

$$S = \sqrt{\frac{d_1^2 + d_2^2 + \dots + d_n^2}{n-1}} \quad \text{If } n \leq 20$$

sample std. deviation

ii) variance (σ^2)

Defined as sq. of std. deviation
 $\therefore \sigma^2 = S^2$

Expressed as:

$$\sigma^2 = (S)^2 = (S)^2$$

iii) Gaussian Probability curve

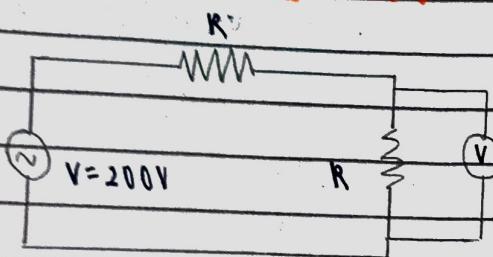


Fig (i)

Voltage Reading (V)

99.7

1

99.8

3

99.9

12

100.0

19

100.1

10

100.2

4

100.3

1

No. of observations

Table (i)

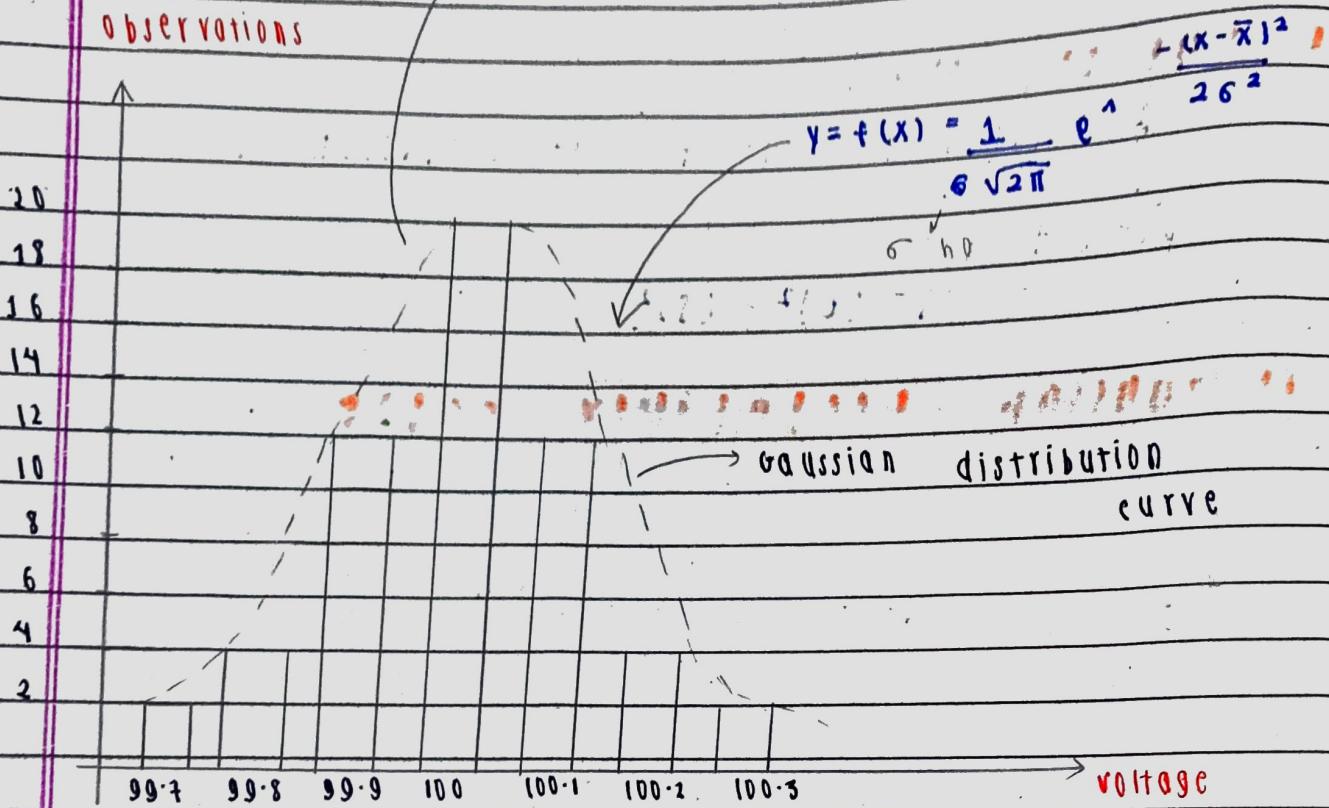
Observations

Fig.(ii)

Consider an eg. where v drop across the resistor is taken using voltmeters & following reading were obtained

Table (i) shows 50 v readings that were taken at a small time interval & recorded to the nearest 0.1 v voltage range.

The nominal (true) value of measured voltage was 100V. The result of this series of measurement can be presented graphically in the form of histogram.



bar graph

In which the no. of observations is plotted against each observed voltage reading. This bell shaped curve is known as Gaussian probability curve.



It's eqn is given by:

$$y = f(x) = \frac{1}{\sigma \sqrt{2\pi}} e^{-\frac{(x-\mu)^2}{2\sigma^2}}$$

mean.



std. deviation

exp power

no. of observations

Probable Error

occurrence

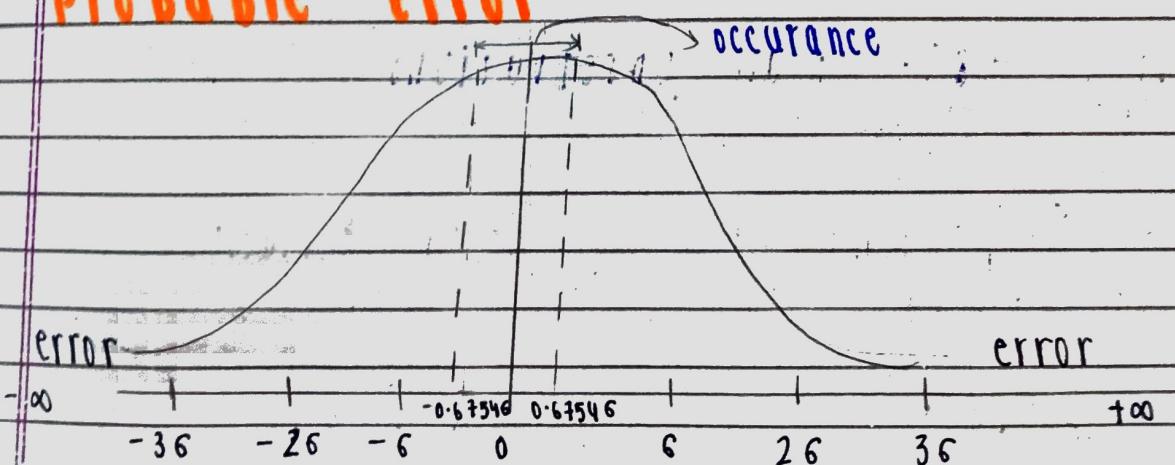


Fig (i)

Deviation	Fraction of area in Gaussian prob. curve
± 0.67546	0.5
± 6	0.6828
± 2.6	0.6946
± 3.6	0.9972

Table (i)

Area under Gaussian prob. curve in fig (i) betⁿ $-\infty$ to $+\infty$ represents entire no. of observations

The area under curve betⁿ limit -6 to 6 rep. observations that differs from the mean by no more than 6

Integration of area under the curve within the limit ± 6 gives total no. of observation within that limit

Approx. 68% of all observations lie betⁿ the limit ± 6 from the mean.

The corresponding value of other deviations are given in table (i).

- The probable error is denoted by 'r'

\pm is given by:

$$r = \pm 0.67546$$



This value is probable in the sense that there is 50-50 chances that the new value will lie betn $-r \pm r$

some formula

i) probable error of one reading (r)

$$r = \pm 0.67546 \quad \text{for } n > 20$$

$$= \pm 0.67548 \quad \text{for } n < 20$$

ii) probable error of mean (r_m)

$$r_m = \frac{r}{\sqrt{n-1}} \quad \text{for } n > 20$$

$$= \frac{r}{\sqrt{n}} \quad \text{for } n \leq 20$$

Numerical

1. Following 10 observation were recorded when measuring voltage

41.7, 42, 41.8, 42, 42.1, 41.0, 42.5, 41.9, 42, 41.0.

- FIND:
- i) mean
 - ii) std deviation
 - iii) prob error of ~~one~~ reading
 - iv) prob error of mean
 - v) range

i) MEAN

$$\bar{x} = \frac{41.7 + 42 + 41.8 + 42 + 42.1 + 41.9 + 42.5 + 41.9 + 42 + 41.9}{10}$$

$$= 41.98$$

ii) std. deviation

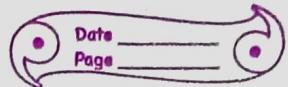
x	d	d^2
1. 41.7	-0.28	0.0784
2. 42	0.02	0.0004
3. 41.8	-0.18	0.0324
4. 42	0.01	0.0001
5. 42.1	0.12	0.0144
6. 41.9	-0.08	0.0064
7. 42.5	0.52	0.2704
8. 41.9	-0.08	0.0064
9. 42	0.02	0.0004
10. 41.9	-0.08	0.0064

FDR $n < 20$

std. deviation

$$s = \sqrt{\frac{\sum (x - \bar{x})^2}{n-1}}$$

$$= \sqrt{\frac{0.4196}{9}}$$



$$= 0.2159$$

iii) Prob error of one reading (for $n < 20$)

$$r = \pm 0.6754 s$$

$$= \pm 0.6754 * 0.2159$$

$$= \pm 0.1458$$

iv) Prob error of mean (for $n < 20$)

$$r_m = \frac{r}{\sqrt{n-1}}$$

$$= \pm 0.1458$$

$$\sqrt{10-1}$$

$$= \pm 0.0486$$

v) Range: $41.7 - 42.5$



lowest reading

highest reading

static & dynamic characteristics of measurement system

When an input is applied to a system or instrument, the response doesn't take its max. or const. value immediately.

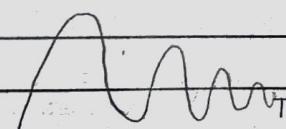
There will be some delay in time known as transient / dynamic period.

Behaviour shown by system during this period is known as transient / dynamic characteristics.

After the transient period the response takes its const. value. This time period is steady state period.

Behaviour shown by system during this period is static characteristics.

Response



transient / dynamic
period

steady / static
period

time

Fig: Response of system

DYNAMIC CHARACTERISTICS

① SPEED OF RESPONSE

Rapidity in which an instrument responds to change of quantity under measurement.

② RESPONSE TIME

Time reqd by the system/instrument to settle its final steady state position, after the application of input.

③ MEASURING LAG

Delay in response of an instrument to a change in the measured quantity.

STATIC CHARACTERISTICS

① ACCURACY

Specifies the diff. b/w measured value & the true value of quantity.

It is the closeness w/ which an instrument reading approaches to the true value of quantity.

Deviation from the true value is the indication of how accurately a measurement has been done.

Concept of accuracy usually refer to the full scale reading.

(ii)

Precision / Repeatability

specifies the repetition of a set of reading each made independently w. the same instrument.

It is used in measurement to describe the consistency of results.

↑ precision means tight cluster of repeated results while

scattering ↓ precision indicates a broad of results.

- To differentiate betw accuracy & precision consider an instrument that has defect in its operation.

The instrument may give result that is highly repeatable from measurement to measurement yet

far from the t.v.

The data obtained from this instrument would be

- ↑ (highly) precised

but,

- inaccurate.

∴ Precision does not guarantee accuracy.

Although,

accuracy requires precision.