

# Program Verification in Elixir

Master's Degree in Formal Methods and Computer Engineering

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Adrián Enríquez Ballester

Supervisor: Manuel Montenegro Montes

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Complutense University of Madrid



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# Introduction

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# Motivation

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  - Compiled to Boogie, an IR for verification
  - Verification conditions discharged by the Z3 theorem prover
  - Compiled also to other programming languages

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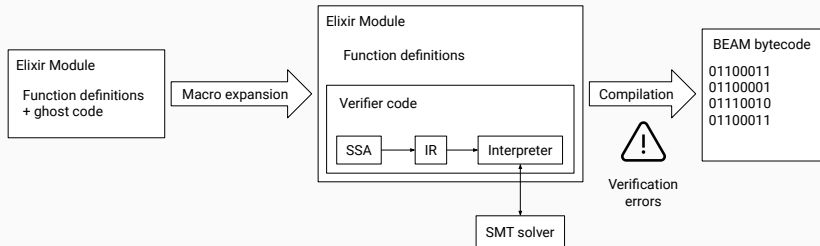
- A functional programming language that runs on the Erlang Virtual Machine
- Dynamically typed
- Suitable for developing DSLs through macros
- Main current verification approaches:
  - Dialyzer (static)
  - Property-based testing (dynamic)
  - Both of them show the presence of errors rather than their absence

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Provide a system similar to Dafny but specialized for Elixir and implemented in Elixir itself

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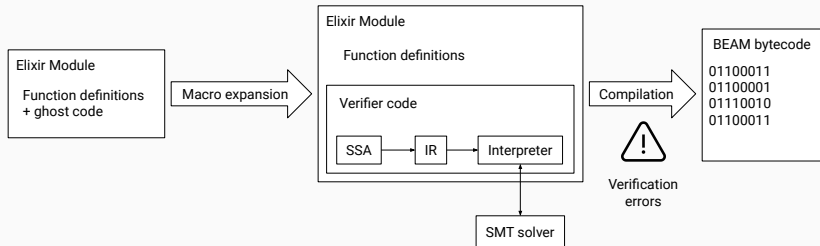


<https://github.com/adrianen-ucm/verixir-project>



# Our aim

Provide a system similar to Dafny but specialized for Elixir and implemented in Elixir itself



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Scope: only a subset of sequential Elixir for the moment, and partial verification (i.e. not verifying termination)

# A valid Elixir program

```
result =  
  if selector === 1 do  
    1  
  else  
    false  
  end
```

```
result =  
  if selector === 1 do  
    result + 1  
  else  
    not result  
  end
```



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4. L2, a high level language that models Elixir + verification annotations

# SMT Solver Integration in Elixir

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- A DSL for a subset of SMT-LIB
- Different SMT solvers that implement SMT-LIB can be easily integrated
- Out-of-the-box support for Z3

## Elixir SMT-LIB binding example

```
import SmtLib

with_local_conn do
  declare_const x: Int,
               y: Int

  assert !(
    (:x + 3 <= :y + 3) ~> (:x <= :y)
  )

  check_sat
end
```

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- The lowest level language of our verification stack
- Close to the SMT solver
- Restricted SMT-LIB + control flow + failure

$\text{Exp}^0 \ni \epsilon ::=$

- skip**
- fail**
- $\epsilon_1; \epsilon_2$
- local**  $\epsilon$
- add**  $\varphi$
- declare**  $x$
- when-unsat**  $\epsilon_1$  **do**  $\epsilon_2$  **else**  $\epsilon_3$

$$\begin{array}{lcl} \mathbf{Exp}^0 \ni \epsilon & ::= & \mathbf{skip} \\ & | & \mathbf{fail} \\ & | & \epsilon_1; \epsilon_2 \\ & | & \mathbf{local} \ \epsilon \\ & | & \mathbf{add} \ \varphi \\ & | & \mathbf{declare} \ x \\ & | & \mathbf{when-unsat} \ \epsilon_1 \ \mathbf{do} \ \epsilon_2 \ \mathbf{else} \ \epsilon_3 \end{array}$$

where  $x \in V$  is a variable name and  $\varphi \in \mathbb{F}$  is a formula with many-sorted terms  $t \in \mathbb{T}$

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- $(X, \Phi)$  SMT solver state
- $\langle \epsilon, X, \Phi \rangle \Downarrow (X', \Phi')$  judgement

$$\frac{}{\langle \text{skip}, X, \Phi \rangle \Downarrow (X, \Phi)}$$

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## L0 big-step operational semantics

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$$\frac{\langle \epsilon_1, X, \Phi \rangle \Downarrow (X', \Phi') \quad \langle \epsilon_2, X', \Phi' \rangle \Downarrow (X'', \Phi'')}{\langle \epsilon_1; \epsilon_2, X, \Phi \rangle \Downarrow (X'', \Phi')}$$

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$$\frac{\langle \epsilon_1, X, \Phi \rangle \Downarrow (X', \Phi') \quad \neg \textit{unsat}(\Phi') \quad \langle \epsilon_3, X, \Phi \rangle \Downarrow (X'', \Phi'')}{\langle \mathbf{when-unsat} \ \epsilon_1 \ \mathbf{do} \ \epsilon_2 \ \mathbf{else} \ \epsilon_3, X, \Phi \rangle \Downarrow (X'', \Phi')}$$



## L0 Elixir example

```
eval conn do
  declare_const :x

  when_unsat add :x != :x do
    skip # Does not reach fail
  else
    fail
  end
end
```

## L0 Elixir example

```
eval conn do
  declare_const :x

  when_unsat add :x == :x do
    skip
  else
    fail # Reaches fail
  end
end
```

# Intermediate Representation for Verification

---



- IR for Verification

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- Statements for writing verification annotations (ghost code)

$$\begin{array}{lcl} \mathbf{Exp}^1 \ni e & ::= & c \\ & | & x \\ & | & e_1 \mathbf{and} e_2 \\ & | & e_1 \mathbf{or} e_2 \\ & | & [] \\ & | & [e_1 \mid e_2] \\ & | & \{e_1, \dots, e_n\} \\ & | & f(e_1, \dots, e_n) \end{array}$$



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where  $c$  is a constant literal of a simple type, currently integer or boolean, and  $f \in \Sigma^1$  a function name

**Stm**  $\ni S$  ::= **skip**  
                  | **block**  $S$   
                  | **havoc**  $x$   
                  |  $S_1; S_2$   
                  | **assume**  $e$   
                  | **assert**  $e$   
                  | **unfold**  $f(e_1, \dots, e_n)$

## Built-in SMT-LIB declarations

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```
(declare-sort Term 0)
(declare-sort Type 0)
...
(declare-const int Type)
(declare-const bool Type)
(assert (distinct int bool))
...
(declare-fun type (Term) Type)
(define-fun is_integer ((x Term)) Bool
  (= (type x) int)
)
...
```

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$$\}$$

There could be more for other types (e.g. float)

## Translation from L1 into L0

$$\begin{aligned} trExp \llbracket - \rrbracket &: \mathbf{Exp}^0 \times \mathbf{Exp}^1 \rightarrow \mathbf{Exp}^0 \times \mathbb{T} \\ trStm \llbracket - \rrbracket &: \mathbf{Stm} \rightarrow \mathbf{Exp}^0 \end{aligned}$$



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$trExp \gamma \llbracket e \rrbracket$  returns a tuple  $(\epsilon, t)$  where

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- $\epsilon$  is an L0 expression that models the semantics of  $e$
- $t$  is a term in the underlying logic to refer to the result of  $e$
- $\gamma$  models known facts by the time  $e$  is evaluated

## Translation of L1 lists

$trExp \text{ - } \llbracket [] \rrbracket \equiv (\mathbf{skip}, nil)$

$trExp \gamma \llbracket [e_1 \mid e_2] \rrbracket \equiv (\epsilon_1; \epsilon_2; \epsilon, t)$

**where**  $(\epsilon_1, t_1) = trExp \gamma \llbracket e_1 \rrbracket$

$(\epsilon_2, t_2) = trExp \gamma \llbracket e_2 \rrbracket$

$t = cons(t_1, t_2)$

$\epsilon = \left[ \begin{array}{l} \mathbf{add} \text{ is-nonempty-list}(t); \\ \mathbf{add} \text{ hd}(t) = t_1; \\ \mathbf{add} \text{ tl}(t) = t_2 \end{array} \right]$

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**Remember:** the constants and functions involved in the result of the translation must be defined in the SMT prelude. For example:

```
(declare-const nil Term)
(declare-fun cons (Term Term) Term)
```

# L1 Elixir example

```
import Boogiex

with_local_env do
  assert (false or 2) === 2
  assert elem({1, 2, 3}, 0) === 1
  assert true or true + true

  havoc x
  assert x === x
  assert not (x !== x)
end
```

# Elixir Code Verification

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# The L2 language

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- A subset of Elixir + ghost verification annotations

```
Exp2  $\ni$  E ::= e
      | P = E
      | empty
      | E1; E2
      | case E do
          P1 when f1 → E1
          ⋮
          Pn when fn → En
      | end
      | ghost do S end
```

$$\begin{array}{lcl} \mathbf{Exp}^2 \ni E & ::= & e \\ & | & P = E \\ & | & \mathbf{empty} \\ & | & E_1; E_2 \\ & | & \mathbf{case } E \mathbf{ do} \\ & & \quad P_1 \mathbf{ when } f_1 \rightarrow E_1 \\ & & \quad \vdots \\ & & \quad P_n \mathbf{ when } f_n \rightarrow E_n \\ & & \mathbf{end} \\ & | & \mathbf{ghost do } S \mathbf{ end} \end{array}$$

where  $P, P_1, \dots, P_n$  are patterns:

$$\mathbf{Pat} \ni P ::= c \mid x \mid [] \mid [P_1 \mid P_2] \mid \{P_1, \dots, P_n\}$$

$$\begin{aligned} trEXP \llbracket - \rrbracket &: \mathbf{Exp}^2 \rightarrow [\mathbf{Stm} \times \mathbf{Exp}^1] \\ trMatch \llbracket - \rrbracket \llbracket - \rrbracket &: \mathbf{Exp}^1 \times \mathbf{Pat} \rightarrow \mathbf{Exp}^1 \end{aligned}$$

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$trEXP \llbracket E \rrbracket$  generates a sequence of pairs  $(S, e)$  where

- $S$  is an L1 statement that models the semantics of  $E$



## Translation from L2 into L1

$$\begin{aligned} trEXP \llbracket - \rrbracket &: \mathbf{Exp}^2 \rightarrow [\mathbf{Stm} \times \mathbf{Exp}^1] \\ trMatch \llbracket - \rrbracket \llbracket - \rrbracket &: \mathbf{Exp}^1 \times \mathbf{Pat} \rightarrow \mathbf{Exp}^1 \end{aligned}$$

$trEXP \llbracket E \rrbracket$  generates a sequence of pairs  $(S, e)$  where

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- $S$  is an L1 statement that models the semantics of  $E$
- $e$  is an L1 expression that represents the result to which  $E$  is evaluated
- Each pair corresponds to an execution path

## Translation of L2 lists pattern matching

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$$\begin{aligned} trMatch \llbracket e \rrbracket \llbracket [P_1 \mid P_2] \rrbracket = \\ is-nelist(e) \text{ and} \\ trMatch \llbracket hd(e) \rrbracket \llbracket P_1 \rrbracket \text{ and} \\ trMatch \llbracket tl(e) \rrbracket \llbracket P_2 \rrbracket \end{aligned}$$

## Translation of L2 pattern matching expressions

$trEXP \llbracket P = E \rrbracket = [(S_1; S'_1, e_1), \dots, (S_n; S'_n, e_n)]$

**where**  $[(S_1, e_1), \dots, (S_n, e_n)] = trEXP \llbracket E \rrbracket$

$\{y_1, \dots, y_m\} = vars(P)$

$\forall i \in \{1..n\} : S'_i = \left( \begin{array}{l} \mathbf{assert} \ trMatch \llbracket e_i \rrbracket \llbracket P \rrbracket; \\ \mathbf{havoc} \ y_1; \\ \vdots \\ \mathbf{havoc} \ y_m; \\ \mathbf{assume} \ e_i == P \end{array} \right)$

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Clauses of a function  $f$  with arity  $n$ :

$$Defs(f/n) = (def_1, \dots, def_k)$$



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**Note:** our formalization does not address currently the verification of user-defined function invocations (i.e. their specifications and body unfolding), but our implementation does it by automatically generating ghost code

Live demo



## Conclusions

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  - The current implementation is in an early proof of concept stage

# Program Verification in Elixir

Master's Degree in Formal Methods and Computer Engineering

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Adrián Enríquez Ballester

Supervisor: Manuel Montenegro Montes

July 7, 2022

Complutense University of Madrid

