

One can check that if Player 1 plays $s_1 = (0.9, 0.1)$, then the strategy that maximizes Player 2's expected utility is $s'_2 = (0, 1)$.

In other words, $s'_2 = (0, 1)$ is Player 2's *best response* to $s_1 = (0.9, 0.1)$.

So is $s = (s_1, s'_2)$ a Nash equilibrium?

No! If Player 2 plays $s'_2 = (0, 1)$, Player 1 wants to deviate to $s'_1 = (1, 0)$:

$$\begin{aligned}\mathbb{E}[s_1 \mid s'_2] &= \mathbb{E}[\text{Heads} \mid s'_2] \cdot 0.9 + \mathbb{E}[\text{Tails} \mid s'_2] \cdot 0.1 \\ &= (-1) \cdot 0.9 + 1 \cdot 0.1 \\ &= -0.8\end{aligned}$$