TECSDIO MAS

Lecture 12: Bargaining

Exercise: Bargaining 1

Quertion 1

a) What would be a sniteable protocol for bargaining in this case? Spesify the needed requirements.

We have to reallocate resources among agents in order to increase in 'nd Cenefit.

Protocol for resource Mocation

5 2° is défined as current allocation

2 truy ayent can propose a new allocation

Where & is current allocation

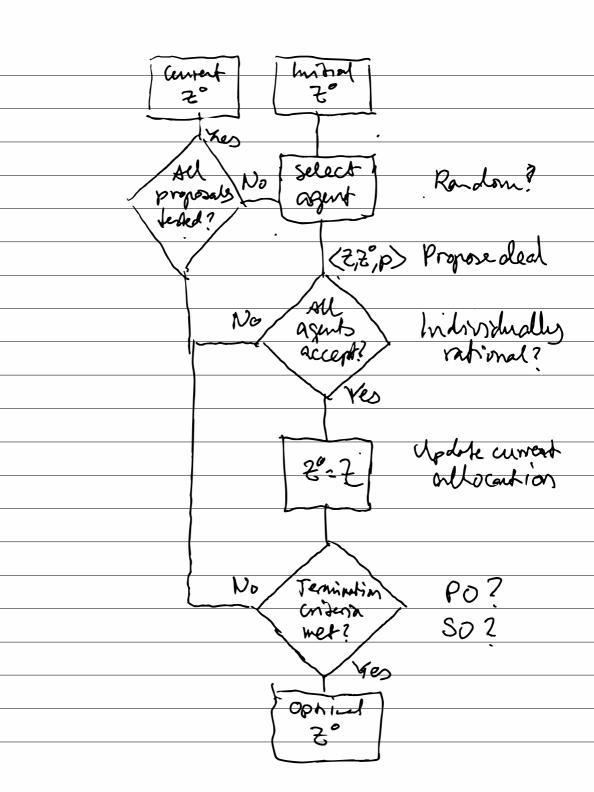
7 is proposed allocation

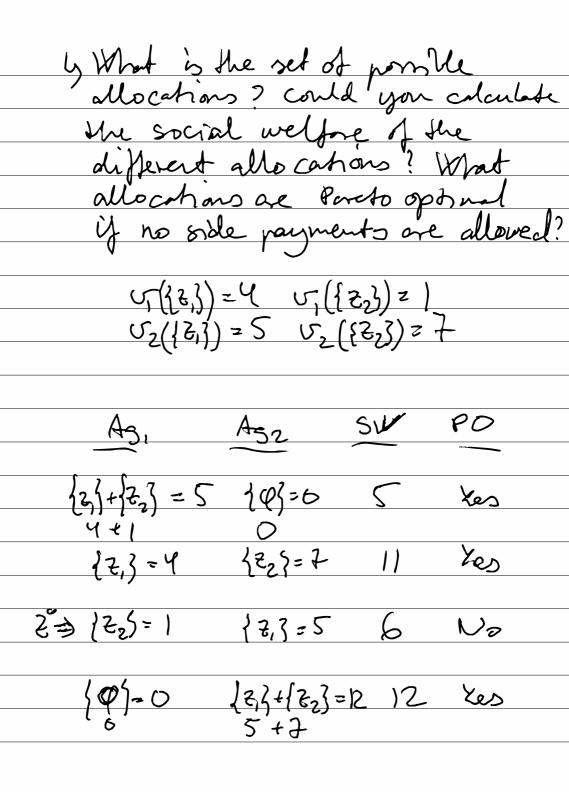
p is sollepayments

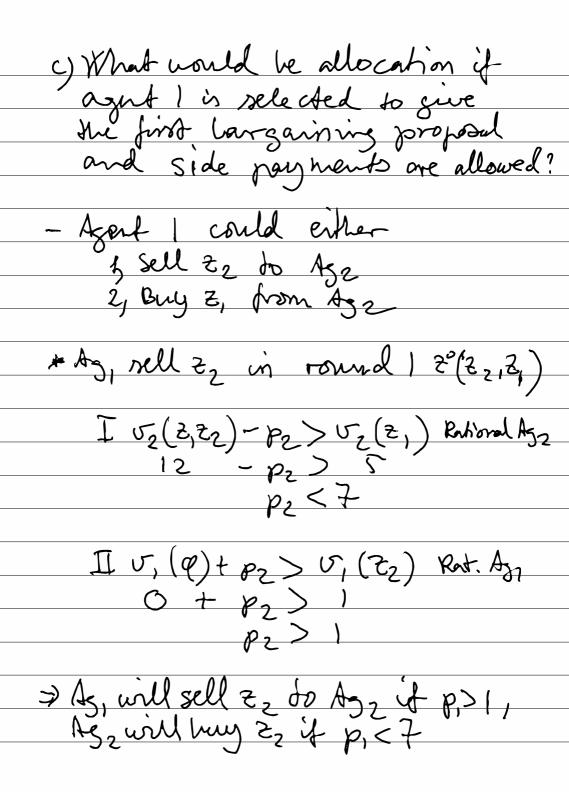
3, If this deal is a) Accepted by all eyes and by Termination criteria is met then Z is implemented with p side payments 4,1fthis deal is by Bit termination enteria is not met When Zig uplemented with orde pergenent and regolation continue with next agent performing 5) If this deal is or not accepted by all agus then 2° = 2° and regolishions continue with rest agent 6, If all rational proposals have heln rejected current zo is implemented

Requirements: 1 Individual rationality I v;(2)-p; > v;(2°) buyer \overline{L} $U_i^*(\overline{z}) + p_i^* > U_i^*(\overline{z}^*)$ seller Z Pi=0 2, Termination enteria Pareto optimelity or Social gotimen PO is grannfæd if all doals are individually rational In one-contracts 50 is reachable but not guaranteed

PO is NP-hard to calculate







#Ag, huy z, from Ag 2 in round 1

I $S_1(z_1z_2)-p_1 > S_1(z_2)$ Ratified Ag, $S_1 = p_1 < Y$ If $S_2(q)+p_1 > S_2(z_1)$ Ratified Ag 2

O $S_1 = S_2(z_1)$ Ratified Ag 2

 $p_{1} > 5$

3) Not possible for As, to buy 8, from Asz in round!

Ag, will propose a deal to sell of to Ag, for a side payment of p2 < 7

Ag = 1 Q3 + p2 = 0+7 = 7 Ag 2 = 12,3+5723-p2 = 12-7 = 5 This is PO and So allocation
So bargaining Emps.

Lets check if thre:..

- As 2 is selected round 2

3 sell 2,

2, sell 22

* Azz sell Z,

I $\sigma_1(z_1)-\rho_1>\sigma_1(\varrho)$ Rutismal Ag, $\gamma=\rho_1>0$ $\gamma=0$ $\gamma=0$

p, > 5

DNA possible to sell 2,

* Asz sells zz I v, (2)-p, > v, (Q) Ratinel As, $p_j < 1$ IT $V_2(2,)+p_1>V_2(2,2_2)$ Radinal Age

5 + p, > 12 p, > 7=) Impossible to sell =z What if to, in round I does not know the valuation furction of agent 2? Az, then proposes to sell Ez to Azz for pz>1 Allocation is the same of goods but different net whility of agents

Ag = 10(+p2 = 0 +1= | Ag = 12, 1+122-p2 = 12-1=11 - Agz is selected round 2 1, sell & 2 sell Z, * Az rells 3, 10 Az, I $\sigma_1(z_1) - p_2 > \sigma_1(Q)$ rational A_{21} If $\sigma_2(z_1) + p_2 > \sigma_2(z_1, z_2)$ ratinal A_{22} Some as before? * Az sells z to Az, I v₂(2₁) + p, > v₂(2, 7₂) rational A₃,

II v₂(2₁) + p, > v₂(2, 7₂) rational A₃,

Same as before?

d, What would be allocation if agus 2 is selected for first proposal in Blead? - Az could a Mer 1 sell 2, to Az 2 huy 22 from Az, * Ag rell Z, to Ag, in round 1 $T_{s}(3,2)-p_{s}>5(2)$ Radional Ag, $5-p_{s}>1$ p, < 4 $\frac{\prod \sigma_2(Q) + p > \sigma_2(2)}{\sigma_1 + \rho_1 > \sigma_2(2)}$ Rational Aze p, > 5Dupori Me to sell z, to Az,

 $I_{\nu_1(\varrho)+p_2}>V_{\nu_1(z_2)}$ Reliand Ag₁ $O_{\nu_1}>V_{\nu_2}>V_{\nu_3}$ p2>1 IT $v_2(z,z_1)-p_2>v_2(z_1)$ Refined As 2 12 - $p_2>5$ $p_2 \in 7$ 3 Azz can lung zz fran Az, if porze is between 1 and 7 Agent 2 will propose to buy

= 2 from Az at a side payment

of p2>1, zing allocation $A_{5}, = \{e_1 + p_2 = 0 + 1 = 1$ $A_{52} = \{e_1\} + 3e_3 - p_2 = 12 - 1 = 11$ This is PO and SO, vargain 8hps 1

* Agz huy zz from Agn

e) This is one-contract bargaining with one resource and me side jayment, will dways and up in PO (unt not guaranteed to be SO).

However, when Po is reached net white among agents are dependent on vargarining history. Side payments are surstine to information of other agents valuation function

Side jayments lets us reach PD allocations with higher SW.