Package 'BRIL'

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Title Bootstrap and Refine Iterative Locator

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Maintainer Adrien Brilhault <adrien.brilhault@gmail.com>

Description The BRIL algorithm estimates the main mode of bivariate distributions through three principal steps:

- BOOTSTRAP: a recursive depth (or convex body minimizers) trimming to locate a first estimate.
- REFINE: a two-pass outliers filtering, the first relying on euclidean distances to the first estimate and unimodality tests, the second on robust distances and multinormality tests.
- ITERATE: after removing the samples selected in the REFINE step from the global distribution, the same process is reapplied, the first mode corresponding to the iteration with the largest number of samples.

For more details, consult the publication https://rdcu.be/cI9Pf>.

```
Depends R (>= 3.5.0)
Imports ddalpha,
     depth,
     OjaNP,
     MASS,
     diptest,
     robustbase,
     stats,
     utils,
     nortest,
     ICS,
     graphics,
     grDevices,
     CompQuadForm
Remotes cran/OjaNP
Suggests mytnorm
License GPL-3 | file LICENSE
URL https://adrienbrilhault.github.io/BRIL/, https:
     //github.com/adrienbrilhault/BRIL/
BugReports https://github.com/adrienbrilhault/BRIL/issues
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```

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bril

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Bootstrap and Refine Iterative Locator

Description

Robust Estimate of Mode in Multivariate Distribution

Usage

```
bril(
  data,
  maxIterations = NULL,
  minUnassigned = 0.1,
  method = "Projection",
  alpha = 0.5,
  testUnimodal = "DIP",
  threshUnimodal = 0.05,
  distUnimodal = "Euclidean",
  testNormal = "Mardia",
  threshNormal = 0.05,
  distNormal = "MCD",
  trimmedPerFilteringIteration = 1,
  exitWhenUnimodal = FALSE,
  debug = FALSE,
  warnings = FALSE
)
```

Arguments

data Matrix of numerical values containing the observations (one per row, with two columns for X and Y coordinates)

maxIterations Maximum number of iterations performed by the algorithm (set to NULL or 0 for unlimited number)

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minUnassigned Numerical value between 0 and 1 (default: 0.1), providing the proportion of

unassigned samples from data below which the algorithm will terminate

method Method to use. Valid options are "MCD" and "MVE" for convex body minimiz-

ers, or "L2", "Lui", "Mahalanobis", "Oja", "Projection" (default), "Spatial" and

"Tukey" for depth functions

alpha Proportion of samples trimmed at each iteration of the recursive median estimate

(numerical value between 0 and 1, default: 0.5), see median_rec()

testUnimodal Statistical test used for unimodality. Valid options are "DIP" only, see filter_outliers()

threshUnimodal Threshold of significance for the unimodality test (numerical value between 0

and 1, default: 0.05)

distUnimodal Distance metric used for ordering the samples in the unimodal filtering. Valid

options are "Euclidean" (default), or "MCD", "MVE", and "OGK" for robust

distances. "Euclidean" is strongly advised for unimodality tests.

testNormal Statistical test used for normality. Valid options are "Mardia" (default), "Kurto-

sis", "Skewness", "KS", "KS-adj", "Shapiro", "Lillie" and "Chisq", see filter_outliers()

threshNormal Threshold of significance for the normality test (numerical value between 0 and

1, default: 0.05)

distNormal Distance metric used for ordering the samples in the normal filtering. Valid

options are "Euclidean", or "MCD" (default), "MVE", and "OGK" for robust

distances. Robust distances are strongly advised for normality tests.

trimmedPerFilteringIteration

Number of samples trimmed at each iteration of the unimodality and normality

filtering (default: 1), see filter_outliers()

exitWhenUnimodal

Logical value. TRUE will terminate the execution of the algorithm as soon as an

unimodal subset is encountered on the start of a global iteration. FALSE (default)

will let that last iteration proceed before terminating

debug Logical value. TRUE will compute all p.values in the filtering steps (even after

they exceed the selection threshold, see plot.BRIL.Filtering())

warnings Logical value, to display the warnings and errors caught

Value

The function returns an S3 object of type BRIL containing the following values:

call Parameters of the call (contains data, maxIterations, minUnassigned, method,

alpha, testUnimodal, threshUnimodal, distUnimodal, testNormal, threshNormal,

 $\verb|distNormal|, trimmedPerFilteringIteration|, and exitWhenUnimodal|)$

iterations A list with every global iteration of the algorithm, each containing the two filter-

ing procedures performed: filteringUnimodal and filteringNormal (both

being S3 object of class BRIL.Filtering, see filter_outliers())

nbClusters Number of groups encountered

labels Labels of the groups encountered (corresponding to the number of the iteration

they were identified in)

clustersCenters

Matrix containing the coordinates of the centers of each group (row-wise)

clustersSizes Array with the number of samples in each group mainCluster Index of the group identified as main mode

mode Coordinates of the main mode

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References

Adrien Brilhault, Sergio Neuenschwander, and Ricardo Rios - A New Robust Multivariate Mode Estimator for Eye-tracking Calibration - Behavior Research Methods, 2022 - rdcu.be/cI9Pf

See Also

```
plot.BRIL(), print.BRIL(), filter_outliers(), median_rec(), median_mv(), depth_values()
```

Examples

```
# Create a sample distribution and run bril() function
XY <- rbind(
    mvtnorm::rmvnorm(300, c(0, 0), diag(2) * 3 - 1),
    mvtnorm::rmvnorm(100, c(15, 20), diag(2)),
    mvtnorm::rmvnorm(150, c(-10, 15), diag(2) * 2 - 0.5),
    mvtnorm::rmvnorm(200, c(5, 5), diag(2) * 200)
)

res <- bril(XY, debug = TRUE)
print(res)

# Plot the mode and groups encountered
plot(res)

# Plot the different iterations (interactive)
## Not run:
plot(res, contents = "iterations", asp = 1)

## End(Not run)

# See ?plot.BRIL() for other plotting examples</pre>
```

depth_values

Depth functions wrapper

Description

Computes the depth values with respect to the distribution provided in data of either all the coordinates given in u, or all observations from data if u is not provided. Depth computations rely on the packages depth and ddalpha.

Usage

```
depth_values(data, u = NULL, method = "Projection", warnings = FALSE)
```

Arguments

data

Matrix of numerical values containing the observations (one per row, with two columns for X and Y coordinates)

u

Matrix of numerical values containing the coordinates for which depth values are to be computed (in rows, with two columns for X and Y coordinates). When missing or NULL, depth values will be computed for all observations from data

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method Depth function used. Valid options are "L2", "Lui", "Mahalanobis", "Oja", "Projection" (default), "Spatial", "Tukey"

Logical value, to display the warnings and error raised by the underlying depth functions

Value

Array of numerical values containing the depth of each observation from data, or from u if provided (these values are all set to 0 in the occurrence of errors)

See Also

```
bril(), filter_outliers(), median_rec(), median_mv()
```

Examples

```
# Illustrative data
XY <- rbind(</pre>
  mvtnorm::rmvnorm(300, c(0, 0), diag(2)),
  mvtnorm::rmvnorm(100, c(15, 20), diag(2) * 3 - 1),
  mvtnorm::rmvnorm(150, c(-10, 15), diag(2) * 2 - 0.5),
 mvtnorm::rmvnorm(200, c(5, 5), diag(2) * 200)
# Compute depths
D <- depth_values(XY, method = "L2", warnings = TRUE)
# Plot distribution with depth color scale
plotColors <- colorRampPalette(c("maroon4", "steelblue4", "green4", "gold"))(20)</pre>
plot(XY, pch = 20, asp = 1, col = plotColors[as.numeric(cut(D, breaks = 20))],
     xlab = "X", ylab = "Y")
# Plot depth values
plot(1:nrow(XY), D, pch = 20, col = plotColors[as.numeric(cut(D, breaks = 20))],
     xlab = "Index", ylab = "Depth")
# Compute depth for a single point
depth\_values(XY, c(10, 3), method = "L2")
# Compute depth for three sets of coordinates
depth\_values(XY, rbind(c(10, 3), c(65, 8), c(0, 1)), method = "L2")
```

filter_outliers

Recursive outlier filtering based on unimodality and multinormality tests

Description

Recursive outlier filtering based on unimodality and multinormality tests

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Usage

```
filter_outliers(
  data,
  center,
  test = "Mardia",
  threshold = 0.05,
  distType,
  trimmedPerIteration = 1,
  debug = FALSE,
  warnings = FALSE
)
```

Arguments

data Matrix of numerical values containing the observations (one per row, with two

columns for X and Y coordinates)

center Coordinates used to computes the distances of the samples and order them (array

of numerical two values, for X and Y)

test Statistical test to use. Valid options are "DIP" for unimodality test, or "Mardia",

"Kurtosis", "Skewness", "KS", "KS-adj", "Shapiro", "Lillie", and "Chisq" for

multivariate normality test

threshold Threshold of significance for the statistical test (between 0 and 1, default: 0.05)

distType Distance metric used to order the samples. Valid options are "Euclidean", "MCD",

"MVE", and "OGK". If empty or NULL, "Euclidean" will be automatically se-

lected for unimodality tests, and "MCD" for normality tests

trimmedPerIteration

Number of samples trimmed at each iteration (positive integer, default: 1)

debug Logical value. TRUE will compute all p.values, even after exceeding the thresh-

old, for plotting purpose (see plot.BRIL.Filtering())

warnings Logical value, to display the warnings and errors caught

Details

For unimodality tests parameter distType should be set to "Euclidean" (as the distribution might contains a large amount of outliers). For normality tests robust distances are preferable, using a robust estimate estimates of location and scatter ("MCD","MVE", or "OGK").

Value

The function returns an S3 object of type BRIL.Filtering containing the following values:

call Parameters of the call (contains data, test, testType, center, threshold,

trimmedPerIteration and distType)

distances Distances of each sample from data to the center provided

p. values P. Values of the test at each iteration

index.p.values Subset size corresponding to each P.Value, for plotting purpose selected Indices of the samples from data selected at the end of the filtering

cutoffDistance Distance of the furthest inlier selected

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See Also

```
plot.BRIL.Filtering(), print.BRIL.Filtering(), bril(), median_rec(), median_mv(), depth_values()
```

Examples

```
## Example 1
# Illustrative data
XY <- rbind(</pre>
 mvtnorm::rmvnorm(300, c(0, 0), diag(2) * 3 - 1),
 mvtnorm::rmvnorm(100, c(15, 20), diag(2)),
 mvtnorm::rmvnorm(150, c(-10, 15), diag(2) * 2 - 0.5),
 mvtnorm::rmvnorm(200, c(5, 5), diag(2) * 200)
)
# Compute an estimate for the center
center <- median_rec(XY)$median</pre>
# Remove non unimodal outliers from this location
filtering <- filter_outliers(XY, center, test = "DIP", debug = TRUE)</pre>
print(filtering, maxDisplayed = 200)
plot(filtering)
## Example 2
# Illustrative data
XY <- rbind(</pre>
 mvtnorm::rmvnorm(300, c(0, 0), diag(2) * 4 - 1.5),
 mvtnorm::rmvnorm(150, c(5, 5), diag(2) * 400)
# Compute an estimate for the center
center <- median_rec(XY)$median</pre>
# Remove non normal outliers from this location
filtering <- filter_outliers(XY, center, test = "Chisq", distType = "MVE", debug = TRUE)
print(filtering)
plot(filtering, asp = 1)
```

median_mv

Multivariate Median

Description

Computes the Multivariate Median of the distribution provided in data (depth computations rely on the packages depth, OjaNP and ddalpha, while convex body minizers "MCD" and "MVE" use the package MASS).

Usage

```
median_mv(data, method = "Projection", sampleMedian = TRUE, warnings = FALSE)
```

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Arguments

data Matrix of numerical values containing the observations (one per row, with two

columns for X and Y coordinates)

method Method to use. Valid options are "CW", "MCD", "MVE", "L2", "Lui", "Maha-

lanobis", "Oja", "Projection" (default), "Spatial" and "Tukey"

sampleMedian Logical value. If TRUE (default), the function will return the Sample Median

(observation from data with the highest depth). If FALSE, it will return the classic Multivariate Median (point in space with the highest depth), when applicable

(methods "Oja", "Turkey" and "Spatial")

warnings Logical value, to display the warnings and error caught by the underlying func-

tions

Value

Coordinates of the Multivariate Median

See Also

```
median_rec(), depth_values(), bril()
```

Examples

```
# Illustrative data
XY <- rbind(</pre>
  mvtnorm::rmvnorm(200, c(0, 0), diag(2)),
 mvtnorm::rmvnorm(100, c(15, 20), diag(2) * 3 - 1),
 mvtnorm::rmvnorm(150, c(-10, 15), diag(2) * 2 - 0.5),
 mvtnorm::rmvnorm(100, c(5, 5), diag(2) * 200)
# Compute median
m <- median_mv(XY, method = "L2", warnings = TRUE)</pre>
# Plot results
plot(XY, asp = 1, xlab = "X", ylab = "Y")
points(m[1], m[2], col = "red", pch = 3, cex = 1.5, lwd = 3)
## Others examples of medians
## Not run:
median_mv(XY, method = "0ja")
median_mv(XY, method = "Tukey", sampleMedian = TRUE)
median_mv(XY, method = "Tukey", sampleMedian = FALSE)
## End(Not run)
```

median_rec

Recursive estimate of central location

Description

Recursive estimate of central location based on depth measures (from the packages depth and ddalpha) or convex body minimizers (package MASS).

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Usage

```
median_rec(
  data,
  method = "Projection",
  alpha = 0.5,
  maxIterations = NULL,
  warnings = FALSE
)
```

Arguments

Matrix of numerical values containing the observations (one per row, with two columns for X and Y coordinates)

Method to use. Valid options are "MCD" and "MVE" for convex body minimizers, or "L2", "Lui", "Mahalanobis", "Oja", "Projection" (default), "Spatial" and "Tukey" for depth functions

alpha Proportion of samples trimmed at each iteration (numerical value between 0 and 1, default: 0.5)

maxIterations Set to a positive integer to limit the number of iterations, to NULL or 0 (default) for no limits

warnings Logical value, to display the warnings and error raised by the underlying func-

tions

Value

The function returns an S3 object of type BRIL. MedianRec, containing the following values:

median Coordinate of the recursive median

max Coordinate of the sample with the highest depth (or the center of the first iteration in the case of convex body minimizers)

iterations List containing the indices from the samples of data selected at each iteration

References

Adrien Brilhault, Sergio Neuenschwander, and Ricardo Rios - A New Robust Multivariate Mode Estimator for Eye-tracking Calibration - Behavior Research Methods, 2022 - rdcu.be/cI9Pf

See Also

```
plot.BRIL.MedianRec(), print.BRIL.MedianRec(), median_mv(), depth_values(), bril()
```

```
# Illustrative data
XY <- rbind(
    mvtnorm::rmvnorm(300, c(0, 0), diag(2)),
    mvtnorm::rmvnorm(100, c(15, 20), diag(2) * 3 - 1),
    mvtnorm::rmvnorm(150, c(-10, 15), diag(2) * 2 - 0.5),
    mvtnorm::rmvnorm(200, c(5, 5), diag(2) * 200)
)
# Compute the recursive median</pre>
```

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```
res <- median_rec(XY)
print(res)
plot(res)</pre>
```

plot.BRIL

Plot method for BRIL objects

Description

Plot method for BRIL objects

Usage

```
## S3 method for class 'BRIL'
plot(
    x,
    contents = "plot",
    showClusters = TRUE,
    showMode = TRUE,
    col,
    colMode,
    colClusters = NULL,
    iterationsIndices = NULL,
    iterationsOptions = NULL,
    ...
)
```

Arguments

x An object of class BRIL (see bril())

contents Contents to be displayed, options are "scatterplot", or "iterations" (only one op-

tion possible)

showClusters Logical value used when contents = "scatterplot", to show or not the dif-

ferent clusters

showMode Logical value used when contents = "scatterplot", to show or not the main

mode

col Default color of samples

colMode Color of the mode when contents = "scatterplot"

colClusters List (or array) of colors for each of the clusters/iterations (length must be at least

equal to the number of groups identified by the function bril(), i.e. x\$nbClusters)

iterationsIndices

Numerical value or array of numerical values, used when contents = "iterations", which provides the indices of the iterations to be plotted. If more than one iteration is requested, an interactive menu in the console will be used for the selection. 0 or NULL (default) will include all the iterations. Values that are negative or superior to the number of iterations performed by the execution bril() will be ignored

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iterationsOptions

List of additional parameters to be passed to the plot.BRIL.Filtering() function when contents = "iterations" is selected (see plot.BRIL.Filtering() for details). Example: iterationsOptions = list(xlab = NA, ylab = NA, contents = c("p.values", "scatterplot"), asp = 1)

Other arguments passed to or from other methods (such as pch for the symbols, main and sub for title and subtitle, xlab, xmin, ...)

See Also

. . .

```
bril(), print.BRIL(), filter_outliers(), print.BRIL.Filtering()
```

```
# Create a sample distribution and run bril() function
XY <- rbind(</pre>
  mvtnorm::rmvnorm(300, c(0, 0), diag(2) * 3 - 1),
  mvtnorm::rmvnorm(100, c(15, 20), diag(2)),
 mvtnorm::rmvnorm(150, c(-10, 15), diag(2) * 2 - 0.5),
 \verb|mvtnorm::rmvnorm(200, c(5, 5), diag(2) * 200)|\\
res <- bril(XY, debug = TRUE)</pre>
# Plot the mode and groups encountered (default)
plot(res)
# Plot the mode only
plot(res, showClusters = FALSE)
# Plot the mode only (with extra graphic options)
plot(res, showClusters = FALSE, main = "Multivariate Mode Estimate",
     col = "blue", colMode = "black", asp = 1, pch = 3 )
# Plot the clusters without the mode
plot(res, showMode = FALSE, col = "gray",
     colClusters = c("yellow","cyan","purple","red"))
\# Plot the second iteration
plot(res, contents = "iteration", iterationsIndices = 2)
# Plot the second iteration (with arguments to plot.BRIL.filtering())
plot(res, contents = "iteration", iterationsIndices = 2,
     iterationsOptions = list(
       contents = c("scatterplot", "p.values"),
       colSelection = "blue", mfrow = c(2,1), asp = 1))
## Not run:
# Plot all iterations (interactive mode)
plot(res, contents = "iterations")
# Plot the 3 first iterations with options (interactive mode)
plot(res, contents = "iterations", iterationsIndices = c(1:3),
     iterationsOptions = list(
       contents = c("scatterplot"),
       xlim = c(-50,50), ylim = c(-30,30), asp = 1)
```

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```
## End(Not run)
```

```
plot.BRIL.Filtering Plot method for BRIL.Filtering objects
```

Description

Plot method for BRIL. Filtering objects

Usage

```
## S3 method for class 'BRIL.Filtering'
plot(
    x,
    contents = c("p.values", "scatterplot", "dist", "hist"),
    showCenter = TRUE,
    showSelection = TRUE,
    col = "black",
    colSelection = "red",
    colCenter = "orange",
    mtextTitles = TRUE,
    mfrow,
    ...
)
```

Arguments

X	An object of class BRIL.Filtering (see filter_outliers())
••	
contents	Contents to be displayed, options are "p.values", "scatterplot", "dist", "hist" and
	"all"
showCenter	Logical value, to show the center used in the filtering
showSelection	Logical value, to highlight the samples selected by the filtering process
col	Default color for non-selected samples (default: "black")
colSelection	Color of the selected samples (default: "red")
colCenter	Color for the center in "scatterplot" (default: "orange")
mtextTitles	Logical value, TRUE to set smaller titles/subtitles on top, FALSE to use the default
	plot title options.
mfrow	Number of rows and columns of the figure (example: $c(4,1)$)
	Other arguments passed to or from other methods (such as pch for the symbols,
	main and sub for title and subtitle, xlab, xmin,)

Details

Red intercept lines correspond to the selection based on the p.values exceeding the given threshold. To display all the p.values, rerun the function filter_outliers() with the parameter debug = TRUE

contents options:

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- "p.values" provides a plot of the test p.values (in function of the subset size)
- "scatterplot" displays the data in cartesian coordinates. Selected samples are displayed in red, and the center used to compute distances as an orange cross
- "dist" shows the distances of each sample to the center provided in filter_outliers() (in function of sample index)
- "hist" draws an histogram of the distances of the samples to the center provided in filter_outliers()
- "all" displays a figure with all of the options above

See Also

```
filter_outliers(), print.BRIL.Filtering(), bril(), median_rec(), median_mv(), depth_values()
```

```
# Illustrative data
XY <- rbind(</pre>
  mvtnorm::rmvnorm(300, c(0, 0), diag(2) * 3 - 1),
  mvtnorm::rmvnorm(100, c(15, 20), diag(2)),
 mvtnorm::rmvnorm(150, c(-10, 15), diag(2) * 2 - 0.5),
 mvtnorm::rmvnorm(200, c(5, 5), diag(2) * 200)
# Process the data
filtering <- filter_outliers(XY, median_rec(XY)$median, test = "DIP", debug = TRUE)</pre>
# Plot all default figures
plot(filtering)
# Plot P. Values and Scatterplot only
plot(filtering, contents = c("pvalues", "scatterplot"))
# Change the layout to vertical
plot(filtering, contents = c("pvalues", "scatterplot"), mfrow = c(2, 1))
# Remove title, subtitle, and axis labels
plot(filtering, contents = "scatterplot", main = "", sub = "",
  ylab = "", xlab = "")
# Other graphical options
plot(filtering, contents = "scatterplot", asp = 1,
  xlim = c(-30, 30), ylim = c(-30, 30))
plot(filtering,
  contents = "scatterplot", asp = 1, pch = 4, lwd = 2, col = "blue",
  colSelection = "green", showCenter = FALSE
)
plot(filtering, contents = "hist", main = "My Histogram",
  showSelection = FALSE, breaks = 50)
```

plot.BRIL.MedianRec

plot.BRIL.MedianRec Plot method for BRIL.MedianRec objects

Description

Plot method for BRIL. MedianRec objects

Usage

```
## S3 method for class 'BRIL.MedianRec'
plot(x, nbIterations = 5, showMedian = FALSE, showMax = FALSE, ...)
```

Arguments

```
An object of class BRIL.MedianRec (see median_rec())

Number of iterations to display, or 0 to show all of them (default: 5)

ShowMedian Logical value, to show the final recursive median (indicated by a "+")

Logical value, to show the overall deepest point, or the center of the first MCD/MVE iteration (indicated by a "x")

Other arguments passed to or from other methods
```

See Also

```
median_rec(), median_mv(), bril()
```

```
# Illustrative data
XY <- rbind(
    mvtnorm::rmvnorm(300, c(0, 0), diag(2)),
    mvtnorm::rmvnorm(100, c(15, 20), diag(2) * 3 - 1),
    mvtnorm::rmvnorm(150, c(-10, 15), diag(2) * 2 - 0.5),
    mvtnorm::rmvnorm(200, c(5, 5), diag(2) * 200)
)

# Process the data
res <- median_rec(XY)

# Default plot
plot(res)

# Adjust axis
plot(res, asp = 1, xlim = c(-20, 20), ylim = c(-20, 20))

# Change other graphical options
plot(res, showMedian = TRUE, pch = 16, main = "Recursive Median")</pre>
```

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print.BRIL

Print method for BRIL objects

Description

Print method for BRIL objects

Usage

```
## S3 method for class 'BRIL'
print(x, maxDisplayed = NULL, ...)
```

Arguments

```
x An object of class BRIL (see bril())
```

maxDisplayed Number of elements to display in the output. Set to NULL (or 0) to show all

values.

.. Other arguments passed to or from other methods

See Also

```
bril(), plot.BRIL()
```

```
print.BRIL.Filtering Print method for BRIL.Filtering objects
```

Description

Print method for BRIL. Filtering objects

Usage

```
## S3 method for class 'BRIL.Filtering'
print(x, maxDisplayed = 200, ...)
```

Arguments

```
    x An object of class BRIL.Filtering (see filter_outliers())
    maxDisplayed Number of elements to display in the output (default: 200). Set to NULL (or 0) to show all values.
    ... Other arguments passed to or from other methods
```

See Also

```
filter_outliers(), plot.BRIL.Filtering(), bril()
```

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```
print.BRIL.MedianRec Print method for BRIL.MedianRec objects
```

Description

Print method for BRIL. MedianRec objects

Usage

```
## S3 method for class 'BRIL.MedianRec' print(x, ...)
```

Arguments

```
x An object of class BRIL.MedianRec (see median_rec())... Other arguments passed to or from other methods
```

See Also

```
median_rec(), plot.BRIL.MedianRec()
```

test_multinormality

Test the multivariate normality of a distribution

Description

Test the multivariate normality of a distribution

Usage

```
test_multinormality(
  values,
  test = "Mardia",
  threshold = 0.05,
  data,
  center,
  warnings = FALSE
)
```

Arguments

values l	Jnic	limensional	l array o	f n	umerical	values	(distances)
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test Statistical test used, valid options are "Mardia", "Kurtosis", "Skewness", "KS",

"KS-adj", "Shapiro", "Lillie", and "Chisq"

threshold Threshold of significance for the statistical test (default: 0.05)

data Matrix of numerical values containing the observations (one per row, with two

columns for X and Y coordinates)

center Center of the observations from data

warnings Logical value, to display the warnings and errors caught

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Details

Parameter data is only required for the tests "Mardia", "Skewness", "Kurtosis" and "Chisq", while parameter center is only required for "Chisq"

Value

p-value of the test (lower values suggest non normality)

See Also

```
filter_outliers()
```

test_unimodality

Test the unimodality of a distribution

Description

Test the unimodality of a distribution

Usage

```
test_unimodality(values, test = "DIP", warnings = FALSE)
```

Arguments

values Unidimensional array of numerical values (distances)
test Statistical test used (for now the only option is "DIP")
warnings Logical value, to display the warnings and errors caught

Value

p-value of the test (lower values suggest multimodality)

See Also

```
filter_outliers()
```

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