

# metrica: an R package to evaluate prediction performance of regression and classification point-forecast models

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## Summary



The *metrica* R package (Correndo et al., 2022) is an open-source software designed to facilitate the quantitative and visual assessment of prediction performance of point-forecast simulation models for continuous (regression) and categorical variables (classification). The package ensembles a series of 80+ functions that account for multiple aspects of the agreement between predicted and observed values. Without the need of advanced skills on programming, *metrica* enables users to automate the estimation of multiple prediction performance metrics including goodness of fit, error metrics, error decomposition, model efficiency, indices of agreement, and to produce stylish data visualization outputs. This article introduces *metrica*, an R package developed with the main objective of contributing to transparent and reproducible evaluation of point-forecast models performance.

## Statement of need

Evaluating the prediction quality is a crucial step for any simulation model, for which a myriad of metrics and visualization techniques have been developed (Tedeschi, 2006; Wallach et al., 2019; Yang et al., 2014). Nonetheless, to conduct a comprehensive assessment of the predicted-observed agreement in R (R Core Team, 2021), users normally have to rely on multiple packages, and even on self-defined functions, which increases the risk of involuntary mistakes due to the need of fluctuating syntax and data wrangling.

As the reproducibility of data analysis continues to be a challenge for science (Seibold, 2022), developing open source software like *metrica* offers a step toward a transparent and reproducible process to assist researchers in evaluating models performance. We decided to create *metrica* in R (R Core Team, 2021) due to its substantial role in data science (Thieme, 2018). Under its open-source philosophy, R empowers the democratization of statistical

33 computing ([Hackenberger, 2020](#)) by hosting and globally distributing cutting-edge algorithms  
34 through the Comprehensive R Archive Network (CRAN).

35 Finally, it is noteworthy that in the area of agricultural sciences, although point-forecast simu-  
36 lation models such as the Agricultural Production Systems sIMulator (APSIM) ([D. Holzworth](#)  
37 [et al., 2018](#); [D. P. Holzworth et al., 2014](#)) count with tools to facilitate the integration into R  
38 through packages such as *apsimx* ([Miguez, 2022](#)), the assessment of its prediction quality is not  
39 yet integrated for R users. Therefore, we aim for *metrica* to offer users of simulation models  
40 for agriculture, plant, and soil sciences community a toolbox for assessing the performance of  
41 regression and classification point-forecast models.

## 42 Package features

43 For regression models, *metrica* includes four plotting functions (scatter, tiles, density, &  
44 Bland-Altman plots) using *ggplot2* ([Wickham, 2016](#)), and 48 prediction performance metrics.  
45 For classification models (two-class or multi-class), it includes one function to visualize a  
46 confusion matrix, and 27 functions of prediction scores. The full list of metrics with description,  
47 formula, and literature sources is presented in the package documentation at:

- 48 ■ Regression metrics: [https://adriancorrendo.github.io/metrica/articles/available\\_metrics\\_regression.html](https://adriancorrendo.github.io/metrica/articles/available_metrics_regression.html).
- 49
- 50 ■ Classification metrics: [https://adriancorrendo.github.io/metrica/articles/available\\_metrics\\_classification.html](https://adriancorrendo.github.io/metrica/articles/available_metrics_classification.html).
- 51

52 To extent of our knowledge, *metrica* covers several functions not supported, or partially sup-  
53 ported by similar R packages (or components) designed for model evaluation such as *yardstick*  
54 ([Kuhn & Vaughan, 2022](#)) from *tidymodels* ([Kuhn & Wickham, 2020](#)), the measuring perfor-  
55 mance components from *caret* ([Kuhn, 2022](#)) or *mlr3* ([Lang et al., 2019](#)), *Metrics* ([Hamner](#)  
56 [& Frasco, 2018](#)), *hydroGOF* ([Zambrano-Bigiarini, 2020](#)), *cvms* ([Olsen & Zachariae, 2021](#)),  
57 *scoringutils* ([Bosse et al., 2020](#)), or *performance* ([Lüdecke et al., 2021](#)). Unique features  
58 include:

- 59 ■ the most extensive collection of prediction performance metrics for regression and  
60 classification models up to date.
- 61 ■ working under both vectorized (calling variables with `$`) or tabulated forms ([Wickham et](#)  
62 [al., 2019](#)).
- 63 ■ controlling the output format as a list (`tidy = FALSE`) or as a table (`tidy = TRUE`).
- 64 ■ for classification, functions automatically recognizing two-class or multi-class data; and  
65 specifically for multi-class cases, several metrics can be estimated for each class (`atom`  
66 `= TRUE`) ([Ferri et al., 2009](#)), ([Ben-David, 2007](#)), including balanced and imbalanced  
67 scenarios ([Kubat et al., 1997](#)).
- 68 ■ for regression, implementing a symmetric linear regression (standardized major axis-SMA-,  
69 ([Warton et al., 2006](#))) to describe: i) pattern of the bivariate relationship with linear  
70 parameters (`B0_sma`, `B1_sma`), and ii) degree of predicted-observed agreement by using  
71 SMA-line to decompose the mean-squared-error (MSE) into lack of accuracy (MLA, PLA,  
72 RMLA) and lack of precision (MLP, PLP, RMLP) components ([Correndo et al., 2021](#)).
- 73 ■ offering MSE decomposition approaches described by ([Kobayashi & Salam, 2000](#)) (SB,  
74 SDS, LCS), and ([Smith & Rose, 1995](#)) (`Ub`, `Uc`, `Ue`).
- 75 ■ including multiple indices of agreement and model efficiency such as: i) index of agreement  
76 `d` ([Willmott, 1981](#)), and its modified `d1` ([Willmott et al., 1985](#)) and refined `d1r` ([Willmott](#)  
77 [et al., 2012](#)) variants, ii) Nash–Sutcliffe model efficiency (NSE) ([Nash & Sutcliffe, 1970](#))  
78 and its improved variants `E1` ([Legates & McCabe Jr., 1999](#)), `Erel` ([Krause et al., 2005](#)),

79 and Kling-Gupta model efficiency (KGE) (Kling et al., 2012), iii) Robinson's index of  
 80 agreement (RAC) (Robinson, 1957, 1959), iv) Ji & Gallo agreement coefficient (AC) (Ji  
 81 & Gallo, 2006), v) Duvellier's Lambda (Duvellier & Meroni, 2016), vi) distance correlation  
 82 (dcorr) (Székely et al., 2007), or vii) maximal information coefficient (MIC) (Reshef et  
 83 al., 2011)), among others.

- 84 ■ importing files from APSIM Classic with `import_apsim_out()`, and from APSIM Next  
 85 Generation with the `import_apsim_db()` function.

## 86 System requirements and installation

87 Since *metrica* operates within R, the first step is to install R ( $\geq 4.2.0$ ). To install and load  
 88 the package:

```
# Stable version (CRAN)
install.packages("metrica")

# Development version (GitHub)
devtools::install_github("adriancorrendo/metrica")

# Load
library(metrica)
```

## 89 Using the functions

90 There are two core arguments to all *metrica* functions: (i) `obs` ( $O_i$ ; observed, a.k.a. actual,  
 91 measured, truth, target, label), and (ii) `pred` ( $P_i$ ; predicted, a.k.a. simulated, fitted, modeled,  
 92 estimate) values. For regression, specific functions require defining the axis orientation (e.g.  
 93 predicted vs. observed -PO- or observed vs. predicted -OP-).

94 For two-class models, the `pos_level` argument serves to indicate the alphanumeric order of the  
 95 "positive level". Following most two-class denominations as `c(0,1)`, `c("Negative", "Positive")`,  
 96 and `c("FALSE", "TRUE")`, the default `pos_level = 2` (1, "Positive", "TRUE"). However,  
 97 we recognize other cases as possible (e.g. `c("Crop", "NoCrop")`), for which the user needs  
 98 to specify `pos_level = 1`. For multi-class classification, some functions present the `atom`  
 99 argument (TRUE / FALSE), which controls the output to be an overall average estimate  
 100 across all classes (default), or class-wise.

## 101 Example 1: Regression (continuous variables)

102 The following lines of code serve to run basic regression performance analysis using a native  
 103 dataset called `wheat`.

```
# Define dataset
data_wheat <- metrica::wheat

# Estimate Root Mean Square Error, result as a list
RMSE(data = data_wheat, obs = obs, pred = pred, tidy = FALSE)
#> $RMSE
#> [1] 1.666441

# Store results as a data frame
RMSE(data = data_wheat, obs = obs, pred = pred, tidy = TRUE)

#>      Metric      Score
#> 1      RMSE      1.6664412
```

104 To estimate multiple regression metrics at once using `metrica::metrics_summary()`:

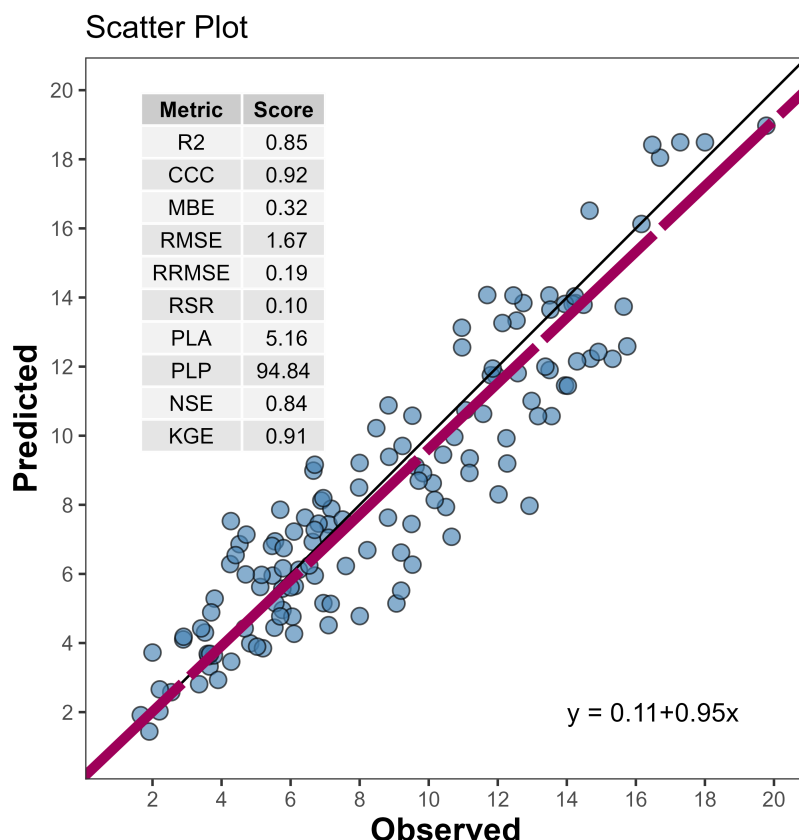
```
# Define metrics list
my_reg_metrics <- c("R2", "CCC", "MBE", "RMSE", "RSR", "NSE", "KGE")
```

```
# Run metrics summary
metrics_summary(data = data_wheat,
  obs = obs, pred = pred,
  type = "regression",
  metrics_list = my_reg_metrics)
```

```
#>      Metric      Score
#> 1      R2      0.84555376
#> 2     CCC      0.91553253
#> 3     MBE      0.31815953
#> 4     RMSE     1.66644142
#> 5    RRMSE     0.19094834
#> 6     RSR      0.09678632
#> 7     PLP      5.15949064
#> 8     PLA     94.84050936
#> 9     NSE      0.83871126
#> 10    KGE      0.91064709
```

105 To produce a scatter plot of predicted vs. observed values as a customizable ggplot object:

```
scatter_plot(data = data_wheat,
  obs = obs , pred = pred,
  orientation = "PQ",
  print_metrics = TRUE,
  metrics_list = my_reg_metrics,
  print_eq = TRUE,
  position_eq = c(x=14, y = 2),
  # Optional arguments to customize the plot
  shape_type = 21,
  shape_color = "steelblue",
  shape_size = 3,
  regline_type = "F1",
  regline_color = "#9e0059",
  regline_size = 2)+
  # Customize axis breaks
  scale_y_continuous(breaks = seq(0,20, by = 2))+
  scale_x_continuous(breaks = seq(0,20, by = 2))
```



**Figure 1:** Predicted vs. Observed scatter plot using `metrica::scatter_plot()`.

#### 106 **Example 2: Classification (categorical variables)**

107 The following lines of code serve to run a basic classification performance analysis using a  
108 native dataset called `maize_phenology`.

```
# Define dataset
data_multiclass <- metrica::maize_phenology

# Estimate accuracy, result as a list
accuracy(data = data_multiclass, obs = actual, pred = predicted, tidy = FALSE)

#> $accuracy
#> [1] 0.8834951

# Result as a data frame
accuracy(data = data_multiclass, obs = actual, pred = predicted, tidy = TRUE)

#>      Metric      Score
#> 1    accuracy 0.8834951

# Define selected metrics
my_class_metrics <- c("accuracy", "precision", "recall", "specificity",
                      "fscore", "gmean", "khat")

# Run the summary for selected metrics
metrics_summary(data = data_multiclass,
```

```
obs = actual, pred = predicted,  
type = "classification")
```

```
#>      Metric      Score  
#> 1  accuracy 8.834951e-01  
#> 2  precision 8.335108e-01  
#> 3   recall 8.405168e-01  
#> 4 specificity 9.915764e-01  
#> 5   fscore 8.369991e-01  
#> 6    agf 8.370017e-01  
#> 7   gmean 9.129275e-01  
#> 8    khat 8.624527e-01
```

109 To produce a confusion matrix plot users may use:

```
confusion_matrix(data = data_multiclass,  
  obs = actual, pred = predicted,  
  plot = TRUE,  
  colors = c(low="grey85" , high="steelblue"),  
  unit = "count",  
  # Print metrics_summary  
  print_metrics = TRUE,  
  # List of performance metrics  
  metrics_list = my_class_metrics,  
  # Position (bottom or top)  
  position_metrics = "bottom")
```

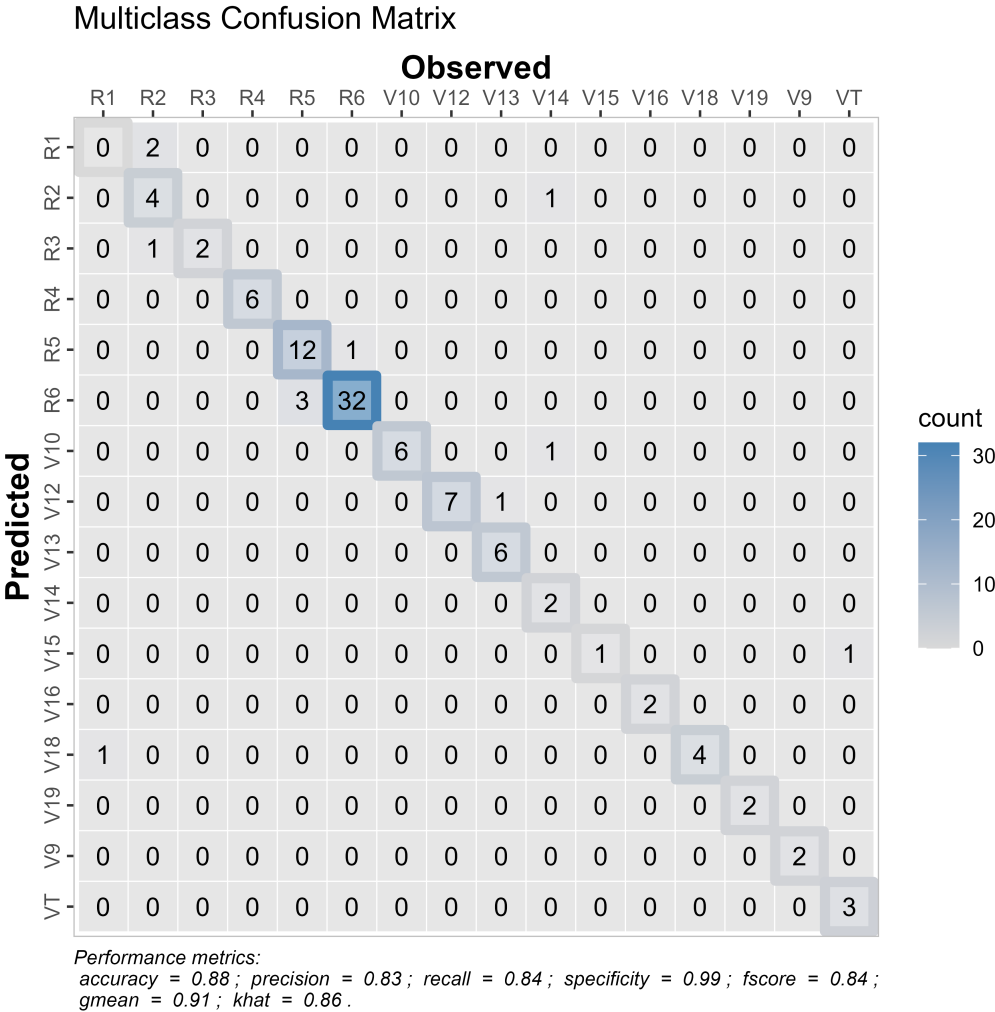


Figure 2: Confusion matrix plot using `metrica::confusion_matrix()`.

## Documentation & License

The complete documentation and vignettes of the package can be found online at <https://adriancorrendo.github.io/metrica/>. *metrica* is under the MIT License (<https://opensource.org/licenses/MIT>). Source code is available at GitHub (<https://github.com/adriancorrendo/metrica>) along with its corresponding section to report issues and suggestions (<https://github.com/adriancorrendo/metrica/issues>).

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