The network grows by adding agents that listen to the central agent 1.

The eigenvector centralities are:

$$\boldsymbol{c} = \left(\frac{1}{2}, \frac{1}{2(n-1)}, \ldots, \frac{1}{2(n-1)} \right)$$

Agent 1 retains a constant share of (network) influence as n grows.

And thus decides the consensus belief.

No bueno.