UNIVERSITY OF OSLO



IN4310/3310 Vision Transformers

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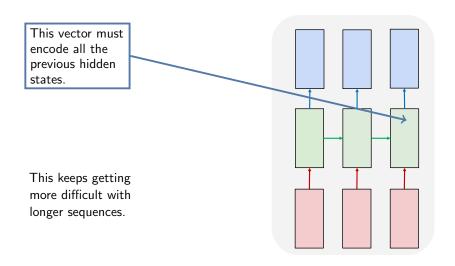
Outline

- 1. Attention mechanism
- 2. Self-attention
- 3. Multi-head self-attention
- 4. Transformer encoder block
- 5. Transformer decoder block
- 6. Vision transformer (ViT)
- 7. Swin transformer
- 8. DEtection TRansformer (DETR) for object detection
- 9. Suggested resources

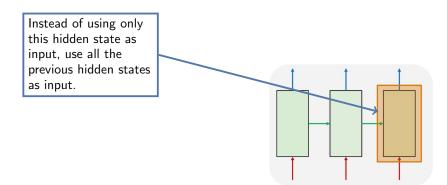
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RNNs suffer from a bottleneck problem



Idea: Use all previous hidden states

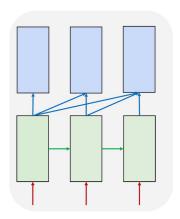


Idea: Use all previous hidden states

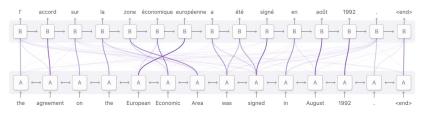
Naïve method: Connect the output layer to all previous hidden states.

It has at least three problems:

- Additional parameters: Adding connections to k hidden states instead of just one will increase the parameter count k-times for the layer.
- Fixed length: Since the parameters of a network are fixed, we can process hidden states only up to a certain length.
- Training long sequences: If the sequence length in the training data varies, some parameters might receive an insufficient amount of gradient updates to learn something useful.



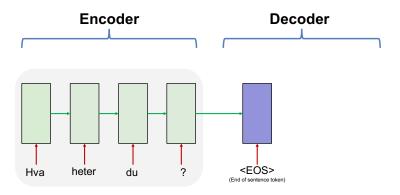
- When people say "attention mechanism", they usually refer to either the attention mechanism proposed by Bahdanau et al. for Neural Machine Translation (NMT) or one of its derived forms.
- Basic intuition: use all the hidden states of the input sentence but focus more on the relevant ones.



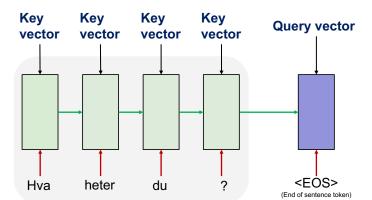
Source: Olah & Carter, "Attention and Augmented Recurrent Neural Networks", Distill, 2016. http://doi.org/10.23915/distill.00001

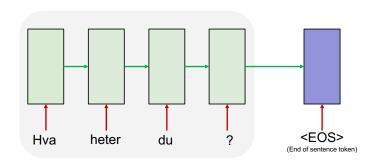
Diagram derived from Fig. 3 of Bahdanau et al. 2014

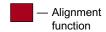
- We will look at attention mechanism via Neural Machine Translation (NMT), i.e., translating text from a source language to a target language using neural networks.
- NMT typically uses an encoder-decoder architecture.
- The decoder makes use of the attention mechanism.

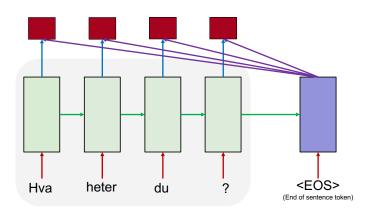


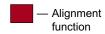
- The input to the attention mechanism is a single query vector and multiple key vectors. Additionally, we can also have value vectors.
- Each query-key pair gets a score that determines how much attention each key vector (or the value vector if present) will get.
- We will use the encoder's hidden states as both key and value vectors.

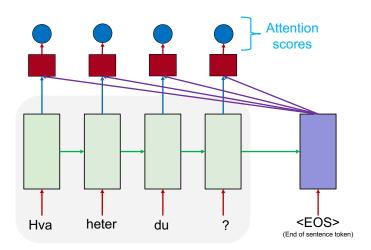


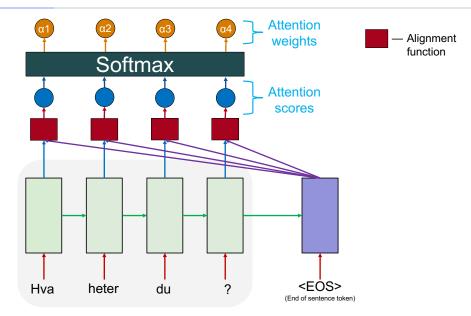


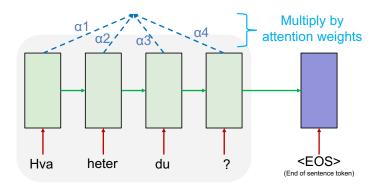


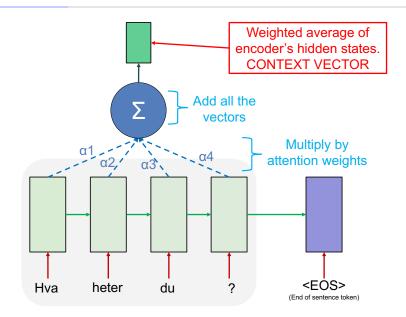


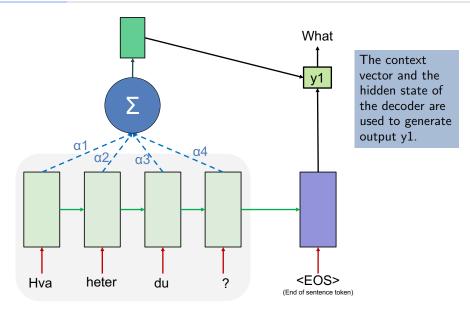


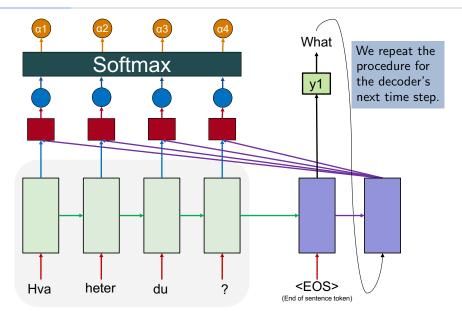


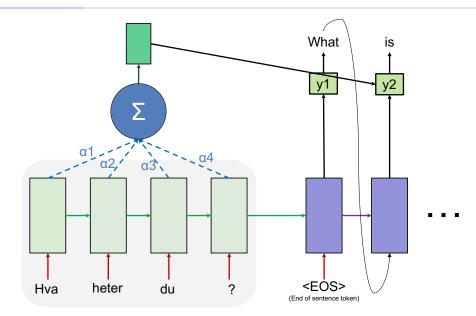












Attention mechanism: alignment function

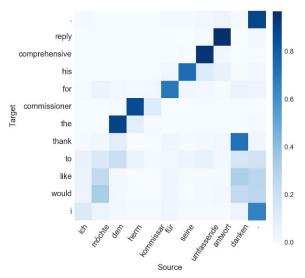
- Alignment function takes a query (q) and a key (k) vector as input and outputs a score for the query-key pair.
- Popular alignment functions:
 - Additive/concat attention: $a(q,k) = v^T \tanh(W_a\left[q;k\right])$ Bahdanau et al. 2014
 - \blacksquare General attention: $a(q,k) = q^T W_a k$ Luong et al. 2015
 - \blacksquare Dot-product attention: $a(q,k)=q^Tk$ Luong et al. 2015
 - Scaled dot-product attention: $a(q,k) = \frac{q^T k}{\sqrt{d_k}} \text{ where } d_k = length \, of \, k \, \text{Vaswani et al. 2017}$
- Transformers use scaled dot-product attention in self-attention.

- The attention mechanism solves the bottleneck problem.
 - The encoder doesn't need to store all the information in the last hidden state, as the decoder now looks directly at all the hidden states.
- The attention mechanism helps with the vanishing gradient problem.
 - Gradients can now be transferred directly from the decoder to all the time steps in the encoder.
- The attention mechanism provides some interpretability.
 - By looking at the attention weights, we can determine what the decoder focused on.

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Attention mechanism: interpretability example



Source: Ghader, Hamidreza, and Christof Monz. "What does Attention in Neural Machine Translation Pay Attention to?" Proceedings of the Eighth International Joint Conference on Natural Language Processing (Volume 1: Long Papers). 2017.

Attention mechanism: interpretability example



Source: Xu, Kelvin, et al. "Show, Attend and Tell: Neural Image Caption Generation with Visual Attention." arXiv preprint arXiv:1502.03044 (2015).

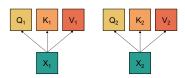
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Self-Attention: Step 1: Compute Query, Key, Value vectors

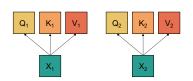
- In step 1, each input vector Xi is multiplied with 3 different matrices to get query, key, and value vectors.
- You can imagine this as having 3 torch.nn.Linear layers:

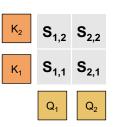
 - $Q = L_{Q}(X) K = L_{Q}(X) V = L_{Q}(X)$
- Query, key, and value vectors typically have the same dimensions.



Self-Attention: Step 2a: Compute score

- Apply scaled dot product attention using query and key vectors to get scores for each pair.
- Each Ki, Qi pair generates a score.
 - $S_{1,1} = dot_product(Q_1, K_1)$ $S_{1,2} = dot_product(Q_1, K_2)$
 - $\hspace{0.5cm} \hspace{0.5cm} \mathbb{S}_{2,1} = \mathtt{dot_product}(\mathbb{Q}_2,\mathbb{K}_1) \qquad \mathbb{S}_{2,2} = \mathtt{dot_product}(\mathbb{Q}_2,\mathbb{K}_2)$
- Each score is divided by the square root of the dimension of the key vector.
 - $S_{i,j} = S_{i,j} / \sqrt{\text{dimension of } K_i \text{ vectors}}$
 - This is done to stabilise gradients during backpropagation.

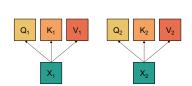


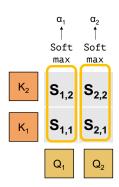


Self-Attention: Step 2b: Compute softmax score

- Next, scores corresponding to each query vector are passed through a softmax layer to get softmax scores.

 - $\qquad \alpha_2 = \mathtt{Softmax}(\mathtt{S}_{2,1},\mathtt{S}_{2,2})$



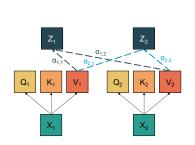


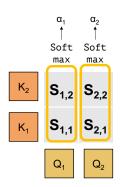
Self-Attention: Step 2b: Compute softmax score

 For every Xi, compute the weighted average of the value vectors using the softmax scores (corresponding to Xi) as weights.

$$Z_1 = (\alpha_{1,1} * V_1) + (\alpha_{1,2} * V_2)$$

$$\blacksquare \ \mathtt{Z_2} = (\alpha_{\mathtt{2,1}} * \mathtt{V_2}) + (\alpha_{\mathtt{2,2}} * \mathtt{V_2})$$





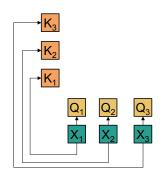




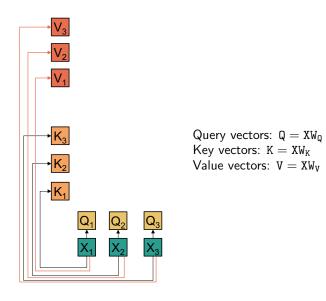


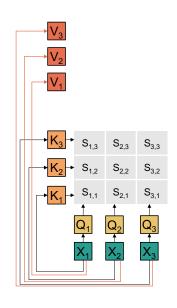
Query vectors:
$$\mathbf{Q} = \mathbf{X} \mathbf{W}_{\mathbf{Q}}$$



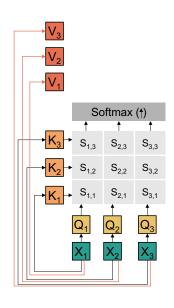


Query vectors: $Q = XW_Q$ Key vectors: $K = XW_K$

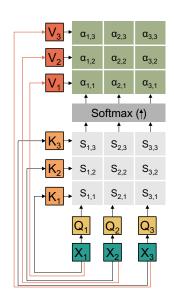




 $\begin{array}{l} \text{Query vectors: } \mathbb{Q} = \mathtt{XW}_{\mathbb{Q}} \\ \text{Key vectors: } \mathbb{K} = \mathtt{XW}_{\mathbb{K}} \\ \text{Value vectors: } \mathbb{V} = \mathtt{XW}_{\mathbb{V}} \\ \text{Scores: } \mathbb{S}_{\mathtt{i},\mathtt{j}} = \mathbb{Q}_{\mathtt{i}} \cdot \mathbb{K}_{\mathtt{j}}/\sqrt{\mathtt{D}} \\ \end{array}$

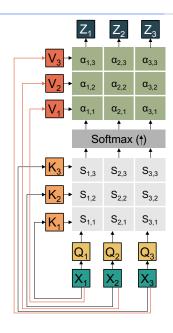


 $\begin{array}{ll} \text{Query vectors: } \mathbb{Q} = X \mathbb{W}_{\mathbb{Q}} \\ \text{Key vectors: } \mathbb{K} = X \mathbb{W}_{\mathbb{K}} \\ \text{Value vectors: } \mathbb{V} = X \mathbb{W}_{\mathbb{V}} \\ \text{Scores: } \mathbb{S}_{\mathrm{i},\mathrm{j}} = \mathbb{Q}_{\mathrm{i}} \cdot \mathbb{K}_{\mathrm{j}} / \sqrt{D} \\ \end{array}$



Query vectors: $\mathbb{Q} = XW_{\mathbb{Q}}$ Key vectors: $K = XW_{K}$ Value vectors: $V = XW_{V}$ Scores: $S_{i,j} = \mathbb{Q}_{i} \cdot K_{j}/\sqrt{D}$

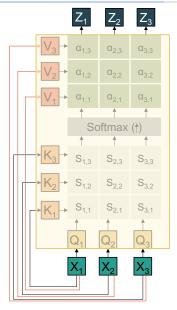
Self-Attention: Overview



$$\begin{split} \mathbf{Z}_1 &= (\alpha_{1,1} * \mathbf{V}_1) + (\alpha_{1,2} * \mathbf{V}_2) + (\alpha_{1,3} * \mathbf{V}_3)) \\ \mathbf{Z}_2 &= (\alpha_{2,1} * \mathbf{V}_1) + (\alpha_{2,2} * \mathbf{V}_2) + (\alpha_{2,3} * \mathbf{V}_3)) \\ \mathbf{Z}_3 &= (\alpha_{3,1} * \mathbf{V}_1) + (\alpha_{3,2} * \mathbf{V}_2) + (\alpha_{3,3} * \mathbf{V}_3)) \end{split}$$

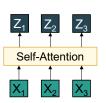
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Self-Attention: Overview

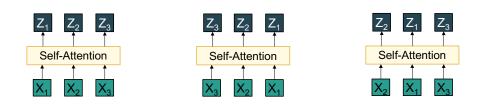


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Query vectors: $Q = XW_Q$ Key vectors: $K = XW_K$ Value vectors: $V = XW_V$ Scores: $S_{i,j} = Q_i \cdot K_j / \sqrt{D}$



Self-Attention: Permutation equivariance

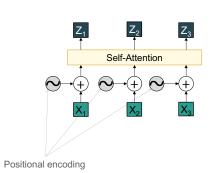


- Self-attention layer is permutation equivariant.
- Self-attention layer doesn't care about the order of the input sequence.

Problem: How to encode the order of input sequence when it matters, like in language or images?

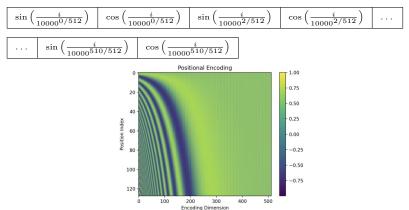
Positional encoding

- There are multiple ways of encoding position:
 - Absolute/fixed positional encoding.
 - Relative positional encoding.
 - A hybrid of relative and absolute positional encoding.
 - Learned positional encoding.
 - etc.
- Positional encodings are vectors with the same dimension as the input vectors.
- Positional encodings are usually added to the input vectors.

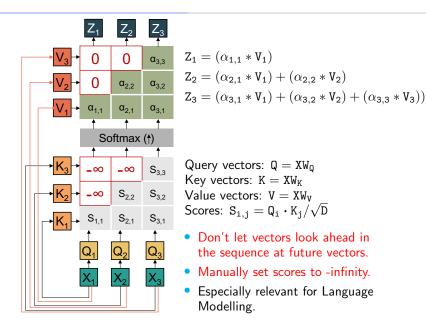


Positional encoding: Absolute positional encoding

- Absolute positional encoding at position **pos** for dimension i = 0...(d/2 1):
 - $PE(pos, 2i) = \sin(pos/10000^{2i/d})$
 - $PE(pos, 2i + 1) = \cos(pos/10000^{2i/d})$
- A 512-dimensional encoding for i in the sequence:



Self-Attention: Overview



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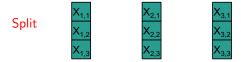
- Use H independent "attention heads" in parallel.
 - Attention heads do NOT share parameters.
- Each Input embedding is split into H parts.
- Each part is then processed by an attention head.

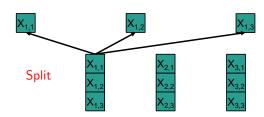


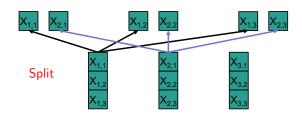


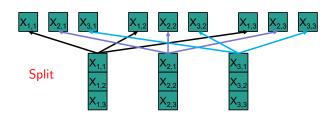




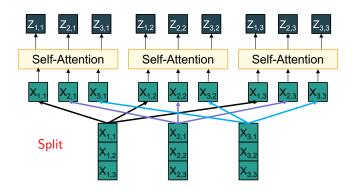


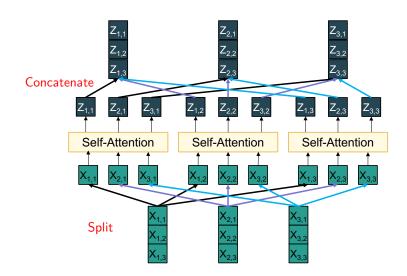


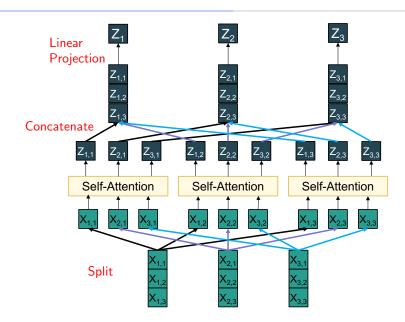




Run self-attention in parallel on each set of input vectors using a different set of parameters for each self-attention head.

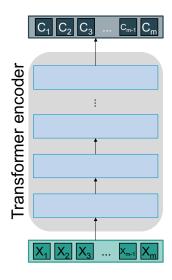




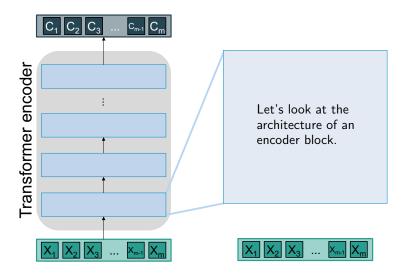


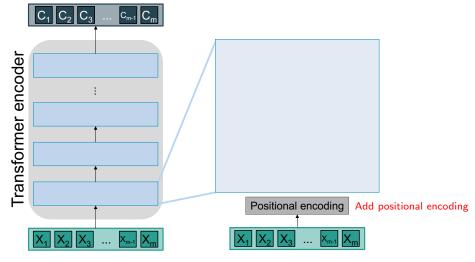
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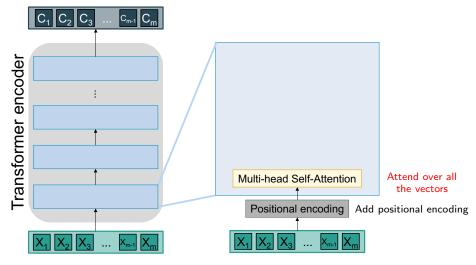
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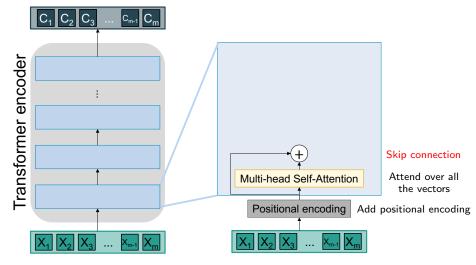


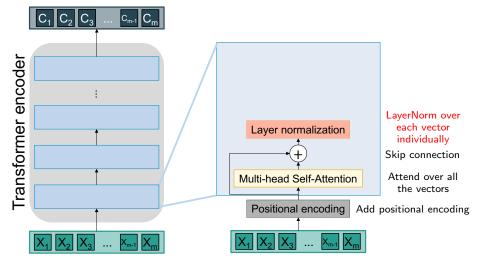
Transformer encoder is made up of a series of N encoder blocks. In the original model (Vaswani et al.) N=6

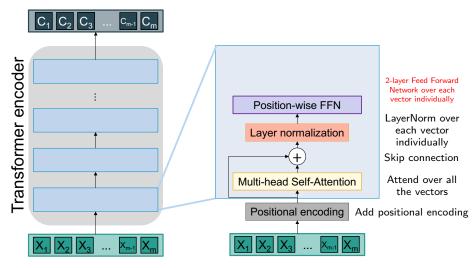


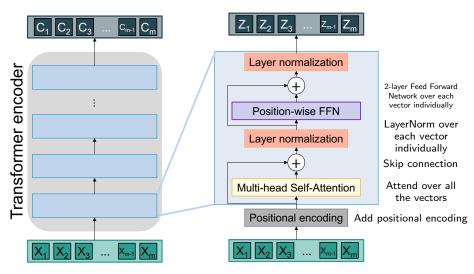


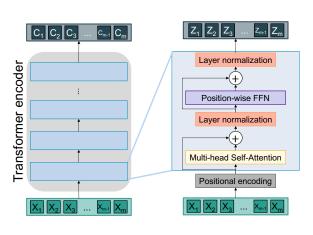












Input: Set of vectors XOutput: Set of vectors Z

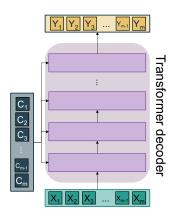
Self-attention is the only interaction between vectors.

LayerNorm and FFN operate independently per vector.

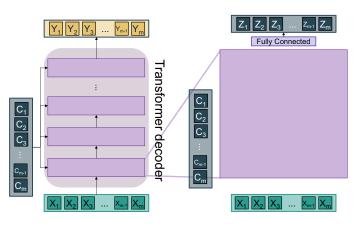
Highly parallelisable but has high memory usage.

Outline

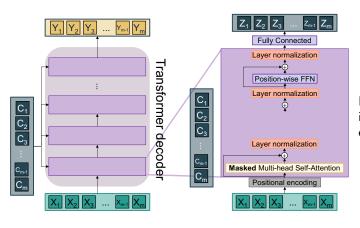
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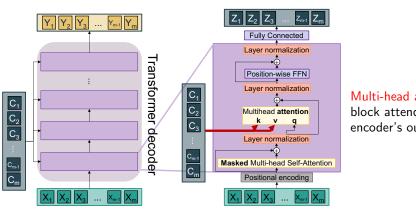
Transformer decoder is made up of a series of N decoder blocks. In the original model (Vaswani et al.) N=6



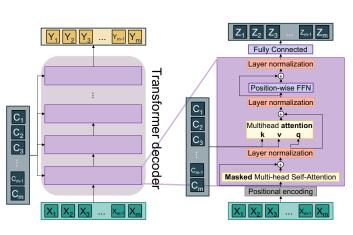
Let's look at the architecture of a decoder block.



Most of the block is the same as the encoder block.



Multi-head attention block attends over encoder's outputs.



Transformer Decoder Block:

Input: Set of vectors X and set of context vectors C

Output: Set of

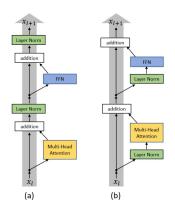
vectors ${\sf Z}$

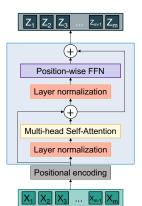
Masked Self-attention interacts only with past inputs.

Multi-head attention is NOT self-attention. It attends over the encoder's outputs.

Highly parallelisable but has high memory usage.

Transformer block: Pre-Norm Transformer





Pre-Norm Transformer:

Layer normalization is inside residual (skip) connections.

Gives more stable training.

(a) Post-norm transformer (b) Pre-norm transformer.

Image Source: https://arxiv.org/pdf/2002.04745.pdf

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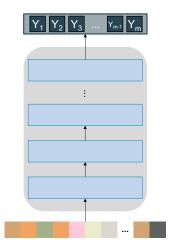
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- 7. Swin transformer
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- 9. Suggested resources

How to use transformers for images?

Idea: Treat an image as a sequence of pixels and use the standard transformer



Flatten and feed as input



How to use transformers for images?

Problem: Memory usage!

 $N \times N$ image has N^2 pixels (sequence length).

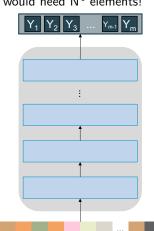
Self-attention is an $O(N^2)$ operation.

Therefore, self-attention would need N⁴ elements!

Idea: Treat an image as a sequence of pixels and use the standard transformer



Flatten and feed as input



Idea: Use standard transformer on patches



Photo by Josh Hild on Unsplash

Idea: Use standard transformer on patches



Photo by Josh Hild on Unsplash

N input patches, each of shape $3\times16\times16$











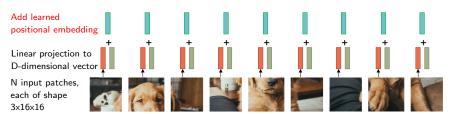


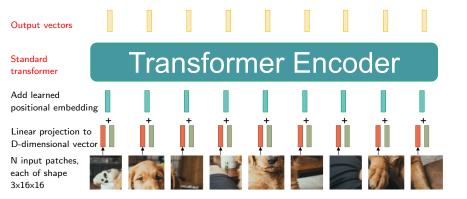


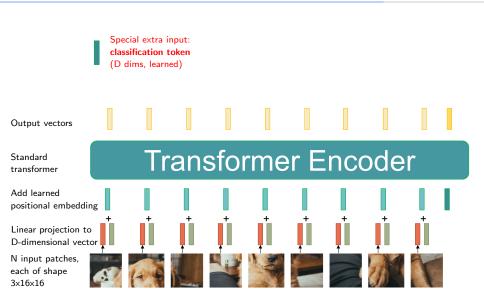


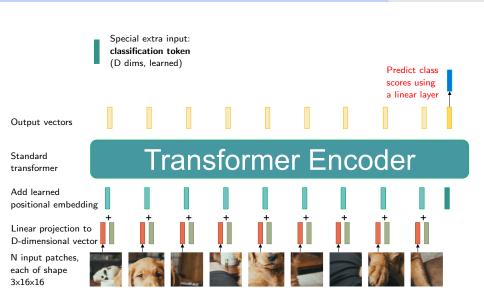








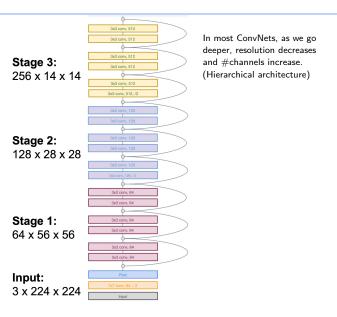




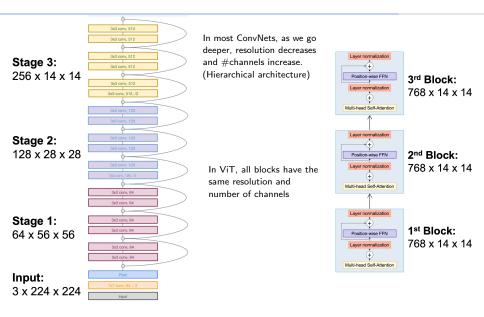
Outline

- Attention mechanism
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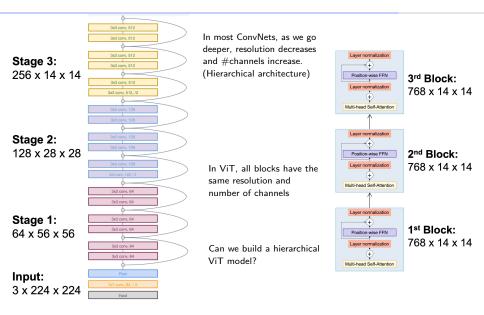
ViT vs ConvNet

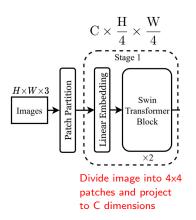


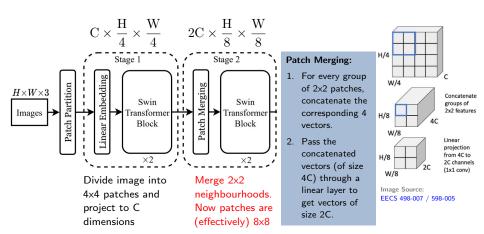
ViT vs ConvNet

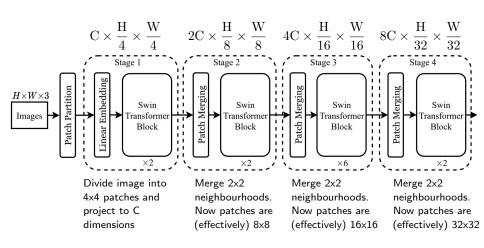


ViT vs ConvNet



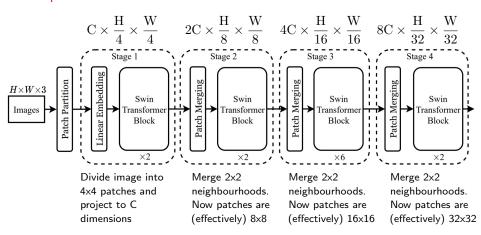






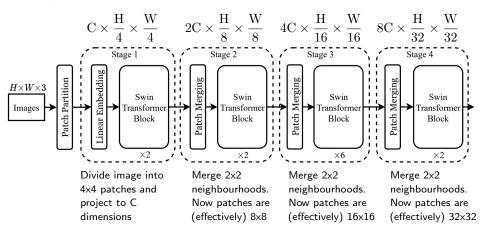
Problem: 224x224 image with 56x56 grid of

4x4 patches \Rightarrow attention matrix has $56^4 = 9.8$ M elements



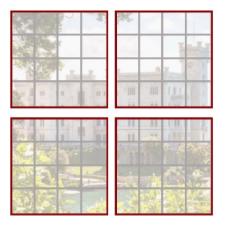
Problem: 224x224 image with 56x56 grid of

4x4 patches \Rightarrow attention matrix has $56^4 = 9.8M$ elements



Solution: Limit the attention of a patch to its "window".

Swin Transformer: Window Attention



Instead of allowing each token to attend to all other tokens, divide the image into $M \times M$ windows (here M=4).

Compute attention only within each window.

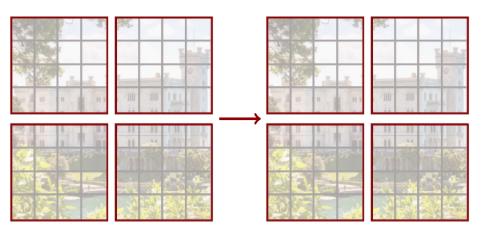


____ A

A patch

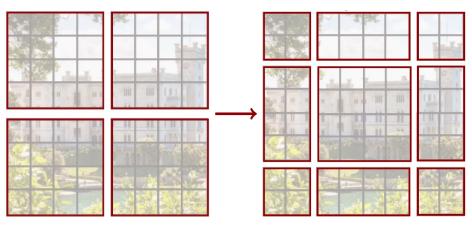
Swin Transformer: Window Attention

Problem: No communication across windows. Global context?



Swin Transformer: Window Attention

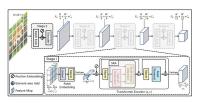
Solution: Alternate between normal windows and shifted windows in successive Transformer blocks.



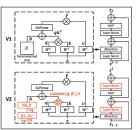
Block I: Normal windows

Block L+1: Shifted windows

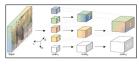
Other hierarchical vision transformers



Wang, Wenhai, et al. "Pyramid vision transformer: A versatile backbone for dense prediction without convolutions.". ICCV 2021



Liu, Ze, et al. "Swin transformer v2: Scaling up capacity and resolution.", arXiv 2021, CVPR 2022

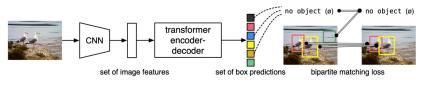


Fan ,Haoqi, et al. "Multiscale vision transformers.", ICCV 2021

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- Simple object detection pipeline: directly output a set of boxes from a Transformer.
- Anchor-free approach, i.e., no pre-defined anchors are used.
- No Non-Maximum Suppression (NMS) used. It is learned by the transformer automatically.
- Match predicted boxes to ground truth boxes with bipartite matching.

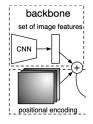


Carion et al, "End-to-End Object Detection with Transformers", ECCV 2020



A backbone ConvNet (like ResNet50) is used to extract features from the input.

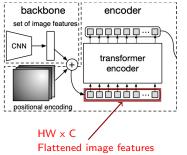
1x1 conv layer is used to reduce the number of channels.



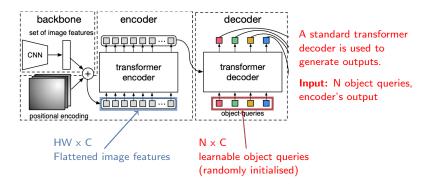
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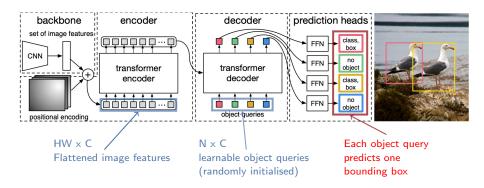
1x1 conv layer is used to reduce the number of channels.

Fixed positional encodings are added to every encoder block's input



Standard transformer encoder is used to process the flattened image features.





Is self-attention magical and absolutely necessary?

- A lot of works have explored replacing self-attention with X, and some of them achieve competitive results.
 - Wu et al. replace self-attention with convolution.
 - Tay et al. replace alignment scores in self-attention with random projection.
 - Tolstikhin et al. replace self-attention with an MLP-mixer, making the architecture exclusively based on MLPs.
 - Lee-Thorp et al. replace self-attention with Fourier Transforms.
 - Tatsunami and Taki replace self-attention with LSTM.
- But, self-attention continues to be the standard choice.

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Suggested resources

- The Illustrated Transformer: A famous blog post covering the basics of Transformers.
- The Annotated Transformer: A blog post that implements Transformer line by line with explanation.