



JULY 7, 2025

REAL LIFE GAMES:
HOW GAME THEORY SHAPES HUMAN
DECISIONS

THE GAME THEORY OF COOPERATION

PUBLIC GOODS GAMES & SOCIAL NORMS

Adrian Haret
a.haret@lmu.de

Let's play a game!

A PUBLIC GOODS GAME

Players start out with an *endowment*, or *budget*.

Each contributes a fraction of their endowment.

Contributions are pooled, multiplied by 1.5, and the result is divided equally among the players.

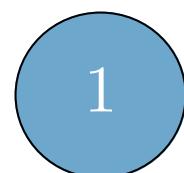
The original endowment, minus the contribution, plus the amount earned becomes the budget for the next round.

Starting with round 3, players have the option of imposing penalties: they give up x points to penalize a player of their choice by $2x$ points.

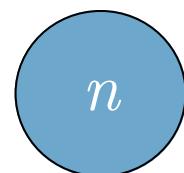
Player who finishes the game with the most points is the winner.

PUBLIC GOODS GAMES: THE MODEL

There is a set $N = \{1, \dots, n\}$ of *players*.



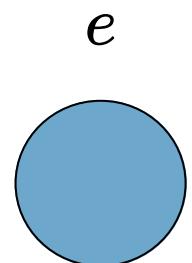
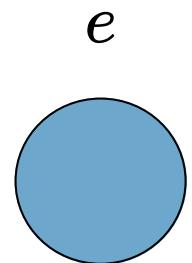
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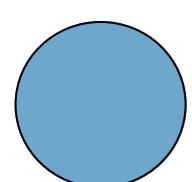
PUBLIC GOODS GAMES: THE MODEL

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Each player i starts with an *endowment* e



...

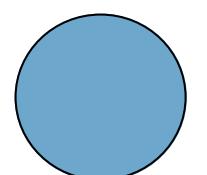


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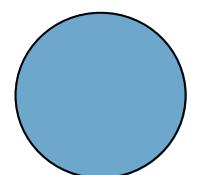
There is a set $N = \{1, \dots, n\}$ of *players*.

Each player i starts with an *endowment* e and makes a *contribution* $c_i \in [0, e]$.

$$e - c_1$$

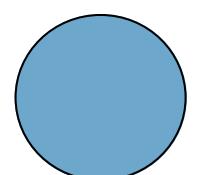


$$e - c_2$$



...

$$e - c_n$$



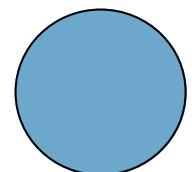
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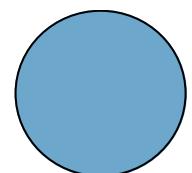
Each player i starts with an *endowment* e and makes a *contribution* $c_i \in [0, e]$.

The *public good* is obtained by pooling all contributions

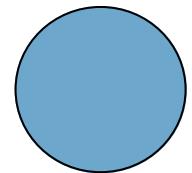
$$e - c_1 + c_1 + c_2 + \cdots + c_n$$



$$e - c_2 + c_1 + c_2 + \cdots + c_n$$



$$e - c_n + c_1 + c_2 + \cdots + c_n$$



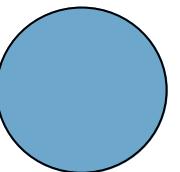
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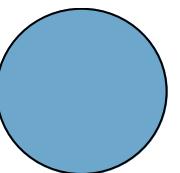
Each player i starts with an *endowment* e and makes a *contribution* $c_i \in [0, e]$.

The *public good* is obtained by pooling all contributions, and multiplying them by a constant $r > 1$.

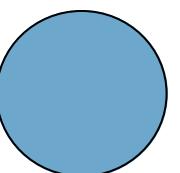
$$e - c_1 + r \cdot c_1 + c_2 + \cdots + c_n$$



$$e - c_2 + r \cdot c_1 + c_2 + \cdots + c_n$$



$$\cdots e - c_n + r \cdot c_1 + c_2 + \cdots + c_n$$



PUBLIC GOODS GAMES: THE MODEL

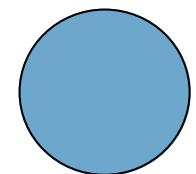
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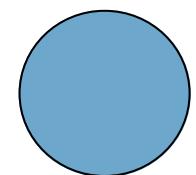
The *public good* is obtained by pooling all contributions, and multiplying them by a constant $r > 1$.

Each player receives an equal share of the public good.

$$e - c_1 + r \cdot \frac{c_1 + c_2 + \cdots + c_n}{n}$$

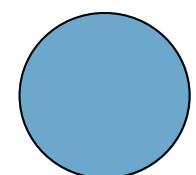


$$e - c_2 + r \cdot \frac{c_1 + c_2 + \cdots + c_n}{n}$$



$$\cdots$$

$$e - c_n + r \cdot \frac{c_1 + c_2 + \cdots + c_n}{n}$$

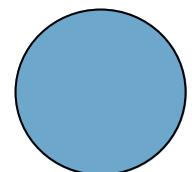


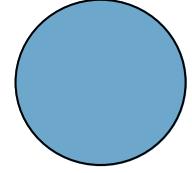
What are the equilibria?

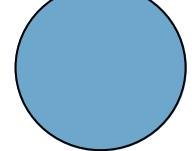
PUBLIC GOODS GAMES: BEST RESPONSES

If player i contributes $c_i > 0$, they make:

$$e - c_i + r \cdot \frac{\sum_{j \neq i} c_j + c_i}{n}.$$

$$e - c_1 + r \cdot \frac{c_1 + c_2 + \cdots + c_n}{n}$$


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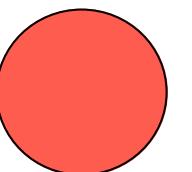
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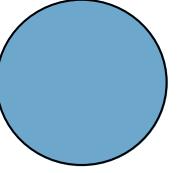
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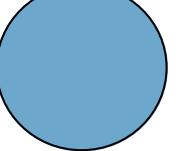
$$e - c_i + r \cdot \frac{\sum_{j \neq i} c_j + c_i}{n}.$$

If player i lowers their contribution to $c'_i < c_i$, while everyone else keeps their contribution constant, they make:

$$e - c'_i + r \cdot \frac{\sum_{j \neq i} c_j + c'_i}{n}.$$

$$e - c'_i + r \cdot \frac{c'_1 + c_2 + \cdots + c_n}{n}$$


$$e - c_2 + r \cdot \frac{0 + c_2 + \cdots + c_n}{n}$$


$$e - c_n + r \cdot \frac{0 + c_2 + \cdots + c_n}{n}$$


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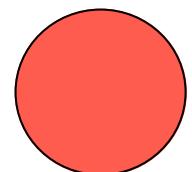
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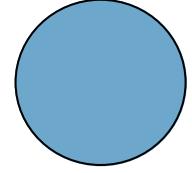
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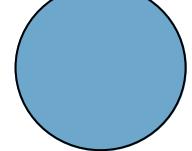
$$e - c'_i + r \cdot \frac{\sum_{j \neq i} c_j + c'_i}{n}.$$

Lowering the contribution is worth it just in case:

$$e - c'_i + r \cdot \frac{\sum_{j \neq i} c_j + c'_i}{n} > e - c_i + r \cdot \frac{\sum_{j \neq i} c_j + c_i}{n} \quad \text{iff}$$

$$e - c'_i + r \cdot \frac{c'_1 + c_2 + \dots + c_n}{n}$$


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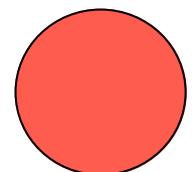
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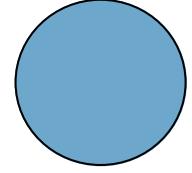
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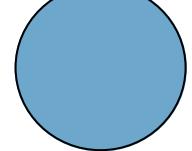
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$$c_i - c'_i > r \cdot \frac{c_i - c'_i}{n} \quad \text{iff}$$

$$e - c'_i + r \cdot \frac{c'_1 + c_2 + \dots + c_n}{n}$$


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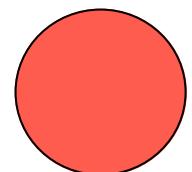
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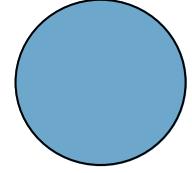
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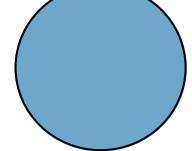
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$$\begin{aligned} c_i - c'_i &> r \cdot \frac{c_i - c'_i}{n} \\ n &> r. \end{aligned} \quad \text{iff}$$

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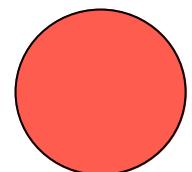
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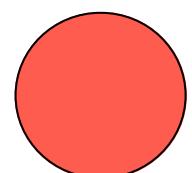
PUBLIC GOODS GAMES: BEST RESPONSES

If everyone contributes 0, there is no public good and each player is stuck with their initial endowment e .

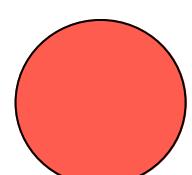
$$e - 0 + r \cdot \frac{0 + 0 + \cdots + 0}{n}$$



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$$e - 0 + r \cdot \frac{\overset{\cdots}{0} + 0 + \cdots + 0}{n}$$



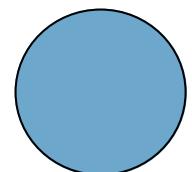
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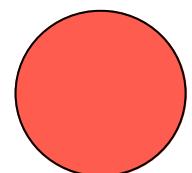
In this situation, if a player i decides to deviate and contribute $c_i > 0$, they make:

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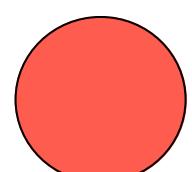
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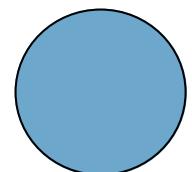
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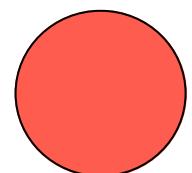
In this situation, if a player i decides to deviate and contribute $c_i > 0$, they make:

$$e - c_i + r \cdot \frac{c_i}{n} < e, \quad \text{as long as } r < n.$$

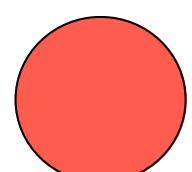
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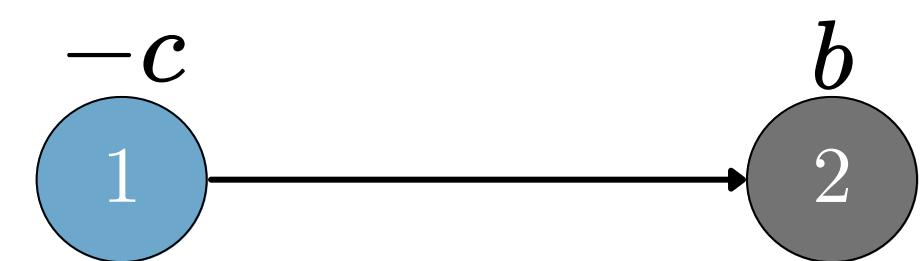


So there is one equilibrium, where no one contributes and the public good is not provisioned.

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PUBLIC GOODS GAMES & PRISONER'S DILEMMAS

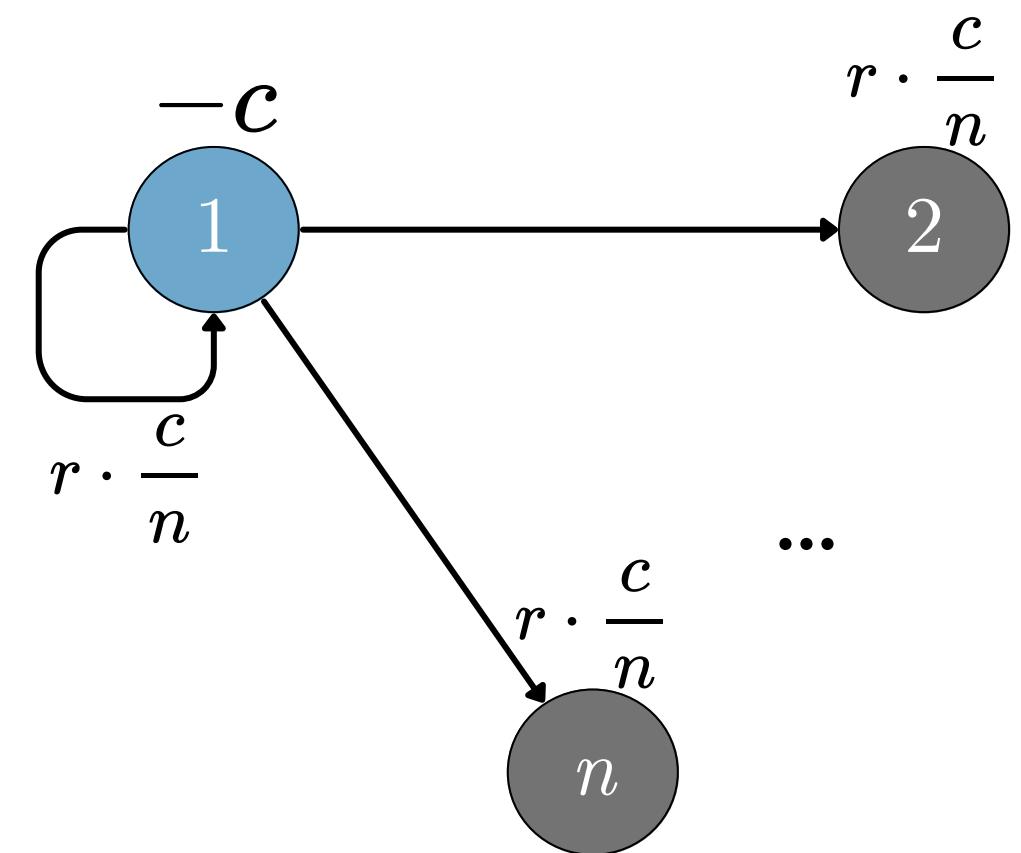
In a Prisoner's Dilemma a cooperator pays a cost to provide a benefit to the other player.



PUBLIC GOODS GAMES & PRISONER'S DILEMMAS

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In a Public Goods Game, everyone gets a share of the cooperator's contribution, including the focal player themselves.

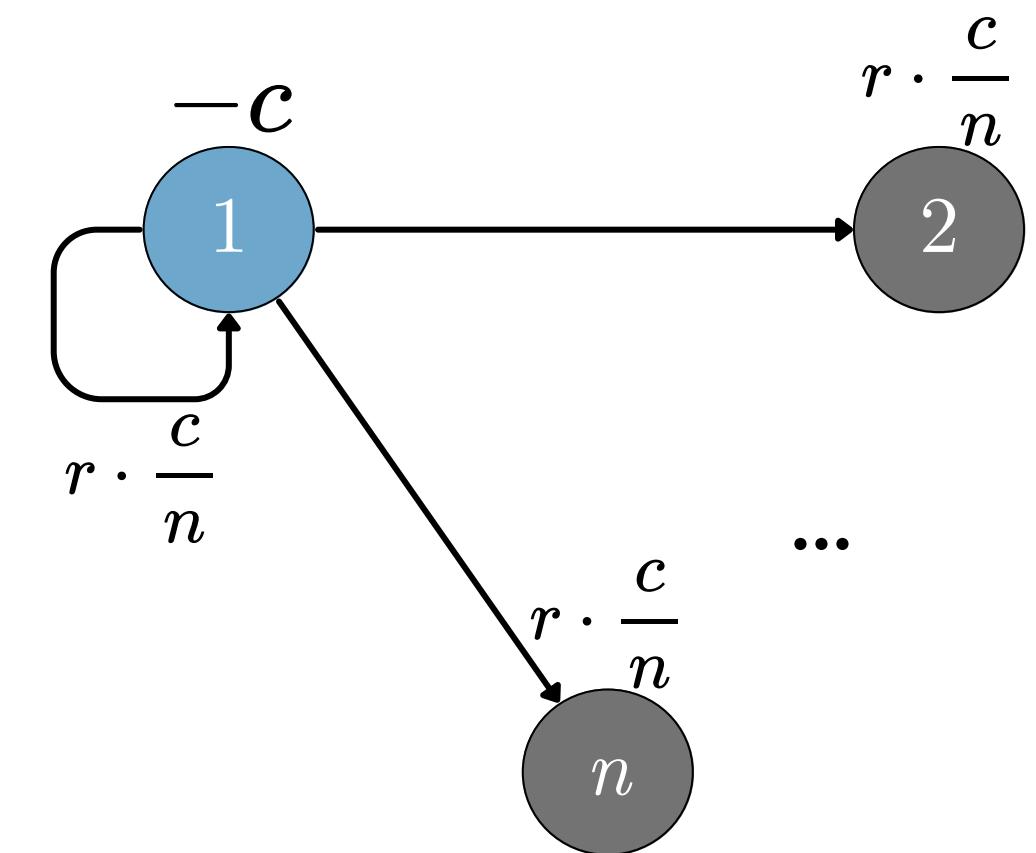


PUBLIC GOODS GAMES & PRISONER'S DILEMMAS

In a Prisoner's Dilemma a cooperator pays a cost to provide a benefit to the other player.

In a Public Goods Game, everyone gets a share of the cooperator's contribution, including the focal player themselves.

In this sense, a Public Goods Game are a more general version of a Prisoner's Dilemma.



Public goods games show up everywhere... but
do we see robust contributions?

Public goods games show up everywhere... but
do we see robust contributions? It's tricky...

Chuck Feeney

1931 - 2023



Chuck Feeney

1931 - 2023

Co-founder of Duty Free Shoppers Group.



Chuck Feeney

1931 - 2023

Co-founder of Duty Free Shoppers Group.

Gave away most of his wealth, in the billions.

Would also pick up rubbish from the street.

If everybody picked up trash, there would be no trash on the streets.



At the same time...

A polar bear stands on a small, blue-tinted ice floe in a vast, icy landscape. The bear is facing left, its mouth slightly open as if it's barking or communicating. The background shows a vast expanse of white ice and snow under a clear blue sky.

In January 2025, the US withdrew (again) from the Paris Climate Accords.

A polar bear stands on a small, blue-tinted ice floe in a vast, icy landscape. The bear is facing left, its mouth slightly open as if it's barking or communicating. The background shows more icebergs and a hazy sky.

In January 2025, the US withdrew (again) from the Paris Climate Accords. We don't know what the text chain was.

A polar bear stands on a small, blue-tinted ice floe in a vast, icy landscape. The bear is facing left, its mouth slightly open as if it's barking or communicating. The background shows more ice floes and distant snow-covered land under a clear sky.

In January 2025, the US withdrew (again) from the Paris Climate Accords. We don't know what the text chain was. But it might have looked like this...

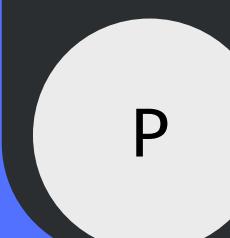
 VP

VP
Shall we commit to the goals of the Paris
Agreement and work towards reducing
emissions?

 POTUS
... P

 VP

VP
Shall we commit to the goals of the Paris Agreement and work towards reducing emissions?

 POTUS

I don't see the point, if it hurts our industry. Especially while there are other large polluters out there...

Noor, D. (2025, January 20). [Trump signs order to withdraw US from Paris climate agreement for second time](#). *The Guardian*.

The dilemma of public goods. We all prefer the good to be provided.

The dilemma of public goods. We all prefer the good to be provided. But we'd like someone else to pay for it.

The dilemma of public goods. We all prefer the good to be provided. But we'd like someone else to pay for it. Widespread freeriding, though, can be disastrous...

THE TRAGEDY OF THE COMMONS

A pasture, open to all: a commons.

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Unrestricted grazing leads to a depleted pasture,
and everyone suffers.



THE TRAGEDY OF THE COMMONS

A pasture, open to all: a *commons*.

Unrestricted grazing leads to a depleted pasture,
and everyone suffers.

But each herder wants to give their *own* livestock
as much grazing time as possible.



GARRETT HARDIN
Therein is the tragedy.

Hardin, G. (1968). The Tragedy of the Commons. *Science*, 162(3859), 1243–1248.



GARRETT HARDIN

Therein is the tragedy.

Each man is locked into a system that compels
him to increase his herd without limit—in a
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Ruin is the destination toward which all men rush, each pursuing his own best interest in a society that believes in the freedom of the commons.

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Freedom in a commons brings ruin to all.

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How do we avoid ‘ruin’? How do we get less freeriding and more Chuck Feeney-ing?



MANCUR OLSON

Unless ... there is coercion..., rational, self-interested individuals will not act to achieve their common or group interests.

Olson, M. (1971). *The Logic of Collective Action: Public Goods and the Theory of Groups*.
Harvard University Press.



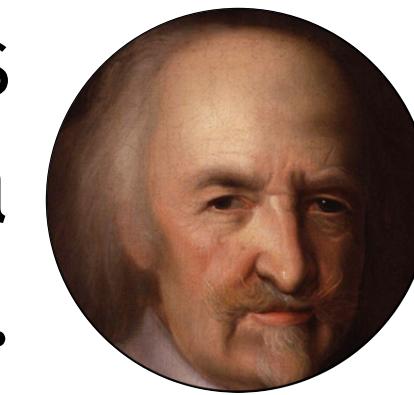
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Unless ... there is coercion..., rational, self-interested individuals will not act to achieve their common or group interests.

Olson, M. (1971). *The Logic of Collective Action: Public Goods and the Theory of Groups*. Harvard University Press.

THOMAS HOBBES

We need an external authority, a *Leviathan*, to keep people in check.

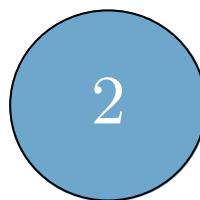
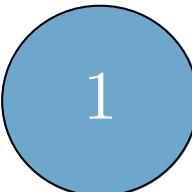


The most obvious mechanism of coercion is
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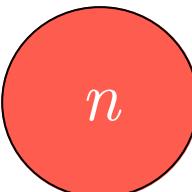
The most obvious mechanism of coercion is *punishment*. Let's model it using a simplified version of a public goods game.

PUBLIC GOODS GAMES WITH PUNISHMENT

There is a set $N = \{1, \dots, n\}$ of *players*.



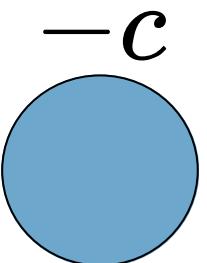
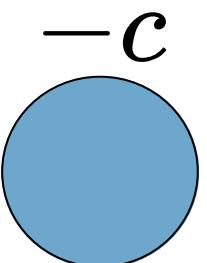
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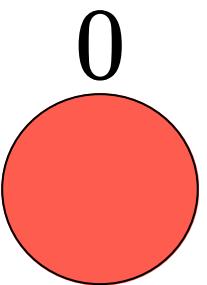
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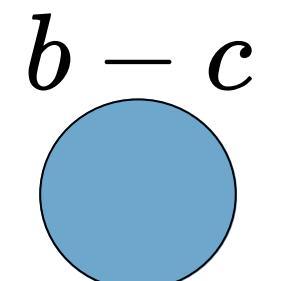
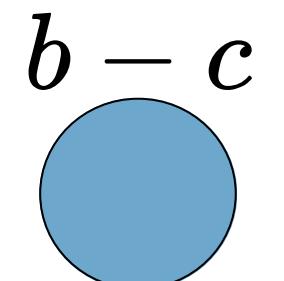


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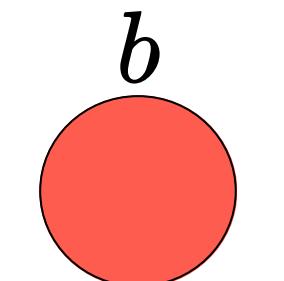
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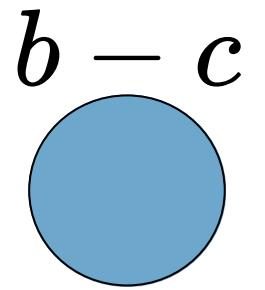
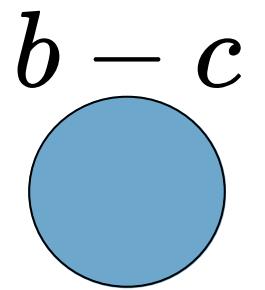
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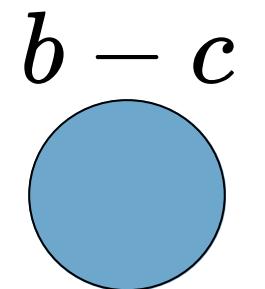
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SIDENOTE

As long as the public good is provided, at this point each player has an incentive to freeride.



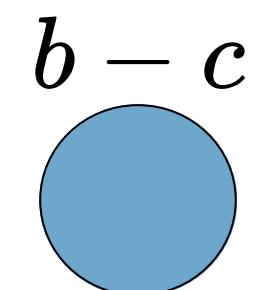
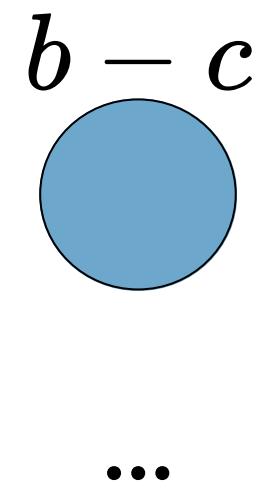
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Widespread cooperation is, again, not an equilibrium.

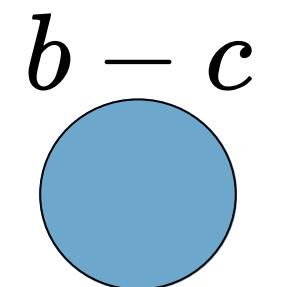
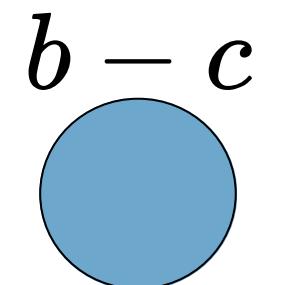


PUBLIC GOODS GAMES WITH PUNISHMENT

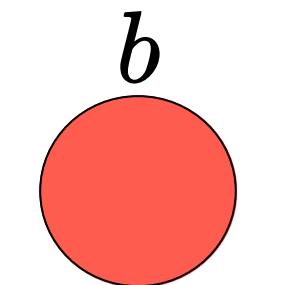
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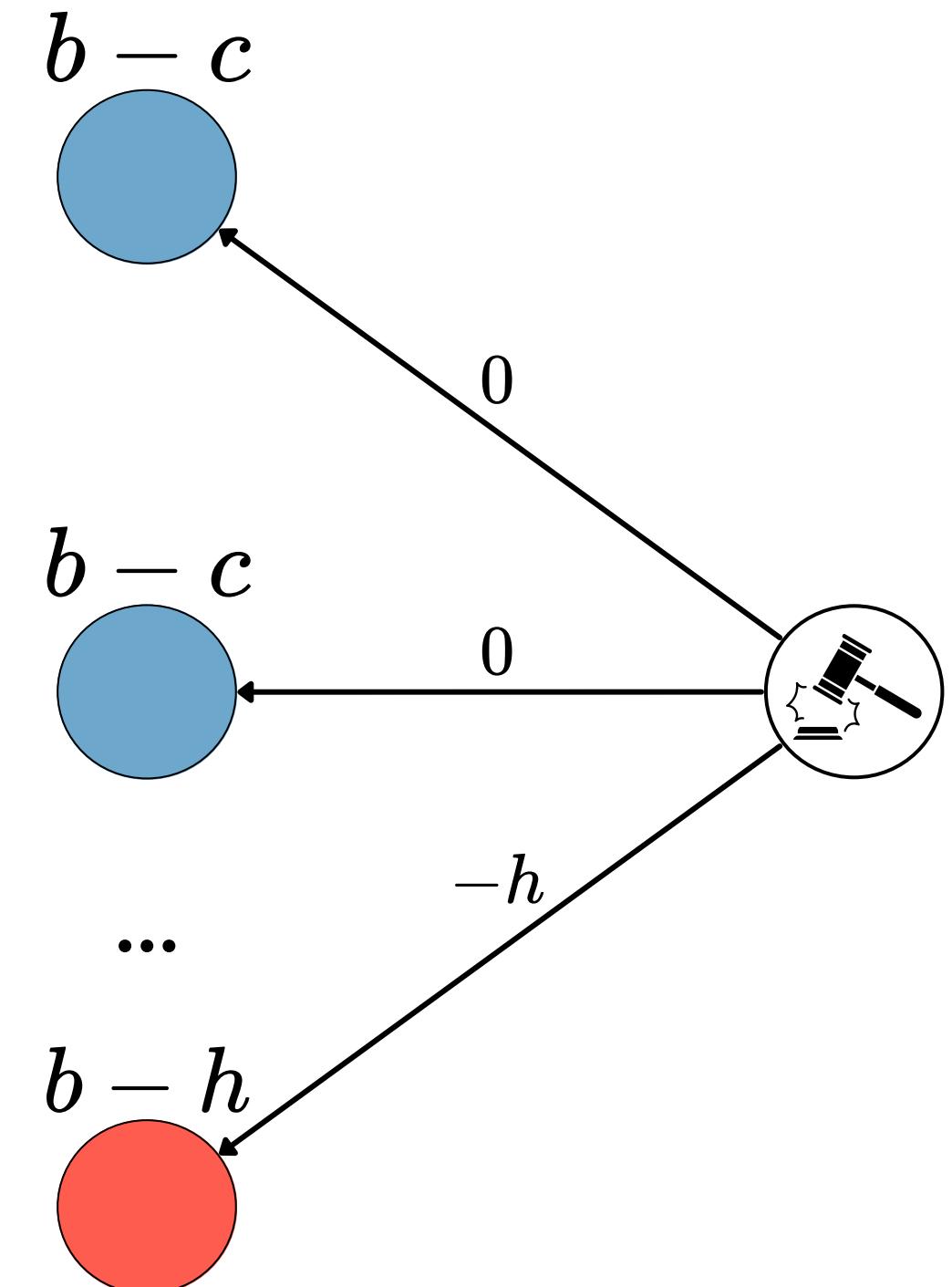
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At the second round an authority imposes a penalty h to non-contributors.

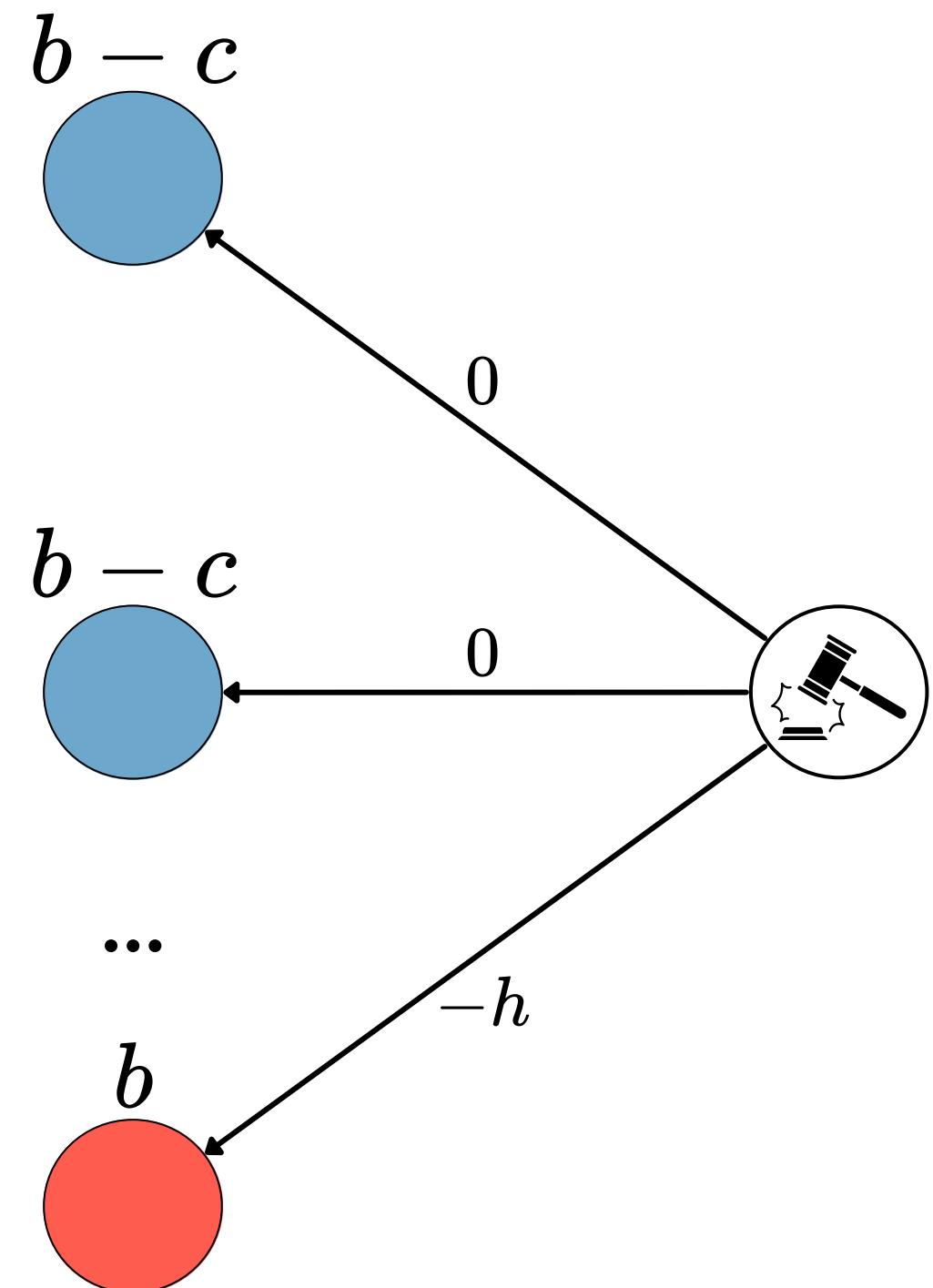
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Now universal cooperation can be an equilibrium!

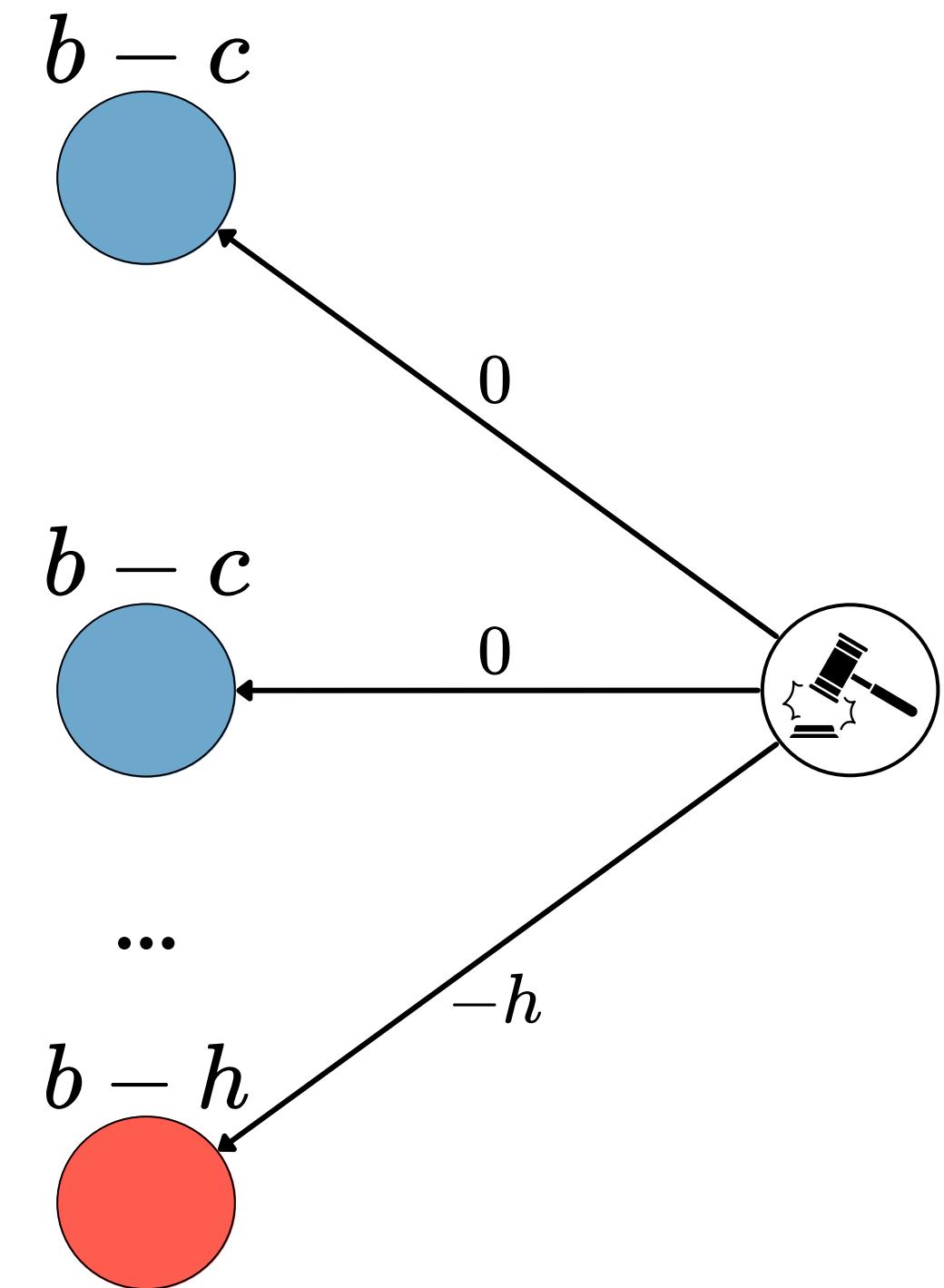
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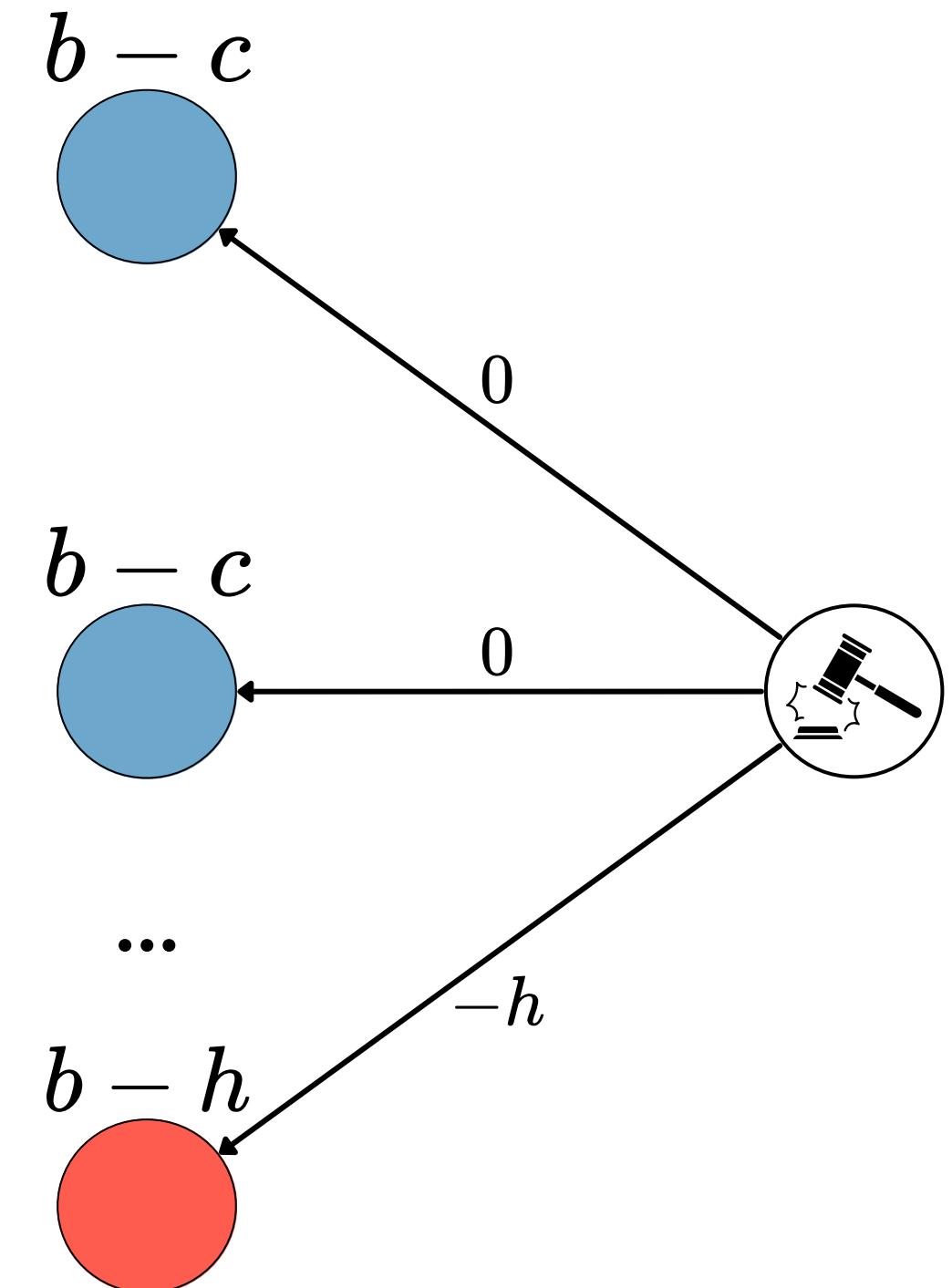


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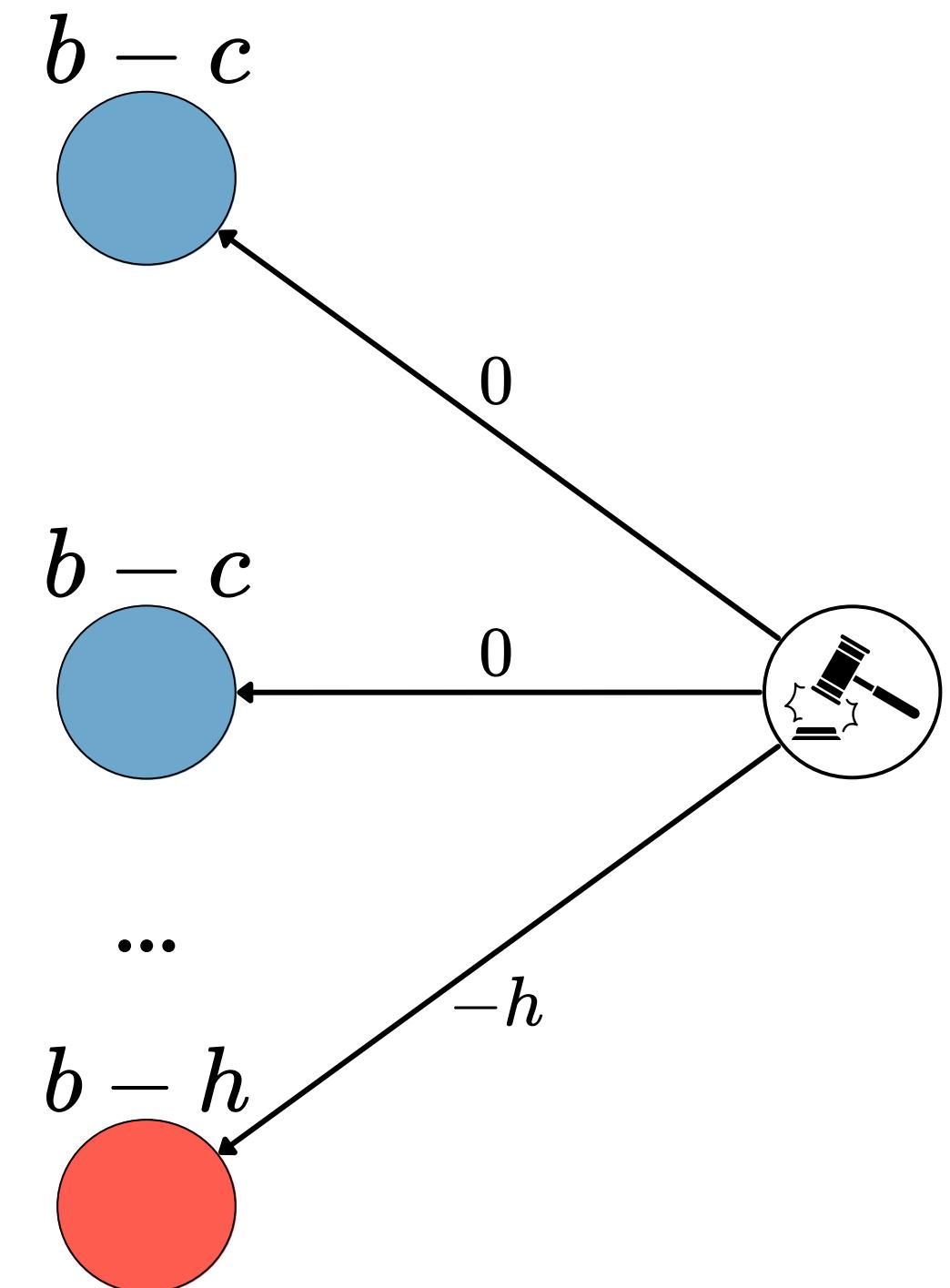
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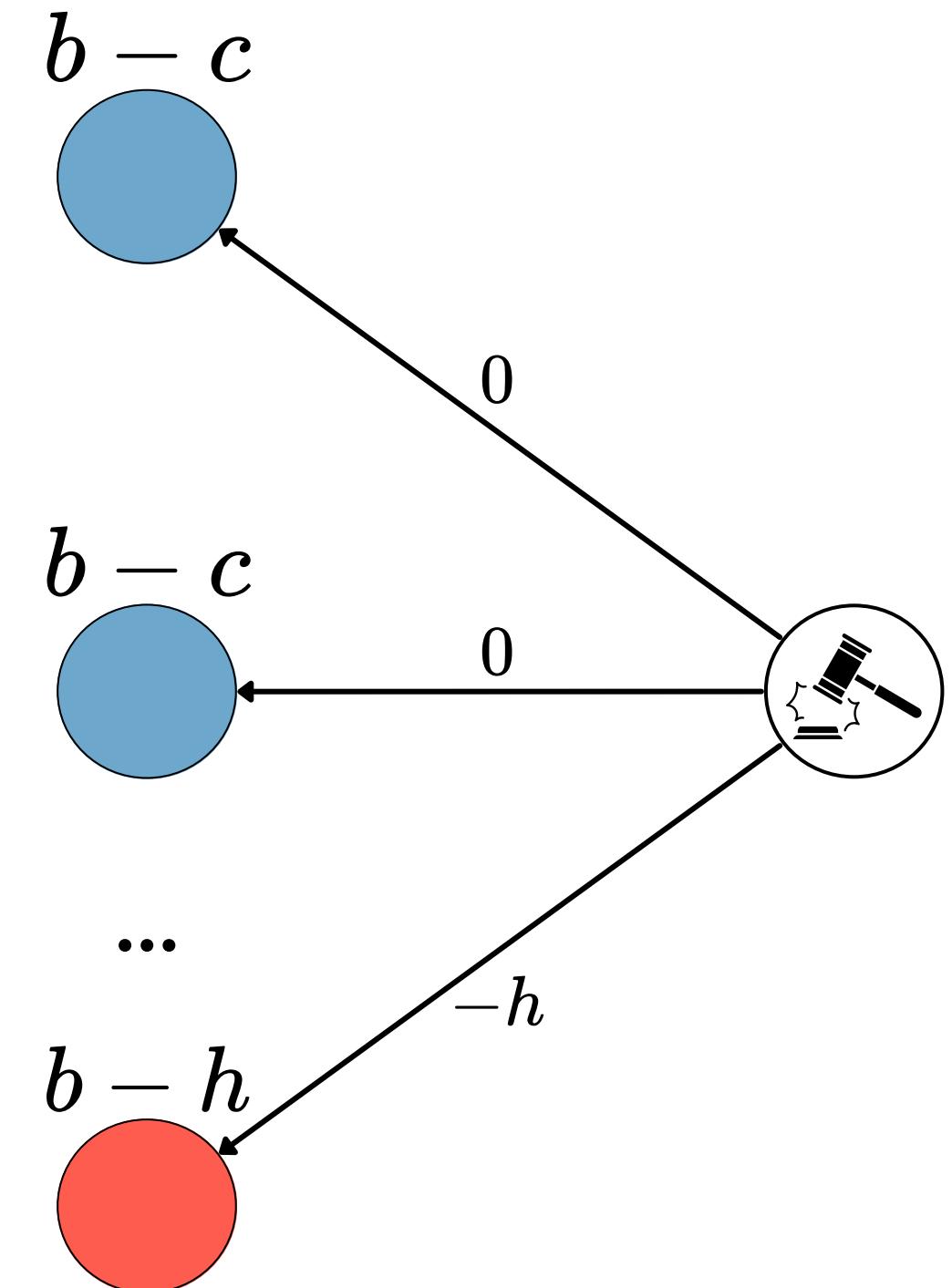
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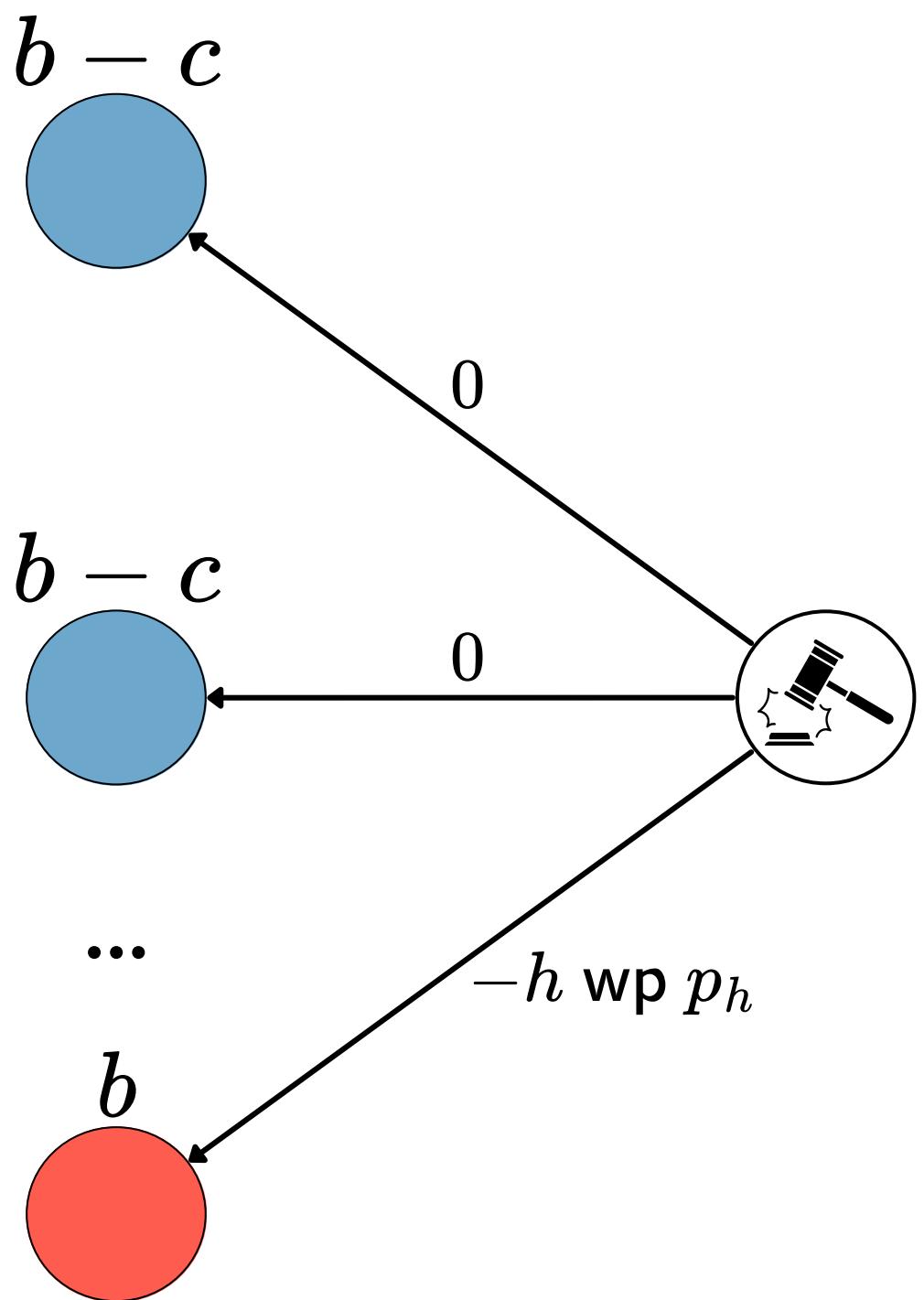
With punishment, the only equilibrium is with universal cooperation.



But this model is rather unrealistic. What if, for instance, the Leviathan is not perfectly efficient in enacting punishment?

IMPERFECT PUNISHMENT

Suppose the Leviathan punishes a defection with probability p_h .

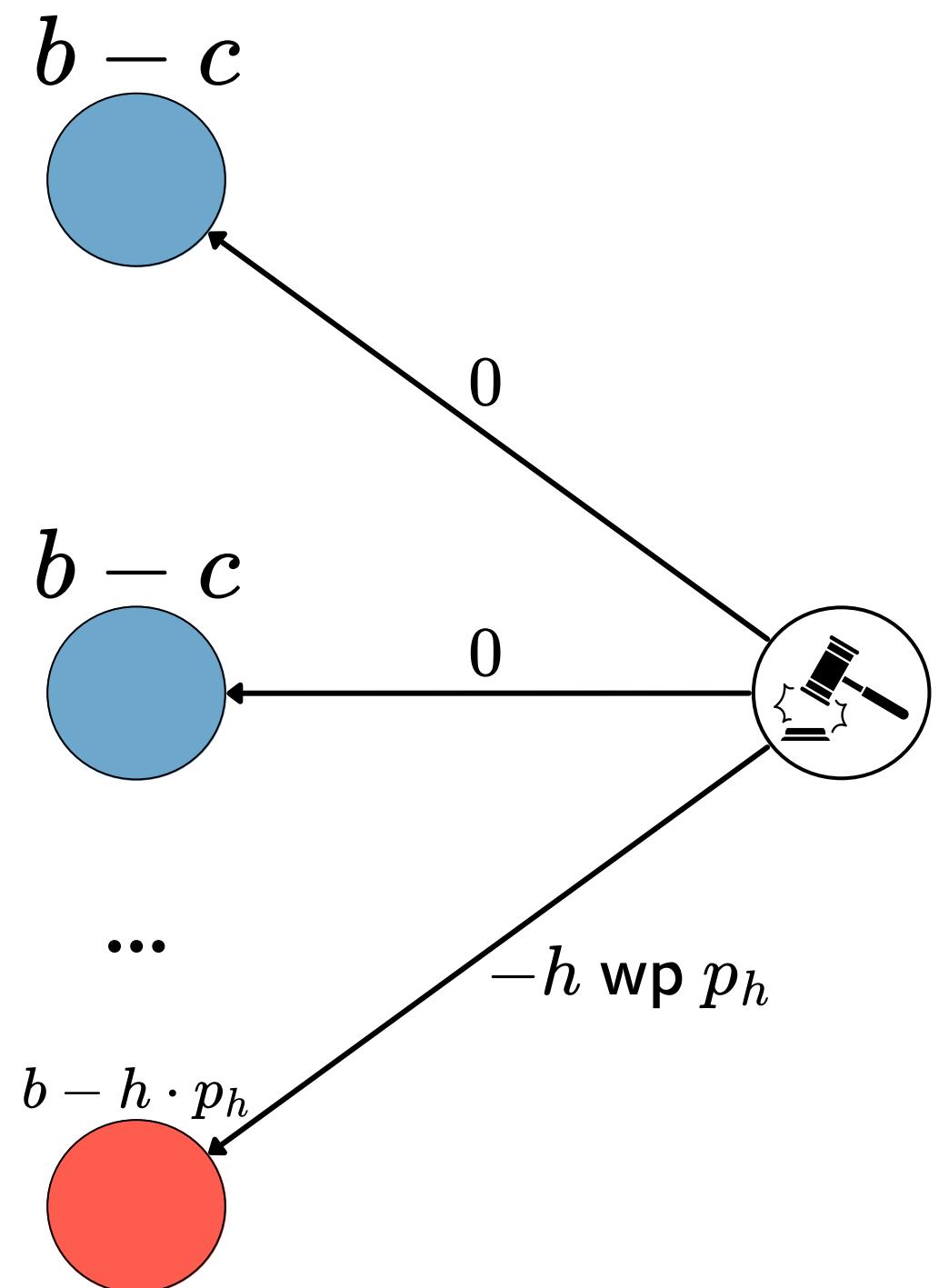


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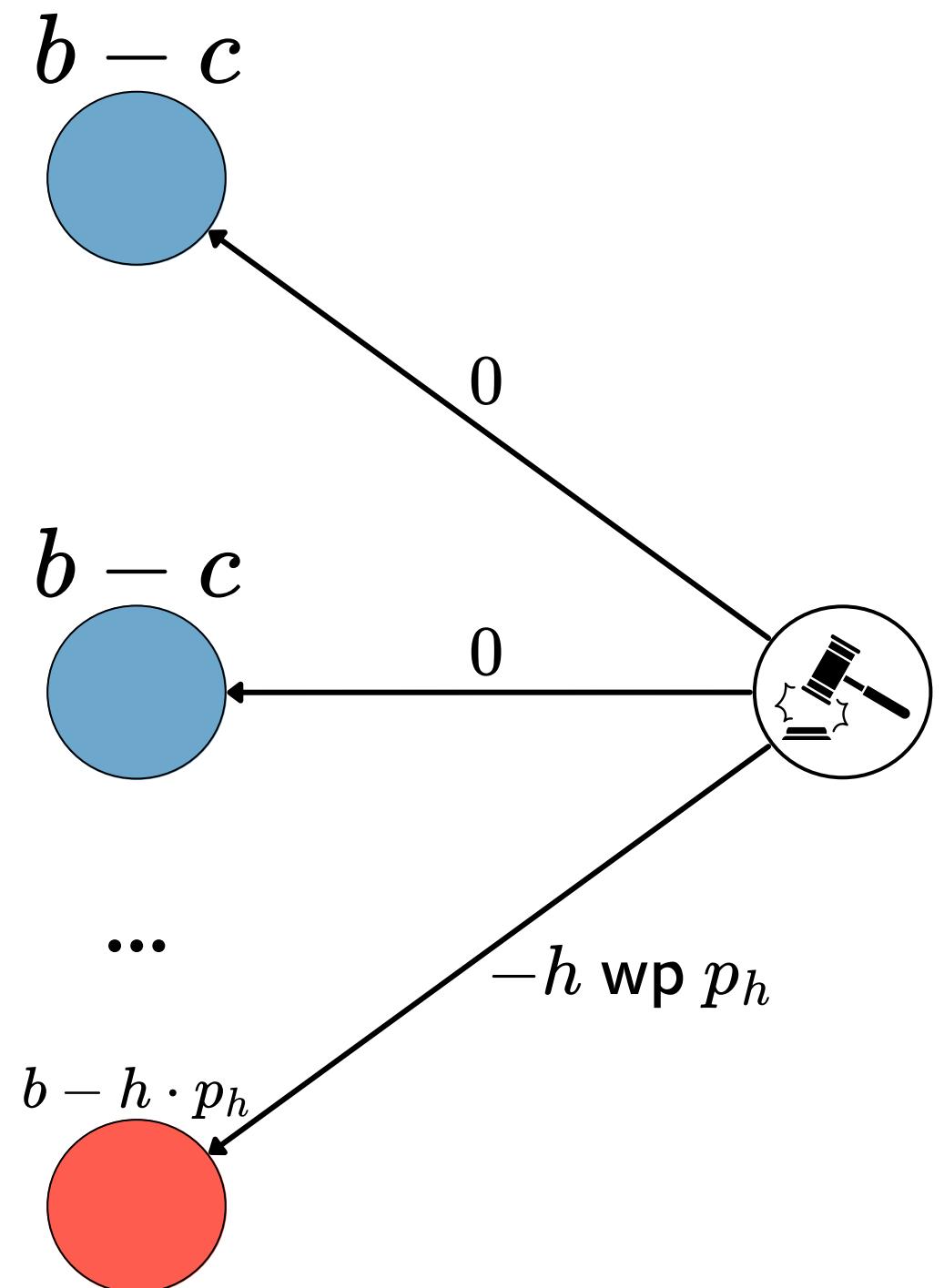
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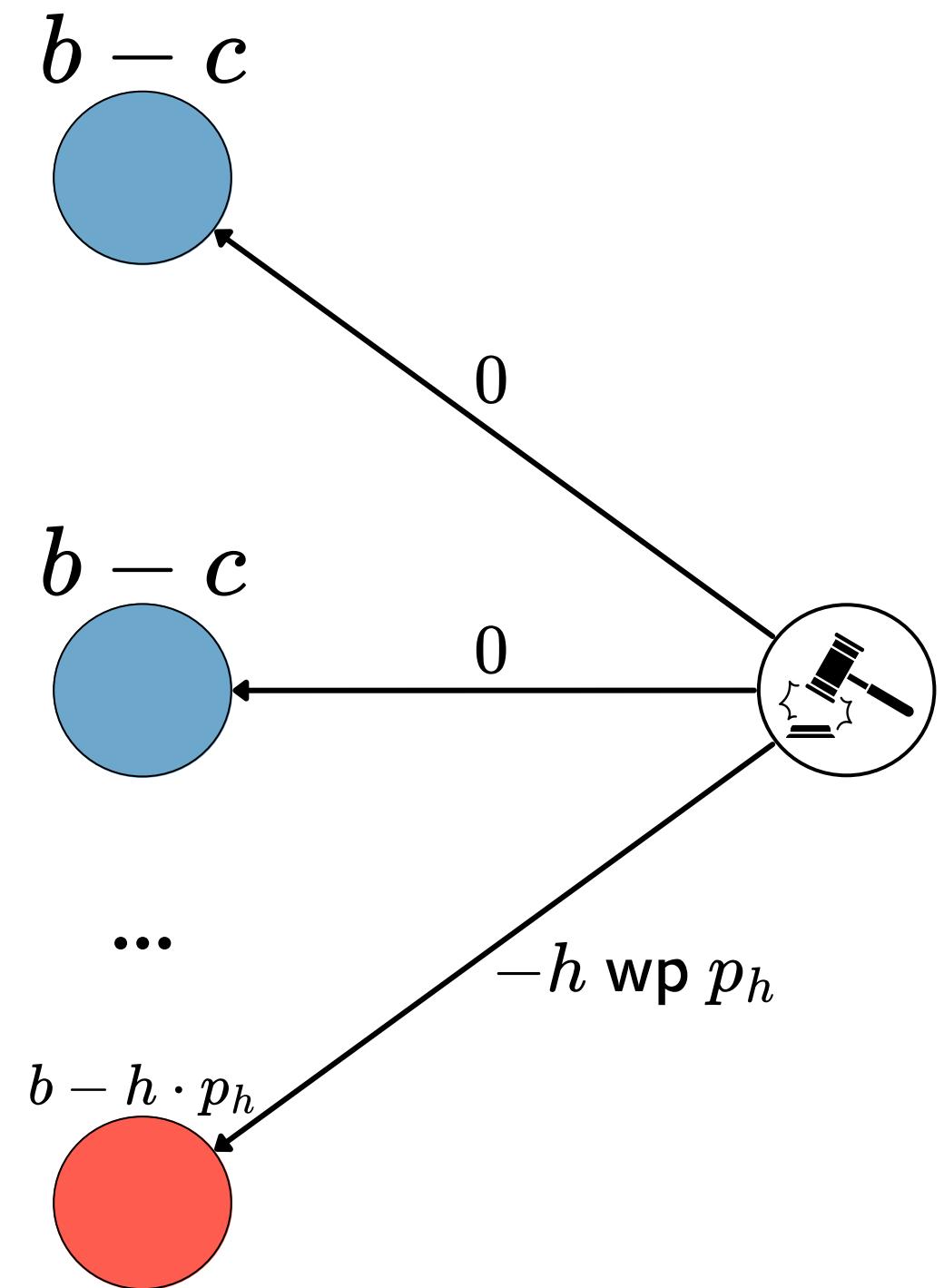
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One immediate lesson is that as the authority gets less effective at enacting punishment (i.e., as $p_h \rightarrow 0$), the penalty (h) has to grow...





EREZ YOELI

The Leviathan can be an institution, like the state.



EREZ YOELI

The Leviathan can be an institution, like the state.

MOSHE HOFFMAN

But it can also be a person, like the captain of a ship.



Yoeli, E., & Hoffman, M. (2022). *Hidden Games: The Surprising Power of Game Theory to Explain Irrational Human Behavior*. Basic Books.

PIRATE CODES

Pirate crews had very strict codes of conduct, with high penalties.

Punishment was generally decided by officers.

Yoeli, E., & Hoffman, M. (2022). *Hidden Games: The Surprising Power of Game Theory to Explain Irrational Human Behavior*. Basic Books.

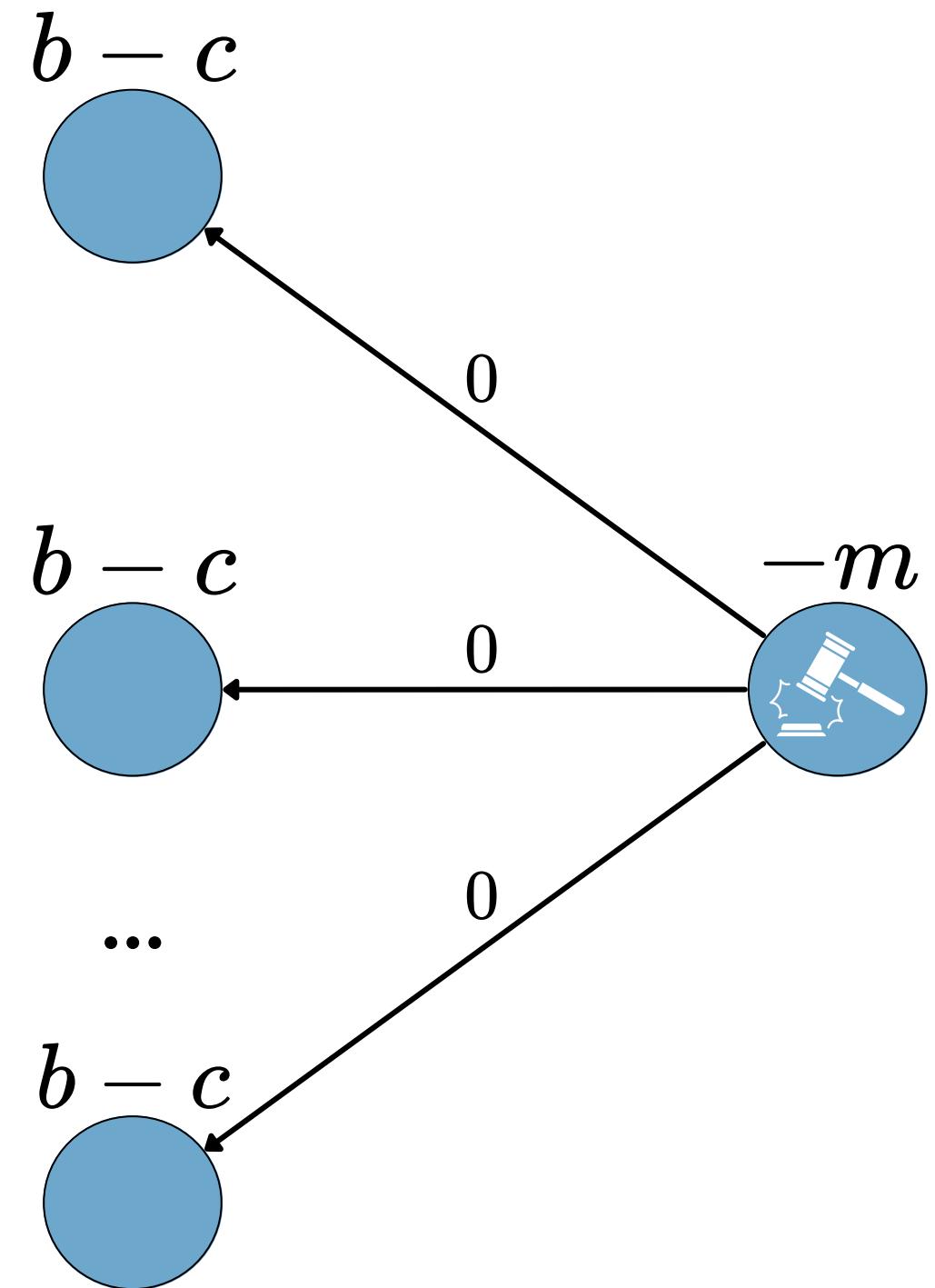


EDWARD TEACH, AKA BLACKBEARD

What of the Leviathan itself? Punishment is costly...

COSTLY PUNISHMENT

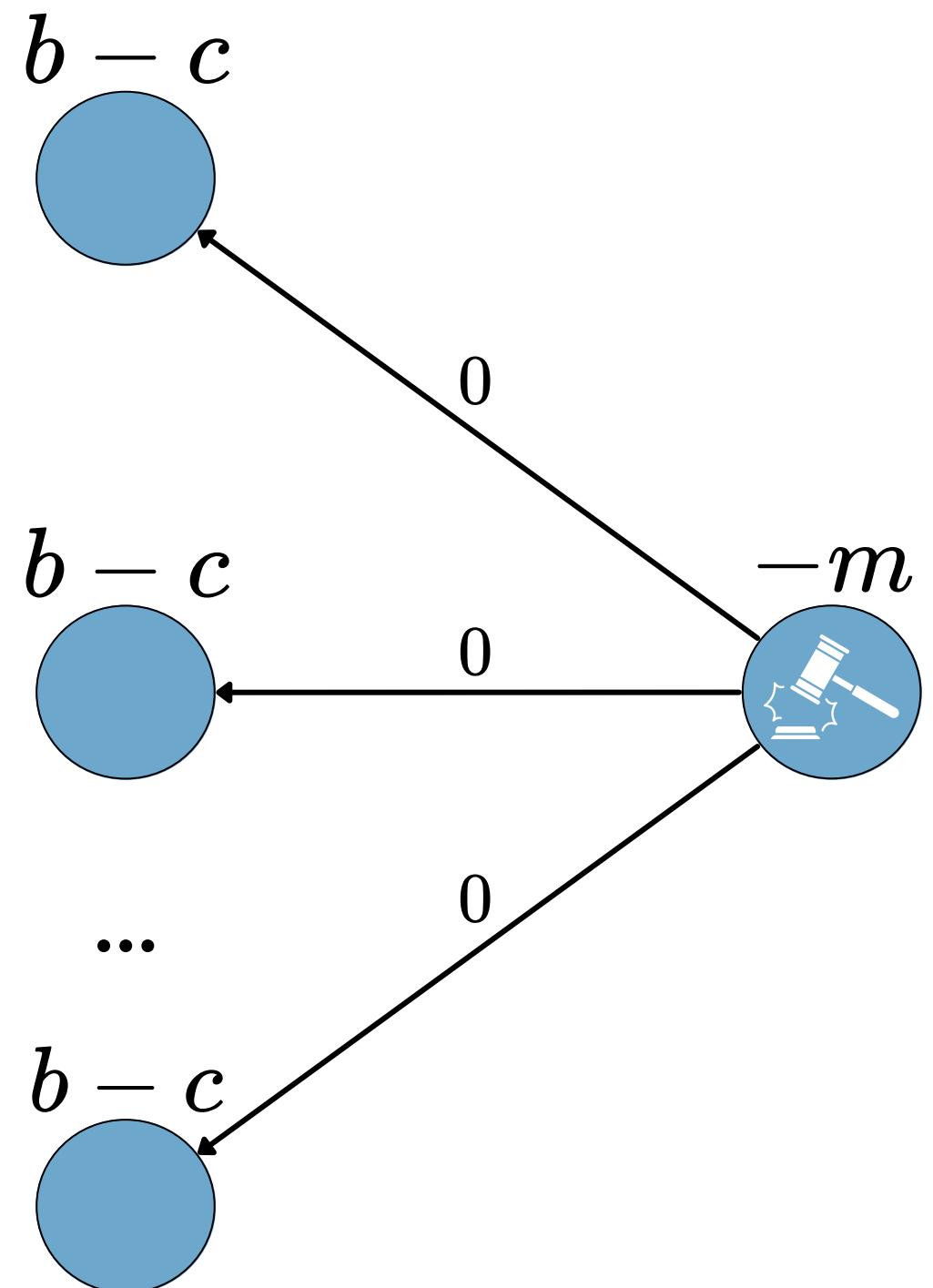
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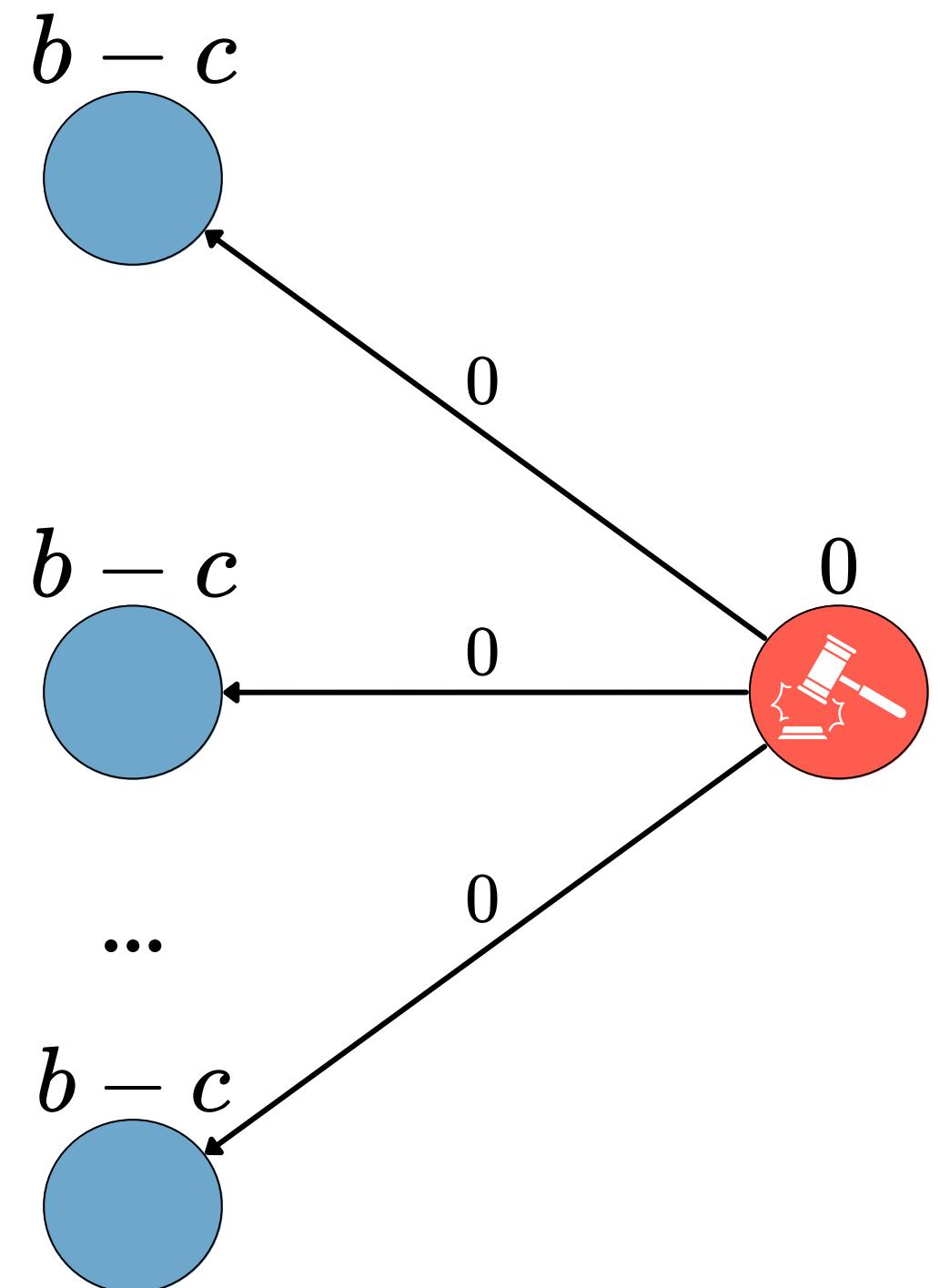
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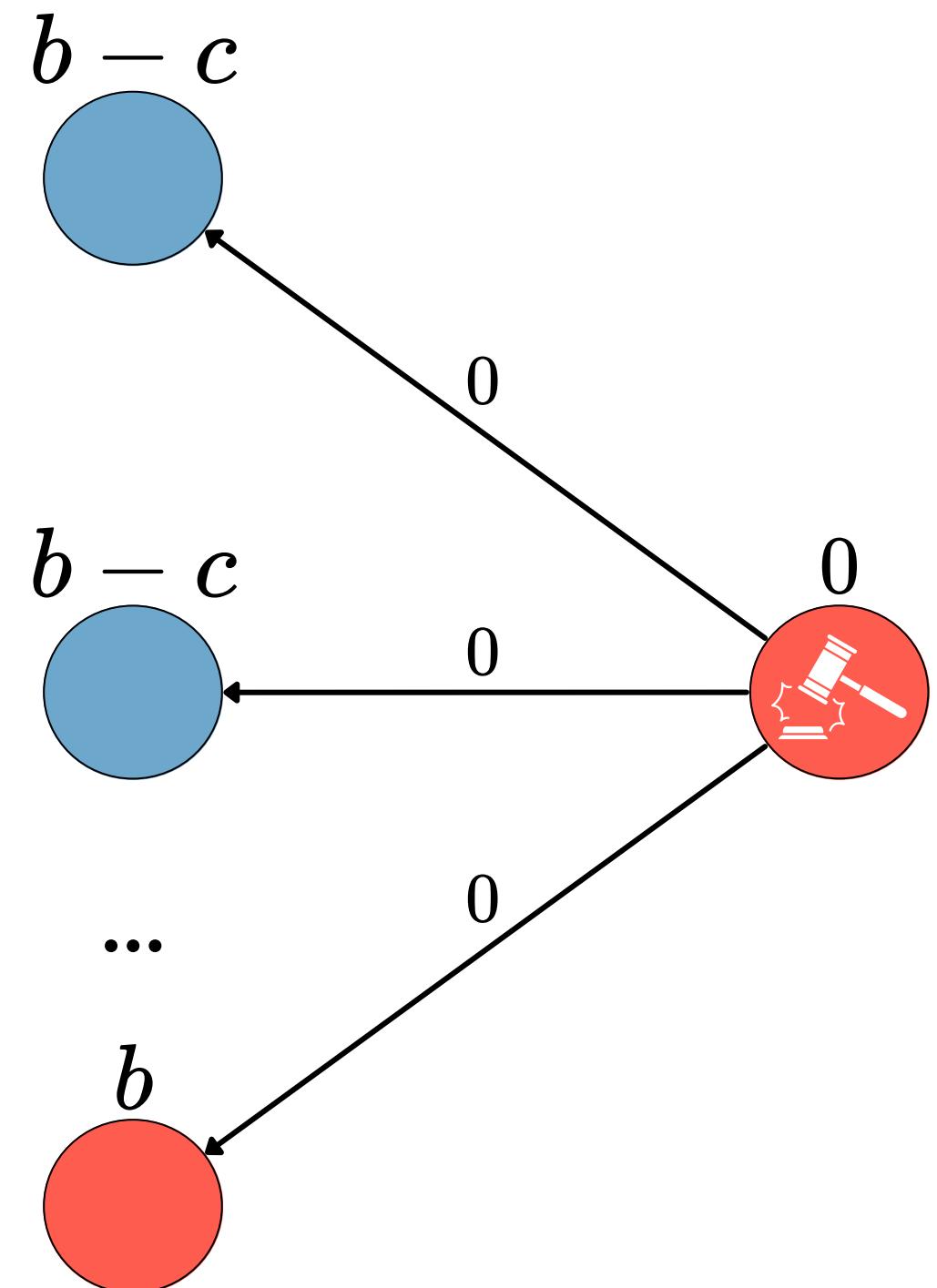


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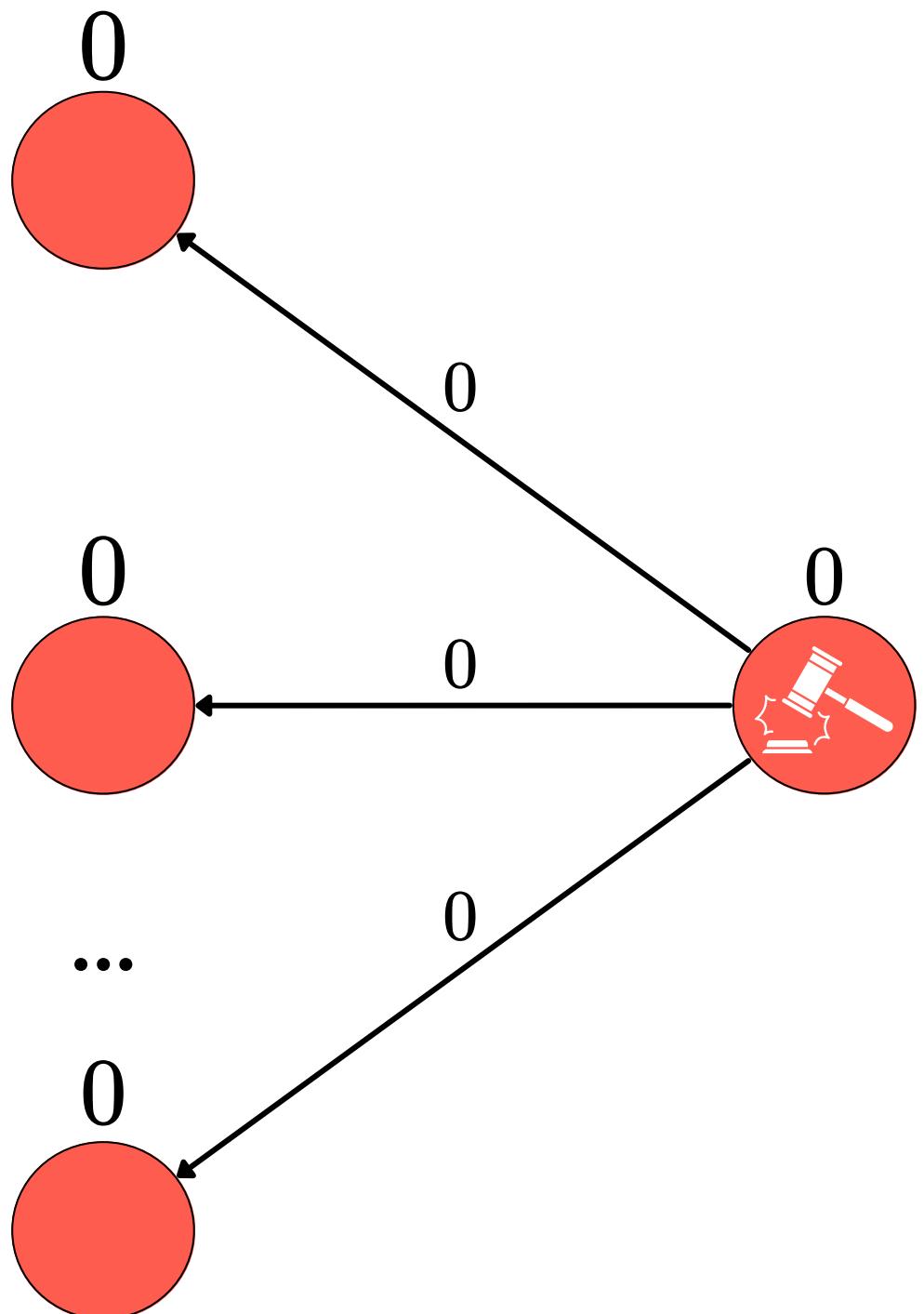


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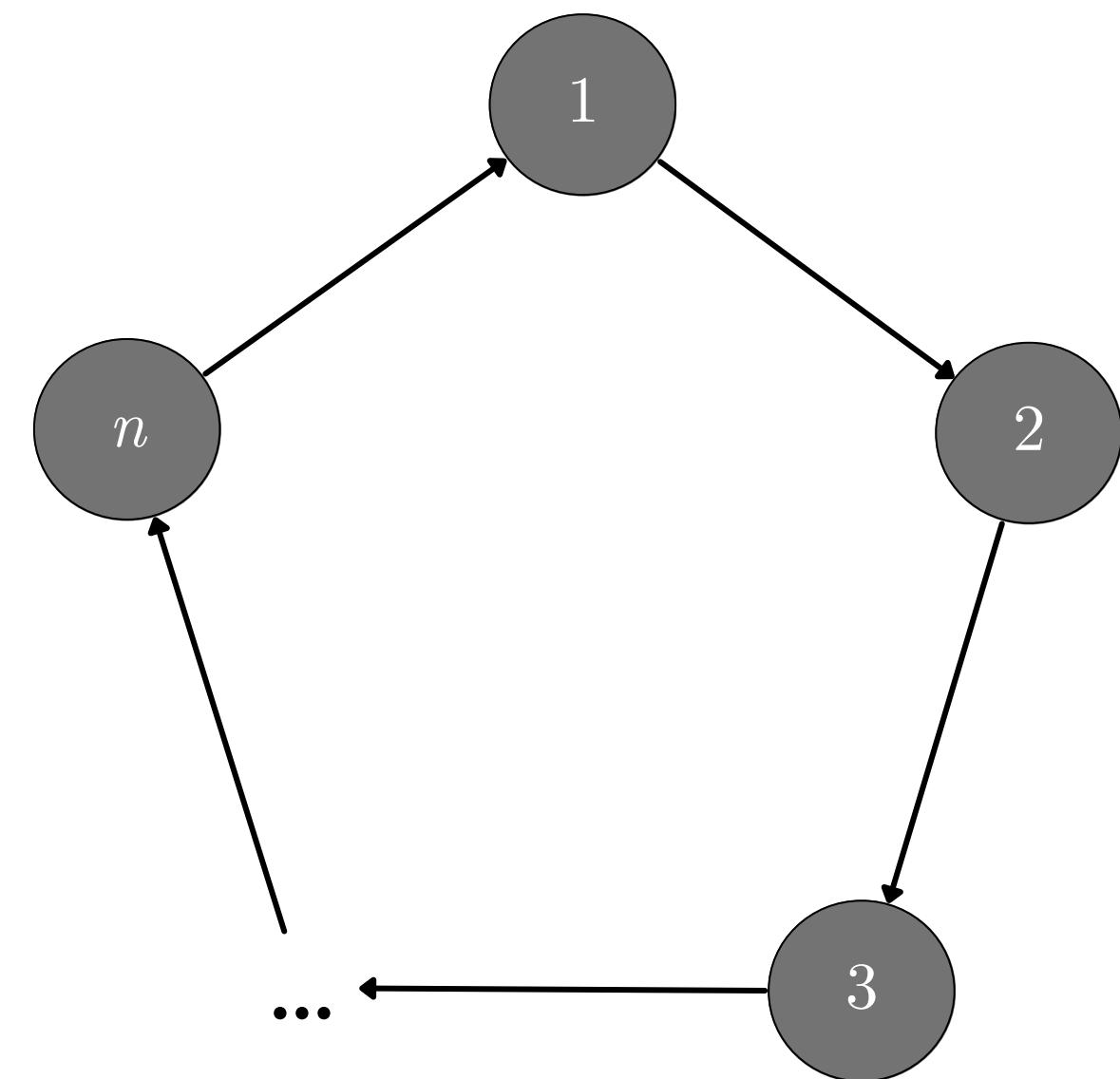


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Punishing is like contributing towards a public good in its own right. And is also subject to the free rider problem...

PUBLIC GOODS WITH THIRD PARTY PUNISHMENT

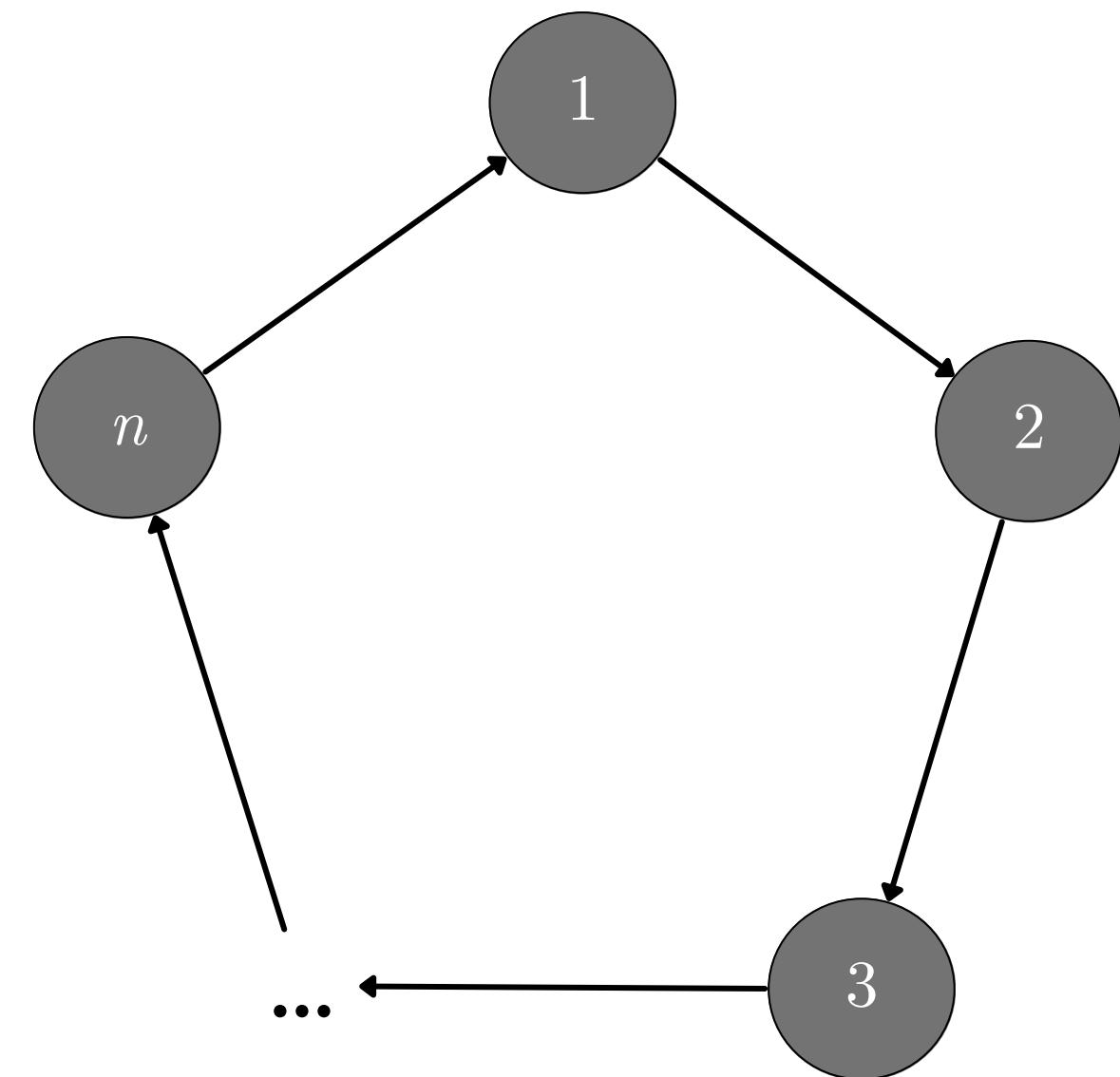
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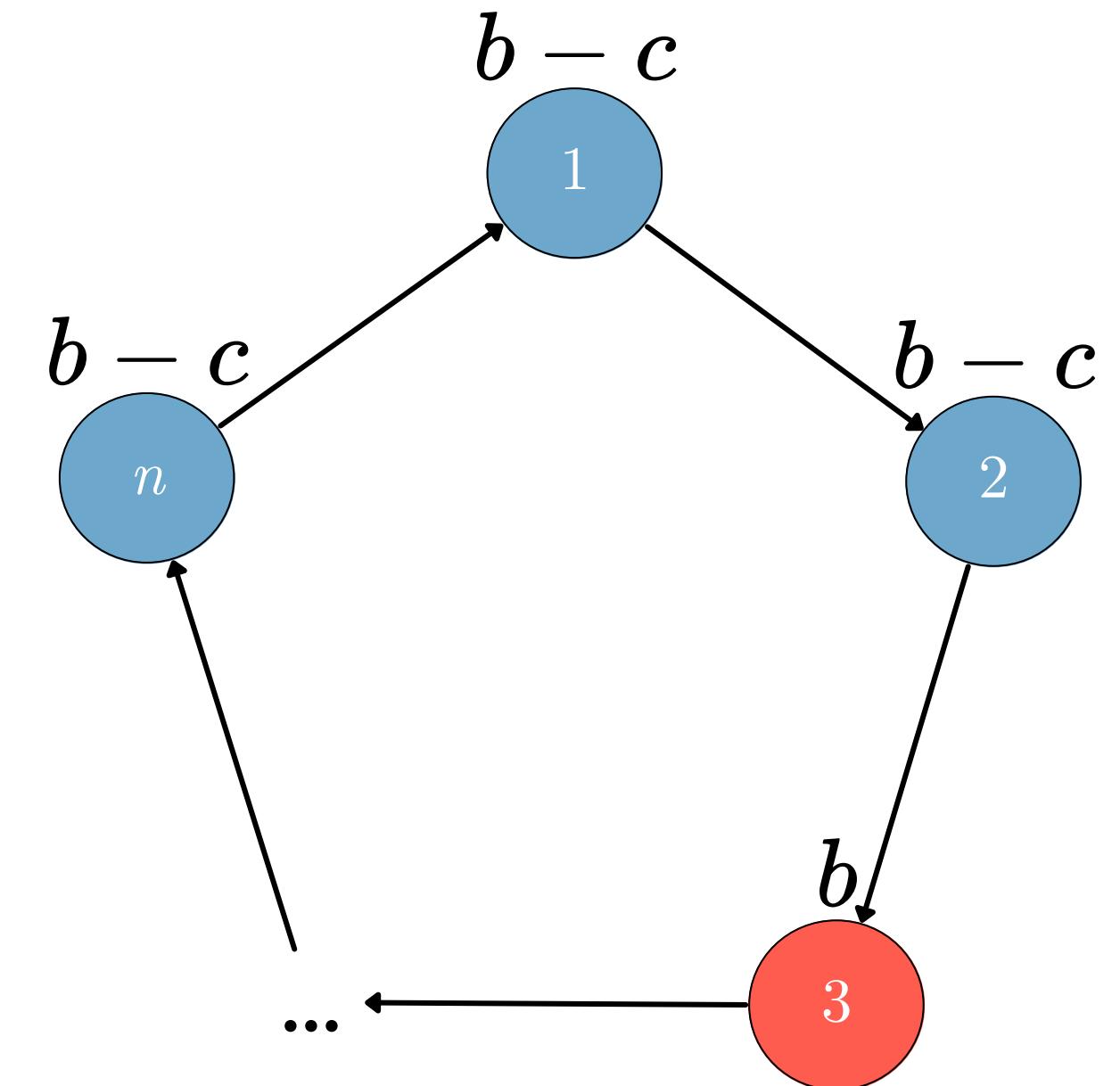


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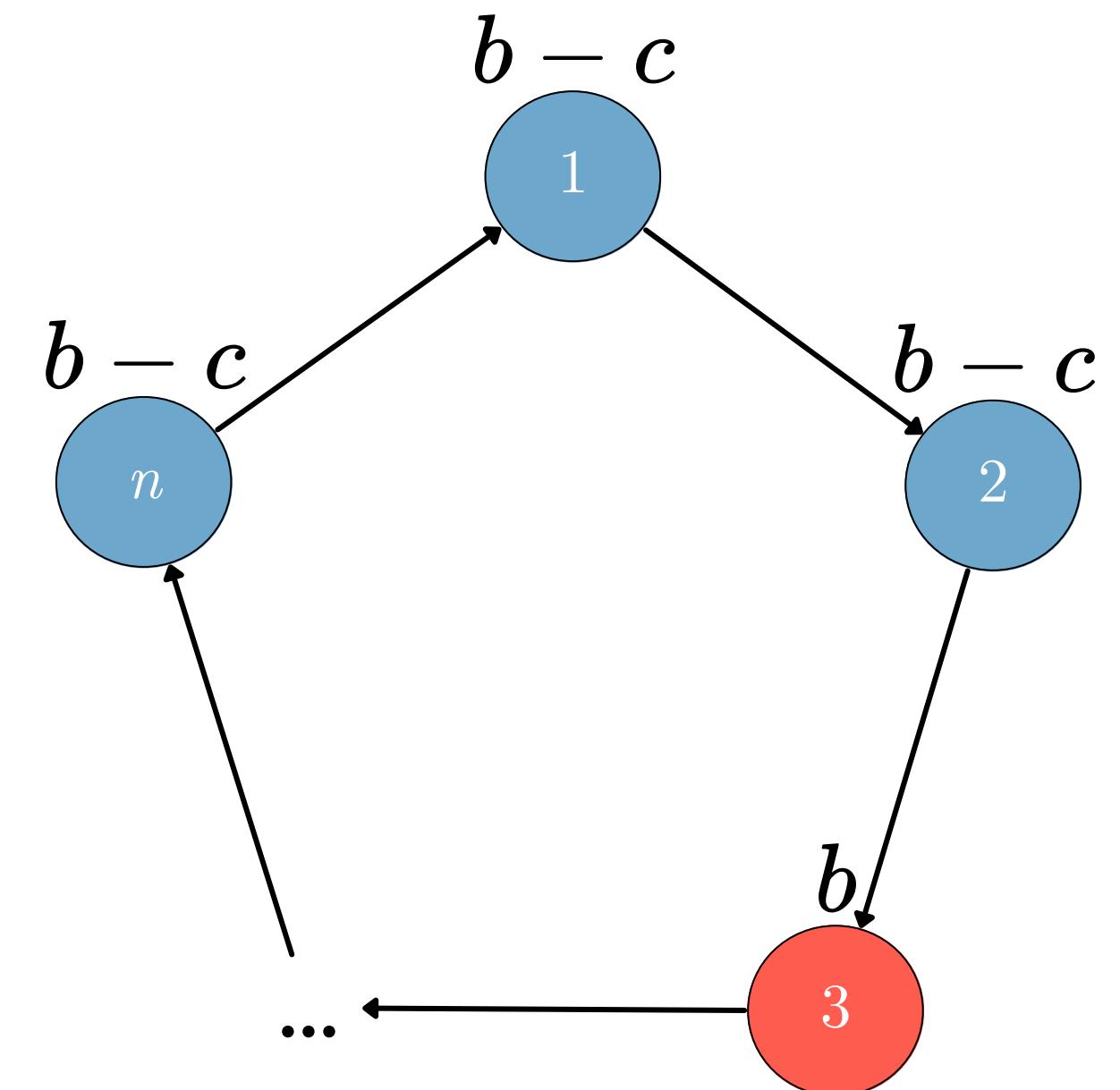
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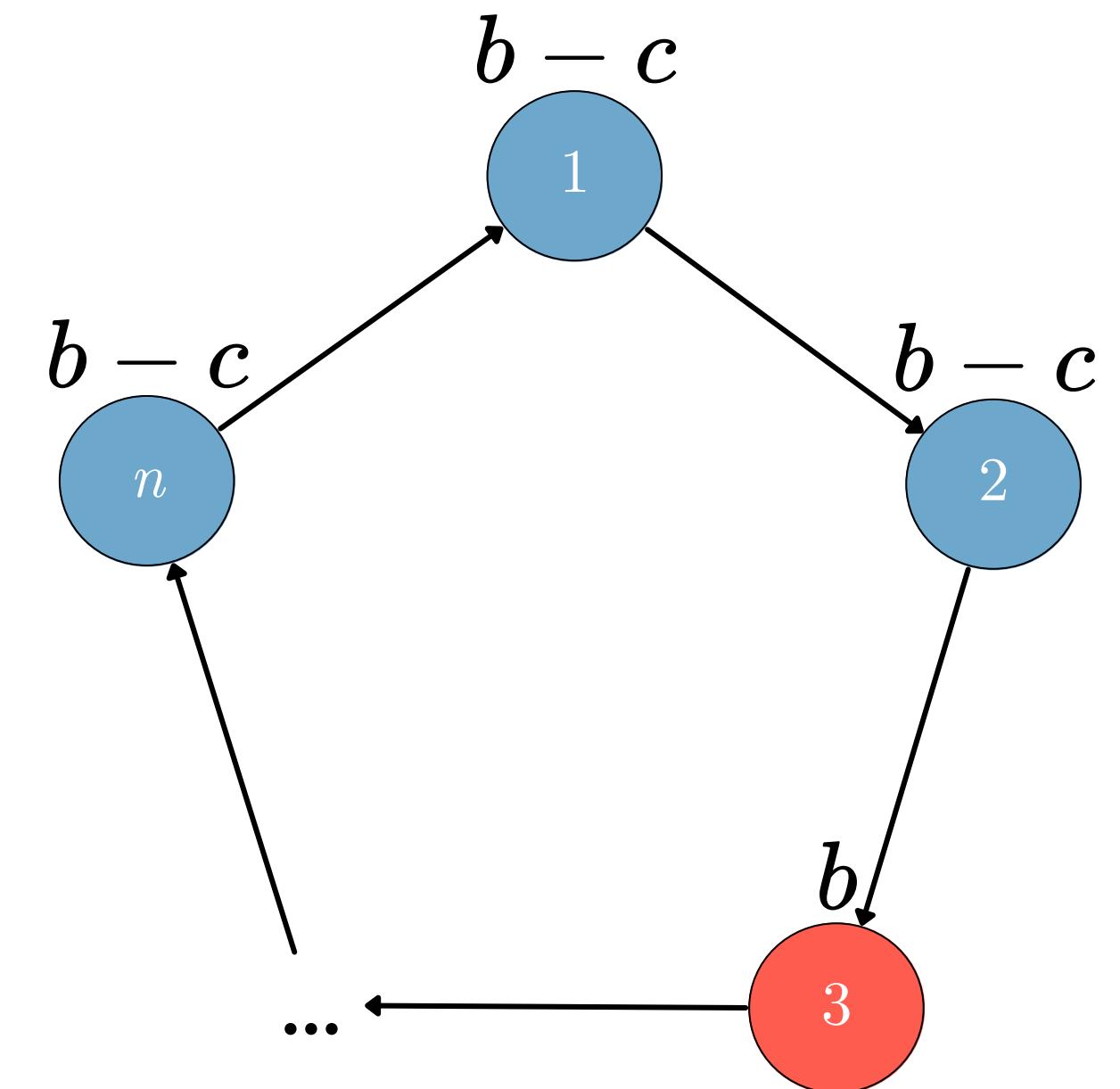
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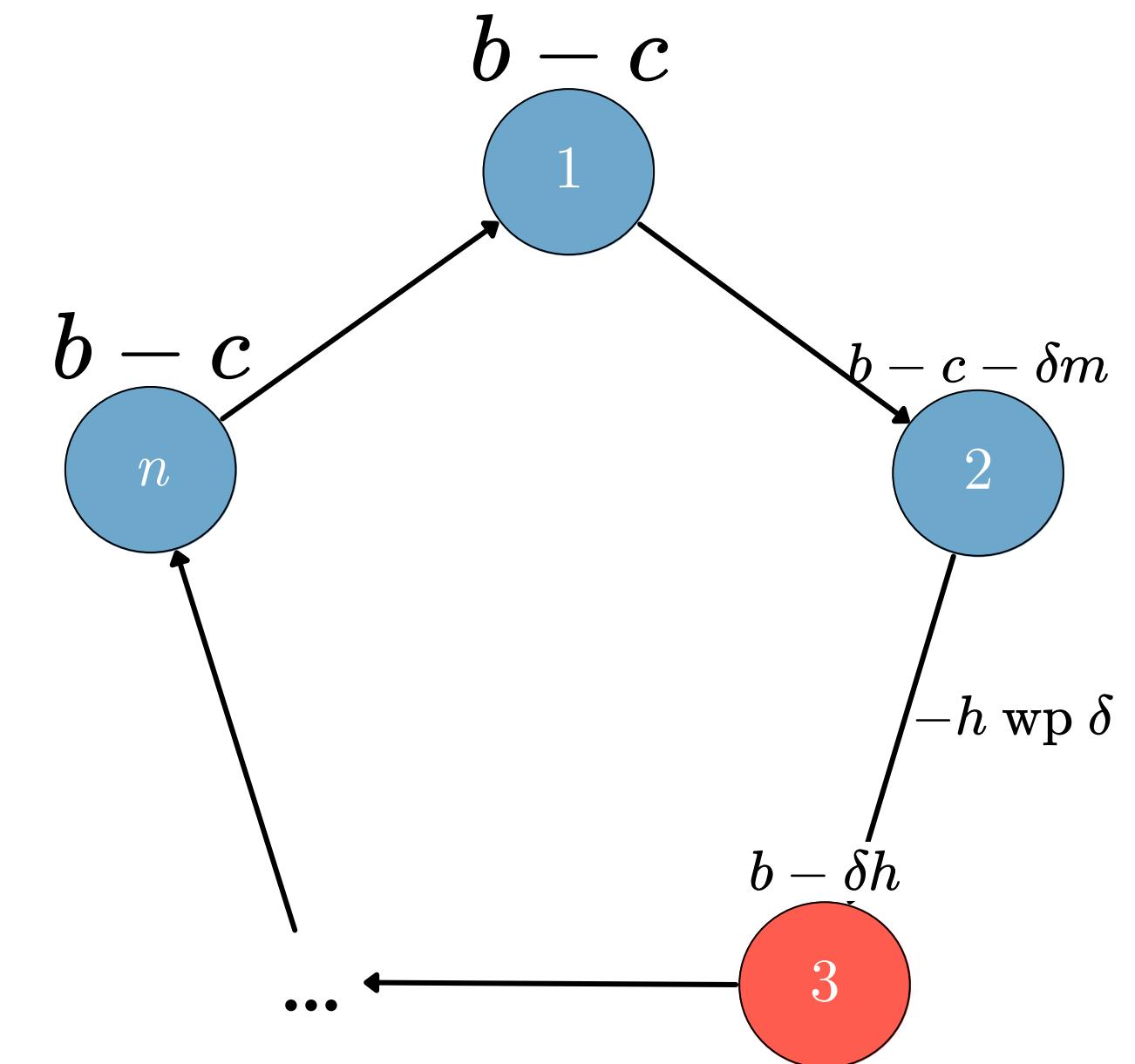
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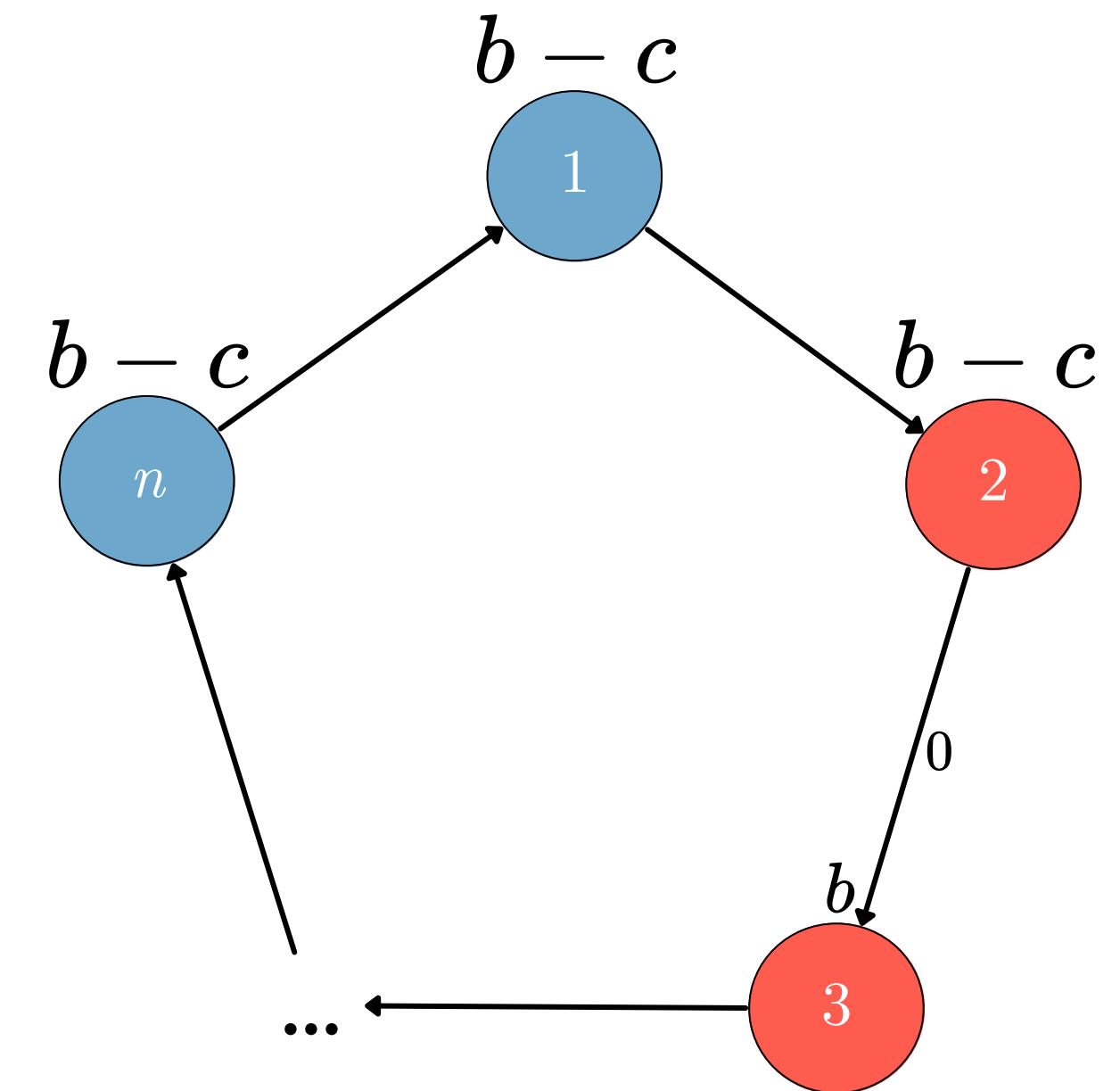
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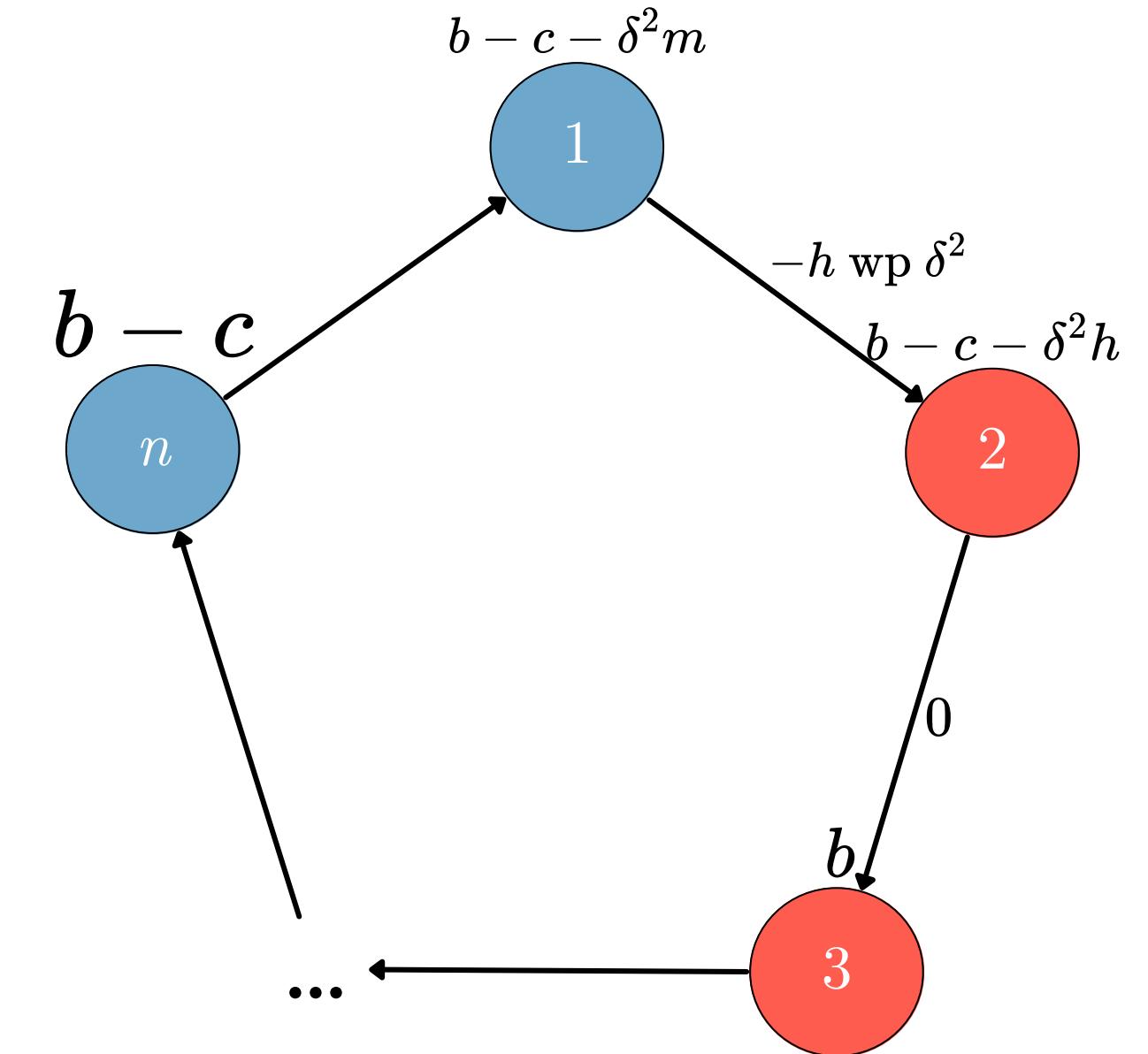
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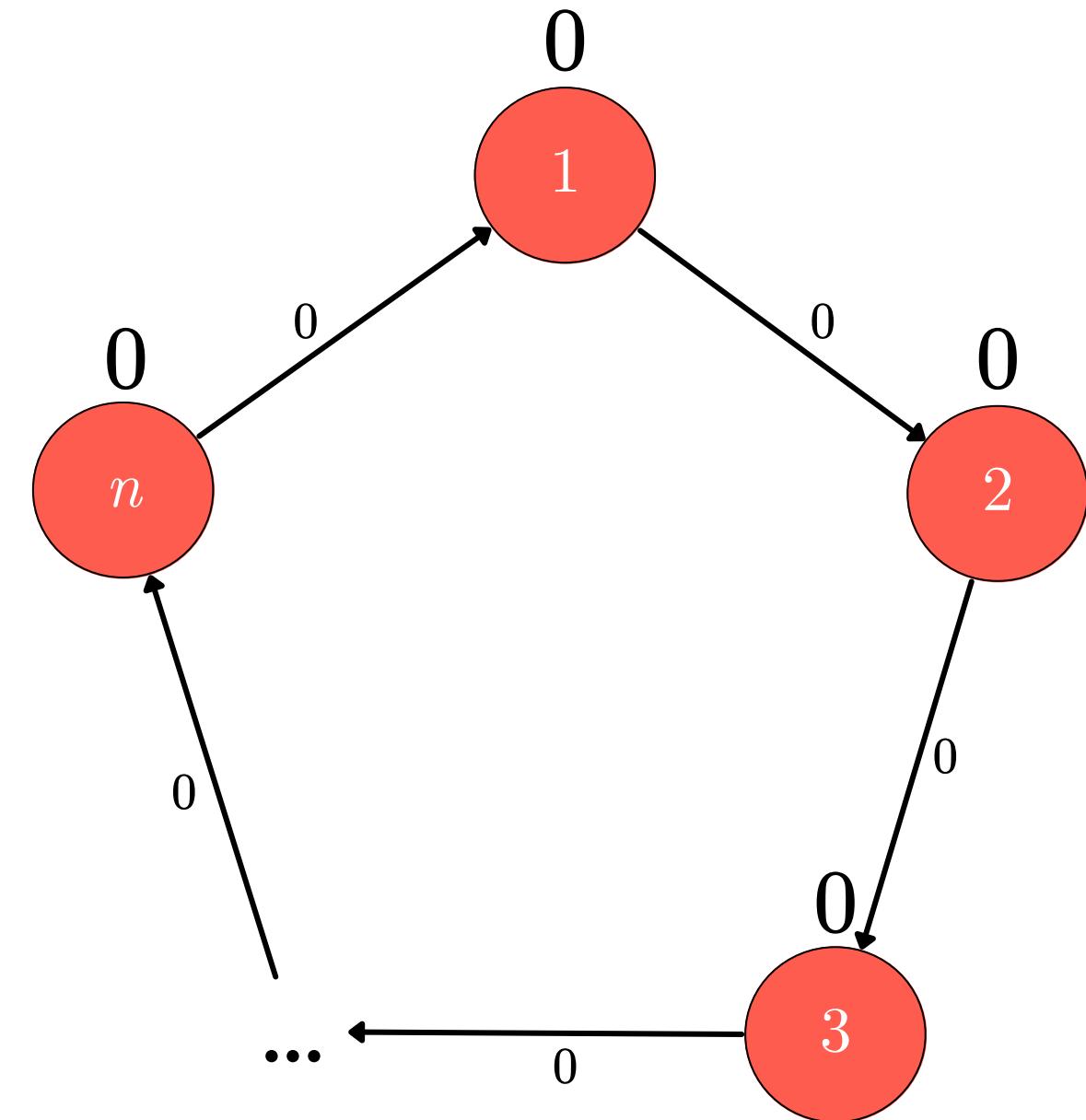
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Equilibria?

NO CONTRIBUTION, NO PUNISHMENT

Suppose no one contributes, and no one punishes.

This is an equilibrium, since any deviation incurs costs and no benefits.*

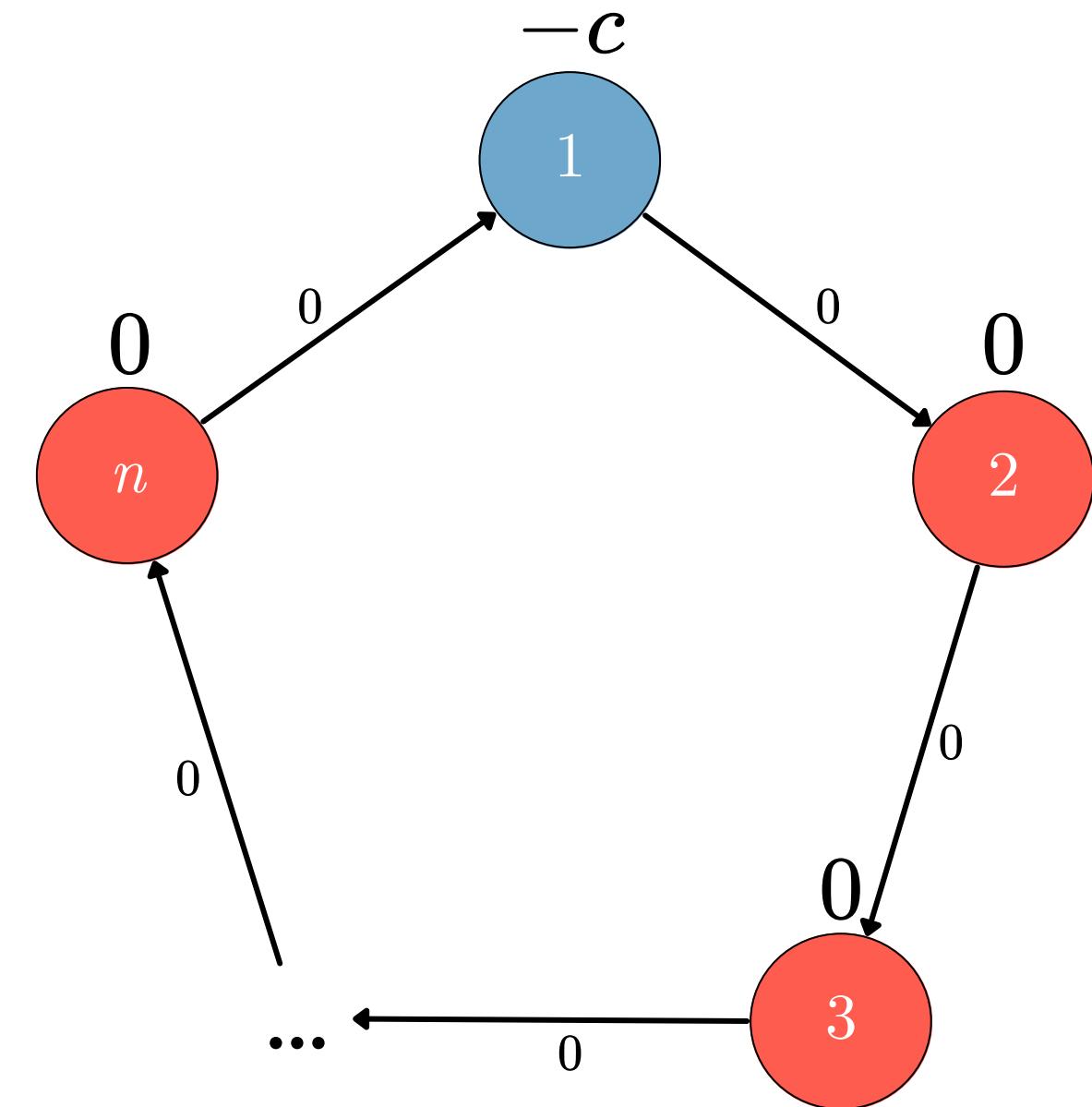


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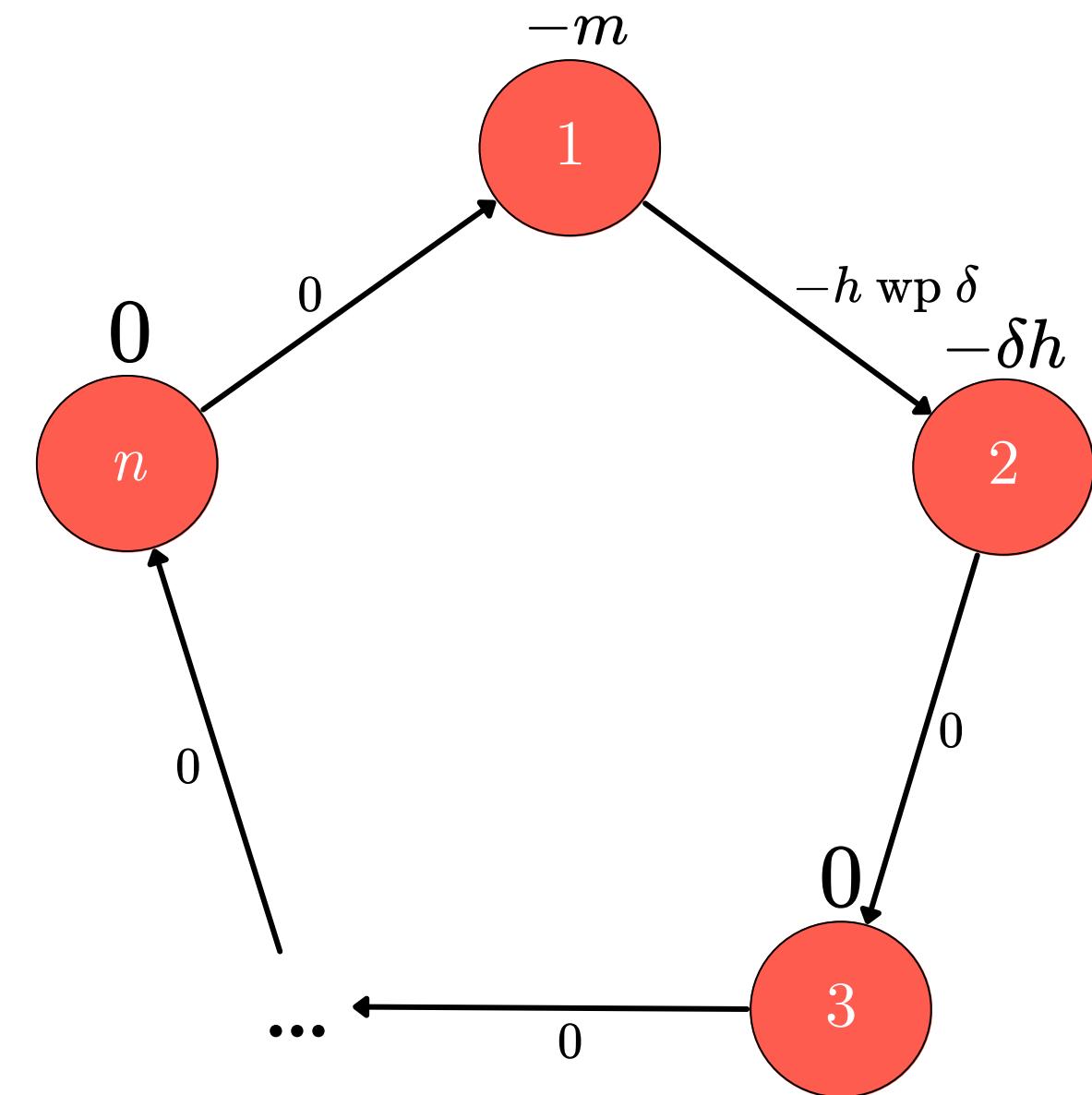
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Player 1 switches to contributing

NO CONTRIBUTION, NO PUNISHMENT

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Player 1 switches to punishing player 2

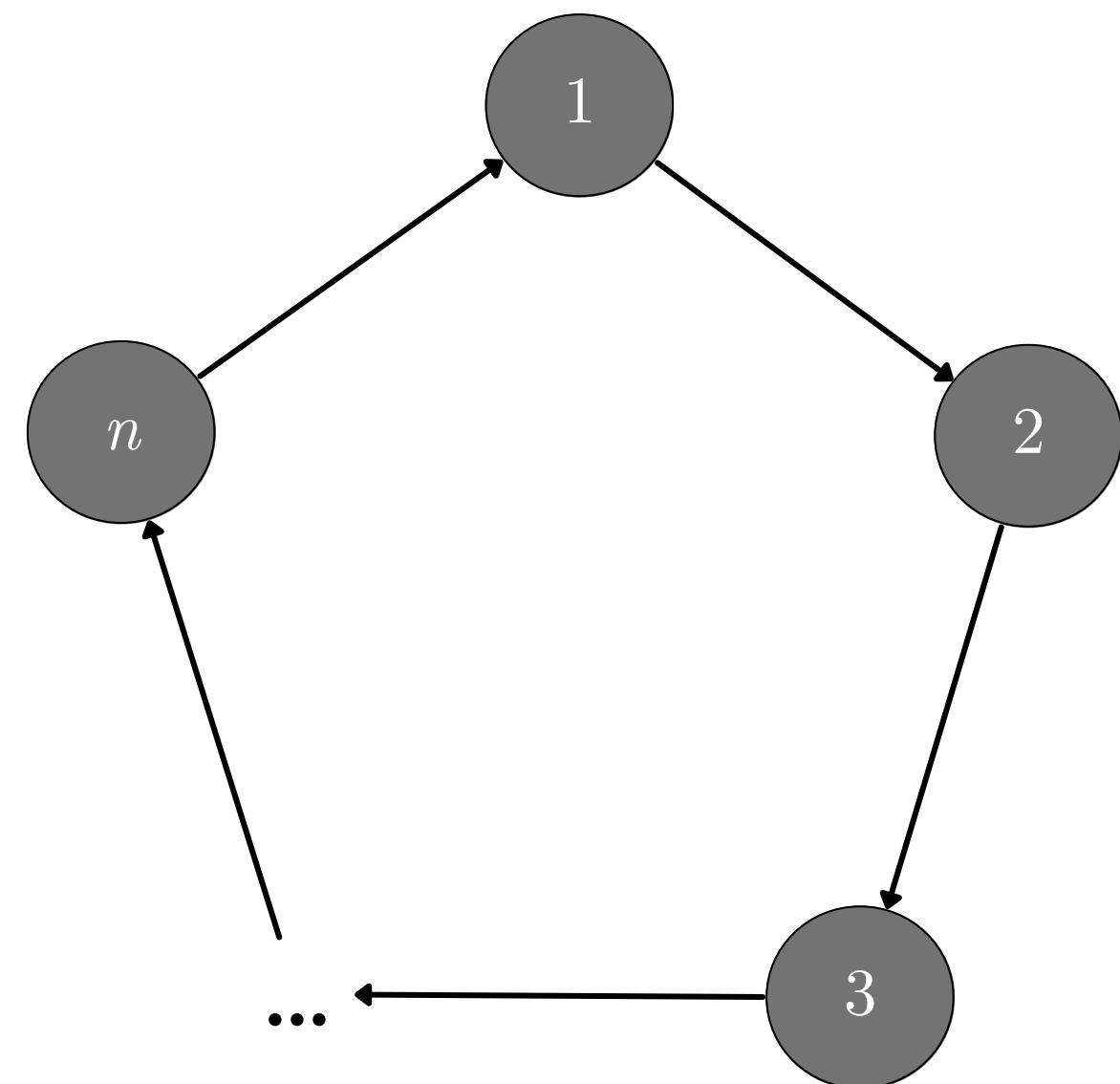
This is a very bad equilibrium. Anything else?

CONTRIBUTE AND PUNISH

Suppose players have different strategies:
start by contributing, and punish any
transgressions of the monitored agent from
the previous round.

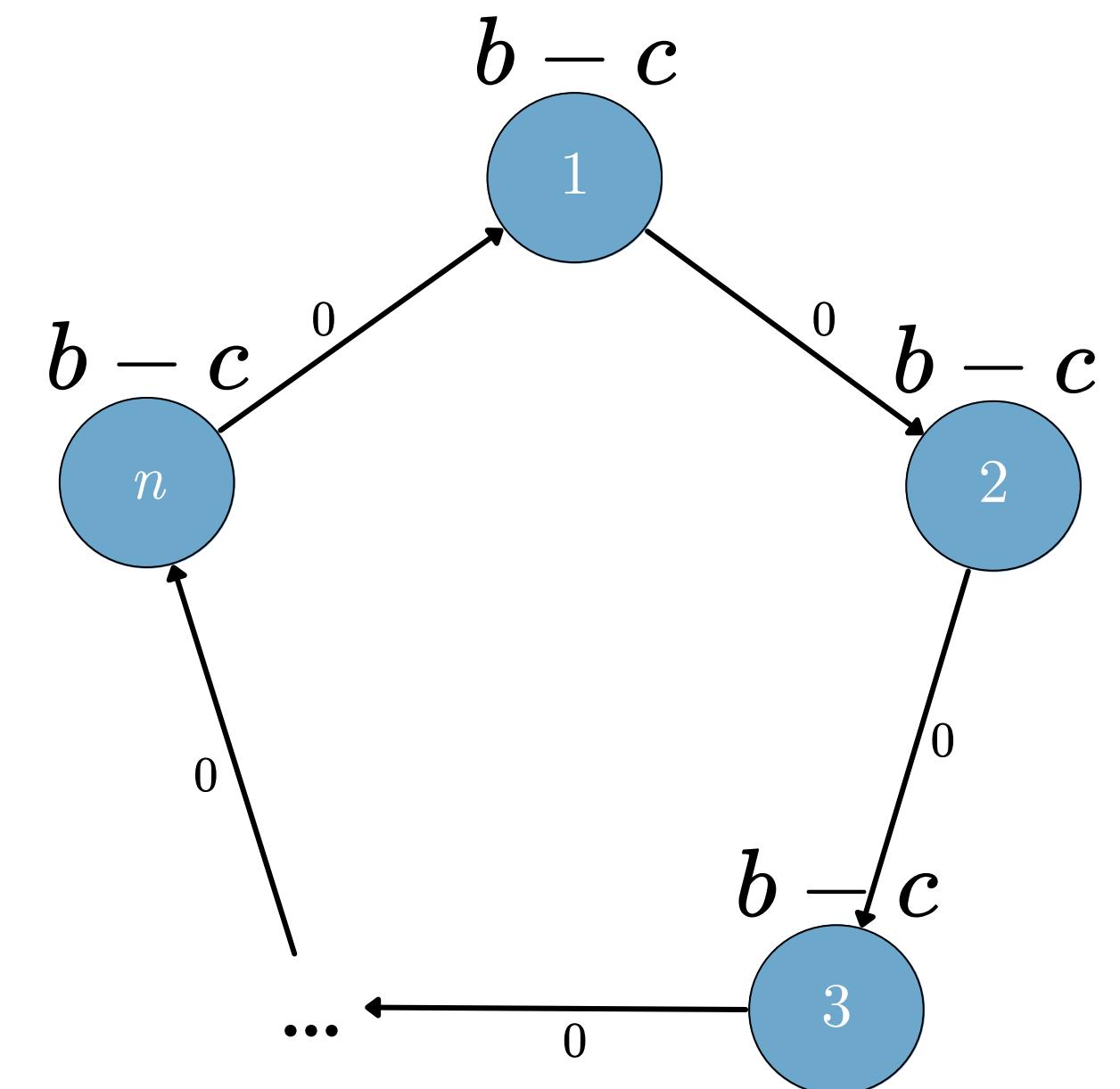
A transgression at round 1 is to not
contribute.

A transgression at round $t+1$ is failure to
punish transgressions at round t .



CONTRIBUTE AND PUNISH

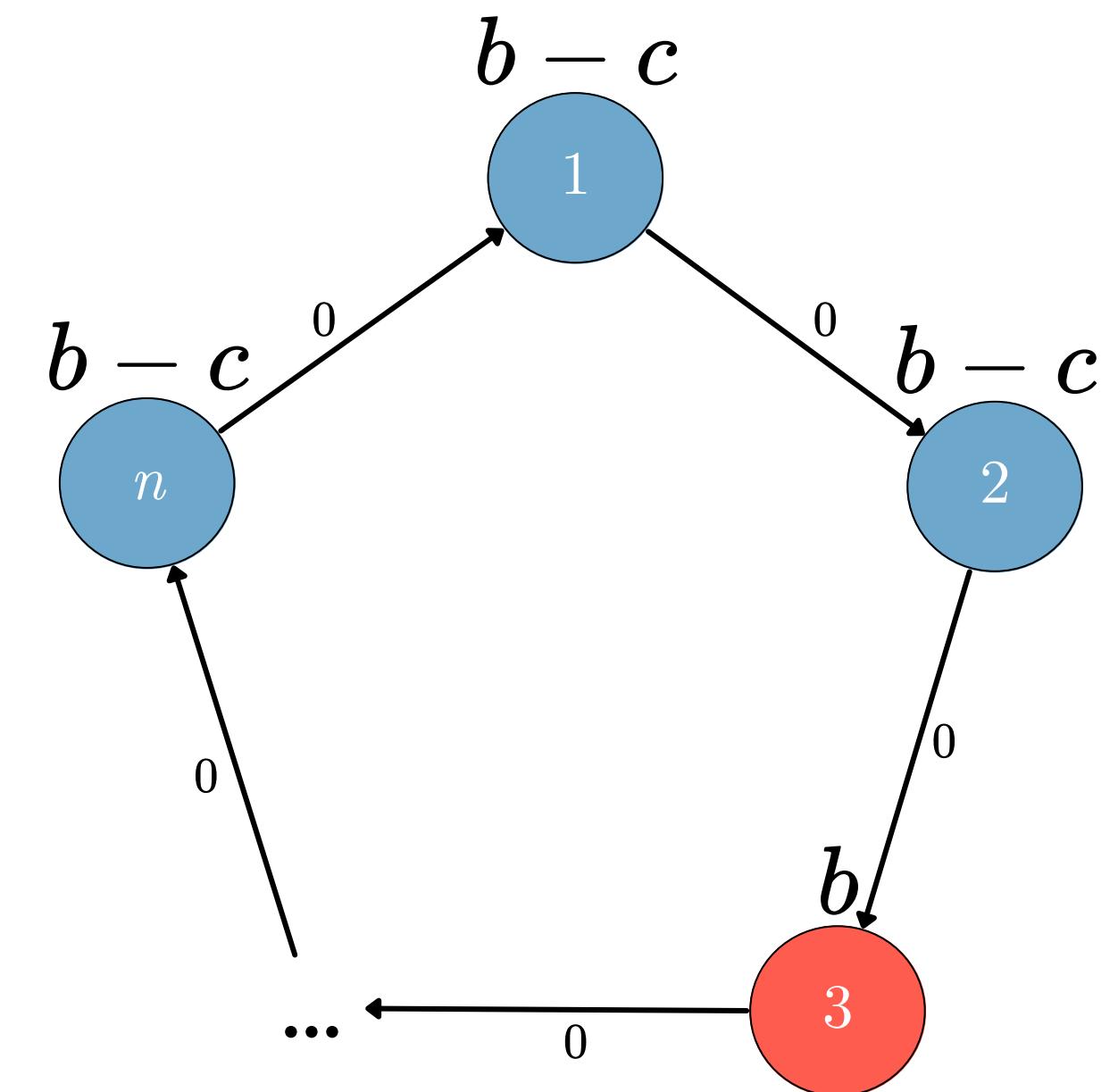
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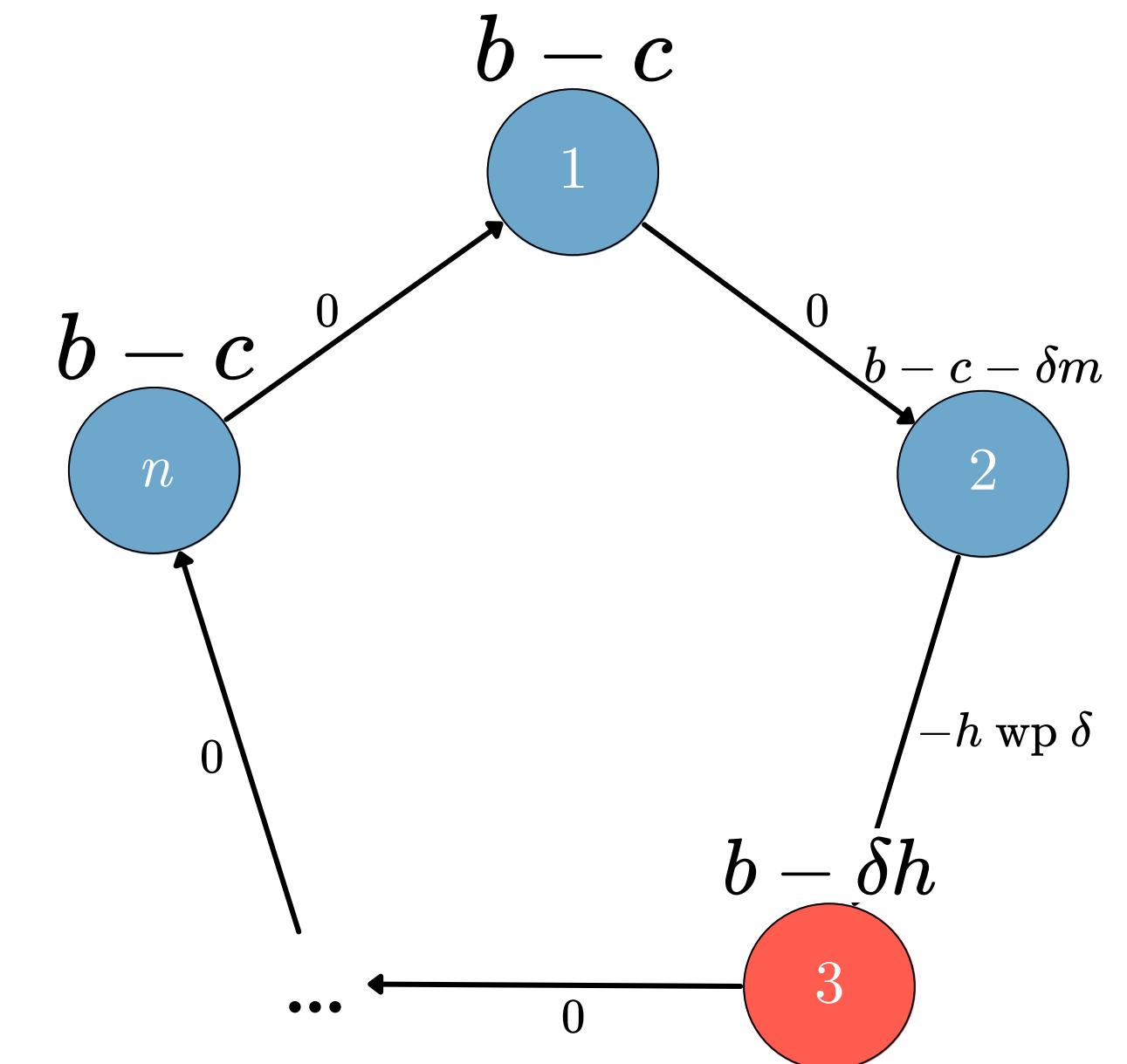
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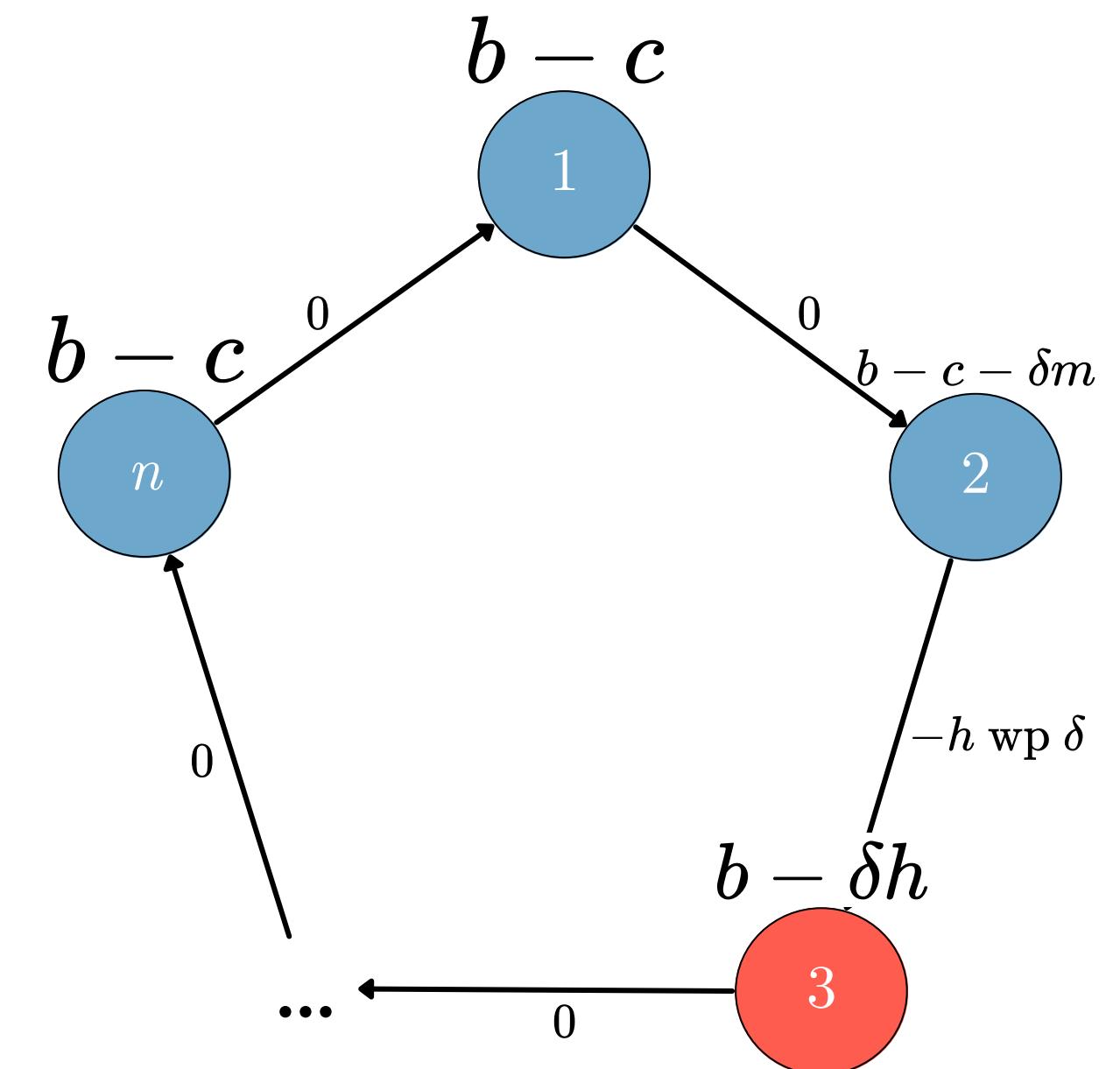
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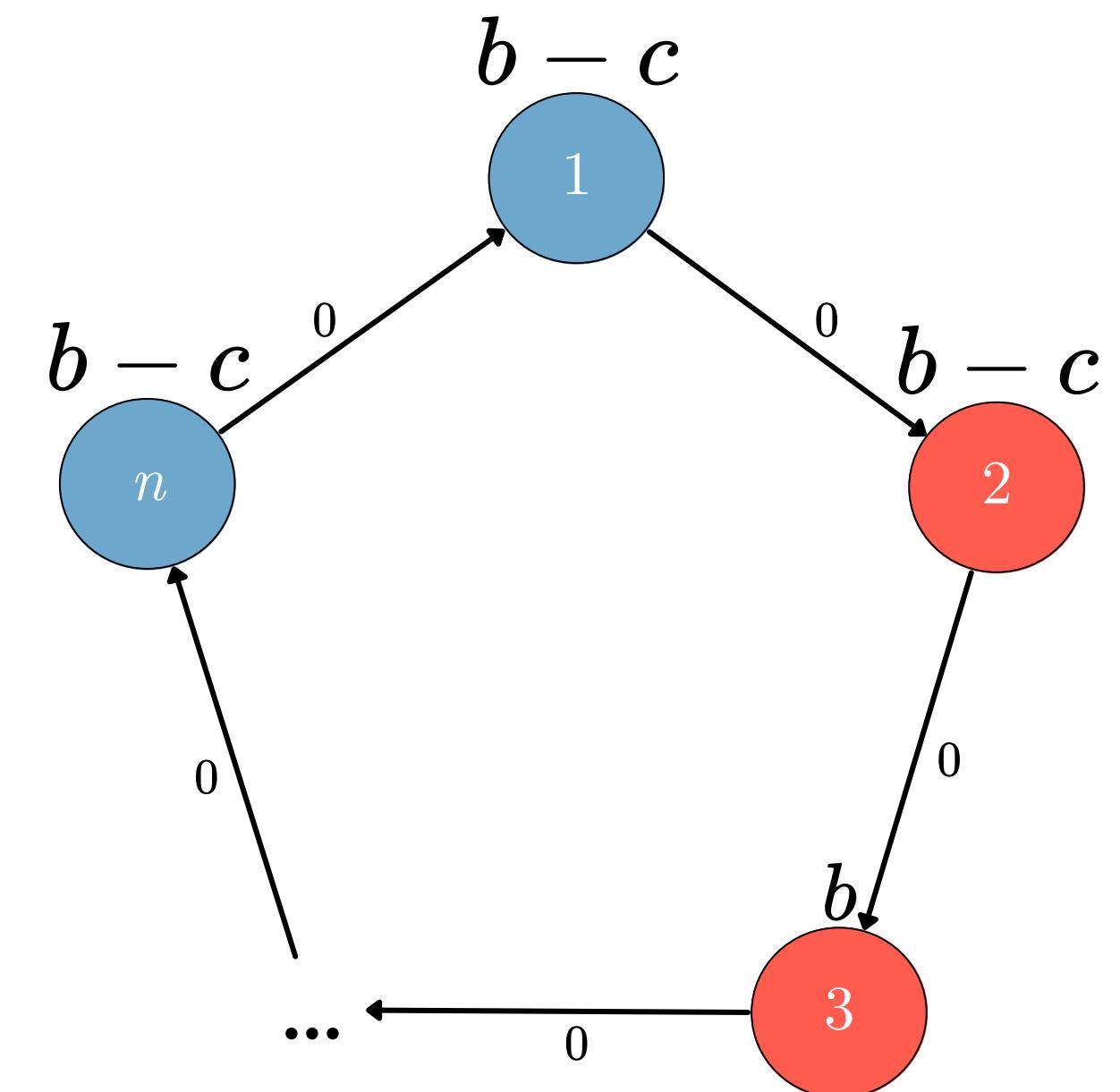
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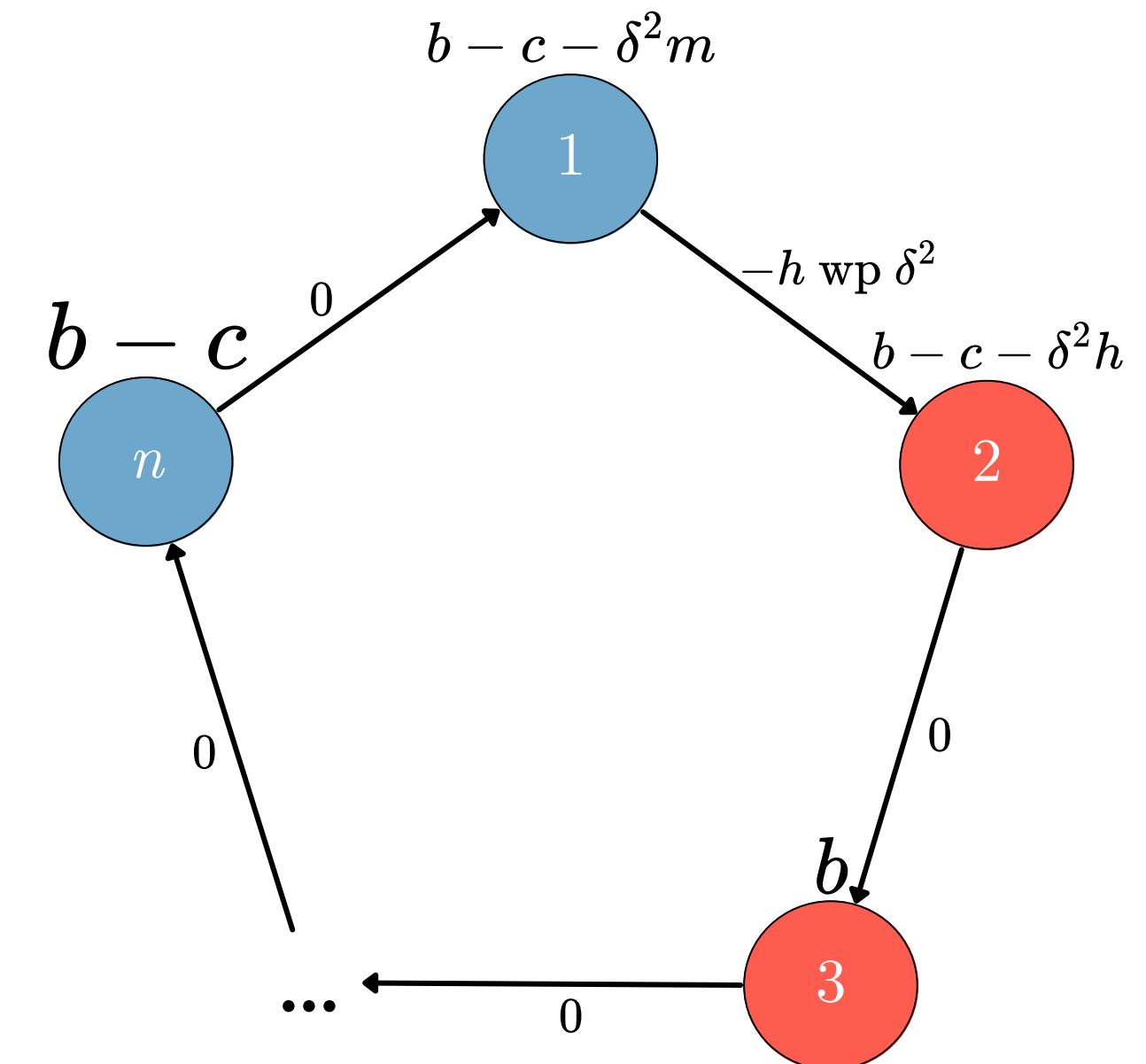
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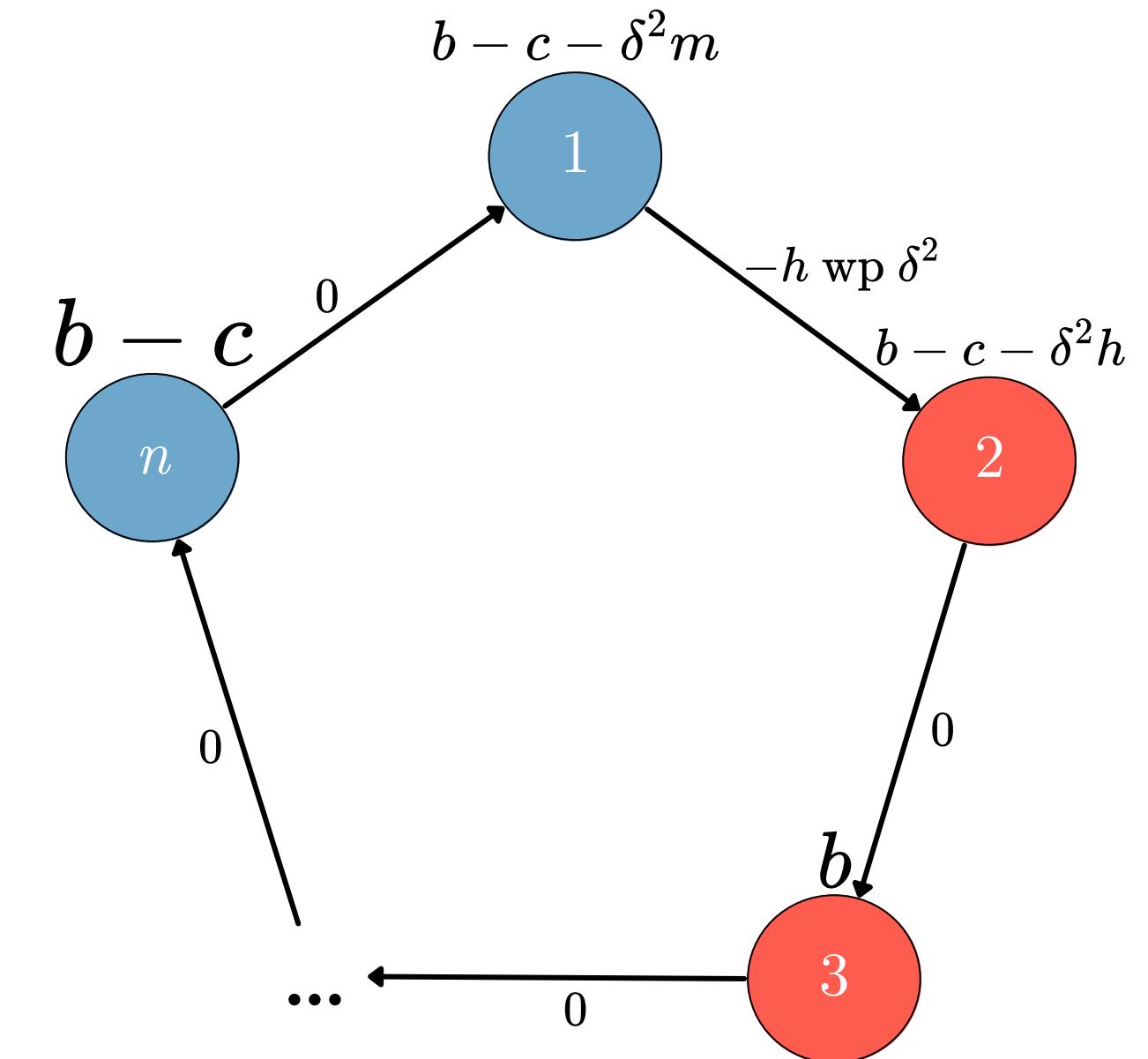
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If some player deviates at a round i by not punishing a defector, they get punished at the next round by the player upstream. This is not worth it as long as:

$$b - c - \delta^i m > b - c - \delta^{i+1} h \quad \text{iff}$$

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So, if players are willing to monitor and punish each other, if the penalties are high enough, and if the game goes on long enough, cooperation can be maintained.

So, if players are willing to monitor and punish each other, if the penalties are high enough, and if the game goes on long enough, cooperation can be maintained. Lots of ifs.



EREZ YOELI

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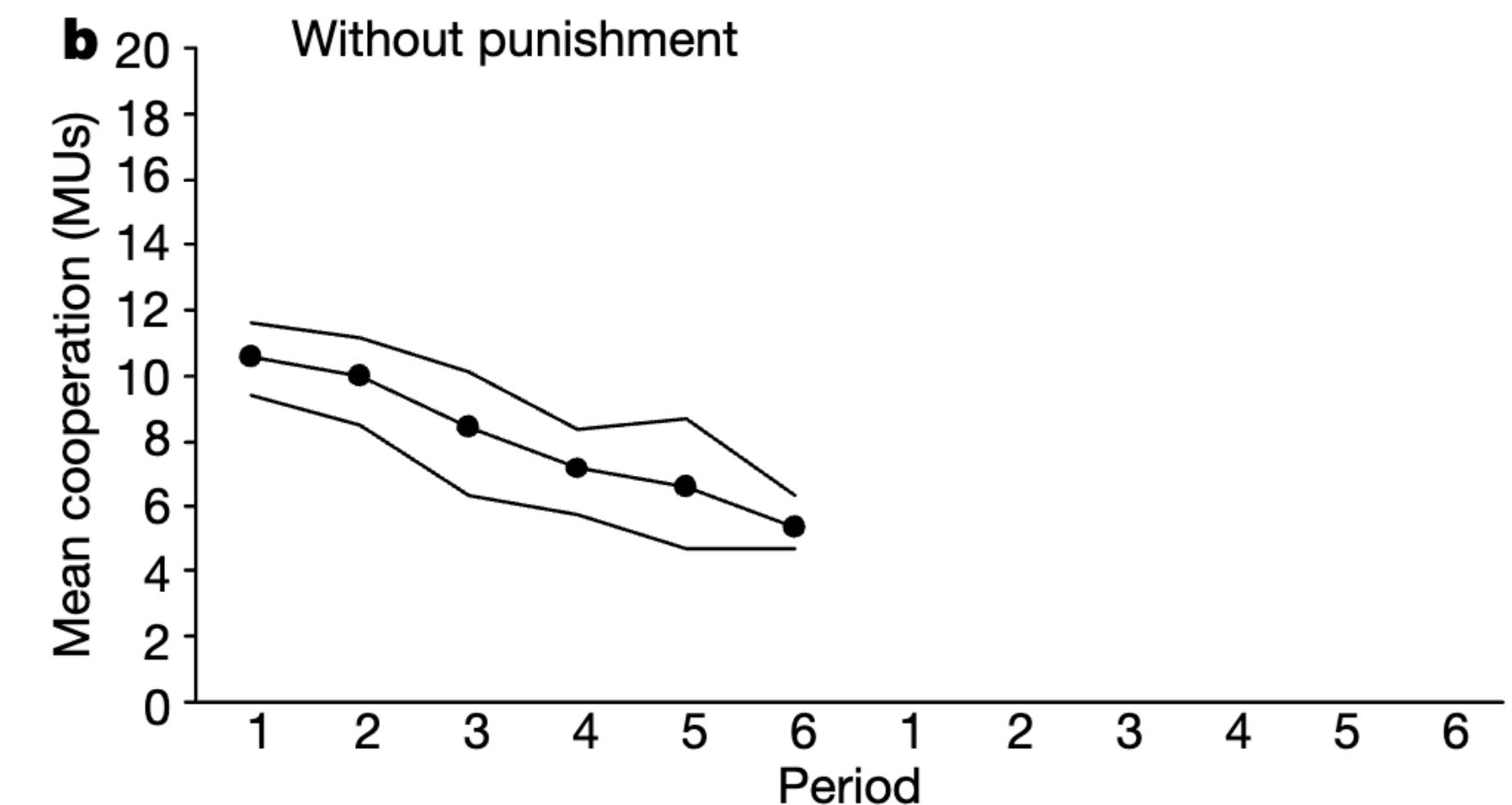
MOSHE HOFFMAN
What do people do?

In the lab people generally contribute above the Nash equilibrium.

PUBLIC GOODS GAMES: EXPERIMENTS

Contributions typically decline over time (are people learning the Nash equilibrium?...)

But generally they start above 0.



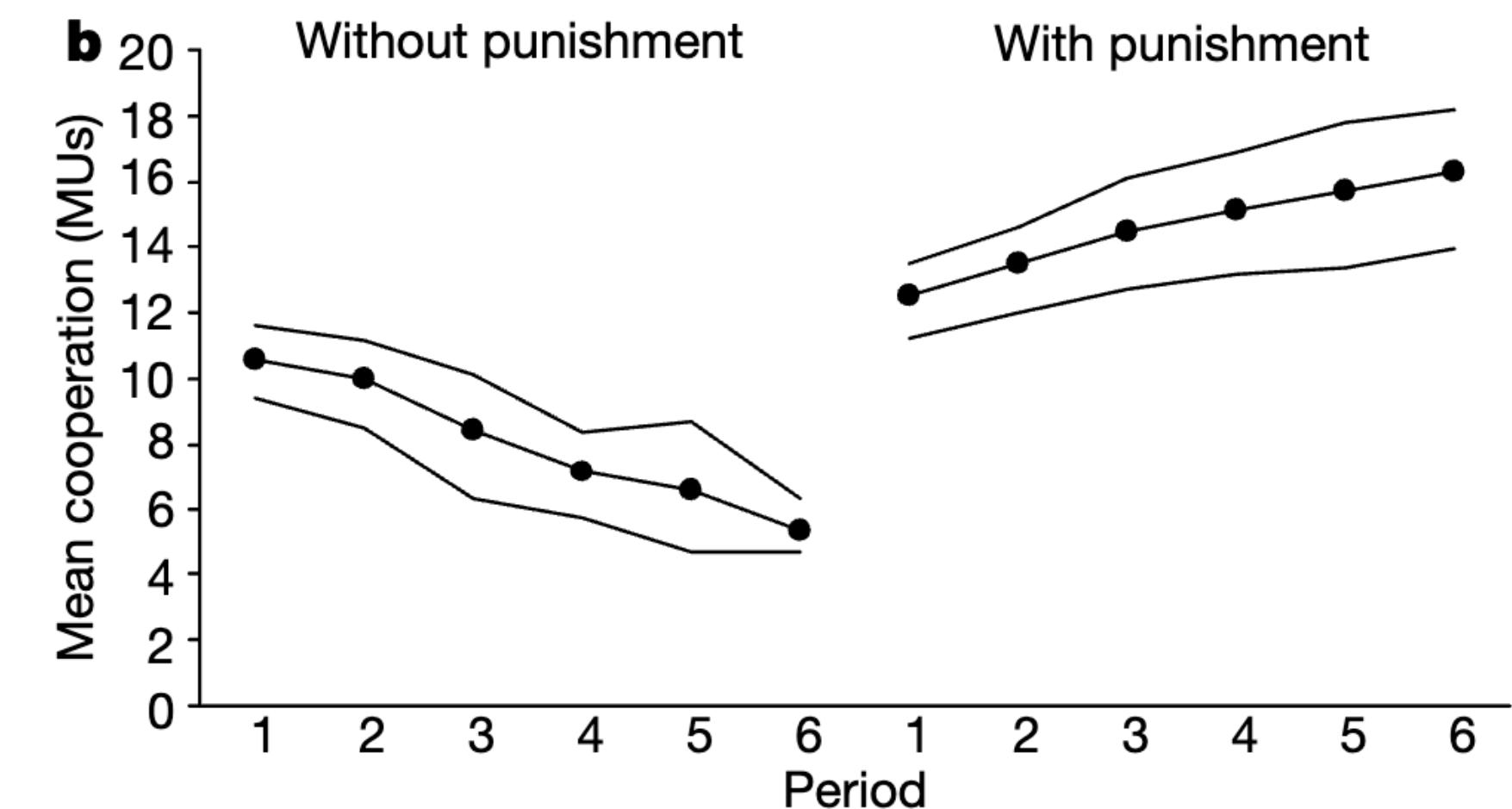
Fehr, E., & Gächter, S. (2002). Altruistic punishment in humans. *Nature*, 415(6868), 137–140.

PUBLIC GOODS GAMES: EXPERIMENTS

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But generally they start above 0.

Punishment helps (!).*



*Interesting, considering that people could default to the other equilibrium.

Fehr, E., & Gächter, S. (2002). Altruistic punishment in humans. *Nature*, 415(6868), 137–140.

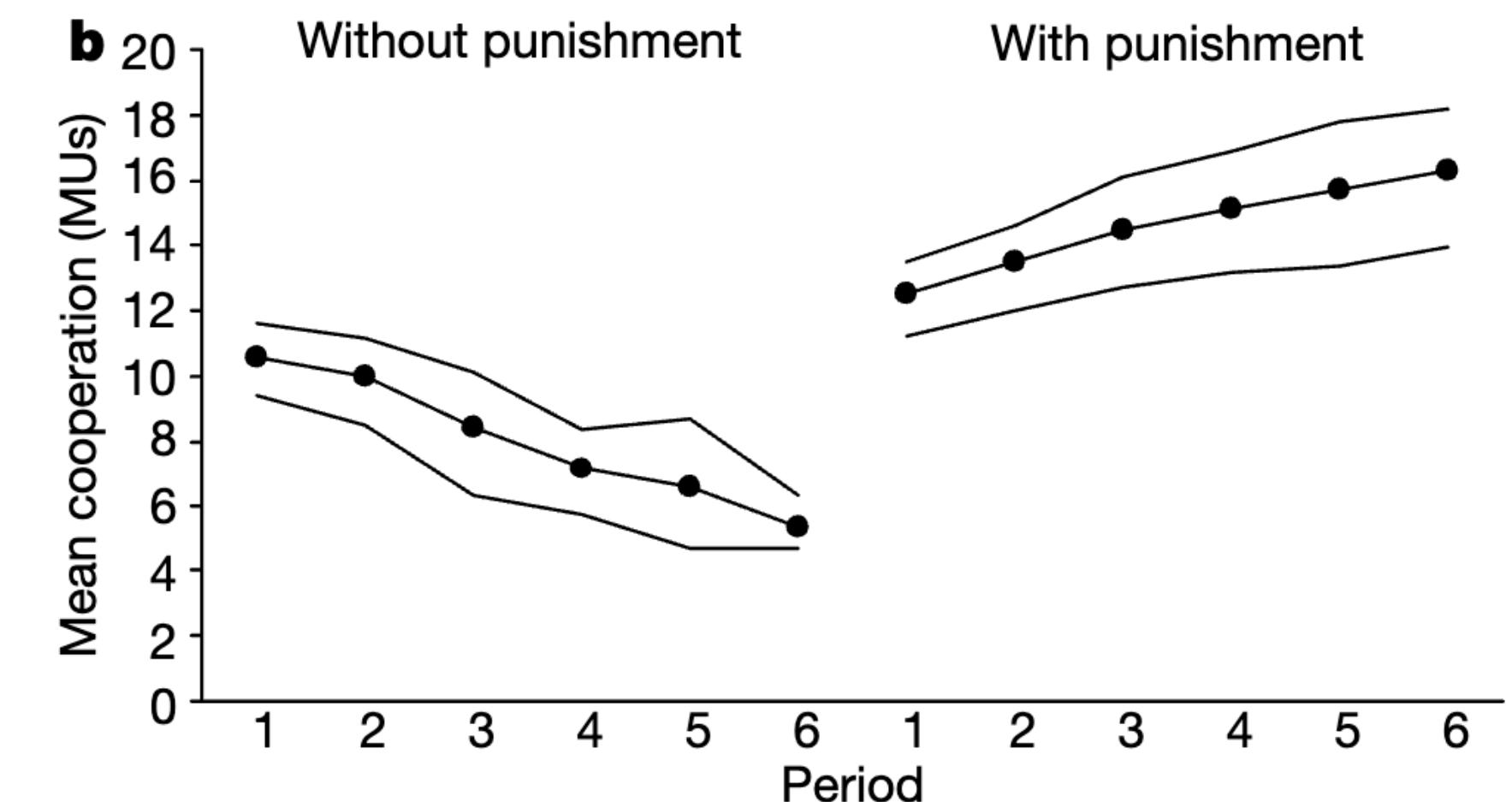
PUBLIC GOODS GAMES: EXPERIMENTS

Contributions typically decline over time (are people learning the Nash equilibrium?...)

But generally they start above 0.

Punishment helps (!).*

Explaining these trends is an ongoing field of research.



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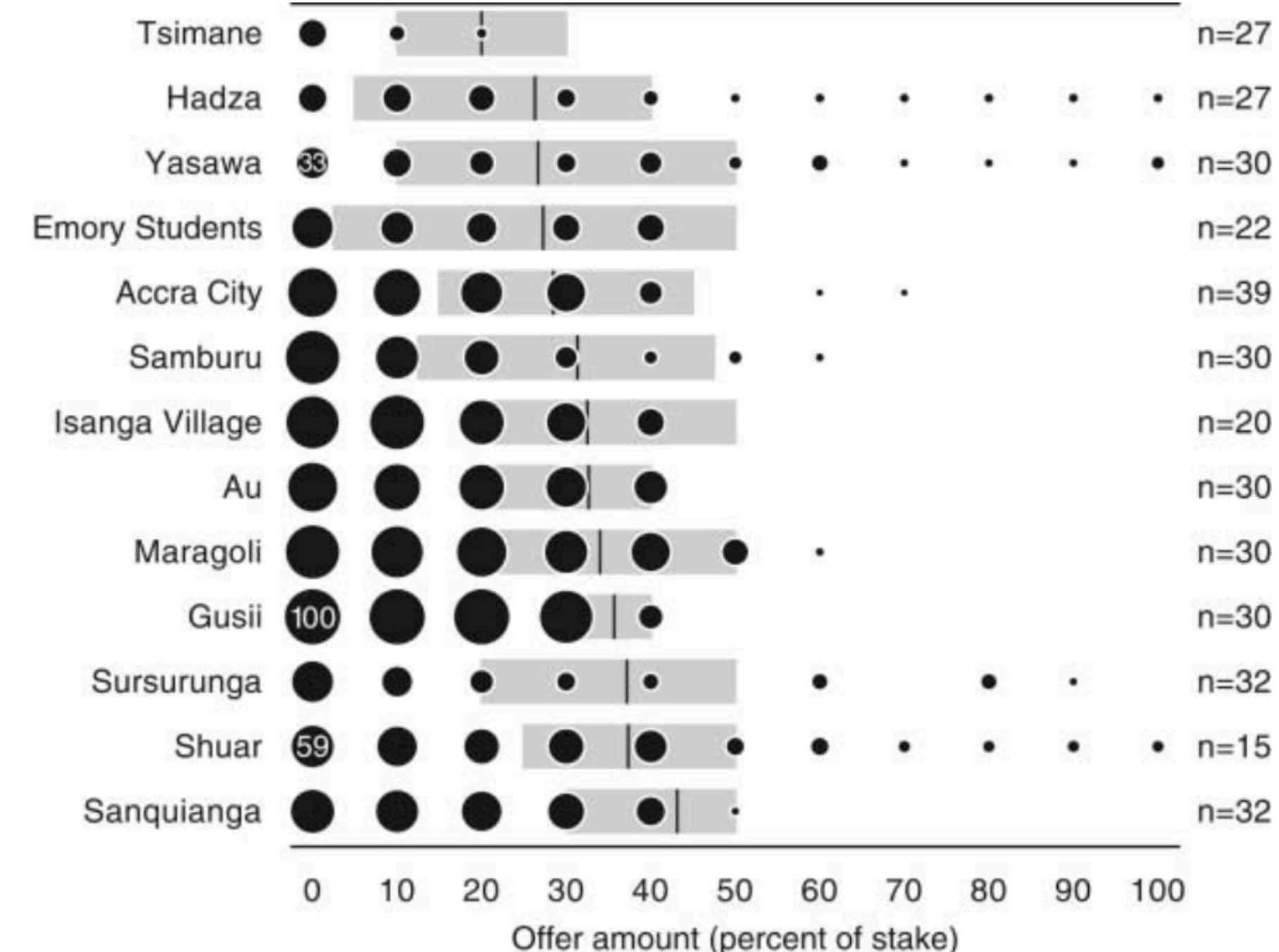
Fehr, E., & Gächter, S. (2002). Altruistic punishment in humans. *Nature*, 415(6868), 137–140.

Interestingly, people seem willing to punish even when the transgression does not affect them personally (third-party punishment).

THIRD PARTY PUNISHMENT GAME

A third party can punish unfair splits in a Dictator game, at a personal cost.

The size of the bubble shows the fraction of people willing to punish at that split.

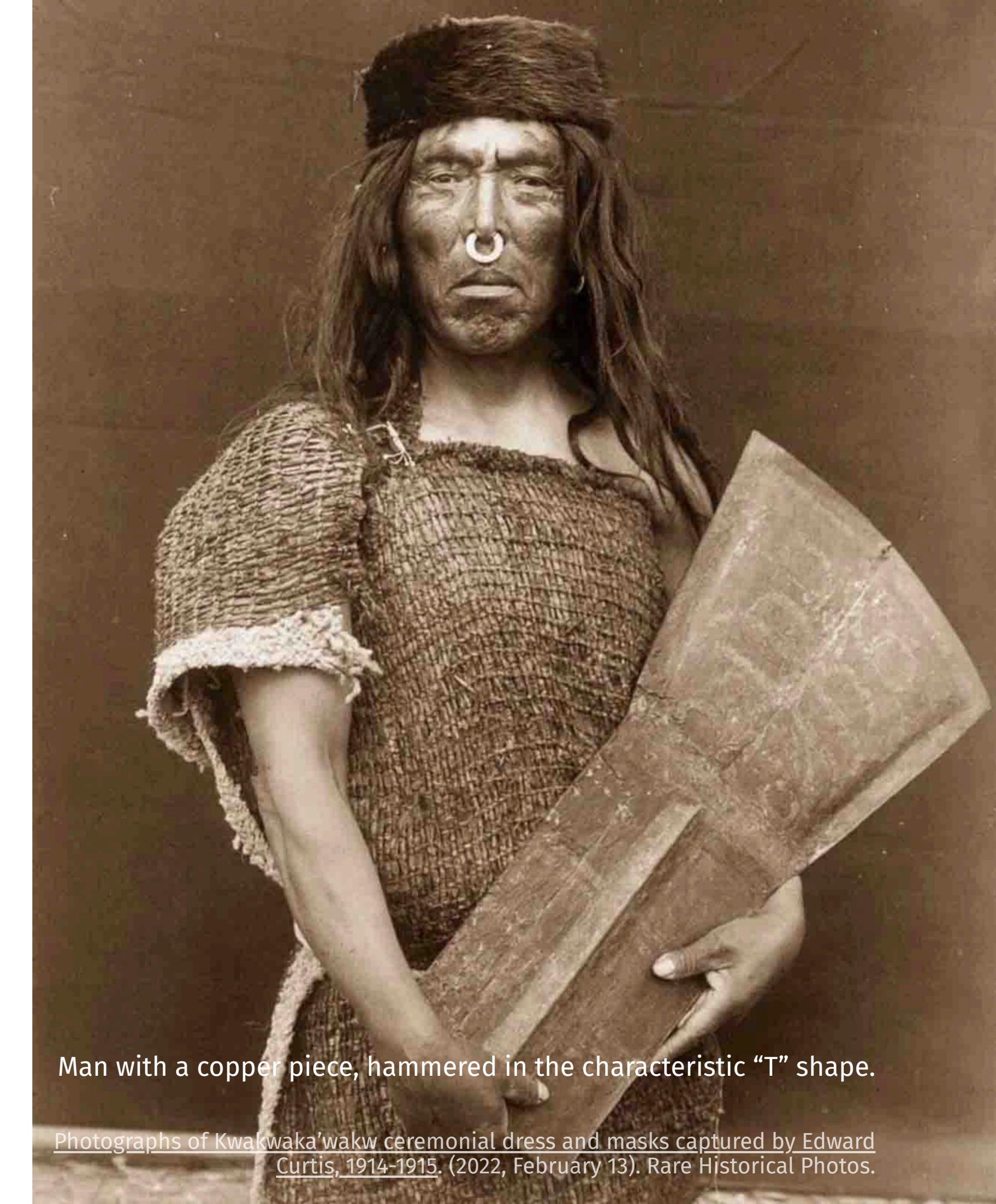


Henrich, J., McElreath, R., Barr, A., Ensminger, J., Barrett, C., Bolyanatz, A., Cardenas, J. C., Gurven, M., Gwako, E., Henrich, N., Lesorogol, C., Marlowe, F., Tracer, D., & Ziker, J. (2006). Costly punishment across human societies. *Science*, 312(5781), 1767–1770.

Anecdotally, virtuous chains of contributions are also a mainstay of many cultures.

POTLATCH

The Kwakw̱aka'wakw are an indigenous group of the Pacific Northwest Coast, in southwestern Canada.



Man with a copper piece, hammered in the characteristic “T” shape.

Photographs of Kwakwaka'wakw ceremonial dress and masks captured by Edward Curtis, 1914-1915. (2022, February 13). Rare Historical Photos.

POTLATCH

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Clan chiefs stage winter feasts (*potlatches*) where they shower rivals with blankets, carved copper ‘shields,’ today even washing-machines.



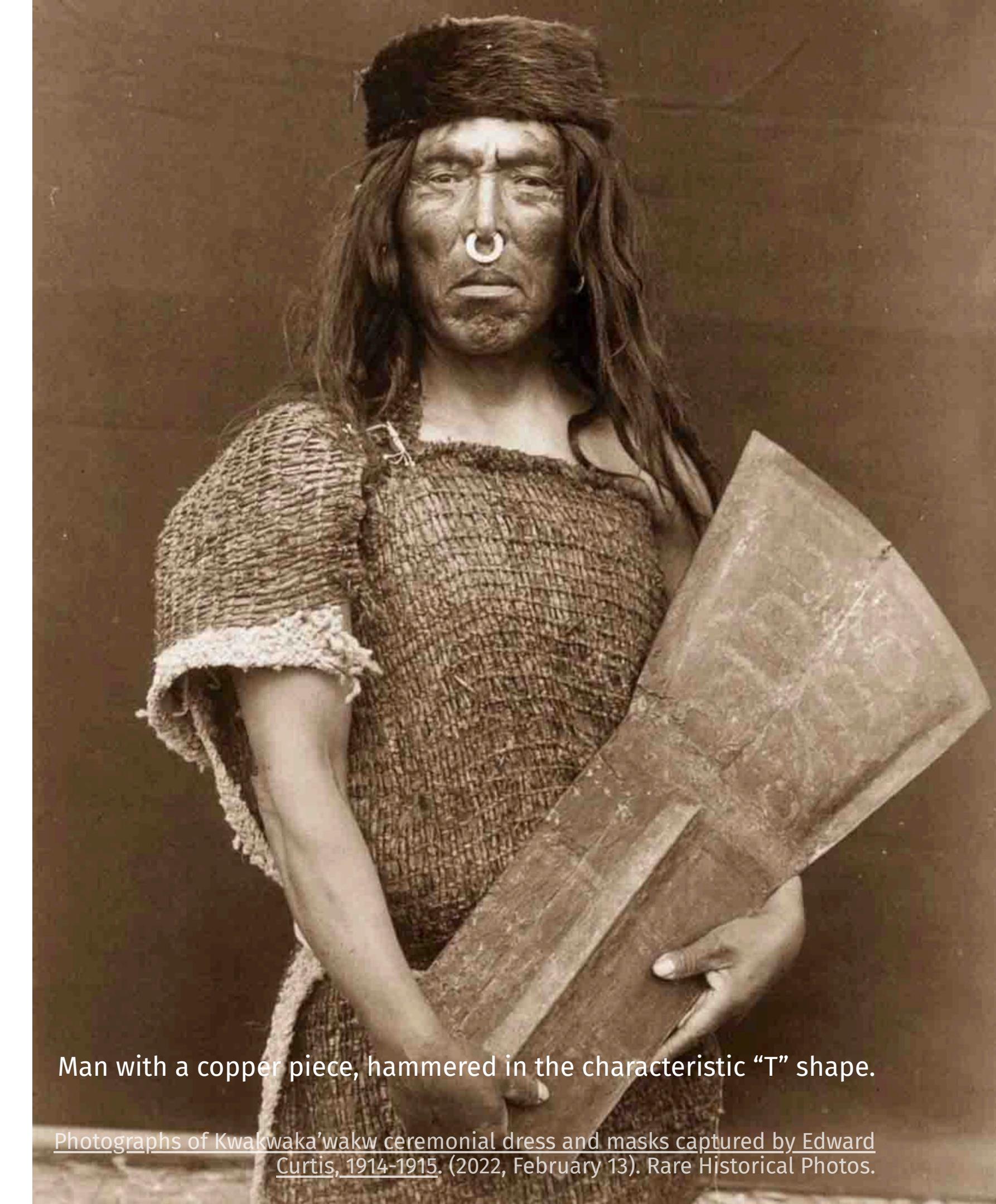
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To keep rank, the honoured guests must later exceed the donation.



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People also seem willing to engage in *higher-order punishment*: punishing those who do not punish.



TURKANA RAIDS

A black and white photograph showing several Turkana men on horseback. They are wearing traditional shukas (wrap) and headgear. Some are holding rifles, and they appear to be in a dry, open landscape, possibly during a raid.

The Turkana are semi-nomadic pastoralists based in North-Western Kenya.

They periodically organize large-scale raids against neighboring ethnic groups to acquire cattle, and gain access to pasture and watering sites.

Mathew, S., & Boyd, R. (2014). The cost of cowardice: punitive sentiments towards free riders in Turkana raids. *Evolution and Human Behavior*, 35(1), 58–64.

TURKANA RAIDS

A black and white photograph showing several Turkana men on horseback. They are wearing traditional headgear and carrying rifles. The setting is a dry, open landscape with sparse vegetation.

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Freeriders are frowned upon and punished.

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So are people who do not punish freeriders.

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ERNST FEHR

It seems that nature has endowed us with a disposition to punish wrongdoers.



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It seems that nature has endowed us with a disposition to punish wrongdoers.

SIMON GÄCHTER

Punishment, in this sense, is an altruistic act.
And demands explanation...



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