

We used the two member MAPK scaffold model (cite PNAS paper) as a basis for our model with the following alterations. First, RAF (MAPKKK) dynamics were removed and a basal level of RAF activation was assumed. Second, we spacially partition the cell into "front" and "back" compartments, each with subcellular regions of cytoplasm, membrane and vesicles. Scaffold is capable of recycling through those three subcellular regions and is initially only cytoplasmic. MAPK components are cytoplasmic however they can be recruited to vesicle scaffolds, which can further catalyze the creation of dually phosphorylated MAPK.

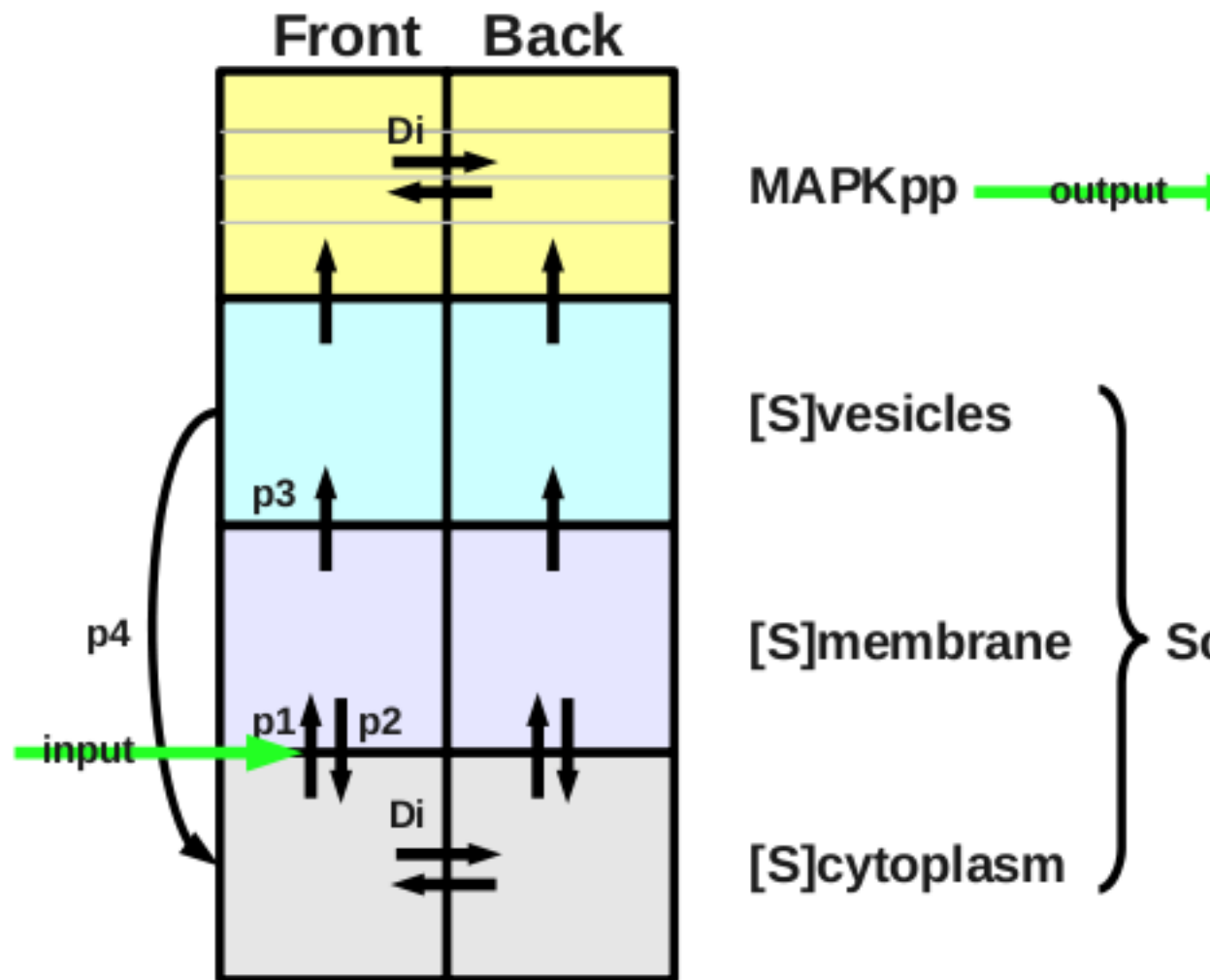
Translocation of cytoplasmic scaffold to the membrane occurs at a rate proportional to input dose. Translocation of membrane scaffold to vesicles occurs at a biphasic rate dependent on membrane scaffold. The readout for the model is the amount of dually phosphorylated MAPK.

Simulation was carried out through temporal integration of the system to steady state until an equilibrium tolerance was reached.

X-p phosphorylation, X-Ph phosphatase, X-k, kinase

$$p3(0) = (p3bSmem(0)(t) + p3a) \left(\frac{1 - p3d}{e^{p3f(Smem(0)(t) - p3e)} + 1} + p3d \right) \quad (1)$$

$$MI = \frac{MAPKpp_{front} - MAPKpp_{back}}{dx * maxdose} \quad (2)$$



a_1	1
$a \cdot 10$	5
a_2	0.5
a_3	3.3
a_4	10
a_5	3.3
a_6	10
a_7	20
a_8	5
a_9	20
Stot	0
d_1	0.4
$d \cdot 10$	0.4
d_2	0.5
d_3	0.42
d_4	0.8
d_5	0.4
d_6	0.8
d_7	0.6
d_8	0.4
d_9	0.6
k_1	0.1
$k \cdot 10$	0.1
k_2	0.1
k_3	0.1
k_4	0.1
k_5	0.1
k_6	0.1
k_7	0.1
k_8	0.1
k_9	0.1
MAPKPhTot	0.3
MAPKtot	0.4
MEKPhTot	0.2
MEKtot	0.2
of ₁	0.05
of ₂	0.05
of ₃	0.05
of ₄	0.5
on ₁	10
on ₂	10
RAFp	0.14
RAFPhTot	0.3
RAFtot	0.3
p_2	0.1
Di	0.0001
$p_1(0)$	0.1
$p_3(0)$	0.1
$p_4(0)$	0.1
$p_1(1)$	0.1
$p_3(1)$	0.1
$p_4(1)$	0.1

$$\begin{aligned}
S'_{\text{cyto}}(0, t) &= p_4(0)C_1(0, t) + \text{Di}(S_{\text{cyto}}(1, t) - S_{\text{cyto}}(0, t)) - p_1(0)S_{\text{cyto}}(0, t) + p_2S_{\text{mem}}(0, t) \\
\text{MEK}'(0, t) &= -a_3\text{RAFpMEK}(0, t) - \text{on}_1\text{MEK}(0, t)(C_1(0, t) + C_4(0, t) + C_5(0, t)) \\
&\quad + \text{of}_1(C_2(0, t) + C_6(0, t) + C_9(0, t)) + d_3\text{MEKRAFp}(0, t) \\
&\quad + \text{Di}(\text{MEK}(1, t) - \text{MEK}(0, t)) + k_4\text{MEKpMEKPh}(0, t) \\
\text{MEKRAFp}'(0, t) &= a_3\text{RAFpMEK}(0, t) + (-d_3 - k_3)\text{MEKRAFp}(0, t) \\
&\quad + \text{Di}(\text{MEKRAFp}(1, t) - \text{MEKRAFp}(0, t)) \\
\text{MEKp}'(0, t) &= -a_4\text{MEKp}(0, t)(-\text{MEKpMEKPh}(0, t) - \text{MEKppMEKPh}(0, t) \\
&\quad + \text{MEKPh}_{\text{tot}}) - a_5\text{RAFpMEKp}(0, t) + d_4\text{MEKpMEKPh}(0, t) \\
&\quad + d_5\text{MEKpRAFp}(0, t) + \text{Di}(\text{MEKp}(1, t) - \text{MEKp}(0, t)) \\
&\quad + k_3\text{MEKRAFp}(0, t) + k_6\text{MEKppMEKPh}(0, t) \\
\text{MEKpMEKPh}'(0, t) &= a_4\text{MEKp}(0, t)(-\text{MEKpMEKPh}(0, t) - \text{MEKppMEKPh}(0, t) \\
&\quad + \text{MEKPh}_{\text{tot}}) + (-d_4 - k_4)\text{MEKpMEKPh}(0, t) \\
&\quad + \text{Di}(\text{MEKpMEKPh}(1, t) - \text{MEKpMEKPh}(0, t)) \\
\text{MEKpRAFp}'(0, t) &= a_5\text{RAFpMEKp}(0, t) + (-d_5 - k_5)\text{MEKpRAFp}(0, t) \\
&\quad + \text{Di}(\text{MEKpRAFp}(1, t) - \text{MEKpRAFp}(0, t)) \\
\text{MEKpp}'(0, t) &= -a_6\text{MEKpp}(0, t)(-\text{MEKpMEKPh}(0, t) - \text{MEKppMEKPh}(0, t) \\
&\quad + \text{MEKPh}_{\text{tot}}) \\
&\quad - a_7\text{MAPK}(0, t)\text{MEKpp}(0, t) - a_9\text{MAPKp}(0, t)\text{MEKpp}(0, t) \\
&\quad + \text{of}_3(C_3(0, t) + C_7(0, t) + C_8(0, t)) + d_6\text{MEKppMEKPh}(0, t) \\
&\quad + (d_7 + k_7)\text{MAPKMEKpp}(0, t) + (d_9 + k_9)\text{MAPKpMEKpp}(0, t) \\
&\quad + \text{Di}(\text{MEKpp}(1, t) - \text{MEKpp}(0, t)) + k_5\text{MEKpRAFp}(0, t) \\
\text{MEKppMEKPh}'(0, t) &= a_6\text{MEKpp}(0, t)(-\text{MEKpMEKPh}(0, t) - \text{MEKppMEKPh}(0, t) \\
&\quad + \text{MEKPh}_{\text{tot}}) - (d_6 + k_6)\text{MEKppMEKPh}(0, t) \\
&\quad + \text{Di}(\text{MEKppMEKPh}(1, t) - \text{MEKppMEKPh}(0, t)) \\
\text{MAPK}'(0, t) &= -a_7\text{MAPK}(0, t)\text{MEKpp}(0, t) \\
&\quad - \text{on}_2\text{MAPK}(0, t)(C_1(0, t) + C_2(0, t) + C_3(0, t)) \\
&\quad + \text{of}_2(C_4(0, t) + C_6(0, t) + C_7(0, t)) + d_7\text{MAPKMEKpp}(0, t) \\
&\quad + \text{Di}(\text{MAPK}(1, t) - \text{MAPK}(0, t)) + k_8\text{MAPKpMAPKPh}(0, t) \\
\text{MAPKMEKpp}'(0, t) &= a_7\text{MAPK}(0, t)\text{MEKpp}(0, t) + (-d_7 - k_7)\text{MAPKMEKpp}(0, t) \\
&\quad + \text{Di}(\text{MAPKMEKpp}(1, t) - \text{MAPKMEKpp}(0, t)) \\
\text{MAPKp}'(0, t) &= -a_8\text{MAPKp}(0, t)(-\text{MAPKpMAPKPh}(0, t) \\
&\quad - \text{MAPKppMAPKPh}(0, t) + \text{MAPKPh}_{\text{tot}}) \\
&\quad - a_9\text{MAPKp}(0, t)\text{MEKpp}(0, t) + d_8\text{MAPKpMAPKPh}(0, t) \\
&\quad + d_9\text{MAPKpMEKpp}(0, t) + \text{Di}(\text{MAPKp}(1, t) - \text{MAPKp}(0, t)) \\
&\quad + k_{10}\text{MAPKppMAPKPh}(0, t) + k_7\text{MAPKMEKpp}(0, t) \\
\text{MAPKpMEKpp}'(0, t) &= a_9\text{MAPKp}(0, t)\text{MEKpp}(0, t) \\
&\quad + (-d_9 - k_9)\text{MAPKpMEKpp}(0, t) \\
&\quad + \text{Di}(\text{MAPKpMEKpp}(1, t) - \text{MAPKpMEKpp}(0, t))
\end{aligned}$$

$$\begin{aligned}
\text{MAPKpp}'(0, t) &= -a \cdot 10 \text{MAPKpp}(0, t) (-\text{MAPKpMAPKPh}(0, t) \\
&\quad - \text{MAPKppMAPKPh}(0, t) + \text{MAPKPh}_{\text{tot}}) \\
&\quad + \text{of}_4(C_5(0, t) + C_8(0, t) + C_9(0, t)) + d \cdot 10 \text{MAPKppMAPKPh}(0, t) \\
&\quad + \text{Di}(\text{MAPKpp}(1, t) - \text{MAPKpp}(0, t)) + k_9 \text{MAPKpMEKpp}(0, t) \\
\text{MAPKpMAPKPh}'(0, t) &= a_8 \text{MAPKp}(0, t) (-\text{MAPKpMAPKPh}(0, t) \\
&\quad - \text{MAPKppMAPKPh}(0, t) + \text{MAPKPh}_{\text{tot}}) \\
&\quad + (-d_8 - k_8) \text{MAPKpMAPKPh}(0, t) \\
&\quad + \text{Di}(\text{MAPKpMAPKPh}(1, t) - \text{MAPKpMAPKPh}(0, t)) \\
\text{MAPKppMAPKPh}'(0, t) &= a \cdot 10 \text{MAPKpp}(0, t) (-\text{MAPKpMAPKPh}(0, t) \\
&\quad - \text{MAPKppMAPKPh}(0, t) + \text{MAPKPh}_{\text{tot}}) \\
&\quad - (d \cdot 10 + k \cdot 10) \text{MAPKppMAPKPh}(0, t) \\
&\quad + \text{Di}(\text{MAPKppMAPKPh}(1, t) - \text{MAPKppMAPKPh}(0, t)) \\
C_1'(0, t) &= -C_1(0, t)(\text{on}_2 \text{MAPK}(0, t) + \text{on}_1 \text{MEK}(0, t)) - p_4(0) C_1(0, t) \\
&\quad + \text{of}_1 C_2(0, t) + \text{of}_3 C_3(0, t) + \text{of}_2 C_4(0, t) + \text{of}_4 C_5(0, t) + p_3(0) S_{\text{mem}}(0, t) \\
C_2'(0, t) &= \text{on}_1 C_1(0, t) \text{MEK}(0, t) - k_5 \text{RAFp} C_2(0, t) \\
&\quad - C_2(0, t)(\text{on}_2 \text{MAPK}(0, t) + \text{of}_1) + \text{of}_2 C_6(0, t) + \text{of}_4 C_9(0, t) \\
C_3'(0, t) &= k_5 \text{RAFp} C_2(0, t) - \text{on}_2 C_3(0, t) \text{MAPK}(0, t) \\
&\quad - \text{of}_3 C_3(0, t) + \text{of}_2 C_7(0, t) + \text{of}_4 C_8(0, t) \\
C_4'(0, t) &= \text{on}_2 C_1(0, t) \text{MAPK}(0, t) - C_4(0, t)(\text{on}_1 \text{MEK}(0, t) + \text{of}_2) \\
&\quad + \text{of}_1 C_6(0, t) + \text{of}_3 C_7(0, t) \\
C_5'(0, t) &= -C_5(0, t)(\text{on}_1 \text{MEK}(0, t) + \text{of}_4) + \text{of}_3 C_8(0, t) + \text{of}_1 C_9(0, t) \\
C_6'(0, t) &= \text{on}_2 C_2(0, t) \text{MAPK}(0, t) + \text{on}_1 C_4(0, t) \text{MEK}(0, t) \\
&\quad - k_5 \text{RAFp} C_6(0, t) + (-\text{of}_1 - \text{of}_2) C_6(0, t) \\
C_7'(0, t) &= \text{on}_2 C_3(0, t) \text{MAPK}(0, t) + k_5 \text{RAFp} C_6(0, t) \\
&\quad - k_9 C_7(0, t) - \text{of}_2 C_7(0, t) - \text{of}_3 C_7(0, t) \\
C_8'(0, t) &= k_9 C_7(0, t) - (\text{of}_3 + \text{of}_4) C_8(0, t) + k_5 \text{RAFp} C_9(0, t) \\
C_9'(0, t) &= \text{on}_1 C_5(0, t) \text{MEK}(0, t) - k_5 \text{RAFp} C_9(0, t) + (-\text{of}_1 - \text{of}_4) C_9(0, t) \\
S'_{\text{mem}}(0, t) &= p_1(0) S_{\text{cyto}}(0, t) - p_2 S_{\text{mem}}(0, t) - p_3(0) S_{\text{mem}}(0, t) \\
S'_{\text{cyto}}(1, t) &= p_4(1) C_1(1, t) + \text{Di}(S_{\text{cyto}}(0, t) - S_{\text{cyto}}(1, t)) - p_1(1) S_{\text{cyto}}(1, t) + p_2 S_{\text{mem}}(1, t) \\
\text{MEK}'(1, t) &= -a_3 \text{RAFpMEK}(1, t) - \text{on}_1 \text{MEK}(1, t)(C_1(1, t) + C_4(1, t) + C_5(1, t)) \\
&\quad + \text{of}_1(C_2(1, t) + C_6(1, t) + C_9(1, t)) + d_3 \text{MEKRAFp}(1, t) \\
&\quad + \text{Di}(\text{MEK}(0, t) - \text{MEK}(1, t)) + k_4 \text{MEKpMEKPh}(1, t) \\
\text{MEKRAFp}'(1, t) &= a_3 \text{RAFpMEK}(1, t) + (-d_3 - k_3) \text{MEKRAFp}(1, t) \\
&\quad + \text{Di}(\text{MEKRAFp}(0, t) - \text{MEKRAFp}(1, t)) \\
\text{MEKp}'(1, t) &= -a_4 \text{MEKp}(1, t) (-\text{MEKpMEKPh}(1, t) - \text{MEKppMEKPh}(1, t) \\
&\quad + \text{MEKPh}_{\text{tot}}) - a_5 \text{RAFpMEKp}(1, t) + d_4 \text{MEKpMEKPh}(1, t) \\
&\quad + d_5 \text{MEKpRAFp}(1, t) + \text{Di}(\text{MEKp}(0, t) - \text{MEKp}(1, t)) \\
&\quad + k_3 \text{MEKRAFp}(1, t) + k_6 \text{MEKppMEKPh}(1, t)
\end{aligned}$$

$$\begin{aligned}
\text{MEKpMEKPh}'(1, t) &= a_4 \text{MEKp}(1, t)(-\text{MEKpMEKPh}(1, t) - \text{MEKppMEKPh}(1, t) \\
&\quad + \text{MEKPh}_{\text{tot}}) + (-d_4 - k_4) \text{MEKpMEKPh}(1, t) \\
&\quad + \text{Di}(\text{MEKpMEKPh}(0, t) - \text{MEKpMEKPh}(1, t)) \\
\text{MEKpRAFp}'(1, t) &= a_5 \text{RAFpMEKp}(1, t) + (-d_5 - k_5) \text{MEKpRAFp}(1, t) \\
&\quad + \text{Di}(\text{MEKpRAFp}(0, t) - \text{MEKpRAFp}(1, t)) \\
\text{MEKpp}'(1, t) &= -a_6 \text{MEKpp}(1, t)(-\text{MEKpMEKPh}(1, t) - \text{MEKppMEKPh}(1, t) \\
&\quad + \text{MEKPh}_{\text{tot}}) \\
&\quad - a_7 \text{MAPK}(1, t) \text{MEKpp}(1, t) - a_9 \text{MAPKp}(1, t) \text{MEKpp}(1, t) \\
&\quad + \text{of}_3(C_3(1, t) + C_7(1, t) + C_8(1, t)) + d_6 \text{MEKppMEKPh}(1, t) \\
&\quad + (d_7 + k_7) \text{MAPKMEKpp}(1, t) + (d_9 + k_9) \text{MAPKpMEKpp}(1, t) \\
&\quad + \text{Di}(\text{MEKpp}(0, t) - \text{MEKpp}(1, t)) + k_5 \text{MEKpRAFp}(1, t) \\
\text{MEKppMEKPh}'(1, t) &= a_6 \text{MEKpp}(1, t)(-\text{MEKpMEKPh}(1, t) - \text{MEKppMEKPh}(1, t) \\
&\quad + \text{MEKPh}_{\text{tot}}) - (d_6 + k_6) \text{MEKppMEKPh}(1, t) \\
&\quad + \text{Di}(\text{MEKppMEKPh}(0, t) - \text{MEKppMEKPh}(1, t)) \\
\text{MAPK}'(1, t) &= -a_7 \text{MAPK}(1, t) \text{MEKpp}(1, t) \\
&\quad - \text{on}_2 \text{MAPK}(1, t)(C_1(1, t) + C_2(1, t) + C_3(1, t)) \\
&\quad + \text{of}_2(C_4(1, t) + C_6(1, t) + C_7(1, t)) + d_7 \text{MAPKMEKpp}(1, t) \\
&\quad + \text{Di}(\text{MAPK}(0, t) - \text{MAPK}(1, t)) + k_8 \text{MAPKpMAPKPh}(1, t) \\
\text{MAPKMEKpp}'(1, t) &= a_7 \text{MAPK}(1, t) \text{MEKpp}(1, t) + (-d_7 - k_7) \text{MAPKMEKpp}(1, t) \\
&\quad + \text{Di}(\text{MAPKMEKpp}(0, t) - \text{MAPKMEKpp}(1, t)) \\
\text{MAPKp}'(1, t) &= -a_8 \text{MAPKp}(1, t)(-\text{MAPKpMAPKPh}(1, t) \\
&\quad - \text{MAPKppMAPKPh}(1, t) + \text{MAPKPh}_{\text{tot}}) \\
&\quad - a_9 \text{MAPKp}(1, t) \text{MEKpp}(1, t) + d_8 \text{MAPKpMAPKPh}(1, t) \\
&\quad + d_9 \text{MAPKpMEKpp}(1, t) + \text{Di}(\text{MAPKp}(0, t) - \text{MAPKp}(1, t)) \\
&\quad + k'_{10} \text{MAPKppMAPKPh}(1, t) + k_7 \text{MAPKMEKpp}(1, t) \\
\text{MAPKpMEKpp}'(1, t) &= a_9 \text{MAPKp}(1, t) \text{MEKpp}(1, t) \\
&\quad + (-d_9 - k_9) \text{MAPKpMEKpp}(1, t) \\
&\quad + \text{Di}(\text{MAPKpMEKpp}(0, t) - \text{MAPKpMEKpp}(1, t)) \\
\text{MAPKpp}'(1, t) &= -a'_{10} \text{MAPKpp}(1, t)(-\text{MAPKpMAPKPh}(1, t) \\
&\quad - \text{MAPKppMAPKPh}(1, t) + \text{MAPKPh}_{\text{tot}}) \\
&\quad + \text{of}_4(C_5(1, t) + C_8(1, t) + C_9(1, t)) + d'_{10} \text{MAPKppMAPKPh}(1, t) \\
&\quad + \text{Di}(\text{MAPKpp}(0, t) - \text{MAPKpp}(1, t)) + k_9 \text{MAPKpMEKpp}(1, t) \\
\text{MAPKpMAPKPh}'(1, t) &= a_8 \text{MAPKp}(1, t)(-\text{MAPKpMAPKPh}(1, t) \\
&\quad - \text{MAPKppMAPKPh}(1, t) + \text{MAPKPh}_{\text{tot}}) \\
&\quad + (-d_8 - k_8) \text{MAPKpMAPKPh}(1, t) \\
&\quad + \text{Di}(\text{MAPKpMAPKPh}(0, t) - \text{MAPKpMAPKPh}(1, t)) \\
\text{MAPKppMAPKPh}'(1, t) &= a'_{10} \text{MAPKpp}(1, t)(-\text{MAPKpMAPKPh}(1, t) \\
&\quad - \text{MAPKppMAPKPh}(1, t) + \text{MAPKPh}_{\text{tot}}) \\
&\quad - (d'_{10} + k'_{10}) \text{MAPKppMAPKPh}(1, t) \\
&\quad + \text{Di}(\text{MAPKppMAPKPh}(0, t) - \text{MAPKppMAPKPh}(1, t))
\end{aligned}$$

$$\begin{aligned}
C'_1(1, t) &= -C_1(1, t)(\text{on}_2\text{MAPK}(1, t) + \text{on}_1\text{MEK}(1, t)) - p_4(1)C_1(1, t) \\
&\quad + \text{of}_1C_2(1, t) + \text{of}_3C_3(1, t) + \text{of}_2C_4(1, t) + \text{of}_4C_5(1, t) + p_3(1)S_{\text{mem}}(1, t) \\
C'_2(1, t) &= \text{on}_1C_1(1, t)\text{MEK}(1, t) - k_5\text{RAFp}C_2(1, t) \\
&\quad - C_2(1, t)(\text{on}_2\text{MAPK}(1, t) + \text{of}_1) + \text{of}_2C_6(1, t) + \text{of}_4C_9(1, t) \\
C'_3(1, t) &= k_5\text{RAFp}C_2(1, t) - \text{on}_2C_3(1, t)\text{MAPK}(1, t) \\
&\quad - \text{of}_3C_3(1, t) + \text{of}_2C_7(1, t) + \text{of}_4C_8(1, t) \\
C'_4(1, t) &= \text{on}_2C_1(1, t)\text{MAPK}(1, t) - C_4(1, t)(\text{on}_1\text{MEK}(1, t) + \text{of}_2) \\
&\quad + \text{of}_1C_6(1, t) + \text{of}_3C_7(1, t) \\
C'_5(1, t) &= -C_5(1, t)(\text{on}_1\text{MEK}(1, t) + \text{of}_4) + \text{of}_3C_8(1, t) + \text{of}_1C_9(1, t) \\
C'_6(1, t) &= \text{on}_2C_2(1, t)\text{MAPK}(1, t) + \text{on}_1C_4(1, t)\text{MEK}(1, t) \\
&\quad - k_5\text{RAFp}C_6(1, t) + (-\text{of}_1 - \text{of}_2)C_6(1, t) \\
C'_7(1, t) &= \text{on}_2C_3(1, t)\text{MAPK}(1, t) + k_5\text{RAFp}C_6(1, t) \\
&\quad - k_9C_7(1, t) - \text{of}_2C_7(1, t) - \text{of}_3C_7(1, t) \\
C'_8(1, t) &= k_9C_7(1, t) - (\text{of}_3 + \text{of}_4)C_8(1, t) + k_5\text{RAFp}C_9(1, t) \\
C'_9(1, t) &= \text{on}_1C_5(1, t)\text{MEK}(1, t) - k_5\text{RAFp}C_9(1, t) + (-\text{of}_1 - \text{of}_4)C_9(1, t) \\
S'_{\text{mem}}(1, t) &= p_1(1)S_{\text{cyto}}(1, t) - p_2S_{\text{mem}}(1, t) - p_3(1)S_{\text{mem}}(1, t)
\end{aligned}$$