

Program Verification in Elixir

Master's Degree in Formal Methods and Computer Engineering

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Introduction

Motivation

- Light-weight program verification systems:

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- Dafny:
 - Specify code with pre/post conditions
 - Compiled to Boogie, a verification IR
 - Verification conditions discharged by the Z3 theorem prover
 - Compiled also to other programming languages to be executed

The Elixir programming language

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The Elixir programming language

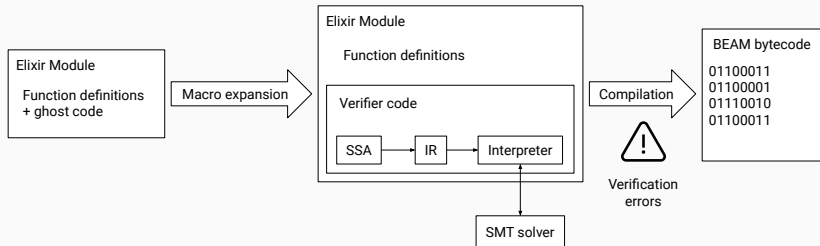
- A functional programming language that runs on the Erlang Virtual Machine
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- Suitable for developing DSLs through macros
- Main current verification approaches:
 - Dialyzer (static)
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 - Both of them show the presence of errors rather than their absence

Our aim

Provide a system similar to that of Dafny but specialized for Elixir and implemented in Elixir itself

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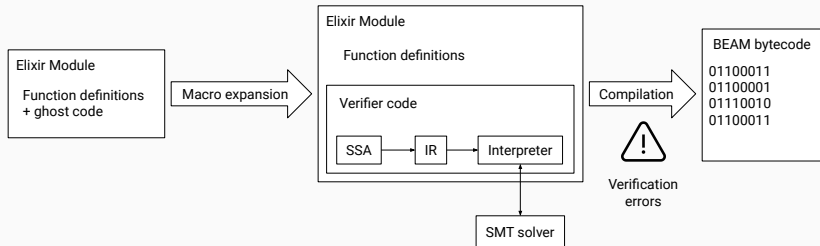
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Scope: only a subset of sequential Elixir for the moment, and partial verification (i.e. not verifying termination)

1. SMT solver integration in Elixir

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2. L0, a low level language close to the SMT solver

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4. L2, a high level language that models Elixir + verification code

SMT Solver Integration in Elixir

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- An SMT-LIB (subset) DSL
- Different SMT solvers can be easily integrated
- Out-of-the-box support for Z3

Elixir SMT-LIB binding example

```
import SmtLib

with_local_conn do
  declare_const x: Int,
               y: Int

  assert !(
    (:x + 3 <= :y + 3) ~> (:x <= :y)
  )

  check_sat
end
```

The L0 language

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- The lowest level language of our verification stack
- Close to the SMT solver
- Restricted SMT-LIB + control flow + failure

$\text{Exp}^0 \ni \epsilon ::=$

- skip**
- fail**
- $\epsilon_1; \epsilon_2$
- local** ϵ
- add** φ
- declare** x
- when-unsat** ϵ_1 **do** ϵ_2 **else** ϵ_3

$$\begin{array}{lcl} \mathbf{Exp}^0 \ni \epsilon & ::= & \mathbf{skip} \\ & | & \mathbf{fail} \\ & | & \epsilon_1; \epsilon_2 \\ & | & \mathbf{local} \ \epsilon \\ & | & \mathbf{add} \ \varphi \\ & | & \mathbf{declare} \ x \\ & | & \mathbf{when-unsat} \ \epsilon_1 \ \mathbf{do} \ \epsilon_2 \ \mathbf{else} \ \epsilon_3 \end{array}$$

where $x \in V$ is a variable name and $\varphi \in \mathbb{F}$ is a formula with many-sorted terms $t \in \mathbb{T}$

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- $\langle \epsilon, X, \Phi \rangle \Downarrow (X', \Phi')$ judgement

$$\frac{}{\langle \text{skip}, X, \Phi \rangle \Downarrow (X, \Phi)}$$

$$\frac{}{\langle \mathbf{skip}, X, \Phi \rangle \Downarrow (X, \Phi)}$$

$$\frac{\varphi \in \mathbb{F}(X)}{\langle \mathbf{add} \ \varphi, X, \Phi \rangle \Downarrow (X, \Phi \cup \{\varphi\})}$$

L0 big-step operational semantics

$$\frac{}{\langle \text{skip}, X, \Phi \rangle \Downarrow (X, \Phi)}$$

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$$\frac{\langle \epsilon_1, X, \Phi \rangle \Downarrow (X', \Phi') \quad \langle \epsilon_2, X', \Phi' \rangle \Downarrow (X'', \Phi'')}{\langle \epsilon_1; \epsilon_2, X, \Phi \rangle \Downarrow (X'', \Phi')}$$

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$$\frac{\langle \epsilon_1, X, \Phi \rangle \Downarrow (X', \Phi') \quad \text{unsat}(\Phi') \quad \langle \epsilon_2, X, \Phi \rangle \Downarrow (X'', \Phi'')}{\langle \mathbf{when-unsat} \ \epsilon_1 \ \mathbf{do} \ \epsilon_2 \ \mathbf{else} \ \epsilon_3, X, \Phi \rangle \Downarrow (X'', \Phi')}$$

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L0 Elixir implementation

A simple implementation in Elixir is straightforward by using our SMT-LIB binding

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```
defmacro eval(conn, {:local, _, [e]}) do
  quote do
    conn = unquote(conn)
    :ok = push conn
    eval conn, unquote(e)
    :ok = pop conn
  end
end
```

L0 Elixir example

```
eval conn do
  declare_const :x

  when_unsat add :x != :x do
    skip # Does not reach fail
  else
    fail
  end
end
```


L0 Elixir example

```
eval conn do
  declare_const :x

  when_unsat add :x == :x do
    skip
  else
    fail # Reaches fail
  end
end
```

Verification Intermediate Representation

The L1 language

- Verification IR

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- It models Elixir expressions dynamically typed
- Statements for writing verification code

$$\begin{array}{lcl} \mathbf{Exp}^1 \ni e & ::= & c \\ & | & x \\ & | & e_1 \mathbf{and} e_2 \\ & | & e_1 \mathbf{or} e_2 \\ & | & [] \\ & | & [e_1 \mid e_2] \\ & | & \{e_1, \dots, e_n\} \\ & | & f(e_1, \dots, e_n) \end{array}$$

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where c is a constant literal of a simple type, currently integer or boolean, and $f \in \Sigma^1$ a function name

Stm $\ni S$::= **skip**
 | **block** S
 | **havoc** x
 | $S_1; S_2$
 | **assume** e
 | **assert** e
 | **unfold** $f(e_1, \dots, e_n)$

Built-in SMT-LIB declarations

Foundation to represent L1 expressions in the underlying many-sorted logic

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```
(declare-sort Term 0)
(declare-sort Type 0)
...
(declare-const int Type)
(declare-const bool Type)
(assert (distinct int bool))
...
(declare-fun type (Term) Type)
(define-fun is_integer ((x Term)) Bool
  (= (type x) int)
)
...
```

Built-in L1 specifications

Built-in **sets** of pair/postconditions for functions to model their behavior in Elixir

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$$\{is_integer(x) \wedge is_integer(y)\}$$
$$x + y$$
$$\{$$
$$is_integer(\hat{+}(x, y)) \wedge$$
$$integer_value(\hat{+}(x, y)) = integer_value(x) + integer_value(y)$$
$$\}$$

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$$\}$$

There could be more for other types (e.g. float)

$$\begin{aligned} trExp \llbracket - \rrbracket &: \mathbf{Exp}^0 \times \mathbf{Exp}^1 \rightarrow \mathbf{Exp}^0 \times \mathbb{T} \\ trStm \llbracket - \rrbracket &: \mathbf{Stm} \rightarrow \mathbf{Exp}^0 \end{aligned}$$

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- t is a term in the underlying logic to refer to the result of e
- γ models known facts by the time e is evaluated

$$trExp \text{ - } \llbracket [] \rrbracket \equiv (\mathbf{skip}, nil)$$

$$trExp \gamma \llbracket [e_1 \mid e_2] \rrbracket \equiv (\epsilon_1; \epsilon_2; \epsilon, t)$$

$$\mathbf{where} \ (\epsilon_1, t_1) = trExp \gamma \llbracket e_1 \rrbracket$$

$$(\epsilon_2, t_2) = trExp \gamma \llbracket e_2 \rrbracket$$

$$t = cons(t_1, t_2)$$

$$\epsilon = \left[\begin{array}{l} \mathbf{add} \ is\text{-}nonempty\text{-}list(t); \\ \mathbf{add} \ hd(t) = t_1; \\ \mathbf{add} \ tl(t) = t_2 \end{array} \right]$$

Translation of L1 lists example

$trExp \ \gamma \ \llbracket [2, x] \rrbracket \equiv (\epsilon, cons(2, cons(\hat{x}, nil)))$

where $\epsilon =$

add *is-integer(integer-lit(2));*
add *integer-value(integer-lit(2)) = 2;*
add *is-nonempty-list(cons(\hat{x} , nil));*
add *hd(cons(\hat{x} , nil)) = \hat{x} ;*
add *tl(cons(\hat{x} , nil)) = nil;*
add *is-nonempty-list(cons(2, cons(\hat{x} , nil)));*
add *hd(cons(2, cons(\hat{x} , nil))) = 2;*
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L1 Elixir implementation

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```
def tr_exp(_, [{:|, _, [h, t]}]) do
  {h, h_sem} = tr_exp(_, h)
  {y, t_sem} = tr_exp(_, t)
  t =
    quote(do: :cons.(unquote(h), unquote(t)))

  { t, quote do
    unquote(h_sem)
    unquote(t_sem)
    add :is_nonempty_list.(unquote(t))
    add :hd.(unquote(t)) == unquote(h)
    add :tl.(unquote(t)) == unquote(t)
  end }
end
```

L1 Elixir example

```
import Boogiex

with_local_env do
  assert (false or 2) === 2
  assert elem({1, 2, 3}, 0) === 1
  assert true or true + true

  havoc x
  assert x === x
  assert not (x !== x)
end
```


Elixir Code Verification

The L2 language

- The highest level language of our verification stack

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- Elixir (subset) + ghost verification code

```
Exp2  $\ni$  E ::= e
                | P = E
                | empty
                | E1; E2
                | case E do
                    P1 when f1 → E1
                    ⋮
                    Pn when fn → En
                | end
                | ghost do S end
```

$$\begin{array}{lcl} \mathbf{Exp}^2 \ni E & ::= & e \\ & | & P = E \\ & | & \mathbf{empty} \\ & | & E_1; E_2 \\ & | & \mathbf{case } E \mathbf{ do} \\ & & P_1 \mathbf{ when } f_1 \rightarrow E_1 \\ & & \vdots \\ & & P_n \mathbf{ when } f_n \rightarrow E_n \\ & & \mathbf{end} \\ & | & \mathbf{ghost do } S \mathbf{ end} \end{array}$$

where P, P_1, \dots, P_n are patterns:

$$\mathbf{Pat} \ni P ::= c \mid x \mid [] \mid [P_1 \mid P_2] \mid \{P_1, \dots, P_n\}$$

$$\begin{aligned} trEXP \llbracket - \rrbracket &: \mathbf{Exp}^2 \rightarrow [\mathbf{Stm} \times \mathbf{Exp}^1] \\ trMatch \llbracket - \rrbracket \llbracket - \rrbracket &: \mathbf{Exp}^1 \times \mathbf{Pat} \rightarrow \mathbf{Exp}^1 \end{aligned}$$

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- S is an L1 statement that models the semantics of E
- e is an L1 expression that represents the result to which E is evaluated
- Each pair corresponds to an execution path

Translation of L2 lists pattern matching

$trMatch \llbracket e \rrbracket \llbracket P \rrbracket$ returns an L1 expression that is a *boolean* term and is evaluated to *true* if and only if e matches P

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$$\begin{aligned} trMatch \llbracket e \rrbracket \llbracket [P_1 \mid P_2] \rrbracket = \\ is-nelist(e) \textbf{ and } \\ trMatch \llbracket hd(e) \rrbracket \llbracket P_1 \rrbracket \textbf{ and } \\ trMatch \llbracket tl(e) \rrbracket \llbracket P_2 \rrbracket \end{aligned}$$

Translation of L2 pattern matching expressions

$trEXP \llbracket P = E \rrbracket = [(S_1; S'_1, e_1), \dots, (S_n; S'_n, e_n)]$

where $[(S_1, e_1), \dots, (S_n, e_n)] = trEXP \llbracket E \rrbracket$

$\{y_1, \dots, y_m\} = vars(P)$

$\forall i \in \{1..n\} : S'_i = \left(\begin{array}{l} \mathbf{assert} \ trMatch \llbracket e_i \rrbracket \llbracket P \rrbracket; \\ \mathbf{havoc} \ y_1; \\ \vdots \\ \mathbf{havoc} \ y_m; \\ \mathbf{assume} \ e_i == P \end{array} \right)$

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A single clause of a function with arity n :

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Clauses of a function f with arity n :

$$Defs(f/n) = (def_1, \dots, def_k)$$

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Note: our formalization does not address currently the verification of user-defined function invocations (i.e. their specifications and body unfolding), but our implementation does it by automatically generating ghost code.

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```
def tr_match({:|, _, [p1, p2]}, e) do
  tr_1 =
    tr_match(p1, quote(do: hd(unquote(e))))
  tr_2 =
    tr_match(p2, quote(do: tl(unquote(e))))

  quote(do:
    is_list(unquote(e)) and
    unquote(e) != [] and
    unquote(tr_1) and unquote(tr_2)
  )
end
```

Live demo

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- We have developed a framework for Elixir code verification across several areas (i.e. SMT solver integration, verification IR and code verification)
- Future work may address concurrent code and total verification
- Also, we have left several improvements on the way:
 - More of the SMT-LIB standard and SMT solvers support
 - Extend our IR to model more Elixir value types and built-in functions

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- We have developed a framework for Elixir code verification across several areas (i.e. SMT solver integration, verification IR and code verification)
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 - The current implementation is in an early proof of concept stage

Program Verification in Elixir

Master's Degree in Formal Methods and Computer Engineering

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