Verificación de programas en Elixir Program Verification in Elixir



Trabajo de Fin de Máster Curso 2021–2022

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Dedication

TODO, this is optional

Acknowledgements

TODO

This is optional

Resumen

Verificación de programas en Elixir

TODO

Un resumen en castellano de media página, incluyendo el título en castellano. A continuación, se escribirá una lista de no más de 10 palabras clave.

Palabras clave

Máximo 10 palabras clave separadas por comas

Abstract

Program Verification in Elixir

TODO

An abstract in English, half a page long, including the title in English. Below, a list with no more than 10 keywords.

${\bf Keywords}$

10 keywords max., separated by commas.

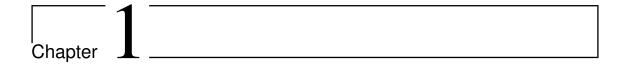
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Introduction

"This is an interesting quote"
— Someone smart

TODO En algun punto explicar la idea general, incluyendo un diagrama

1.1. Motivation

TODO

1.2. Goals

TODO

- Use the Elixir macro system to implement a verification system for Elixir itself.
- To integrate SMT solvers in Elixir and offer a Domain Specific Language (DSL) to specify restriction problems.
- Develop a verification Intermediate Representation (IR) to express Erlang terms and its dynamically typed nature.
- Translate the developed IR into the previous DSL.
- Design a mechanism to translate a subset of the Elixir programming language into the verification IR.

1.3. Non-goals

TODO

- Concurrency.
- Termination (i.e. only partial verification for the moment).

1.4. Work plan

TODO

Describe the work plan to achieve the proposed goals.



State of the Art

TODO

Discuss the state of the Art regarding the topics of this research project. You can cite the appearing references from the bibliography in different ways:

- With cite: Oetiker et al. (1996)
- With citep: (Oetiker et al., 1996)
- With citet: Oetiker et al. (1996)

Multiple cites at the same time (Mittelbach et al., 2004; Lamport, 1994; Knuth, 1986)

- Elixir
- Propery-based testing: Proper, QuickCheck (excheck)
- Erlang Verification Tool (Lars-Åke Freudlund)
- SMT solvers: Z3, CVC4, MATHSAT, Yices...
- Dafny
- Verification IRs:
 - Boogie
 - Why3 / WhyML
 - Viper
 - CAVI-ART
 - CHC (Constrained Horn Clauses)
 - Rule-based representation (COSTA group)
- Other IRs:
 - LLVM
 - BEAM
 - WebAssembly



Preliminaries

This chapter introduces some required topics and tools that are a basis to our project.

On the one hand, Elixir is the programming language that is the verification subject of this document and, at the same time, the one in which our implementation has been coded.

On the other hand, our verification system relies on the Satisfiability Modulo Theories (SMT) problem and its encoding in SMT-LIB, a standard language and interface to interact with theorem provers such as Z3.

3.1. Elixir

Elixir is a general-purpose programming language that runs on the Erlang Virtual Machine, where also the Erlang programming language runs [referenciar]. Both of them share some features, like their actor-based concurrency model, and have a native capability to interoperate. Although Elixir is younger than Erlang, this has allowed the former to be part of an ecosystem which has been developed across more than three decades.

We have chosen such a programming language for this research because, first, it is a modern programming language ready to be used in the industry [referenciar]. Second, it has the unusual property in formal verification to be dynamically typed, but its functional programming principles will make it easier to reason about. Finally, its metaprogramming capabilities will allow us to extend it according to our needs without requiring to modify its compiler.

3.1.1. General description

In this section, we introduce the basic concepts and constructs of sequential programming in Elixir. Our aim is to show the behavior of the language subset that is studied later in this document for its verification, and also its metaprogramming mechanism based on macros, on top of which our proposed verification system has been implemented.

The following examples will be exposed in the Elixir Read-Eval-Print-Loop (REPL), called iex, where iex> represents its default prompt:

```
iex> "Hello world"
"Hello world"
```

3.1.1.1. Value types

As usual, one of the core value types in Elixir is the integer, for which arithmetic operators behave as expected:

```
iex> (2 + 2) * 5
20
iex> -1
-1
iex> 1 / 0
** (ArithmeticError)
```

The boolean value type is also at its core, but its operators have some worth to mention semantics when involving non-boolean types, and also with respect to short-circuit evaluation:

```
iex> true and 2 # Evaluates to the second term
2
iex> 2 and true # Requires the first one to be a boolean
** (BadBooleanError)
iex> false and 1 / 0 # Does not evaluate the second term
false
```

Some built-in Elixir functions allow checking if a given value is of a given type in terms of a boolean result:

```
iex > is_boolean(true)
true
iex > is_boolean(2)
false
iex > is_integer(2)
true
```

Equality and comparison operators also evaluate to boolean values and allow mixing types:

```
iex> 2 === 2
true
iex> 2 === true
false
iex> 2 !== true
true
iex> 2 > 1
true
iex> 2 < true
true</pre>
```

3.1.1.2. Collection types

One of the simplest built-in collection types in Elixir is the inductive list, which consists of nested cons cells (i.e. pairs) and can be written in different ways:

```
iex> [] # The empty list
[]
```

3.1. Elixir 7

```
iex> [3 | []] # A cons cell
[3]
iex> [1 | [2 | [3 | []]]] # Nested cons cells
[1, 2, 3]
iex> [1, 2, 3] # Syntax sugar
[1, 2, 3]
iex> [1, 2 | [3]] # Syntax mix
[1, 2, 3]
```

It is not required for the list elements to be of the same type, and improper lists (i.e. those that do not have an empty list as the second element in the last cons cell [referenciar docs]) are also allowed:

```
iex > [1, 2, false]
[1, 2, false]
iex > [1 | [2 | 3]]
[1, 2 | 3]
```

Functions in Elixir use to be referred by its name and arity. The hd/1 and t1/1 built-in functions for lists allow to respectively obtain the first and second components of a cons cell:

```
iex> hd([1, 2, false])
1
iex> tl([1, 2, false])
[2, false]
iex> hd([])
** (ArgumentError)
iex> tl([])
** (ArgumentError)
```

There is also a function for checking the list type membership. Consider the following code to apply the is_list/1 function to several provided lists and return the conjunction of its results:

Another core collection type in Elixir is the tuple, which also does not restrict its elements to be of the same type:

```
iex> {} # The empty tuple
{}
iex> {1, false, {3, 4}, []}
{1, false, {3, 4}, []}
```

They have a size, which can be retrieved with the tuple_size/1 function, and each tuple component can also be retrieved with the elem/2 function by specifying its position with a zero-based index:

```
iex> tuple_size({1, 2, 3})
3
```

```
iex> elem({1, 2, 3}, 0)
1
iex> elem({1, 2, 3}, 2)
3
iex> elem({1, 2, 3}, 3)
** (ArgumentError)
```

In this case, the tuple type membership checking function is is_tuple/1.

3.1.1.3. Blocks, pattern matching and control flow

Elixir statements can be evaluated sequentially by gathering them inside a block delimited by a semicolon or a line break:

```
iex> 2 + 1;5 === 5;false
false # Evaluates to the last statement value
iex> (
          2 + 1
          5 === 5
          false
    )
false
```

The match operator = allows binding values to variable names. Note that these bindings are not locally scoped inside blocks and, in contrast to Erlang, variable bindings can be overridden:

```
iex > x = 2
2
iex > y = 2
2
iex > (z = 2, 4)
4
iex > z = 2
```

This operator also allows performing pattern matching, which destructures expressions according to patterns in order to check for a given shape and bind subexpressions to variable names. They are particularly useful for dealing with collection value types:

```
iex> {x, 3} = {2, 3}
{2, 3}
iex> {x, 3} = {2, 4}
** (MatchError)
iex> [h | t = [_, 3]] = [1, 2, 3] # A nested match
[1, 2, 3]
iex> t
[2, 3]
```

Regarding control flow, although Elixir also has usual constructs such as if, one of the most general ones is case. It Evaluates to the first branch that matches the pattern and is compliant with a possible guard expression, and this is the only one that is evaluated:

```
iex > case {1, 2, 3} do
```

3.1. Elixir 9

3.1.1.4. Function definitions

A named function, identified by its name and arity, can be defined inside modules with different body definitions and different matching for its arguments:

```
defmodule Example do
  def fact(0) do
   1
  end

def fact(n) when is_integer(n) and n > 0 do
   n * fact(n - 1) # Recursion is allowed
  end
end
```

The rules for which one is applied are the same as in case expressions, so function definitions can also express control flow [referencia].

3.1.2. Macros

TODO

Describe, this will be our way to extend Elixir for code verification.

3.1.3. Interoperability

TODO for the SMT solver integration.

Elixir offers several ways to interoperate with processes or libraries that are external to the Erlang Virtual Machine, apart from conventional Input/Output (I/O).

One of them are Native Implemented Function (NIF)s, which allow loading and calling libraries implemented in other programming languages such as C. A crash in a NIF brings the Erlang Virtual Machine down too. [referencia docs erlang]

A more safe approach is to launch an external process managed by the Erlang Virtual Machine and communicate with it by means of message passing, which in Elixir is provided as a mechanism called *ports*:

```
port = Port.open({:spawn, "cat"}, [:binary])
iex> send(port, {self(), {:command, "hello"}})
iex> flush()
# Received from the process
```

```
{#Port<0.1444>, {:data, "hello"}} send(port, {self(), :close})
```

A known drawback of this is that if the Erlang Virtual Machine crashes after having launched a long-running process, its stdin and stdout channels will be closed, it won't be automatically terminated. This depends on the behavior of the specific process when its communication channels are closed.

3.2. Satisfiability Modulo Theories

The SMT problem consists of checking whether a given logical formula is satisfiable within a specific theory (Clark Barrett and Tinelli, 2017). This allows to define theories in which the SMT problem is decidable and, moreover, to design efficient algorithms specialized in solving this problem for a theory.

TODO

Para esto último, poner un ejemplo referenciado de una teoría con SMT decidible y algún algoritmo eficiente.

3.2.1. SMT-LIB

SMT-LIB is an initiative which tries to provide a common interface to interact with SMT solvers. It defines a solver-agnostic standard language with a Lisp-like syntax to both configure a solver, manage it, encode an SMT problem instance and query for solutions.

General description (many sorted, citado) and example, show the subset of commands that we are going to use

TODO

```
 \langle \; command \; \rangle \; ::= \; (\; assert \; \langle \; term \; \rangle \; ) \\ | \; \; (\; check-sat \; ) \\ | \; \; \; (\; pop \; \langle \; numeral \; \rangle \; ) \\ | \; \; \; (\; push \; \langle \; numeral \; \rangle \; ) \\ | \; \; \; (\; declare-sort \; \langle \; symbol \; \rangle \; \langle \; numeral \; \rangle \; ) \\ | \; \; \; (\; declare-const \; \langle \; symbol \; \rangle \; \langle \; sort \; \rangle \; ) \\ | \; \; \; (\; declare-fun \; \langle \; symbol \; \rangle \; (\; \langle \; symbol \; \rangle^* \; ) \; \langle \; sort \; \rangle \; )
```

TODO Poner un problema sencillo de ejemplo. Separar a anexo o buscar otro mas corto?

```
; The propositional variable 'pi_j' means that the node i appears in ; the path position j, where nodes are labeled as natural numbers ; starting from 0.

(declare-const p0_0 Bool)

(declare-const p0_1 Bool)

(declare-const p0_2 Bool)

(declare-const p0_3 Bool)

(declare-const p1_0 Bool)

(declare-const p1_1 Bool)

(declare-const p1_2 Bool)

(declare-const p1_3 Bool)
```

```
(declare-const p2_0 Bool)
(declare-const p2_1 Bool)
(declare-const p2_2 Bool)
(declare-const p2_3 Bool)
(declare-const p3_0 Bool)
(declare-const p3_1 Bool)
(declare-const p3_2 Bool)
(declare-const p3_3 Bool)
; Every node should appear in at least one position.
(assert (or p0_0 p0_1 p0_2 p0_3))
(assert (or p1_0 p1_1 p1_2 p1_3))
(assert (or p2_0 p2_1 p2_2 p2_3))
(assert (or p3_0 p3_1 p3_2 p3_3))
; Two different nodes do not appear in the same path position.
(assert (not (and p0_0 p1_0)))
(assert (not (and p0_1 p1_1)))
(assert (not (and p0_2 p1_2)))
(assert (not (and p0_3 p1_3)))
(assert (not (and p0_0 p2_0)))
(assert (not (and p0_1 p2_1)))
(assert (not (and p0_2 p2_2)))
(assert (not (and p0_3 p2_3)))
(assert (not (and p0_0 p3_0)))
(assert (not (and p0_1 p3_1)))
(assert (not (and p0_2 p3_2)))
(assert (not (and p0_3 p3_3)))
(assert (not (and p1_0 p0_0)))
(assert (not (and p1_1 p0_1)))
(assert (not (and p1_2 p0_2)))
(assert (not (and p1_3 p0_3)))
(assert (not (and p1_0 p2_0)))
(assert (not (and p1_1 p2_1)))
(assert (not (and p1_2 p2_2)))
(assert (not (and p1_3 p2_3)))
(assert (not (and p1_0 p3_0)))
(assert (not (and p1_1 p3_1)))
(assert (not (and p1_2 p3_2)))
(assert (not (and p1_3 p3_3)))
(assert (not (and p2_0 p0_0)))
(assert (not (and p2_1 p0_1)))
(assert (not (and p2_2 p0_2)))
(assert (not (and p2_3 p0_3)))
(assert (not (and p2_0 p1_0)))
(assert (not (and p2_1 p1_1)))
(assert (not (and p2_2 p1_2)))
(assert (not (and p2_3 p1_3)))
(assert (not (and p2_0 p3_0)))
```

```
(assert (not (and p2_1 p3_1)))
(assert (not (and p2_2 p3_2)))
(assert (not (and p2_3 p3_3)))
(assert (not (and p3_0 p0_0)))
(assert (not (and p3_1 p0_1)))
(assert (not (and p3_2 p0_2)))
(assert (not (and p3_3 p0_3)))
(assert (not (and p3_0 p1_0)))
(assert (not (and p3_1 p1_1)))
(assert (not (and p3_2 p1_2)))
(assert (not (and p3_3 p1_3)))
(assert (not (and p3_0 p2_0)))
(assert (not (and p3_1 p2_1)))
(assert (not (and p3_2 p2_2)))
(assert (not (and p3_3 p2_3)))
; If two nodes are not adjacent, then they do not appear
; consecutively in the path.
(assert (=> p1_0 (not p3_1)))
(assert (=> p1_1 (not p3_2)))
(assert (=> p1_2 (not p3_3)))
(assert (=> p2_0 (not p3_1)))
(assert (=> p2_1 (not p3_2)))
(assert (=> p2_2 (not p3_3)))
(assert (=> p3_0 (not p1_1)))
(assert (=> p3_1 (not p1_2)))
(assert (=> p3_2 (not p1_3)))
(assert (=> p3_0 (not p2_1)))
(assert (=> p3_1 (not p2_2)))
(assert (=> p3_2 (not p2_3)))
(check-sat)
```

3.2.2. Z3

One of the SMT solvers that implements the SMT-LIB standard is the Z3 theorem prover from Microsoft Research.

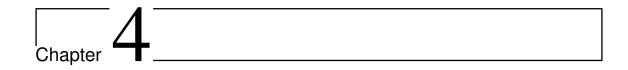
TODO

Poner alguna referencia, enseñar su uso con -i

Decir porque lo hemos elegido y que aun así hemos intentado utilizarlo como interprete SMT-LIB para no depender completamente de el.

Note that there may exist subtle non-compliances when a solver implements the SMT-LIB standard. For example, we have found that Z3 does not include the surrounding double-quotes when it prints back the provided string literal, which is the specified behavior in the standard.

This may add confusion because the **echo** command is the only one whose response is a string literal and, as this is not the case for Z3, there are corner cases in which a command response can be confused with a printed string intended to delimit command responses, which is one of the proposed usages for **echo** in Clark Barrett and Tinelli (2017).



SMT Solver Integration in Elixir

In order to implement our system, we will require to be able to interact with an SMT solver from Elixir. We have decided to use the Z3 theorem prover, which implements SMT-LIB, and to communicate with it precisely by using this standard.

Then, we will introduce a simple formal language whose semantics are defined in terms of the SMT problem, and an example of its implementation in Elixir as a result of the previous integration with a solver.

4.1. SMT-LIB interpreter bindings

Initially, we found an Elixir package that provides integration with Z3 and is implemented using ports, but it seemed to be not so mature and maintained. It was also not published in Hex, the Elixir package manager, and we had no guarantees about if it would lack some functionality that we would require at some point.

To implement our own SMT-LIB interpreter binding was an opportunity to get started with Elixir in practice, and also with its macro system. This has given place to a side project which consists of an Elixir DSL to communicate with SMT-LIB interpreters, which may be at short term useful to the Elixir community.

4.1.1. Elixir SmtLib example

Present the resulting tool, the DSL and an example.

4.1.2. SmtLib implementation

Although Elixir is dynamically typed, it has a system to annotate the intended types for functions and a tool to perform a static analysis on them. We will use these specifications together with function identifiers to outline the ideas behind our implementation.

First, we define a type to represent an SMT-LIB command from the subset that we have exposed in 3.2.1:

```
@type command_t ::
    {:assert, term_t}
    | :check_sat
    | {:push, numeral_t}
    | {:pop, numeral_t}
```

```
| {:declare_const, symbol_t, sort_t}
| {:declare_sort, symbol_t, numeral_t}
| {:declare_fun, symbol_t, [sort_t], sort_t}
```

where other involved types like numeral_t and sort_t are defined similarly.

Then, we implement a function commands/1 that, given a subset of the Elixir AST (i.e. our DSL), transforms it into a list of SMT-LIB commands:

```
@spec commands(ast) :: [command_t]
```

The implementation defines cases for each possible term and its possible subterms, like the following:

```
@spec command(ast) :: command_t
def command({:declare_const, _, [{v, s}]}) do
   {:declare_const, symbol(v), sort(s)}
end
```

TODO explain the DSL and think about split this into subsections distinguish from function names by modules

Once we are able to transform the DSL into SMT-LIB commands, we require a function to render each command into a string that an SMT-LIB interpreter understands:

```
@spec command(command_t) :: String.t
```

It handles compositionally the command_t type with cases like the following:

```
{:declare_const, s1, s2} ->
  "(declare-const #{symbol(s1)} #{sort(s2)})"
```

Communication with ports, implementation for Z3 but it can be other

Finally, in order to understand the solver responses, we have also implemented a failable function that parses the received string:

```
@spec general_response(String.t()) ::
    {:ok, general_response_t}
    | {:error, term}
```

It has been implemented using nimble, an Elixir package of parser combinators, in order to delegate this task and get the reliability of a well tested tool [referencia]. Its top level parser definition is as follows:

```
defparsec :general_response,
    skip_blanks_and_comments()
    |> choice([
        token(success()) |> eos(),
        token(unsupported()) |> eos(),
        token(error()) |> eos(),
        token(specific_success_response()) |> eos()
])
```

4.2. The L0 language

This section exposes a formal language that we have called L0 and will represent the lowest level of our verification system.

It is intended to be implemented as Elixir expressions that send SMT-LIB statements to an SMT solver and will allow us to define a verification IR on top of it.

4.2.1. Notation

We assume that \mathbb{F} is the set of many-sorted logic formulae involving equality, uninterpreted function symbols and arithmetic. We use φ , ψ , etc. to denote elements from this set.

Also, we assume a set Σ^0 of uninterpreted function symbols and a set \mathbb{T} of terms in many-sorted logic, generated by the following grammar:

$$\mathbb{T} \ni t ::= n \mid x \mid f(t_1, \dots, t_m)$$

where n is a number, x is a variable, and $f \in \Sigma^0$ is a function symbol of arity m.

4.2.2. Syntax

The syntax of L0 expressions is given by the following grammar:

If $I = [i_1, \ldots, i_n]$ is a sequence of elements, we use the notation $\overline{\epsilon_i}^{i \in I}$ to denote the sequential composition $\epsilon_{i_1}; \ldots; \epsilon_{i_n}$.

4.2.3. Semantics

Let V be a set of variable names, $\mathbb{F}(V)$ the subset of \mathbb{F} with free variables in V, and a predicate unsat $\llbracket _ \rrbracket$ which, given a set of formulas from \mathbb{F} , determines whether they are unsatisfiable or not. We define the big step operational semantics of L0 expressions as the smallest relation $\langle \epsilon, X, \Phi \rangle \Downarrow (X', \Phi')$ between $\mathbf{Exp}^0 \times \mathcal{P}(V) \times \mathcal{P}(\mathbb{F}(V))$ and $\mathcal{P}(V) \times \mathcal{P}(\mathbb{F}(V))$ that satisfies the following rules:

$$\begin{tabular}{ll} \hline \langle {\bf skip}, \ X, \ \Phi \rangle \Downarrow (X, \Phi) \\ \\ \hline \\ \frac{\varphi \in \mathbb{F}(X)}{\langle {\bf add} \ \varphi, \ X, \ \Phi \rangle \Downarrow (X, \Phi \cup \{\varphi\})} & \frac{x \notin X}{\langle {\bf declare\text{-}const} \ x, \ X, \ \Phi \rangle \Downarrow (X \cup \{x\}, \Phi)} \\ \hline \\ \hline \end{tabular}$$

$$\frac{\langle \epsilon_1, X, \Phi \rangle \Downarrow (X', \Phi') \qquad \langle \epsilon_2, X', \Phi' \rangle \Downarrow (X'', \Phi'')}{\langle \epsilon_1; \epsilon_2, X, \Phi \rangle \Downarrow (X'', \Phi'')}$$

$$\frac{\langle \epsilon, X, \Phi \rangle \downarrow (X', \Phi')}{\langle \mathbf{local} \ \epsilon, \ X, \ \Phi \rangle \downarrow (X, \Phi)}$$

$$\frac{\langle \epsilon_1, X, \Phi \rangle \Downarrow (X', \Phi') \quad \textit{unsat } \llbracket \Phi' \rrbracket \quad \langle \epsilon_2, X, \Phi \rangle \Downarrow (X'', \Phi'')}{\langle \mathbf{when\text{-}unsat } \epsilon_1 \mathbf{\ do } \epsilon_2 \mathbf{\ else } \epsilon_3, \ X, \ \Phi \rangle \Downarrow (X'', \Phi'')}$$

$$\frac{\langle \epsilon_1, X, \Phi \rangle \Downarrow (X', \Phi') \quad \neg unsat \ \llbracket \Phi' \rrbracket \quad \langle \epsilon_3, X, \Phi \rangle \Downarrow (X'', \Phi'')}{\langle \mathbf{when\text{-}unsat} \ \epsilon_1 \ \mathbf{do} \ \epsilon_2 \ \mathbf{else} \ \epsilon_3, \ X, \ \Phi \rangle \Downarrow (X'', \Phi'')}$$

The absence of rules for the **fail** expression is intentional, because we want any reachable **fail** to prevent the whole expression for evaluating. We have also required this to happen if the same variable is declared twice or if a formula with undeclared variables is being added.

4.2.4. Implementation

TODO

Simple implementation using the SMT-LIB bindings for Elixir. Show a simple example.

```
defmacro eval(_, {:skip, _, _}) do
  quote do
    nil
  end
end
defmacro eval(_, {:fail, _, _}) do
  quote do
    raise "Verification failed"
  end
end
defmacro eval(conn, {:seq, _, [e1, e2]}) do
  quote do
    conn = unquote(conn)
    eval(conn, unquote(e1))
    eval(conn, unquote(e2))
  end
end
defmacro eval(conn, {:local, _, [e]}) do
  quote do
    conn = unquote(conn)
    \{\_, : ok\} = run(conn, push)
    eval(conn, unquote(e))
    \{\_, : ok\} = run(conn, pop)
  end
```

```
end
defmacro eval(conn, {:add, _, [f]}) do
  quote do
    conn = unquote(conn)
    {_, :ok} = run(conn, assert(unquote(f)))
  end
end
defmacro eval(conn, {:declare_const, _, [x]}) do
  quote do
    conn = unquote(conn)
    \{\_, : ok\} = run(
      conn,
      declare_const([{unquote(x), Term}])
  end
end
defmacro eval(
  conn,
  {:when_unsat, _, [e1, [do: e2, else: e3]]})
do
  quote do
    conn = unquote(conn)
    \{\_, : ok\} = run(conn, push)
    eval(conn, unquote(e1))
    {_, {:ok, result}} = run(conn, check_sat)
    \{\_, : ok\} = run(conn, pop)
    case result do
      :unsat -> eval(conn, unquote(e2))
      _ -> eval(conn, unquote(e3))
    end
  end
end
defmacro eval(_, e) do
  raise "Unknown expression #{Macro.to_string(e)}"
end
```

Chapter 5

The L1 Intermediate Representation

"This process of using tools you built yesterday to help build bigger tools today is called abstraction, and it is the most powerful force I know of in the universe"

— Sandy Maguire

TODO

5.1. Syntax

We denote by $\Sigma^1 = \{ = = =, < =, > =, +, -, \dots \}$ the set of operators and functions allowed in L1. We assume that for every element $f \in \Sigma^1$ there is an uninterpreted function symbol in Σ^0 , which will be denoted by \widehat{f} . If f has arity n, its corresponding function symbol \widehat{f} will have sort $Term \times .^n . \times Term \to Term$.

Let us define the syntax of L1 expressions and statements:

```
{literal}
                                         {variable}
                                         {conjunction}
                                         {disjunction}
                                         {empty list}
                                         {list constructor}
                                         {tuple}
                                         {function or operator application}
\mathbf{Stm} \ni S ::= \mathbf{skip}
                block S
                \mathbf{havoc}\ x
                S_1; S_2
                assume e
                 assert e
                 unfold f(e_1,\ldots,e_n)
```

TODO

5.2.1. Built-in declarations

TODO

Required SMT-LIB preamble for the translation.

During the translation of L1 expressions we require some defined sorts, constants and functions. In our implementation, the SMT-LIB commands with that purpose are the following:

```
(declare-sort Term 0)
(declare-sort Type 0)
(declare-fun type (Term) Type)
(declare-fun term_size (Term) Int)
(declare-fun integer_val (Term) Int)
(declare-fun boolean_val (Term) Bool)
(declare-fun integer_lit (Int) Term)
(declare-fun boolean_lit (Bool) Term)
(declare-fun tuple_size (Term) Int)
(declare-fun elem (Term Int) Term)
(declare-fun nil () Term)
(declare-fun cons (Term Term) Term)
(declare-fun hd (Term) Term)
(declare-fun tl (Term) Term)
(declare-const int Type)
(declare-const bool Type)
(declare-const tuple Type)
(declare-const nonempty_list Type)
(assert (distinct int bool))
(assert (distinct int tuple))
(assert (distinct int nonempty_list))
(assert (distinct bool tuple))
(assert (distinct bool nonempty_list))
(assert (distinct tuple nonempty_list))
(define-fun is_integer ((x Term)) Bool (= (type x) int))
(define-fun is_boolean ((x Term)) Bool (= (type x) bool))
(define-fun is_tuple ((x Term)) Bool (= (type x) tuple))
(define-fun is_nonempty_list ((x Term)) Bool (= (type x) nonempty_list))
(define-fun is_list ((x Term)) Bool (or (= x nil) (= (type x) nonempty_list)))
```

Also, tuple constructors for any size n must be declared with sort $Term \times .^n . \times Term \to Term$, but in our implementation we declare each one the first time that it is required.

5.2.2. Built-in specifications

TODO

Built-in specifications and SMT-LIB code to emulate the Elixir semantics.

We shall also assume that for every function symbol $f \in \Sigma^1$ of arity n there is an overloaded specification expressed in terms of L0 formulae. Here the word *overloaded* means that there could by many pre/post-condition pairs for each function. For example, equality can be specified as follows:

```
 \{ is\text{-}integer(x) \land is\text{-}integer(y) \} 
 x === y 
 \{ boolean\text{-}value(\widehat{===}(x,y)) \Leftrightarrow integer\text{-}value(x) = integer\text{-}value(y) \} 
 \{ is\text{-}boolean(x) \land is\text{-}boolean(y) \} 
 x === y 
 \{ boolean\text{-}value(\widehat{===}(x,y)) \Leftrightarrow boolean\text{-}value(x) = boolean\text{-}value(y) \} 
 \vdots 
 \{ true \} 
 x === y 
 \{ is\text{-}boolean(\widehat{===}(x,y)) \land boolean\text{-}value(\widehat{===}(x,y)) \Leftrightarrow (x=y) \}
```

Here $\stackrel{\textstyle \frown}{===}$ is the uninterpreted symbol in Σ^0 corresponding to Elixir's strict equality operator $===\in \Sigma^1$. We write the former in prefix form in order to highlight the fact that it is an uninterpreted function symbol in the logic. On the contrary, the =, \Leftrightarrow , \wedge in the specification above are actual connectives and operators of the underlying logic.

These specifications are built-in into the system. They are not provided by the user. If we apply an operator that has several pre/postcondition pairs, we check all the preconditions and only assume those postconditions corresponding to the preconditions that hold.

Therefore, each function $f \in \Sigma^1$ of arity n may have several specifications $\sigma_1, \ldots, \sigma_m$. Each specification is a pair $(\varphi(x_1, \ldots, x_n), \psi(x_1, \ldots, x_n))$, where the x_i variables denote the parameters of the function. We denote by Spec(f) the set of specifications of f.

In order to allow L1 expressions to model the semantics of Elixir, the corresponding uninterpreted functions must be declared in SMT-LIB with sort $Term \times .^n . \times Term \rightarrow Term$. We provide some built-in specifications which are explained in this section.

For integer arithmethic, the specification of + can be as

```
 \{is\text{-}integer(x) \land is\text{-}integer(y)\} \\ x + y \\ \{is\text{-}integer(\widehat{+}(x,y)) \land integer\text{-}value(\widehat{+}(x,y)) = integer\text{-}value(x) + integer\text{-}value(y)\} \\ \text{and similar for - and *. The unary version of - can be specified as follows:} \\ \{is\text{-}integer(x)\} \\ - x \\ \{is\text{-}integer(\widehat{-}(x)) \land integer\text{-}value(\widehat{-}(x)) = -integer\text{-}value(x)\} \\ \text{It is similar to the Elixir boolean negation:} \\ \{is\text{-}boolean(x)\} \\ not(x) \\ \{is\text{-}boolean(\widehat{not}(x)) \land boolean\text{-}value(\widehat{not}(x)) \Leftrightarrow \neg boolean\text{-}value(x)\} \\ \end{aligned}
```

We have only provided the comparison for integer terms as

```
\begin{aligned} &\{is\text{-}integer(x) \land is\text{-}integer(y)\} \\ &x < y \\ &\{is\text{-}boolean(\widehat{<}(x,y)) \land boolean\text{-}value(\widehat{<}(x,y)) \Leftrightarrow integer\text{-}value(x) < integer\text{-}value(y)\} \end{aligned}
```

and it is similar for >, <= and >=. An improvement would be to extend this for any term, including lists and tuples. Term equality can be specified as

```
\{is\text{-}integer(x) \land is\text{-}integer(y)\}
x === y
\{boolean\text{-}value(\widehat{=}==(x,y)) \Leftrightarrow integer\text{-}value(x) = integer\text{-}value(y)\}
\{is-boolean(x) \land is-boolean(y)\}
x === y
\{boolean\text{-}value(\widehat{=}==(x,y)) \Leftrightarrow boolean\text{-}value(x) = boolean\text{-}value(y)\}
\{is\text{-}list(x) \land is\text{-}list(y)\}
x === y
\{boolean\text{-}value(\widehat{=}=(x,y)) \Leftrightarrow (x=nil \land y=nil) \lor (hd(x)=hd(y) \land tl(x)=tl(y))\}
\{is\text{-}tuple(x) \land is\text{-}tuple(y) \land tuple\text{-}size(x) = tuple\text{-}size(y)\}
x === y
\{boolean\text{-}value(\widehat{=}==(x,y)) \Leftrightarrow (\forall i.i >= 0 \land i < tuple\text{-}size(x) \Rightarrow elem(x,i) = elem(y,i))\}
\{is-tuple(x) \land is-tuple(y) \land tuple-size(x) \neq tuple-size(y)\}
\{\neg boolean\text{-}value(\widehat{\equiv} = = (x, y))\}
\{true\}
x === y
\{is-boolean(\widehat{=}==(x,y)) \land boolean-value(\widehat{=}==(x,y)) \Leftrightarrow (x=y)\}
```

and it is also similar for !==.

The *tuple-size* and *elem* functions can be specified directly in terms of the built-in declarations used during the translation:

```
 \{is\text{-}tuple(x)\}   tuple\text{-}size(x)   \{is\text{-}integer(tuple\text{-}size(x)) \land integer\text{-}value(tuple\text{-}size(x)) = tuple\text{-}size(x)\}   \{is\text{-}tuple(x) \land is\text{-}integer(i) \land integer\text{-}value(i) >= 0 \land integer\text{-}value(i) < tuple\text{-}size(x)\}   elem(x,i)   \{elem(x,i) = elem(x,integer\text{-}value(i))\}
```

The same can be applied to the hd function

$$\begin{aligned} &\{is\text{-}nonempty\text{-}list(x)\}\\ &hd(x)\\ &\{\widehat{hd}(x) = hd(x)\} \end{aligned}$$

and it is similar for tl. Note that, in these last examples, the L1 function is not the same as the one mentioned in the postcondition, which is a built-in L0 function although we have used the same name.

The functions to mention the term types can also be specified directly with the built-in declared L0 functions:

```
 \begin{aligned} &\{true\}\\ &is\text{-}integer(x)\\ &\{is\text{-}boolean(is\text{-}integer(x)) \land boolean\text{-}value(is\text{-}integer(x)) \Leftrightarrow is\text{-}integer(x)\} \end{aligned}
```

and it is similar for the remaining types.

5.2.3. Translation into L0

TODO

We shall define two functions:

$$\begin{array}{ll} trExp & \llbracket _ \rrbracket : & \mathbf{Exp}^0 \times \mathbf{Exp}^1 \to \mathbf{Exp}^0 \times \mathbb{T} \\ trStm & \llbracket _ \rrbracket : & \mathbf{Stm} \to \mathbf{Exp}^0 \end{array}$$

Given an L1 expression e, the application trExp γ $[\![e]\!]$ returns a tuple (ϵ,t) , in which ϵ is an L0 expression that models the semantics of e, and t is the term in the underlying logic that will be used to refer to the result of e. The γ models those facts that are known by the time e is evaluated. This is needed to handle the short circuit-based semantics of and and or. We are going to omit this γ parameter when it models no knowledge:

$$trExp \ \llbracket e \rrbracket \equiv trExp \ \mathbf{skip} \ \llbracket e \rrbracket$$

Let us define $trExp = [\![\]\!]$ case by case. In the case of literals, we get:

$$trExp \quad [c] \equiv (add \ is - \tau(\tau - lit(\hat{c})); add \ \tau - value(\tau - lit(\hat{c})) = \hat{c}, \tau - lit(\hat{c}))$$

where τ is the type of the literal, which can be determined at compile time since it is a literal, and \hat{c} is the constant in the underlying logic represented by that literal. For example, the Elixir term **2** corresponds to the actual number $2 \in \mathbb{Z}$, so $\hat{\mathbf{2}} = 2$.

In the case of variables, we get:

$$trExp \ _ \ [x] \equiv (\mathbf{skip}, \hat{x})$$

It returns the logic variable \hat{x} corresponding to the L1 variable x. No L0 expression is generated.

The L0 expressions generated by a tuple correspond to the ones generated by each component, the projection function for each one and its tuple size function. Its translated term is a specific tuple constructor for its size n applied to its translated term components:

```
\begin{split} \mathit{trExp} \ \gamma \ [\![\{e_1, \dots, e_n\}]\!] &\equiv (\epsilon_1; \dots; \epsilon_n; \epsilon; \epsilon'_1; \dots; \epsilon'_n, t) \\ \mathbf{where} \ \forall i \in \{1..n\}. (\epsilon_i, t_i) &= \mathit{trExp} \ \gamma \ [\![e_i]\!] \\ t &= \mathit{n-tuple}(t_1, \dots, t_n) \\ \epsilon &= \mathbf{add} \ \mathit{is-tuple}(t); \mathbf{add} \ \mathit{tuple-size}(t) = n \\ \forall i \in \{1..n\}. \epsilon'_i &= \mathbf{add} \ \mathit{elem}(t, i) = t_i \end{split}
```

The translation for lists is defined recursively, with the empty list as the base case. The generated L0 expressions set the corresponding heads and tails for the generated list terms, and it does not require the second argument for the list constructor to be a list:

$$trExp \ _ \ \llbracket[]\rrbracket \equiv (\mathbf{skip}, nil)$$

$$trExp \ \gamma \ \llbracket[e_1 \mid e_2]\rrbracket \equiv (\epsilon_1; \epsilon_2; \epsilon, t)$$

$$\mathbf{where} \ (\epsilon_1, t_1) = trExp \ \gamma \ \llbracket e_1 \rrbracket$$

$$(\epsilon_2, t_2) = trExp \ \gamma \ \llbracket e_2 \rrbracket$$

$$t = cons(t_1, t_2)$$

$$\mathbf{add} \ is-nonempty-list(t);$$

$$\mathbf{add} \ hd(t) = t_1;$$

$$\mathbf{add} \ tl(t) = t_2$$

The most complex case is that of function application:

$$trExp \ \gamma \ \llbracket f(e_1,\ldots,e_n) \rrbracket \equiv (\epsilon_1;\ldots;\epsilon_n;\epsilon;\overline{\epsilon_\sigma}^{\sigma \in Spec(f)},\widehat{f}(t_1,\ldots,t_n))$$
 where $\forall i \in \{1..n\}.(\epsilon_i,t_i) = trExp \ \gamma \ \llbracket e_i \rrbracket$
$$\epsilon = \begin{bmatrix} \text{when-unsat} \ \gamma; \text{add} \ \neg \bigvee_{\sigma \in Spec(f)} Pre(\sigma)(t_1,\ldots,t_n) \\ \text{do skip} \\ \text{else fail} \end{bmatrix}$$

$$\forall \sigma \in Spec(f) \text{ such that } \sigma = (\varphi_\sigma(x_1,\ldots,x_n), \psi_\sigma(x_1,\ldots,x_n)).$$

$$\epsilon_\sigma = \begin{bmatrix} \text{when-unsat} \ \gamma; \text{add} \ \neg \varphi_\sigma(t_1,\ldots,t_n) \\ \text{add} \ \varphi_\sigma(t_1,\ldots,t_n); \\ \text{add} \ \psi_\sigma(t_1,\ldots,t_n) \\ \text{else skip} \end{bmatrix}$$

Firstly, we generate the L0 expression ϵ_i corresponding to each argument e_i , and its corresponding uninterpreted term t_i . Then, for each pre/post-condition pair of the specification of the function being applied, we generate code that checks whether the precondition holds and, in case it does, we assert both the precondition and postcondition. Finally, we also check and fail if none of the preconditions hold.

We distinguish the cases of logical connectives from function application because of their specific short-circuit semantics in Elixir:

```
trExp \ \gamma \ [e_1 \ \mathbf{and} \ e_2] \equiv (\epsilon, t)
      where (\epsilon_1, t_1) = trExp \ \gamma \ \llbracket e_1 \rrbracket
                 (\epsilon_2, t_2) = trExp \ \gamma' \ [e_2]
                          \gamma' = \gamma; add boolean-value(t_1)
                          t = \mathbf{and}(t_1, t_2)
                                   \epsilon_1;
                                   when-unsat \gamma; add \neg is-boolean(t_1) do
                                       when-unsat \gamma; add boolean-value(t_1) do
                                          add t = false
                                       else
                                          when-unsat \gamma; add \neg boolean\text{-}value(t_1) do
                                             add t = t_2
                                          else when-unsat \gamma'; add \neg is-boolean(t_2) do
                                             add is-boolean(t);
                                             add boolean-value(t) = boolean-value(t<sub>1</sub>)
                                                                            \land boolean\text{-}value(t_2)
                                          else fail
                                   else fail
```

In the translation for an **and** expression, we firstly check if the term to the left is a boolean. Then, on the one hand, if it is known to be always *false*, the resulting term is *false*. On the other hand, if it is known to be always *true*, the resulting term is the right one regardless of its type. Note that this right term has been translated with the knowledge that the left one is *true*. If the value of the left term is not exactly known at this point, we check if the right term is a boolean, again with the knowledge that the left one is *true*, and translate the whole expression into the underlying logical conjunction.

The translation corresponding to **or** is analogous:

```
trExp \ \gamma \ \llbracket e_1 \ \mathbf{or} \ e_2 \rrbracket \equiv (\epsilon, t)
      where (\epsilon_1, t_1) = trExp \ \gamma \ [e_1]
                  (\epsilon_2, t_2) = trExp \ \gamma' \ \llbracket e_2 \rrbracket
                           \gamma' = \gamma; add \neg boolean\text{-}value(t_1)
                           t = \widehat{\mathbf{or}}(t_1, t_2)
                                     when-unsat \gamma; add \neg is-boolean(t_1) do
                                        when-unsat \gamma; add \neg boolean\text{-}value(t_1) do
                                            add t = true
                                        else
                                            when-unsat \gamma; add boolean-value(t_1) do
                                               add t = t_2
                                           else when-unsat \gamma'; add \neg is-boolean(t_2) do
                                               add is-boolean(t);
                                               add boolean-value(t) = boolean-value(t_1)
                                                                               \vee boolean\text{-}value(t_2)
                                            else fail
                                     else fail
```

Now we move on to L1 statements. The following ones are translated in a quite straightforward way:

```
trStm \ [\![\mathbf{skip}]\!] \equiv \mathbf{skip}
trStm \ [\![\mathbf{block}\ S]\!] \equiv \mathbf{local}\ trStm \ [\![S]\!]
trStm \ [\![\mathbf{havoc}\ x]\!] \equiv \mathbf{declare\text{-}const}\ \widehat{x}
trStm \ [\![S_1; S_2]\!] \equiv trStm \ [\![S_1]\!]; trStm \ [\![S_2]\!]
\mathbf{where}\ (\epsilon_1, t_1) = trExp \ [\![e_1]\!]
(\epsilon_2, t_2) = trExp \ [\![e_2]\!]
```

In the case of **assume**, we generate the expression ϵ that corresponds to the expression being assumed and its uninterpreted term t. We ensure that the term t actually denotes a boolean value and, in this case, we assert that this boolean value is true:

$$trStm \ [\![\![\mathbf{assume} \ e]\!] \equiv \left[\begin{array}{c} \epsilon; \\ \mathbf{when\text{-}unsat} \ \mathbf{add} \ \neg is\text{-}boolean(t) \\ \mathbf{do} \ \mathbf{add} \ boolean\text{-}value(t) \\ \mathbf{else} \ \mathbf{fail} \end{array} \right] \qquad \mathbf{where} \ (\epsilon,t) = trExp \ [\![\![e]\!]\!]$$

In the case of **assert**, we also generate the expression ϵ that corresponds to the expression being assumed and its uninterpreted term t. We ensure that the term t actually denotes a boolean value and also that its boolean value is true:

```
trStm \ [\![ assert \ e ]\!] \equiv \left[ \begin{array}{l} \epsilon; \\ \textbf{when-unsat} \ \textbf{add} \ \neg is\text{-}boolean(t) \\ \textbf{do skip} \\ \textbf{else fail}; \\ \textbf{when-unsat} \ \textbf{add} \ \neg boolean\text{-}value(t) \\ \textbf{do add} \ boolean\text{-}value(t) \\ \textbf{else fail} \end{array} \right] \quad \textbf{where} \ (\epsilon,t) = trExp \ [\![ e ]\!]
```

Finally, the **unfold** statement relies on having an user-provided definition for the involved function body as a parameterized L1 expression, and also user-provided pre/post-condition pair specifications in terms of L1 expressions:

```
trStm \ [ \textbf{unfold} \ f(e_1,\ldots,e_n) ] \equiv \epsilon; \overline{\epsilon_\sigma}{}^{\sigma \in UserSpec(f)}   \textbf{where} \ \epsilon = trStm \ [ \textbf{assume} \ f(e_1,\ldots,e_n) === Body(f)(e_1,\ldots,e_n) ]   \forall \sigma \in UserSpec(f) \ \text{such that} \ \sigma = (p_\sigma(e_1\ldots,e_n),q_\sigma(e_1,\ldots,e_n)).   (\epsilon_p,t_p) = trExp \ [ p_\sigma(e_1\ldots,e_n) ]   \textbf{when-unsat} \ \textbf{add} \ \neg is-boolean(t_p) \ \textbf{do}   \textbf{when-unsat} \ \textbf{add} \ \neg boolean-value(t_p) \ \textbf{do}   \textbf{trStm} \ [ \textbf{assume} \ p_\sigma(e_1\ldots,e_n) ] ;   trStm \ [ \textbf{assume} \ q_\sigma(e_1\ldots,e_n) ]   \textbf{else skip}   \textbf{else skip}
```

5.2.4. Term size modelling

TODO

Intended to be used for reasoning about termination.

We also provide the following axioms in order to reason about term sizes:

```
\begin{aligned} term\text{-}size(nil) &= 1 \\ \forall x.is\text{-}integer(x) \Rightarrow term\text{-}size(x) &= 1 \\ \forall x.is\text{-}boolean(x) \Rightarrow term\text{-}size(x) &= 1 \\ \forall x.is\text{-}nonempty\text{-}list(x) \Rightarrow term\text{-}size(x) &= 1 + term\text{-}size(hd(x)) + term\text{-}size(tl(x)) \\ \forall x.is\text{-}tuple(x) \Rightarrow \forall i.i > = 0 \land i < tuple\text{-}size(x) \Rightarrow term\text{-}size(elem(x,i)) < term\text{-}size(x) \end{aligned}
```

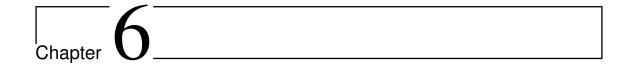
They are based on the types and will be useful for reasoning about termination.

5.3. Implementation

TODO

Show examples in a separate section before this one if possible.

Mention relevant facts of the development process and implementation details.



Elixir Code Verification

"Do not fear mistakes - there are none" — Miles Davis

TODO

6.1. The L2 verification language

TODO

6.1.1. Syntax

TODO

6.1.2. Extended verification functions

TODO

Allowing L2 expressions in user defined functions.

6.1.3. Translation and verification

TODO

Translate L2 code into L1 for verification and into Elixir code.

6.1.4. Termination

TODO

Show our current ideas about termination using term sizes.

6.2. Implementation

TODO

Show examples in a separate section before this one if possible.

Mention relevant facts of the development process and implementation details.

7	!		
Chapter			

Conclusions and Future Work

"That's just how it is: when you get over one milestone, there's another, bigger one" — Allan Holdsworth

TODO

Bibliography

Y así, del mucho leer y del poco dormir, se le secó el celebro de manera que vino a perder el juicio.

Miguel de Cervantes Saavedra

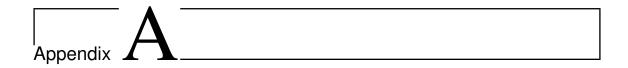
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Title of the Appendix A

TODO

Appendix content. Think if something should be converted into an appendix.



Title of the Appendix B

TODO

Appendix content. Think if something should be converted into an appendix.

Acronyms

```
DSL Domain Specific Language. 1, 13, 14
```

I/O Input/Output. 9

 ${\bf IR}$ Intermediate Representation. 1, 3, 15

NIF Native Implemented Function. 9

 $\bf REPL$ Read-Eval-Print-Loop. 5

SMT Satisfiability Modulo Theories. 1, 3, 5, 9, 10, 12, 13, 15

"Computing without a computer," said the president impatiently, "is a contradiction in terms." $\[$

"Computing," said the congressman,
"is only a system for handling data. A machine might do it, or the human brain might. Let
me give you an example." And, using the skills he had learned, he worked out sums and products
until the president, despite himself, grew interested.

"Does this always work?" "Every time, Mr. President. It is foolproof."

 ${\it Isaac~Asimov} \\ {\it The~Feeling~of~Power}$

TODO Illustration