

Ex: 9-19 odd, 25(1,5,9)

$$\begin{aligned} & \text{9 } wxyz \vee w\bar{x}\bar{y}z \vee w\bar{x}\bar{y}\bar{z} \vee w\bar{x}yz \vee w\bar{x}y\bar{z} \\ & \vee w\bar{x}\bar{y}\bar{z} \vee \bar{w}x\bar{y}\bar{z} \vee \bar{w}x\bar{y}z \vee \bar{w}x\bar{y}\bar{z} \\ & \vee \bar{w}\bar{x}y\bar{z} \vee \bar{w}\bar{x}y\bar{z} \end{aligned}$$

$$\text{11 } x \vee xy = x(y \vee \bar{y}) \vee xy = x\bar{y} \vee xy$$

$$\begin{aligned} \text{13 } f(x,y,z) &= x \vee y(x \vee \bar{z}) \\ &= x \vee xy \vee y\bar{z} \\ &= xyz \vee xy\bar{z} \vee x\bar{y}z \vee x\bar{y}\bar{z} \vee \bar{x}y\bar{z} \end{aligned}$$

$$\begin{aligned} \text{15 } f(x,y,z) &= (\bar{x}y \vee \bar{x}\bar{z})(\overline{x \vee yz}) \\ &= (\bar{x}y \vee \bar{x}\bar{z})(\bar{x}(\bar{y} \vee \bar{z})) = \bar{x}\bar{y} \vee \bar{x}\bar{z} \\ &= (\bar{x} \vee \bar{z})(\bar{x}\bar{y} \vee \bar{x}\bar{z}) = \bar{x}\bar{y} \vee \bar{x}\bar{z} \vee \bar{x}\bar{y}\bar{z} \vee \bar{x}\bar{z} \\ &= \bar{x}\bar{y}z \vee \bar{x}\bar{y}\bar{z} \vee \bar{x}y\bar{z} \end{aligned}$$

$$\begin{aligned} \text{17 } f(x,y,z) &= (x \vee \bar{x}y \vee \bar{x}y\bar{z})(xy \vee \bar{x}\bar{z})(y \vee xy\bar{z}) \\ &= (x \vee y)(xy \vee \bar{x} \vee \bar{z})y \quad \text{note } y(x+y) = xy+y = y \\ &= y \\ &= xyz \vee xy\bar{z} \vee \bar{x}yz \vee \bar{x}y\bar{z} \end{aligned}$$

$$\begin{aligned} \text{19 } f(w,x,y,z) &= wy \vee (w\bar{y} \vee z)(x \vee \bar{w}z) \\ &= wy \vee wx\bar{y} \vee xz \vee \bar{w}\bar{y}z \vee \bar{w}z \\ &= wy \vee wx\bar{y} \vee xz \vee \bar{w}z \\ &= wxyz \vee wx\bar{y}z \vee w\bar{x}yz \vee w\bar{x}\bar{y}z \vee wx\bar{y}z \vee w\bar{x}\bar{y}z \\ & \vee \bar{w}xyz \vee \bar{w}x\bar{y}z \vee \bar{w}\bar{x}yz \vee \bar{w}\bar{x}\bar{y}z \end{aligned}$$

$$(25) \textcircled{1} \quad xy \vee \bar{x}y \vee x\bar{y}$$

$$\textcircled{5} \quad xyz \vee xy\bar{z} \vee x\bar{y}z \vee \bar{x}y\bar{z} \vee \bar{x}\bar{y}z \vee \bar{x}\bar{y}\bar{z}$$

$$\textcircled{9} \quad wxyz \vee wxy\bar{z} \vee w\bar{x}\bar{y}\bar{z} \vee \bar{w}xyz \vee \bar{w}\bar{x}yz$$