$r_i = \hat{q}_i - \lfloor \hat{q}_i \rfloor$