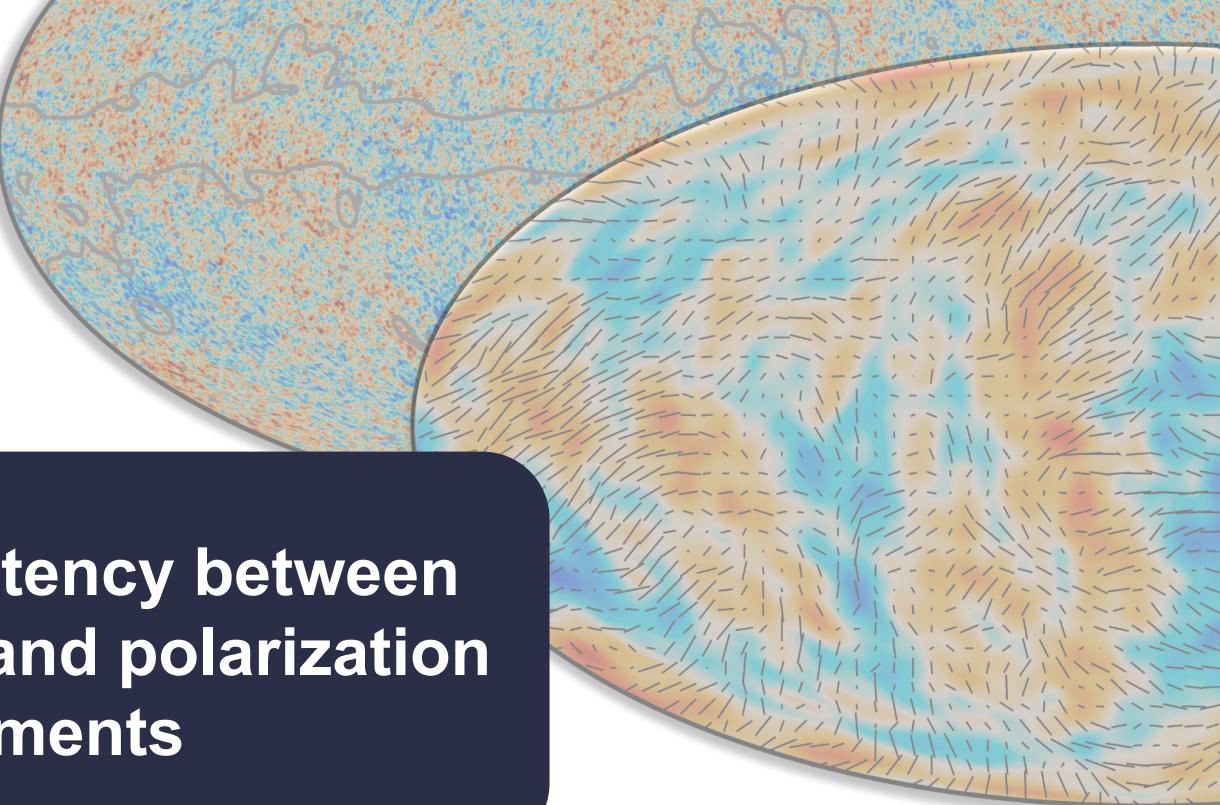
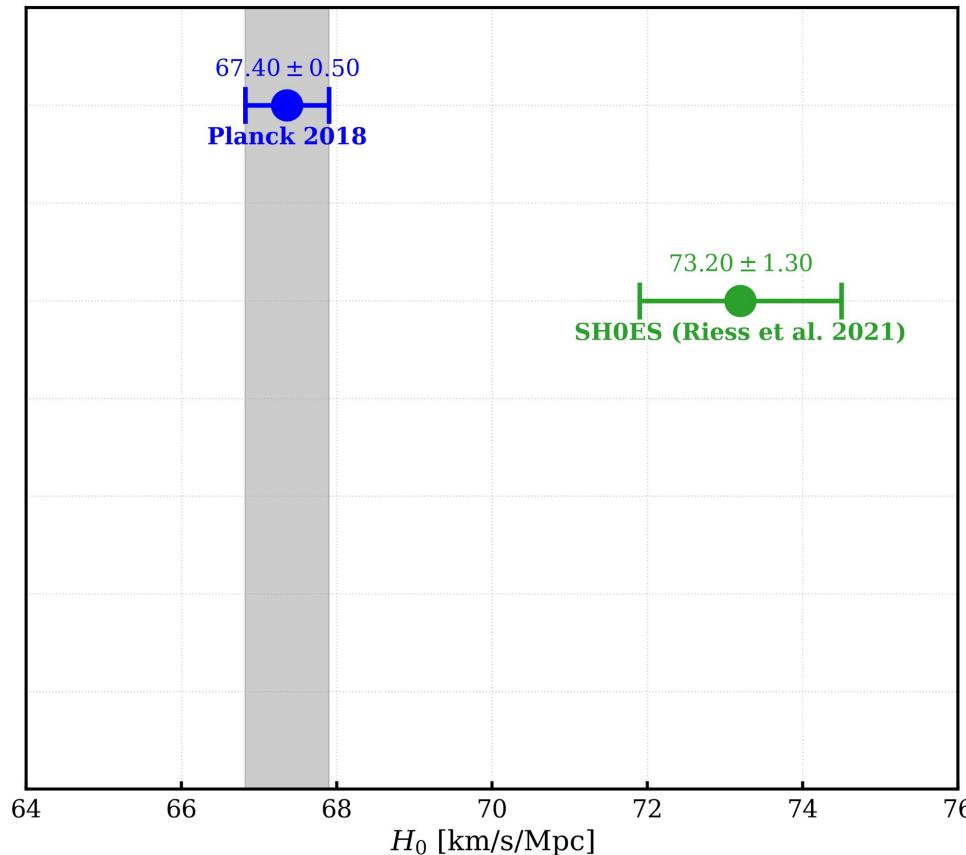


Assessing consistency between CMB temperature and polarization measurements

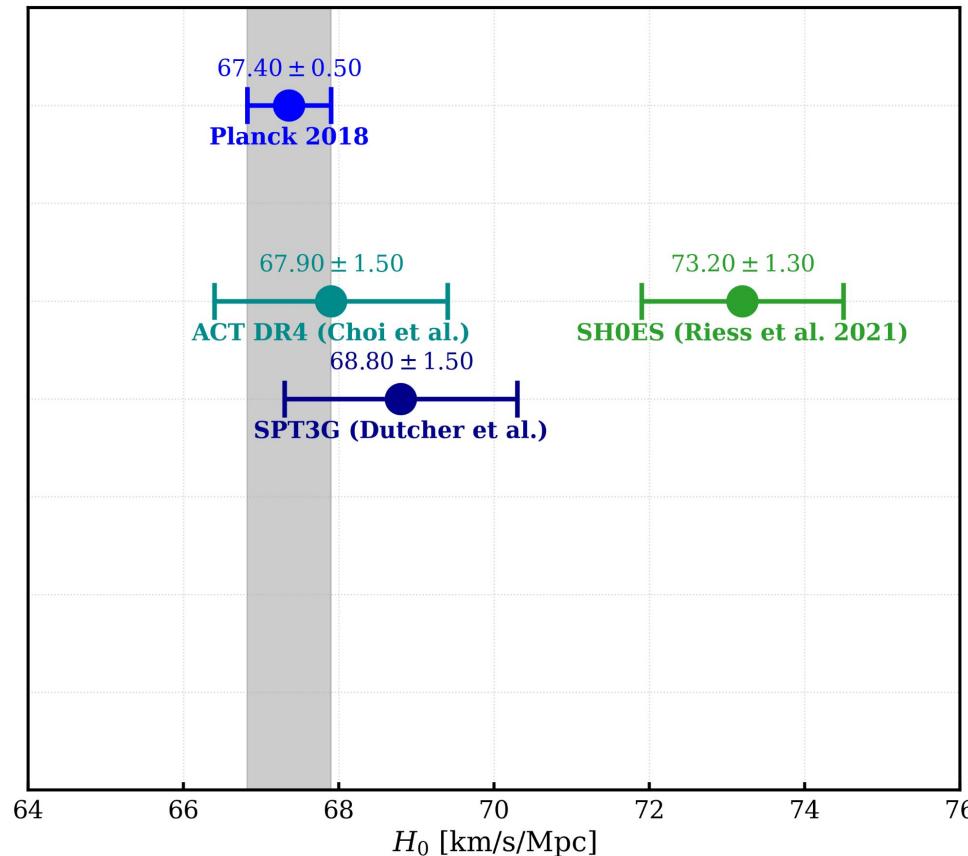
Adrien La Posta - IJClab



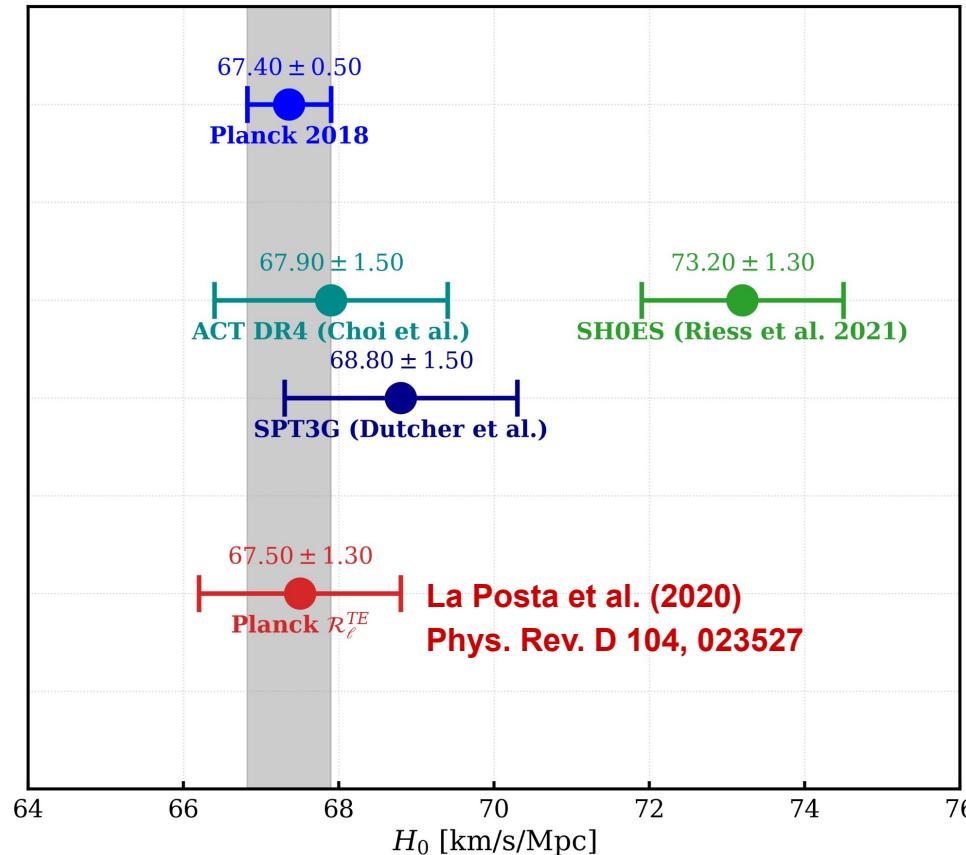
The Hubble tension



The Hubble tension

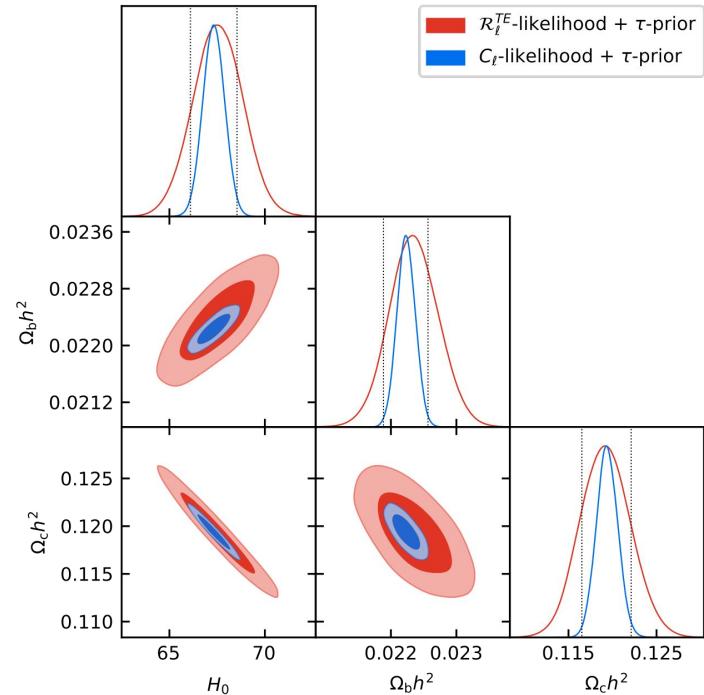
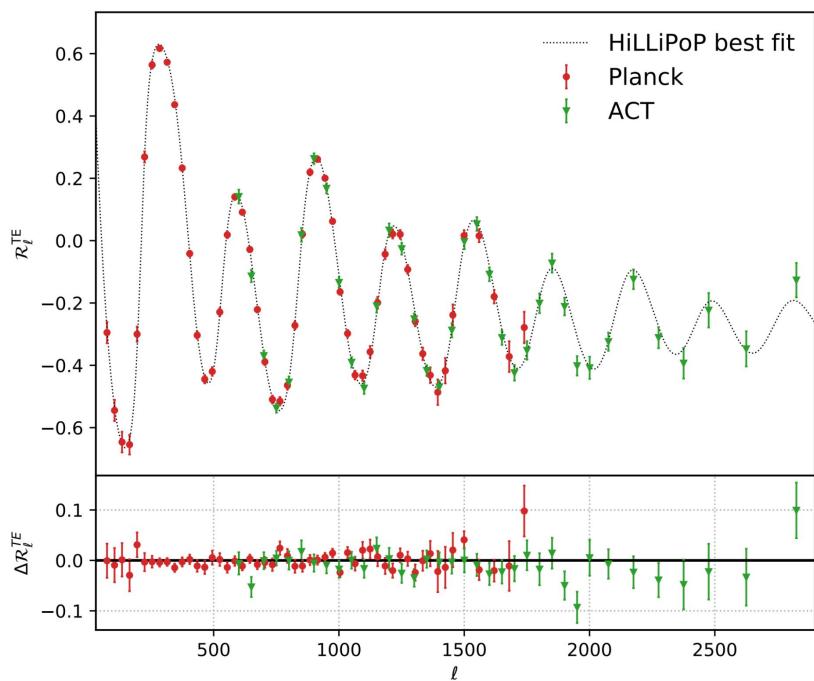


The Hubble tension

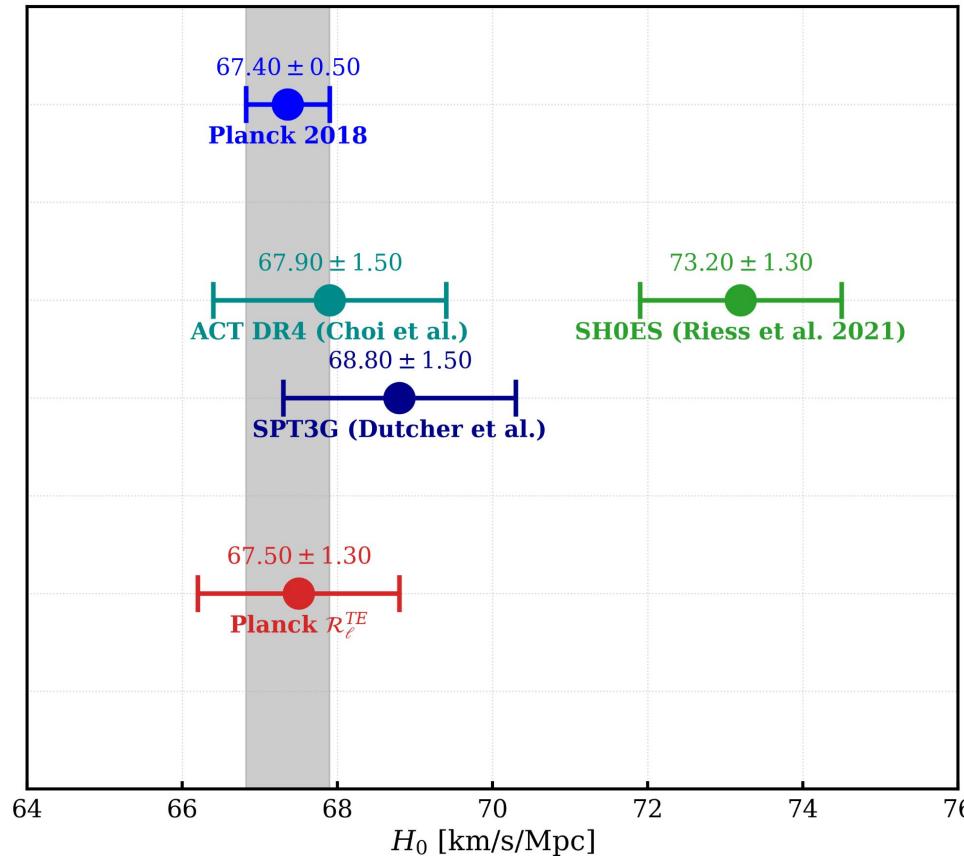


T-E Correlation coefficient

$$\mathcal{R}_\ell^{TE} = \frac{C_\ell^{TE}}{\sqrt{C_\ell^{TT} C_\ell^{EE}}}$$

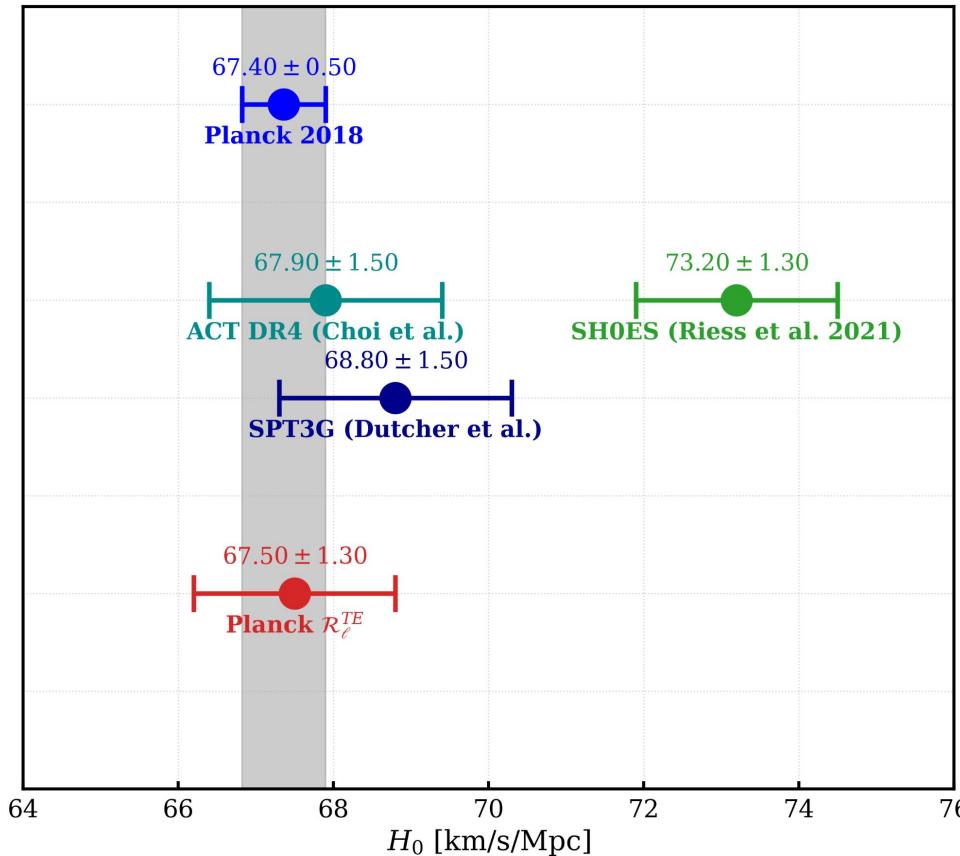


Solutions to the Hubble tension ?



Option 1 :
Systematics affecting the local
measurements of H_0 ?

Solutions to the Hubble tension ?



Option 1 :

Systematics affecting the local measurements of H_0 ?

Option 2 :

Physics beyond Λ CDM that shift the constraints on H_0 derived from the CMB

Beyond Λ CDM

The H_0 Olympics: A fair ranking of proposed models

Nils Schöneberg^{a,*}, Guillermo Franco Abellán^b, Andrea Pérez Sánchez^a, Samuel J. Witte^c, Vivian Poulin^b, Julien Lesgourgues^a

arXiv:2107.10291

^aInstitute for Theoretical Particle Physics and Cosmology (TTK), RWTH Aachen University, D-52056 Aachen, Germany.

^bLaboratoire Univers & Particules de Montpellier (LUPM), CNRS & Université de Montpellier (UMR-5299), Place Eugène Bataillon, F-34095 Montpellier Cedex 05, France.

^cGRAPPA Institute, Institute for Theoretical Physics Amsterdam and Delta Institute for Theoretical Physics, University of Amsterdam, Science Park 904, 1098 XH Amsterdam, The Netherlands

Model	ΔN_{param}	M_B	Gaussian Tension	Q_{DMAP} Tension	$\Delta\chi^2$	ΔAIC	Finalist	
Λ CDM	0	-19.416 ± 0.012	4.4σ	4.5σ	X	0.00	0.00	X
ΔN_{ur}	1	-19.395 ± 0.019	3.6σ	3.8σ	X	-6.10	-4.10	X
SIDR	1	-19.385 ± 0.024	3.2σ	3.3σ	X	-9.57	-7.57	✓
mixed DR	2	-19.413 ± 0.036	3.3σ	3.4σ	X	-8.83	-4.83	X
DR-DM	2	-19.388 ± 0.026	3.2σ	3.1σ	X	-8.92	-4.92	X
$S\bar{\nu}+\text{DR}$	3	$-19.440^{+0.037}_{-0.039}$	3.8σ	3.9σ	X	-4.98	1.02	X
Majoron	3	$-19.380^{+0.027}_{-0.021}$	3.0σ	2.9σ	✓	-15.49	-9.49	✓
primordial B	1	$-19.390^{+0.018}_{-0.024}$	3.5σ	3.5σ	X	-11.42	-9.42	✓
varying m_e	1	-19.391 ± 0.034	2.9σ	2.9σ	✓	-12.27	-10.27	✓
varying $m_e + \Omega_k$	2	-19.368 ± 0.048	2.0σ	1.9σ	✓	-17.26	-13.26	✓
EDE	3	$-19.390^{+0.016}_{-0.035}$	3.6σ	1.6σ	✓	-21.98	-15.98	✓
NEDE	3	$-19.380^{+0.023}_{-0.040}$	3.1σ	1.9σ	✓	-18.93	-12.93	✓
EMG	3	$-19.397^{+0.017}_{-0.023}$	3.7σ	2.3σ	✓	-18.56	-12.56	✓
CPL	2	-19.400 ± 0.020	3.7σ	4.1σ	X	-4.94	-0.94	X
PEDE	0	-19.349 ± 0.013	2.7σ	2.8σ	✓	2.24	2.24	X
GPEDE	1	-19.400 ± 0.022	3.6σ	4.6σ	X	-0.45	1.55	X
$\text{DM} \rightarrow \text{DR+WDW}$	2	-19.420 ± 0.012	4.5σ	4.5σ	X	-0.19	3.81	X
$\text{DM} \rightarrow \text{DR}$	2	-19.410 ± 0.011	4.3σ	4.5σ	X	-0.53	3.47	X

Table 1: Test of the models based on dataset $\mathcal{D}_{\text{baseline}}$ (Planck 2018 + BAO + Pantheon), using the direct measurement of M_b by SH0ES for the quantification of the tension (3rd column) or the computation of the AIC (5th column). Eight models pass at least one of these three tests at the 3σ level.

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Early Dark Energy

Goal : obtain a higher expansion rate H_0

$$\theta_* = \frac{r_s^*}{D_A^*}$$

Fixed by
observations

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$$\left. \frac{3H^2(z)}{8\pi G} \right|_{\text{early}} = \rho_{\text{rad}}(z) + \rho_{\text{matter}}(z)$$

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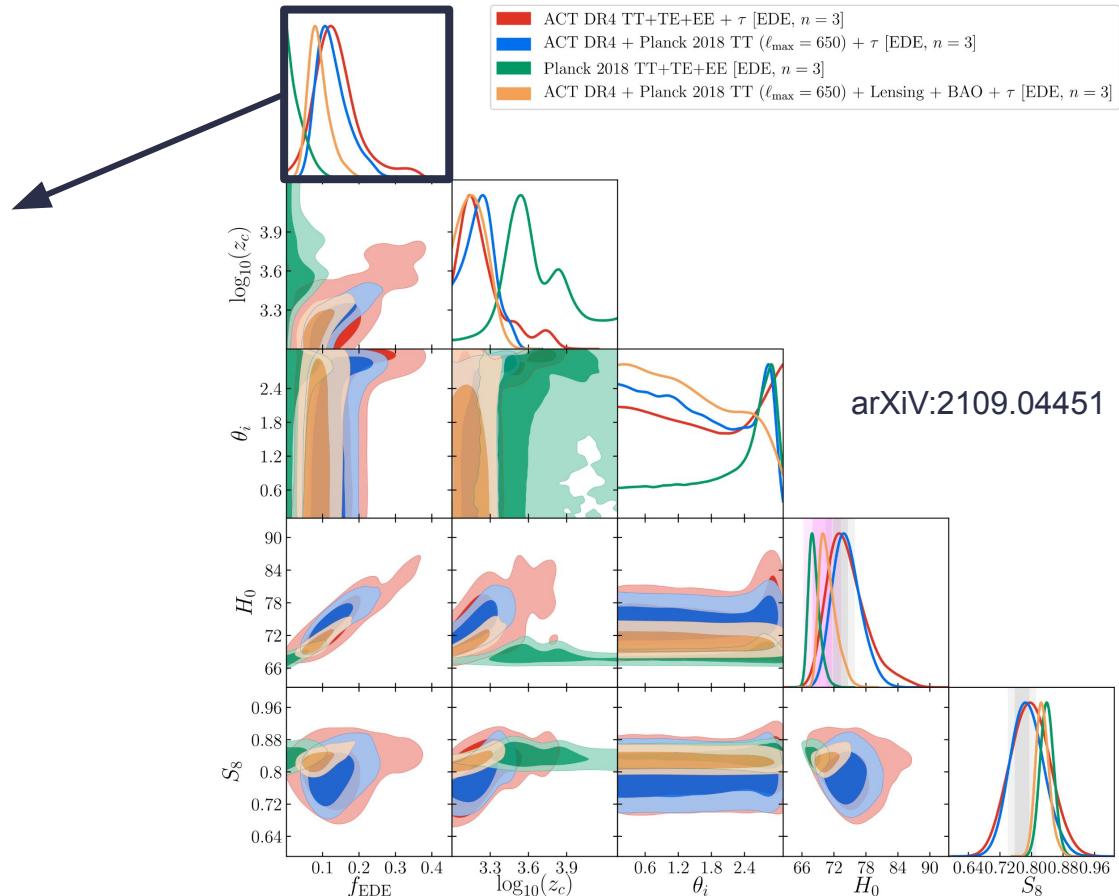
$$\ddot{\phi} + 3H\dot{\phi} + V'(\phi) = 0$$

$$V_n(\phi) = m^2 f^2 \left[1 - \cos \left(\frac{\phi}{f} \right) \right]^n$$

- **Field initially frozen :** act as dark energy at early times
- Starts to oscillate when $H \sim m$

Early Dark Energy - ACT DR4 results

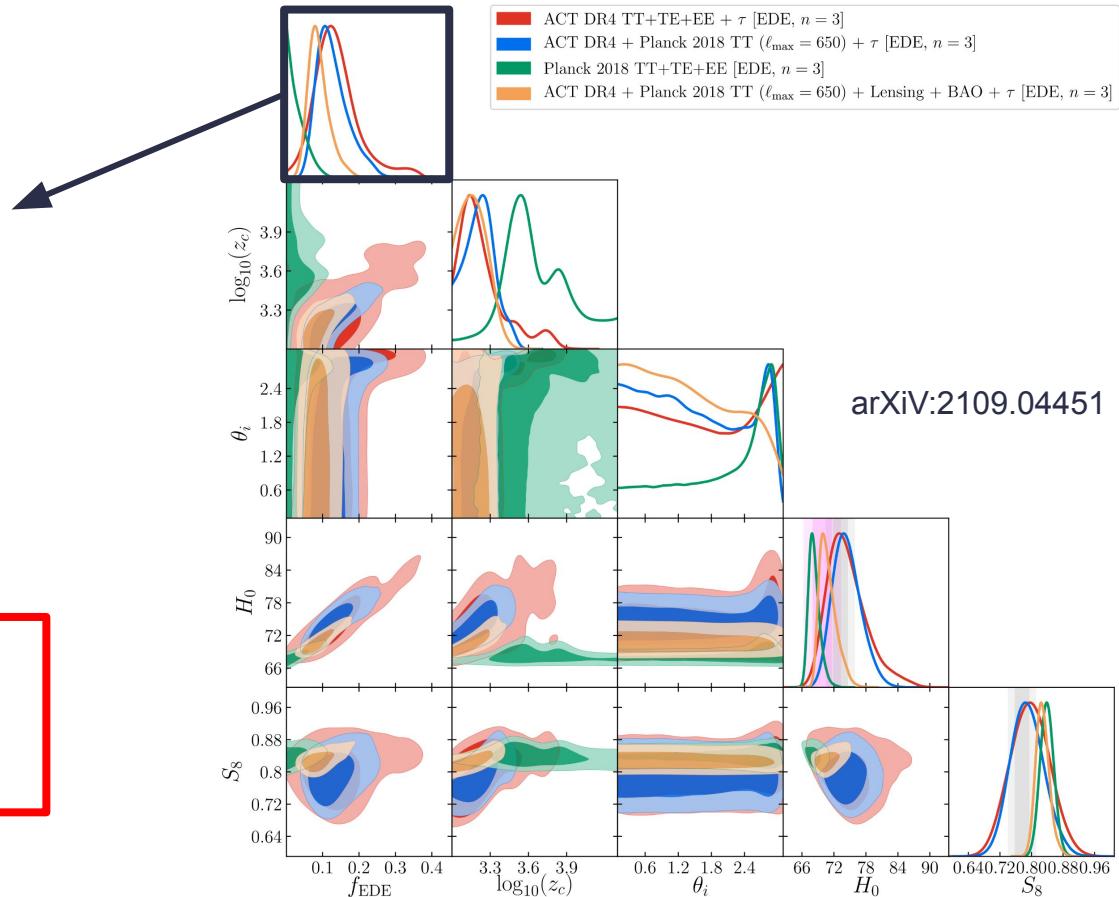
- ACT DR4 data shows a preference for EDE (improvement of the χ^2) with a $\sim 2.5 \sigma$ evidence
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Early Dark Energy - ACT DR4 results

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We need additional constraints on EDE



Model independent constraints

Many models have already been proposed to solve the Hubble tension

Model	ΔN_{param}
Λ CDM	0
ΔN_{ur}	1
SIDR	1
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- **Option 1 :** Put constraints on all available model with different experiments to have a strong evidence for some of them ...
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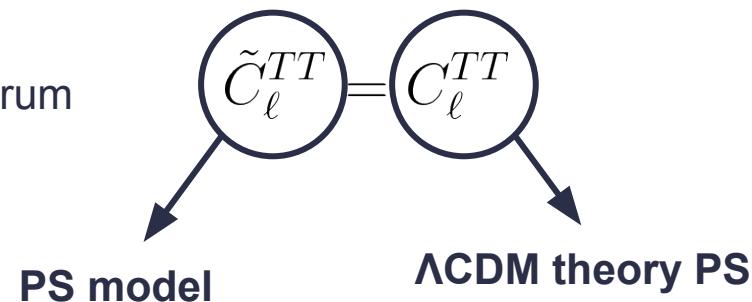
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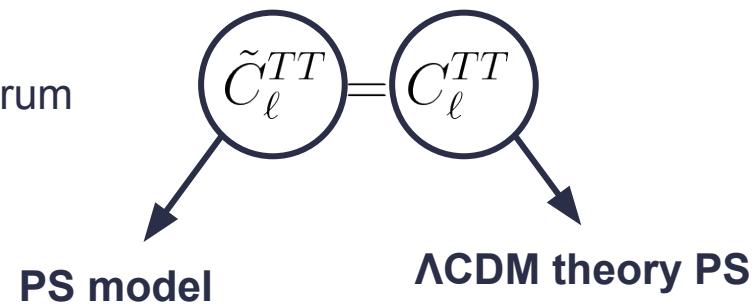
We fix the cosmology with the TT power spectrum



Modelling deviations with transfer functions

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We fix the cosmology with the TT power spectrum



We have to define a model for \tilde{C}_ℓ^{TE} and \tilde{C}_ℓ^{EE}

Modelling deviations with transfer functions

$$\text{Transfer function} \times \text{Theory Power Spectrum} = \text{Power Spectra Model}$$

Modelling deviations with transfer functions

10

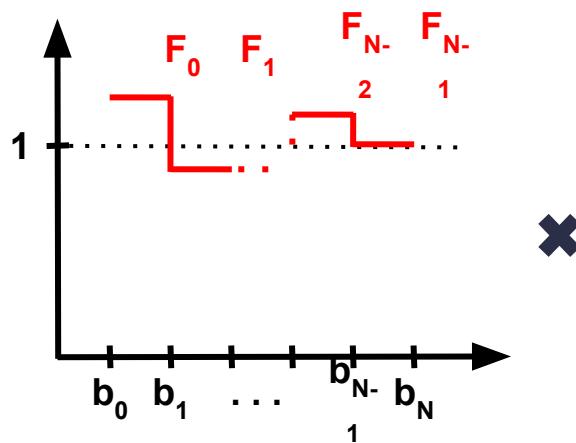
N extra-parameters



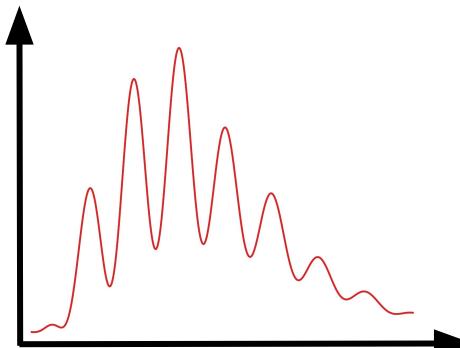
Modelling deviations with transfer functions

10

N extra-parameters



Λ CDM parameters



\times

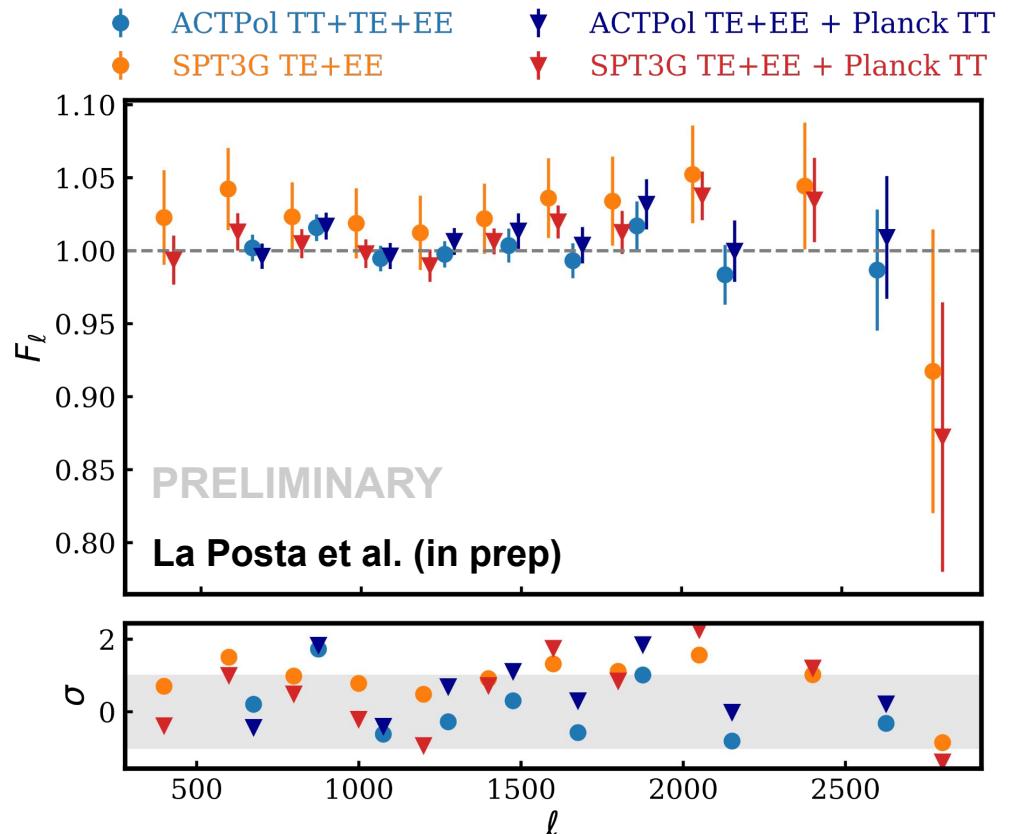
$=$

Power Spectra
Model

Polarization transfer function

11

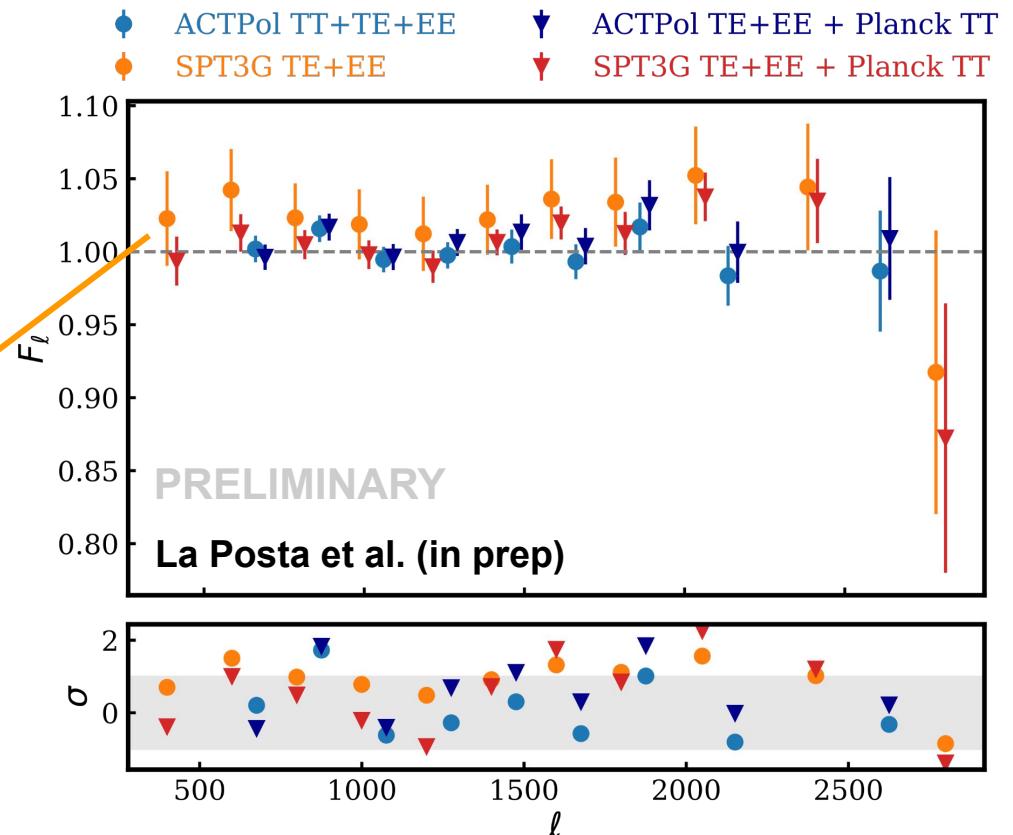
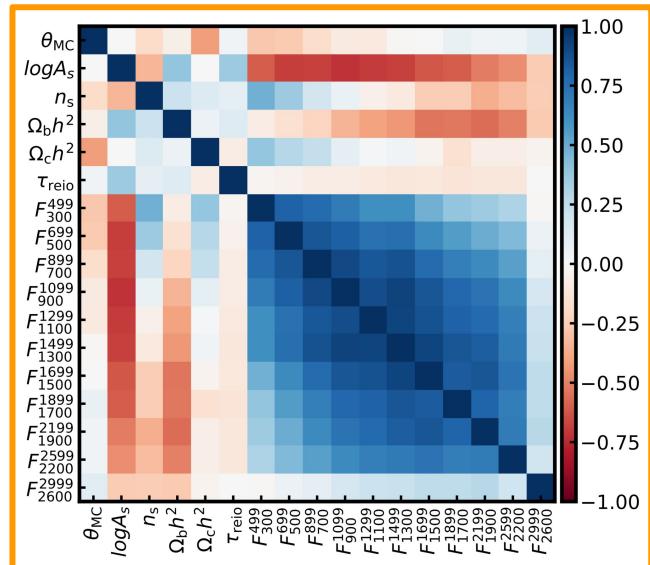
$$\tilde{C}_\ell^{TE} = F_\ell C_\ell^{TE}$$
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SPT3G [https://github.com/xgarrido/spt_likelihoods]ACT DR4 [<https://github.com/ACTCollaboration/pyactlike>]Planck Plik_lite [<https://github.com/CobayaSampler/cobaya>]

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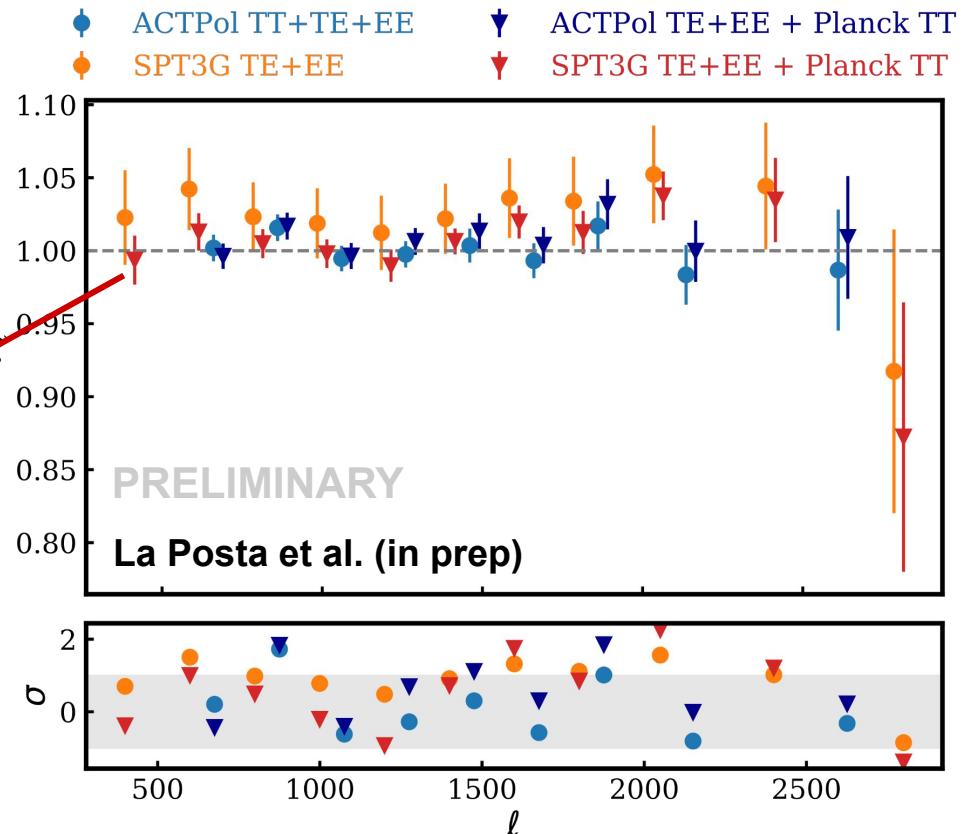
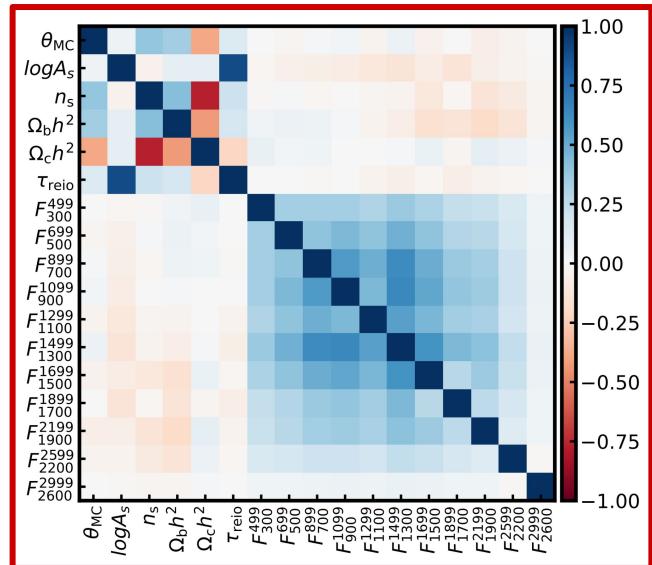


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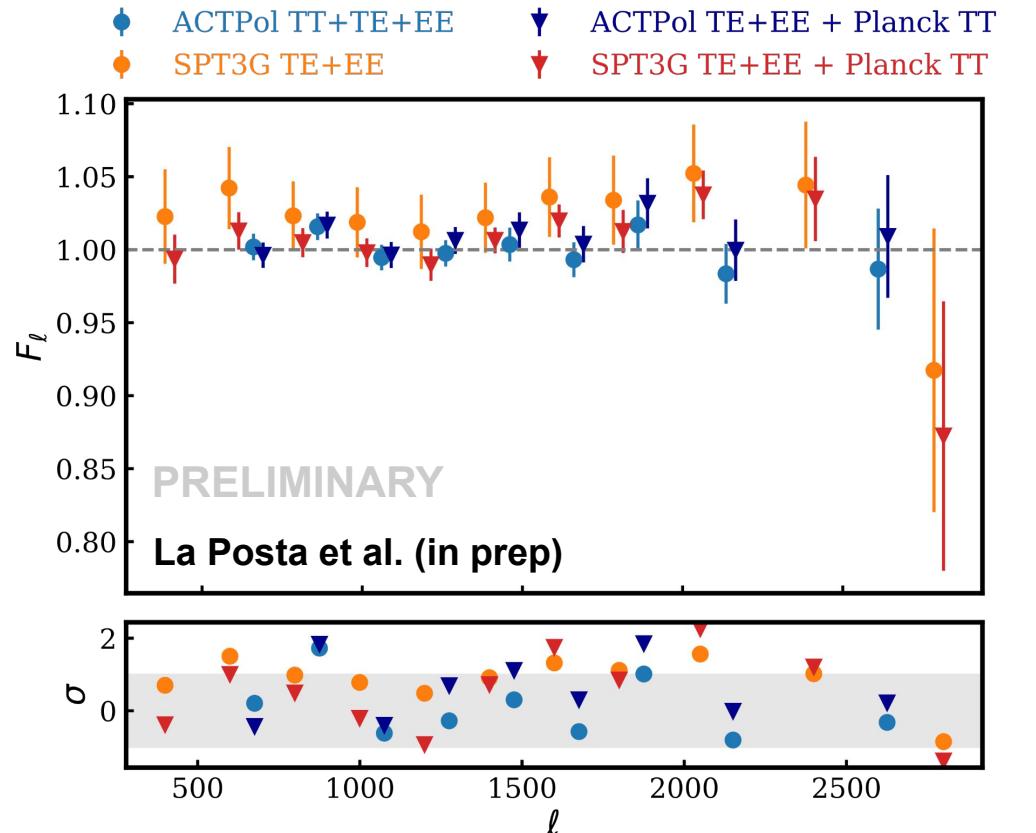
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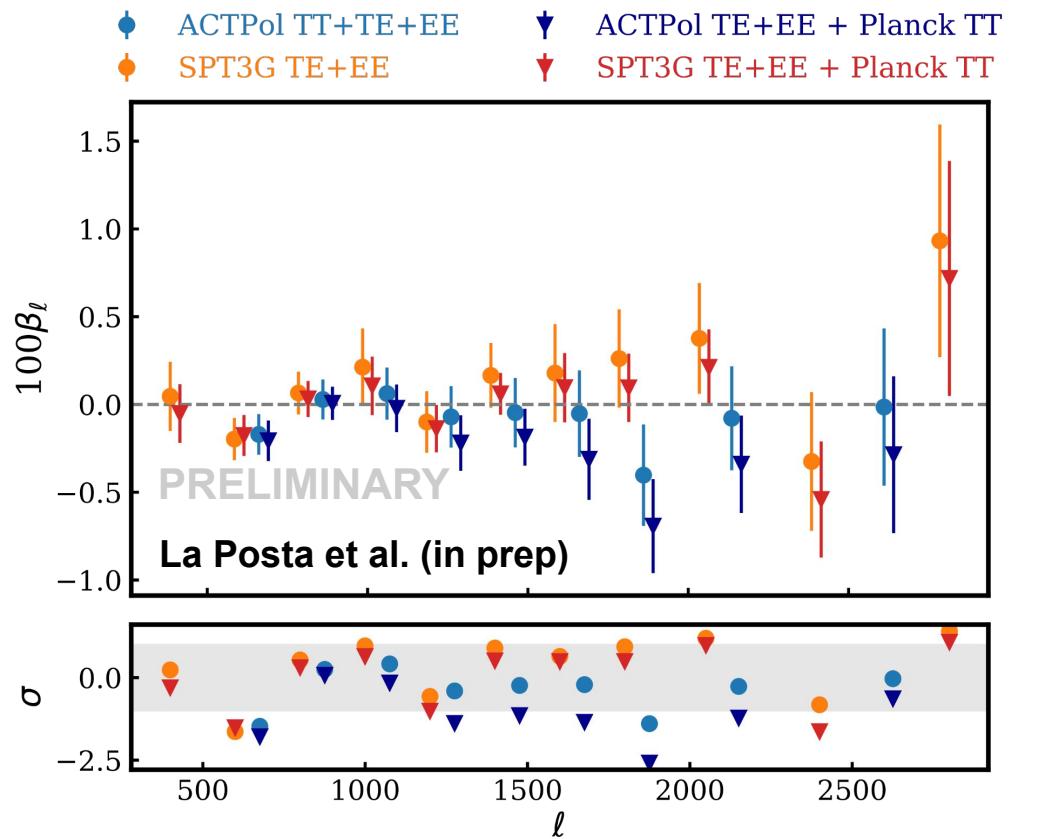
	x ² / dof (PTE)
ACT TT/TE/EE	6.00/9 (0.74)
ACT TE/EE + Planck TT	8.64/9 (0.47)
SPT3G TE/EE	12.82/11 (0.31)
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T to E leakage

$$\begin{aligned}\tilde{C}_\ell^{TE} &= C_\ell^{TE} + \beta_\ell C_\ell^{TT} \\ \tilde{C}_\ell^{EE} &= C_\ell^{EE} + 2\beta_\ell C_\ell^{TE} \\ &\quad + \beta_\ell^2 C_\ell^{TT}\end{aligned}$$



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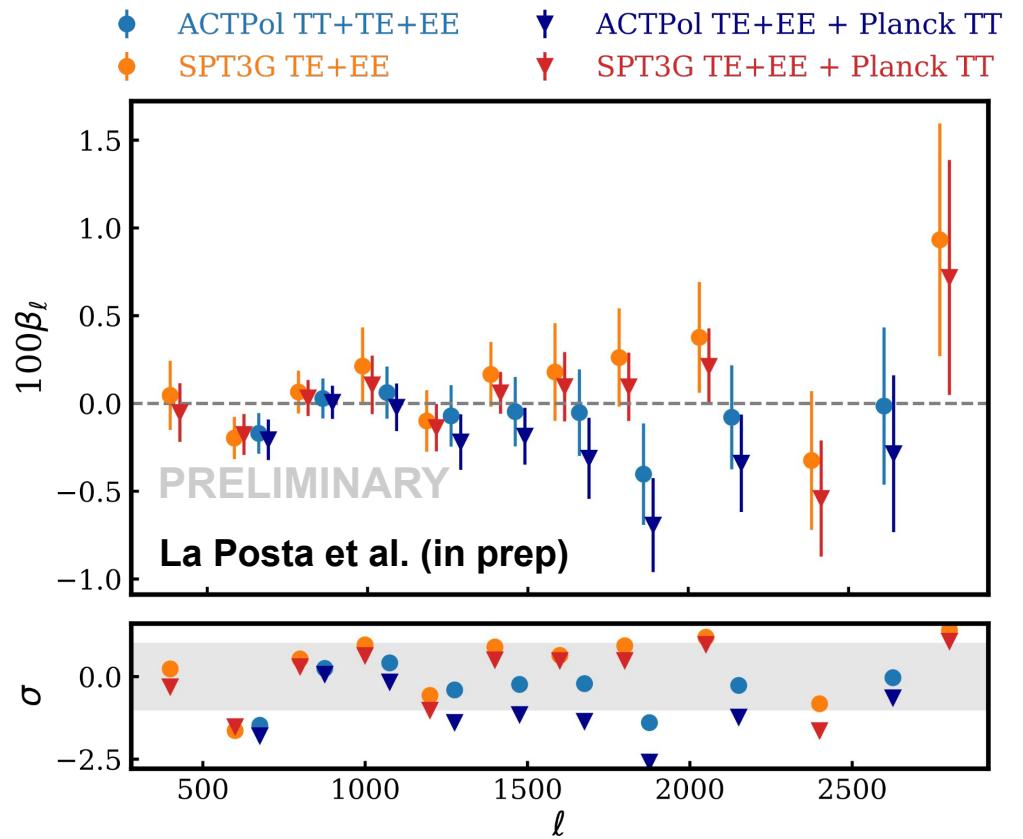
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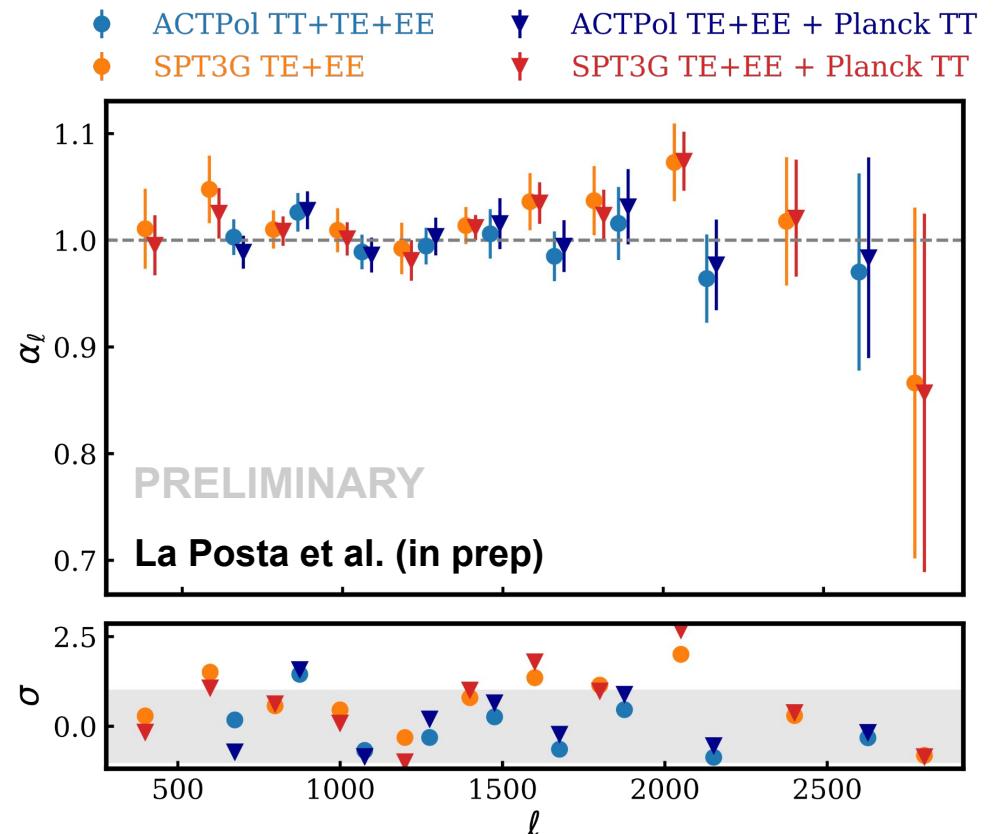
	$\chi^2 / \text{dof (PTE)}$
ACT TT/TE/EE	4.63/9 (0.87)
ACT TE/EE + Planck TT	15.11/9 (0.09)
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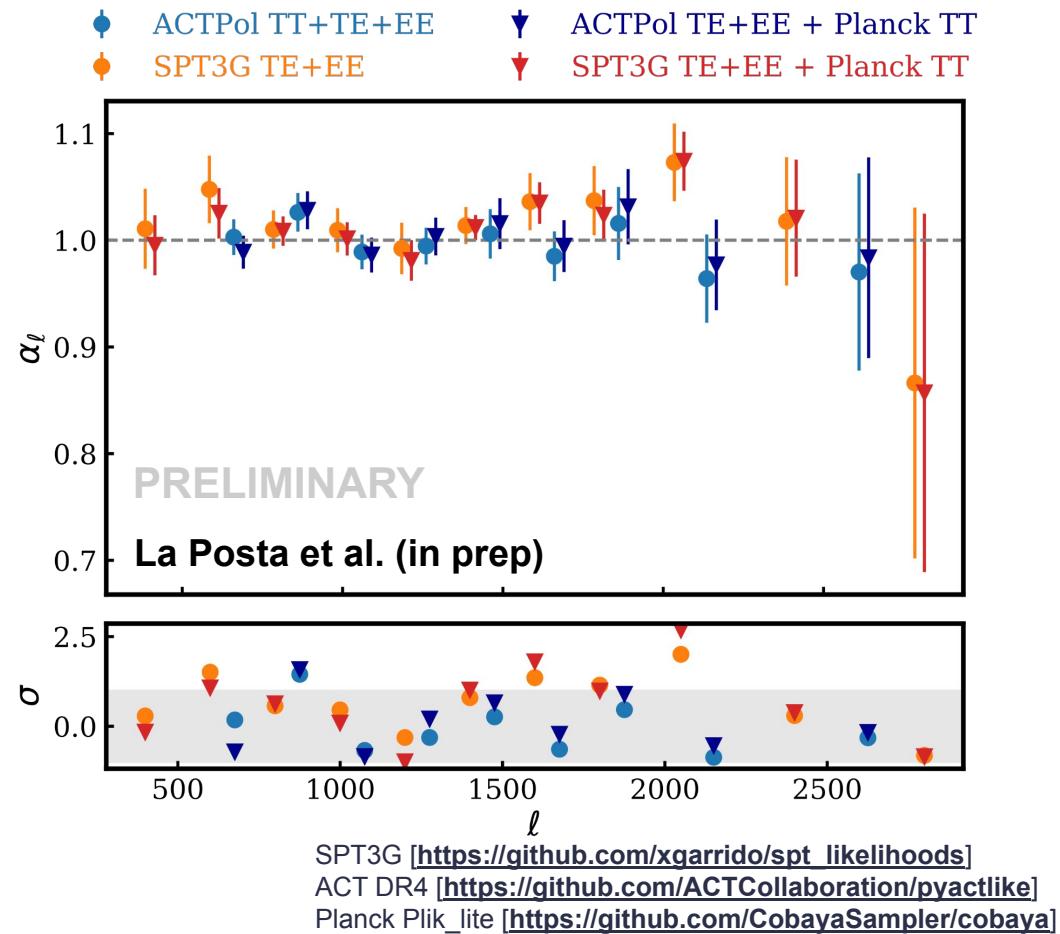
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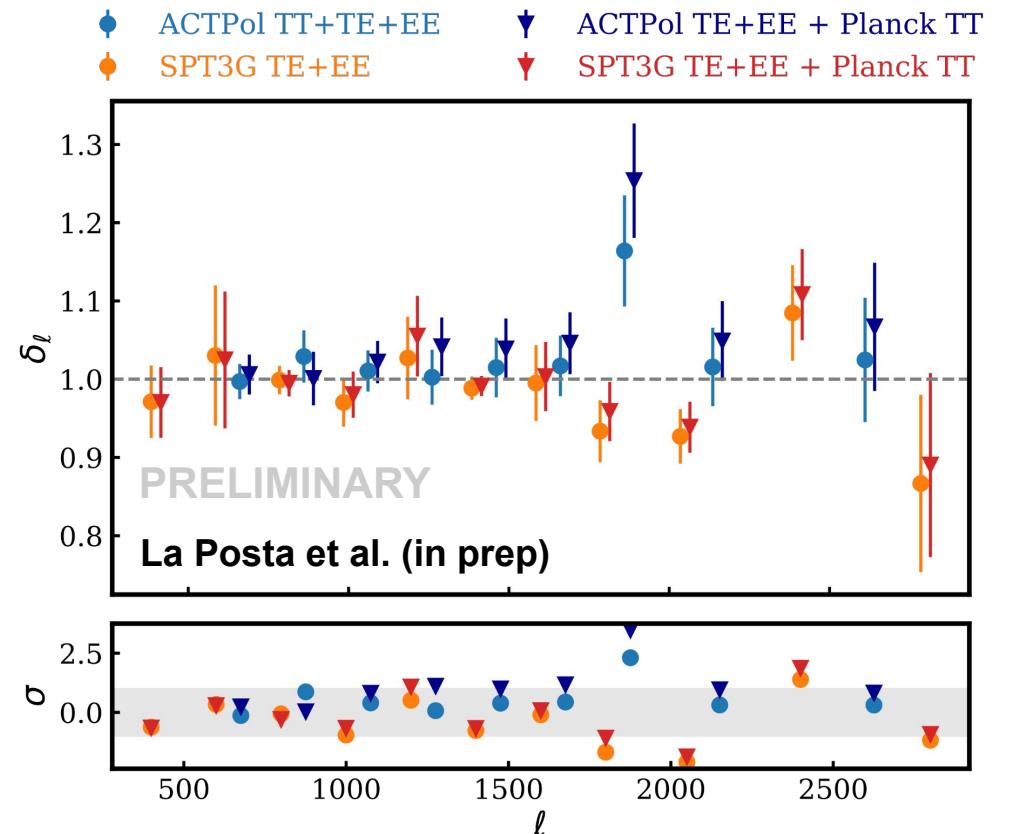
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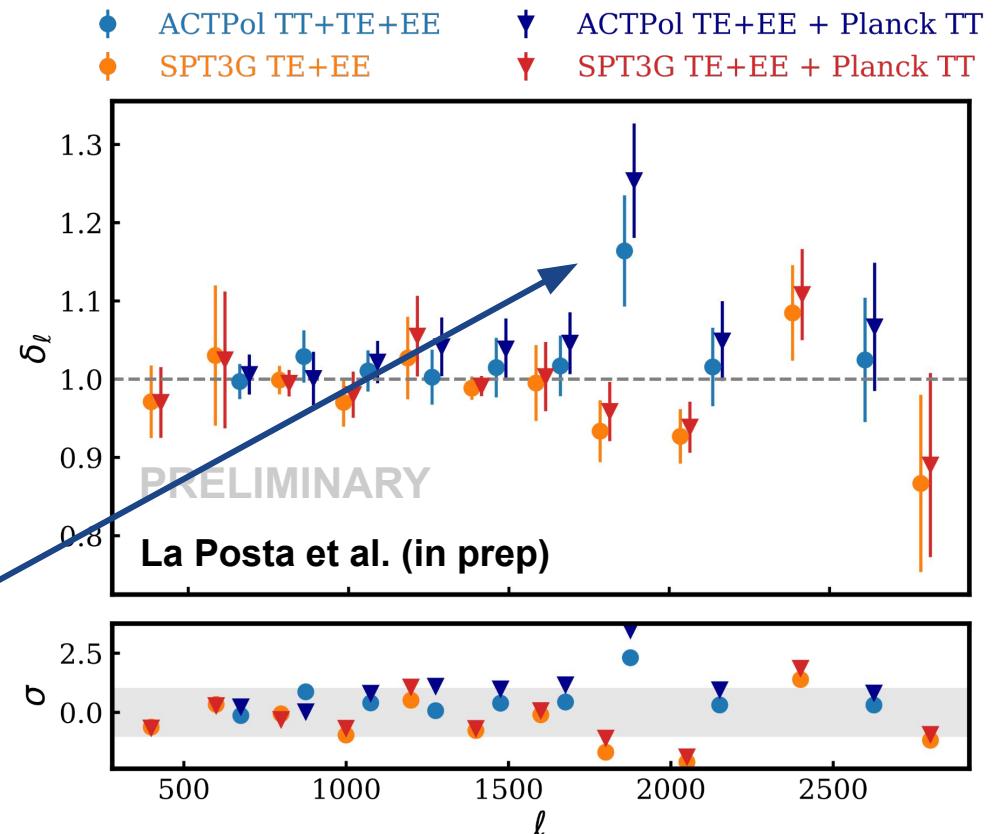
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TE bias

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$$\tilde{C}_\ell^{TE} = \delta_\ell C_\ell^{TE}$$
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TE amplitude difference with respect to Planck have already been noticed in Aiola et al. (2020)



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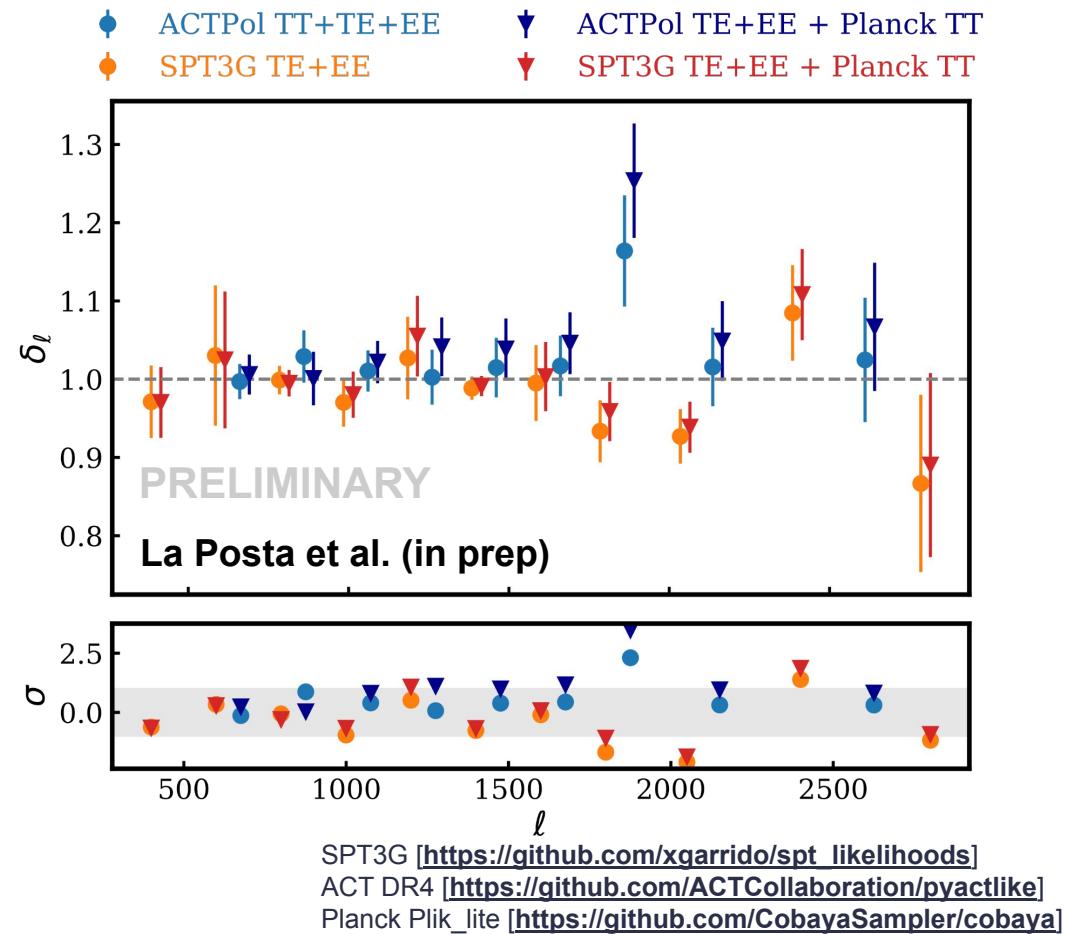
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ACT TT/TE/EE	6.54/9 (0.68)
ACT TE/EE + Planck TT	17.43/9 (0.04)
SPT3G TE/EE	11.93/11 (0.37)
SPT3G TE/EE + Planck TT	10.68/11 (0.47)



Conclusion

- We found no significant deviations from Λ CDM in this analysis of Planck, SPT3G, ACTPol data
- With these methods, we are able to spot scale dependent T-E inconsistencies in a model independent way [with respect to Λ CDM]
- These methods also catch deviations due to instrumental systematic effects