

For each of the following truth tables, write the disjunctive normal of the equation.

Table 1

x	y	$f(x,y)$
1	1	1
1	0	1
0	1	0
0	0	1

$$xy \vee x\bar{y} \vee \bar{x}\bar{y}$$

$$f(x,y)=$$

Table 2-3

x	y	z	$f(x,y,z)$
1	1	1	0
1	1	0	1
1	0	1	0
1	0	0	1
0	1	1	1
0	1	0	0
0	0	1	1
0	0	0	1

$$xy\bar{z} \vee x\bar{y}\bar{z} \vee \bar{x}yz \vee \bar{x}\bar{y}z \vee \bar{x}\bar{y}\bar{z}$$

$$f(x,y,z)=$$

Table 4-5

x	y	z	$f(x,y,z)$
1	1	1	1
1	1	0	1
1	0	1	0
1	0	0	1
0	1	1	0
0	1	0	1
0	0	1	0
0	0	0	1

$$xyz \vee xy\bar{z} \vee x\bar{y}\bar{z} \vee \bar{x}y\bar{z} \vee \bar{x}\bar{y}z$$

$$f(x,y,z)=$$

Table 6-7

W	x	y	z	$f(w, x, y, z)$
1	1	1	1	0
1	1	1	0	1
1	1	0	1	1
1	1	0	0	1
1	0	1	1	0
1	0	1	0	0
1	0	0	1	1
1	0	0	0	1
0	1	1	1	0
0	1	1	0	0
0	1	0	1	0
0	1	0	0	1
0	0	1	1	1
0	0	1	0	1
0	0	0	1	0
0	0	0	0	0

$$\begin{aligned}
 &wx\bar{y}\bar{z} \vee w\bar{x}\bar{y}z \vee w\bar{x}\bar{y}\bar{z} \\
 &\vee w\bar{x}\bar{y}z \vee w\bar{x}\bar{y}\bar{z} \\
 &\vee \bar{w}x\bar{y}\bar{z} \vee \bar{w}\bar{x}yz \\
 &\vee \bar{w}\bar{x}\bar{y}z
 \end{aligned}$$

$$f(w, x, y, z) =$$

For each of the following Boolean functions, write the expression in disjunctive normal form.

$$f(x, y) = (\bar{y})(\bar{x} \vee y) = \bar{x}\bar{y}$$

$$f(x, y) = x\bar{y} \vee \bar{x}y \vee x\bar{y} = x\bar{y} \vee \bar{x}y$$

$$\begin{aligned}
 f(x, y, z) = (\bar{x} \vee \bar{y})(\bar{x} \vee z) &= \bar{x}\bar{y}z \vee \bar{x}\bar{y}\bar{z} \vee \bar{x}\bar{y}z \vee \bar{x}\bar{y}\bar{z} \\
 &\vee x\bar{y}z
 \end{aligned}$$

$$\boxed{\bar{x} \vee \bar{y}z}$$

$$\begin{aligned}
 f(w, x, y, z) = \bar{w}y \vee \bar{x}y \vee x\bar{y}z &= \bar{w}x\bar{y}\bar{z} + \bar{w}x\bar{y}z + \bar{w}x\bar{y}\bar{z} + \bar{w}x\bar{y}z + \bar{w}x\bar{y}z \\
 &+ \bar{w}\bar{x}\bar{y}\bar{z} + \bar{w}\bar{x}\bar{y}z
 \end{aligned}$$

$$\boxed{\bar{x}\bar{y} + \bar{w}\bar{x}\bar{y} + \bar{w}\bar{x}\bar{y}z}$$

$$\begin{aligned}
 f(x, y, z) = \bar{x}(\bar{y} \vee xz)(\bar{y} \vee xz) &= \bar{w}x\bar{y}z + \bar{w}x\bar{y}\bar{z} + \bar{w}x\bar{y}z + \bar{w}x\bar{y}\bar{z} \\
 &+ \bar{w}x\bar{y}z + \bar{w}x\bar{y}\bar{z}
 \end{aligned}$$

$$\boxed{\bar{x}\bar{y} + \bar{x}\bar{y}z}$$

Name \_\_\_\_\_

III.

-32 16 8 4 2 1

-16 8 4 2 1

Write each decimal number in a 6-bit 2s complement representation.		Write each decimal number in a 5-bit 2s complement representation. What do you bubble on scantron?	
29 =	011101	-15 =	ABCDE A E 10001
13 =	001101	-13 =	ABCDE A D E 10011
6 =	000110	-6 =	ABCDE A B D 11010
0 =	000000	-1 =	ABCDE A B C D E 11111
-4 =	111100	0 =	ABCDE bubble nothing!
-19 =	101101	4 =	ABCDE C 00100
-27 =	100101	11 =	ABCDE B D E 01011
-32 =	100000	14 =	ABCDE B C D 01110

Perform the following 2s complement addition problems using 4-bit arithmetic. What would you bubble if the answer is zero? Would you ever bubble A only?

$$\begin{array}{r} 1101 \\ +1011 \\ \hline ABCDE \\ 1000 \\ B \end{array}$$

$$\begin{array}{r} 1010 \\ +1101 \\ \hline ABCDE \\ CDE \end{array}$$

$$\begin{array}{r} 0101 \\ +1010 \\ \hline ABCDE \\ BDE \end{array}$$

$$\begin{array}{r} 1001 \\ +0111 \\ \hline ABCDE \\ 0000 \\ \text{ABDE} \text{ for zero} \end{array}$$

**Half Adders**

Half adder	x	y	c	s
	1	1	1	0
	1	0	0	1
	0	1	0	1
	0	0	0	0

Write the Boolean function for c in a half adder:  $c = xy$

Write the Boolean function for s in a half adder:  $s = x \oplus y$

**Full Adder**

Write the Boolean function for c in a full adder:  $c = xy \vee xz \vee yz$

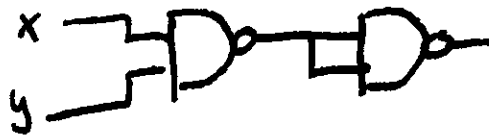
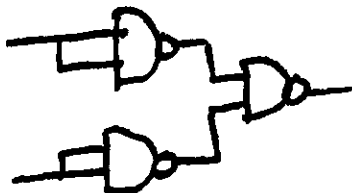
Write the Boolean function for s in a full adder:  $s = x \oplus y \oplus z$

Full adder

x	y	z	c	s
1	1	1	1	1
1	1	0	1	0
1	0	1	1	0
1	0	0	0	1
0	1	1	1	0
0	1	0	0	1
0	0	1	0	1
0	0	0	0	0

**NAND Implementations:**

Draw the NAND implementation for each of the following

NOT  $\neg x$ AND  $(x \wedge y)$ OR  $(x \vee y)$ 

$(xy) \vee (\bar{y}z)$  /\* Do not forget to simplify \*/

