

# BiiPS software: statistical learning in finance

ALEA project-team, Inria Bordeaux - Sud-Ouest

# **Context**

The last two decades have seen a rapid development of increasingly realistic and sophisticated stochastic models and methods for pricing, hedging and risk management in rapidly growing markets.



## **Problem**

Modern finance is becoming increasingly technical, requiring the use of advanced stochastic algorithms.



# Advanced Particle and Sequential Monte Carlo Algorithms



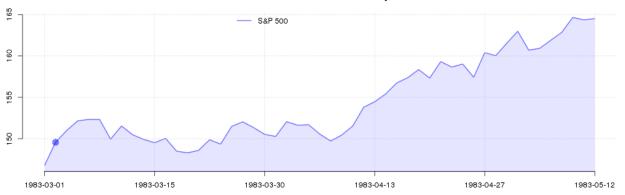
# Our expertise

As a pioneer in the field of **new adaptive and interacting particle algorithm** and **SMC methods**, the
ALEA project-team is working on **a great variety of numerical applications**.

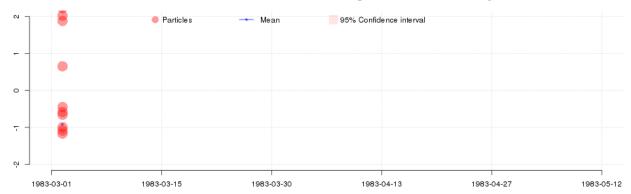


# Particle algorithms illustrated

#### Standard and Poor's 500 stock price index



#### Particle filter estimate of the log-stochastic volatility





# **Numerical applications**

- Parameter estimation
- Calibration of valuation models
- Derivative pricing
- Sensitivity analysis
- Hedging in incomplete markets
- Credit risk
- Risk and uncertainty quantification
- Portfolio optimization
- Etc.

#### Team members implied in financial mathematics:

P. Del Moral, P. Hu, A. Richou, F. Caron, A. Todeschini, C. Li (Master X2009).



# The software BiiPS



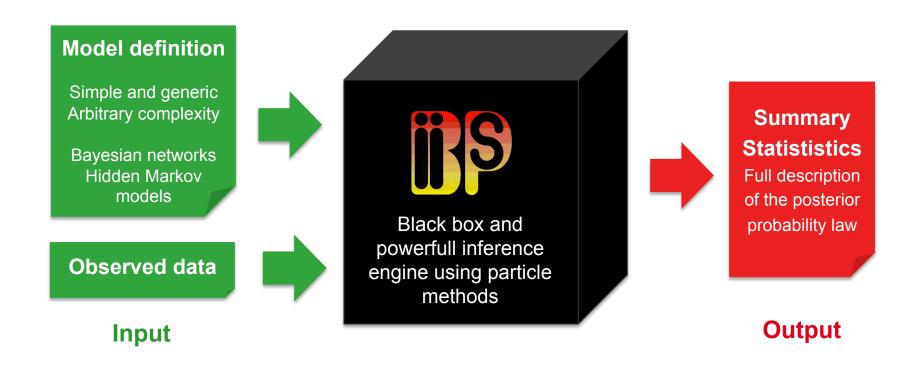
# A new software for Bayesian inference using interacting particle systems



Design and development: A. Todeschini

Free and open source software soon available for Windows, Linux and Mac OS at <a href="http://biips.gforge.inria.fr">http://biips.gforge.inria.fr</a>

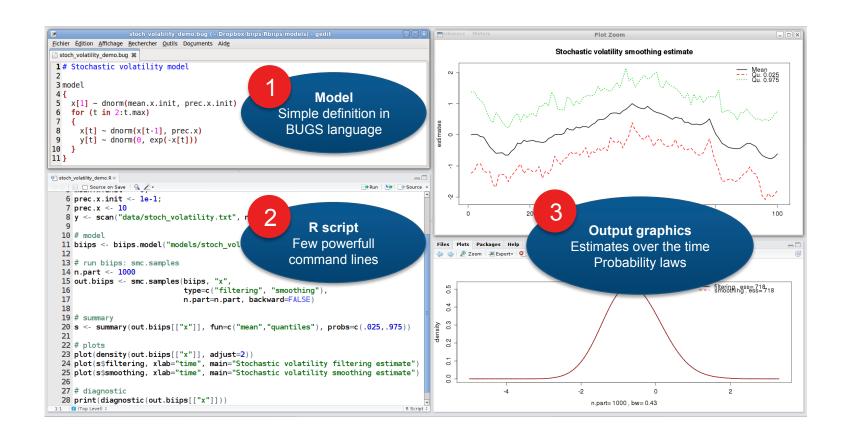




#### **Financial models calibration**

Stochastic volatility / Partial observations





Future works: Matlab interface, Parallelization and more...



# 3

# More finance applications



# **Pricing financial products**

European barrier options, Asian options, American options,...

#### Mathematical tools:

- Optimal control
- Particle approximation of Snell envelope

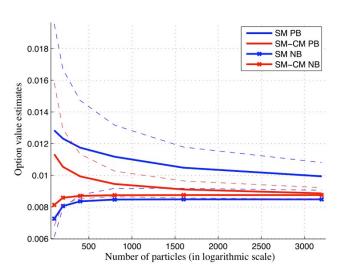
#### References:

- R. Carmona, P. Del Moral, P. Hu and N. Oudjane (eds.), Numerical Methods in Finance, to appear, Springer-Verlag.
- R. Carmona, P. Del Moral, P. Hu and N. Oudjane, "An introduction to particle methods in finance" [43 pages], to appear in Numerical Methods in Finance.
- P. Del Moral, P. Hu and N. Oudjane, "Snell Envelope with small probability criteria" [22 pages], preprint inria-00507794 [submitted], 2010.
- P. Del Moral, P. Hu, N. Oudjane and B. R´emillard, "On the Robustness of the Snell Envelope" [40 pages], SIAM J. Finan. Math., Vol. 2, pp. 587–626, 2011.

#### Collaboration:

EDF R&D

# Pricing efficiency improved by using advanced particle estimation



Monte Carlo estimates vs. advanced particle estimates

Pavoff	K	d=1	d=2	d=3	d=4	d = 5
Geometric	0.95	1 (1%)	1 (3%)	1 (6%)	1 (9%)	1 (10%)
Put	0.85	5 (2%)	8 (6%)	6 (11%)	4 (14%)	3 (14%)
	0.75	18 (6%)	28 (11%)	18 (17%)	16 (18%)	11 (16%)
Arithmetic	0.95	1 (1%)	3 (2%)	3 (7%)	4 (13%)	5 (18%)
Put	0.85	5 (2%)	13 (6%)	24 (19%)	56 (24%)	100 (20%)
	0.75	18 (6%)	71 (15%)	363 (14%)	866 (16%)	- (-)

Ratios of estimated MC results vs. advanced particle results



# **Hedging**

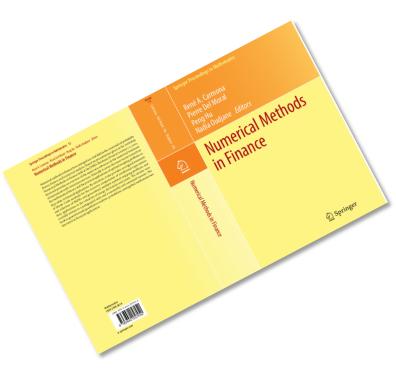
#### Greeks calculation

#### Mathematical tools:

- Sequential Monte Carlo particle methods
- Particle gradient models

#### References:

- R. Carmona, P. Del Moral, P. Hu and N. Oudjane (eds.),
   Numerical Methods in Finance, to appear, Springer-Verlag.
- R. Carmona, P. Del Moral, P. Hu and N. Oudjane, "An introduction to particle methods in finance" [43 pages], to appear in Numerical Methods in Finance.
- P. Del Moral, P. Hu and L. Wu, On the concentration properties of Interacting particle processes, Foundations and Trends in Machine Learning, vol. 3, nos. 3–4, pp. 225–389, 2012.





### **Credit Risk**

### Default Probability

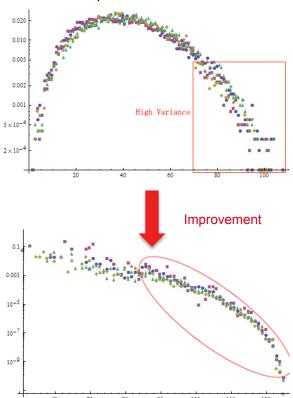
#### Mathematical tools:

- Rare event simulation
- Particle default tree models

#### References:

- R. Carmona, P. Del Moral, P. Hu and N. Oudjane, "An introduction to particle methods in finance" [43 pages], to appear in Numerical Methods in Finance.
- R. Carmona and S. Crépey. Importance Sampling and Interacting Particle Systems for the Estimation of Markovian Credit Portfolios Loss Distribution. International Journal of Theoretical and Applied Finance, vol. 13, No. 4 (2010) 577 – 602.
- R. Carmona, J.-P. Fouque and D. Vestal. Interacting Particle Systems for the Computation of Rare Credit Portfolio Losses. Finance and Stochastics, vol. 13, no. 4, 2009 pp. 613-633 (2009).

### Default distribution (log-scale) for a portfolio of 125 stocks



Rare credit portfolio losses are better captured with advanced particle estimation



# **Portfolio optimization**

Maximizing expected utility function of the terminal wealth



#### Mathematical tools:

 Abstract solutions with backward SDEs

#### References:

- Y. Hu, P. Imkeller, M. Müller, "Utility maximization in incomplets markets." Ann. Appl. Probab., 15(3): 1691-1712, 2005.
- Y. Hu, P. Imkeller, M. Müller, "Partial equilibrium and market completion." Int. J. Theor. Appl. Finance, 8(4): 483-508, 2005.
- U. Horst, Y. Hu, P. Imkeller, A. Réveillac, J. Zhang, "Forward-backward systems for expected utility maximization", Preprint, 2011.

 Numerical simulation: time discretization of the solution of quadratic backward SDEs

#### References:

- A. Richou, "Numerical simulation of BSDEs with drivers of quadratic growth." Ann. Appl. Probab., 21 (5):1933-1964.
- A. Richou, "Markovian quadratic and superquadratic BSDEs with an unbounded terminal condition."
   Preprint, 2012.
- A. Richou, "Etude théorique et numérique des équations différentielles stochastiques rétrogrades", PhD thesis, Univ. Rennes 1, 2010.



### **Collaborations**

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Imperial College, D. Crisan

Columbia University, J. Blanchet, Ph. Protter

Ecole Polytechnique, E. Gobet, N. Touzi

EDF R&D, N. Oudjane

Conference information

Workshop on Sequential Monte Carlo methods and Efficient simulation in Finance.

ALEA - CMAP. Ecole Polytechnique, Paris October 8-12th, 2012

