

Lesson 3: Order of Operations and Exponents

Objectives

- To understand how to identify the correct order of operations.
- To simplify expressions using order of operations.
- To understand the three main properties of exponents.
- To define and use negative exponents.

Terms

- Order of Operations
- Simplify
- Base
- Power
- Product Property
- Quotient Property
- Power Property

Think about this:

What can you do with the following expressions?

1. $2 + 5 - 3 - 1 + 10$	2. $2 \times (5 - 3) \times 1 + 10$	3. $2 \times 5 - (3 \times 1) \times 10$
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Answer these questions in the space provided:

1. What steps did you take to get to each value?
2. Did you get the same answers? Why or why not?
3. What does it mean to simplify?

Definitions:

Order of Operations: Tells us how to _____ expressions that have more than one operation. Also known as _____.

Simplify: To apply _____ indicated in an expression to write in the most _____, concise form.

Use Order of Operations to simplify the expressions:

1. $(1 + 4) \times 3 - \underline{\hspace{2cm}}$

2. $\underline{\hspace{2cm}} - (28 \div 2) - 1$

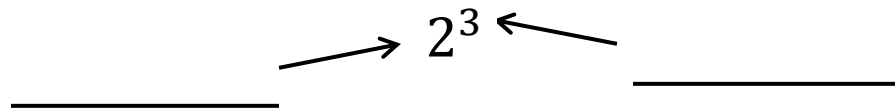
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Think about this:

How do you simplify the following?

1. $2^3 + 3^2$	2. $(1 + 4)^2 \times 3 + \underline{\hspace{2cm}}$	3. $(1 + 4)^2 \times 3 - \underline{\hspace{2cm}}$
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Label the Diagram:



Discuss: In this example, what does this format tell us to do?

- This tells us to: $\underline{\hspace{2cm}}$ the $\underline{\hspace{2cm}}$ of $\underline{\hspace{2cm}}$ by itself $\underline{\hspace{2cm}}$ times.
- We read it as: $\underline{\hspace{4cm}}$
- If there is no exponent stated: $\underline{\hspace{4cm}}$

Product Property

How do we simplify this expression?

<i>Original Expression</i>
<i>Write in $\underline{\hspace{2cm}}$ form</i>
<i>Write as a single exponential expression</i>

Definition:

Product Property of Exponents: When we multiply two exponential expressions with the same $\underline{\hspace{2cm}}$ we can $\underline{\hspace{2cm}}$ the exponents and keep the $\underline{\hspace{2cm}}$.

General Rule: $x^a \cdot x^b =$

Example: $m^2 \cdot m^3 =$

Practice: simplify the expression by using the Product Property of Exponents.

$$y^{15} \cdot y^4$$

$$2^2 \cdot 2^4$$

Answer:

Answer:

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Practice: expand and simplify the expressions.

$$\frac{n^7}{n^3} =$$

Answer:

$$\frac{8^8}{8^5} =$$

Answer:

Quotient Property

How do we simplify this expression?

$\frac{x^5}{x^2}$	<i>Original expression</i>
	<i>Write in expanded form</i>
	<i>Factor forms of one</i>
	<i>Write as a single exponential expression</i>

Definition:

Quotient Property of Exponents: When we divide two exponential expressions with the same _____ we can _____ the exponents and keep the _____.

General Rule: $\frac{x^a}{x^b} =$

Example: $\frac{g^5}{g^2} =$

Practice: expand and simplify the expression by using the Power Property of Exponents.

$$(m^2n^3)^5$$

Answer:

$$(2m^6)^2$$

Answer:

Power Property

How do we simplify this expression?

$(x^4)^2$	<i>Original expression</i>
	<i>Expand the outside exponent</i>
	<i>Expand each exponential expression</i>
	<i>Write as a single exponential expression</i>

Definition:

Power Property of Exponents: When we have an exponential expression raised to another exponent, we can _____ the exponents and keep the _____.

General Rule: $(x^a)^b =$

Example: $(3z^3)^2 =$

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Negative Exponents: How do we define a negative exponent?

10^3	10^2	10^1	10^0	10^{-1}	10^{-2}	10^{-3}

How do we simplify this expression?

2^{-3}	<i>Original Expression</i>
	<i>Rewrite without negative exponents</i>
	<i>Evaluate 2^{-3}</i>

Definition:

Negative exponent: to rewrite an expression with a negative exponent to have a positive exponent, find the _____.

General Rule: $x^{-n} =$

Example: $x^{-2} =$

Practice: simplify the expression by using the Power Property of Exponents.

$$x^2 \cdot x^{-6}$$

$$\frac{1}{a^{-3}}$$

Answer:

Answer:

Discuss:

1. Where do exponents occur in PEMDAS?
2. If you aren't sure about a rule, what can you do to help simplify exponential expressions?
3. **Note:** Almost anything to the power of _____ is _____.

Where will you see these concepts in upcoming material?	What are the calculator skills you needed?
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