

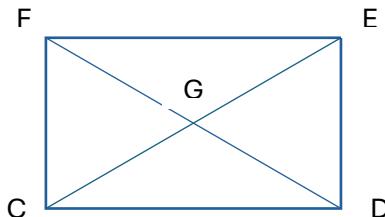
MTAP SATURDAY PROGRAM IN MATHEMATICS GRADE 9 SESSION 4
PROPORTION/PARALLELOGRAM

A. Determine if each statement is true or false. Write T on the space provided if the statement is true and F if it is false.

- _____ 1. All squares are rectangles.
- _____ 2. The diagonals of a rectangle are congruent.
- _____ 3. Not every rectangle is a rhombus.
- _____ 4. Parallelograms have four sides.
- _____ 5. All parallelograms are rhombus.
- _____ 6. The diagonals of a rhombus are perpendicular.
- _____ 7. Rectangles are always square.
- _____ 8. The diagonals of a square are perpendicular.
- _____ 9. Parallelogram is always a square.
- _____ 10. A square is an equilateral and equiangular polygon.
- _____ 11. All rhombi are rectangles.
- _____ 12. A rectangle is an equiangular polygon.
- _____ 13. Squares are sometimes rhombi.
- _____ 14. The diagonals of a rhombus are never congruent.
- _____ 15. Rectangles are always parallelogram.
- _____ 16. A kite has one pair of opposite angles that are congruent.
- _____ 17. An isosceles trapezoid has congruent legs.
- _____ 18. A trapezoid has exactly one pair of parallel sides.
- _____ 19. A kite has two distinct pairs of adjacent congruent sides.
- _____ 20. The area of a kite is determined using its diagonals.

B. Carefully examine each of the given quadrilaterals. Then, answer the questions that follow.

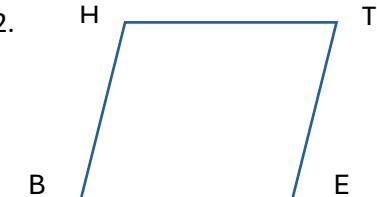
1.



CDEF is a rectangle. Solve each.

- $CG = 5x + 2$ and $EG = 3x + 20$. Find FD .
- $FD = 4(x + 1)$ and $CE = 3(x + 4)$. Find GC .
- $CF = 4x + 20$ and $DE = 6x - 50$. Find CF .

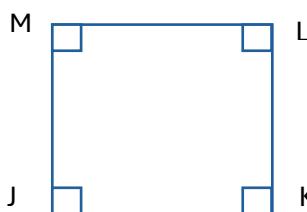
2.



BETH is a rhombus. Solve each.

- If $m\angle B = 2x + 20$ and $m\angle H = 6x$, what is $m\angle T$?
- If $m\angle HTE = 3x - 10$ and $m\angle HBE = 4x - 40$, what is $m\angle HTB$?

3.



JKLM is a square. Solve each.

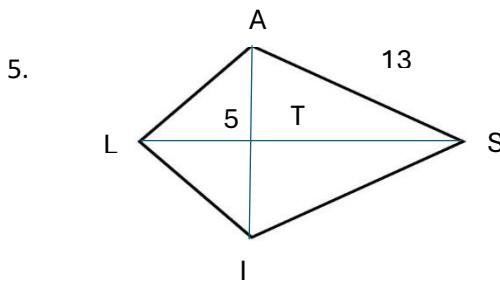
- If $ML = 2x - 1$ and $JK = 4x - 11$, find its perimeter.
- If $MJ = 2x + 1$ and $JK = x + 4$, find its area.

4.



ABCD is a trapezoid with a median \overline{EF} .

- If $DC = 2x + 10$, $AB = 3x + 20$, and $EF = 4x$, what is EF ?
- If $DC = 2x + 3$, $EF = 6x$, and $AB = 8x + 5$, what is AB ?



Quadrilateral LISA is a kite with diagonals \overline{LS} and \overline{AI} . If $AS = 13$, $LT = 5$, and $IT \cong LT$, find the following.

- The area of kite LISA
- The perimeter of kite LISA.

C. Find the value of x in each of the following:

- | | | |
|-----------------|------------------------|--------------------------|
| 1. $3:5 = x:10$ | 3. $18:(x+2) = 6:1$ | 5. $5:12 = (x+2):(3x+6)$ |
| 2. $2:x = 6:15$ | 4. $(x-1):8 = 3:(x+4)$ | 6. $4(x+1):(x+5) = 8:3$ |

D. Find the positive mean proportional between each pair of numbers below:

1. 3 and 12 2. 5 and 20 3. 7 and 28 4. 6 and 24 5. 10 and 40 6. 18 and 50

E. Solve the following problems.

- What is the length of a diagonal of a television screen if the screen is 408 mm wide and 544 mm high? Give your answer to the nearest centimeter.
- One side of a triangle is 36 m long. The side opposite the right angle is 50 m long. Find the length of the third side.
- A plane is flying at an altitude of 30,000 m. The horizontal distance of the plane to the airport is 10 km. What distance is the plane from the airport if it flies directly in a straight line towards the airport?
- The ratio of the angles in a triangle is 3:4:5. Find the measure of each angle.
- In a school, the number of boys is fewer than the number of girls by 120. If every group of 7 boys is matched with 8 girls, all students will be grouped without leftovers. How many students are there in total?
- KITE** is a park shaped like an isosceles trapezoid. The perimeter of the park is 100 cm. The legs of the park, KI and TE , are congruent and each measure $(2x + 4)$ cm. The bases are $IT = x$ cm and $KE = (x + 2)$ cm. What are the lengths of all the sides of the park?
- Quadrilateral ABCD is an isosceles trapezoid with $AD \cong BC$. If $m\angle A = x + 30$ and $m\angle B = 3x - 10$, what is $m\angle B$?
- What is the area of a kite with diagonals 18 and 24?

Challenge!

- TIME is a trapezoid with $\overline{TI} \parallel \overline{EM}$ and its median is \overline{JK} which divides the area of the trapezoid in the ratio 2:5. Find the ratio of \overline{TI} to \overline{EM} .
- Points U,H,R,A divide the sides of a rectangle in the ratio 1:2 with the points U,H,R,A being nearer to E,P,O,I respectively. Find the ratio of the area of rectangle to the area of a parallelogram UHRA.
- STAR is a square and $\triangle STR$ is an equilateral triangle outside the square. Find the measure of $\angle RBA$.

Figure for number 1

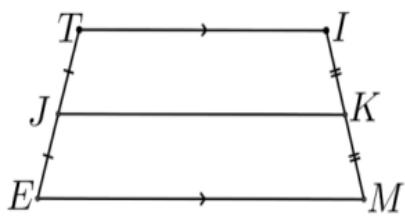


Figure for number 2

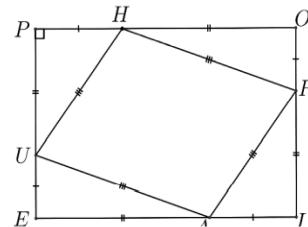


Figure for number 3

