$$\int_{\mathbf{Y}} F'(z) dz = \int_{\alpha}^{\beta} F'(\mathbf{Y}(t)) \cdot \mathbf{Y}'(t) dt$$