The deviation is not worth it just in case:

$$2 + 2\delta + 2\delta^2 + \dots + 2\delta^{k-1} + 2\delta^k + \dots \ge 2 + 2\delta + 2\delta^2 + \dots + 2\delta^{k-1} + 3\delta^k$$
 iff 
$$2\delta^k + 2\delta^{k+1} + \dots \ge 3\delta^k$$
 iff 
$$2\delta + 2\delta^2 + \dots > 1$$
 iff

$$2\delta$$

$$2\delta(1+\delta+\ldots) \ge 1$$

$$1 + \delta + \dots) \ge 1$$

$$2\delta \cdot \frac{1}{2\delta} > 1$$

iff

$$2\delta \cdot \frac{1}{1-\delta} \ge 1$$

$$2\delta \cdot \frac{1}{1-\delta} \ge 1$$

$$\delta \ge \frac{1}{2}.$$