

CV

Project 5: Connected Components

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My Algorithms:

connectPass1(int connectness):

This method takes the connectness input, 4 or 8, and performs the first pass of the connected component. My algorithm uses an array list and 2 case methods. 1 and 3. Case 2 is excluded because it is essentially case 3 without updating the equivalency table.

If there is one nonzero neighbor, case 2 applies. If there are 2 or more non zero neighbor case 2 or 3 apply. If the min and the max of these are the same then case 2. If the min and max are different, case 3. Either way, the current pixel gets the min value of the neighbors. I skipped this step and applied it if case 1 doesn't apply, and update the EQ table iff case 3 is true.

- 1) **Loop:** $i \rightarrow [1 \text{ to } \text{numRows}]$
 - a) **Loop:** $j \rightarrow [1 \text{ to } \text{numCols}]$
 - i) $\text{pixel} \leftarrow \text{zeroFramedAry}[i][j]$
 - ii) if $\text{pixel} > 0$
 - (1) $\text{Array}\langle \rangle \text{temp} \leftarrow \text{tempArr}(\text{set: } 1, \text{connectness: } 4 \text{ or } 8, i, j) \text{ // all neighbors}$
 - (2) if $\text{case1}(\text{temp})$:
 - (a) $\text{zeroFramedAry}[i][j] \leftarrow ++\text{newLabel}$
 - (b) $\text{EQtable}[\text{newLabel}] \leftarrow \text{newLabel}$
 - (3) Else
 - (a) $\text{min} \leftarrow \text{minValue}(\text{temp})$
 - (b) $\text{zeroFramedAry}[i][j] \leftarrow \text{min}$
 - (c) if $\text{case3}(\text{temp})$:
 - (i) **Loop:** $t \rightarrow \text{temp}$:
 1. $\text{EQtable}[t] \leftarrow \text{min}$

Array<> tempArr(set, connectness, i, j):

This function loads all the neighbors of the pixel into an array list, excluding zeros. Integer SET is used to switch the neighbors, either (b or g) and (d or e) for 4 -connectedness (Integer CONNECTNESS) and (a or f) and (c or h) for 8-connectedness.

Boolean case1(temp):

Case 1 checks if all the values in the array excluding the current pixel are zero. This is done by calculating the size of the array since any element in temp is not zero.

Boolean case3(temp):

Case 3 checks if the min and max from the neighbor array are not equal.

connectPass2(connectness):

Similar to pass1, it only used the connectness(4 or 8) to perform the algorithms second pass.

- 1) $\text{flag} \leftarrow \text{true}$

- 2) **Loop:** $i \rightarrow [\text{numRows}-1 \rightarrow 1]$
 - a) **Loop:** $j \rightarrow [\text{numCols}-1 \rightarrow 1]$
 - i) $\text{pixel} \leftarrow \text{zeroFramedAry}[i][j]$
 - ii) if $\text{pixel} > 0$
 - (1) $\text{Array} \leftarrow \text{tempArr}(\text{set: } -1, \text{connectness: } 4 \text{ or } 8, i, j)$ // all neighbors
 - (2) Loop: $t \rightarrow \text{temp}$:
 - (a) If $t \neq \text{pixel}$:
 - (i) $\text{Flag} \leftarrow \text{false}$
 - (3) If $\text{flag} == \text{false}$:
 - (a) $\text{Min} \leftarrow \text{getMin}(\text{temp})$
 - (b) $\text{changeLabels}(\text{connectness}, \text{min}, i, j)$
 - (c) $\text{zeroFramedAry}[i][j] \leftarrow \text{min}$
 - (d) $\text{flag} \leftarrow \text{true}$
 - (e) $\text{EQtable}[\text{pixel}] \leftarrow \text{min}$

changeLabels(connectness, min, i, j):

This changes the neighbor elements if they are not equal to zero

```
/*
Computer Vision
Project 5
Created by Adrian Noa

usage:

java adrian_noa_main.java 8 data1 pretty label property

*/

import java.util.*;
import java.io.*;

// import

public class CVProject5 {
    public static void main(String[] args) throws IOException {
        if (args.length != 5) {
            System.out.println("Not enough of arguments");
            return;
        }

        try {
            // Scanner inFile = new Scanner(new File(args[1]));
            Scanner inFile = readFile(args[1]);
            BufferedWriter prettyPrintFile = createFile(args[2]);
            BufferedWriter labelFile = createFile(args[3]);
            BufferedWriter propertyFile = createFile(args[4]);
        } {

            ConnCompLabel connCompLabel = new ConnCompLabel(inFile);

            // step 1
            connCompLabel.zero2D(connCompLabel.zeroFramedAry);

            // step 2
            connCompLabel.loadImage(inFile);
        }
    }
}
```

```

// step 3
int whichConnectness = Integer.parseInt(args[0]);

// step 4 & 5

connComplabel.connectPass1(whichConnectness); // pass 1
prettyPrintFile.write("\n");
connComplabel.makeBorder(prettyPrintFile);
prettyPrintFile.write("Result of Pass 1: \n");
connComplabel.makeBorder(prettyPrintFile);
connComplabel.imgReformat(prettyPrintFile);
connComplabel.makeBorder(prettyPrintFile);
prettyPrintFile.write("Equivalence Array after Pass 1: \n");
connComplabel.makeBorder(prettyPrintFile);
connComplabel.printEQary(prettyPrintFile);
connComplabel.makeBorder(prettyPrintFile);
prettyPrintFile.write("\n");

connComplabel.connectPass2(whichConnectness); // pass 2
prettyPrintFile.write("\n");
connComplabel.makeBorder(prettyPrintFile);
prettyPrintFile.write("Result of Pass 2: \n");
connComplabel.makeBorder(prettyPrintFile);
connComplabel.imgReformat(prettyPrintFile);
connComplabel.makeBorder(prettyPrintFile);
prettyPrintFile.write("Equivalence Array after Pass 2: \n");
connComplabel.makeBorder(prettyPrintFile);
connComplabel.printEQary(prettyPrintFile);
connComplabel.makeBorder(prettyPrintFile);
prettyPrintFile.write("\n");

// step 6
connComplabel.trueNumCC = connComplabel.manageEQary();
connComplabel.makeBorder(prettyPrintFile);
prettyPrintFile.write("Equivalence Array after management: \n");
connComplabel.makeBorder(prettyPrintFile);
connComplabel.printEQary(prettyPrintFile);
connComplabel.makeBorder(prettyPrintFile);
connComplabel.newMin = 0;
connComplabel.newMax = connComplabel.trueNumCC;
connComplabel.allocateCCproperty(connComplabel.trueNumCC);

// step 7
connComplabel.connectPass3(connComplabel.zeroFramedAry,
connComplabel.CCproperty);

// step 8
prettyPrintFile.write("\n");
connComplabel.makeBorder(prettyPrintFile);
prettyPrintFile.write("Algorithm Pass 3 \n"); // pass 3
connComplabel.makeBorder(prettyPrintFile);
connComplabel.imgReformat(prettyPrintFile);

// step 9
connComplabel.makeBorder(prettyPrintFile);
prettyPrintFile.write("Equivalence Array after Pass 3 \n");
connComplabel.makeBorder(prettyPrintFile);
connComplabel.printEQary(prettyPrintFile);
connComplabel.makeBorder(prettyPrintFile);

// step 10
labelFile.write(Integer.toString(connComplabel.numRows)+" ");
labelFile.write(Integer.toString(connComplabel.numCols)+" ");
labelFile.write(Integer.toString(connComplabel.newMin)+" ");
labelFile.write(Integer.toString(connComplabel.newMax)+"\n");

// step 11
connComplabel.printImg(labelFile);

// step 12
connComplabel.printCCproperty(propertyFile);

```

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        // step 13
        connCompLabel.drawBoxes(connCompLabel.CCproperty);

        // step 14
        prettyPrintFile.write("\n");
        connCompLabel.makeBorder(prettyPrintFile);
        prettyPrintFile.write("Bounding Boxes result:\n");
        connCompLabel.makeBorder(prettyPrintFile);
        connCompLabel.imgReformat(prettyPrintFile);
        connCompLabel.makeBorder(prettyPrintFile);

        // step 15
        prettyPrintFile.write("Number of Connected Components: " +
            Integer.toString(connCompLabel.trueNumCC)+"\n");
        connCompLabel.makeBorder(prettyPrintFile);

        System.out.println();
    }
}

public static Scanner readFile(String str) throws IOException{
    return new Scanner(new BufferedReader(new FileReader(str)));
}

public static BufferedWriter createFile(String str) throws IOException{
    return new BufferedWriter(new FileWriter(str));
}
}

class Property {
    int label = 0;
    int numPixels = 0;
    int minR = 0;
    int minC = 0;
    int maxR = 0;
    int maxC = 0;
}

class ConnCompLabel extends Property {
    int numRows, numCols, minVal, maxVal, newLabel, newMin, newMax, trueNumCC;
    int zeroFramedAry[][];
    int nonZeroNeighborAry[];
    int EquivalenceArray[];
    Property[] CCproperty;

    ConnCompLabel(Scanner inFile) {
        this.numRows = inFile.nextInt();
        this.numCols = inFile.nextInt();
        this.minVal = inFile.nextInt();
        this.maxVal = inFile.nextInt();
        this.newLabel = 0;
        this.zeroFramedAry = new int[numRows + 2][numCols + 2];
        this.nonZeroNeighborAry = new int[5];
        this.EquivalenceArray = new int[(numRows * numCols) / 4];
    }

    public int[][] zero2D(int[][] arr) {
        /*
         * Initialize a 2-D array to zero
         */
        for (int i = 0; i < numRows; i++) {
            for (int j = 0; j < numCols; j++) {
                arr[i][j] = 0;
            }
        }
        return arr;
    }

    public void loadImage(Scanner b) throws IOException {
        /*
         * Read from input file and write to zeroFramedAry
         * begin at (1,1)

```

```

        */
        for (int i = 1; i <= numRows; i++) {
            for (int j = 1; j <= numCols; j++) {
                this.zeroFramedAry[i][j] = b.nextInt();
            }
        }
    }

    public void imgReformat(BufferedWriter file) throws IOException {
        for (int i = 1; i <= this.numRows; i++) {
            for (int j = 1; j <= this.numCols; j++) {
                if (this.zeroFramedAry[i][j] == 0)
                    file.write(". ");
                else if (this.zeroFramedAry[i][j] >= 10)
                    file.write(Integer.toString(this.zeroFramedAry[i][j]) + " ");
                else file.write(Integer.toString(this.zeroFramedAry[i][j]) + " ");
            }
            file.write("\n");
        }
    }

    public ArrayList<Integer> tempArr(int set, int connectness, int i, int j) {

        // a b c
        //
        // d P(i,j) e
        //
        // f g h
        ArrayList<Integer> temp = new ArrayList<Integer>();
        temp.add(this.zeroFramedAry[i + (-1)*set][j]); // b or g
        temp.add(this.zeroFramedAry[i][j + (-1)*set]); // d or e

        ArrayList<Integer> zero = new ArrayList<Integer>();
        zero.add(0);
        if (connectness == 8) {
            temp.add(this.zeroFramedAry[i + (-1)*set][j - 1]); // a or f
            temp.add(this.zeroFramedAry[i + (-1)*set][j + 1]); // c or h
        }
        temp.removeAll(zero);
        return temp;
    }

    public void changeLabels(int connectness, int val, int i, int j){
        if(this.zeroFramedAry[i + 1][j] != 0 )
            this.zeroFramedAry[i + 1][j] = val; // g

        if(this.zeroFramedAry[i][j + 1] != 0 )
            this.zeroFramedAry[i][j + 1] = val; // e

        if (connectness == 8) {
            if(this.zeroFramedAry[i + 1][j - 1] != 0 )
                this.zeroFramedAry[i + 1][j - 1] = val; // f
            if(this.zeroFramedAry[i + 1][j + 1] != 0 )
                this.zeroFramedAry[i + 1][j + 1] = val; // h
        }
    }

    public boolean case1(ArrayList<Integer> arr) {

        // if(Arrays.stream(arr).sum() == 0)
        if (arr.size() == 0) {
            System.out.print(" - case1 - all are zero\n");
            return true;
        }
        return false;
    }

    public boolean case2(ArrayList<Integer> arr) {

        // if( Arrays.stream(arr).min() == Arrays.stream(arr).max() ){
        if (arr.stream().mapToInt(Integer::intValue).min().getAsInt() ==
arr.stream().mapToInt(Integer::intValue).max())

```

```

        .getAsInt()) {
            System.out.print(" - case2\n");
            return true;
        }
        return false;
    }

    public boolean case3(ArrayList<Integer> arr) {

        // if( Arrays.stream(arr).min() == Arrays.stream(arr).max() ){
        if (arr.stream().mapToInt(Integer::intValue).min().getAsInt() !=
arr.stream().mapToInt(Integer::intValue).max()
        .getAsInt()) {
            System.out.print(" - case3\n");
            return true;
        }
        return false;
    }

    public void printMap() {
        for (int i = 1; i <= this.numRows; i++) {
            for (int j = 1; j <= this.numCols; j++) {
                if (this.zeroFramedAry[i][j] == 0)
                    System.out.print(". ");
                else if(this.zeroFramedAry[i][j]>=10)
                    System.out.print(this.zeroFramedAry[i][j]+" ");
                else System.out.print(this.zeroFramedAry[i][j]+" ");
            }
            System.out.print("\n");
        }
    }

    public void connectPass1(int connectness) {
        for (int i = 1; i <= this.numRows; i++)
            for (int j = 1; j <= this.numCols; j++) {
                int pixel = this.zeroFramedAry[i][j];
                if (pixel > 0) {
                    ArrayList<Integer> temp = tempArr(1, connectness, i, j);
                    if (case1(temp)) {
                        this.zeroFramedAry[i][j] = ++this.newLabel;
                        updateEquivalencyTable(this.newLabel, this.newLabel);
                    } else {
                        int min = temp.stream().mapToInt(Integer::intValue).min().getAsInt();

                        this.zeroFramedAry[i][j] = min;

                        if(case3(temp)){
                            for(int t:temp)
                                updateEquivalencyTable(t,min);
                        }
                    }
                }
            }
    }

    public void connectPass2(int connectness) {

        boolean flag = true;
        for (int i = this.numRows-1; i >= 1; i--) {
            for (int j = this.numCols-1; j >= 1; j--) {
                int pixel = zeroFramedAry[i][j];
                if (pixel > 0) {
                    ArrayList<Integer> temp = tempArr(-1, connectness, i, j);
                    for(int t:temp) if(t!=pixel) flag=false;
                    // case 3
                    if(!flag) {
                        int min = temp.stream().mapToInt(Integer::intValue).min().getAsInt();
                        changeLabels(connectness, min, i, j);
                        zeroFramedAry[i][j] = min;
                        flag = true;
                        updateEquivalencyTable(pixel, min);
                    }
                }
            }
        }
    }

```

```

    }
}

public void connectPass3(int[][] inArr, Property[] CCproperty) {
    int k = 0;
    int nummPixs;
    int pixel;
    for (int i = 1; i <= this.trueNumCC; i++) {
        this.CCproperty[i].label = i;
        this.CCproperty[i].numPixels = 0;
        this.CCproperty[i].minR = this.numRows;
        this.CCproperty[i].maxR = 0;
        this.CCproperty[i].minC = this.numCols;
        this.CCproperty[i].maxC = 0;
    }
    for (int r = 1; r <= this.numRows; r++) {
        for (int c = 1; c <= this.numCols; c++) {
            pixel = inArr[r][c];
            if (pixel > 0) {
                inArr[r][c] = this.EquivalenceArray[pixel];
                k = inArr[r][c];
                nummPixs = this.CCproperty[k].numPixels;
                CCproperty[k].numPixels = ++nummPixs;
                if (r < this.CCproperty[k].minR) {
                    this.CCproperty[k].minR = r - 1;
                }
                if (r > this.CCproperty[k].maxR) {
                    this.CCproperty[k].maxR = r - 1;
                }
                if (c < this.CCproperty[k].minC) {
                    this.CCproperty[k].minC = c - 1;
                }
                if (c > this.CCproperty[k].maxC) {
                    this.CCproperty[k].maxC = c - 1;
                }
            }
        }
    }
}

public void allocateCCProperty(int truenumcc) {
    this.CCproperty = new Property[truenumcc + 1];
    for (int i = 0; i <= truenumcc; i++) {
        this.CCproperty[i] = new Property();
    }
}

public void drawBoxes(Property[] CCproperty) {
    int minRow, minCol, maxRow, maxCol, label;
    for (int index = 1; index <= this.trueNumCC; index++) {
        minRow = this.CCproperty[index].minR + 1;
        minCol = this.CCproperty[index].minC + 1;
        maxRow = this.CCproperty[index].maxR + 1;
        maxCol = this.CCproperty[index].maxC + 1;
        label = this.CCproperty[index].label;

        for (int i = minCol; i <= maxCol; i++) {
            this.zeroFramedAry[minRow][i] = label;
            this.zeroFramedAry[maxRow][i] = label;
        }
        for (int i = minRow; i <= maxRow; i++) {
            this.zeroFramedAry[i][minCol] = label;
            this.zeroFramedAry[i][maxCol] = label;
        }
    }
}

public void updateEquivalencyTable(int index, int label) {
    this.EquivalenceArray[index] = label;
}

```

```

public int manageEQary() {
    int counter = 0;
    for (int i = 1; i < this.EquivalenceArray.length; i++) {
        if (i == this.EquivalenceArray[i]) {
            this.EquivalenceArray[i] = ++counter;
        } else {
            this.EquivalenceArray[i] = this.EquivalenceArray[this.EquivalenceArray[i]];
        }
    }
    return counter;
}

public void printCCproperty(BufferedWriter out) throws IOException {
    out.write(Integer.toString(this.numRows) + " ");
    out.write(Integer.toString(this.numCols) + " ");
    out.write(Integer.toString(this.minVal) + " ");
    out.write(Integer.toString(this.trueNumCC) + " \n");
    out.write(Integer.toString(this.trueNumCC) + " \n");
    for (int i = 1; i <= this.trueNumCC; i++) {
        out.write(Integer.toString(this.CCproperty[i].label) + "\n");
        out.write(Integer.toString(this.CCproperty[i].numPixels) + "\n");
        out.write(Integer.toString(this.CCproperty[i].minR) + " ");
        out.write(Integer.toString(this.CCproperty[i].minC) + "\n");
        out.write(Integer.toString(this.CCproperty[i].maxR) + " ");
        out.write(Integer.toString(this.CCproperty[i].maxC) + "\n");
    }
}

public void printEQary(BufferedWriter file) throws IOException {
    for (int i = 1; i <= this.newLabel; i++)
        file.write(Integer.toString(this.EquivalenceArray[i]) + " ");
    file.write("\n");
}

public void printImg(BufferedWriter out) throws IOException {
    String str = Integer.toString(this.maxVal);
    int width = str.length();

    for (int r = 1; r <= this.numRows; r++) {
        for (int c = 1; c <= this.numCols; c++) {
            if (this.zeroFramedArray[r][c] > 0) {
                out.write(Integer.toString(this.zeroFramedArray[r][c]));
            } else {
                out.write(".");
            }
            String str2 = Integer.toString(this.zeroFramedArray[r][c]);
            int width2 = str2.length();
            out.write(" ");
            while (width2 < width) {
                out.write(" ");
                width2++;
            }
        }
        out.write("\n");
    }
}

public void makeBorder(BufferedWriter out) throws IOException {
    for (int i = 0; i <= this.numRows + 1; i++) {
        out.write("---");
    }
    out.write("\n");
}
}

```


Data1 8-connectness outputs

```
pretty2
1  -----
2  Result of Pass 1:
3  -----
4  1  1  .  2  .  .  3  .  4  .
5  .  1  .  .  2  2  .  3  .  4  .
6  .  1  .  .  2  .  3  .  4  .
7  1  1  .  .  2  .  3  .  4  4
8  1  .  1  1  .  .  3  .  4  .
9  .  .  .  .  1  1  1  1  .  .
10 .  .  5  .  .  .  .  1  .  1
11 6  5  5  5  .  .  1  .  1  .
12 5  .  5  .  5  1  1  1  .  .
13 .  .  .  .  .  1  .  1  .  .
14 -----
15 Equivalence Array after Pass 1:
16 -----
17 1 1 1 1 1 5
18 -----
19
20 -----
21
22 Result of Pass 2:
23 -----
24 1  1  .  1  .  .  1  .  1  .
25 .  1  .  1  1  .  1  .  1  .
26 .  1  .  .  1  .  1  .  1  .
27 1  1  .  .  1  .  1  .  1  1
28 1  .  1  1  .  .  1  .  1  .
29 .  .  .  .  1  1  1  1  1  .
30 .  .  1  .  .  .  .  1  .  1
31 1  1  1  1  .  .  1  .  1  .
32 1  .  1  .  1  1  1  1  .  .
33 .  .  .  .  .  1  .  1  .  .
34 -----
35 Equivalence Array after Pass 2:
36 -----
37 1 1 1 1 1 1
38 -----
39
40 -----
41 Equivalence Array after management:
42 -----
43 1 1 1 1 1 1
44 -----
45

pretty2
45
46 -----
47 Algorithm Pass 3
48 -----
49 1  1  .  1  .  .  1  .  1  .
50 .  1  .  1  1  .  1  .  1  .
51 .  1  .  .  1  .  1  .  1  .
52 1  1  .  .  1  .  1  .  1  1
53 1  .  1  1  .  .  1  .  1  .
54 .  .  .  .  1  1  1  1  .  .
55 .  .  1  .  .  .  .  1  .  1
56 1  1  1  1  .  .  1  .  1  .
57 1  .  1  .  1  1  1  1  .  .
58 .  .  .  .  .  1  .  1  .  .
59 -----
60 Equivalence Array after Pass 3
61 -----
62 1 1 1 1 1 1
63 -----
64
65 -----
66 Bounding Boxes result:
67 -----
68 1  1  1  1  1  1  1  1  1  1
69 1  1  .  1  1  .  1  .  1  1
70 1  1  .  .  1  .  1  .  1  1
71 1  1  .  .  1  .  1  .  1  1
72 1  .  1  1  .  .  1  .  1  1
73 1  .  .  .  1  1  1  1  1  1
74 1  .  1  .  .  .  .  1  .  1
75 1  1  1  1  .  .  1  .  1  1
76 1  .  1  .  1  1  1  1  .  1
77 1  1  1  1  1  1  1  1  1  1
78 -----
79 Number of Connected Components: 1
80 -----
81
```

```
label
1 10 10 0 1
2 1 1 . 1 . . 1 . 1 .
3 . 1 . 1 1 . 1 . 1 .
4 . 1 . . 1 . 1 . 1 .
5 1 1 . . 1 . 1 . 1 1
6 1 . 1 1 . . 1 . 1 .
7 . . . . 1 1 1 1 1 .
8 . . 1 . . . . 1 . 1
9 1 1 1 1 . . 1 . 1 .
10 1 . 1 . 1 1 1 1 . .
11 . . . . . 1 . 1 . .
12

property
1 10 10 0 1
2 1
3 1
4 47
5 0 0
6 9 9
7
```

Data1 4-Connectedness outputs

```
pretty2
1 -----
2 Result of Pass 1:
3 -----
4 1 1 . 2 . . 3 . 4 .
5 . 1 . 2 2 . 3 . 4 .
6 . 1 . . 2 . 3 . 4 .
7 5 1 . . 2 . 3 . 4 4
8 5 . 6 6 . . 3 . 4 .
9 . . . . 7 7 3 3 3 .
10 . . 8 . . . . 3 . 9
11 10 10 8 8 . . 11 . 12 .
12 10 . 8 . 13 13 11 11 . .
13 . . . . 13 . 11 . .
14 -----
15 Equivalence Array after Pass 1:
16 -----
17 1 2 3 3 1 6 3 8 9 8 11 12 11
18 -----
19
20 -----
21
22 Result of Pass 2:
23 -----
24 1 1 . 2 . . 3 . 3 .
25 . 1 . 2 2 . 3 . 3 .
26 . 1 . . 2 . 3 . 3 .
27 1 1 . . 2 . 3 . 3 3
28 1 . 6 6 . . 3 . 3 .
29 . . . . 3 3 3 3 3 .
30 . . 8 . . . . 3 . 9
31 8 8 8 8 . . 11 . 12 .
32 8 . 8 . 11 11 11 11 . .
33 . . . . 11 . 11 . .
34 -----
35 Equivalence Array after Pass 2:
36 -----
37 1 2 3 3 1 6 3 8 9 8 11 12 11
38 -----
39
40 -----
41 Equivalence Array after management:
42 -----
43 1 2 3 3 1 4 3 5 6 5 7 8 7
44 -----
```

```
pretty2
44 -----
45
46 -----
47 Algorithm Pass 3
48 -----
49 1 1 . 2 . . 3 . 3 .
50 . 1 . 2 2 . 3 . 3 .
51 . 1 . . 2 . 3 . 3 .
52 1 1 . . 2 . 3 . 3 3
53 1 . 4 4 . . 3 . 3 .
54 . . . . 3 3 3 3 3 .
55 . . 5 . . . . 3 . 6
56 5 5 5 5 . . 7 . 8 .
57 5 . 5 . 7 7 7 7 . .
58 . . . . 7 . 7 . .
59 -----
60 Equivalence Array after Pass 3
61 -----
62 1 2 3 3 1 4 3 5 6 5 7 8 7
63 -----
64
65 -----
66 Bounding Boxes result:
67 -----
68 1 1 . 2 3 3 3 3 3 3
69 1 1 . 2 3 . 3 . 3 3
70 1 1 . 2 3 . 3 . 3 3
71 1 1 . 2 3 . 3 . 3 3
72 1 1 4 4 3 . 3 . 3 3
73 . . . . 3 3 3 3 3 3
74 5 5 5 5 3 3 3 3 3 6
75 5 5 5 5 7 7 7 7 8 .
76 5 5 5 5 7 7 7 7 . .
77 . . . . 7 7 7 7 . .
78 -----
79 Number of Connected Components: 8
80 -----
81
```

```
property
1 10 10 0 8
2 8
3 1
4 7
5 0 0
6 4 1
7 2
8 5
9 0 3
10 3 4
11 3
12 17
13 0 4
14 6 9
15 4
16 2
17 4 2
18 4 3
19 5
20 7
21 6 0
22 8 3
23 6
24 1
25 6 10
26 6 9
27 7
28 7
29 7 4
30 9 7
31 8
32 1
33 7 8
34 7 8
35
```

```
label
1 10 10 0 8
2 1 1 . 2 . . 3 . 3 .
3 . 1 . 2 2 . 3 . 3 .
4 . 1 . . 2 . 3 . 3 .
5 1 1 . . 2 . 3 . 3 3
6 1 . 4 4 . . 3 . 3 .
7 . . . . 3 3 3 3 3 .
8 . . 5 . . . . 3 . 6
9 5 5 5 5 . . 7 . 8 .
10 5 . 5 . 7 7 7 7 . .
11 . . . . 7 . 7 . .
12
```

Data2 4-connectness outputs:

Result of Pass 1:

Equivalence Array after Pass 1:

1 2 3 4 5 5 7 5 9 10 1 12 13 14 13 16 17 18 19 17 21 22 23 24 25 26 27 22 29 30 31 31 24 24 35 36 37

Result of Pass 2:

Equivalence Array after Pass 2:

1 2 3 3 4 5 7 3 9 10 1 12 13 14 13 16 13 18 19 13 21 22 22 24 22 22 27 22 29 30 31 31 24 24 35 36 37

Equivalence Array after management:

1 2 3 3 3 3 4 3 5 6 1 7 8 9 8 10 8 11 12 8 13 14 14 15 14 14 16 14 17 18 19 19 15 15 20 21 22

1 2 3 3 3 4 3 5 6 1 7 8 9 8 10 8 11 12 8 13 14 14 15 14 14 16 14 17 18 19 19 15 15 20 21 22

pecs 7				property	pecs 7				property
1	30	35	0	22	46	16	32		
2	22				47	12			
3	1				48	1			
4	44				49	16	7		
5	1	5			50	16	7		
6	12	14			51	13			
7	2				52	1			
8	4				53	17	6		
9	1	30			54	17	6		
10	3	31			55	14			
11	3				56	39			
12	37				57	18	3		
13	2	23			58	29	10		
14	10	30			59	15			
15	4				60	33			
16	1				61	18	27		
17	7	5			62	29	32		
18	7	5			63	16			
19	5				64	1			
20	1				65	20	12		
21	8	6			66	20	12		
22	8	6			67	17			
23	6				68	3			
24	1				69	21	13		
25	9	7			70	23	13		
26	9	7			71	18			
27	7				72	5			
28	1				73	24	14		
29	13	10			74	28	14		
30	13	10			75	19			
31	8				76	9			
32	73				77	25	9		
33	13	17			78	29	10		
34	28	24			79	20			
35	9				80	1			
36	1				81	30	13		
37	14	9			82	29	13		
38	14	9			83	21			
39	10				84	1			
40	1				85	30	15		
41	15	8			86	29	15		
42	15	8			87	22			
43	11				88	1			
44	4				89	30	24		
45	15	31			90	29	24		

Data2 8-connectness outputs:

[illegible]

1 2 3 3 3 3 4 3 5 6 1 7 8 9 8 10 8 11 12 8 13 14 14 15 14 14 16 14 17 18 19 19 15 15 20 21 22

1 2 3 3 3 3 4 3 5 6 1 7 8 9 8 10 8 11 12 8 13 14 14 15 14 14 16 14 17 18 19 19 15 15 20 21 22

specs >	property	specs >	property
1	30 35 0 22	38	14 9
2	22	39	10
3	1	40	1
4	44	41	15 8
5	1 5	42	15 8
6	12 14	43	11
7	2	44	4
8	4	45	15 31
9	1 30	46	16 32
10	3 31	47	12
11	3	48	1
12	37	49	16 7
13	2 23	50	16 7
14	10 30	51	13
15	4	52	1
16	1	53	17 6
17	7 5	54	17 6
18	7 5	55	14
19	5	56	39
20	1	57	18 3
21	8 6	58	29 10
22	8 6	59	15
23	6	60	33
24	1	61	18 27
25	9 7	62	29 32
26	9 7	63	16
27	7	64	1
28	1	65	20 12
29	13 10	66	20 12
30	13 10	67	17
31	8	68	3
32	73	69	21 13
33	13 17	70	23 13
34	28 24	71	18
35	9	72	5
36	1	73	24 14
37	14 9	74	28 14
38	14 9	75	19
39	10	76	9
40	1	77	25 9
41	15 8	78	29 10
42	15 8	79	20
43	11	80	1
44	4	81	30 13
45	15 31	82	29 13
46	16 32	83	21
47	12	84	1
48	1	85	30 15
49	16 7	86	29 15
50	16 7	87	22
51	13	88	1
52	1	89	30 24
53	17 6	90	29 24
54	17 6	91	
55	14		
56	30		

specs >	label
1	30 35 0 22
2	.
3	. 1 1 1 1 1 1 1 1 1 1 2
4 1 1 1 1 1 1 1 1 1 1 3 3 3 . . 2 2 . . .
5 1 1 3 3 3 3 3 . 2
6 1 1 3 3 . . . 3 3
7 1 1 3 3 3 3
8 1 1 3 3 3 3
9 4 . . 1 1 3 3 3 3 3
10 5 . 1 1 3 3 . . . 3 3
11 6 . 1 1 3 3 3 3 3
12 1 1 1 1 3 3 3
13 1 1 1 1 1
14 1
15 7 8 8 8
16 9 8 8 8 8 8
17 10 8 8 8 . 8 8 8 11 11 . .
18 12 8 8 . . . 8 8 11 11 . .
19 13 8 8 . . . 8 8
20	. . . 14 14 14 . . . 14 14 8 8 8 8 15 15 . .
21	. . . 14 14 . . . 14 14 8 8 8 8 15 15 . .
22	. . . 14 14 . . 14 14 . . . 16 . . . 8 8 8 8 15 15 . .
23	. . . 14 14 . 14 14 17 . . 8 8 8 8 8 8 8 8 8 15 15 . .
24	. . . 14 14 . 14 14 17 . . 8 8 8 8 8 8 8 8 8 15 15 . .
25	. . . 14 14 14 14 17 . . 8 8 8 8 15 15 . .
26	. . . 14 14 . 14 14 18 . 8 8 8 8 15 15 . .
27	. . . 14 14 19 18 . 8 8 8 8 15 15 . .
28	. . . 14 14 . . . 19 19 18 . 8 8 8 8 . . 15 15 . 15 15 15 . .
29	. . . 14 14 . . . 19 19 18 . 8 8 8 8 . . . 15 15 . 15 15 . .
30	. . . 14 14 . . . 19 19 18 8 15 15 15 15
31	. . . 14 14 19 19 . . 20 . 21 22 15 15 15 15
32	