance.3)["age:sex1"],
      col = "red")
legend(x = 0.1, y = 70000,
      pch = 19,
      legend = c("Female", "Male"),
      col = c("black", "red"))
```

Model 'Im.insurance.3'



```
coef(lm.insurance.3)
    (Intercept)
                         age
                                      sex1
                                               age:sex1
    3811.773852
                  260.681339 -1394.925331
                                              -3.669849
summary(lm.insurance.3)$coefficients
##
                   Estimate Std. Error
                                            t value
                                                        Pr(>|t|)
## (Intercept)
                3811.773852 1308.29248
                                        2.91354869 3.633010e-03
                 260.681339
                              31.62249 8.24354130 3.958052e-16
## age
## sex1
               -1394.925331 1872.29663 -0.74503437 4.563822e-01
                  -3.669849
                              44.95054 -0.08164194 9.349437e-01
## age:sex1
```

3.5 Final Linear Model Development

In this section we want to find an appropriate model, which accounts all relevant parameters and interactions. Afterwards we will then compare the fitted model with a base model and test its performance.

3.5.1 Linear Model with all variables

```
lm.insurance.all <- lm(charges ~ age + sex + bmi + children + smoker + region , data = insurance)
summary(lm.insurance.all)

##
## Call:
## lm(formula = charges ~ age + sex + bmi + children + smoker +
## region, data = insurance)</pre>
```

```
##
## Residuals:
##
       Min
                 1Q
                     Median
                                   30
                      -982.1
                               1393.9
                                       29992.8
## -11304.9 -2848.1
##
## Coefficients:
               Estimate Std. Error t value Pr(>|t|)
##
## (Intercept) -13104.87
                           1090.51 -12.017 < 2e-16 ***
## age
                 256.86
                             11.90 21.587 < 2e-16 ***
## sex1
                 131.31
                            332.95
                                    0.394 0.693348
## bmi
                 339.19
                             28.60 11.860 < 2e-16 ***
## children
                 475.50
                            137.80
                                    3.451 0.000577 ***
## smoker1
               23848.53
                            413.15 57.723 < 2e-16 ***
## region1
                  74.97
                            470.64
                                   0.159 0.873460
                1035.02
                            478.69
                                   2.162 0.030782 *
## region2
## region3
                 682.06
                            478.96
                                   1.424 0.154669
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
##
## Residual standard error: 6062 on 1329 degrees of freedom
## Multiple R-squared: 0.7509, Adjusted R-squared: 0.7494
## F-statistic: 500.8 on 8 and 1329 DF, p-value: < 2.2e-16
```

As the above R Output shows not all variables seems to have a significant effect on the charges.

3.5.1.1 Testing sex before dropping

Before removing those two variables we first will make a deeper analysis.

```
lm.sex <- lm(charges ~ sex, data=insurance)
summary(lm.sex)</pre>
```

```
##
## Call:
## lm(formula = charges ~ sex, data = insurance)
##
## Residuals:
     Min
##
             1Q Median
                           30
                                 Max
  -12835 -8435 -3980
                         3476 51201
##
## Coefficients:
##
              Estimate Std. Error t value Pr(>|t|)
## (Intercept) 13956.8
                            465.2 30.003
                                            <2e-16 ***
                                            0.0361 *
               -1387.2
                            661.3 -2.098
## sex1
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
## Residual standard error: 12090 on 1336 degrees of freedom
## Multiple R-squared: 0.003282,
                                   Adjusted R-squared: 0.002536
## F-statistic:
                 4.4 on 1 and 1336 DF, p-value: 0.03613
coef(lm.sex)
## (Intercept)
                      sex1
     13956.751
                -1387.172
```

As seen in the output considering only the sex it is not a significant and standalone explaining variable for

the charges. Comparing the p-value of the sex within the full model including all possible variables it is so high with a value of 0.693348, that it can be dropped from our final model.

3.5.1.2 Testing region before dropping

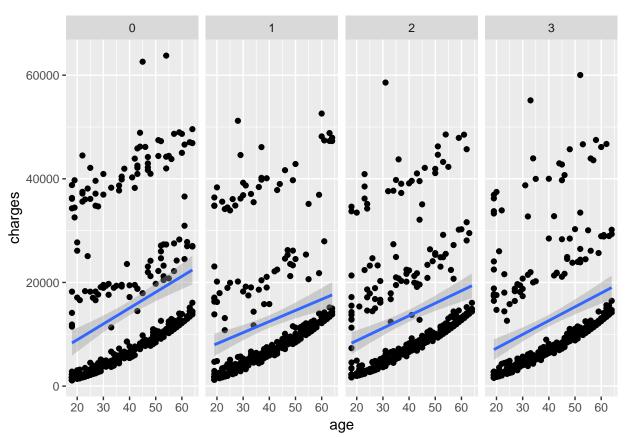
```
lm.region.1 <- lm(charges ~ region, data = insurance)</pre>
aggregate(charges ~ region, FUN = mean, data =insurance)
     region charges
## 1
          0 14735.41
## 2
          1 12346.94
## 3
          2 13406.38
## 4
          3 12417.58
summary(lm.region.1)
##
## Call:
## lm(formula = charges ~ region, data = insurance)
## Residuals:
     Min
              1Q Median
                            3Q
                                  Max
  -13614 -8463 -3793
##
                          3385
                                49035
##
## Coefficients:
##
              Estimate Std. Error t value Pr(>|t|)
## (Intercept) 14735.4
                             633.3
                                    23.266
                                             <2e-16 ***
## region1
               -2388.5
                             922.2 -2.590
                                             0.0097 **
## region2
                -1329.0
                             922.9 -1.440
                                             0.1501
## region3
                -2317.8
                             922.2 -2.513
                                             0.0121 *
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
## Residual standard error: 12080 on 1334 degrees of freedom
## Multiple R-squared: 0.006634,
                                   Adjusted R-squared: 0.0044
## F-statistic: 2.97 on 3 and 1334 DF, p-value: 0.03089
```

There is strong evidence that the mean charges for northeast is not equal to zero. But there isn't any evidence that all other regions differ from the reference region northeast. To have a better understanding we will make an anova test between the above shown model and a base model lm.region.0 as schon below.

```
lm.region.0 <- lm(charges ~ 1 , data = insurance)</pre>
coef(lm.region.0)
## (Intercept)
      13270.42
anova(lm.region.0, lm.region.1)
## Analysis of Variance Table
##
## Model 1: charges ~ 1
## Model 2: charges ~ region
    Res.Df
                   RSS Df Sum of Sq
                                           F Pr(>F)
## 1
       1337 1.9607e+11
       1334 1.9477e+11 3 1300759681 2.9696 0.03089 *
## ---
```

```
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
```

The anova test shows that there is a low evidence that the model with more parameters (in this case only the region) better fits the data. The F-value seems to be very small and also the p-value is not really significant with 0.03089. Anyhow there is a drop in the RSS, by adding 3 additional parameters of the different regions. To have a better understanding we can additionally perform posthoc contrasts to decide afterwards if we will drop the region finally from our model. Before performing several posthoc test and repeating this exercise to all possible combinations we will use the ggplot to explore the data quickly upfront.



Using the visualization it seems that there seems to be no obvoius differnce and effect. Therfore we decide to drop also the variable region from our linear model.

3.5.2 Dropping variables from the model

sex

bmi

1 5.7164e+06 4.8845e+10 23315

1 5.1692e+09 5.4009e+10 23449

```
drop1(lm.insurance.all, test="F")
## Single term deletions
##
## Model:
##
  charges ~ age + sex + bmi + children + smoker + region
            Df Sum of Sq
                                              F value
##
                                  RSS
                                        AIC
                                                          Pr(>F)
                           4.8840e+10 23316
##
  <none>
##
             1 1.7124e+10 6.5964e+10 23717
                                             465.9837 < 2.2e-16 ***
  age
```

0.1556 0.693348

140.6627 < 2.2e-16 ***

```
## children 1 4.3755e+08 4.9277e+10 23326
                                            11.9063 0.000577 ***
            1 1.2245e+11 1.7129e+11 24993 3331.9680 < 2.2e-16 ***
## smoker
            3 2.3343e+08 4.9073e+10 23317
## region
                                             2.1173 0.096221 .
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
lm.insurance.1 <- update(lm.insurance.all, .~. -region -sex)</pre>
formula(lm.insurance.1)
## charges ~ age + bmi + children + smoker
summary(lm.insurance.1)
##
## Call:
## lm(formula = charges ~ age + bmi + children + smoker, data = insurance)
## Residuals:
                      Median
##
       Min
                                           Max
                 1Q
                                   3Q
                      -986.6
## -11897.9 -2920.8
                               1392.2
                                       29509.6
##
## Coefficients:
##
               Estimate Std. Error t value Pr(>|t|)
## (Intercept) -12102.77
                            941.98 -12.848 < 2e-16 ***
                             11.90 21.675 < 2e-16 ***
                 257.85
## bmi
                 321.85
                             27.38 11.756 < 2e-16 ***
                 473.50
                            137.79
                                    3.436 0.000608 ***
## children
## smoker1
               23811.40
                            411.22 57.904 < 2e-16 ***
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
##
## Residual standard error: 6068 on 1333 degrees of freedom
## Multiple R-squared: 0.7497, Adjusted R-squared: 0.7489
## F-statistic: 998.1 on 4 and 1333 DF, p-value: < 2.2e-16
```

Comparing the summary output of lm.insurance.0 and lm.insurance.1 the latest model is only including variables having a p-value that indicates a significant factor.

3.5.3 Considering Interactions

```
drop1(lm.insurance.1, test="F")
## Single term deletions
##
## Model:
## charges ~ age + bmi + children + smoker
           Df Sum of Sq
                                      AIC F value
                                                      Pr(>F)
                                RSS
## <none>
                         4.9078e+10 23315
            1 1.7297e+10 6.6375e+10 23717
                                           469.789 < 2.2e-16 ***
## age
## bmi
            1 5.0884e+09 5.4167e+10 23445
                                           138.203 < 2.2e-16 ***
## children 1 4.3477e+08 4.9513e+10 23325
                                            11.809 0.0006077 ***
## smoker
            1 1.2345e+11 1.7253e+11 24995 3352.911 < 2.2e-16 ***
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
```

```
lm.insurance.2 <- update(lm.insurance.1, .~. +age:bmi + age:children + age:smoker + bmi:children + bmi:</pre>
summary(lm.insurance.2)
##
## Call:
## lm(formula = charges ~ age + bmi + children + smoker + age:bmi +
##
       age:children + age:smoker + bmi:children + bmi:smoker + children:smoker,
##
       data = insurance)
##
## Residuals:
##
       Min
                 1Q
                     Median
                                   30
                                           Max
## -13996.3 -1947.6 -1331.5
                               -406.4
##
## Coefficients:
##
                     Estimate Std. Error t value Pr(>|t|)
## (Intercept)
                   -6.745e+02 2.106e+03 -0.320
                    2.055e+02 4.963e+01
                                           4.140 3.7e-05 ***
## age
                   -6.339e+01 6.756e+01 -0.938
## bmi
                                                    0.348
## children
                    6.957e+02 6.341e+02
                                          1.097
                                                    0.273
## smoker1
                   -1.983e+04 1.861e+03 -10.651 < 2e-16 ***
                    1.912e+00 1.561e+00
## age:bmi
                                          1.225
                                                    0.221
## age:children
                    1.201e+00 8.527e+00
                                           0.141
                                                    0.888
## age:smoker1
                   -9.141e-01 2.384e+01
                                         -0.038
                                                    0.969
## bmi:children
                   -5.334e+00 1.863e+01 -0.286
                                                    0.775
## bmi:smoker1
                    1.437e+03 5.317e+01
                                          27.029 < 2e-16 ***
## children:smoker1 -3.858e+02 2.841e+02 -1.358
                                                    0.175
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
##
## Residual standard error: 4874 on 1327 degrees of freedom
## Multiple R-squared: 0.8392, Adjusted R-squared: 0.838
## F-statistic: 692.8 on 10 and 1327 DF, p-value: < 2.2e-16
```

As the above output shows not all of the added interactions have to be considered in the model. Upfront we also tried to generate a linear model including all possible interactions. Since the output was not satisfying we skiped this analysis at this point. Therfore the working assumption in this step was quite easy by editing only possible and simple interactions. Based on the results we will now drop the unnecessary interactions.

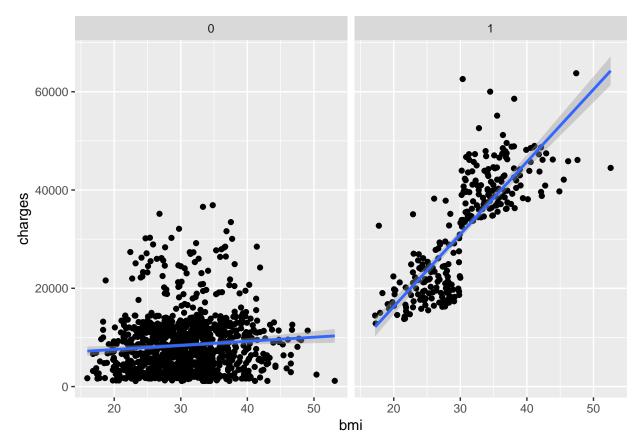
```
drop1(lm.insurance.2, test="F")
```

```
## Single term deletions
##
## Model:
## charges ~ age + bmi + children + smoker + age:bmi + age:children +
##
       age:smoker + bmi:children + bmi:smoker + children:smoker
##
                                       RSS
                                              AIC F value Pr(>F)
                  Df Sum of Sq
## <none>
                                 3.1519e+10 22735
## age:bmi
                   1 3.5624e+07 3.1555e+10 22734
                                                    1.4998 0.2209
## age:children
                   1 4.7151e+05 3.1520e+10 22733
                                                    0.0199 0.8880
## age:smoker
                    1 3.4909e+04 3.1519e+10 22733
                                                    0.0015 0.9694
## bmi:children
                    1 1.9467e+06 3.1521e+10 22733
                                                    0.0820 0.7747
## bmi:smoker
                    1 1.7353e+10 4.8872e+10 23319 730.5705 <2e-16 ***
## children:smoker 1 4.3796e+07 3.1563e+10 22734
                                                    1.8439 0.1747
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
```

```
lm.insurance.3 <- update(lm.insurance.2, .~. -age:bmi - age:children - age:smoker - bmi:children -child
summary(lm.insurance.3)
##
## Call:
## lm(formula = charges ~ age + bmi + children + smoker + bmi:smoker,
##
       data = insurance)
##
## Residuals:
##
       Min
                 1Q
                      Median
                                   3Q
## -14598.6 -1924.4 -1321.4
                               -465.6
                                       29892.4
## Coefficients:
##
                Estimate Std. Error t value Pr(>|t|)
                            831.270 -3.283 0.00105 **
               -2729.002
## (Intercept)
## age
                 264.948
                              9.553 27.735 < 2e-16 ***
## bmi
                   5.656
                             24.873
                                      0.227 0.82014
                            110.615
                                      4.601 4.61e-06 ***
## children
                 508.924
               -20194.709
                           1654.505 -12.206 < 2e-16 ***
## smoker1
## bmi:smoker1
                1433.788
                             52.823 27.143 < 2e-16 ***
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
##
## Residual standard error: 4871 on 1332 degrees of freedom
## Multiple R-squared: 0.8388, Adjusted R-squared: 0.8382
## F-statistic: 1387 on 5 and 1332 DF, p-value: < 2.2e-16
```

After considering also the interaction between bmi and smoker, which seems to be significant with a small p-value of 2e-16. The variable bmi itself has now a p-value of 0.82014. Therfore lets have a look on the relationship between bmi and smoker to have a better understanding:

```
ggplot(data=insurance,
    mapping = aes(y = charges, x= bmi))+ geom_point()+ geom_smooth(method = 'lm') +facet_grid(. ~ sm
```



As expected there seems to be a clear relationship between charges and bmi, considering if a person is smoking or not. Since this relationship makes even sense from the domain perspective, we will definitly keep this in our model.

3.5.4 Measure of Fit

[1] 0.7496945

In this section we were able to fit several models, having different levels of complexity. For the following analysis we have choosen our four models to measure the individual fit. Moreover we will compare them among each other to find the most appropriate model for the given insurance dataset.

```
formula(lm.insurance.all)
## charges ~ age + sex + bmi + children + smoker + region
summary(lm.insurance.all)$r.squared
## [1] 0.750913
summary(lm.insurance.all)$adj.r.squared
## [1] 0.7494136
formula(lm.insurance.1)
## charges ~ age + bmi + children + smoker
summary(lm.insurance.1)$r.squared
```

```
summary(lm.insurance.1)$adj.r.squared

## [1] 0.7489434

formula(lm.insurance.2)

## charges ~ age + bmi + children + smoker + age:bmi + age:children +

## age:smoker + bmi:children + bmi:smoker + children:smoker

summary(lm.insurance.2)$r.squared

## [1] 0.8392491

summary(lm.insurance.2)$adj.r.squared

## [1] 0.8380378

formula(lm.insurance.3)

## charges ~ age + bmi + children + smoker + bmi:smoker

summary(lm.insurance.3)$r.squared

## [1] 0.8388379

summary(lm.insurance.3)$adj.r.squared
```

For the comparison we used R-Squared and the adjusted R-Squared to measure the performance of our models. Since the adjusted R-squared can provide a more precise view of that correlation by also taking into account how many independent variables are added to our particular models against we will base our conclusion on this parameter.

Therefore we are happy to state that the latest model number three is able to explain the charges with a percentage of 83.82329 % based on the independent variables.

Comparing the latest model with the first one there is an increase of 8.88% in the adjusted R-squared. Even if the latest model is performing the best compared to the others, it is always a trade off between the gain in the fit and the corresponding effort.

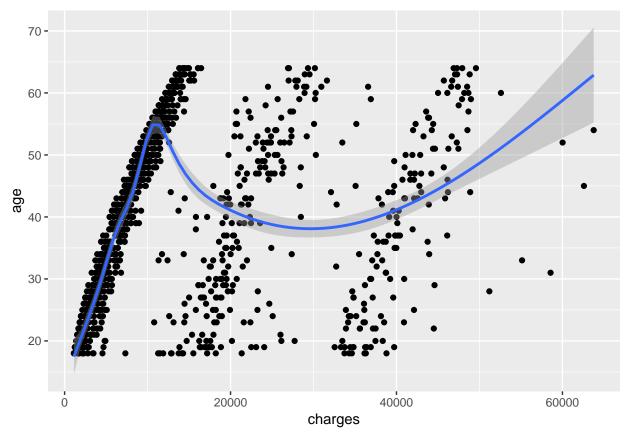
4 Linear models (GAM & Polynomial) -> Yvonne

5 Polynomial

[1] 0.8382329

As we can see from the following plot, the models are not always linear.

`geom_smooth()` using method = 'gam' and formula 'y ~ s(x, bs = "cs")'



Clearly visible is the increase in costs up to about 18'000 with increasing age. The dependence of amount and costs above 10,000 is more difficult to predict due to the non-linearity.

We add linearity to the model by adding a square term to charges.

```
# Model with a linear effect for charges
lm.insurance.1 <- lm(age ~ sex + bmi + children + charges, data = insurance)

#Model with a quadratic effect for charges
lm.insurance.2 <- update(lm.insurance.1, . ~ . + I(charges^2))</pre>
```

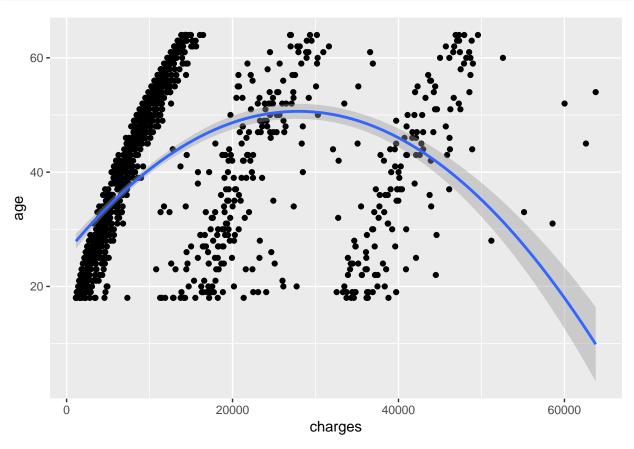
The F-test is used to test the qudrate term.

```
anova(lm.insurance.1, lm.insurance.2)
```

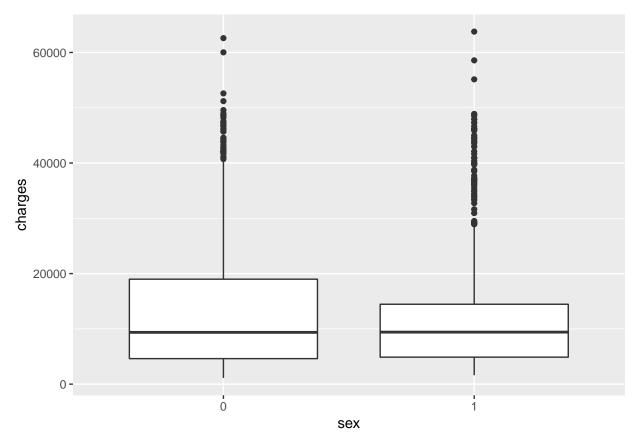
```
## Analysis of Variance Table
##
## Model 1: age ~ sex + bmi + children + charges
## Model 2: age ~ sex + bmi + children + charges + I(charges^2)
## Res.Df RSS Df Sum of Sq F Pr(>F)
## 1 1333 239086
## 2 1332 198860 1 40227 269.45 < 2.2e-16 ***
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1</pre>
```

The F-test shows a strong indication charges requires a quadratic term.

The graphical result is shown below.

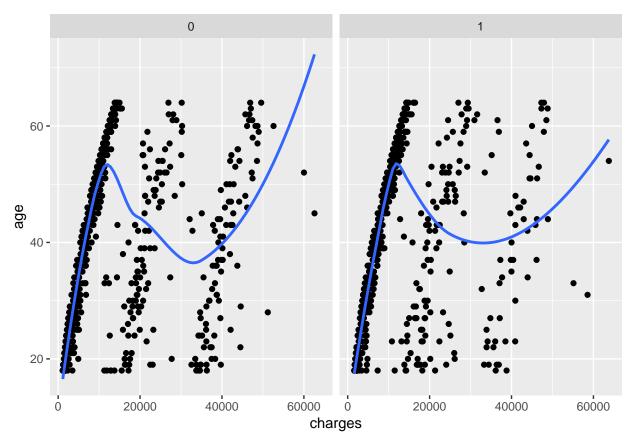


What is the result if you look at the men and women separately.



This graph shows that there is not really a difference in the median between women and men. The only difference is in the middle 50% range where the men have a larger range.

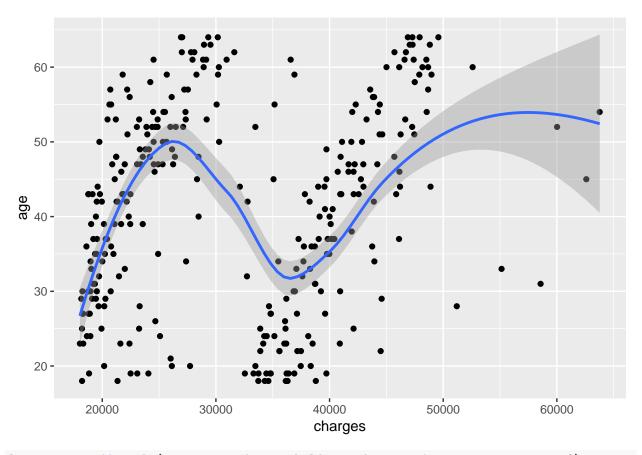
$geom_smooth()$ using method = 'loess' and formula 'y ~ x'



The rough course of costs as a function of age is comparable for men and women. A closer look at the result reveals slight differences. However, this is not a reason to differentiate the models according to gender.

The first cost increase looks more like a linear model. What does the result look like if the costs are brought above 18'000? This will be examined in the following considerations.

$geom_smooth()$ using method = 'loess' and formula 'y ~ x'



```
lm.insurance.11 <- lm(age ~ sex + bmi + children +charges, data = insurance.part2)
lm.insurance.12 <- update(lm.insurance.11, . ~ . + I(charges^2))
anova(lm.insurance.11, lm.insurance.12)
## Analysis of Variance Table
##
## Model 1: age ~ sex + bmi + children + charges</pre>
```

```
##
## Model 1: age ~ sex + bmi + children + charges
## Model 2: age ~ sex + bmi + children + charges + I(charges^2)
## Res.Df RSS Df Sum of Sq F Pr(>F)
## 1 308 53277
## 2 307 52872 1 405.12 2.3523 0.1261
```

The result shows that there is no strong evidence that charges needs a quadratic term. The model appeard to be linear.

6 Generalised Additive Models

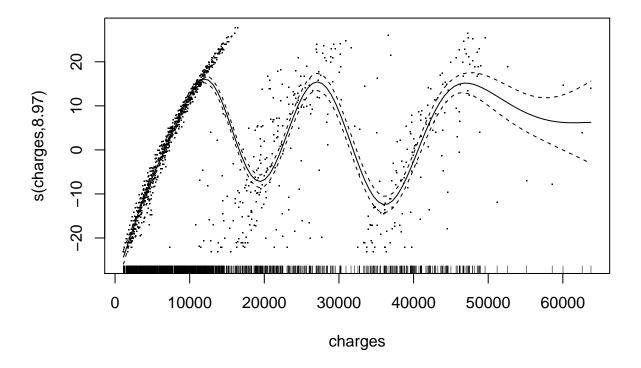
The previous data modelling is now performed with GAM.

```
##
## Family: gaussian
## Link function: identity
```

```
##
## Formula:
  age ~ sex + s(charges) + children
##
## Parametric coefficients:
               Estimate Std. Error t value Pr(>|t|)
##
                41.1364
                            0.3598 114.330 < 2e-16 ***
## (Intercept)
                            0.4186 -2.591 0.00966 **
## sex1
                -1.0849
## children
                -1.2719
                            0.1836 -6.926 6.72e-12 ***
##
## Signif. codes:
                     '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
##
## Approximate significance of smooth terms:
                edf Ref.df
##
                               F p-value
## s(charges) 8.974
                         9 363.9 <2e-16 ***
## ---
                   0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
## Signif. codes:
                  0.71
## R-sq.(adj) =
                         Deviance explained = 71.3%
## GCV = 57.673
                 Scale est. = 57.157
```

The s(changes) value of 8,974 is high and allows us to model the existing predictor with a smooth term. The corresponding visualization is shown below.

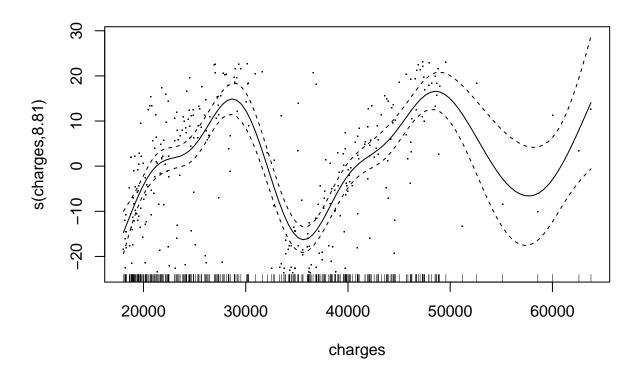
```
plot(gam.insurance.1, residuals = TRUE, select = 1)
```



If you only consider the costs greater than 18'000 should be, the result is identical with the previous

consideration. A linear model is also preferable in this case.

```
gam.insurance.2 <- gam(age \sim sex + s(charges) + children,
                      data = insurance.part2)
summary(gam.insurance.2)
##
## Family: gaussian
## Link function: identity
##
## Formula:
## age ~ sex + s(charges) + children
## Parametric coefficients:
              Estimate Std. Error t value Pr(>|t|)
##
## (Intercept) 41.5861
                         0.9591 43.360
                                           <2e-16 ***
## sex1
               -0.1992
                          1.1457 -0.174
                                            0.862
## children
               -0.2804
                          0.4936 -0.568
                                            0.570
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
## Approximate significance of smooth terms:
##
               edf Ref.df
                              F p-value
## s(charges) 8.815 8.99 32.15 <2e-16 ***
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
##
## R-sq.(adj) = 0.474 Deviance explained = 49.2\%
## GCV = 101.7 Scale est. = 97.857
                                      n = 313
plot(gam.insurance.2, residuals = TRUE, select = 1)
```



7 GLM and cross validation -> Carole

7.1 Generalised Linear Models for count data

7.1.1 Original data

The number of children an insured person has is analysed. We have the following data on children per person. The number of children ranges from 0 to 5 with a median of 1.

```
summary(insurance$children)
```

```
## Min. 1st Qu. Median Mean 3rd Qu. Max.
## 0.000 0.000 1.000 1.095 2.000 5.000
```

7.1.2 Poisson model

To model count data (number of children) the poisson model is used. An analysis performed beforehand showed that only the variables "charges" and "smoker" have a significant impact on the number of children.

```
##
## Call:
## glm(formula = children ~ smoker + charges, family = "poisson",
## data = insurance)
```

```
##
## Deviance Residuals:
##
       Min
                 1Q
                      Median
                                    30
                                            Max
  -1.8561
            -1.4318
                     -0.1057
                                         2.9717
##
                                0.7768
##
##
  Coefficients:
##
                 Estimate Std. Error z value Pr(>|z|)
##
   (Intercept) -3.706e-02
                            4.213e-02
                                       -0.880
                                                 0.3790
   smoker1
               -3.239e-01
                            1.058e-01
                                       -3.061
                                                 0.0022 **
   charges
                1.419e-05
                            3.365e-06
                                        4.217 2.48e-05 ***
##
                   0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
##
  Signif. codes:
##
##
   (Dispersion parameter for poisson family taken to be 1)
##
##
       Null deviance: 2001.6 on 1337
                                        degrees of freedom
## Residual deviance: 1984.1
                               on 1335
                                        degrees of freedom
  AIC: 3879.4
##
## Number of Fisher Scoring iterations: 5
```

To get the coefficients, the log transformation needs to be reversed:

```
exp(coef(glm.children))
```

```
## (Intercept) smoker1 charges
## 0.9636169 0.7233085 1.0000142
```

Smoker (factor): The model shows that for the factor smoker (yes/no), a smoker has on average 72% of the number of children a non-smoker has. The more common-sense interpretation might be the other way around, that people who have 1 or more children smoke less, but for the moment we have no proof of that.

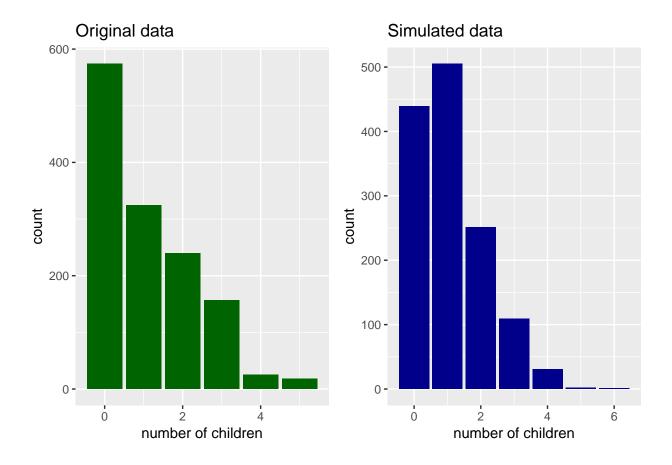
Charges: A person with higher charges will on average have more children. If charges are increased by 1000 dollars, the calculated number of children increases by 1.4%.

7.1.3 Simulation of data and comparison

With the calculated model, data is simulated:

```
## sim_1
## Min. :0.000
## 1st Qu.:0.000
## Median :1.000
## Mean :1.102
## 3rd Qu.:2.000
## Max. :6.000
```

The original and the simulated data are compared visually. The number of children from the simulated data (0-6) seem to be plausible. The distribution has a strong downwards trend starting at 1 like the original data. However the model does not seem to generate enough data with 0 children.



7.2 Generalised Linear Models for binomial data

A model is fitted that predicts if a person is a smoker or not. Only the significant values age, bmi and charges are used.

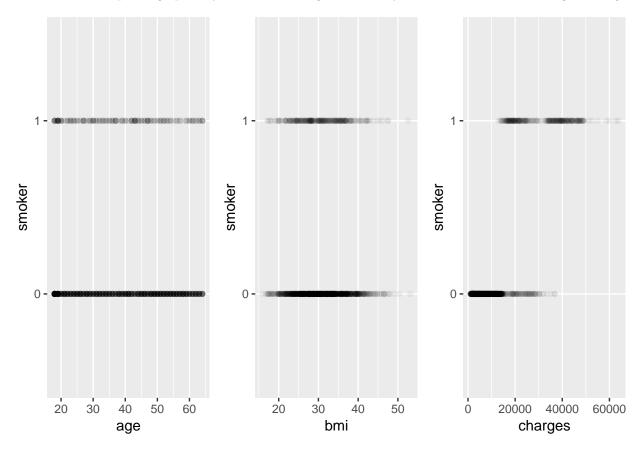
```
glm.smoker.2 <- glm(smoker ~ age+bmi+charges,</pre>
                    data=insurance,
                    family = "binomial")
summary(glm.smoker.2)
##
## Call:
## glm(formula = smoker ~ age + bmi + charges, family = "binomial",
##
       data = insurance)
##
## Deviance Residuals:
##
        Min
                   1Q
                         Median
                                       ЗQ
                                                Max
  -3.09442 -0.10998 -0.04475
                                -0.00970
                                            1.53727
##
## Coefficients:
##
                 Estimate Std. Error z value Pr(>|z|)
## (Intercept) 5.311e+00 1.029e+00
                                       5.163 2.43e-07 ***
               -9.875e-02 1.300e-02 -7.597 3.02e-14 ***
## age
## bmi
               -3.481e-01
                          4.309e-02 -8.078 6.60e-16 ***
## charges
                3.822e-04 2.917e-05 13.104 < 2e-16 ***
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
```

```
##
##
  (Dispersion parameter for binomial family taken to be 1)
##
##
       Null deviance: 1356.63
                               on 1337
                                        degrees of freedom
## Residual deviance: 311.98
                               on 1334 degrees of freedom
  AIC: 319.98
## Number of Fisher Scoring iterations: 8
exp(coef(glm.smoker.2))
## (Intercept)
                                   bmi
                                            charges
                       age
## 202.5686249
                 0.9059677
                             0.7060520
                                          1.0003823
```

Age and BMI has a negative effect on smoker. This means the higher a persons BMI and age, the lower the probability that the person is a smoker. Charges has a positive effect. This means the higher a persons charges, the higher is the possibility that the person smokes.

7.2.1 Graphical analysis

This can also be explored graphically, at least for charges it is clearly visible that smokers have higher charges.



7.2.2 Estimating the model performance

The predicted values are transformed into binary (beforehand they inicated the probability) and compared with the actual data.

```
fitted.smoker.disc <- ifelse(fitted(glm.smoker.2) < 0.5,</pre>
                              yes = 0, no = 1)
head(fitted.smoker.disc)
## 1 2 3 4 5 6
## 1 0 0 1 0 0
d.obs.fit.smoker <- data.frame(obs = insurance$smoker,</pre>
                                fitted = fitted.smoker.disc)
head(d.obs.fit.smoker)
##
     obs fitted
## 1
       1
               1
               0
## 2
       0
## 3
       0
               0
## 4
       0
               1
## 5
       0
               0
## 6
               0
We observe the following fit:
##
      fit
## obs
           0
                1
##
     0 1028
               36
##
          23
              251
```

7.3 Cross Validation

Three linear models are cross validated:

The in sample performance, using R Squared as measure is the following:

```
summary(lm.1)$r.squared

## [1] 0.750913
summary(lm.2)$r.squared

## [1] 0.6236038
summary(lm.3)$r.squared
```

```
## [1] 0.754424
```

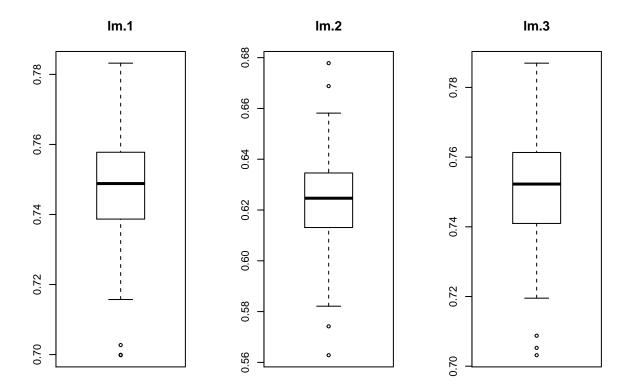
The out of sample performance is computed by using 50:50 training and test data and repeating the process 100 times.

```
set.seed(5)
r.squared.lm.1 <- c()
r.squared.lm.2 <- c()
r.squared.lm.3 <- c()
for(i in 1:100){
    # prepare data</pre>
```

```
train.YES <- sample(x=c(TRUE,FALSE),</pre>
                        size=nrow(insurance),
                        replace = TRUE)
  table(train.YES)
  insurance.train <- insurance[train.YES, ]</pre>
  insurance.test <- insurance[!train.YES, ]</pre>
  # fit model with train data
  lm.1.train <- lm(formula = formula(lm.1),</pre>
                    data = insurance.train)
  lm.2.train <- lm(formula = formula(lm.2),</pre>
                    data = insurance.train)
  lm.3.train <- lm(formula = formula(lm.3),</pre>
                    data = insurance.train)
  # make prediction on test data
  lm.1.predict <- predict(lm.1.train,</pre>
                            newdata = insurance.test)
  lm.2.predict <- predict(lm.2.train,</pre>
                            newdata = insurance.test)
  lm.3.predict <- predict(lm.3.train,</pre>
                            newdata = insurance.test)
  # compute r.squared and save in list
  r.squared.lm.1[i] <- cor(lm.1.predict,</pre>
                             insurance.test$charges)^2
  r.squared.lm.2[i] <- cor(lm.2.predict,</pre>
                             insurance.test$charges)^2
  r.squared.lm.3[i] <- cor(lm.3.predict,</pre>
                             insurance.test$charges)^2
The out of sample performance, using R Squared as measure is the following:
#lm.1
mean(r.squared.lm.1)
## [1] 0.7474233
mean(r.squared.lm.2)
## [1] 0.6235398
#lm.3
mean(r.squared.lm.3)
```

[1] 0.7505379

```
par(mfrow=c(1,3))
boxplot(r.squared.lm.1, main="lm.1")
boxplot(r.squared.lm.2, main="lm.2")
boxplot(r.squared.lm.3, main="lm.3")
```



It can be observed that lm.3 performs slightly better but it is also the most complicated. lm.1 might be the better model, the performance is just slightly lower and it is simpler.

8 Decision Trees -> Adriana

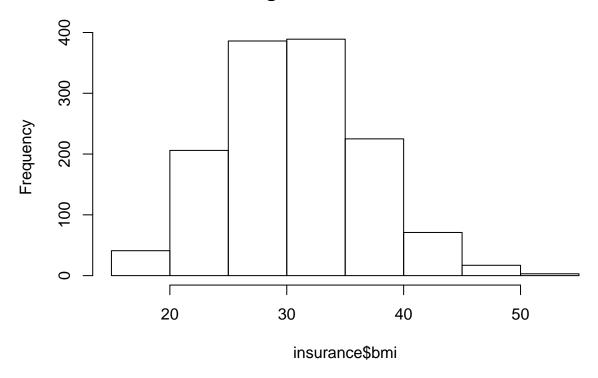
8.1 Regression trees

8.1.1 Inspectig the Data

To start of with our regression trees, we throw a glance at the continuous variables:

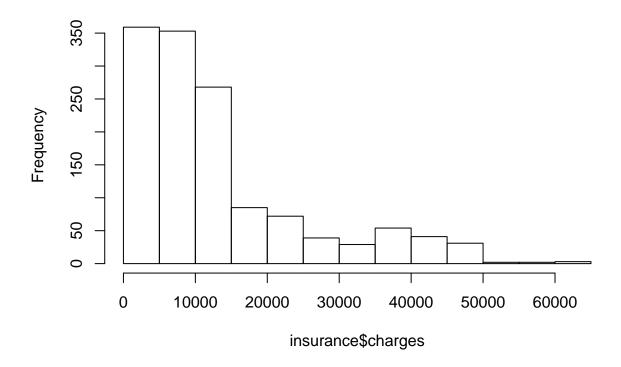
```
hist(insurance$bmi)
```

Histogram of insurance\$bmi



hist(insurance\$charges)

Histogram of insurance\$charges



One can see that BMI seems to be normally distributed whereas charges follows the pattern of a 1/x-function.

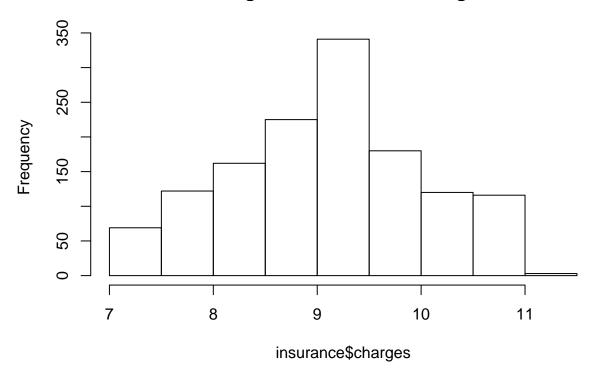
We thus normalize "charges" by logarithming it. (Attention: Please do only execute the code block (convertion to log) below once as executing it several times will apply the logarithmic function several times)

insurance\$charges <- log(insurance\$charges)</pre>

Please note that hence, all charges values for this chaptre will strictly be indicated in log-value and not the true one.

hist(insurance\$charges)

Histogram of insurance\$charges

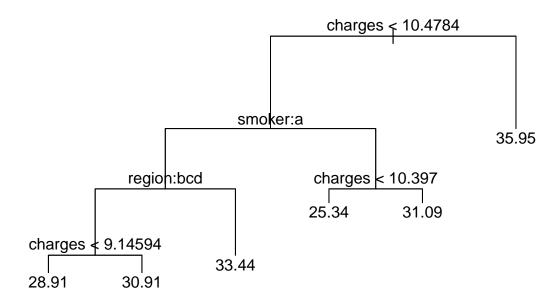


Applying a log-transformation solves this issue.

To begin with, we make the rookie mistake to use all the data, which we will then later change by appying a train-test approach. This is done to empasize the importance of not using all the data to train one's model by showing the differences in methods.

8.1.2 Regression tree - BMI

```
set.seed(99999)
tree.regression.bmi <- tree(bmi~., data=insurance)
plot(tree.regression.bmi)
text(tree.regression.bmi)</pre>
```



We here receive a tree with six terminal nodes. Thanks to the tree-function, the tree is already created by recursive binary splitting. As the variables (internal nodes) determining the BMI, "charges" have been applied as well as if one smokes and from which region one comes. This can also be seen in below summary:

```
summary(tree.regression.bmi)
```

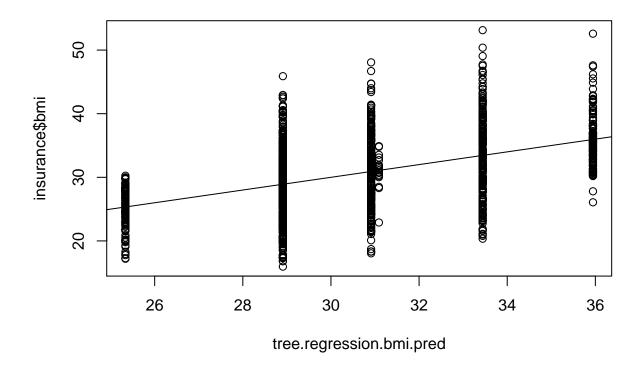
```
##
## Regression tree:
## tree(formula = bmi ~ ., data = insurance)
## Variables actually used in tree construction:
## [1] "charges" "smoker" "region"
## Number of terminal nodes: 6
## Residual mean deviance: 29.23 = 38930 / 1332
## Distribution of residuals:
##
        Min.
               1st Qu.
                          Median
                                      Mean
                                             3rd Qu.
                                                           Max.
## -13.09000 -3.62700 -0.07606
                                   0.00000
                                             3.26700
                                                       19.69000
```

Our residual mean deviance, aka R-squared-error ist at 29.23.

8.1.2.1 Prediction

We here establish a prediction for our BMI tree and also compare the predictions with the true value of the BMI:

```
tree.regression.bmi.pred <- predict(tree.regression.bmi, insurance, type="vector")
plot(tree.regression.bmi.pred, insurance$bmi)
abline(0 ,1)</pre>
```

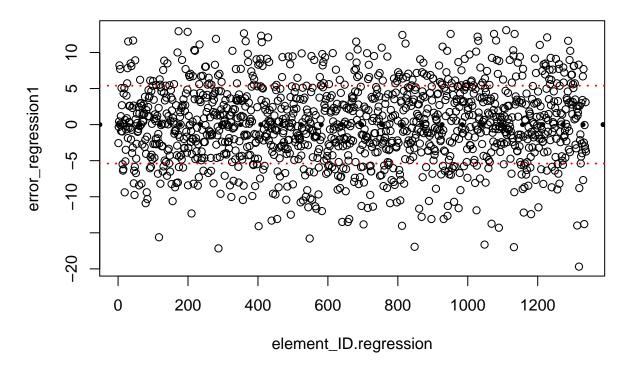


8.1.2.2 Comparison of Prediction <-> True Values

Further, we examine the residuals:

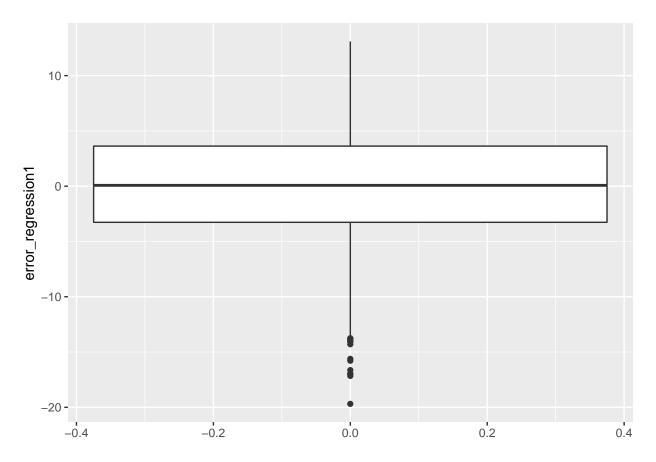
```
error_regression1 <- tree.regression.bmi.pred-insurance$bmi
element_ID.regression <- 1:length(error_regression1)
plot(element_ID.regression, error_regression1)
title(main="Analysis of the residuals")
abline(0 ,0, lwd=5,lty="dotted")
abline(sd(error_regression1) ,0, lwd=2, col="red", lty="dotted")
abline(-sd(error_regression1) ,0, lwd=2, col="red", lty="dotted")</pre>
```

Analysis of the residuals



As can be seen, the residual analysis clearly supports the data to be normally distributed. So it is that most of the residuals are distributed fairly symmetrically around 0. A large portion of the residuals is furthermore within the margins of +- 1 standard deviation.

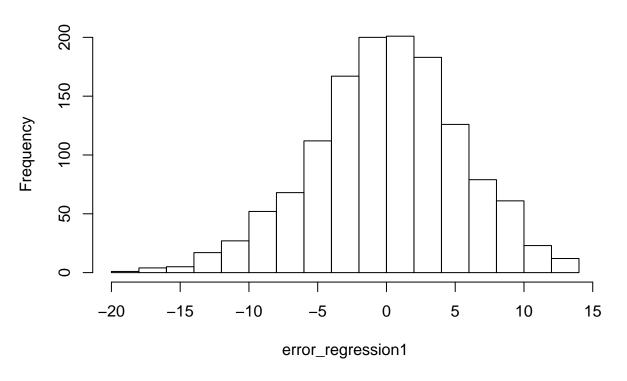
```
error_regression1_dataframe <- tibble(element_ID.regression, error_regression1)
ggplot(data=error_regression1_dataframe) + geom_boxplot(aes(y=error_regression1))</pre>
```



A boxplot further demonstrates the rather normally distributed data with mean around 0. It is apparent for there to be more outliers in the negative y-axis area than the positive y-axis area.

hist(error_regression1)

Histogram of error_regression1



```
RSS_bmi <- sum((insurance[3]-tree.regression.bmi.pred)^2)
MSE_bmi <- RSS_bmi/length(tree.regression.bmi.pred)
deviation_bmi <- sqrt(MSE_bmi)
cat(RSS_bmi)

## 38928.55
cat("\n")
cat(deviation_bmi)</pre>
```

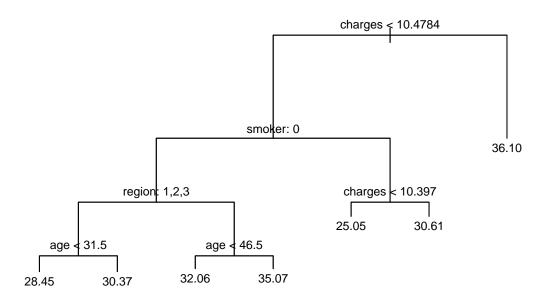
5.39394

So the average estimation of a BMI is about 5.39 BMI points away from the true value (median).

We now switch to the train-test approach.

8.1.2.3 Train <-> Test Approach

```
ratio <- 0.7
total <- nrow(insurance)
train <- sample(1:total, as.integer(total * ratio))
tree.regression.bmi2 <- tree(bmi~., insurance, subset=train)
plot(tree.regression.bmi2)
text(tree.regression.bmi2, pretty=12, cex=0.75)</pre>
```



By working with the test data, we can see at this point a change, meaning a possible overfit. Were there previously six end nodes, we now have seven end notes, with variables used "charges", "smoker", "region" and "age", as also can be seen here:

```
summary(tree.regression.bmi2)
```

```
##
## Regression tree:
## tree(formula = bmi ~ ., data = insurance, subset = train)
## Variables actually used in tree construction:
## [1] "charges" "smoker" "region" "age"
## Number of terminal nodes: 7
## Residual mean deviance: 27.84 = 25860 / 929
## Distribution of residuals:
##
        Min.
               1st Qu.
                          Median
                                      Mean
                                             3rd Qu.
                                                           Max.
## -13.55000 -3.46800 -0.09678
                                   0.00000
                                             3.35700
                                                      16.48000
```

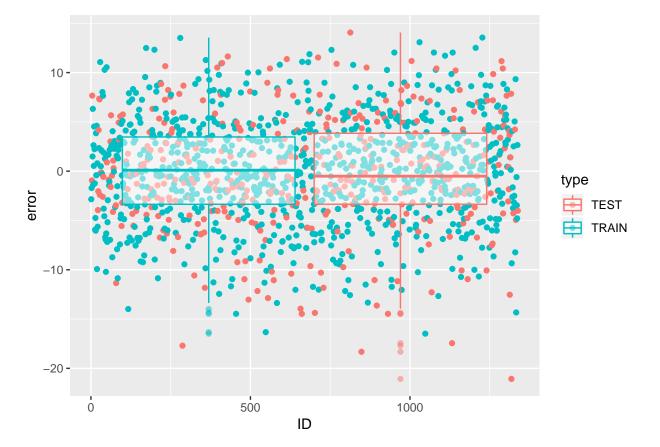
Our residual mean deviance has furthermore gone from 29.23 to 27.84.

8.1.2.4 Error Analysis

```
tree.regression.bmi2.pred <- predict(tree.regression.bmi2, insurance[-train,], type="vector")
(RSS.2.train <- mean(((insurance[train,][3]-predict(tree.regression.bmi2, insurance[train,], type="vect")
## [1] 27.63265
(RSS.2.test <- mean(((insurance[-train,][3]-tree.regression.bmi2.pred)^2)$bmi))
## [1] 32.85365</pre>
```

We receive an RSS for the train dataset of 27.21 whereas for the test set, the RSS is 34.55. We seem to have an overfit as our model performs considerably worse for the test data than the train data.

```
errors.2.in <- predict(tree.regression.bmi2, insurance[train,], type="vector")-insurance[train,]$bmi
element.2.in <- as.integer(names(errors.2.in))
errors.2.in_dataframe <- tibble(element.2.in,errors.2.in,"TRAIN")
colnames(errors.2.in_dataframe) <- c('ID','error','type')
errors.2 <- predict(tree.regression.bmi2, insurance[-train,], type="vector")-insurance[-train,]$bmi
element.2 <- 1:length(errors.2)
element.2 <- as.integer(names(errors.2))
errors.2.out_dataframe <- tibble(element.2,errors.2,"TEST")
colnames(errors.2.out_dataframe) <- c('ID','error','type')
errors.2_dataframe <- bind_rows(errors.2.in_dataframe,errors.2.out_dataframe)
errors.2_dataframe <- arrange(errors.2_dataframe, ID)
ggplot(data = errors.2_dataframe, mapping = aes(x = ID,y = error, color = type)) +
    geom_point() + geom_boxplot(alpha = 0.5)</pre>
```



Both dataframes show the about same boxplots in regard of the errors. Not surprisingly, the distribution of the test data is wider, considering that the model has been trained with

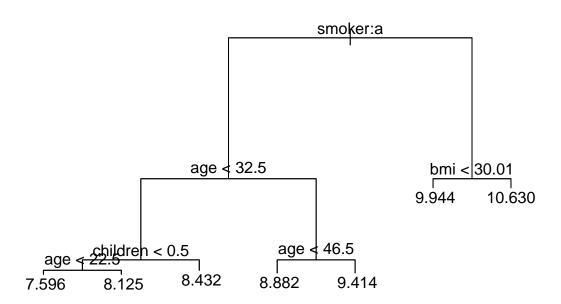
8.1.3 Regression tree - Charges

We now examine the behaviour of the variable "charges". First off again with the entire data values.

```
summary(insurance$charges)
```

```
## Min. 1st Qu. Median Mean 3rd Qu. Max.
## 7.023 8.464 9.147 9.099 9.720 11.063
```

```
tree.regression.charges <- tree(charges~., data=insurance)
plot(tree.regression.charges)
text(tree.regression.charges)</pre>
```



We receive a tree with seven end nodes and four influencing variables, as also the summary further demonstrates:

```
summary(tree.regression.charges)
```

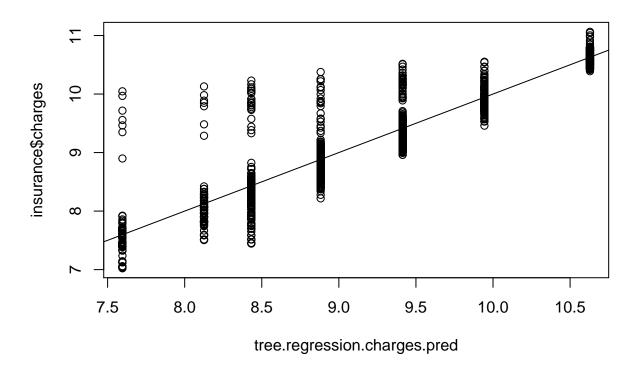
```
##
## Regression tree:
## tree(formula = charges ~ ., data = insurance)
## Variables actually used in tree construction:
## [1] "smoker"
                 "age"
                            "children" "bmi"
## Number of terminal nodes: 7
## Residual mean deviance: 0.1592 = 211.9 / 1331
## Distribution of residuals:
##
      Min. 1st Qu.
                      Median
                                 Mean 3rd Qu.
                                                    Max.
## -0.98730 -0.19690 -0.04999 0.00000 0.09942 2.45100
```

Our residual mean deviance (R-squared-error) us at 0.1592. Note that this value is also log transformed as the numbers on which it has been calculated are log transformed.

8.1.3.1 Prediction

We are now again predicting the data that has already been used for training the modell.

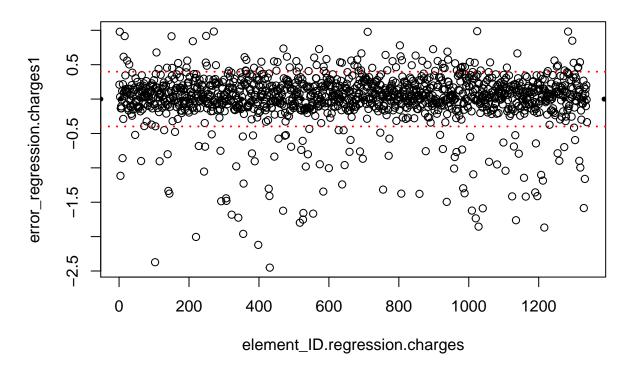
```
tree.regression.charges.pred <- predict(tree.regression.charges, insurance, type="vector")
plot(tree.regression.charges.pred, insurance$charges)</pre>
```



8.1.3.2 Comparison Prediction <-> True Values

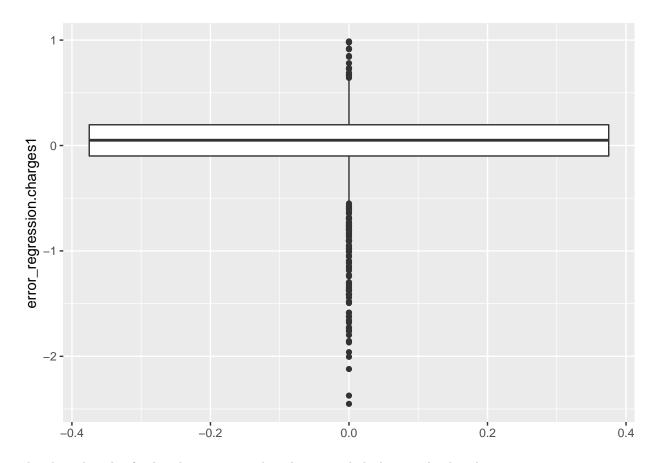
```
error_regression.charges1 <- tree.regression.charges.pred-insurance$charges
element_ID.regression.charges <- 1:length(error_regression.charges1)
plot(element_ID.regression.charges, error_regression.charges1)
title(main="Analysis of the residuals")
abline(mean(error_regression.charges1),0, lwd=5,lty="dotted")
abline(sd(error_regression.charges1),0, lwd=2, col="red", lty="dotted")
abline(-sd(error_regression.charges1),0, lwd=2, col="red", lty="dotted")</pre>
```

Analysis of the residuals



We can furthermore clearly see that the residuals are roughly normalized, with an approximate mean of 0. Outliers are however more distributed in the negative axis of y than in the postiive.

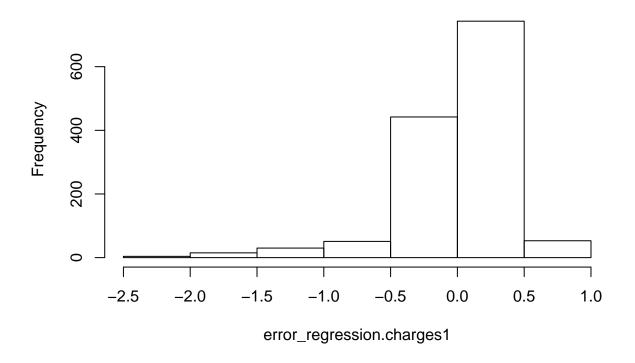
error_regression1_dataframe.charges <- tibble(element_ID.regression.charges, error_regression.charges1)
ggplot(data=error_regression1_dataframe.charges) + geom_boxplot(aes(y=error_regression.charges1))</pre>



The above boxplot further demonstrates that there is a slight bias in the distribution.

hist(error_regression.charges1)

Histogram of error_regression.charges1



Here goes to further show that the data points are slightly skewed. However, mean of the residuals is still roughly at 1.

```
RSS_charges <- sum((insurance[7]-tree.regression.charges.pred)^2)
MSE_charges <- RSS_charges/length(tree.regression.charges.pred)
deviation_charges <- sqrt(MSE_charges)

cat(RSS_charges)

## 211.8598

cat("\n")

cat(deviation_charges)</pre>
```

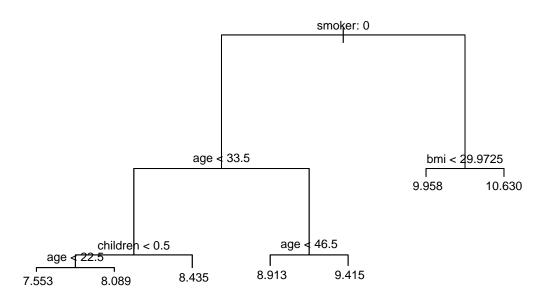
0.3979204

RSS here is at 211.86, the deviation at 0.4.

8.1.3.3 Train-Test-Approach

Again, we use the train-test approach to demonstrate the importance to not use all the data to train one's modell.

```
ratio <- 0.7
total <- nrow(insurance)
train.charges <- sample(1:total, as.integer(total * ratio))
tree.regression.charges2 <- tree(charges~., insurance, subset=train)
plot(tree.regression.charges2)</pre>
```



We now receive a tree with exactly the same number of nodes but where the criterias have different values. summary(tree.regression.charges2)

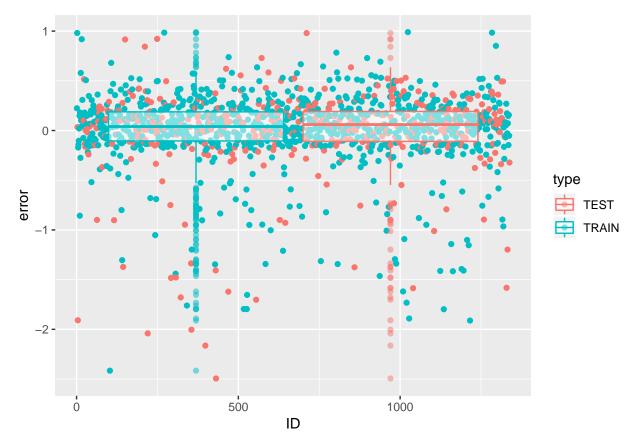
```
##
## Regression tree:
## tree(formula = charges ~ ., data = insurance, subset = train)
## Variables actually used in tree construction:
## [1] "smoker"
                  "age"
                              "children" "bmi"
## Number of terminal nodes: 7
## Residual mean deviance: 0.1475 = 137 / 929
## Distribution of residuals:
##
       Min. 1st Qu.
                       Median
                                   Mean 3rd Qu.
                                                     Max.
## -0.98970 -0.18750 -0.04011 0.00000 0.10500 2.41600
Our residual mean deviance is now a bit lower at 0.1475 (previously: 0.1592)
tree.regression.charges2.pred <- predict(tree.regression.charges2, insurance[-train,], type="vector")</pre>
(RSS.2.train.charges <- mean(((insurance[train,][7]-predict(tree.regression.charges2, insurance[train,]
## [1] 0.146418
(RSS.2.test.charges <- mean(((insurance[-train,][7]-tree.regression.charges2.pred)^2)$charges))
## [1] 0.196484
```

However, our train data, despite still having the same number of terminal nodes, is biased and thus shows an

overfit. Hence it is that RSS for the train set is at e^0.146418, whereas for the test set, we are at e^0.196484.

8.1.3.4 Errors

```
errors.2.in.charges <- predict(tree.regression.charges2, insurance[train,], type="vector")-insurance[trelement.2.in.charges <- as.integer(names(errors.2.in.charges))
errors.2.in_dataframe.charges <- tibble(element.2.in.charges,errors.2.in.charges,"TRAIN")
colnames(errors.2.in_dataframe.charges) <- c('ID','error','type')
errors.2.charges <- predict(tree.regression.charges2, insurance[-train,], type="vector")-insurance[-traelement.2.charges <- 1:length(errors.2.charges)
element.2.charges <- as.integer(names(errors.2.charges))
errors.2.out_dataframe.charges <- tibble(element.2.charges,errors.2.charges,"TEST")
colnames(errors.2.out_dataframe.charges) <- c('ID','error','type')
errors.2_dataframe.charges <- bind_rows(errors.2.in_dataframe.charges,errors.2.out_dataframe.charges)
errors.2_dataframe.charges <- arrange(errors.2_dataframe.charges, ID)
ggplot(data = errors.2_dataframe.charges, mapping = aes(x = ID,y = error, color = type)) +
    geom_point() + geom_boxplot(alpha = 0.5)</pre>
```



There are a few differences, especially in regard of the outliers between the test and the train data. Roughly, one can say however that the boxplot is about the same for train and test. Also, the outliers in the negative area are for both data sets more spread.

8.2 Classification Trees

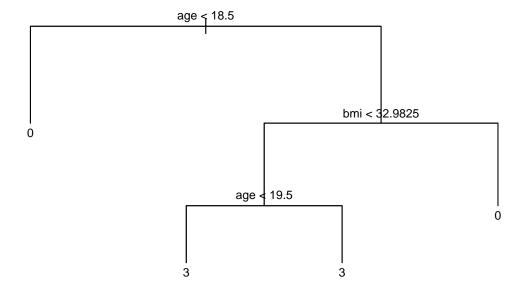
We here examine a decision tree for a non continuous (hence categorical) variable.

```
tree.classification.region_all <- tree(region~., data=insurance)
summary(tree.classification.region_all)</pre>
```

```
##
## Classification tree:
## tree(formula = region ~ ., data = insurance)
## Variables actually used in tree construction:
## [1] "age" "bmi"
## Number of terminal nodes: 4
## Residual mean deviance: 2.604 = 3474 / 1334
## Misclassification error rate: 0.6547 = 876 / 1338
```

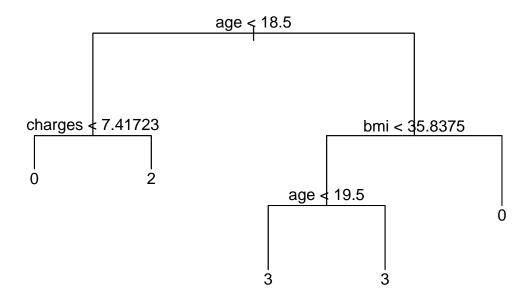
We here receive a classification tree with four end nodes. Furthermore our RMS is at 2.604 and the misclassification rate - which is basically the RSS for classification trees - is at at 65.47%.

```
plot(tree.classification.region_all)
text(tree.classification.region_all, pretty=1, cex=0.75)
```



It appears that the high misclassication rate is partly due to only 2 of the 4 factors being applied in the classification tree. We thus go into testing mode:

```
tree.classification.region <- tree(region~., data=insurance, subset=train)
plot(tree.classification.region)
text(tree.classification.region)</pre>
```



Working with our training set, we see a clear change: we now have five terminal nodes as well as the factor of "northeast" that is not part of the equation.

tree.classification.region.pred <- predict(tree.classification.region, insurance[train,], type="class")</pre>

8.2.1 Confusion Table for Train Data

We now examine the classification error on the train data by comparing the estimation with the true value to elaborate how exact our trained model works.

```
tree.classification.region.pred.ct <- table(tree.classification.region.pred, insurance[train,]$region)
tree.classification.region.pred.correct <- 0
tree.classification.region.pred.error <- 0
for (i1 in 1:4) {
    if (i1 == i2) {
        tree.classification.region.pred.correct <- tree.classification.region.pred.correct + tree.classification.region.pred.error + tree.classification.
    }
    }
}
tree.classification.region.pred.error <- tree.classification.region.pred.error + tree.classification.
}
}
tree.classification.region.pred.rate <- tree.classification.region.pred.correct/sum(tree.classification.tree.classification.region.pred.error <- 1 - tree.classification.region.pred.rate
cat(tree.classification.region.pred.rate)</pre>
```

0.357906

```
cat("\n")
cat(tree.classification.region.pred.error)
```

0.642094

Our "new" tree manages to reduce our classification error by about 1% for the train data.

8.2.2 Confusion Table for Test Data

```
tree.classification.region.pred.test <- predict(tree.classification.region, insurance[-train,], type="c</pre>
```

We now determine the classification error on our test data:

(tree.classification.region.pred.test.ct <- table(tree.classification.region.pred.test, insurance[-trained-tra

```
## tree.classification.region.pred.test 0 1 2 3 ## 0 41 14 16 9 ## 1 0 0 0 0 0 ## 2 3 0 8 0 ## 2 3 73 81 79 78 tree.classification.region.pred.correct <- 0
```

```
tree.classification.region.pred.error <- 0
for (i1 in 1:3) {
   for (i2 in 1:3) {
      if (i1 == i2) {
          tree.classification.region.pred.correct <- tree.classification.region.pred.correct + tree.classification.region.pred.correct + tree.classification.region.pred.error + tree.classification.pred.error + tree.classification.pred.error + tree.classification.pred.error + tree.classification.p
```

(tree.classification.region.pred.rate <- tree.classification.region.pred.correct/sum(tree.classification

[1] 0.1218905

```
(tree.classification.region.pred.error <- 1 - tree.classification.region.pred.rate)</pre>
```

[1] 0.8781095

Whereas the model performed a bit better with the train data in comparison with the entire data set, the model now clearly performs in an all time bad. The training model is thus a clear overfit.

It seems that region, considering the constant high error quote for entire data set, train set as well as test set, is not a variable that has a large connection with the other variables used.

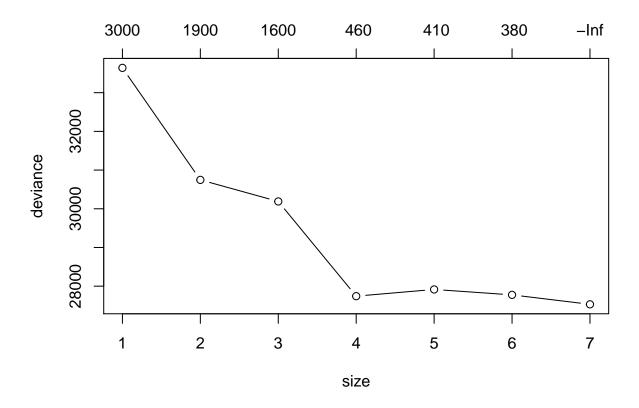
8.3 Pruning

We now continue to prune the trees as so far, we actually managed to create an overfit of our train data in comparison to our test data.

8.3.1 Pruning the continous BMI variable

We recall: the BMI showed a clear overfit when comparing the RSS of train <-> test data: train = 27.21 test = 34.55

```
tree.regression.bmi.pruning = cv.tree(tree.regression.bmi2, FUN = prune.tree)
plot(tree.regression.bmi.pruning, type = "b")
```



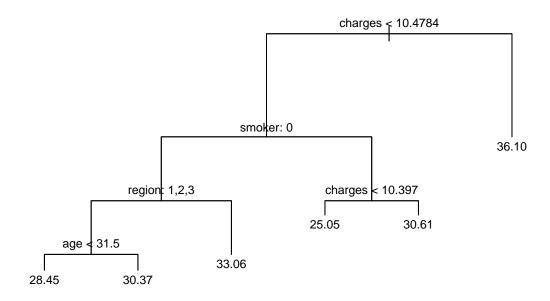
With cytree, the crossvalidation is done automatically for one. We here see that the tree with seven end nodes has the smallest cross-validation error of about 27'250. This is also further shown in below table. Four terminal end leaves is furthermore also very interesting as afterwards (up to 7), the changes are only small in comparison with the steep lines from 1 to 3.

tree.regression.bmi.pruning

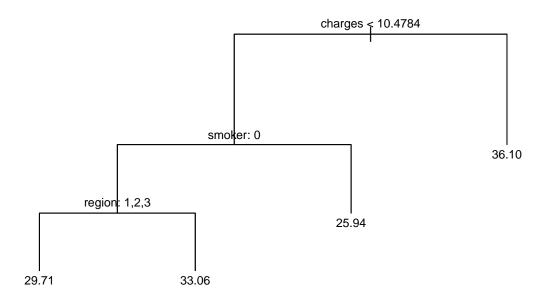
```
## $size
## [1] 7 6 5 4 3 2 1
##
## $dev
##
  [1] 27530.68 27774.88 27914.67 27741.44 30188.86 30746.46 33641.26
##
## $k
## [1]
            -Inf 376.0091 414.7563 462.4535 1571.4867 1872.8382 3018.0179
##
## $method
##
  [1] "deviance"
##
## attr(,"class")
## [1] "prune"
                       "tree.sequence"
```

What is intersting to see is that between the number of end nodes 4 and 7, there is a slight growth as well as decline in terms of variance, so the slope inbetween is both negative as well as positive.

```
tree.regression.bmi.pruned <- prune.tree(tree.regression.bmi2, best = 6)
plot(tree.regression.bmi.pruned)
text(tree.regression.bmi.pruned, pretty=1, cex=0.75)</pre>
```



```
tree.regression.bmi.pruned2 <- prune.tree(tree.regression.bmi2, best = 4)
plot(tree.regression.bmi.pruned2)
text(tree.regression.bmi.pruned2, pretty=1, cex=0.75)</pre>
```



```
##
## Regression tree:
## snip.tree(tree = tree.regression.bmi2, nodes = 9L)
## Variables actually used in tree construction:
## [1] "charges" "smoker" "region" "age"
## Number of terminal nodes: 6
## Residual mean deviance: 28.22 = 26240 / 930
## Distribution of residuals:
##
        Min.
               1st Qu.
                          Median
                                      Mean
                                             3rd Qu.
## -13.55000 -3.57100 -0.09678
                                   0.00000
                                             3.33800
                                                      16.48000
summary(tree.regression.bmi.pruned2)
```

```
##
## Regression tree:
## snip.tree(tree = tree.regression.bmi2, nodes = c(9L, 5L, 8L))
## Variables actually used in tree construction:
## [1] "charges" "smoker" "region"
## Number of terminal nodes: 4
## Residual mean deviance: 29.1 = 27120 / 932
## Distribution of residuals:
##
     Min. 1st Qu.
                   Median
                              Mean 3rd Qu.
                                              Max.
## -13.750
           -3.680
                   -0.110
                             0.000
                                     3.635
                                            16.990
```

summary(tree.regression.bmi.pruned)

In comparison, we can say that the tree with four end nodes more or less performs the same good as the tree with six end nodes. Of course, for the tree with 6 leaves, the residual mean deviance is a bit lower than for

four. In terms of internal nodes however, the construction of the tree is roughly the same - with, of course, the exception of the two additional splits for which is also used an additional variable in comparison, namely "age".

```
(RSS.cv.bmi.test <- sum((insurance[train,][3]-predict(tree.regression.bmi.pruned, insurance[train,], ty)
## [1] 28.03437
tree.regression.bmi.pruned.pred <- predict(tree.regression.bmi.pruned, insurance[-train,], type="vector")
(RSS.cv <- sum((insurance[-train,][3]-tree.regression.bmi.pruned.pred)^2)/length(tree.regression.bmi.pr
## [1] 31.87446</pre>
```

Unsurprisingly, the error for the pruned tree (30.42) is still higher because with pruning, you basically have a fully grown tree and start cutting branches off that are not as necessary as others. Meaning pruning does not grant a perfect performance in an absolute sense.

8.3.2 Pruning regions

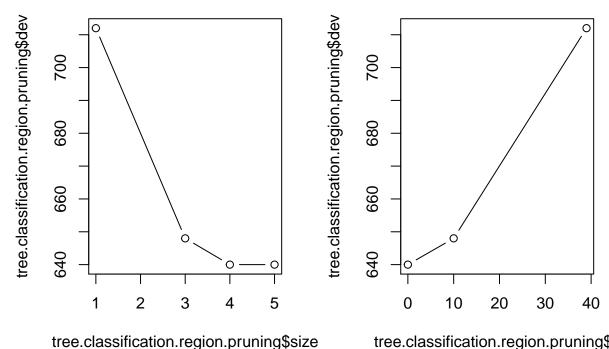
We now prune our classification tree, meaning the tree with the categorical variable. By setting FUN to prune.misclass, we communicate that this decision tree will be handling a continuous variable.

tree.classification.region.pruning <- cv.tree(tree.classification.region, FUN = prune.misclass)
summary(tree.classification.region.pruning)</pre>

```
## Length Class Mode
## size 4    -none- numeric
## dev 4    -none- numeric
## k 4    -none- numeric
## method 1    -none- character
tree.classification.region.pruning
```

We have a length of four whereas the size of four is the optimal size.

```
par(mfrow=c(1,2))
plot(tree.classification.region.pruning$size, tree.classification.region.pruning$dev, type="b")
plot(tree.classification.region.pruning$k, tree.classification.region.pruning$dev, type="b")
```



Residual mean deviance: 2.633 = 2456 / 933

tree.classification.region.pruning\$k

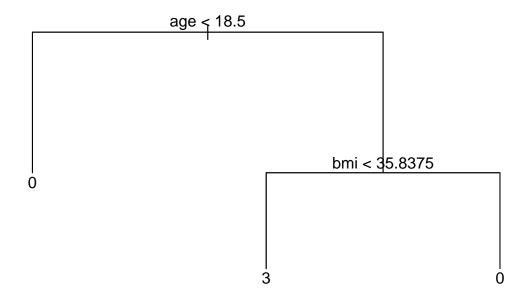
```
par(mfrow=c(1,1))
```

For around 3 and 4, the line is flat whereas before it is very steep and afterwards grows a little bit as well. For deviane, we receive good values for it inbetween 0 to 10.

We go with three for the further processing of pruning this decision tree, as it combines low values in both illustrations above, thus is good in terms of a low deviance.

```
prune.tree.classification.region <- prune.misclass(tree.classification.region, best=3)
summary (prune.tree.classification.region)
##
## Classification tree:
## snip.tree(tree = tree.classification.region, nodes = c(6L, 2L
## ))
## Variables actually used in tree construction:
## [1] "age" "bmi"
## Number of terminal nodes: 3
```

```
## Misclassification error rate: 0.6528 = 611 / 936
plot(prune.tree.classification.region)
text(prune.tree.classification.region,pretty=0)
```

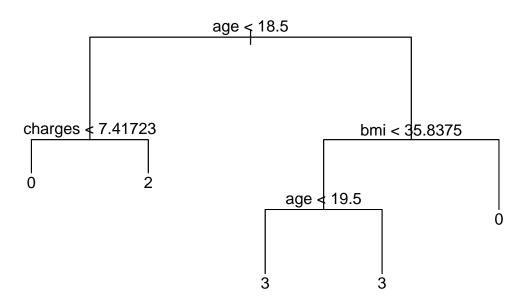


The residual mean deviane is at 2.633 whereas the misclassification error is at 65.28%.

```
prune.tree.classification.region2 <- prune.misclass(tree.classification.region, best=5)
summary (prune.tree.classification.region2)</pre>
```

```
##
## Classification tree:
## tree(formula = region ~ ., data = insurance, subset = train)
## Variables actually used in tree construction:
## [1] "age" "charges" "bmi"
## Number of terminal nodes: 5
## Residual mean deviance: 2.555 = 2379 / 931
## Misclassification error rate: 0.6421 = 601 / 936

plot(prune.tree.classification.region2)
text(prune.tree.classification.region2,pretty=0)
```



The residual mean deviane is at 2.555 with a misclassification error rate of 0.6421.

We now make a prediction on our test data:

 $cat("\n")$

```
cat(prune.tree.classification.region.pred.testError)
```

```
## 0.6965174
```

However, despite the classification rate still being very low, in comparison, the error has drastically reduced in comparison with the unpruned tree.

8.4 Bagging

```
set.seed (5)
train = sample(1:nrow(insurance), nrow(insurance)/2)
insurance.test=insurance[-train ,]
```

We now are bagging our dataset. We furthermore say that we are happy with an estimation and not the real crossyalidation.

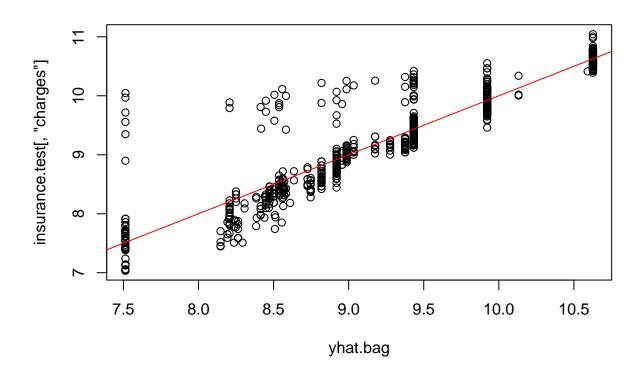
```
bag.insurance=bagging(charges~., data=insurance, subset=train, nbagg=20, coob = TRUE)
print(bag.insurance)
```

```
##
## Bagging regression trees with 20 bootstrap replications
##
## Call: bagging.data.frame(formula = charges ~ ., data = insurance, subset = train,
## nbagg = 20, coob = TRUE)
##
## Out-of-bag estimate of root mean squared error: 0.391
#bag.insurance still needs to be squared at this point
```

We here receive a root mean squared error of 0.391 -> root mean error = 0.152881.

We now predict performance from our bagged model:

```
yhat.bag = predict(bag.insurance, newdata=insurance[-train,])
plot(yhat.bag, insurance.test[,"charges"])
abline(0,1, col="red")
```



On the x-axis, we see the prediction, whereas on the y-axis, the real value (logarithmic).

We also compute the mean: in comparison with the previously caluclated mean value, we can say they are rather related.

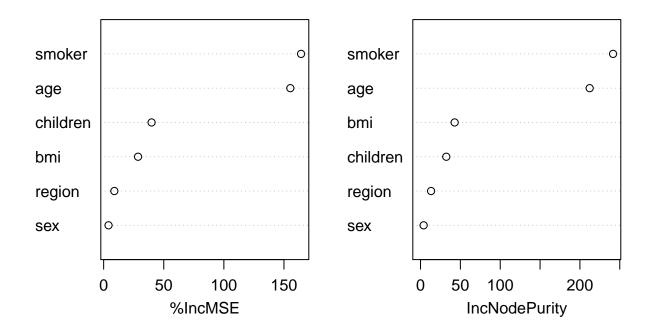
```
mean((yhat.bag-insurance.test[,"charges"])^2)
## [1] 0.1575089
We also test this with the random forest way to do it.
## test with randomForest
bag.insurance.2=randomForest(charges~., data=insurance, subset=train, mtry=6, importance =TRUE)
# mtry = 7 means that we should use all 13 predictors for each split of the tree, hence, do bagging (no
print(bag.insurance.2)
##
## Call:
    randomForest(formula = charges ~ ., data = insurance, mtry = 6,
                                                                           importance = TRUE, subset = tr
##
                  Type of random forest: regression
##
                        Number of trees: 500
##
  No. of variables tried at each split: 6
##
##
             Mean of squared residuals: 0.1497648
                       % Var explained: 82.09
##
importance(bag.insurance.2)
```

%IncMSE IncNodePurity

##

```
212.223089
## age
            155.286361
## sex
              4.046307
                             3.899614
## bmi
             28.599394
                            42.827102
## children 39.871574
                            32.346164
## smoker
            164.251751
                           241.621328
## region
              8.898203
                            13.246871
varImpPlot(bag.insurance.2)
```

bag.insurance.2



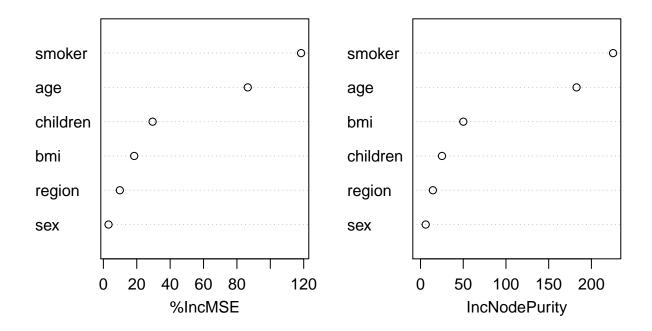
We here see that age and if one smokes are of biggest influence on charges.

8.5 Random Forests

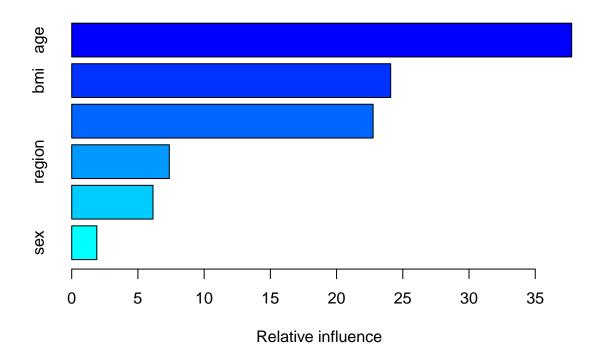
```
set.seed(10)
rf.insurance=randomForest(charges~.,data=insurance,subset=train, mtry=2,importance =TRUE)
yhat.rf = predict(rf.insurance ,newdata=insurance[-train ,])
mean((yhat.rf-insurance.test[,"charges"])^2)
## [1] 0.158069
importance(rf.insurance)
               %IncMSE IncNodePurity
##
                          182.623763
## age
             86.489219
## sex
              3.084226
                            6.073046
## bmi
             18.476454
                           50.077296
## children 29.481898
                           25.129388
## smoker
            118.440509
                          225.385251
```

```
## region 9.858480 14.461133
varImpPlot (rf.insurance)
```

rf.insurance



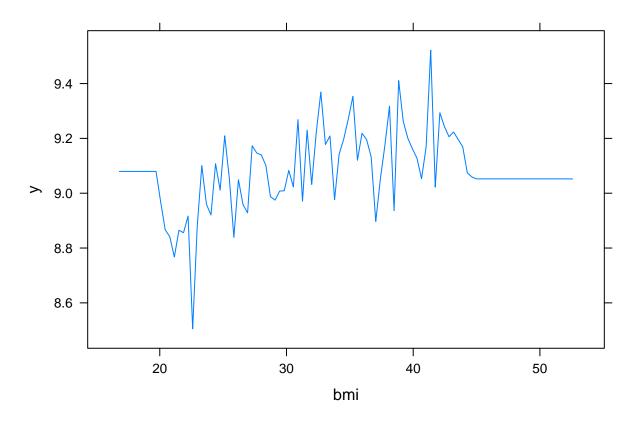
8.6 Boosting



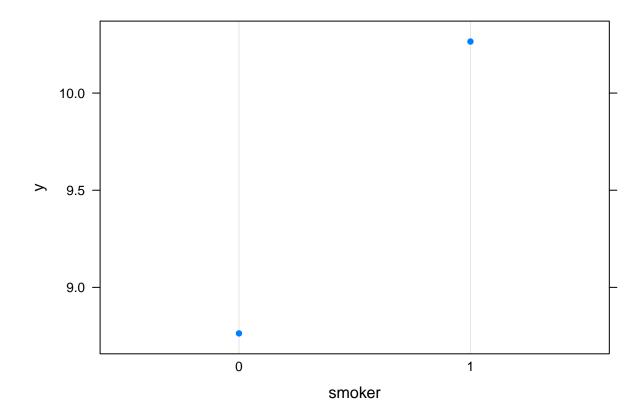
```
## var rel.inf
## age age 37.751923
## bmi bmi 24.084978
## smoker smoker 22.759940
## region region 7.370245
## children children 6.137392
## sex sex 1.895522
```

We now show partial dependence the for most important factors:

```
plot(boost.insurance ,i="bmi")
```



plot(boost.insurance ,i="smoker")



We now do a prediction with the booted model.

```
yhat.boost=predict(boost.insurance, newdata=insurance[-train,], n.trees=5000)
mean((yhat.boost -insurance.test[,"charges"])^2)
```

[1] 0.2383602

The output is our MSE = 0.2383602.

We now are resetting shrinkage /lambda parameter which expresses basically that we have an overfit effect faster:

```
boost.insurance = gbm(charges~.,data=insurance[train,],distribution="gaussian",n.trees=5000, interaction
yhat.boost2=predict(boost.insurance,newdata=insurance[-train,], n.trees=5000)
mean((yhat.boost2 -insurance.test[,"charges"])^2)
```

[1] 0.193239

We now receive a smaller error rate, so one could say this is a better model.

And we do the same thing again but on the other side:

```
boost.insurance2=gbm(charges~.,data=insurance[train,],distribution="gaussian",n.trees=5000, interaction
yhat.boost3=predict(boost.insurance2,newdata=insurance[-train,], n.trees=5000)
mean((yhat.boost -insurance.test[,"charges"])^2)
```

[1] 0.2383602

We now have a higher test MSE which means this model is worse as overfitting has already started.

(Attention: Please do only execute the code block (applying the exponential function) below once as executing

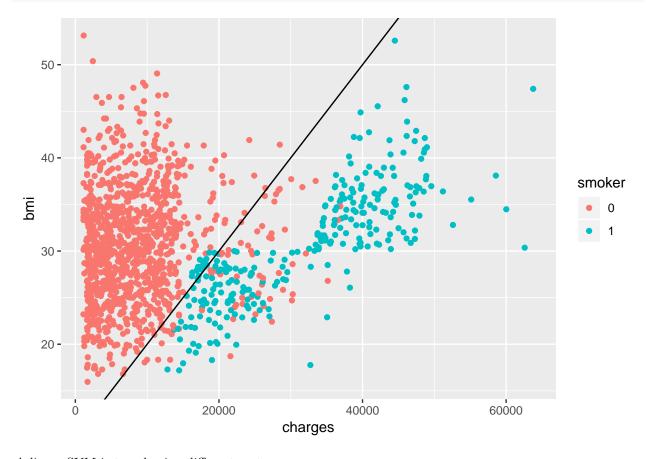
9 Support Vector Machines -> Carole

In this chapter, Support Vector Machines are applied to the insurance dataset.

9.1 two classes linear

By visual exploration, we discover that smokers and non-smokers form two groups. We fit an SVM for those two groups. The lines in the graph are the first guess of how the data could be divided.

```
# guess of hyperplane
slope <- 0.001
intercept <- 10
ggplot(data = insurance) +
  geom_point(aes(x = charges, y = bmi, color=smoker))+
  geom_abline(slope = slope, intercept = intercept)</pre>
```



A linear SVM is tuned using different cost ranges.

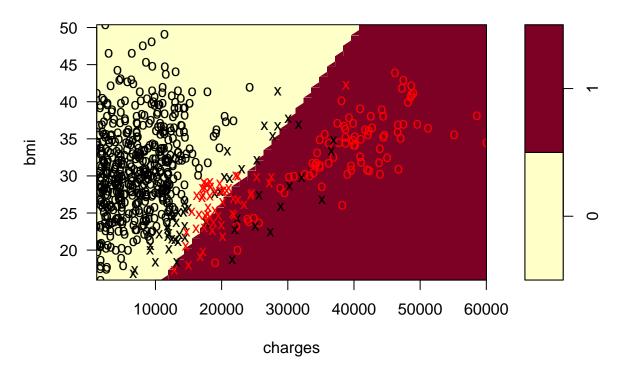
```
set.seed(5)
#get optimal cost
cost_range <-
  c(1e-10,
    1e-7,</pre>
```

```
1e-5,
    0.001,
    0.0025,
    0.005,
    0.0075,
    0.01,
    0.1,
    1,
    5,
    10,
    100,
    200)
tune.out.1 <- tune(</pre>
  svm,
  smoker ~ charges+bmi,
  data = insurance.train,
  kernel = "linear",
  ranges = list(cost = cost_range)
```

The following is the best model. A cost of 5 is used. There are 104 support vectors.

```
#best model
bestmod <- tune.out.1$best.model</pre>
summary(bestmod)
##
## Call:
## best.tune(method = svm, train.x = smoker ~ charges + bmi, data = insurance.train,
       ranges = list(cost = cost_range), kernel = "linear")
##
##
##
## Parameters:
##
     SVM-Type: C-classification
## SVM-Kernel: linear
##
         cost: 5
##
## Number of Support Vectors: 104
##
##
   (5252)
##
##
## Number of Classes: 2
##
## Levels:
## 0 1
plot(bestmod, insurance.train, bmi~charges)
```

SVM classification plot



The confision matrices and the classification error rate for train and test data are:

```
# confusion matrix train
confusion.lin.train <- table(predict = predict(bestmod, insurance.train),</pre>
      truth = insurance.train$smoker)
confusion.lin.train
##
          truth
## predict
             0
##
         0 514 26
         1 18 106
#classification error rate train
(confusion.lin.train[1,2]+confusion.lin.train[2,1])/sum(confusion.lin.train[1:2,1:2])
## [1] 0.06626506
# confusion matrix linear test
confusion.lin.test <- table(predict = predict(bestmod, insurance.test),</pre>
      truth = insurance.test$smoker)
confusion.lin.test
##
          truth
## predict
             0
         0 527 142
#classification error rate test
(confusion.lin.test[1,2]+confusion.lin.test[2,1])/sum(confusion.lin.test[1:2,1:2])
```

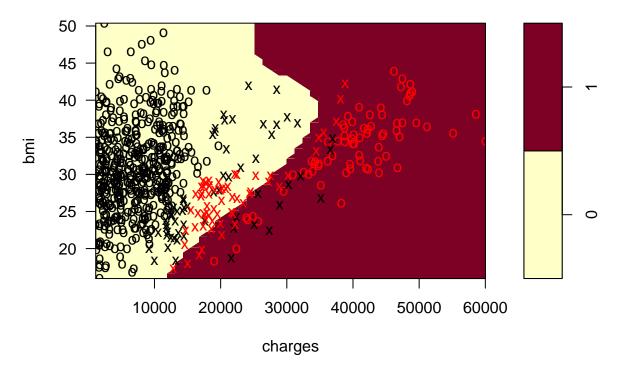
9.2 two classes polynomial

A polynomial model was also tested but the classification error rate was slightly higher:

```
set.seed(5)
#get optimal cost and degree for polynomial
cost_range <-</pre>
  c(1e-10,
    1e-7,
    1e-5.
    0.001,
    0.0025,
    0.005,
    0.0075,
    0.01,
    0.1,
    1,
    5,
    10,
    100)
degree range <- 2:4
tune.out.poly <- tune(</pre>
  smoker ~ charges+bmi,
 data = insurance.train,
 kernel = "polynomial",
 ranges = list(cost = cost_range, degree = degree_range))
#best model poly
tune.out.poly$best.parameters
##
      cost degree
## 26 100
bestmod.poly <- tune.out.poly$best.model</pre>
summary(bestmod.poly)
##
## best.tune(method = svm, train.x = smoker ~ charges + bmi, data = insurance.train,
       ranges = list(cost = cost_range, degree = degree_range),
##
##
       kernel = "polynomial")
##
##
## Parameters:
      SVM-Type: C-classification
##
##
    SVM-Kernel: polynomial
##
          cost: 100
##
        degree: 3
##
        coef.0: 0
##
## Number of Support Vectors: 120
##
##
   (60 60)
##
```

```
##
## Number of Classes: 2
##
## Levels:
## 0 1
plot(bestmod.poly, insurance.train, bmi~charges)
```

SVM classification plot



10 Neural Networks

10.1 Neural Networks using "neuralnet"

In this section we will create and train a neural network which should be able to classify if a person is a smoker (output) based on the information of age, bmi and charges that are provided as input factors for

the model. The assumption of the input variables is retrieved from our analysis already done in section 5. Generalized Linear Models.

10.1.1 Cleaning and Normalization

This part will be needed to ensure a cleansed and normalized database for a proper modeling of neural networks.

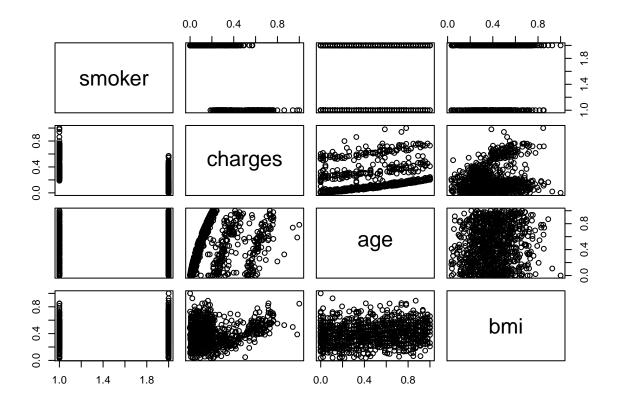
#setwd("~/GitHub/machinelearning/machinelearning/03_rmarkdown") #adrianas extrawurst

```
insurance <- read.csv(".../01_data/insurance.csv", header=TRUE)</pre>
str(insurance)
## 'data.frame':
                    1338 obs. of 7 variables:
             : int 19 18 28 33 32 31 46 37 37 60 ...
              : Factor w/ 2 levels "female", "male": 1 2 2 2 2 1 1 1 2 1 ...
## $ sex
## $ bmi
            : num 27.9 33.8 33 22.7 28.9 ...
## $ children: int 0 1 3 0 0 0 1 3 2 0 ...
## $ smoker : Factor w/ 2 levels "no", "yes": 2 1 1 1 1 1 1 1 1 1 ...
## $ region : Factor w/ 4 levels "northeast", "northwest", ...: 4 3 3 2 2 3 3 2 1 2 ...
## $ charges : num 16885 1726 4449 21984 3867 ...
# smoker = 1 / nonsmoker = 2
insurance$smoker <- as.character(insurance$smoker)</pre>
insurance$smoker[insurance$smoker == "yes"] <- "1"</pre>
insurance$smoker[insurance$smoker == "no"] <- "2"</pre>
insurance$smoker <- as.factor(insurance$smoker)</pre>
# female = 1 / male = 0
insurance$sex <- as.character(insurance$sex)</pre>
insurance$sex[insurance$sex == "female"] <- "1"</pre>
insurance$sex[insurance$sex == "male"] <- "0"</pre>
insurance$sex <- as.factor(insurance$sex)</pre>
\# region / SE = 1 / SW = 0 / NE = 2 / NW = 3
insurance$region <- as.character(insurance$region)</pre>
insurance$region[insurance$region == "southwest"] <- "1"</pre>
insurance$region[insurance$region == "southeast"] <- "0"</pre>
insurance$region[insurance$region == "northeast"] <- "2"</pre>
insurance$region[insurance$region == "northwest"] <- "3"</pre>
insurance$region <- as.factor(insurance$region)</pre>
head(insurance)
                bmi children smoker region
##
     age sex
                                              charges
                                          1 16884.924
## 1 19 1 27.900
                           0
                                   1
## 2 18
           0 33.770
                           1
                                   2
                                          0 1725.552
## 3 28 0 33.000
                           3
                                   2
                                          0 4449.462
                                   2
     33
          0 22.705
                            0
                                          3 21984.471
## 5 32
           0 28.880
                            0
                                   2
                                          3 3866.855
           1 25.740
                                   2
                                          0 3756.622
options(scipen = 99) # penalty for displaying scientific notation
options(digits = 4) # suggested number of digits to display
data <-dplyr::select(insurance, smoker, charges, age, bmi)</pre>
data$charges <- (data$charges - min(data$charges))/(max(data$charges) - min(data$charges)) # Min-Max No
data$age <- (data$age - min(data$age))/(max(data$age) - min(data$age)) # Min-Max Normalization
data$bmi <- (data$bmi - min(data$bmi))/(max(data$bmi)-min(data$bmi)) # Min-Max Normalization
```

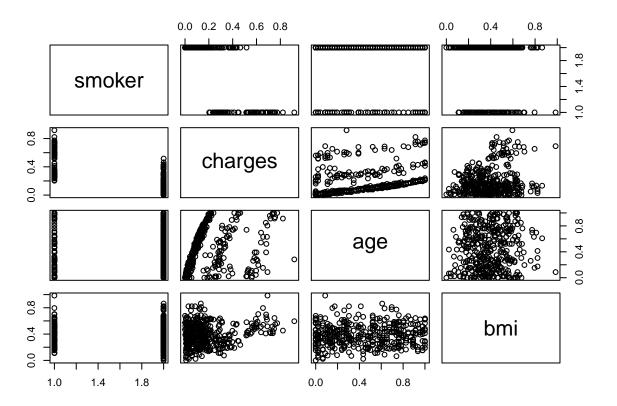
10.1.2 Partition into training and test subsets

As shown above we already cleansed and normalized data. Now we will create two subsets of the insurance data set. Therefore we will execute a partition, so we will have a training set covering 70% of the original dataset while the test set will cover the remaining 30%.

```
set.seed(222)
ind <- sample(2, nrow(data), replace = TRUE, prob = c(0.7, 0.3))
training <- data[ind==1,]
testing <- data[ind==2,]
par(mfrow = c(1, 1))
plot(training)</pre>
```



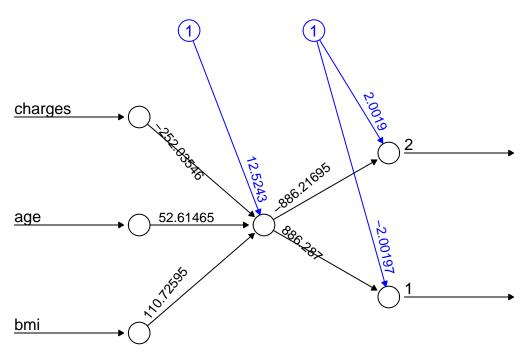
plot(testing)



10.1.3 Creation and Training of the Neural Network

10.1.3.1 Not deep NN - one single hidden layer

10.1.3.1.1 Creation of NN_1



Error: 166.267262 Steps: 17329

```
##### Prediction on training subset
prediction_nn <- predict(nn,training)
#prediction_nn
class_nn <- apply(prediction_nn, 1, which.max)</pre>
```

10.1.3.1.2 Confusion Matrix for training

```
table(training$smoker, class_nn)

## class_nn
## 1 2
## 1 197 0
## 2 27 711

#training$smoker[1]
#class_nn[1]
```

10.1.3.1.3 Performance for training

```
levels(training$smoker)[class_nn[1]]

## [1] "2"

corrects=sum(levels(training$smoker)[class_nn]==training$smoker)
errors=sum(levels(training$smoker)[class_nn]!=training$smoker)
(perf.nn=corrects/(corrects+errors))
```

[1] 0.9711

```
print(paste('training accuracy: ',perf.nn*100,"%"))
## [1] "training accuracy: 97.1122994652406 %"
10.1.3.1.4 Prediction on test subset
prediction_nn <- predict(nn,testing)</pre>
#prediction_nn
class_nn <- apply(prediction_nn, 1, which.max)</pre>
10.1.3.1.5 Confusion Matrix for testing
table(testing$smoker, class_nn)
##
      class_nn
         1
##
##
     1 75
             2
     2 13 313
##
#training$smoker[1]
#class_nn[1]
10.1.3.1.6 Performance for testing
levels(testing$smoker)[class_nn[1]]
## [1] "1"
corrects=sum(levels(testing$smoker)[class_nn]==testing$smoker)
errors=sum(levels(testing$smoker)[class_nn]!=testing$smoker)
(perf.nn=corrects/(corrects+errors))
## [1] 0.9628
print(paste('testing accuracy: ',perf.nn*100,"%"))
## [1] "testing accuracy: 96.2779156327543 %"
10.1.3.2 Deep NN - two hidden layers
10.1.3.2.1 Creation of NN_2
set.seed(444)
nn2 <- neuralnet(smoker~charges + age + bmi,
               data = training,
               hidden = c(7,7),
               threshold = 0.0025,
               lifesign = 'full',
               lifesign.step = 500,
               linear.output = FALSE)
## hidden: 7, 7
                   thresh: 0.0025
                                      rep: 1/1
                                                  steps:
                                                             500 min thresh: 0.11825064758526
##
                                                            1000 min thresh: 0.112617356849393
                                                            1500 min thresh: 0.112617356849393
##
##
                                                            2000 min thresh: 0.107500337348156
                                                            2500 min thresh: 0.0500175621736521
##
```

3000 min thresh: 0.0219775031983741

##

```
3500 min thresh: 0.0129098584782895
##
##
                                                             4000 min thresh: 0.00367818486599488
                                                             4441 error: 19.00295 time: 7.31 secs
##
#summary(nn)
#print(nn)
plot(nn2, rep='best')
charges
age
bmi
                           Error: 19.002947 Steps: 4441
\#\#\#\# Prediction on training subset
prediction_nn2 <- predict(nn2,training)</pre>
#prediction_nn
class_nn <- apply(prediction_nn2, 1, which.max)</pre>
10.1.3.2.2 Confusion Matrix for training
table(training$smoker, class_nn)
##
      class_nn
##
         1
##
     1 197
             0
     2 19 719
```

10.1.3.2.3 Performance for

#training\$smoker[1]

#class_nn[1]

```
levels(training$smoker)[class_nn[1]]
## [1] "2"
corrects=sum(levels(training$smoker)[class_nn]==training$smoker)
errors=sum(levels(training$smoker)[class_nn]!=training$smoker)
(perf.nn=corrects/(corrects+errors))
## [1] 0.9797
print(paste('training accuracy: ',perf.nn*100,"%"))
## [1] "training accuracy: 97.9679144385027 %"
10.1.3.2.4 Prediction on test subset
prediction_nn2 <- predict(nn2,testing)</pre>
#prediction_nn
class_nn <- apply(prediction_nn2, 1, which.max)</pre>
10.1.3.2.5 Confusion Matrix for testing
table(testing$smoker, class_nn)
##
      class_nn
##
         1
##
     1 74
             3
     2 12 314
#training$smoker[1]
#class_nn[1]
10.1.3.2.6 Performance for testing
levels(testing$smoker)[class_nn[1]]
## [1] "1"
corrects=sum(levels(testing$smoker)[class_nn]==testing$smoker)
errors=sum(levels(testing$smoker)[class_nn]!=testing$smoker)
(perf.nn=corrects/(corrects+errors))
## [1] 0.9628
print(paste('testing accuracy: ',perf.nn*100,"%"))
## [1] "testing accuracy: 96.2779156327543 %"
10.1.3.3 Deep NN - three hidden layers
10.1.3.3.1 Creation of NN 3
set.seed(444)
nn3 <- neuralnet(smoker~charges + age + bmi,</pre>
               data = training,
               hidden = c(3,2,1),
               threshold = 0.0025,
               lifesign = 'full',
```

```
lifesign.step = 500,
               linear.output = FALSE)
                                         rep: 1/1
                                                                      min thresh: 0.0938559883189038
## hidden: 3, 2, 1
                      thresh: 0.0025
                                                      steps:
                                                                 500
##
                                                                      min thresh: 0.0938559883189038
                                                                1000
##
                                                                      min thresh: 0.0938559883189038
                                                                1500
##
                                                                2000
                                                                      min thresh: 0.0938559883189038
##
                                                                2500
                                                                      min thresh: 0.0779042619497504
                                                                3000
##
                                                                      min thresh: 0.0477729129630322
##
                                                                3500
                                                                      min thresh: 0.0477729129630322
##
                                                                4000
                                                                      min thresh: 0.0477729129630322
                                                                      min thresh: 0.0477729129630322
##
                                                                4500
##
                                                                5000
                                                                      min thresh: 0.0477729129630322
##
                                                                5500
                                                                      min thresh: 0.0477729129630322
##
                                                                6000
                                                                      min thresh: 0.0477729129630322
##
                                                                6500
                                                                      min thresh: 0.0477729129630322
                                                                7000
##
                                                                      min thresh: 0.0477729129630322
##
                                                                7500
                                                                      min thresh: 0.0401919383687264
##
                                                                8000
                                                                      min thresh: 0.0319441973901314
##
                                                                8500
                                                                      min thresh: 0.0271607588021149
##
                                                                9000
                                                                      min thresh: 0.0231670821049527
##
                                                                9500
                                                                      min thresh: 0.0231670821049527
##
                                                               10000
                                                                      min thresh: 0.0160246751435115
##
                                                               10500
                                                                      min thresh: 0.0143015470518307
##
                                                               11000
                                                                     min thresh: 0.00978614370100106
                                                                      min thresh: 0.00978614370100106
##
                                                               11500
##
                                                               12000
                                                                      min thresh: 0.00813136952436977
##
                                                               12500
                                                                      min thresh: 0.00670291691221209
##
                                                               13000
                                                                      min thresh: 0.00588460075826878
##
                                                               13500
                                                                      min thresh: 0.00568340157694122
##
                                                               14000
                                                                      min thresh: 0.00431292899953402
##
                                                               14500
                                                                      min thresh: 0.00405437903080155
                                                                      min thresh: 0.00396128911212355
##
                                                               15000
##
                                                               15500
                                                                      min thresh: 0.00308676494427534
##
                                                                      min thresh: 0.00289723264713905
                                                               16000
##
                                                               16500
                                                                      min thresh: 0.00274623242108184
##
                                                                      min thresh: 0.00274623242108184
```

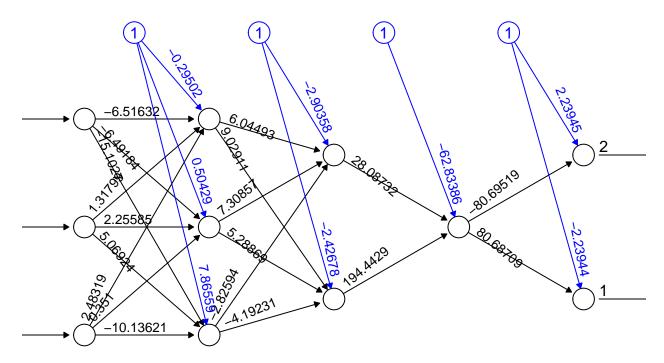
```
#summary(nn)
#print(nn)
plot(nn3, rep='best')
```

##

17000

17163

error: 18.97879 time: 13.78 secs



Error: 18.978788 Steps: 17163

```
##### Prediction on training subset
prediction_nn3 <- predict(nn3,training)
#prediction_nn
class_nn <- apply(prediction_nn3, 1, which.max)</pre>
```

10.1.3.3.2 Confusion Matrix for training

```
table(training$smoker, class_nn)

## class_nn
## 1 2
## 1 197 0
## 2 21 717

#training$smoker[1]
#class_nn[1]
```

10.1.3.3.3 Performance for training

```
levels(training$smoker)[class_nn[1]]

## [1] "2"

corrects=sum(levels(training$smoker)[class_nn]==training$smoker)
errors=sum(levels(training$smoker)[class_nn]!=training$smoker)
(perf.nn=corrects/(corrects+errors))
```

[1] 0.9775

```
print(paste('training accuracy: ',perf.nn*100,"%"))
## [1] "training accuracy: 97.7540106951872 %"
10.1.3.3.4 Prediction on test subset
prediction_nn3 <- predict(nn3,testing)</pre>
#prediction_nn
class_nn <- apply(prediction_nn3, 1, which.max)</pre>
10.1.3.3.5 Confusion Matrix for testing
table(testing$smoker, class_nn)
##
      class_nn
##
         1
##
      76
##
     2
        9 317
#training$smoker[1]
#class_nn[1]
10.1.3.3.6 Performance for testing
levels(testing$smoker)[class_nn[1]]
## [1] "1"
corrects=sum(levels(testing$smoker)[class_nn]==testing$smoker)
errors=sum(levels(testing$smoker)[class_nn]!=testing$smoker)
(perf.nn=corrects/(corrects+errors))
## [1] 0.9752
print(paste('testing accuracy: ',perf.nn*100,"%"))
## [1] "testing accuracy: 97.5186104218362 %"
       Neural Networks using "h20"
10.2.1 Creation NN
set.seed(99)
h2o.init()
   Connection successful!
##
##
## R is connected to the H2O cluster:
                                   2 minutes 36 seconds
##
       H2O cluster uptime:
##
       H20 cluster timezone:
                                   Europe/Berlin
       H2O data parsing timezone: UTC
##
                                   3.30.0.1
##
       H2O cluster version:
##
       H2O cluster version age:
                                   2 months and 5 days
##
       H2O cluster name:
                                   H20_started_from_R_CaroleM_pal554
##
       H2O cluster total nodes:
                                   1.97 GB
##
       H2O cluster total memory:
##
       H2O cluster total cores:
```

```
##
     H2O cluster allowed cores: 4
##
     H2O cluster healthy:
                           TRUF.
##
     H2O Connection ip:
                           localhost
##
     H20 Connection port:
                           54321
     H2O Connection proxy:
##
     H20 Internal Security:
                           FALSE
     H2O API Extensions:
                           Amazon S3, Algos, AutoML, Core V3, TargetEncoder, Core V4
##
     R Version:
                           R version 3.6.1 (2019-07-05)
##
train_hf <- as.h2o(training)</pre>
##
                                                         0%
 |-----| 100%
model_dl <- h2o.deeplearning(x = 2:4, y = 1, training_frame = train_hf, nfolds = 10, seed=545, verbose
##
                                                         0%
                                                      1 32%
## Scoring History for Model DeepLearning model_R_1591727398193_67 at 2020-06-09 20:32:52
## [1] "Model Build is 31.970832% done..."
 |-----
## Scoring History for Model DeepLearning_model_R_1591727398193_67 at 2020-06-09 20:32:56
## [1] "Model Build is 48.247933% done..."
 |----
                                                      | 57%
## Scoring History for Model DeepLearning_model_R_1591727398193_67 at 2020-06-09 20:33:01
## [1] "Model Build is 57.18619% done..."
##
 |-----
                                                      1 78%
## Scoring History for Model DeepLearning model_R_1591727398193_67 at 2020-06-09 20:33:02
## [1] "Model Build is 77.661645% done..."
##
 |-----
                                                      I 84%
## Scoring History for Model DeepLearning_model_R_1591727398193_67 at 2020-06-09 20:33:04
## [1] "Model Build is 84.22654% done..."
##
 |-----
                                                     l 91%
## Scoring History for Model DeepLearning_model_R_1591727398193_67 at 2020-06-09 20:33:06
## [1] "Model Build is 90.78367% done..."
##
 |-----| 98%
```

Scoring History for Model DeepLearning_model_R_1591727398193_67 at 2020-06-09 20:33:08

```
## [1] "Model Build is 98.15168% done..."
##
  |-----| 100%
## Scoring History for Model DeepLearning_model_R_1591727398193_67 at 2020-06-09 20:33:09
## [1] "Model Build is 100% done..."
## Scoring History for Model DeepLearning_model_R_1591727398193_67 at 2020-06-09 20:33:10
## [1] "Model Build is 100% done..."
10.2.2 Prediction on training
predicted_h20_deep_neural_network_probabilites_train <- h2o.predict(model_dl, train_hf)</pre>
##
                                                                0%
  |-----| 100%
table( as.data.frame(predicted_h20_deep_neural_network_probabilites_trainspredict))
##
##
    1
       2
## 228 707
predicted_h20_deep_neural_network_class_train <- as.data.frame(predicted_h20_deep_neural_network_probab
10.2.3 Performance on training
table(training$smoker, as.integer(predicted h20 deep neural network class train[,1]))
##
##
        1
           2
##
    1 197
    2 31 707
predicted_h20_deep_neural_network_performance_train <- mean(as.integer(predicted_h20_deep_neural_network
print(paste('training accuracy: ',predicted_h20_deep_neural_network_performance_train,"%"))
## [1] "training accuracy: 96.6844919786096 %"
10.2.4 Prediction on testing
test_hf <- as.h2o(testing)</pre>
##
                                                                0%
  |-----| 100%
predicted_h20_deep_neural_network_probabilites_test <- h2o.predict(model_dl, test_hf)</pre>
##
                                                                0%
```

```
|-----| 100%
table( as.data.frame(predicted_h20_deep_neural_network_probabilites_test$predict))
##
##
    1
        2
   89 314
predicted_h20_deep_neural_network_class_test <- as.data.frame(predicted_h20_deep_neural_network_probabi
10.2.5 Performance on testing
table(testing$smoker, as.integer(predicted_h20_deep_neural_network_class_test[,1]))
##
##
        1
           2
##
       75
           2
    1
    2
      14 312
##
predicted_h20_deep_neural_network_performance_test <- mean(as.integer(predicted_h20_deep_neural_network
print(paste('testing accuracy: ',predicted_h20_deep_neural_network_performance_test,"%"))
```

10.3 Results and method comparison

[1] "testing accuracy: 96.029776674938 %"

Neural Network	Training Performance	Testing Performance
NN	97.11 %	96.28 %
NN2	97.97~%	96.28~%
NN3	97.75~%	97.52~%
h2o	96.68~%	96.52~%

In the above table you can see the last results for all created models which are nearly the same. Based on the sample results, there is no huge difference between using the neuralnet package or the h2o package. Moreover the parameters for the hidden layer were chosen by a trial and error approach. We tried to create different levels for the hidden parameter, to explore if the performance will increase with the given complexity. Since the results are not reflecting this assumption and all performance results are in the same range, all models can be used for an adequate classification, whether a person is a smoker or not.

11 Cross validation and discussion