



**BookMaster**  
CONECTAMOS CONOCIMIENTOS

**Esquema-formulario**

# GEOMETRÍA



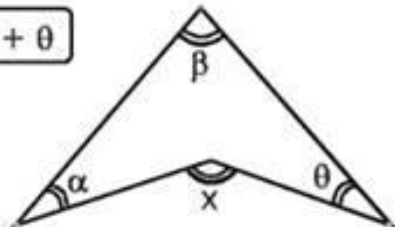
## CONTENIDO:

- Triángulos
- Congruencia de triángulos
- Cuadriláteros
- Circunferencia
- Proporcionalidad y semejanza de triángulos
- Relaciones métricas
- Áreas triangulares
- Áreas cuadrangulares
- Área circular
- Geometría del espacio
- Poliedros regulares
- Prismas y Cilindro
- Pirámide - Cono
- Esfera y teorema de Pappus Guldin
- Poligonos y Poliedros regulares

# TRIÁNGULOS

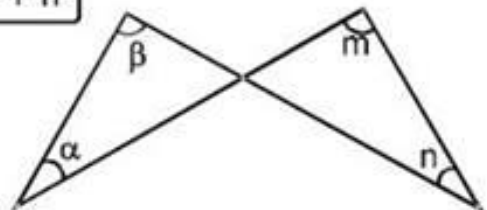
Se cumple:

$$x = \alpha + \beta + \theta$$



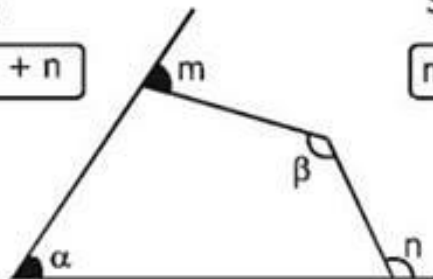
Se cumple:

$$\alpha + \beta = m + n$$



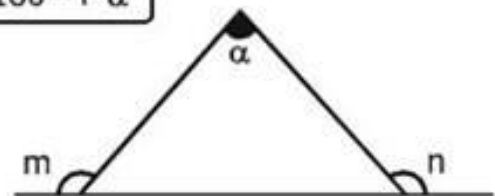
Se cumple:

$$\alpha + \beta = m + n$$

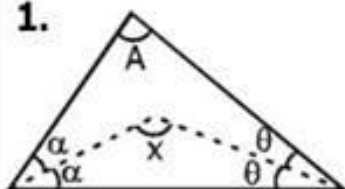


Se cumple:

$$m + n = 180^\circ + \alpha$$

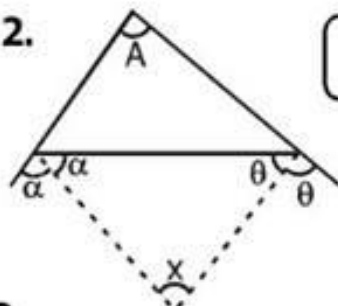


1.



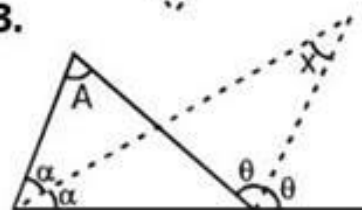
$$x = 90^\circ + \frac{A}{2}$$

2.



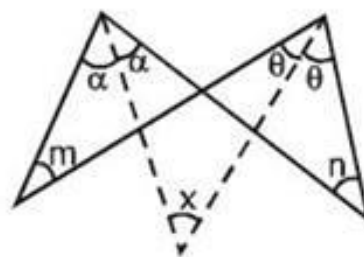
$$x = 90^\circ - \frac{A}{2}$$

3.



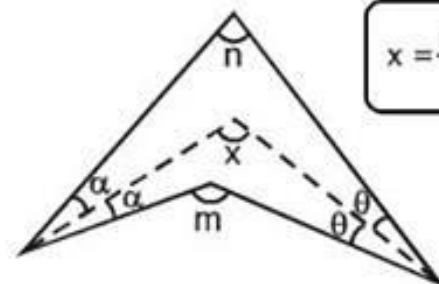
$$x = \frac{A}{2}$$

4.



$$x = \frac{m + n}{2}$$

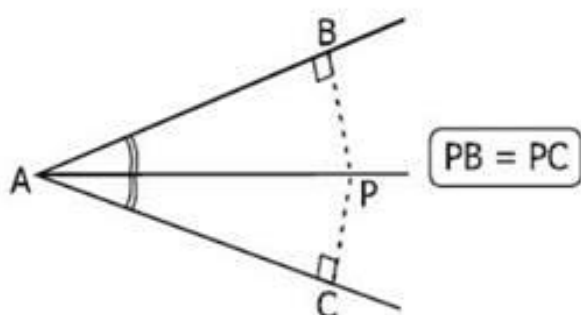
5.



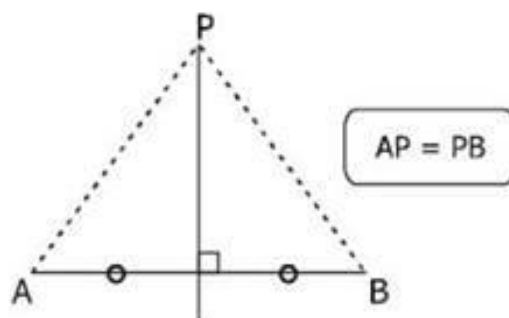
$$x = \frac{m + n}{2}$$

## CONGRUENCIA DE TRIÁNGULOS

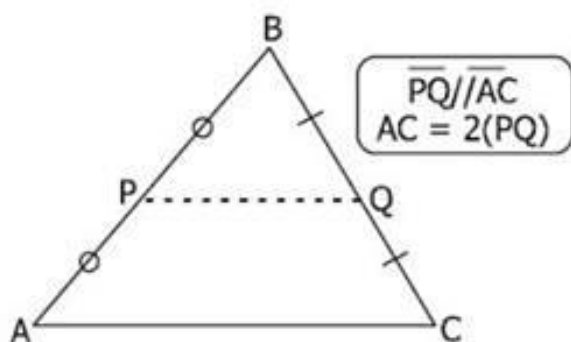
### T. de la Bisectriz



### T. de la Mediatriz

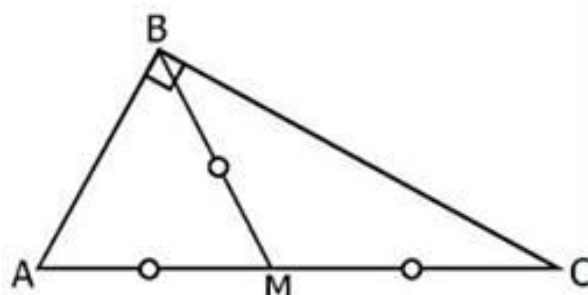


### T. de los Puntos Medios

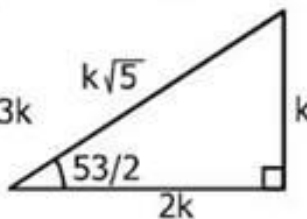
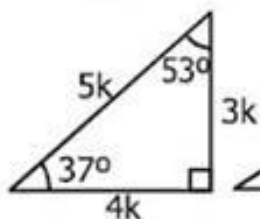
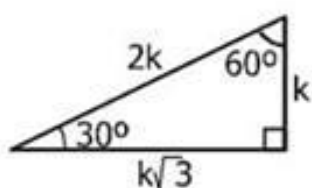
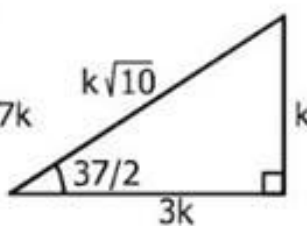
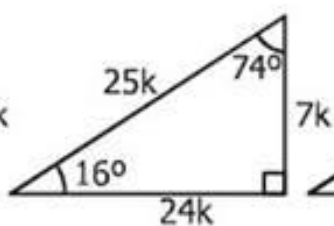
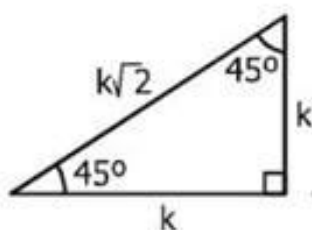


### Mediana relativa a la hipotenusa

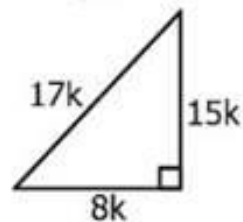
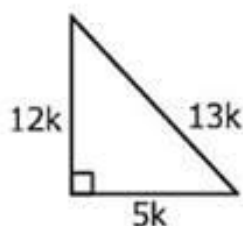
Si BM es la mediana relativa a la hipotenusa  $\Rightarrow BM = AM = MC$



### ⚡ Aproximados



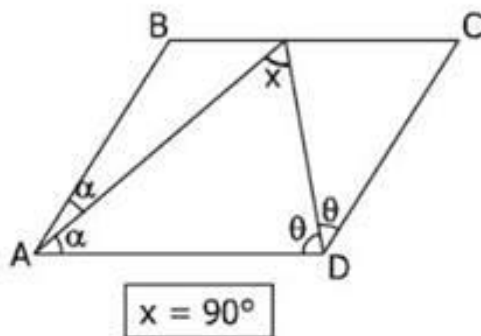
### ⚡ Pitagóricos



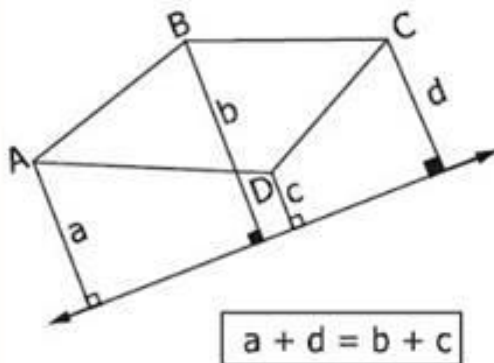


## CUADRILÁTEROS

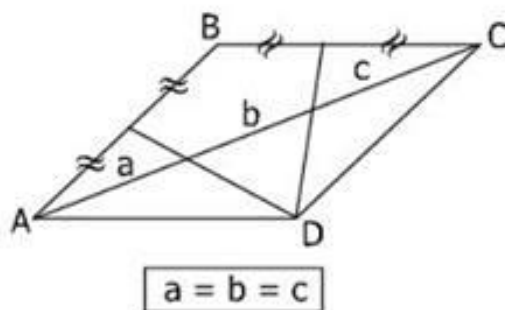
1. ABCD es un paralelogramo



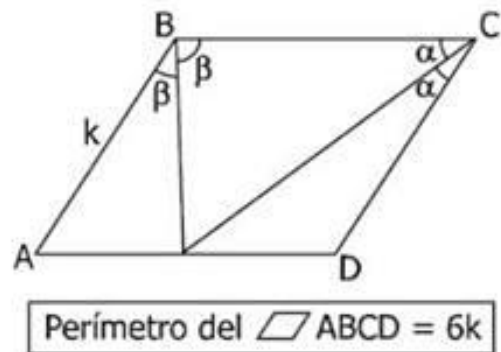
2. Si ABCD es un paralelogramo



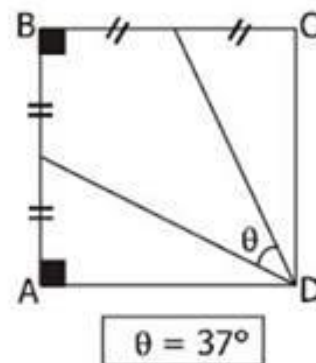
3. Si ABCD es un paralelogramo



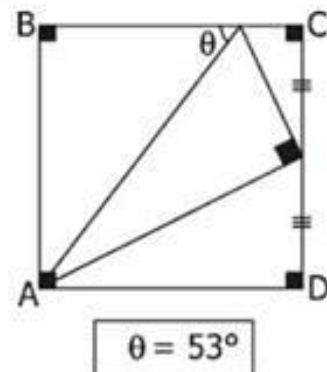
4. Si ABCD es un paralelogramo

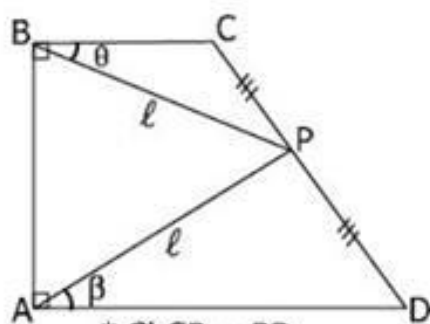


5. Si ABCD es un cuadrado



6. Si ABCD es un cuadrado

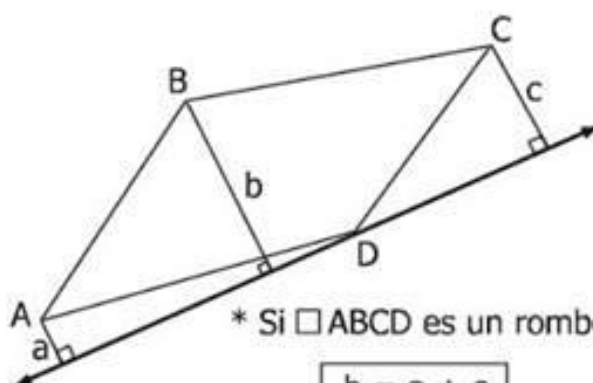




\* Si  $CP = PD$

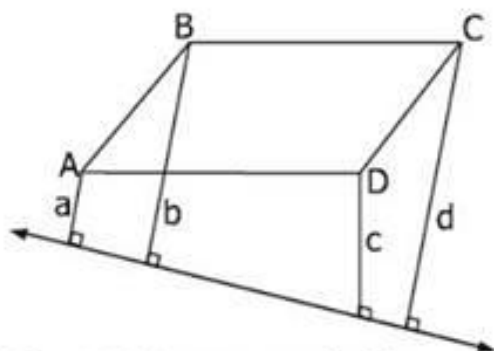
$$PA = PB$$

$$\theta = \beta$$



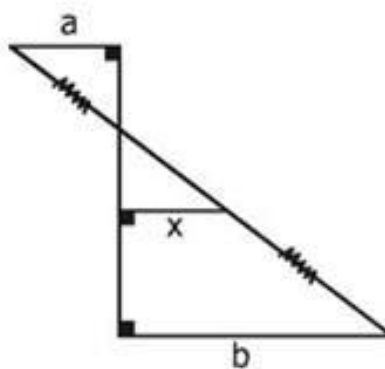
\* Si  $\square ABCD$  es un romboide

$$b = a + c$$



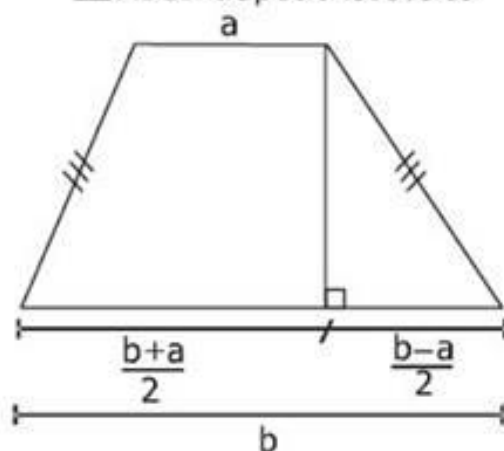
\* Si  $\square ABCD$  es un romboide

$$a + d = b + c$$



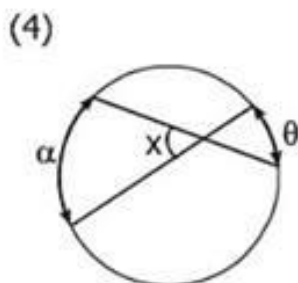
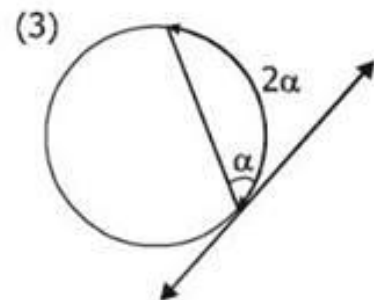
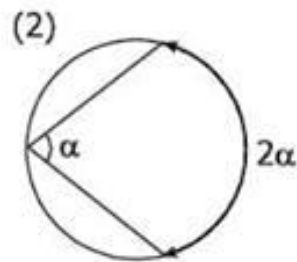
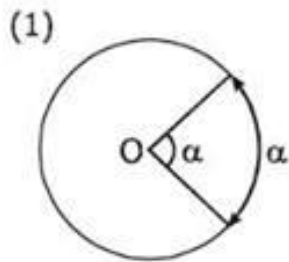
$$x = \frac{b - a}{2}$$

$\square ABCD$  trapecio isósceles

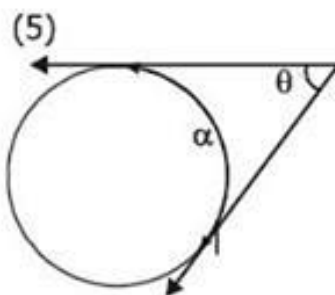


## CIRCUNFERENCIA

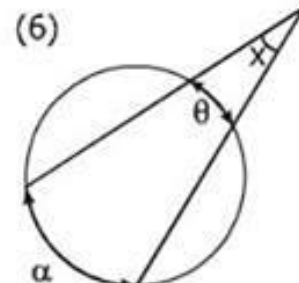
### Ángulos asociados a la circunferencia



$$x = \frac{\alpha + \theta}{2}$$

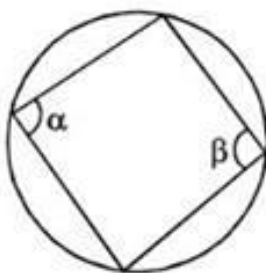


$$\alpha + \theta = 180^\circ$$



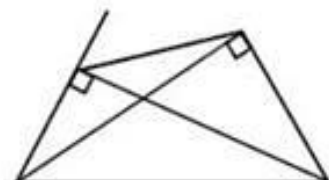
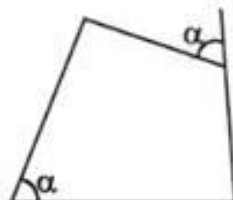
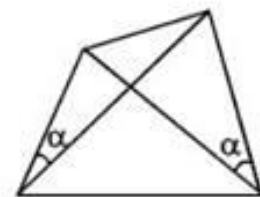
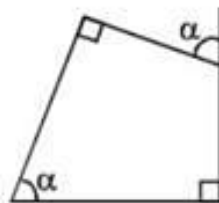
$$x = \frac{\alpha - \theta}{2}$$

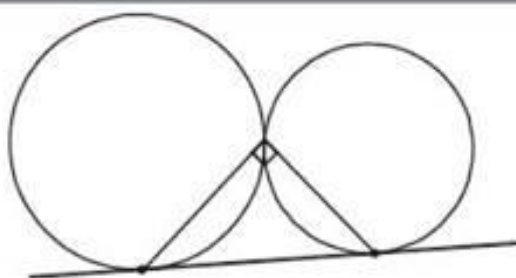
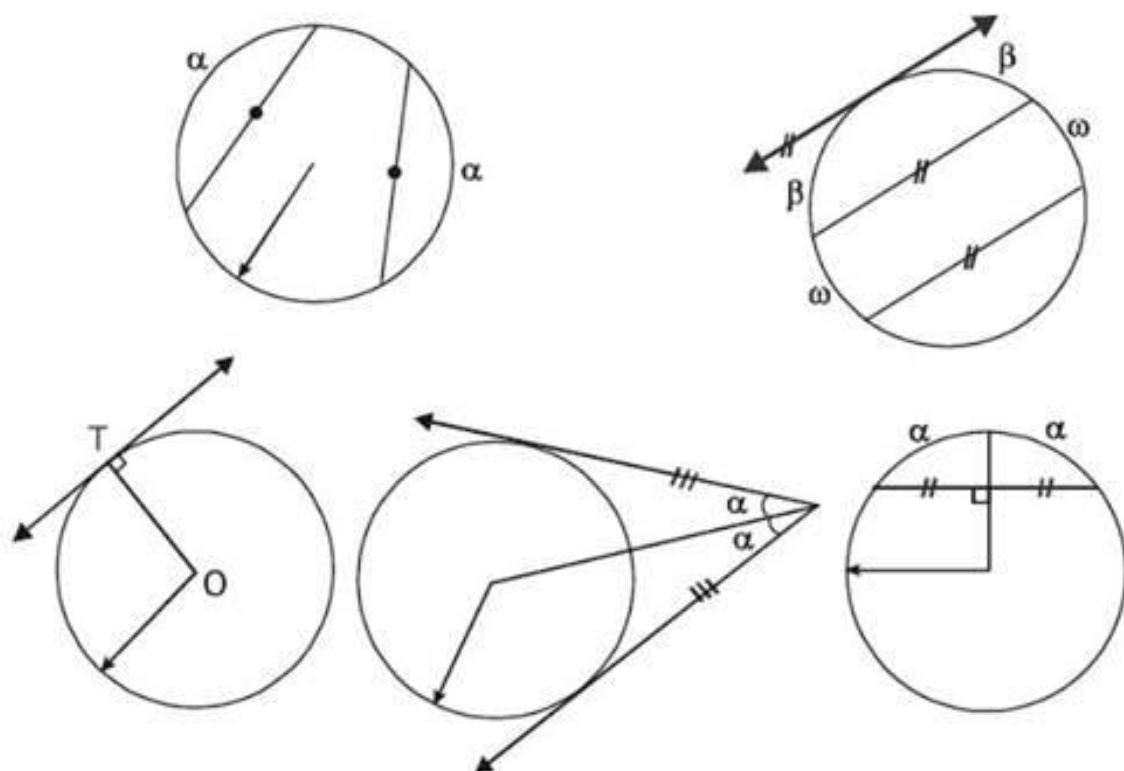
#### Cuadrilátero inscrito



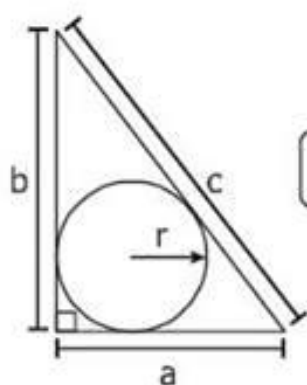
$$\alpha + \beta = 180^\circ$$

#### Cuadrilátero inscriptible



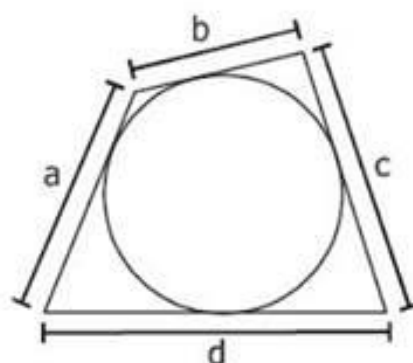


### Teorema de Poncelet



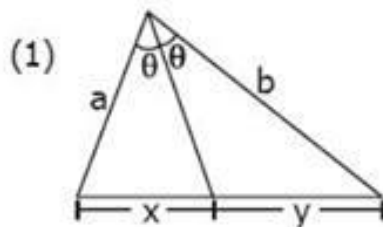
$$a + b = c + 2r$$

### Teorema de Pitot

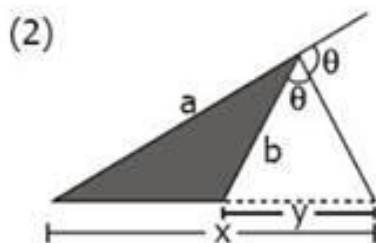


$$a + c = b + d$$

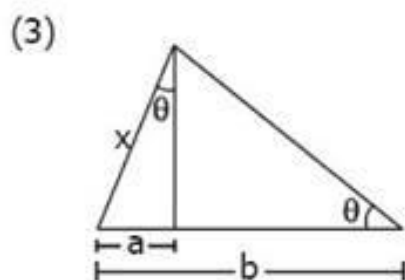
## PROPORCIONALIDAD Y SEMEJANZA DE TRIÁNGULOS



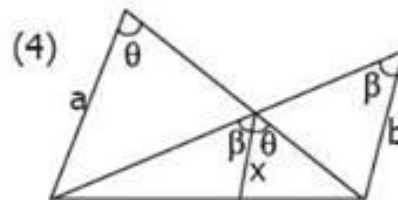
$$\frac{a}{b} = \frac{x}{y}$$



$$\frac{a}{b} = \frac{x}{y}$$

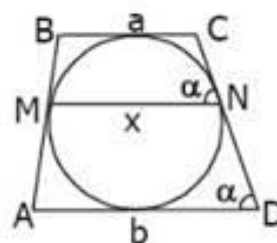


$$x^2 = ab$$

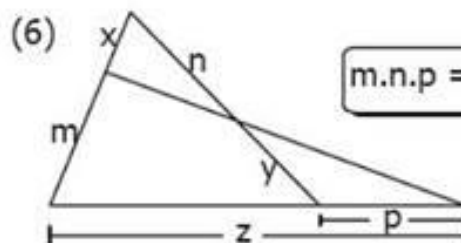


$$x = \frac{ab}{a + b}$$

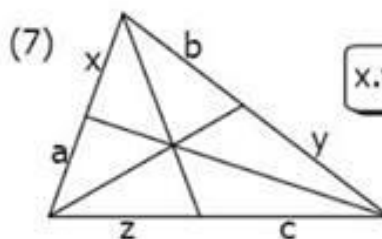
(5) En todo trapecio  
(M y N puntos de tangencia)



$$\frac{2}{x} = \frac{1}{a} + \frac{1}{b}$$



$$m.n.p = x.y.z$$

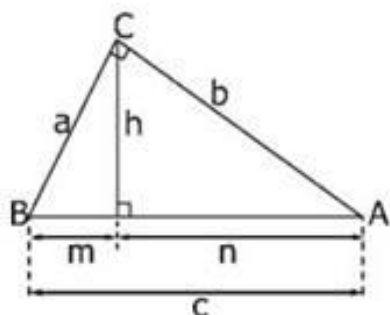


$$x.y.z = a.b.c$$

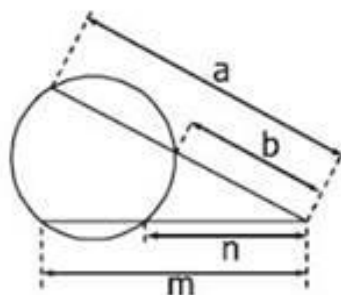


## RELACIONES MÉTRICAS

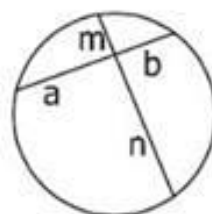
(1)



$$\begin{aligned} a^2 &= c \cdot m & h^2 &= m \cdot n \\ a \cdot b &= c \cdot h & a^2 + b^2 &= c^2 \\ b^2 &= c \cdot n \end{aligned}$$

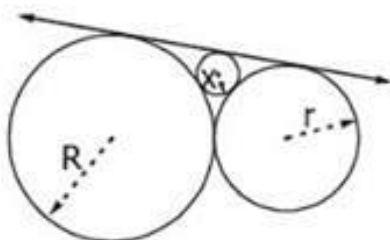


$$a \cdot b = m \cdot n$$



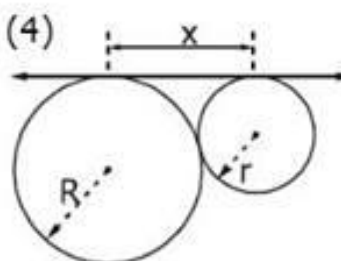
$$a \cdot b = m \cdot n$$

(2)



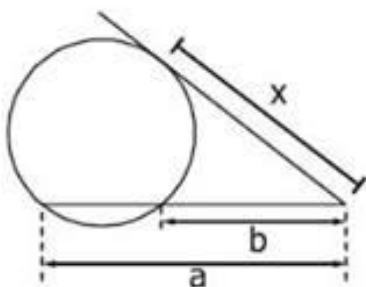
$$\frac{1}{\sqrt{x}} = \frac{1}{\sqrt{R}} + \frac{1}{\sqrt{r}}$$

(4)

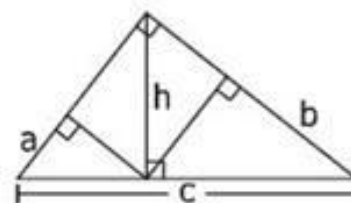


$$x = 2\sqrt{Rr}$$

(3)



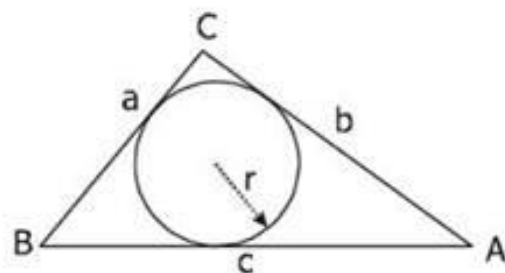
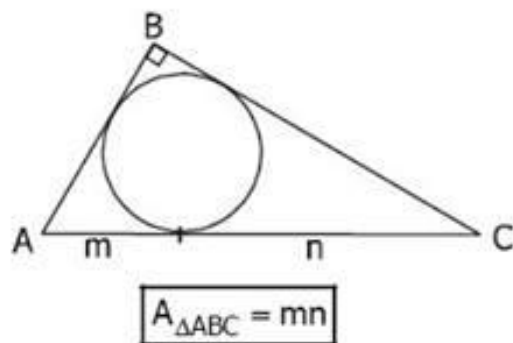
$$x^2 = a \cdot b$$



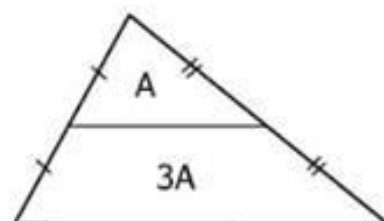
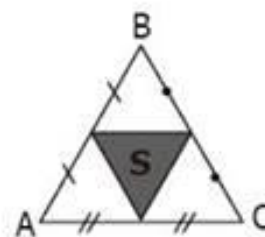
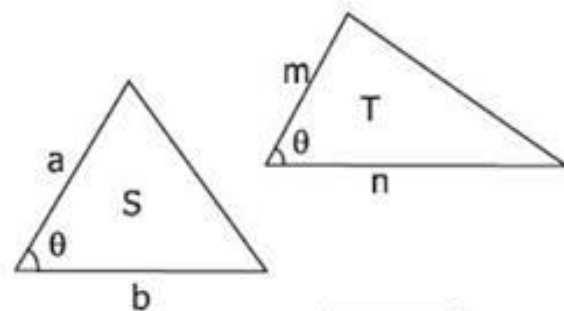
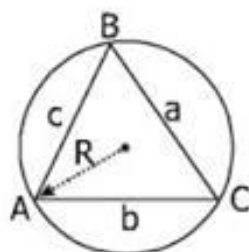
$$\sqrt[3]{a^2} + \sqrt[3]{b^2} = \sqrt[3]{c^2}$$

$$h^3 = abc$$

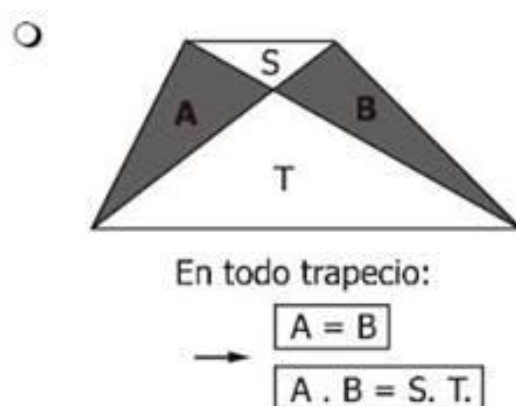
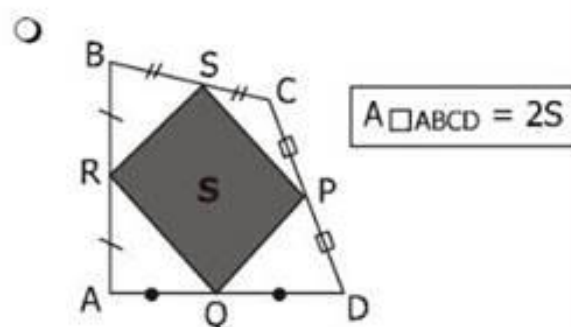
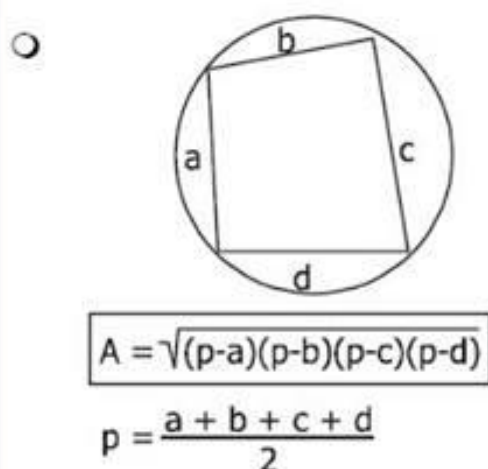
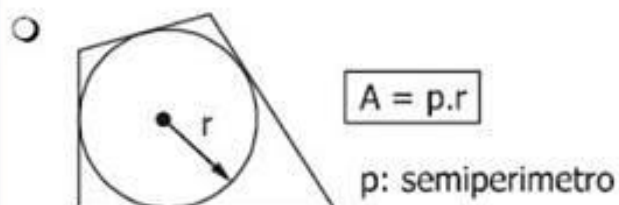
## ÁREAS TRIANGULARES



$$p = \frac{a+b+c}{2}$$

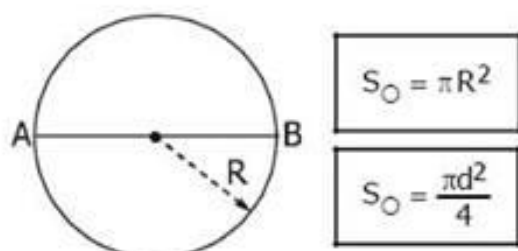


## ÁREAS CUADRANGULARES

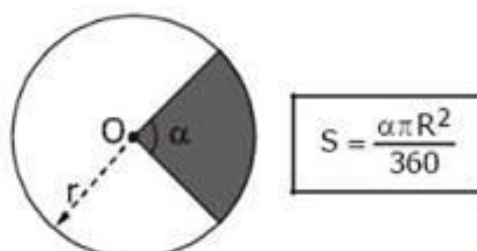


## ÁREA CIRCULAR

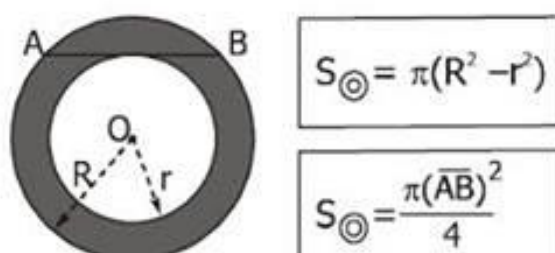
### • Círculo:



### • Sector Circular



### • Corona Circular



## GEOMETRÍA DEL ESPACIO Y POLIEDROS REGULARES

### Teorema de Euler

$$C + V = A + 2$$

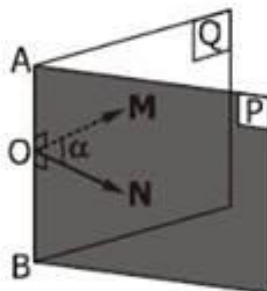
Donde:

C: N.º caras

V: N.º vértices

A: N.º aristas

### Ángulo diedro



Notación:

diedro  $\overline{AB}$  ( $d-\overline{AB}$ )

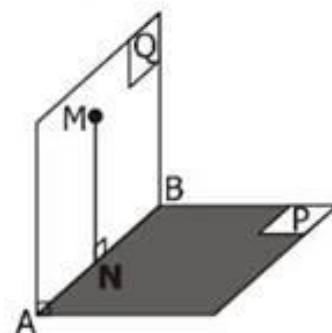
Elementos:

\* Arista:  $\overline{AB}$  \*Caras: P y Q

\*  $\angle$  Plano:  $\angle MON$

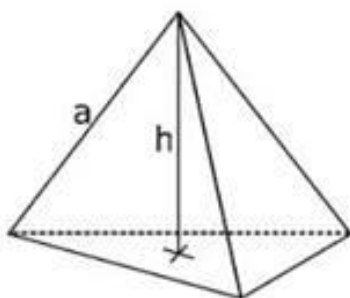
$$m(\text{diedro } \overline{AB}) = m\angle MON = \alpha$$

### Diedro recto o planos perpendiculares



$$\text{Si: } \begin{cases} \square P \perp \square Q \\ \overline{MN} \perp AB \Rightarrow \overline{MN} \perp \square P \\ \overline{MN} \subset \square Q \end{cases}$$

### Tetraedro regular

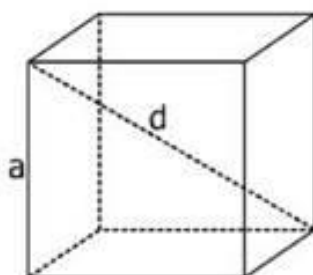


$$C = 4; V = 4; A = 6$$

$$A_T = a^2\sqrt{3}; V = \frac{a^3}{12}\sqrt{2}$$

$$h = \frac{a\sqrt{6}}{3}$$

### Hexaedro regular

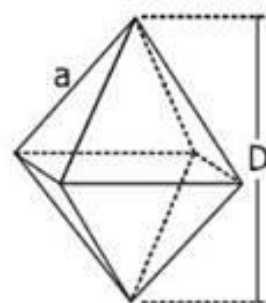


$$C = 6; V = 8; A = 12$$

$$A_T = 6a^2; V = a^3$$

$$d = a\sqrt{3}$$

### Octaedro regular



$$C = 8; V = 6; A = 12$$

$$A_T = 2a^2\sqrt{3}; V = \frac{a^3\sqrt{2}}{3}$$

$$D = a\sqrt{2}$$



## PRISMA Y CILINDRO

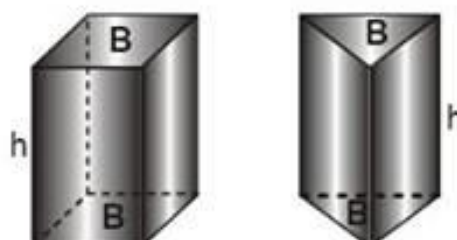
Cilindro recto



### Fórmulas

1.  $V = \pi r^2 g$
2.  $A_L = 2\pi r g$
3.  $A_T = 2\pi r(g + r)$

Prisma recto

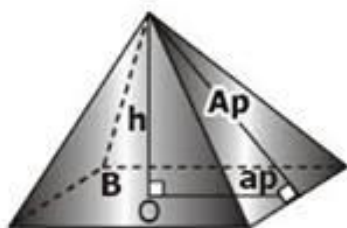


### Fórmulas

1.  $V = B \cdot h$
2.  $A_L = \left( \begin{array}{c} \text{Perímetro de} \\ \text{la base} \end{array} \right) \cdot h$
3.  $A_T = A_L + 2B$

## PIRÁMIDE - CONO

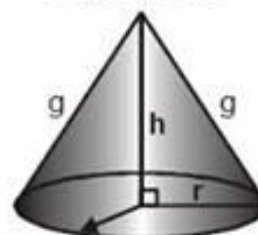
Pirámide regular



### Fórmulas

1.  $V = \frac{Bh}{3}$
2.  $A_L = \left( \begin{array}{c} \text{semiperímetro} \\ \text{de la base} \end{array} \right) \cdot Ap$
3.  $A_T = A_L + B$   $Ap^2 = h^2 + ap^2$

Cono recto

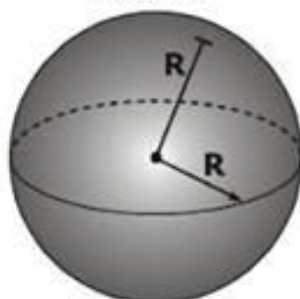


### Fórmulas

1.  $V = \frac{\pi r^2 h}{3}$
2.  $A_L = \pi r g$
3.  $A_T = \pi r(g + r)$   $g^2 = h^2 + r^2$

## ESFERAS Y TEOREMA DE PAPPUS GULDIN

**Esfera**

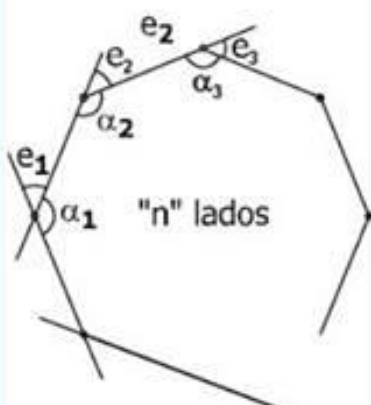


Fórmulas:

$$1. V = \frac{4}{3} \pi R^3$$

$$2. A_T = 4\pi R^2$$

## POLÍGONOS Y POLIEDROS REGULARES



**Fórmulas**

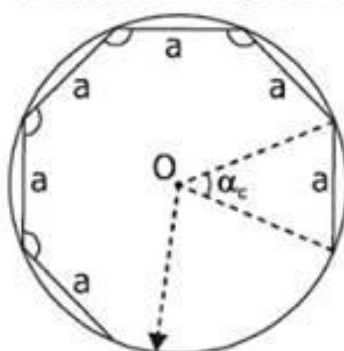
$$Sm_{\alpha_i} = 180^\circ(n - 2)$$

$$Sm_{\alpha_e} = 360^\circ$$

Nº Diagonales:  $N_D$

$$N_D = \frac{n(n-3)}{2}$$

**Polígonos regulares**



n: número de lados

**Fórmulas**

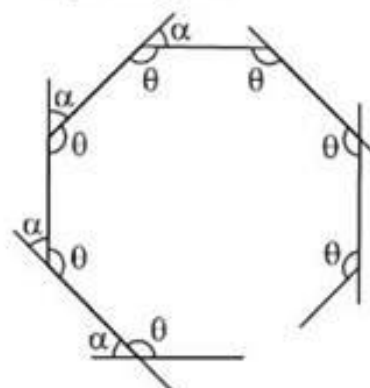
$\alpha_c$ : medida del ángulo central

$$\alpha_c = \frac{360^\circ}{n}$$

$$m_{\alpha_i} = \frac{180^\circ(n-2)}{n}$$

$$m_{\alpha_e} = \frac{360^\circ}{n}$$

**En todo polígono equiángulo:**



**Fórmulas**

$$\theta = 180^\circ \frac{(n-2)}{n}$$

$$\alpha = \frac{360^\circ}{n}$$

**VISITE NUESTRA PÁGINA EN FACEBOOK!!**

<https://web.facebook.com/Preparandote-Para-La-U-1785561948332382>



**Gracias por seguirnos; seguiremos trabajando para Usted.**