

# Lesson 3: Order of Operations and Exponents

Objectives	Terms
<ul style="list-style-type: none"><li>To understand how to identify the correct order of operations.</li><li>To simplify expressions using order of operations.</li><li>To understand the three main properties of exponents.</li><li>To define and use negative exponents.</li></ul>	<ul style="list-style-type: none"><li>Order of Operations</li><li>Simplify</li><li>Base</li><li>Power</li><li>Product Property</li><li>Quotient Property</li><li>Power Property</li></ul>

Think about this:

What can you do with the following expressions?

1.  $2 + 5 - 3 - 1 + 10$

2.  $2 \times (5 - 3) \times 1 + 10$

3.  $2 \times 5 - (3 \times 1) \times 10$

Answer these questions in the space provided:

1. What steps did you take to get to each value?
2. Did you get the same answers? Why or why not?
3. What does it mean to simplify?

## Definitions:

**Order of Operations:** Tells us how to

\_\_\_\_\_ expressions that have more than one operation. Also known as \_\_\_\_\_.

**Simplify:** To apply \_\_\_\_\_ indicated in an expression to write in the most \_\_\_\_\_, concise form.

## Use Order of Operations to simplify the expressions:

1.  $(1 + 4) \times 3 -$  \_\_\_\_\_

2. \_\_\_\_\_ -  $(28 \div 2) - 1$

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Think about this:

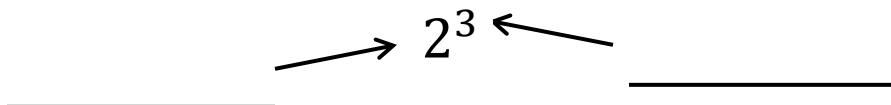
How do you simplify the following?

1.  $2^3 + 3^2$

2.  $(1 + 4)^2 \times 3 + \underline{\hspace{2cm}}$

3.  $(1 + 4)^2 \times 3 - \underline{\hspace{2cm}}$

Label the Diagram:



Discuss: In this example, what does this format tell us to do?

- This tells us to: \_\_\_\_\_ the \_\_\_\_\_ of \_\_\_\_\_ by itself \_\_\_\_\_ times.
- We read it as: \_\_\_\_\_
- If there is no exponent stated: \_\_\_\_\_

### Product Property

How do we simplify this expression?

<i>Original Expression</i>
<i>Write in _____ form</i>
<i>Write as a single exponential expression</i>

Definition:

**Product Property of Exponents:** When we multiply two exponential expressions with the same \_\_\_\_\_ we can \_\_\_\_\_ the exponents and keep the \_\_\_\_\_.

General Rule:  $x^a \cdot x^b =$

Example:  $m^2 \cdot m^3 =$

Practice: simplify the expression by using the Product Property of Exponents.

$y^{15} \cdot y^4$

$2^2 \cdot 2^4$

Answer:

Answer:

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Practice: expand and simplify the expressions.

$$\frac{n^7}{n^3} =$$

Answer:

$$\frac{8^8}{8^5} =$$

Answer:

### Quotient Property

How do we simplify this expression?

$\frac{x^5}{x^2}$	Original expression
	Write in expanded form
	Factor forms of one
	Write as a single exponential expression

Definition:

**Quotient Property of Exponents:** When we divide two exponential expressions with the same \_\_\_\_\_ we can \_\_\_\_\_ the exponents and keep the \_\_\_\_\_.

General Rule:  $\frac{x^a}{x^b} =$

Example:  $\frac{g^5}{g^2} =$

Practice: expand and simplify the expression by using the Power Property of Exponents.

$$(m^2n^3)^5$$

Answer:

$$(2m^6)^2$$

Answer:

### Power Property

How do we simplify this expression?

$(x^4)^2$	Original expression
	Expand the outside exponent
	Expand each exponential expression
	Write as a single exponential expression

Definition:

**Power Property of Exponents:** When we have an exponential expression raised to another exponent, we can \_\_\_\_\_ the exponents and keep the \_\_\_\_\_.

General Rule:  $(x^a)^b =$

Example:  $(3z^3)^2 =$

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**Negative Exponents: How do we define a negative exponent?**

$10^3$	$10^2$	$10^1$	$10^0$	$10^{-1}$	$10^{-2}$	$10^{-3}$

**How do we simplify this expression?**

$$2^{-3}$$

*Original Expression*

*Rewrite without negative exponents*

*Evaluate  $2^{-3}$*

**Definition:**

**Negative exponent:** to rewrite an expression with a negative exponent to have a positive exponent, find the \_\_\_\_\_.

**General Rule:**  $x^{-n} =$

**Example:**  $x^{-2} =$

**Practice: simplify the expression by using the Power Property of Exponents.**

$$x^2 \cdot x^{-6}$$

$$\frac{1}{a^{-3}}$$

**Answer:**

**Answer:**

**Discuss:**

1. Where do exponents occur in PEMDAS?
2. If you aren't sure about a rule, what can you do to help simplify exponential expressions?
3. **Note:** Almost anything to the power of \_\_\_\_\_ is \_\_\_\_\_.

Where will you see these concepts in upcoming material?

What are the calculator skills you needed?