

Take  $\mathbf{p} = (p_1, \dots, p_n)$  to be the vector of competences of  $n$  voters.

Note, first, that if we improve the competence of one voter, then the probability of a correct majority decision increases.

Formally, suppose we replace some  $p_i$  in  $\mathbf{p}$  with  $p'_i > p_i$ , while keeping all other competences the same. We say the resulting vector  $\mathbf{p}'$  is *improvement* of  $\mathbf{p}$ .

If  $S'_n$  is the sum of the votes determined by  $\mathbf{p}'$ , we have that:

$$\Pr[S'_n > n/2] > \Pr[S_n > n/2]$$

Note, now, that we can get from  $\mathbf{p}^* = (1/2 + \varepsilon, \dots, 1/2 + \varepsilon)$  to any  $\mathbf{p} = (p_1, \dots, p_n)$  by a series of improvements.

But we already know, from the Condorcet Jury Theorem, that the group accuracy of  $\mathbf{p}^*$  approaches 1 asymptotically.

So the accuracy of  $\mathbf{p}$  does the same.