



Rm Palaniappan, *Alien Planet-X-9*  
Viscosity, pencil colour and ink on  
handmade paper

# Are modern ML models like scientific instruments?

Anand D. Sarwate (Rutgers University)  
28 July 2025

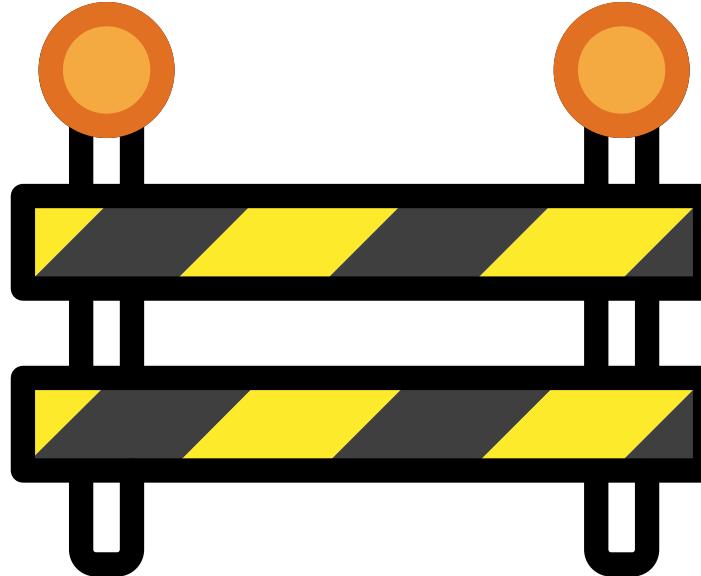
IEEE ITSOC Distinguished Lecture  
2025 Guangzhou, Hong Kong and Taipei Joint Workshop  
on Artificial Intelligence, Communications and Information Theory (AICIT 2025)  
Guangzhou, China

# **Some pre-apologies**

**I am still trying to figure out how to talk about this work**

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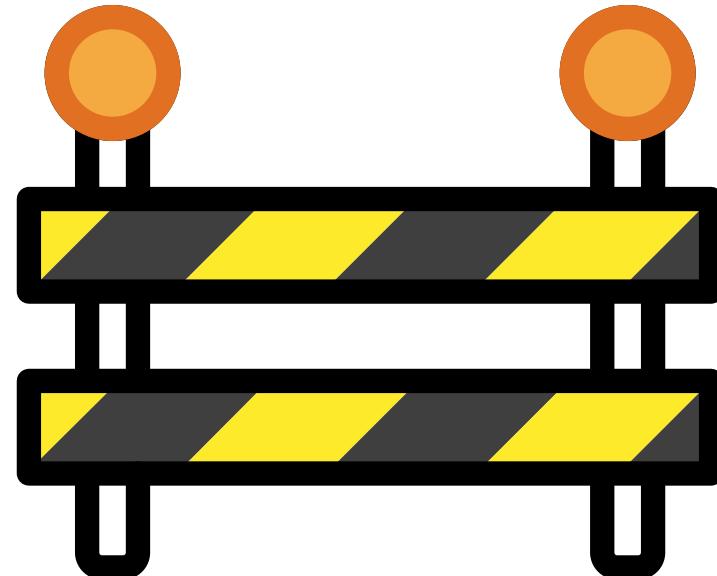
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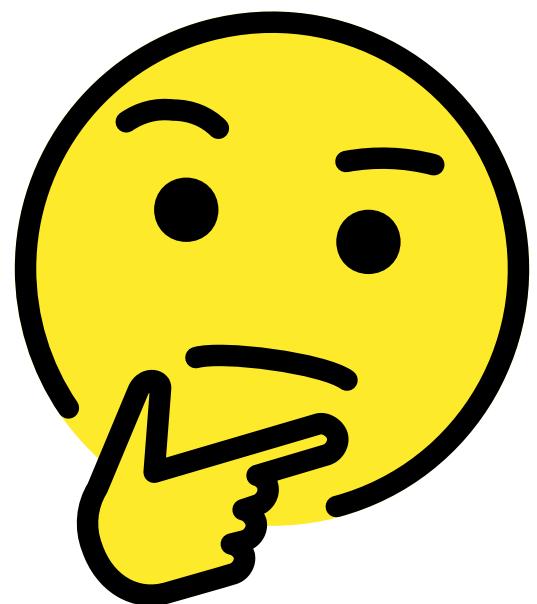
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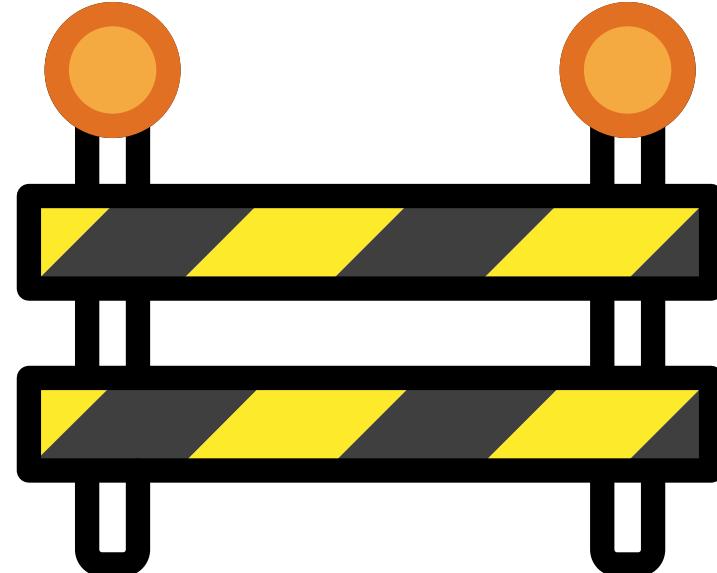
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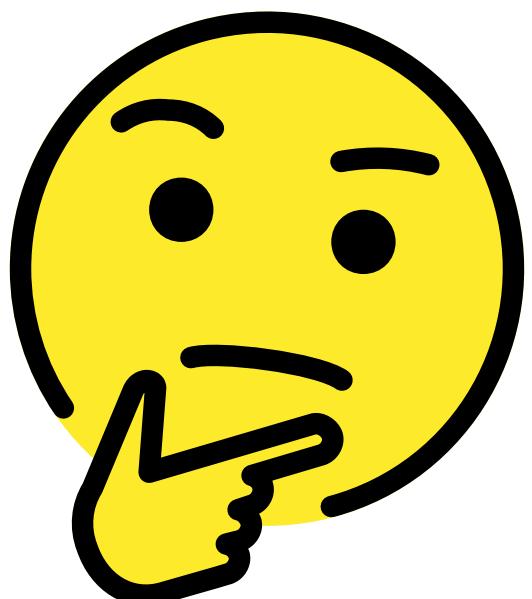
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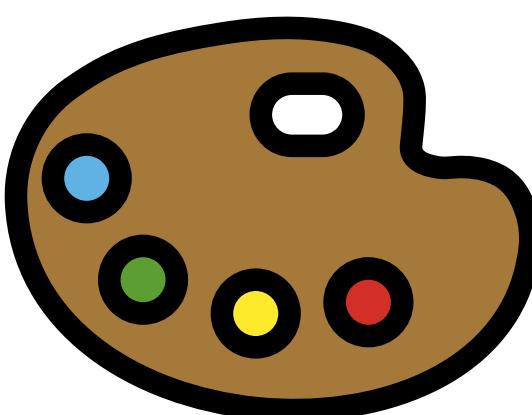
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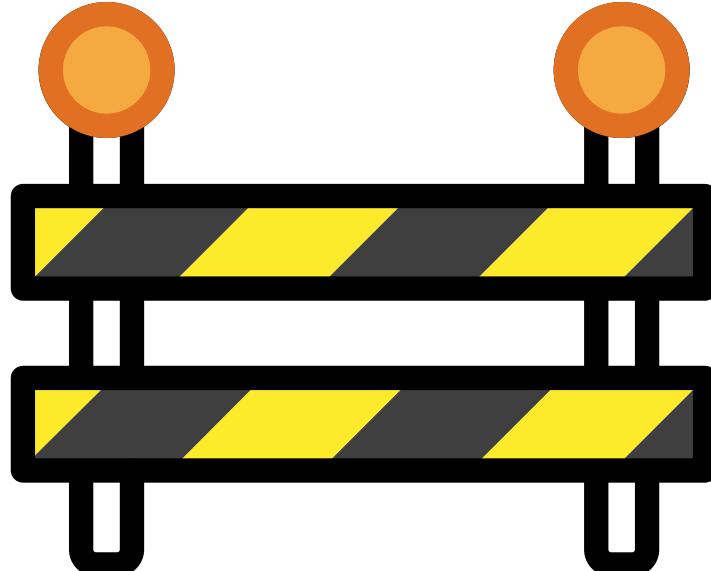
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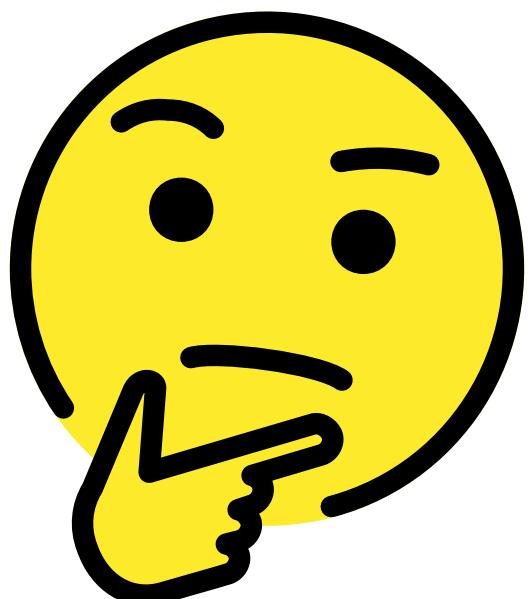
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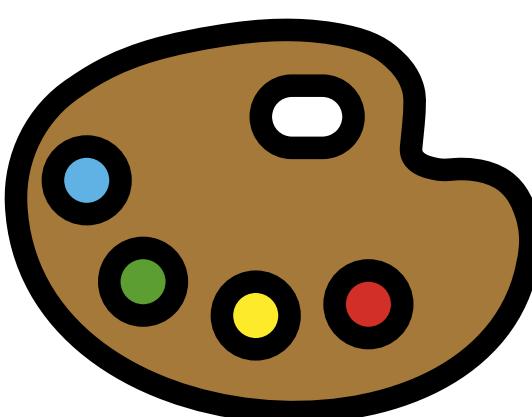
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There are a lot of metaphors and analogies (some science-fictional) which are **not always precise**.

Real life is a bit messy...

# Thanks to my collaborators/coauthors!

Most of this is their work, obviously

Sinjini Banerjee (Rutgers)

Sutenay Choudhury (PNNL)

Xin Li (Rutgers)

Reilly Cannon (PNNL)

Ioana Dumitriu (UC San Diego)

Tim Marrinan (PNNL)

Tony Chiang (ARPA-H)

Andrew Engel (Ohio State)

Max Vargas (PNNL)

Sutenay Choudhury (PNNL)

Zhichao Wang (UC Berkeley)

## Papers:

[JSTSP] Banerjee et al. <https://doi.org/10.1109/JSTSP.2025.3583140>

[NeurIPS 2023] Wang et al. <https://openreview.net/forum?id=gpqBGyKeKH>

[ICLR 2024] Engel et al. <https://openreview.net/forum?id=yKksu38BpM>

[ArXiV] Vargas et al. <https://arxiv.org/abs/2408.10437>

# What does the title mean?

What do ML models have to do with science?

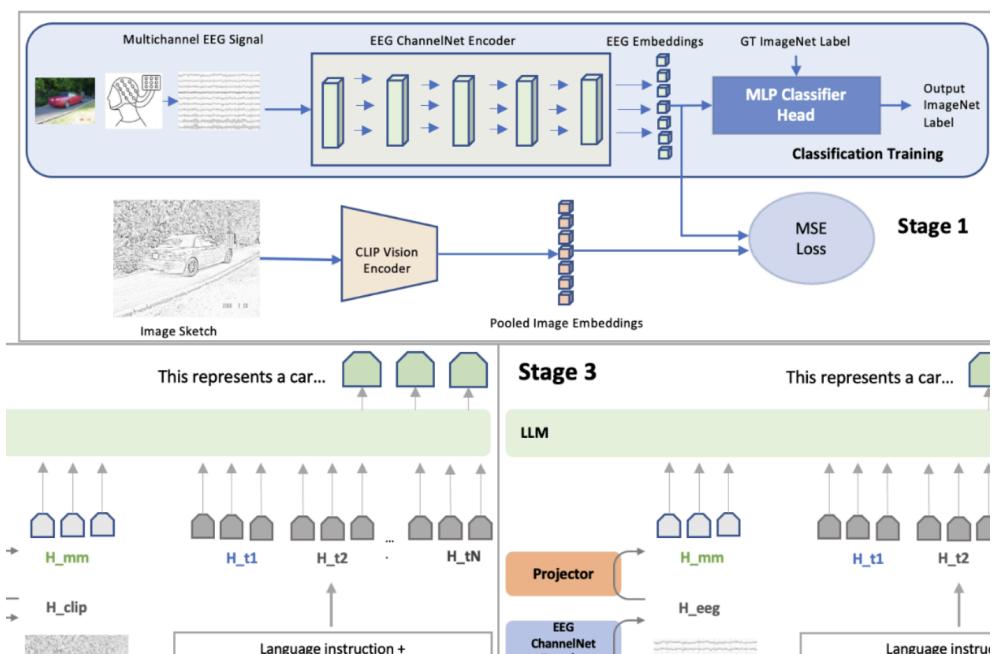
Source: Wikipedia



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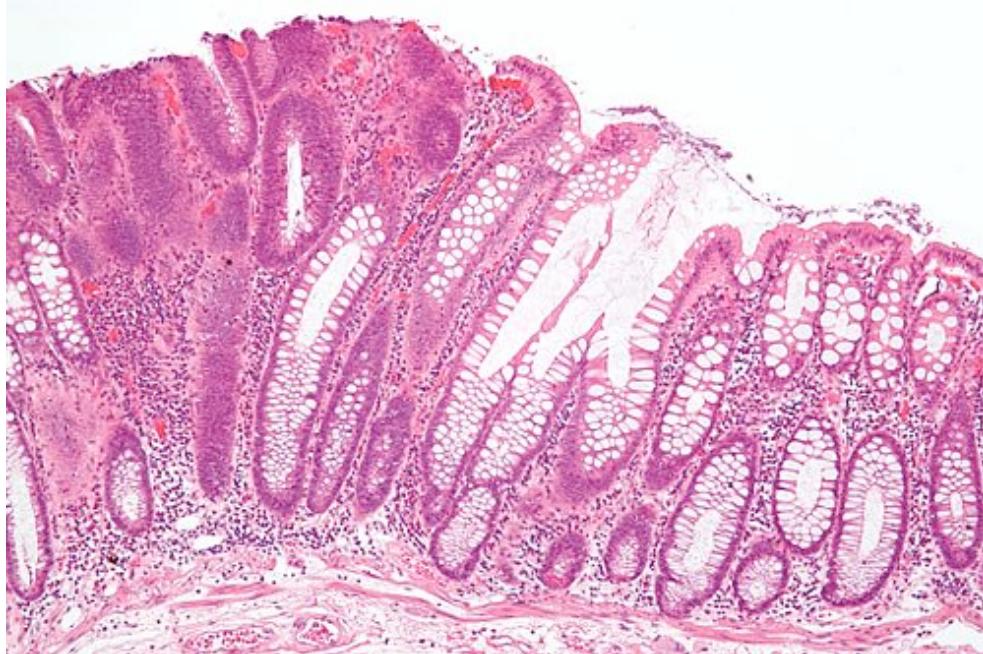
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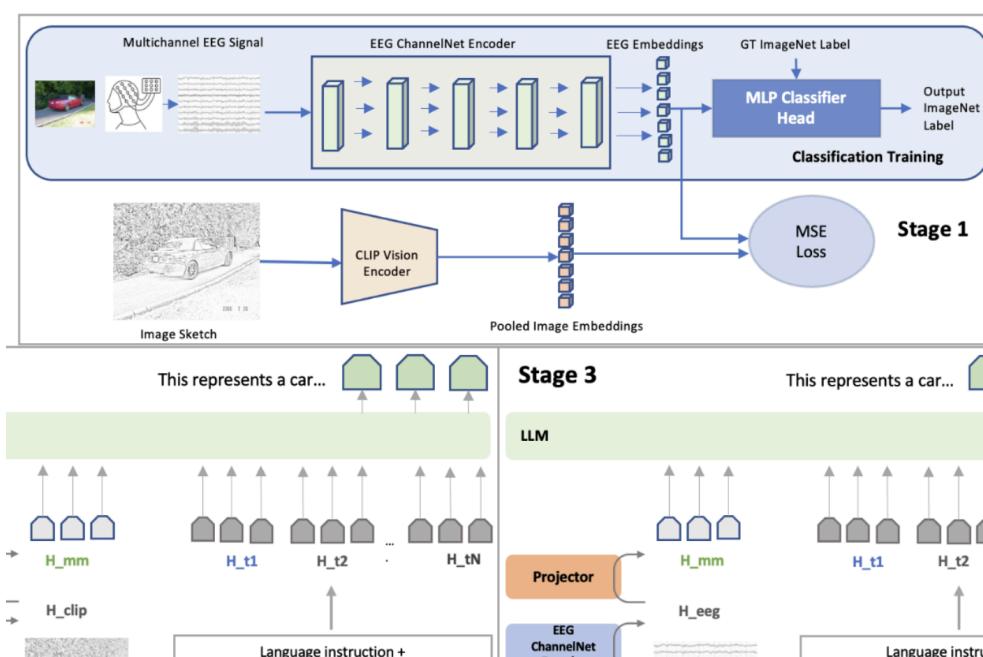
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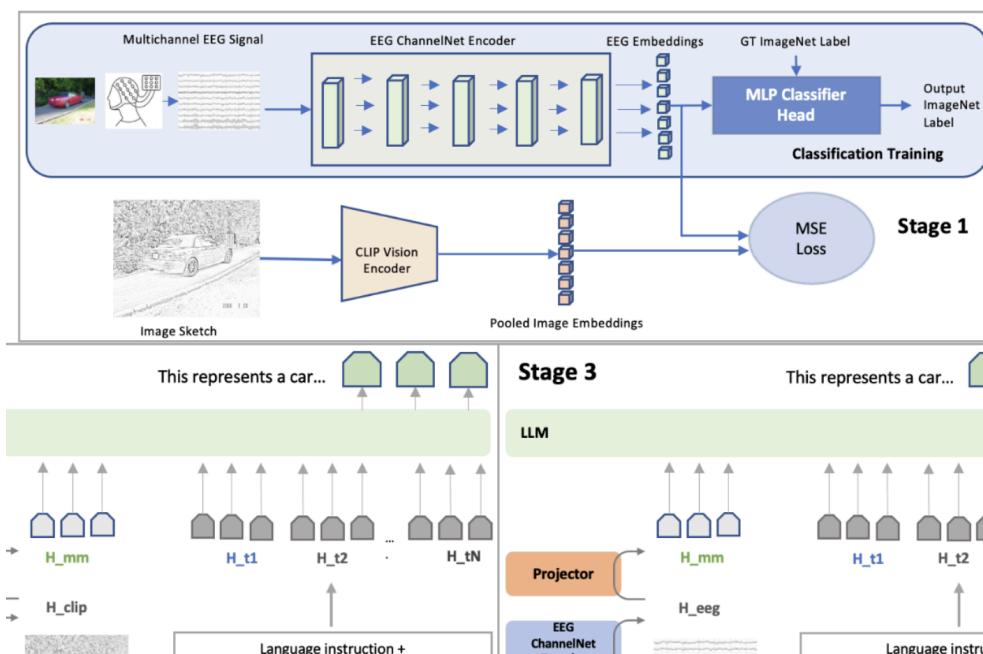
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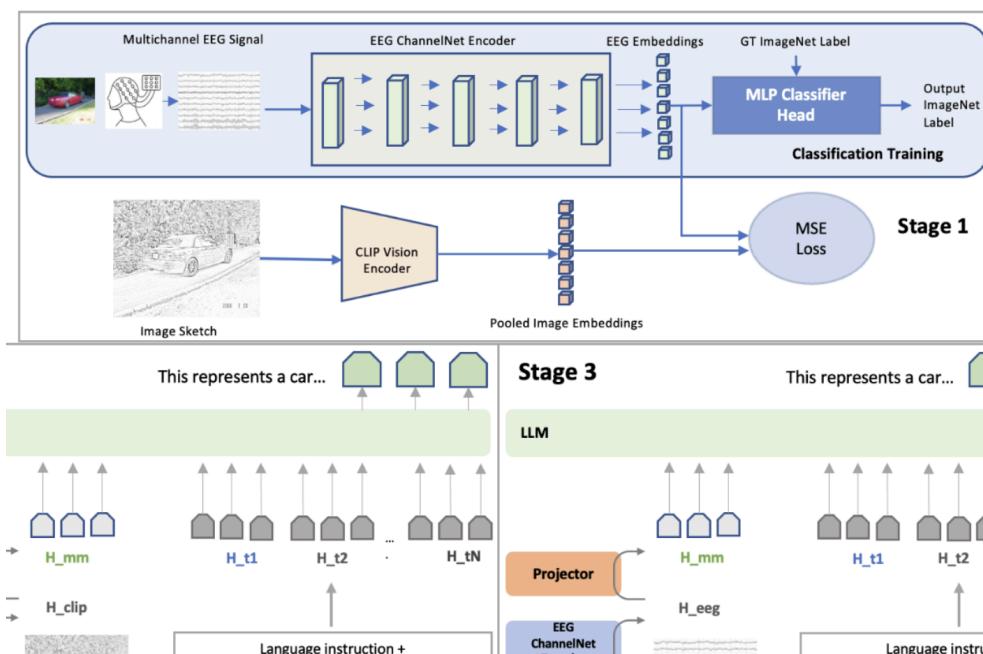
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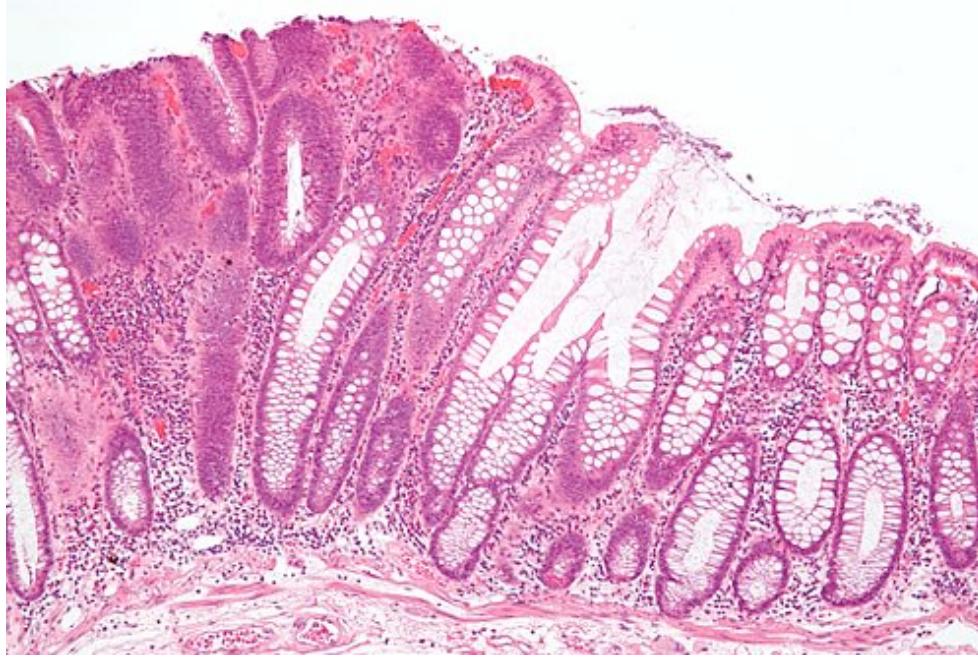
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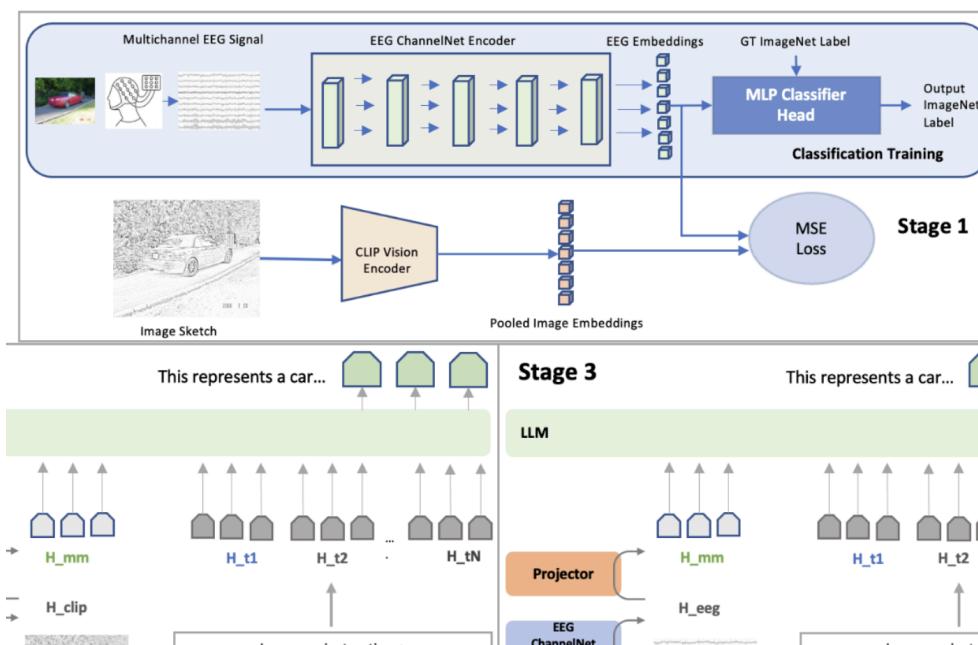
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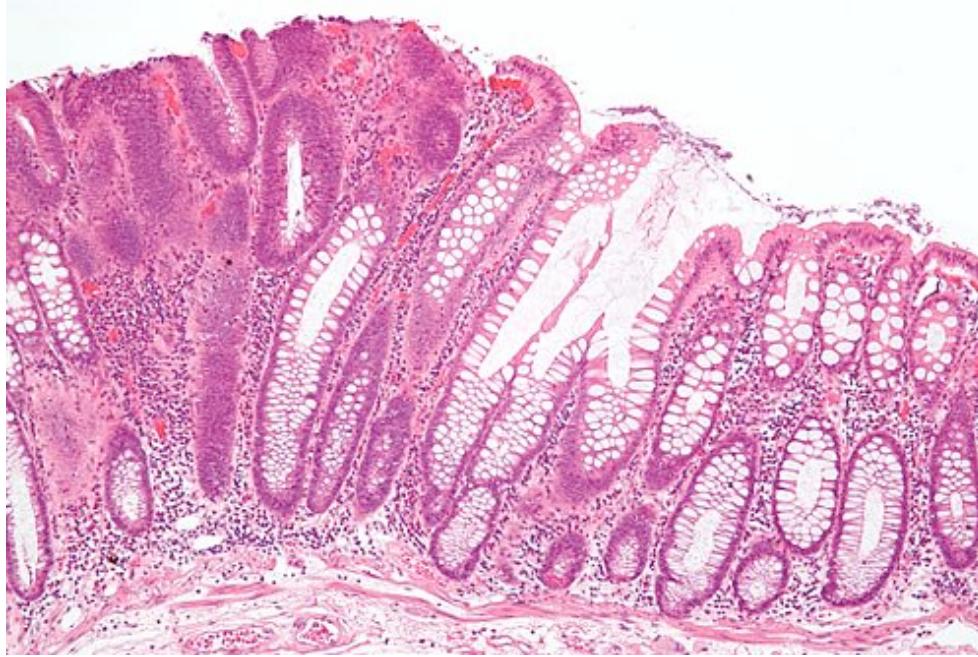
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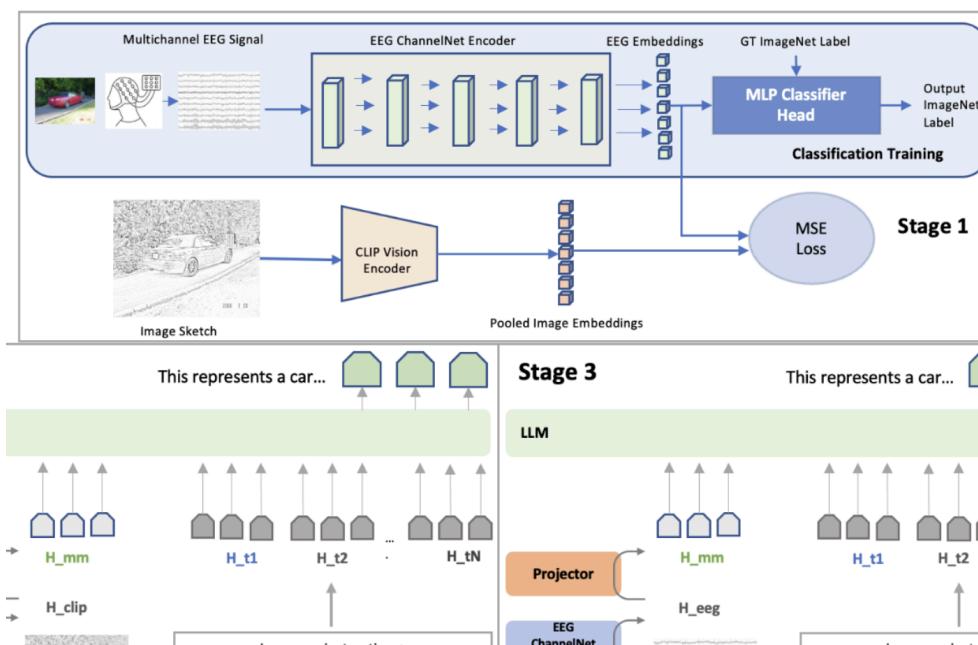
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- Many more...

# **Is “AI for science” the new “Bandwagon”?**

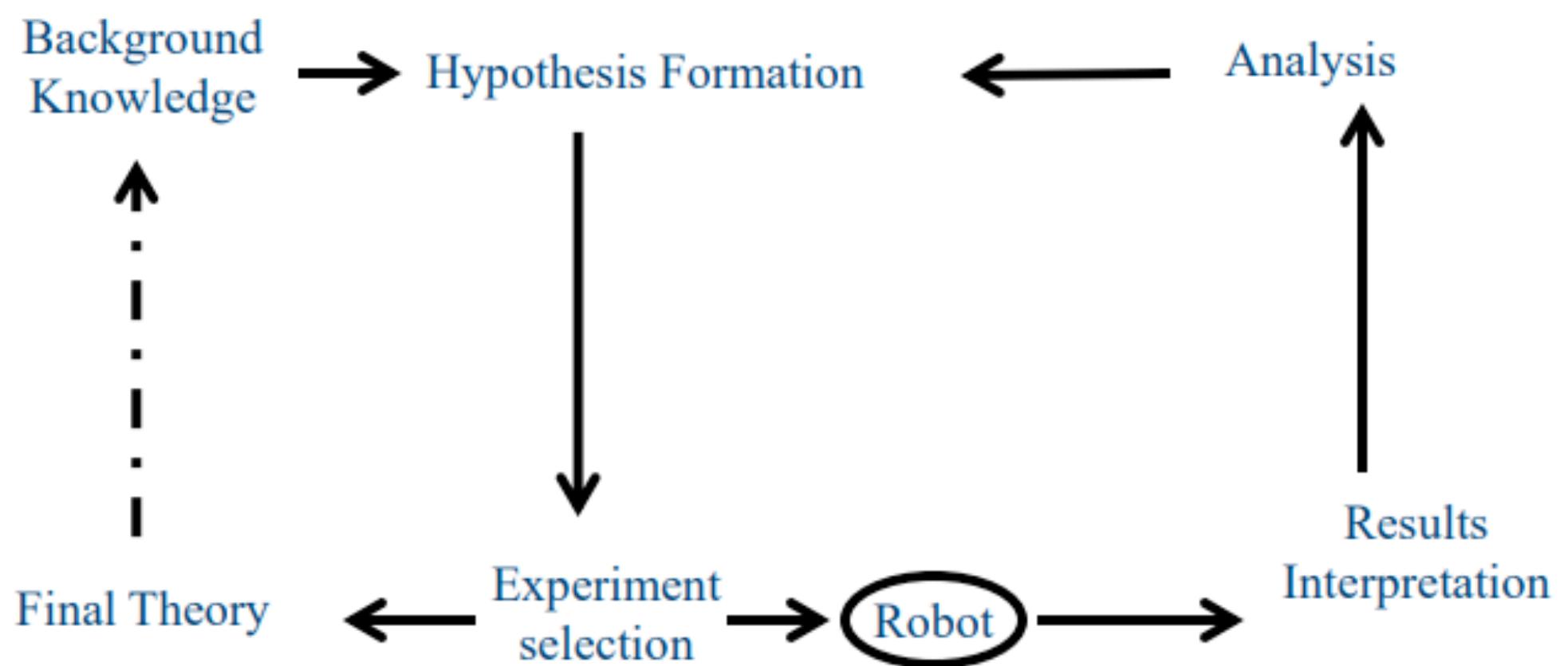
## **Some gap between hype and reality**

# Is “AI for science” the new “Bandwagon”?

## Some gap between hype and reality

### The Concept of a Robot Scientist

Computer system capable of originating its own experiments, physically executing them, interpreting the results, and then repeating the cycle.



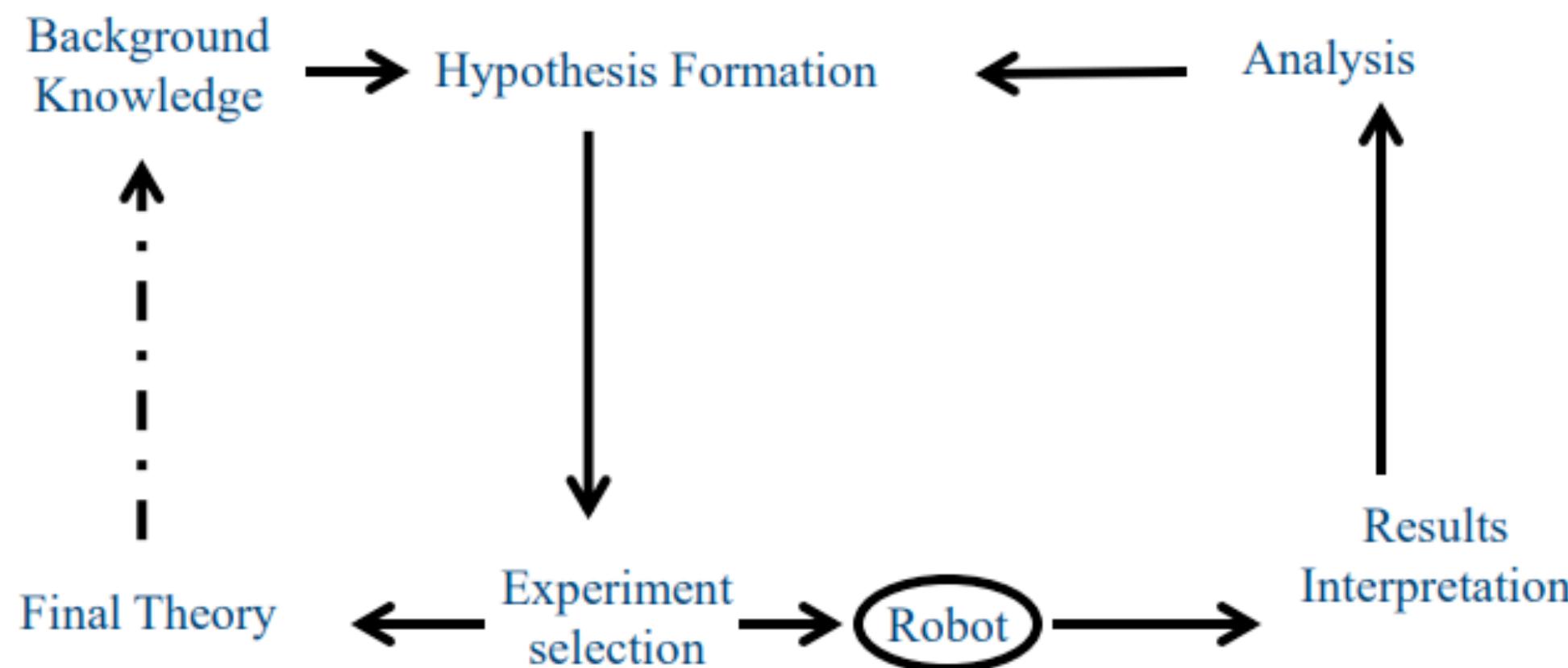
<https://futuretech.mit.edu/news/ai-and-the-future-of-scientific-discovery>

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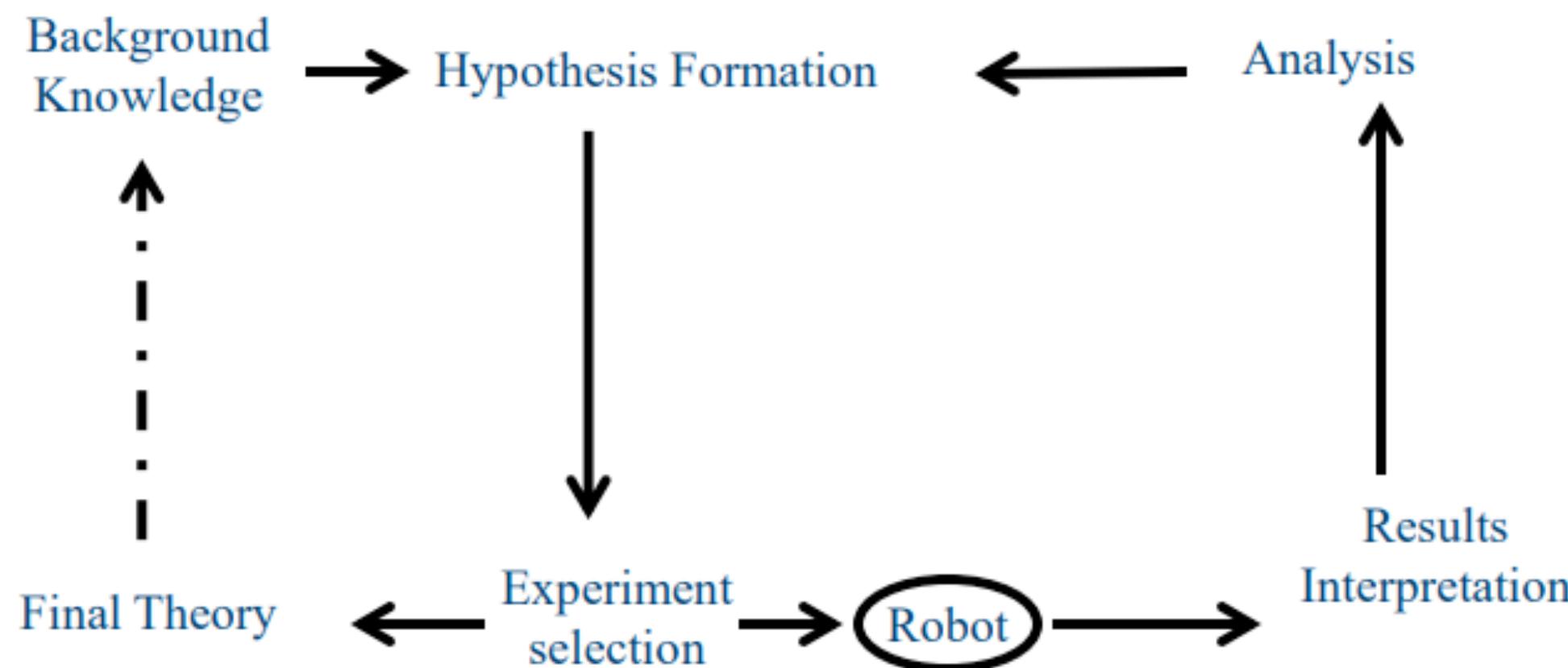
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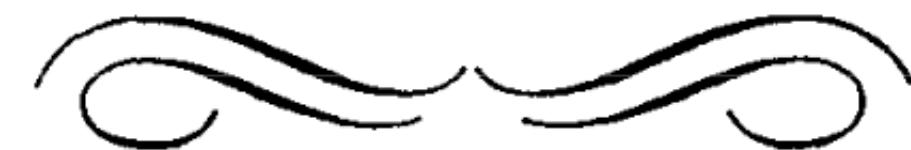
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NY Times  
14 May 2025

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IRE TRANSACTIONS—INFORMATION THEORY



## The Bandwagon

CLAUDE E. SHANNON

Shannon, 1956

# **What about information/signal processing?**

**Some perspective from more solid ground**

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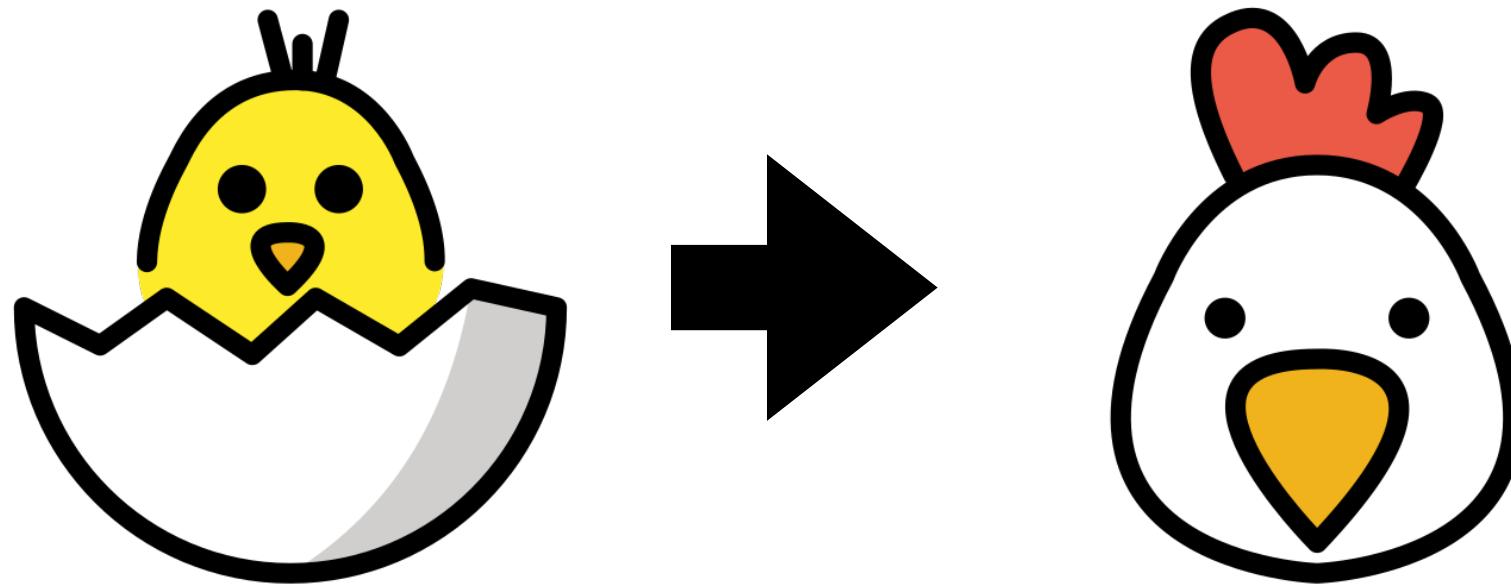
Some perspective from more solid ground

*At the end of the day “artificial neural nets” are just a bunch of computational signal processing primitives chained together and jointly optimized with stochastic gradient methods.*

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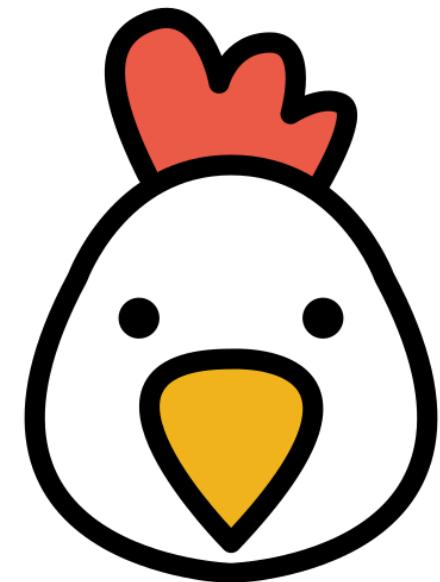
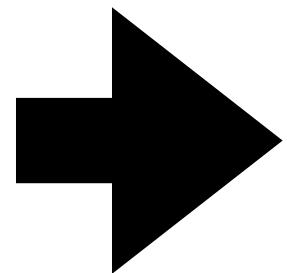
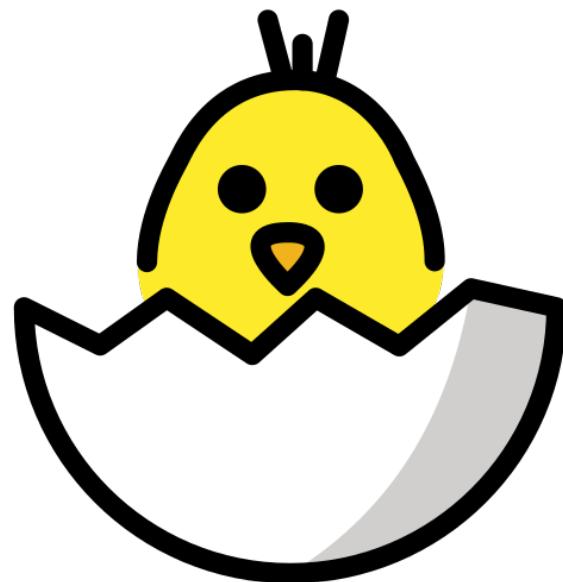
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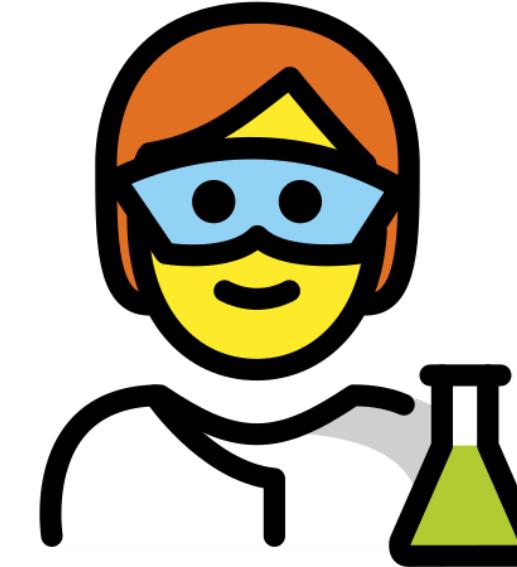
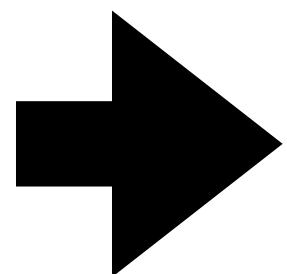
**ML/AI frameworks are evolving very quickly.**

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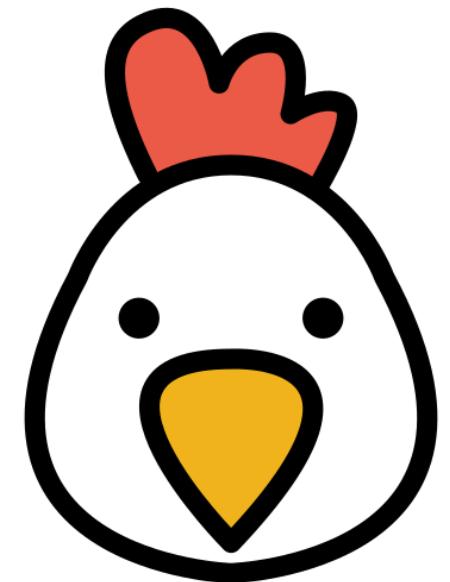
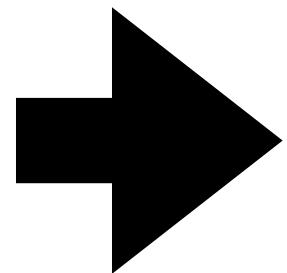
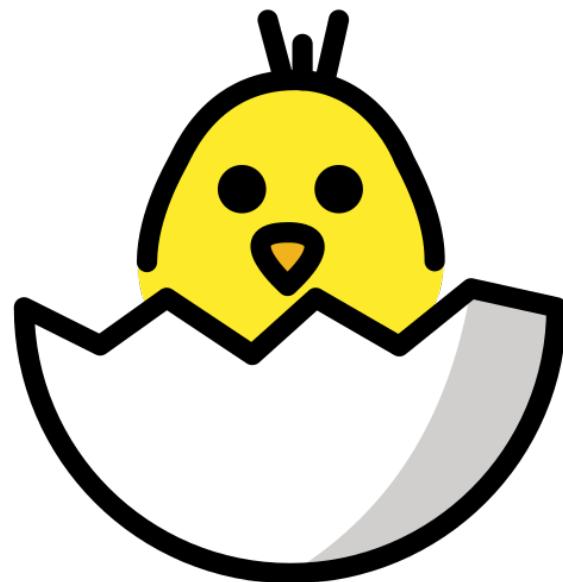


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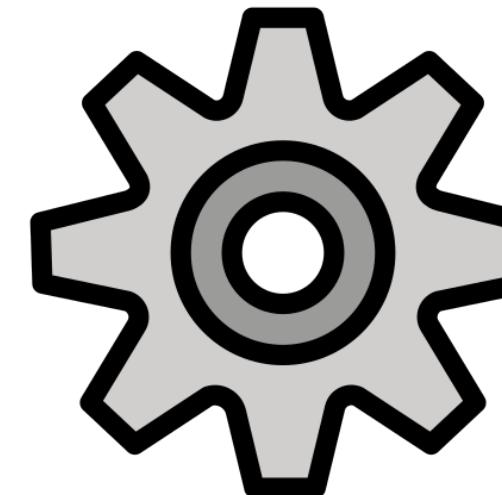
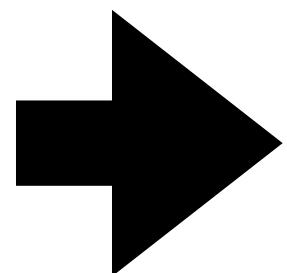
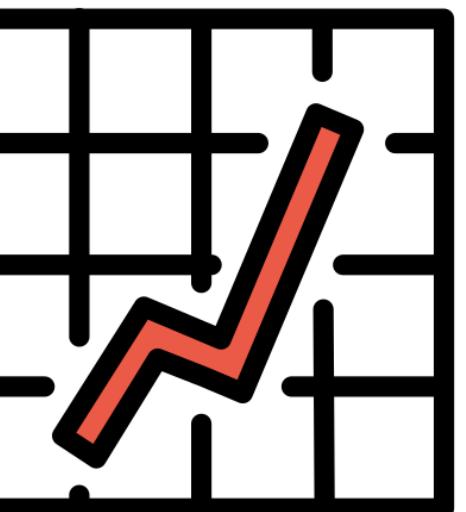
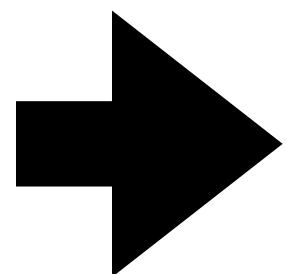
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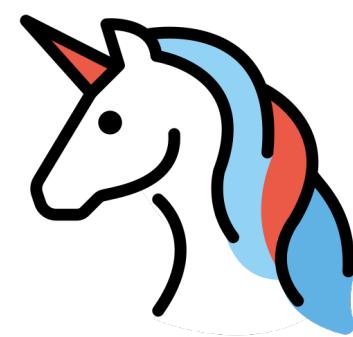
→ IT, SP, control, etc. are still relevant!

# **A traditional division of labor**

**The EE/CS divide in some sense**

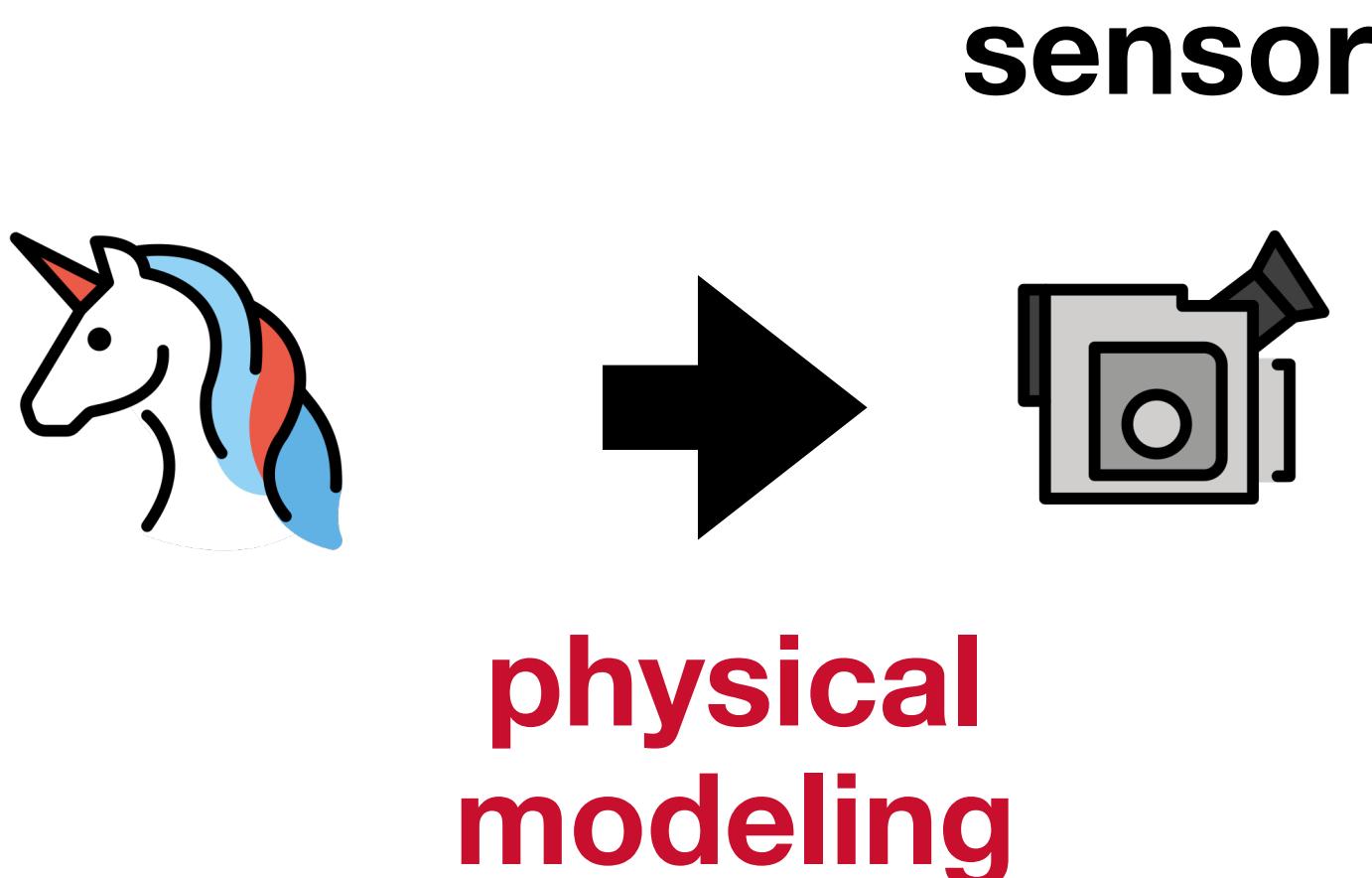
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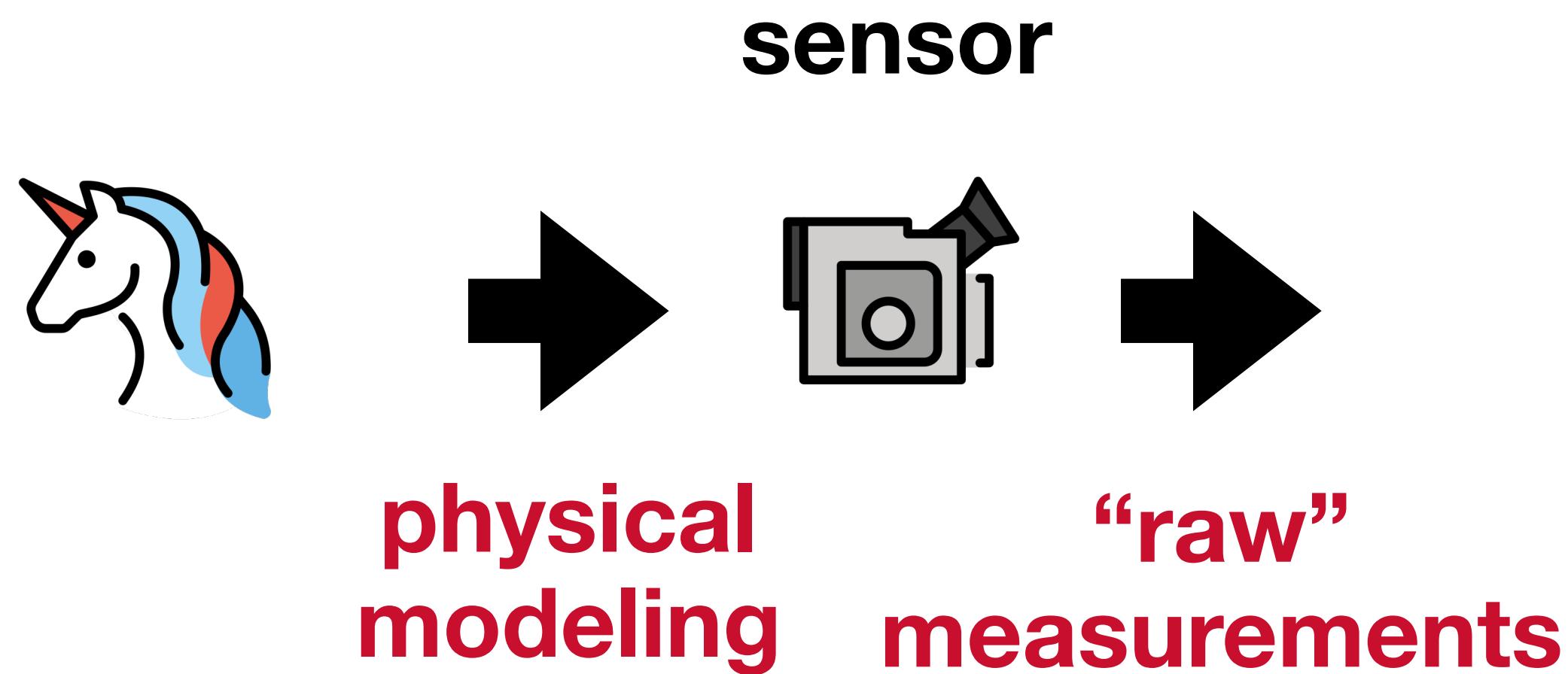
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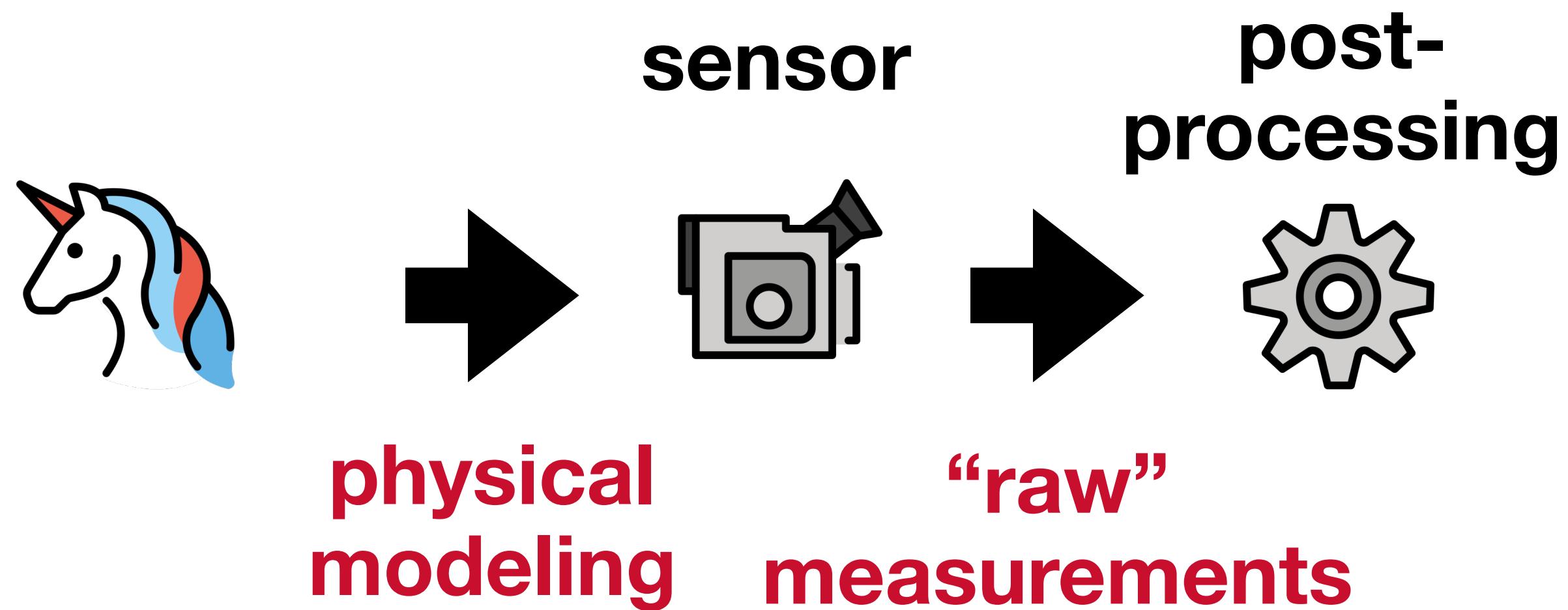
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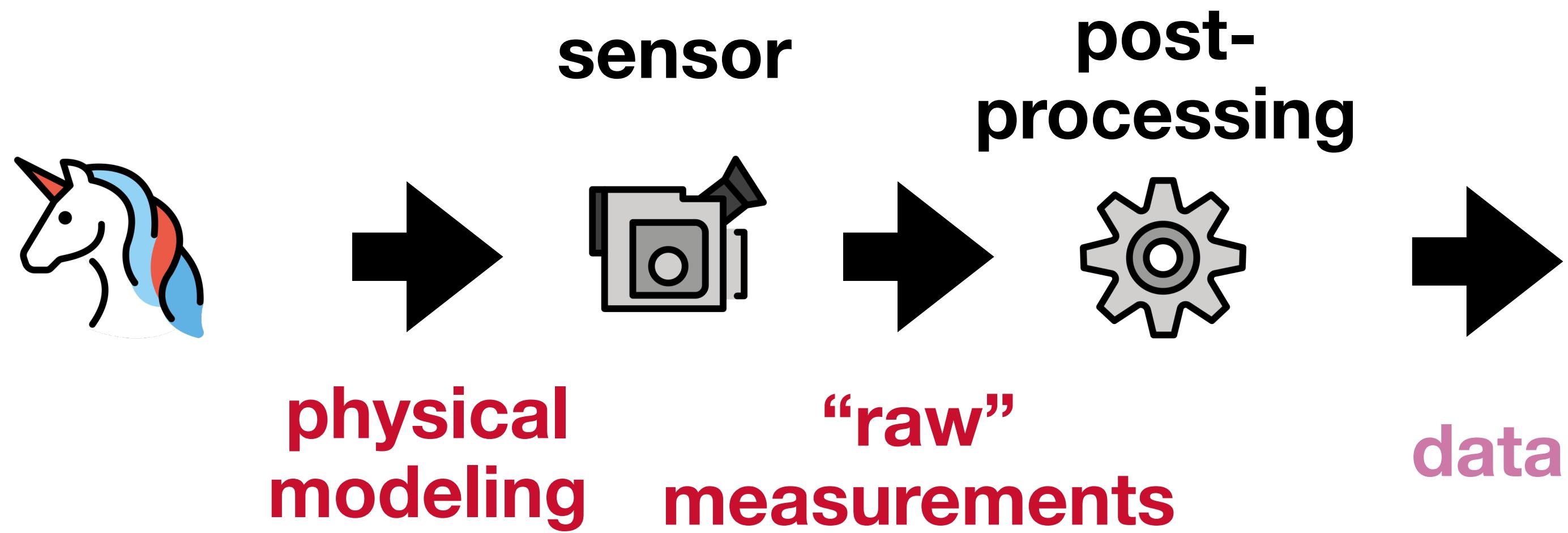
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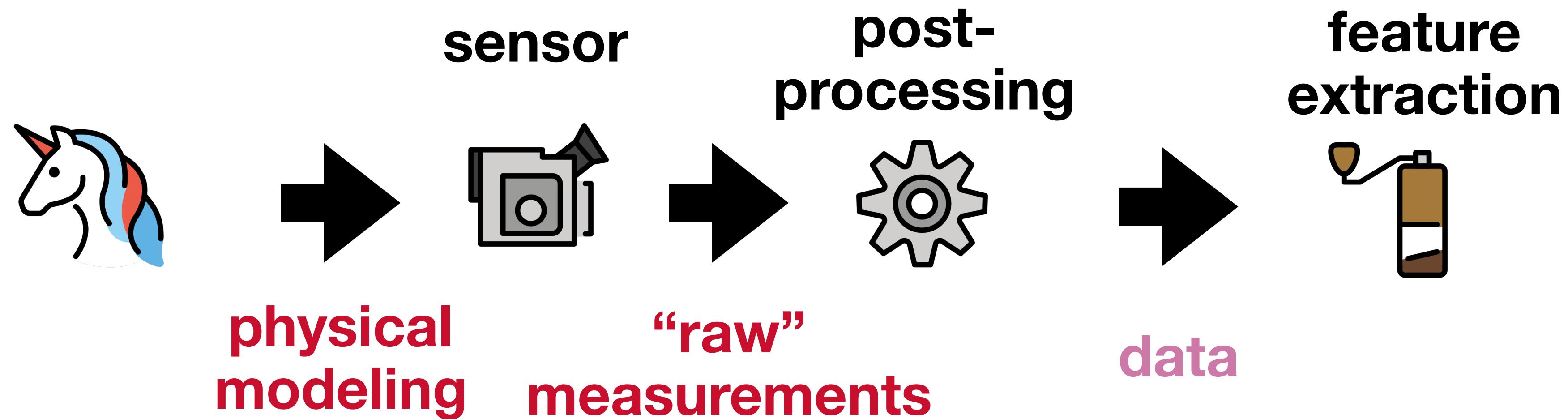
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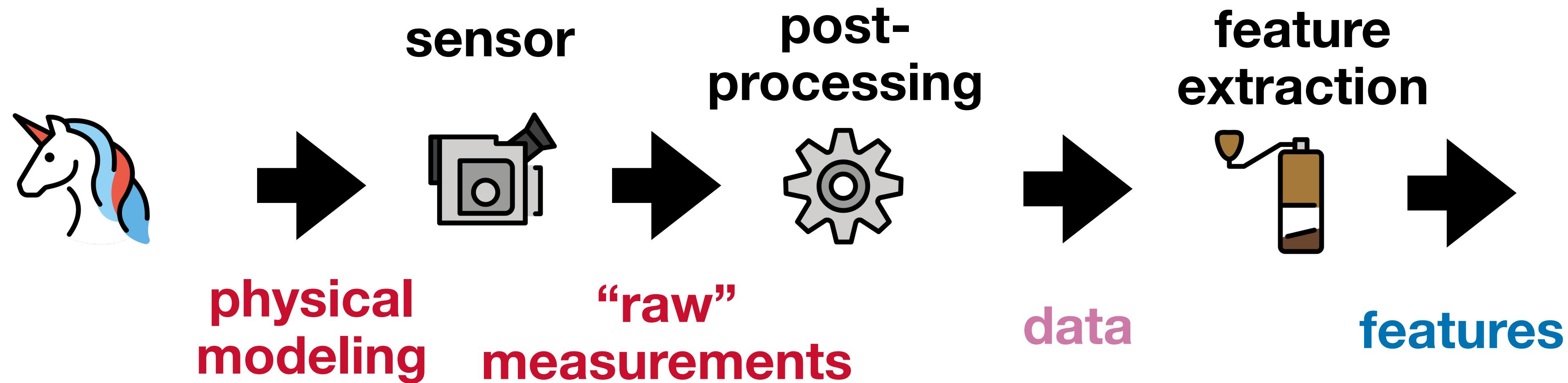
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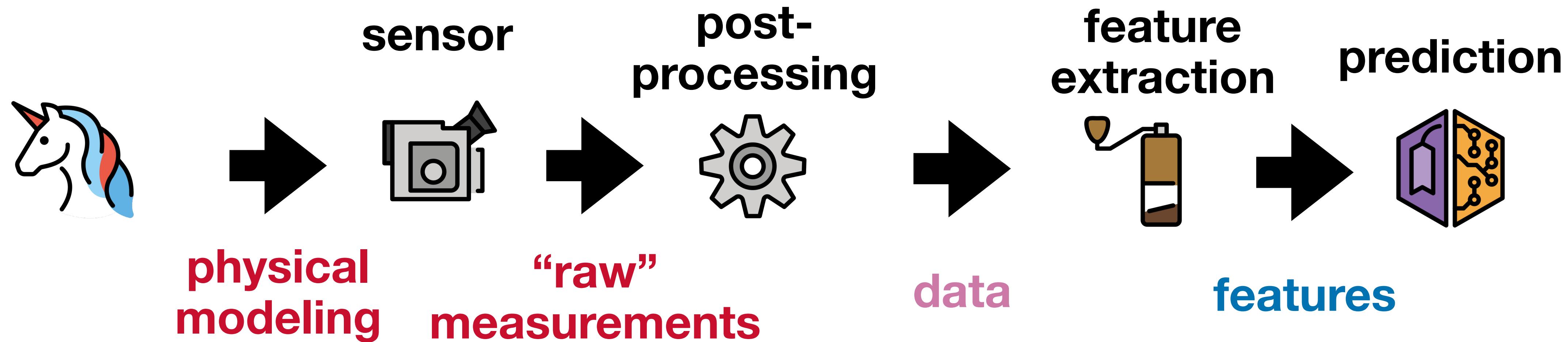
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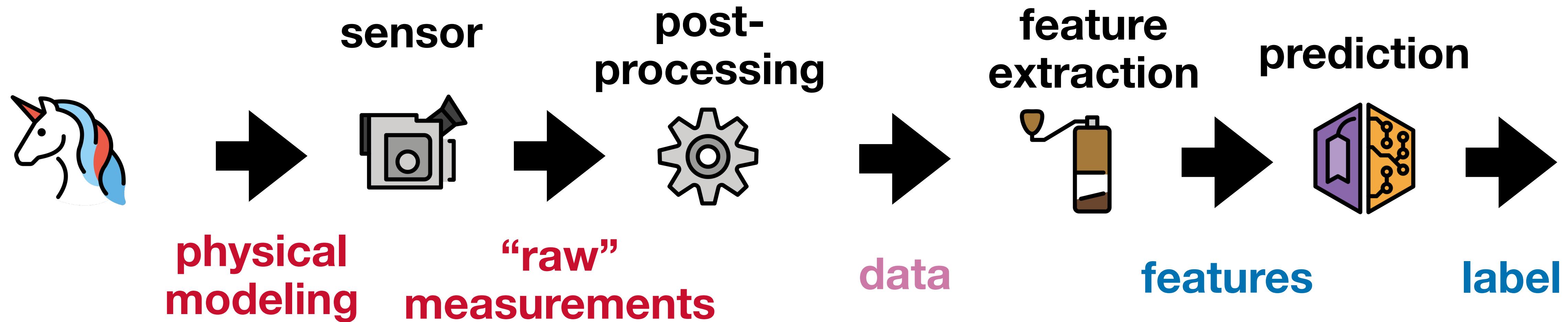
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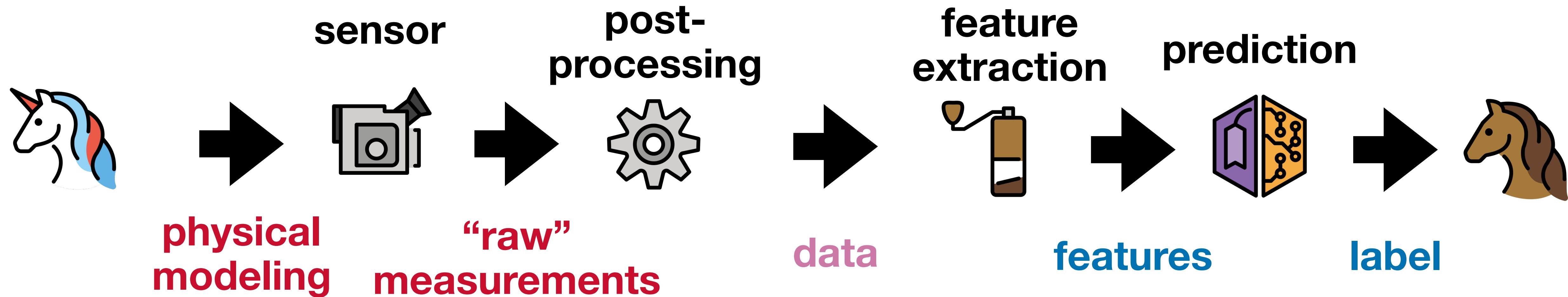
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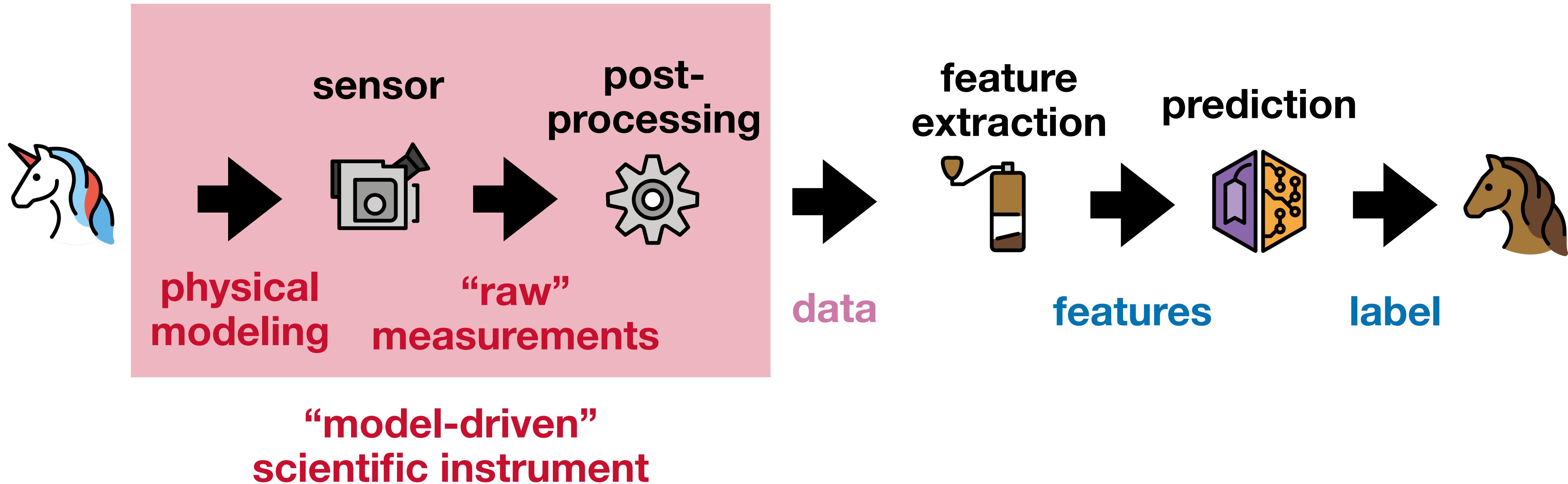
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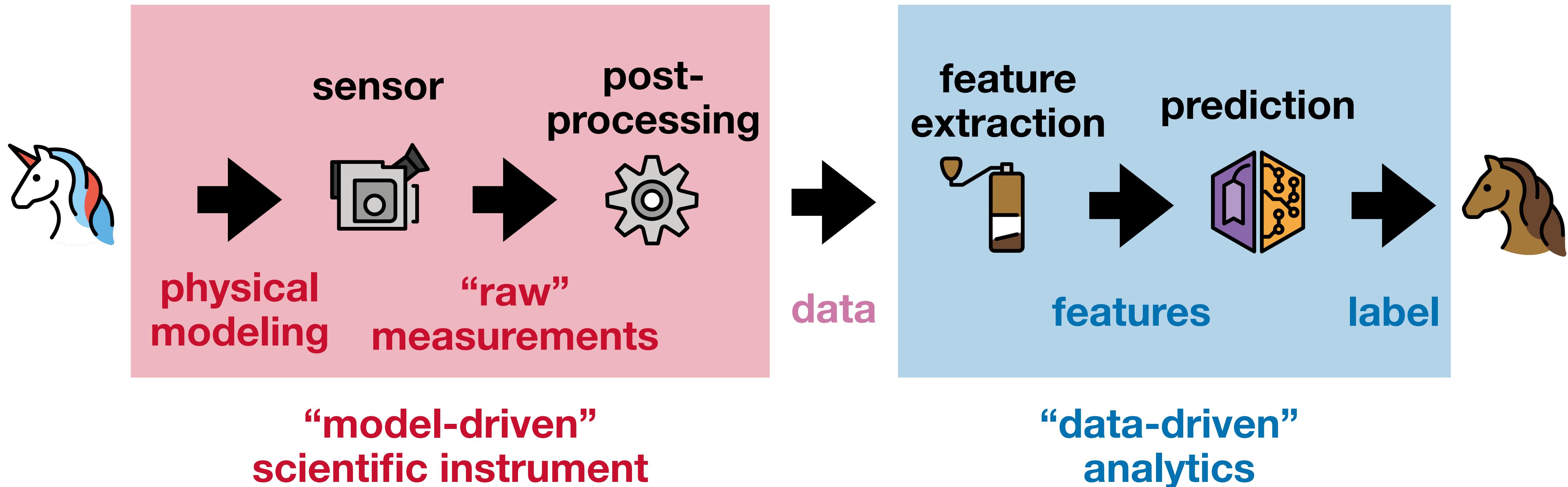
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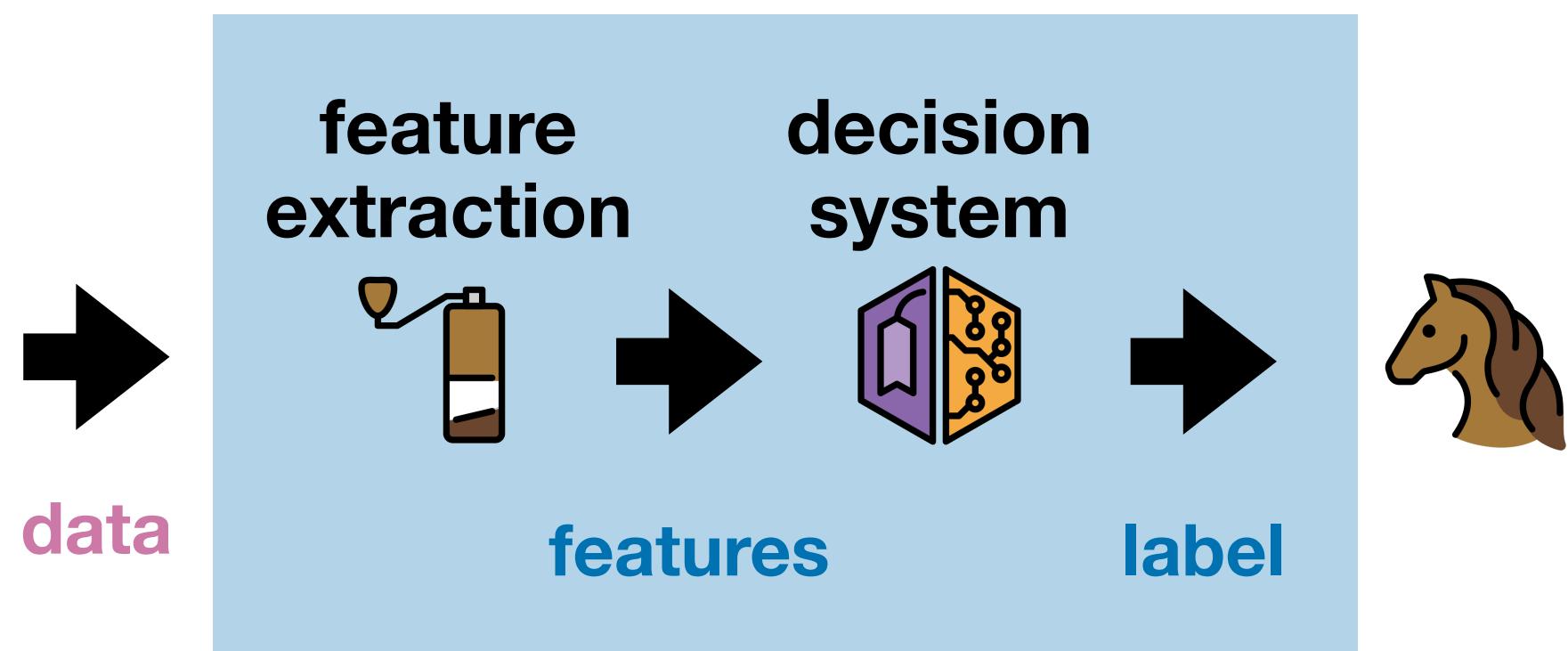
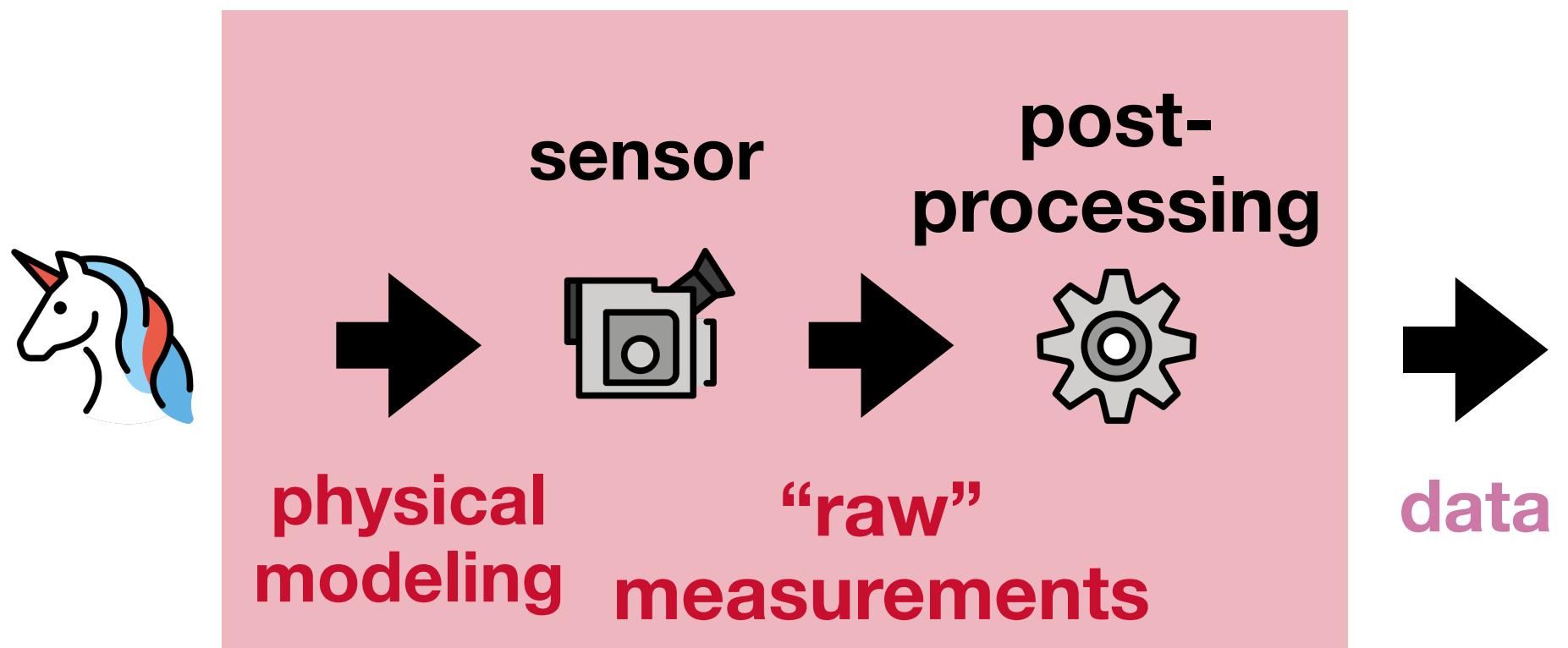
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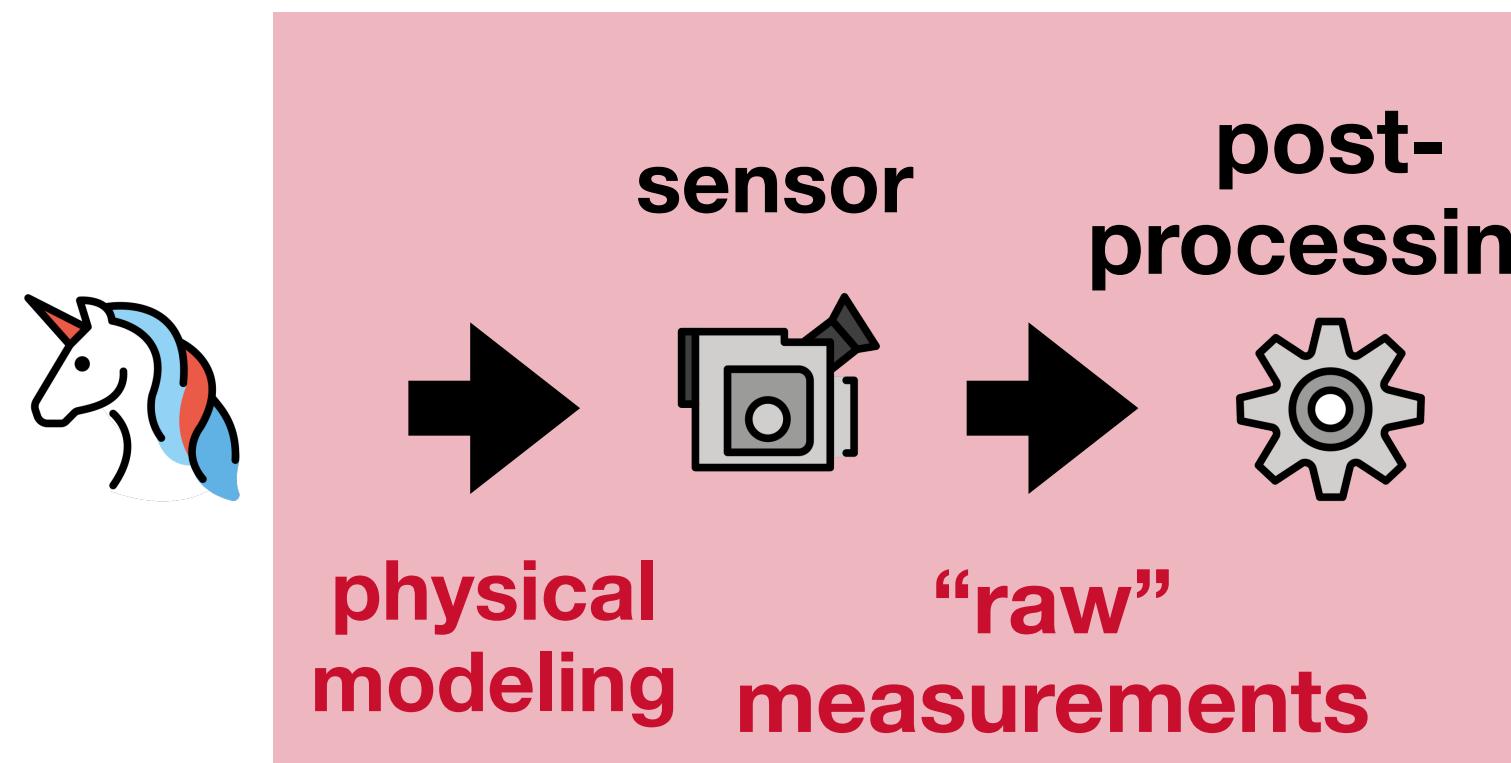
# What is “AI as instrumentation”?

Putting neural networks into measurement devices

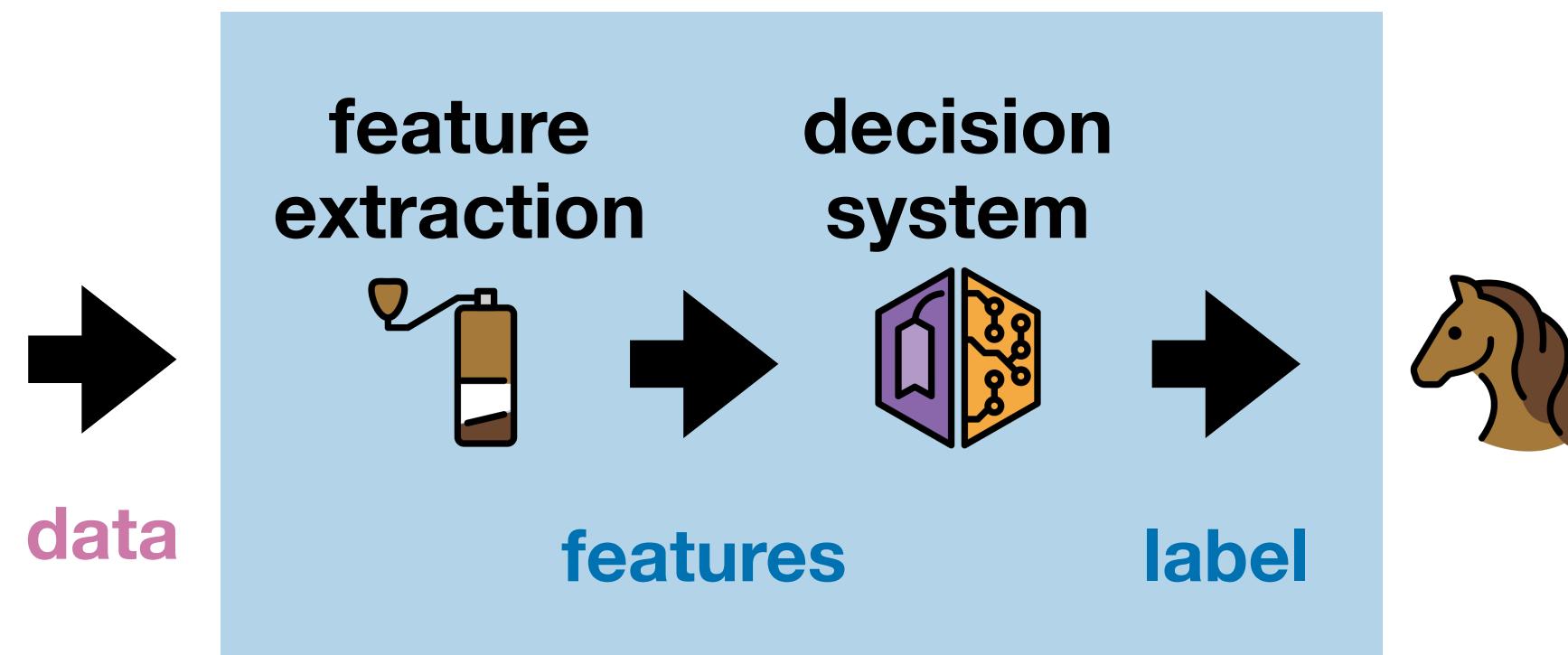


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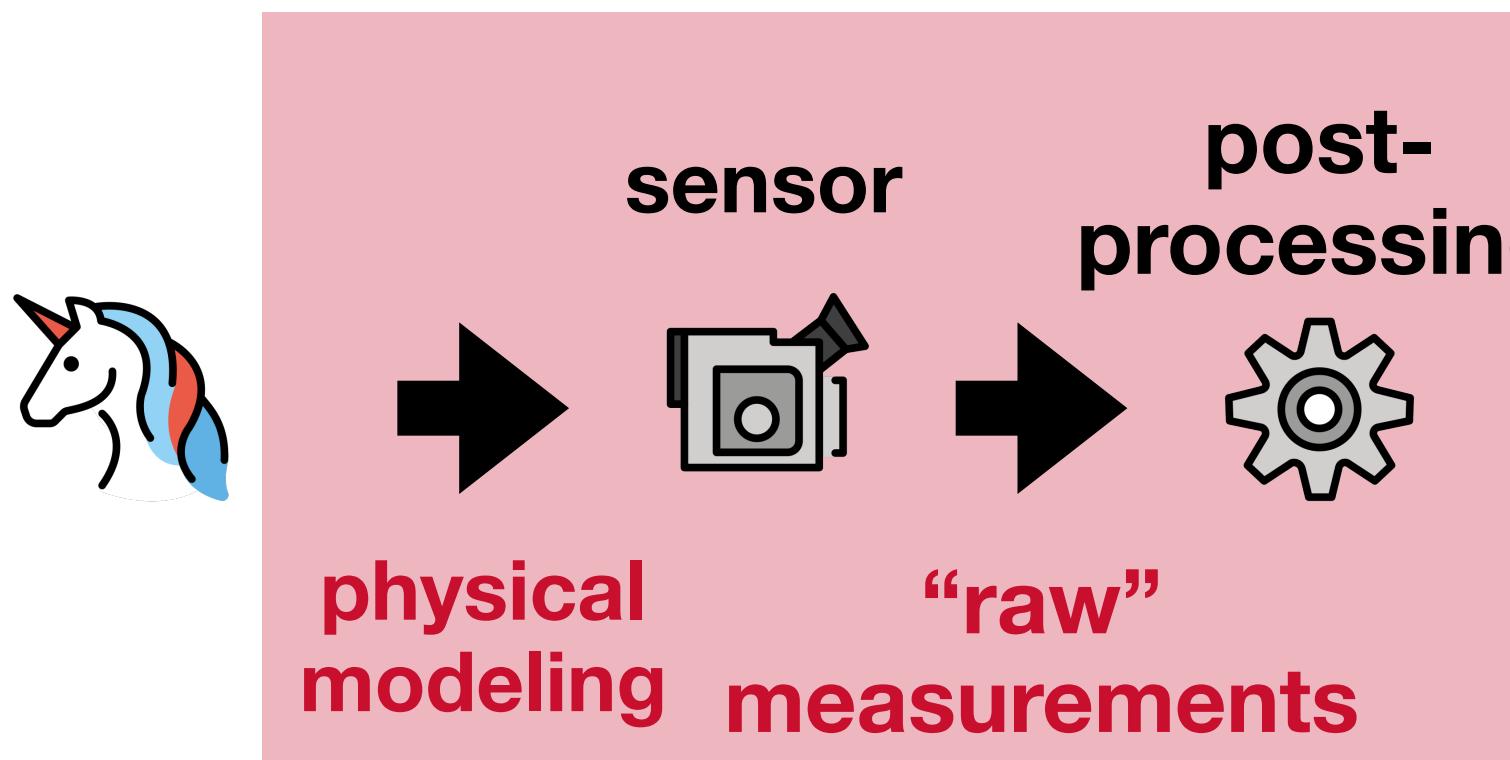


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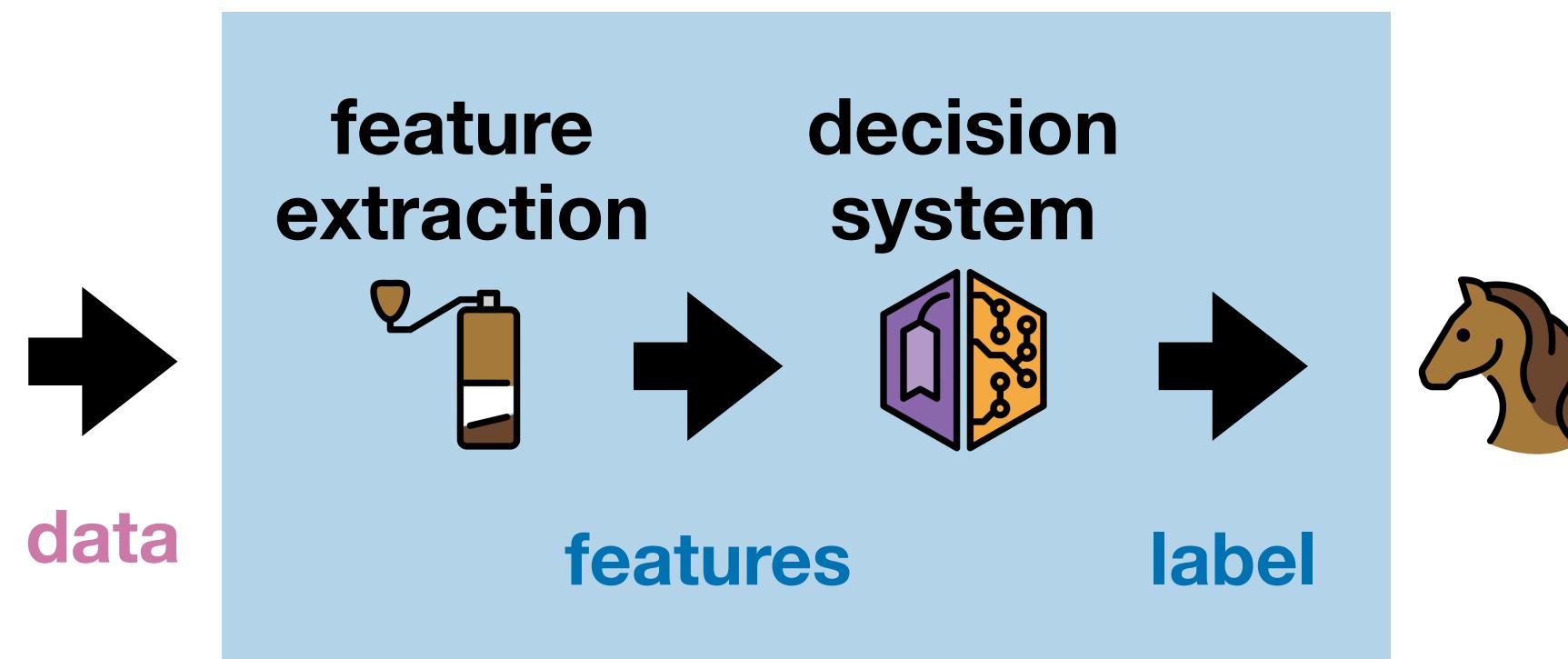
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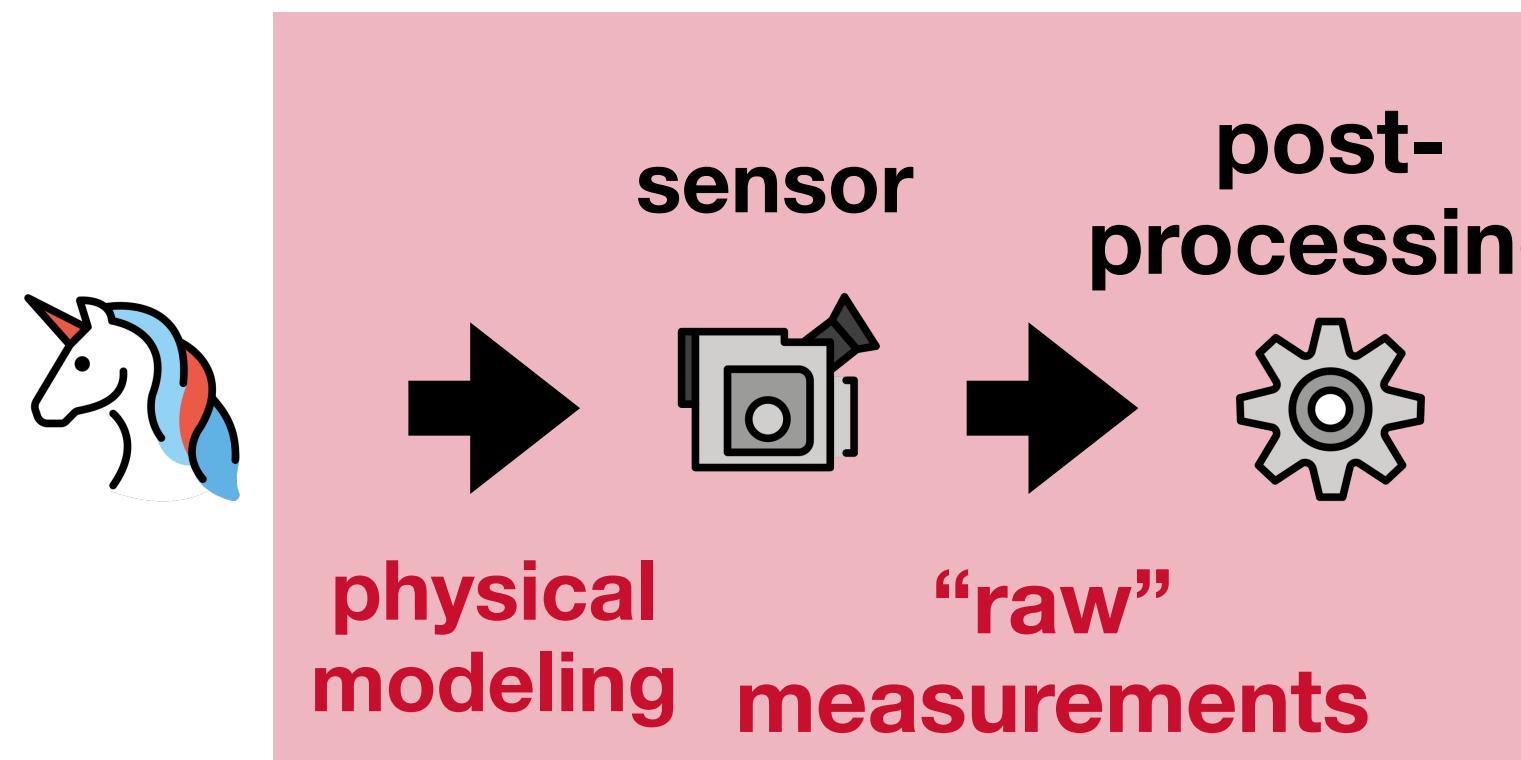
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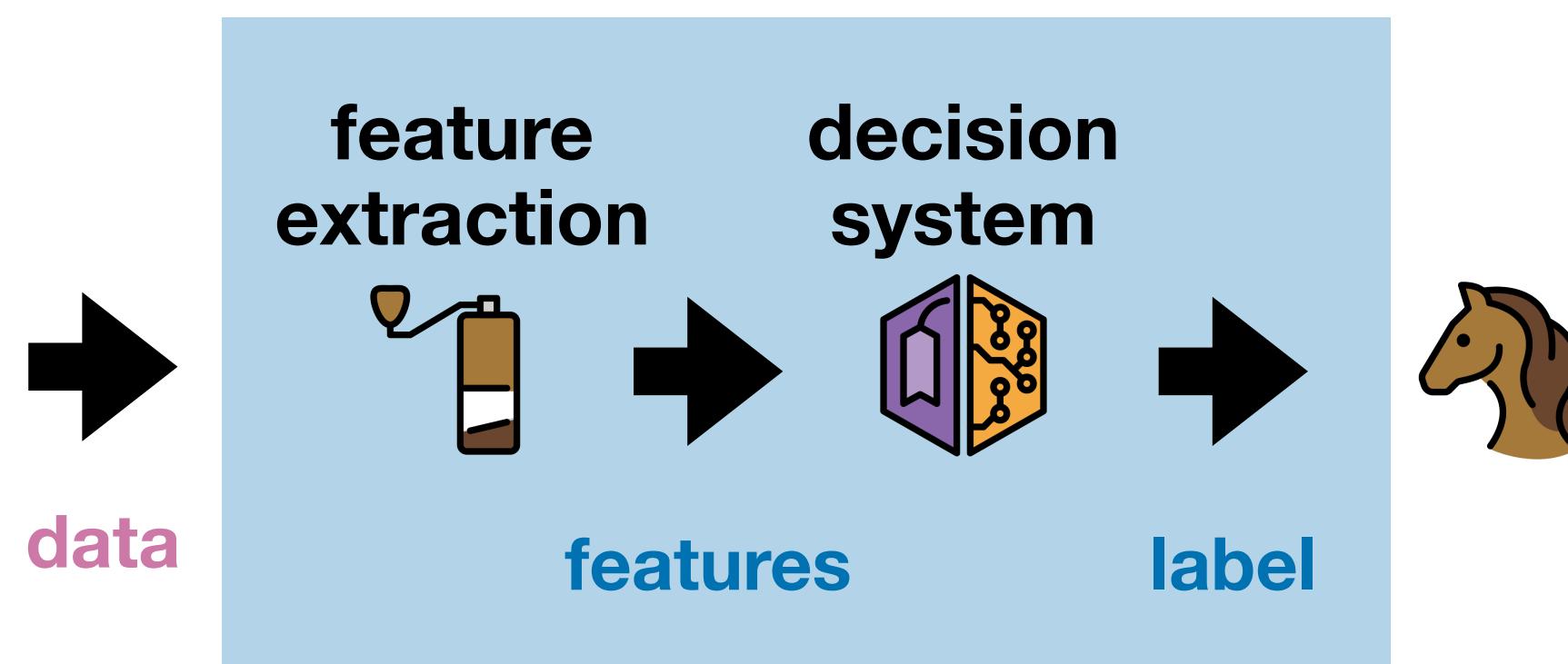
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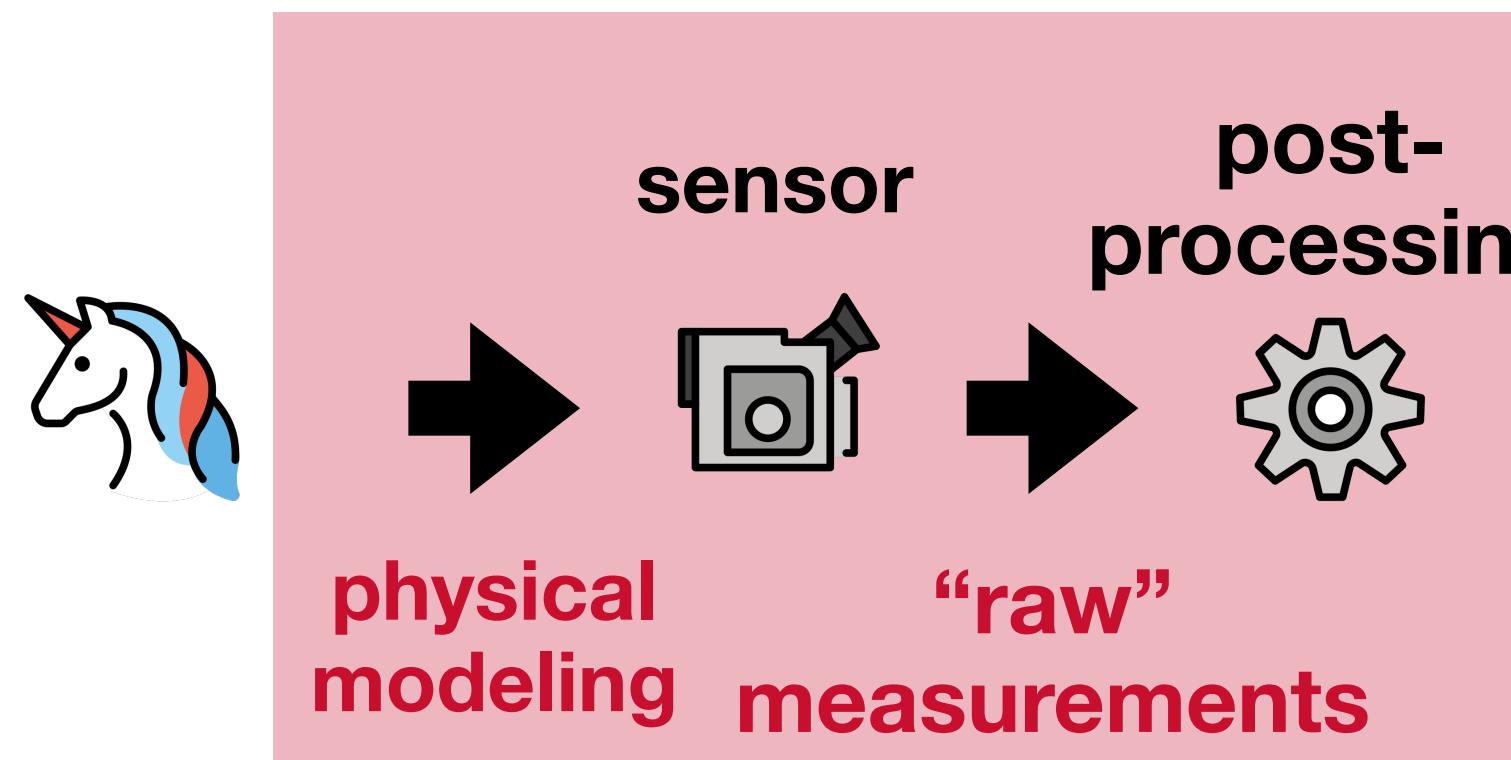
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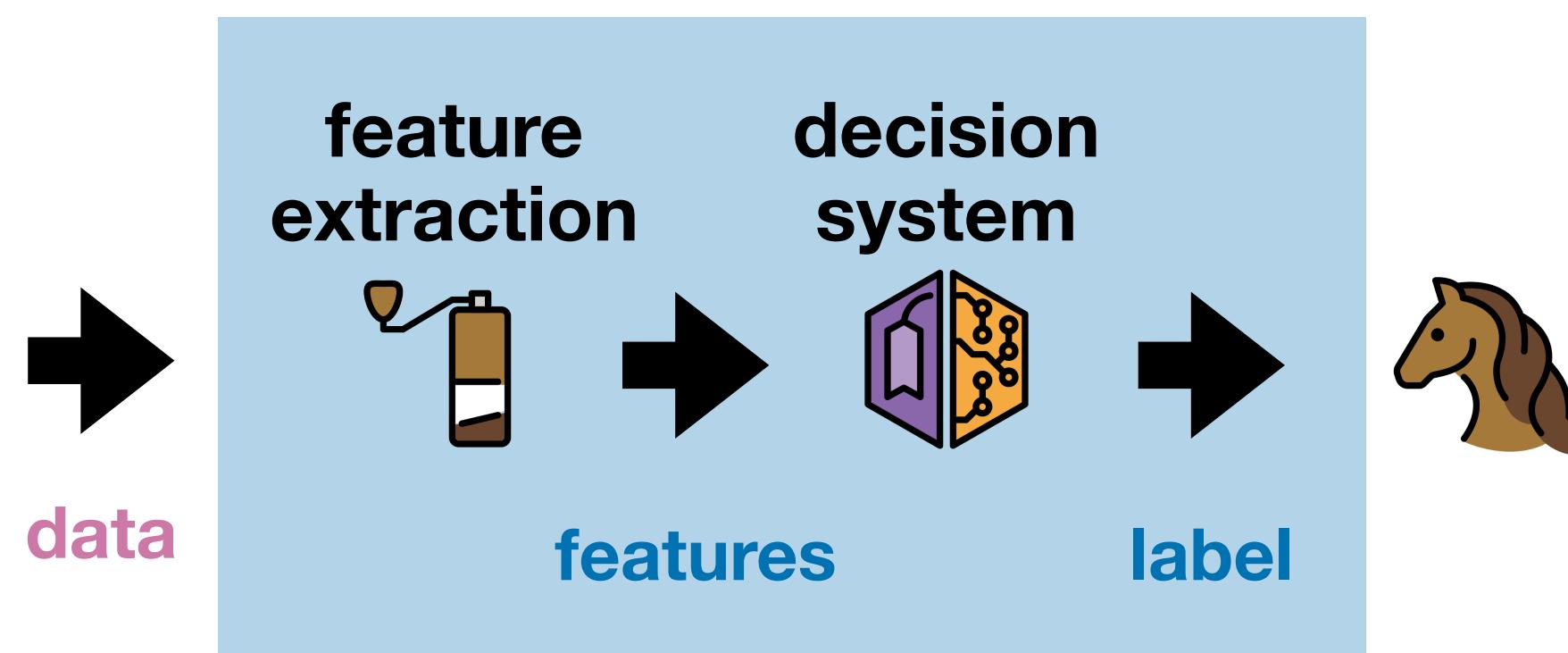


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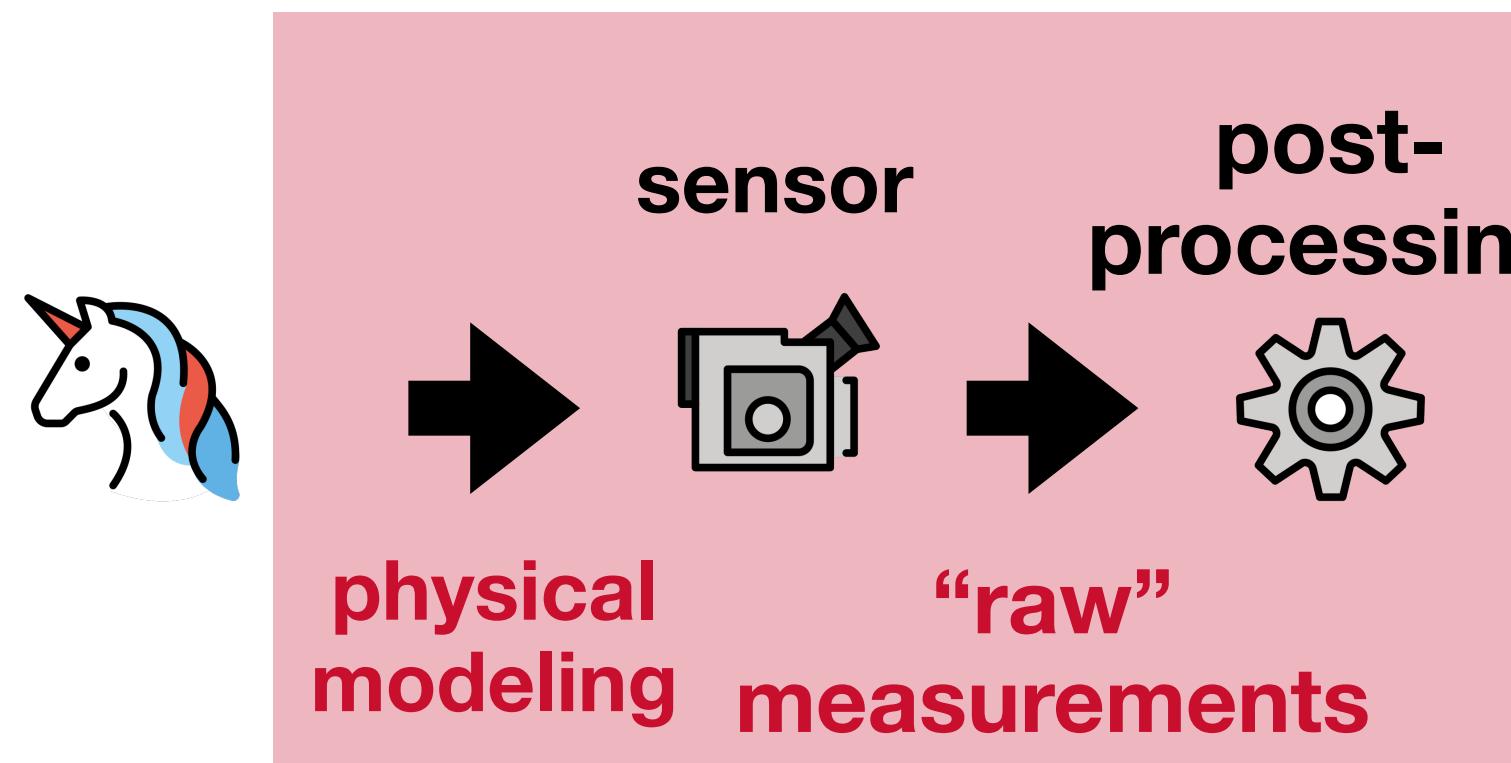
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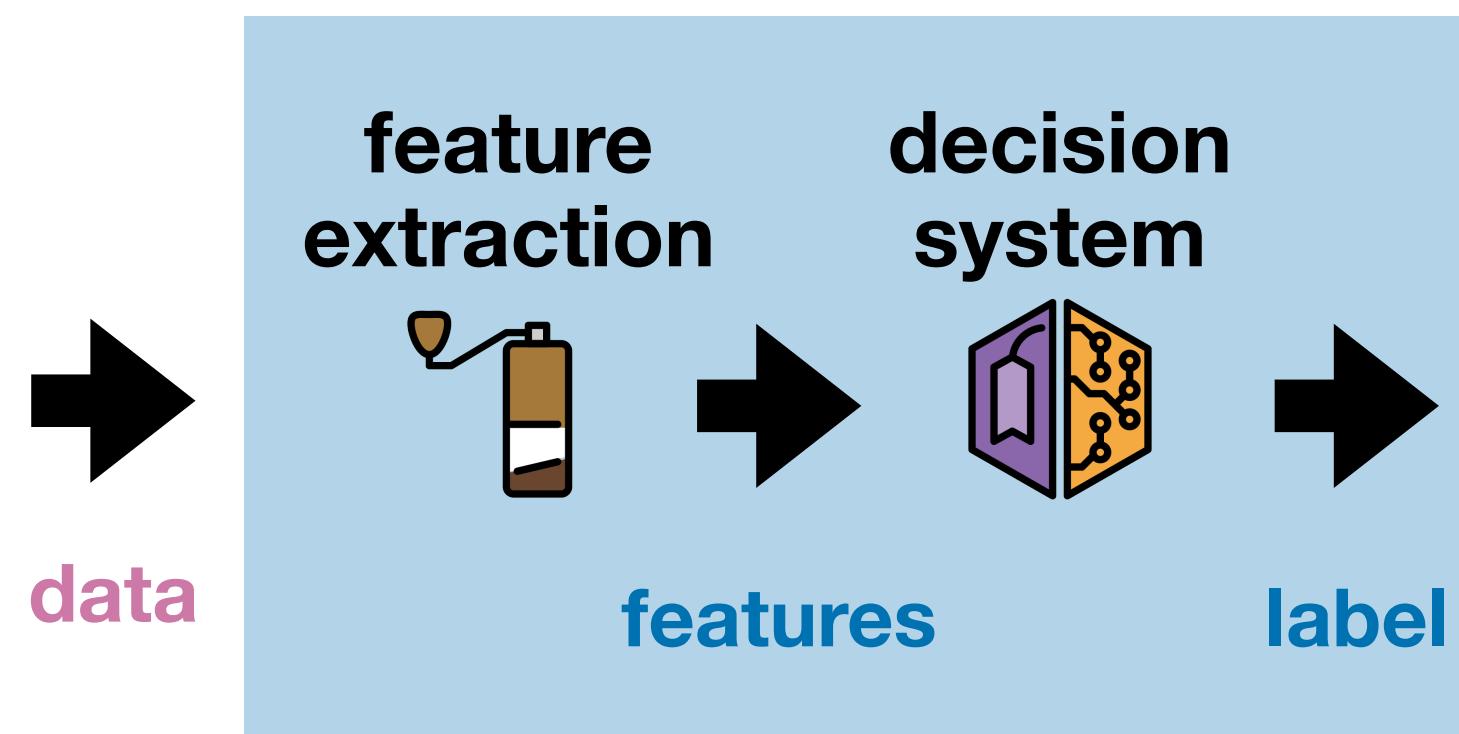
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If we put AI “into the camera” will these be true?

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**Assumptions are wrong, but maybe correctable?**

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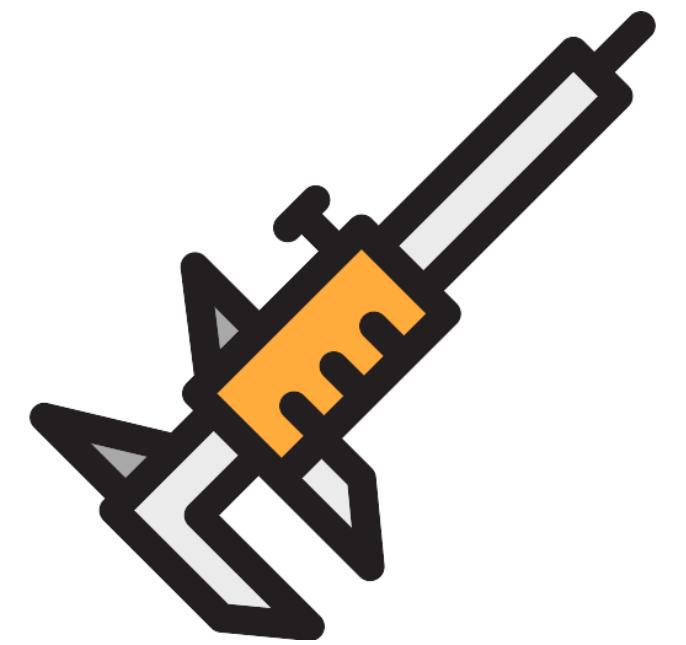
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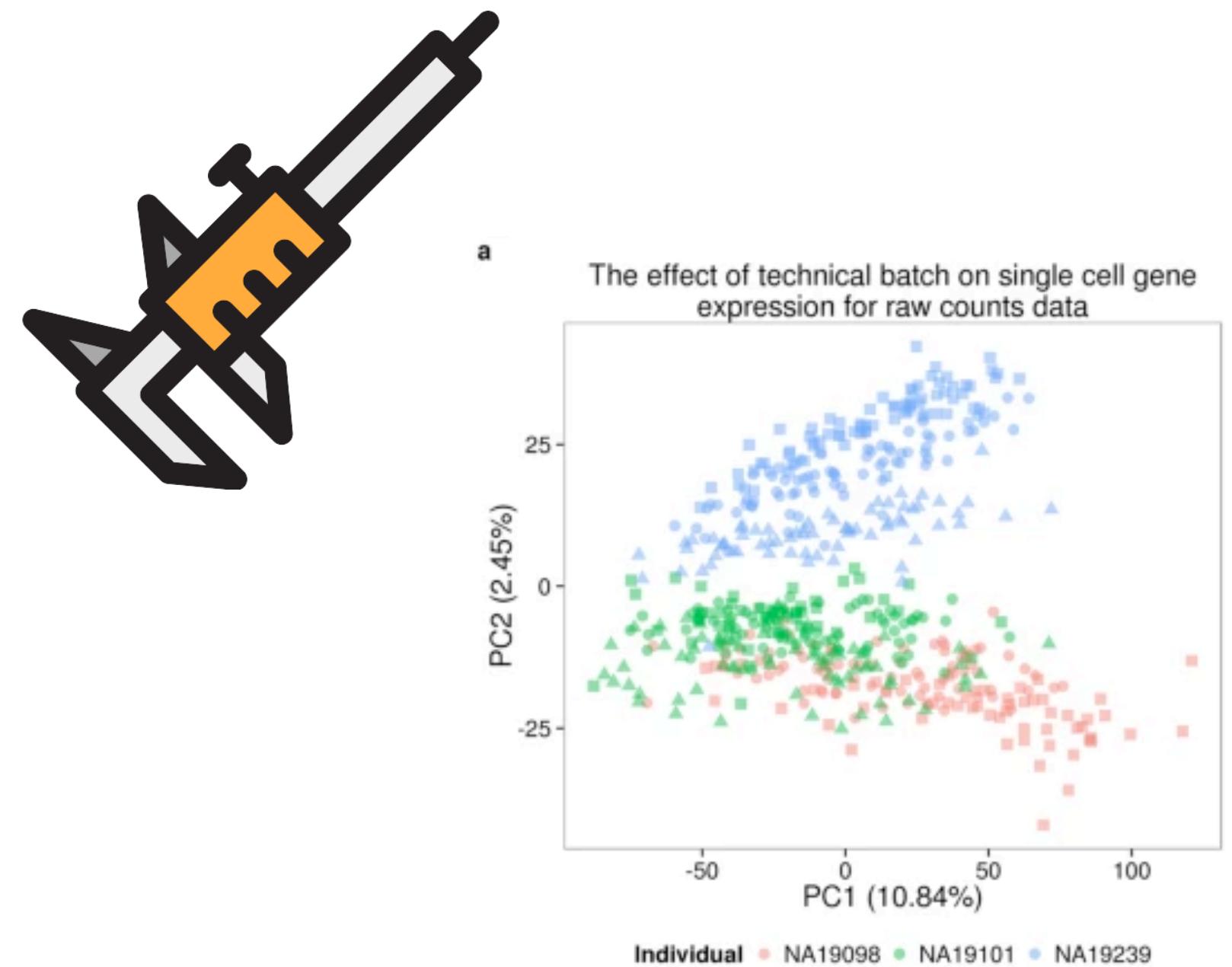


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- “Batch effects” (c.f. DNA/RNA sequencing)

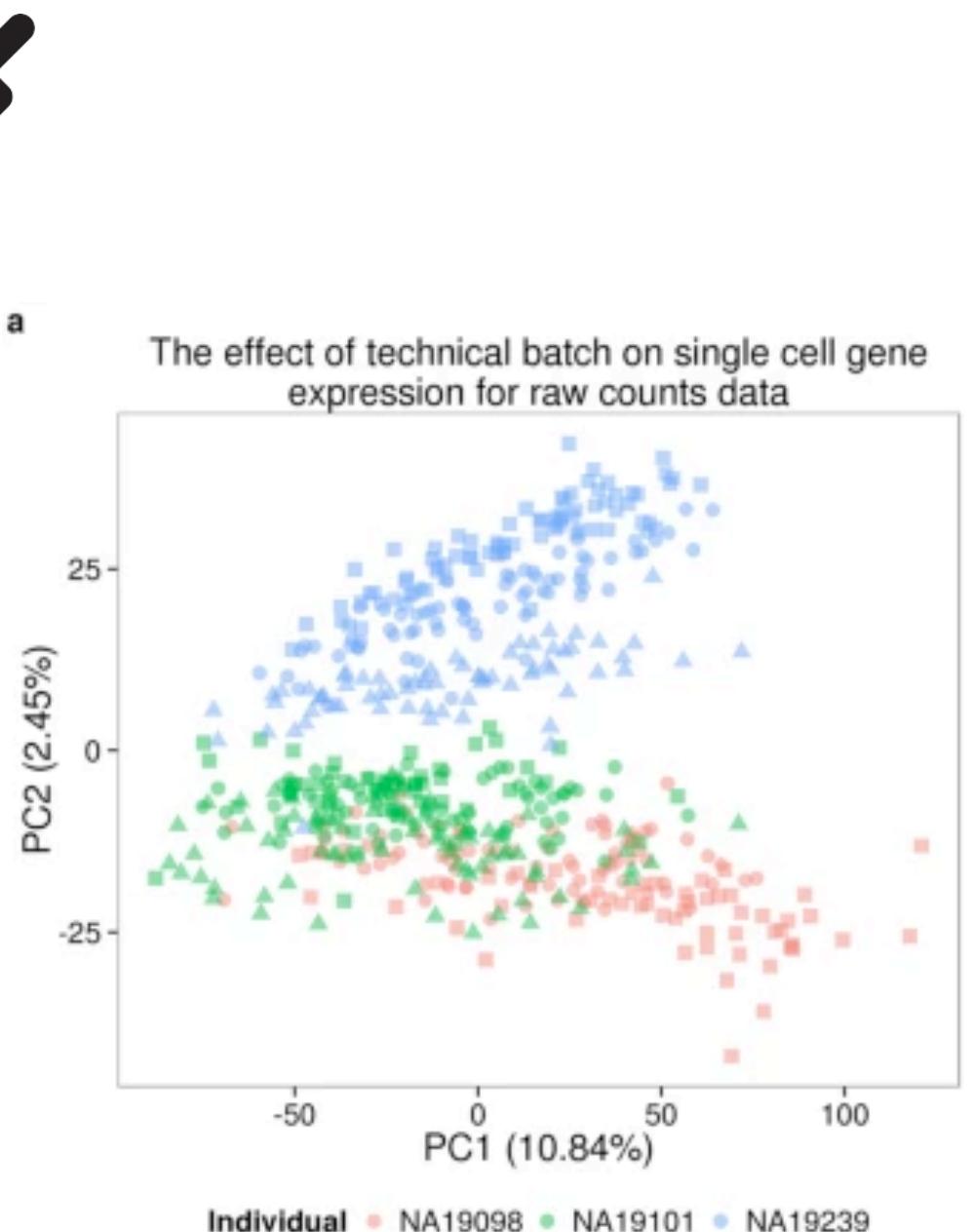


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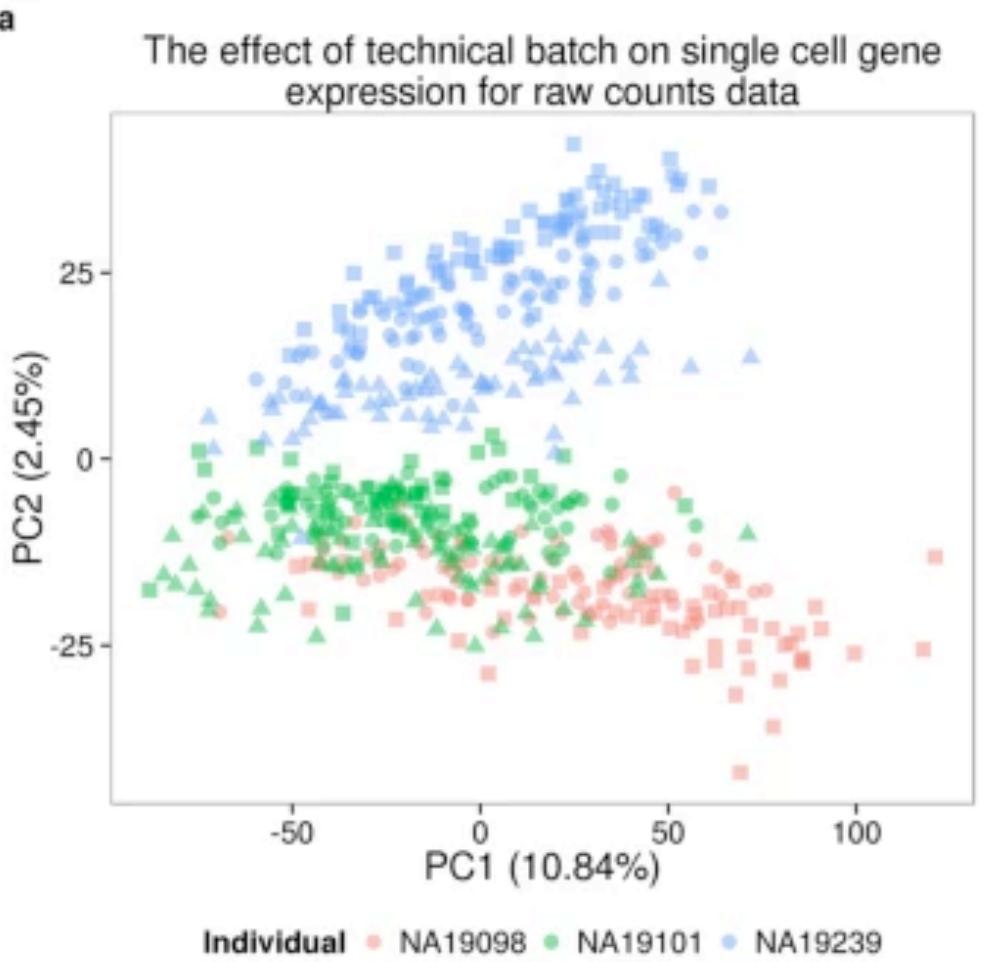


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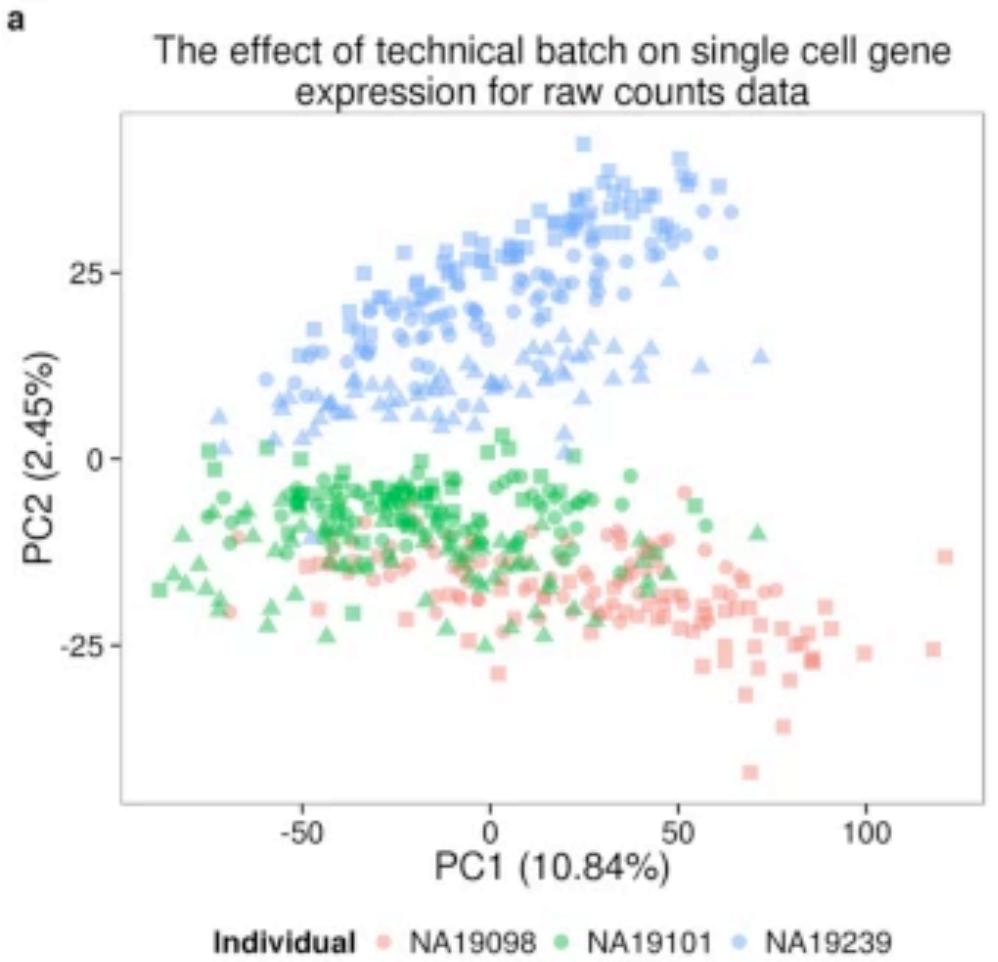


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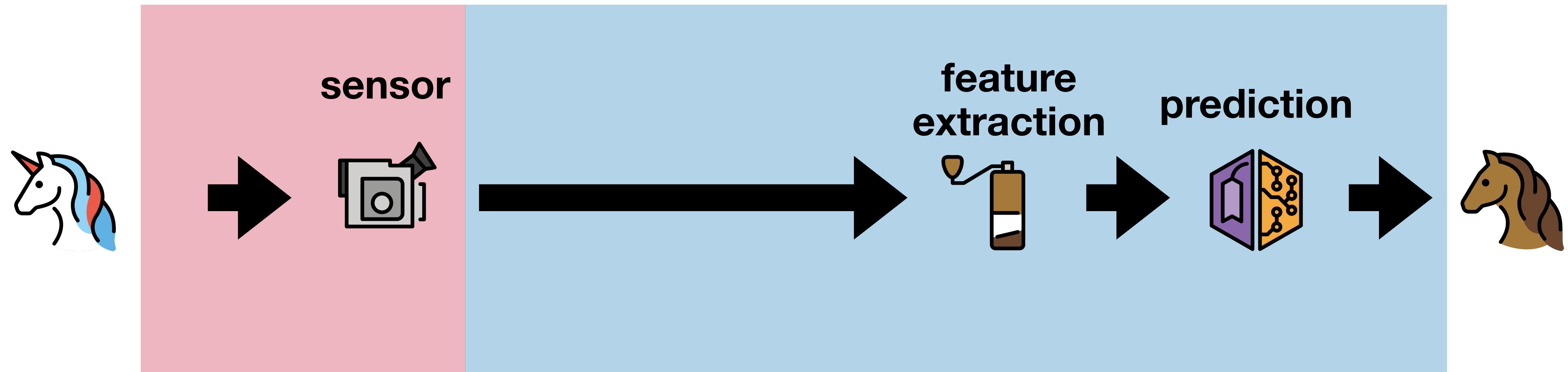
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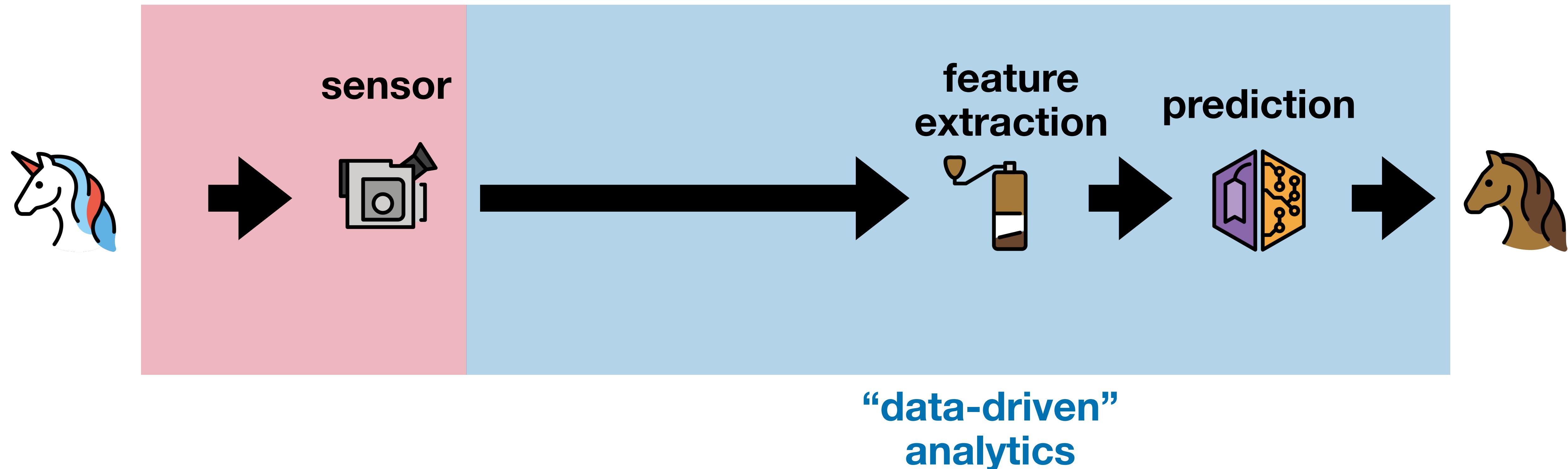
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Sensors, instrumentation, and decision support



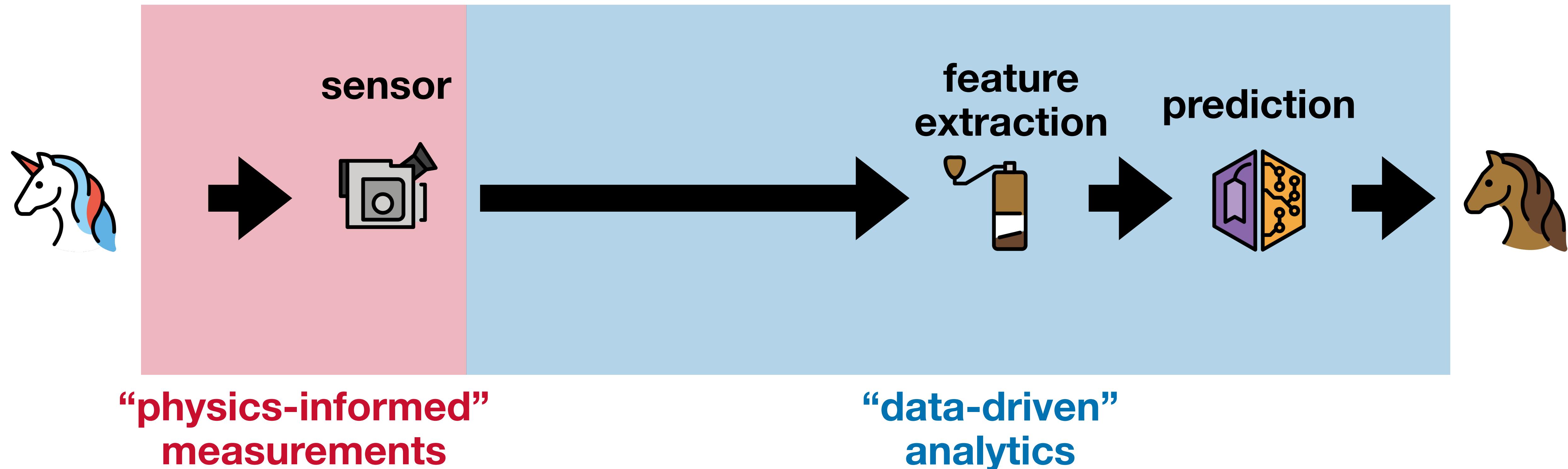
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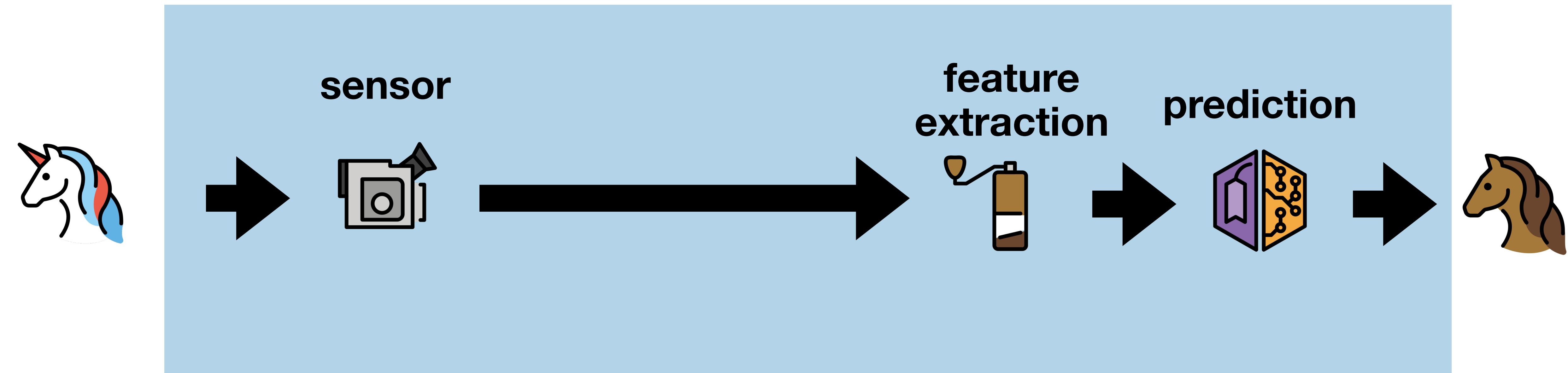
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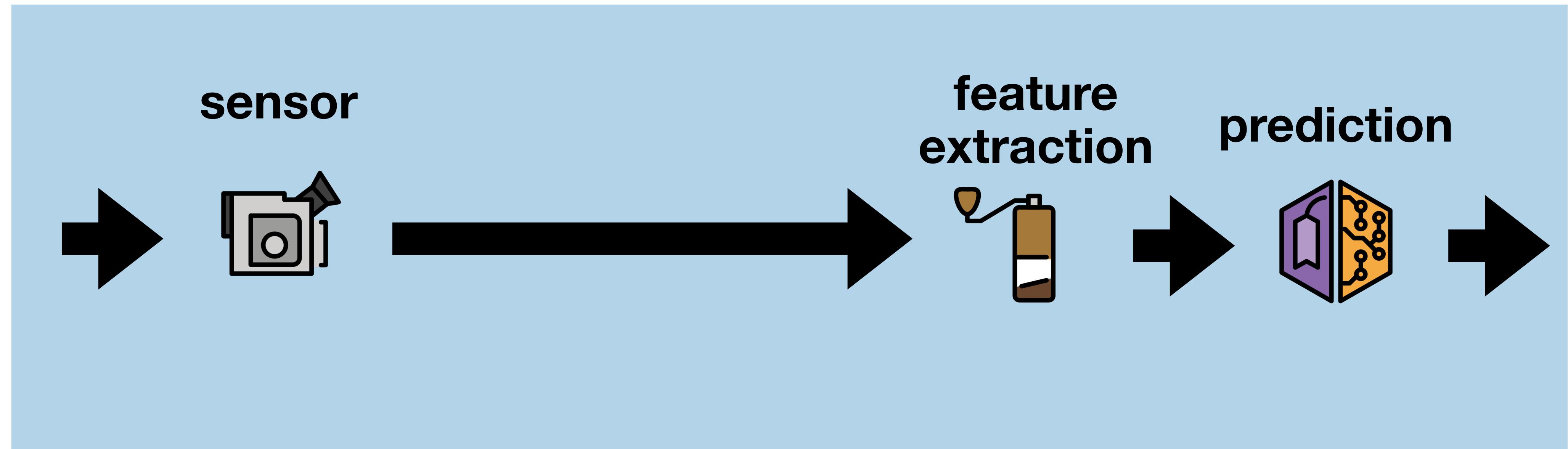
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**“data-driven”  
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What would it mean of them to hold (if they do)?



iOS 8.3



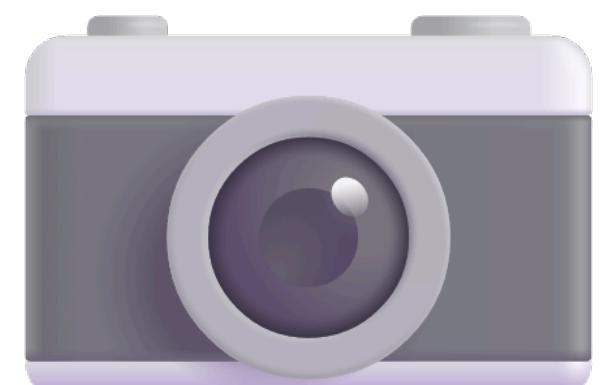
iOS 18.4



HarmonyOS 4.0



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MS 3D Fluent



SerenityOS

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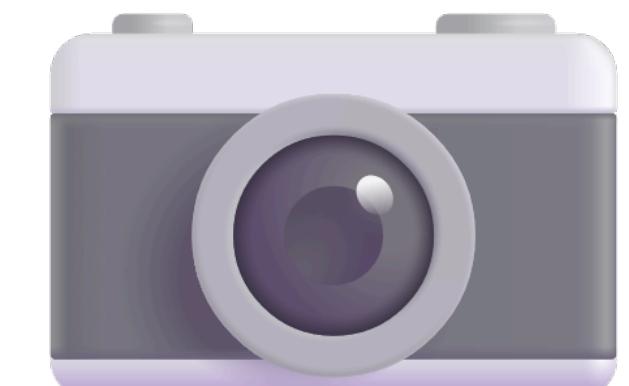
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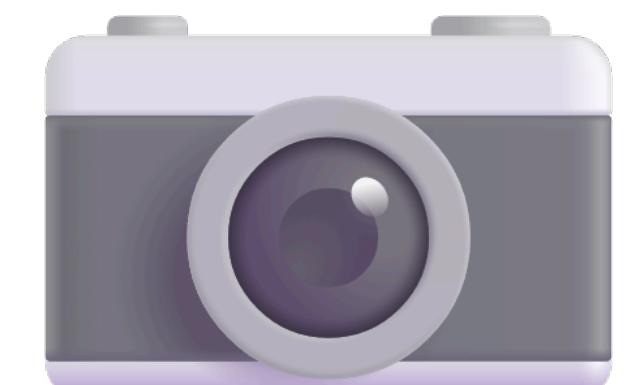
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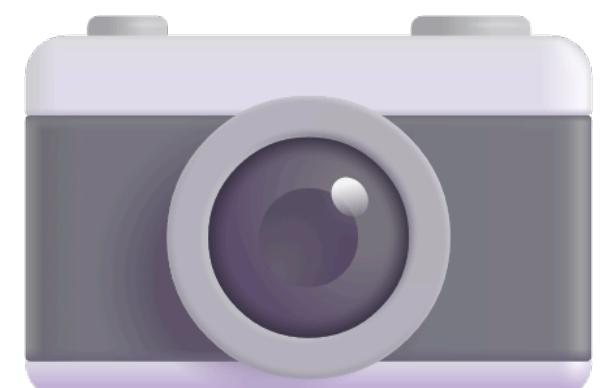
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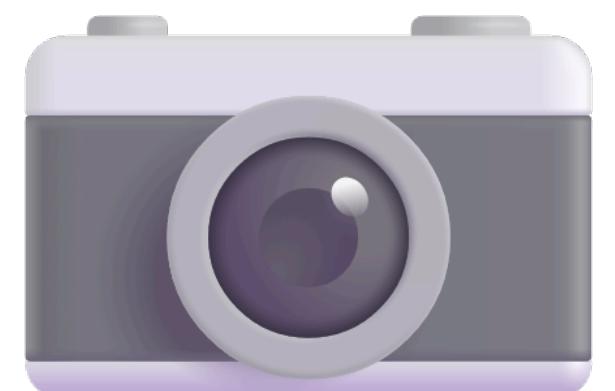
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**These questions are not new!** We can use “classical” tools to try and understand them.



iOS 8.3



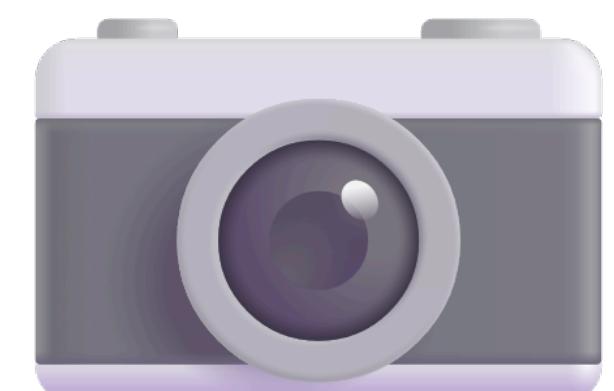
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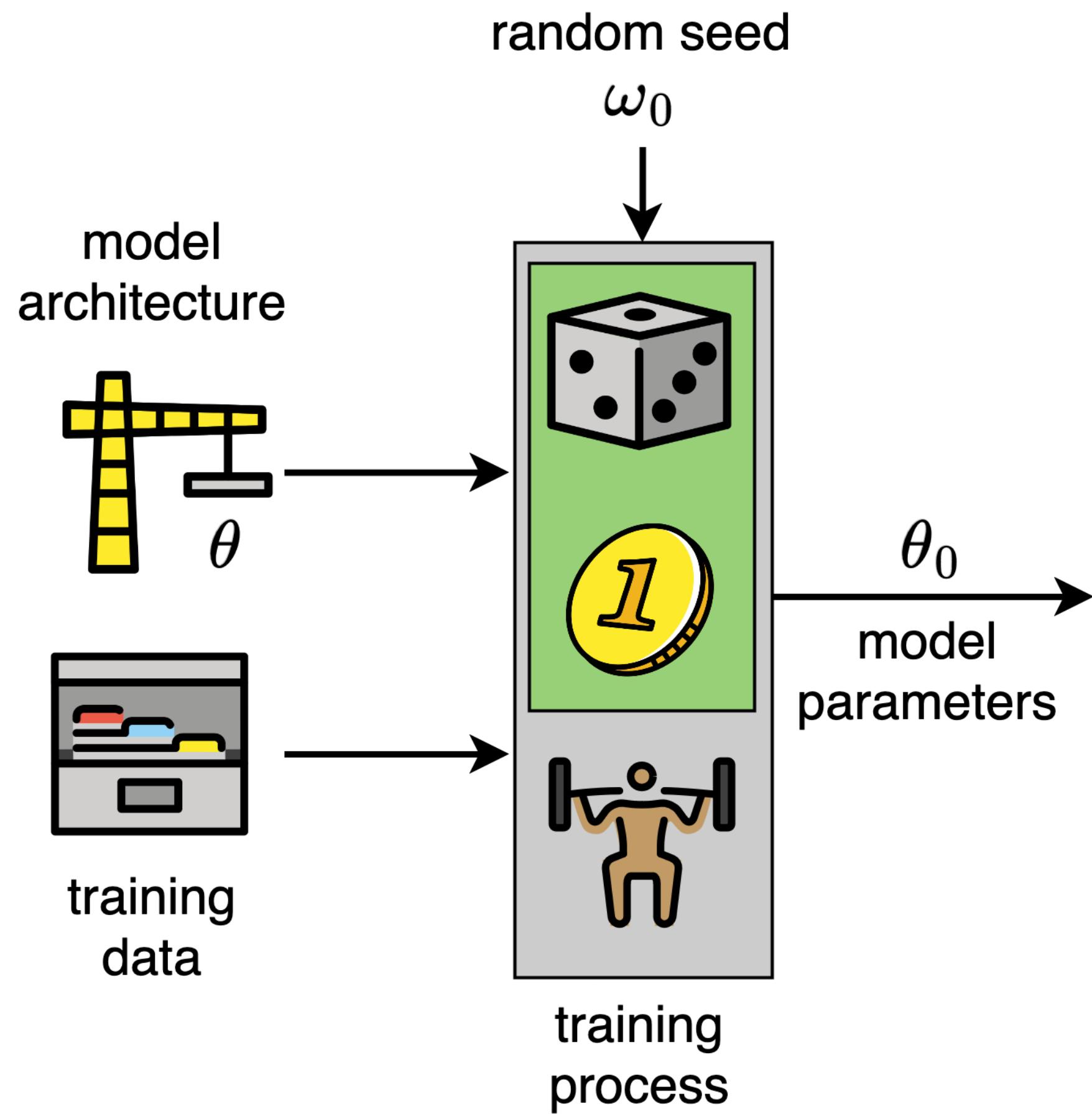
# Some preliminaries



Rm Palaniappan, *Alien Planet-A*  
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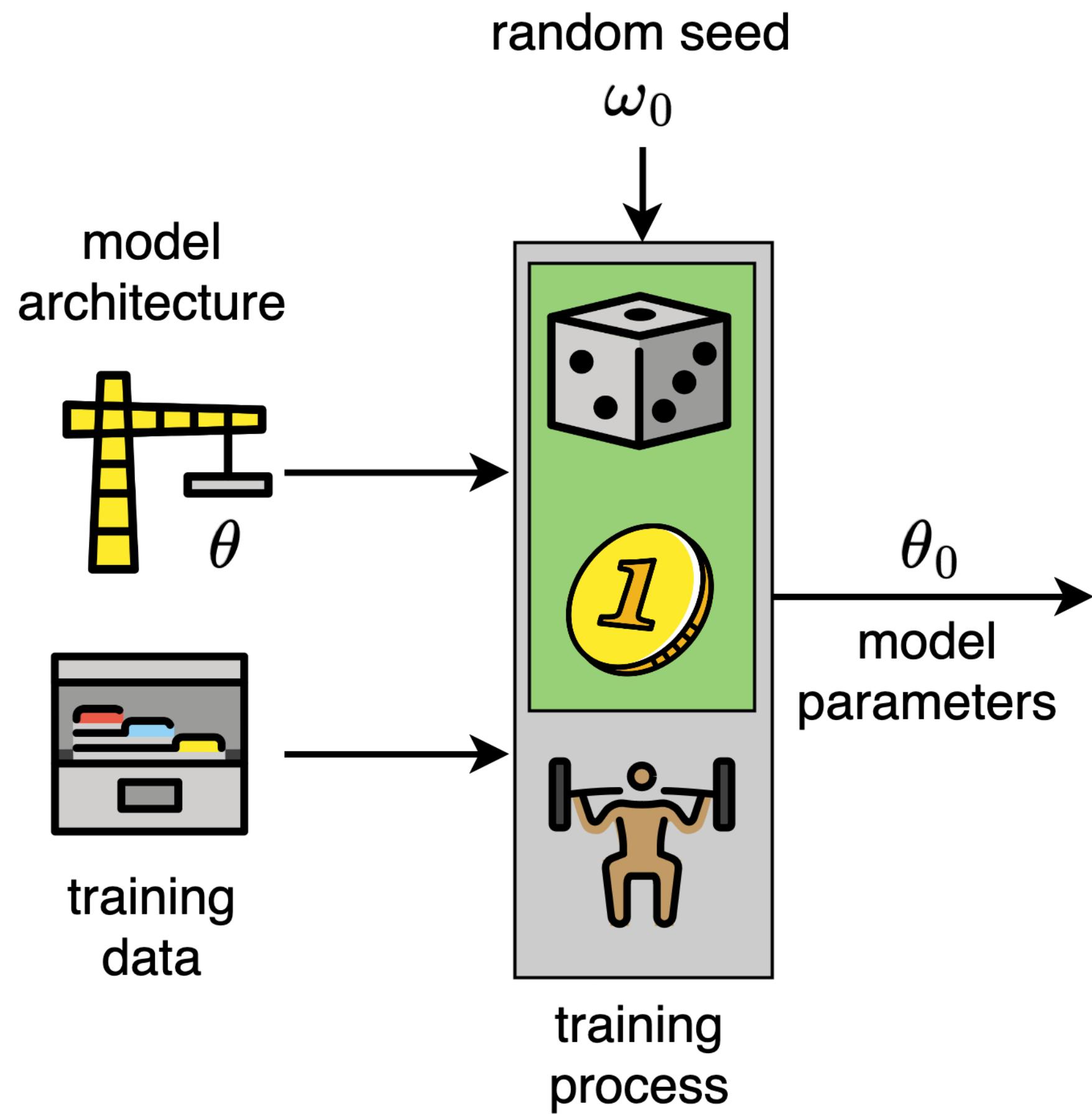
# The standard statistical setup for modern ML

## Machine learning as function-fitting



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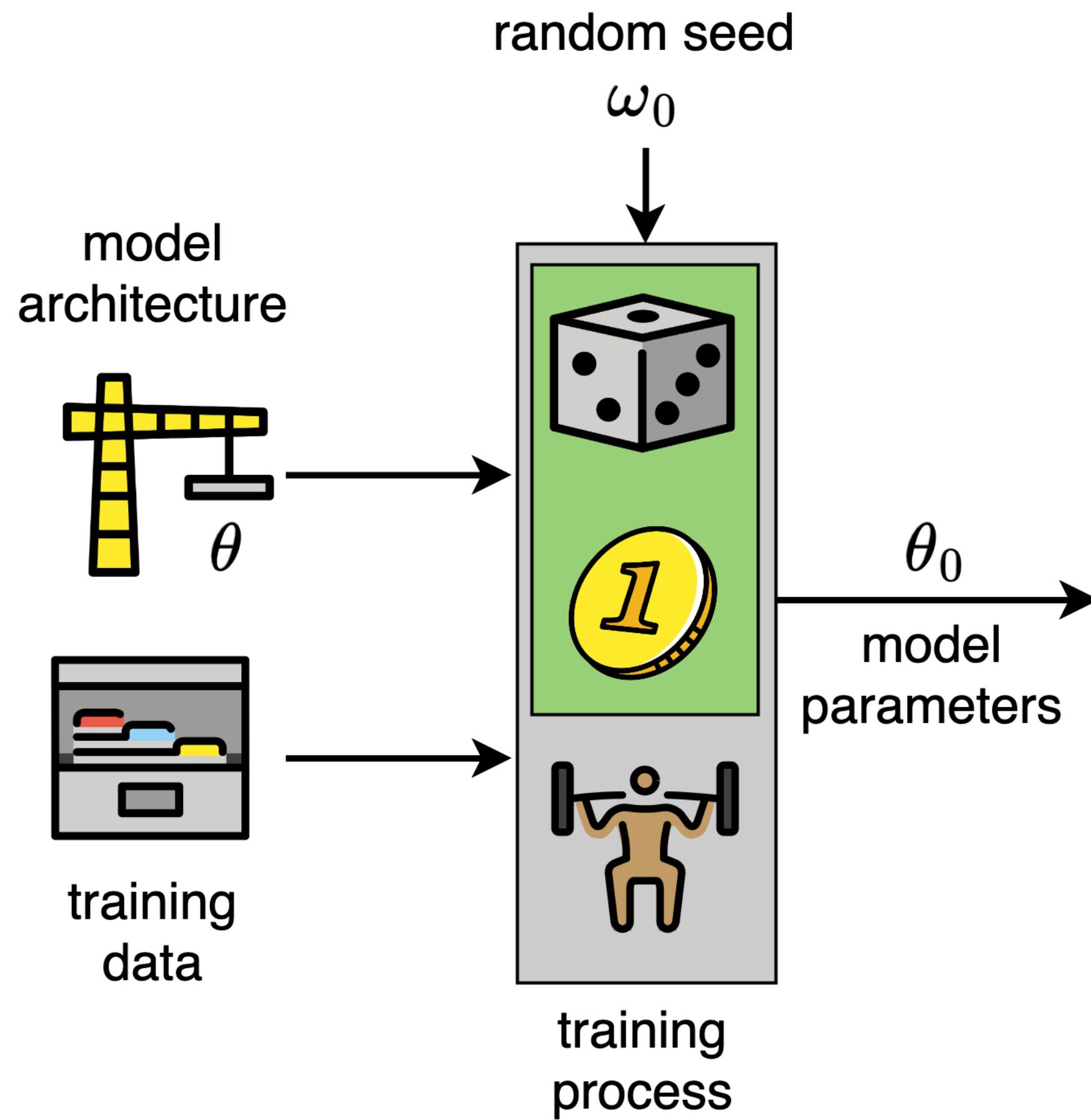
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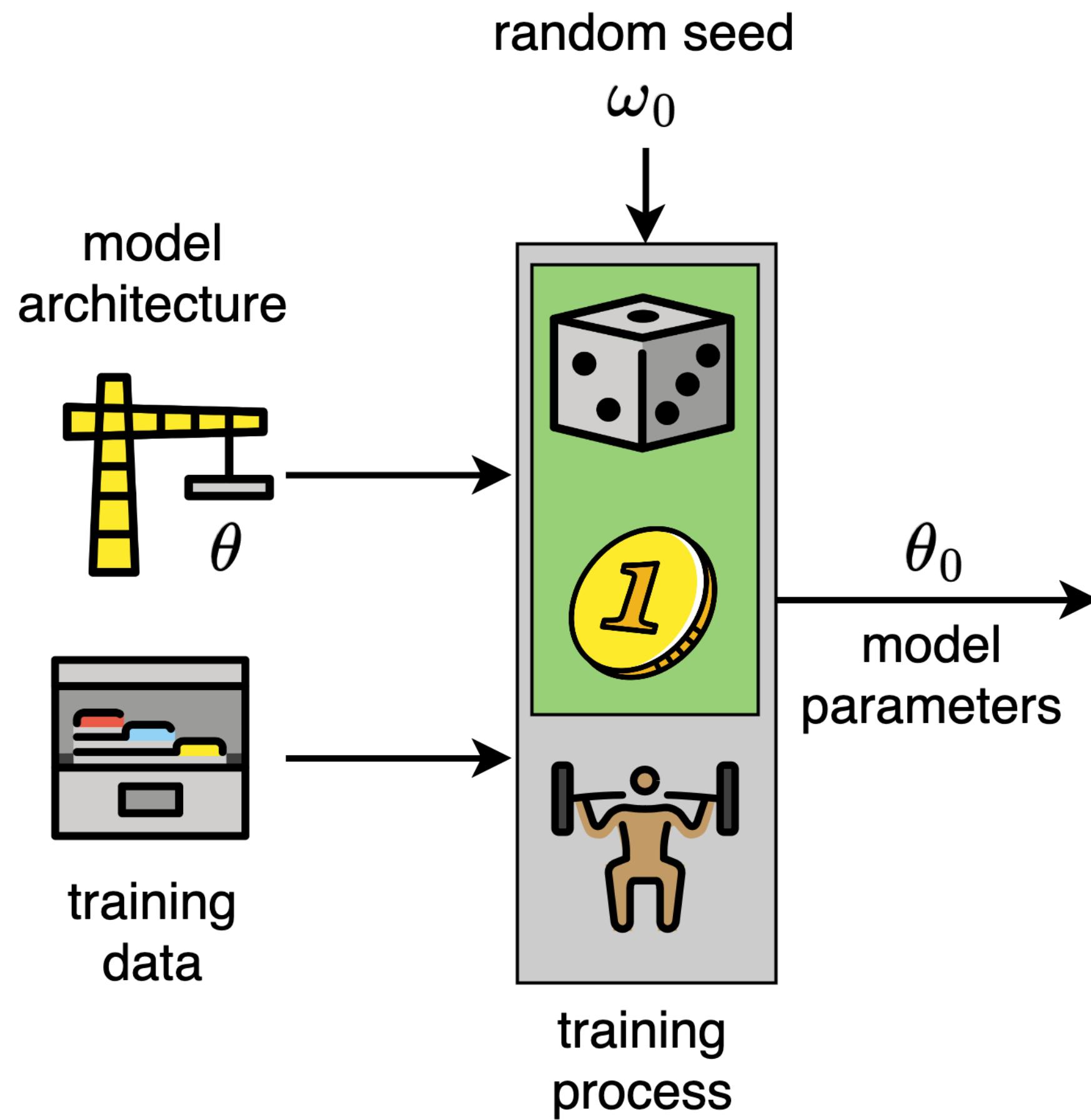


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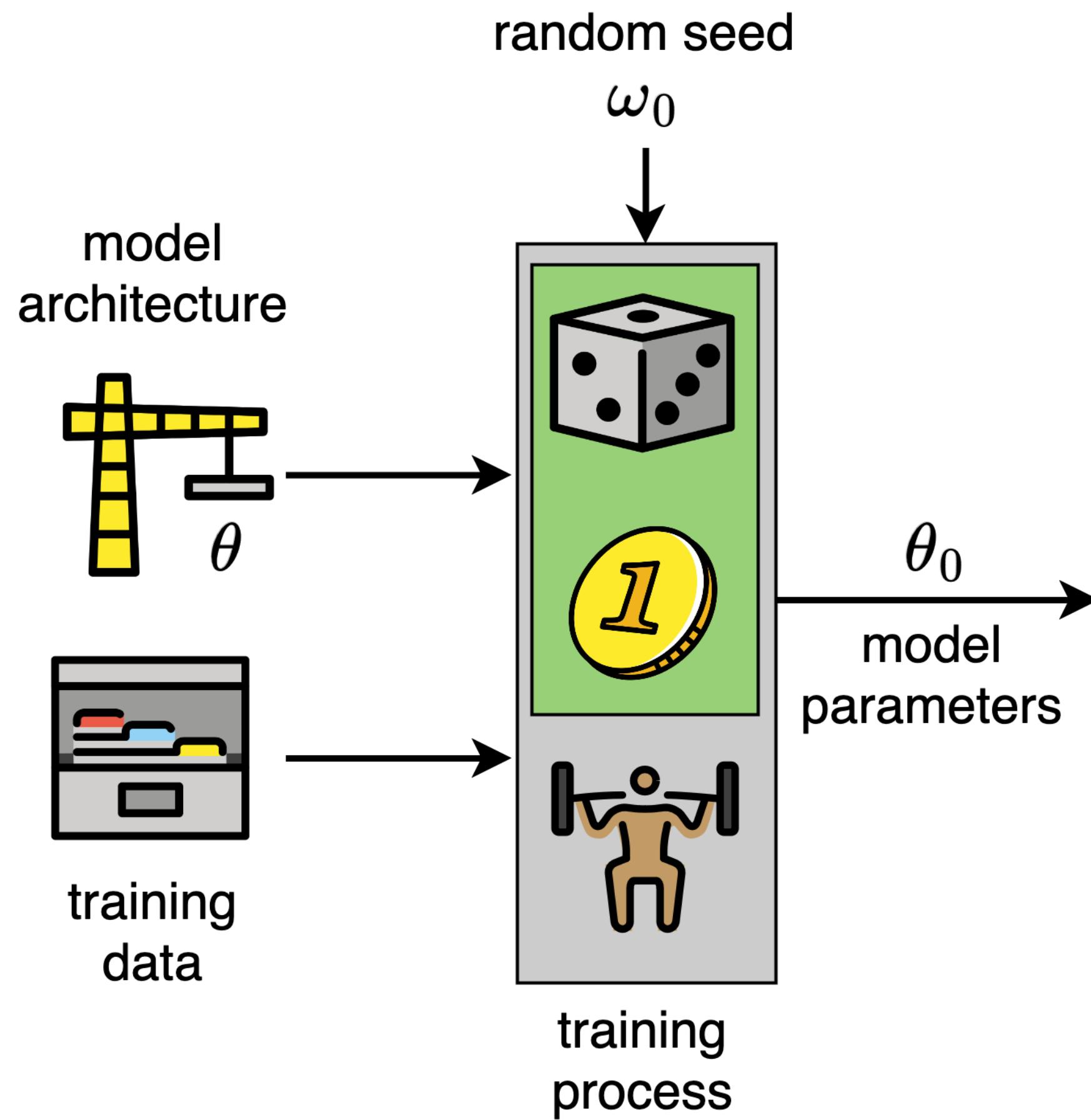


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- Stochastic optimization algorithm that does the actual minimization.

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- In representation learning, each  $f: \mathcal{X} \rightarrow \mathcal{R}$  maps inputs to representations/embeddings.

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- If  $\mathcal{F} = \mathcal{G}$  we can use their outputs to do a comparison.
- If  $\mathcal{F} \neq \mathcal{G}$  we need some way to do a comparison.

# Variability in the training process

Is training reliable?



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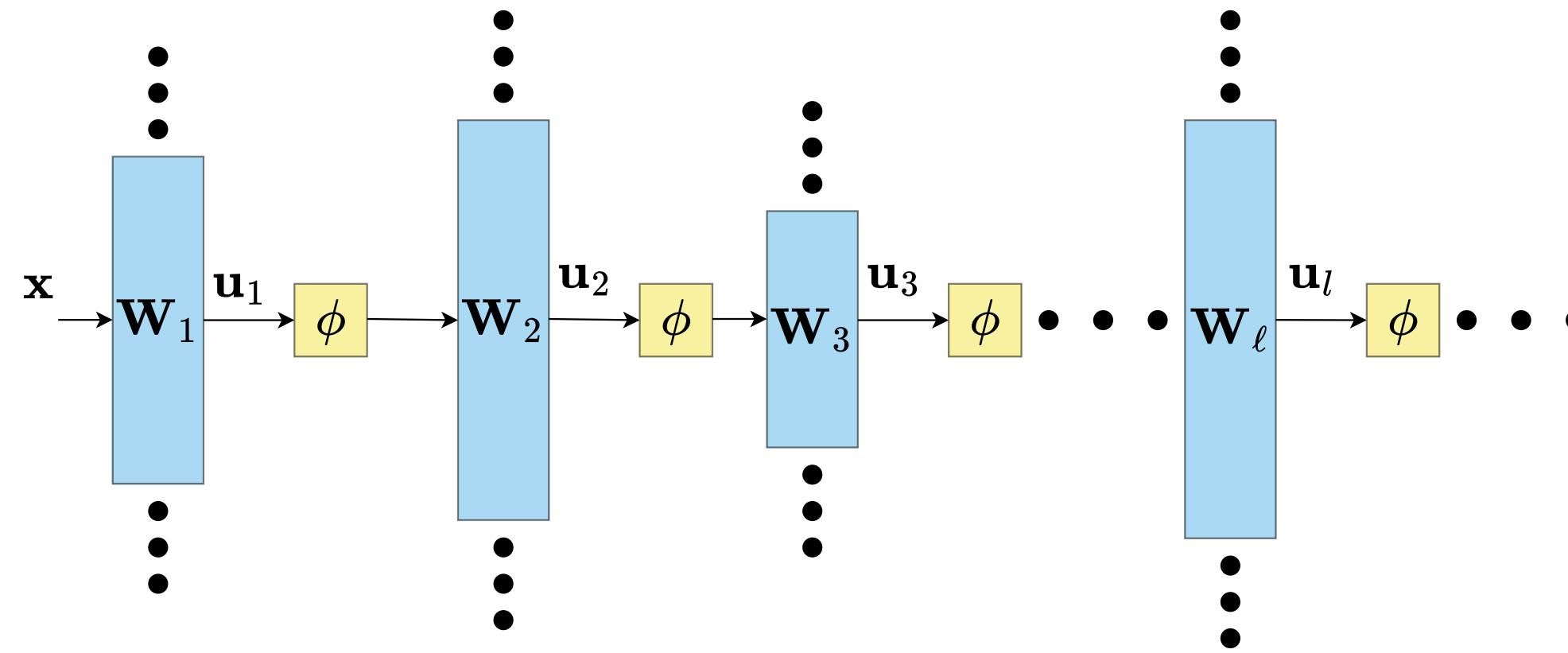
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If we have two different architectures  $\mathcal{F}$  and  $\mathcal{G}$  with different output spaces, how can we measure their similarity?

- Focus on **performance**: two models with the same error are “effectively the same”.
- Focus on **features**: come up with a mapping from one model to the other to show they are the same.
- Focus on **approximations**: use proxies for each model which are more comparable.

# Approximating the NN with a kernel machine

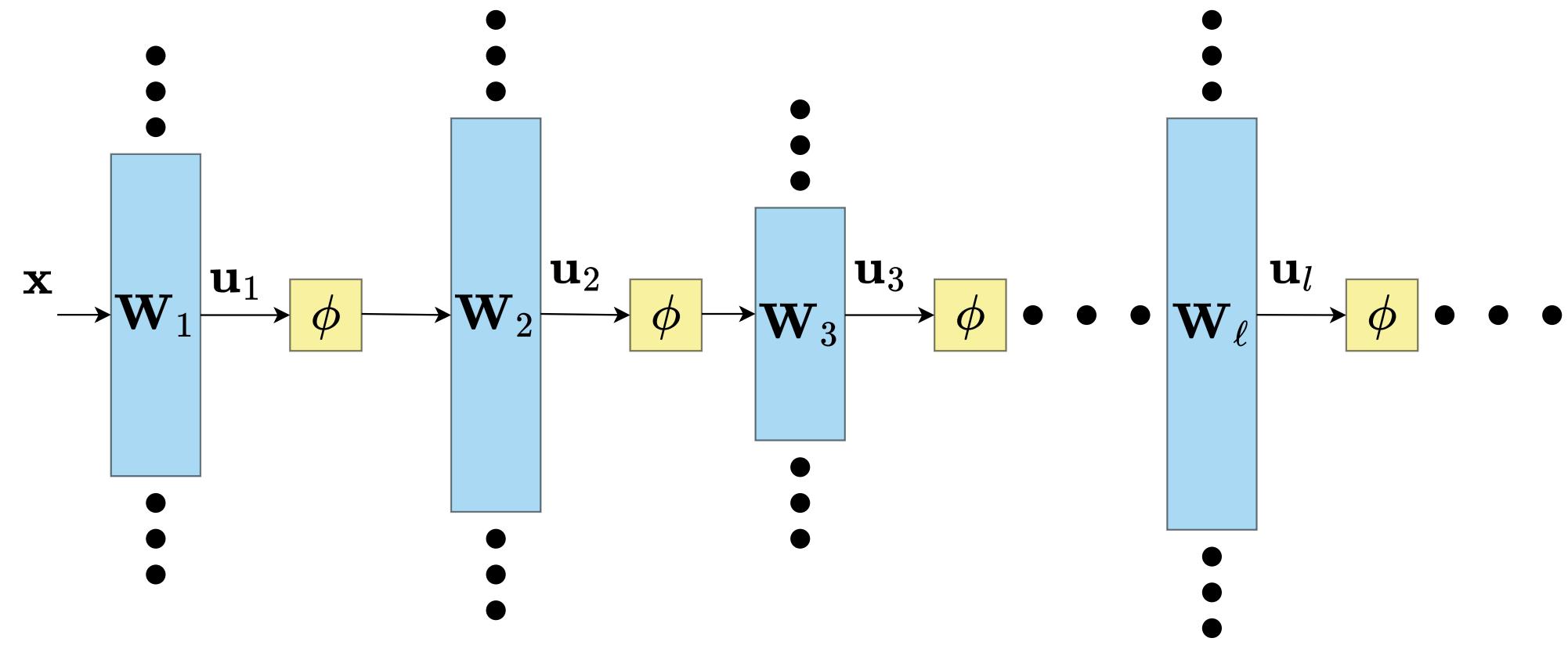
Not practical, but perhaps informative?



$\approx$   
kGLM

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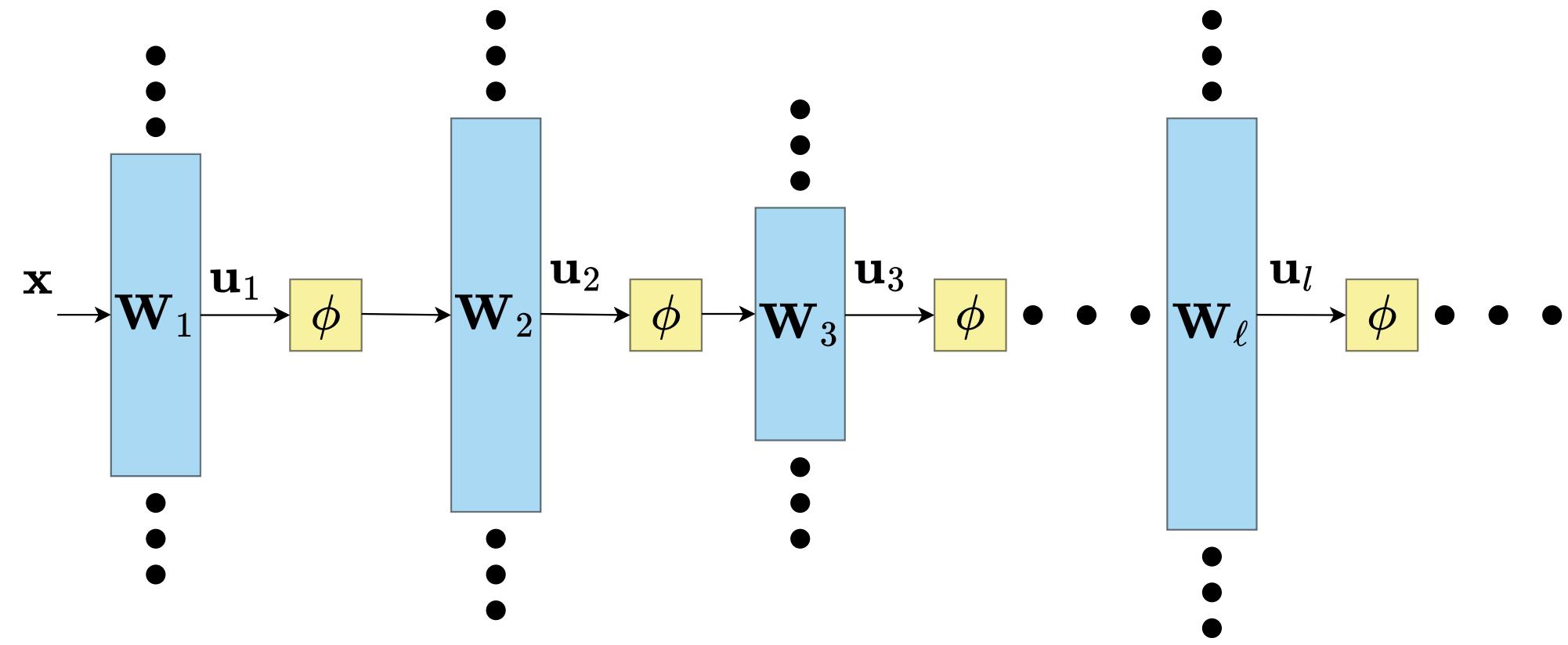
Suppose we compute some kernel function  $\mathbf{K}$  associated to the model and fit a **surrogate model**  $(\mathbf{V}, \mathbf{b})$ :

$$\mathbf{y}_i = \mathbf{VK}(\mathbf{x}_i, \mathbf{X}) + \mathbf{b}$$

where  $\mathbf{y}_i, \mathbf{b} \in \mathbb{R}^C$  and  $\mathbf{V} \in \mathbb{R}^{C \times N}$ . Fitting is done with the same training data (double dipping).

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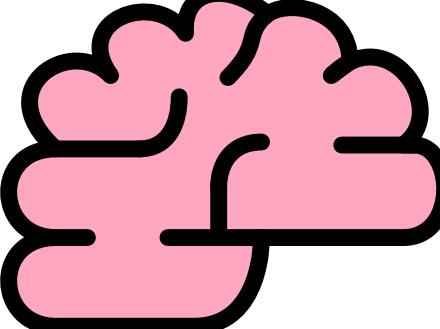
One example: the **neural tangent kernel**.

# Neural Networks as Kernel Machines

Approximating an NN with a “simpler” model

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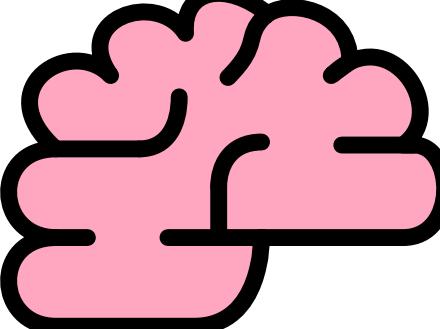
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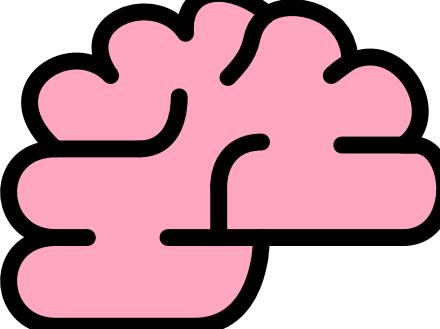


Jacot et al. (2018) showed that **infinitely wide** NNs are equivalent to a kernel machine with the “**neural tangent kernel**” (NTK):

$$K(\mathbf{x}, \mathbf{x}') = \langle \nabla_{\theta} f(\mathbf{x}; \theta), \nabla_{\theta} f(\mathbf{x}'; \theta) \rangle$$

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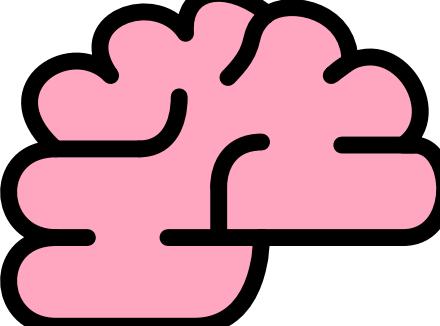
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Finite width networks don’t really behave like infinite width networks... (Chizat et al., 2018; Yang & Hu, 2021; Wang et al., 2022).

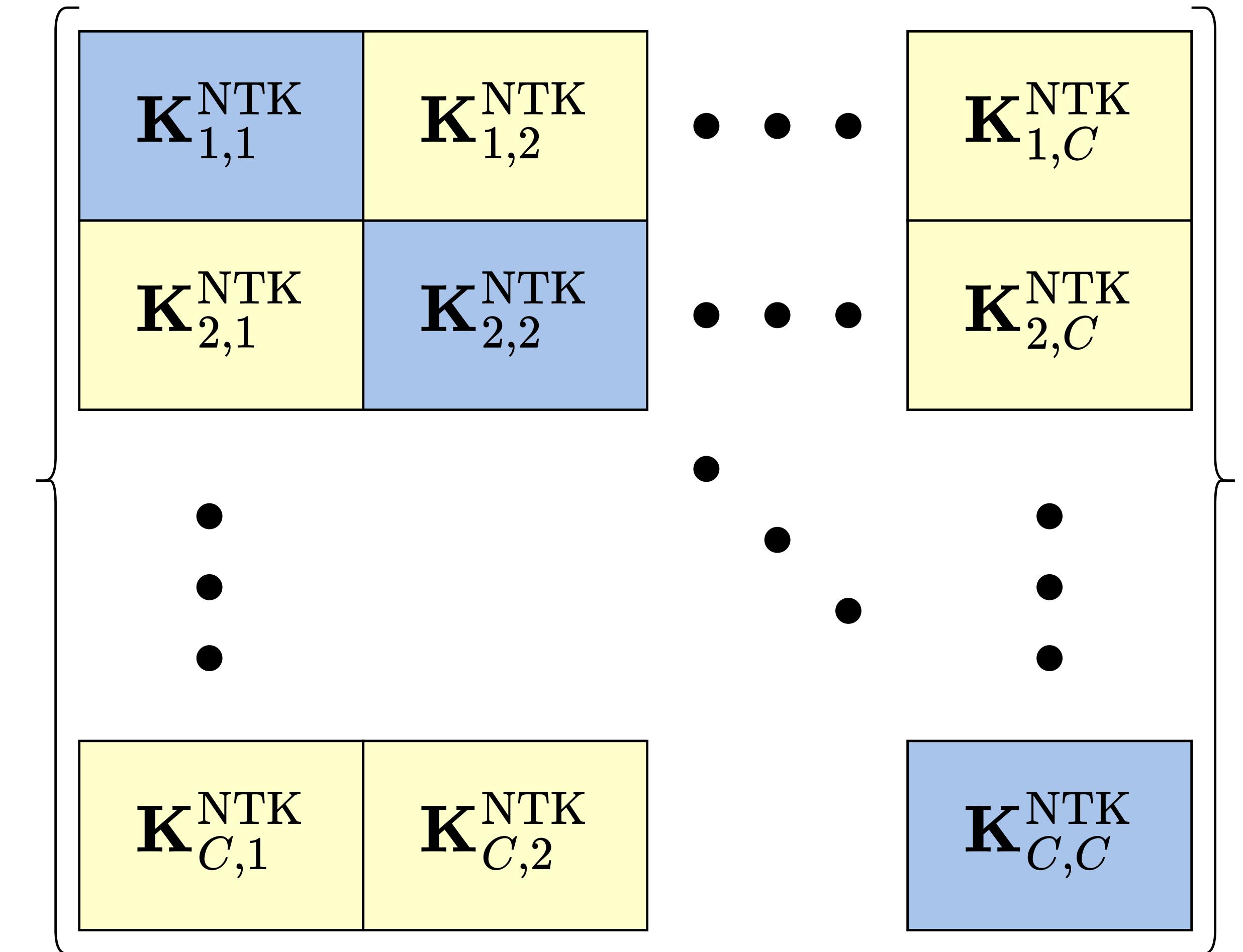
# Challenge: NTK is asymptotic (infinite width)

## Writing an empirical version of the NTK

We would like to handle multi-class problems and large data sets. In the setting **the empirical NTK becomes huge**. For classes  $i$  and  $j$  define:

$$\mathbf{K}_{(c,c')}^{\text{NTK}}(\mathbf{x}_i, \mathbf{x}_j) = \left\langle \nabla_{\theta} f^c(\mathbf{x}_i; \theta), \nabla_{\theta} f^{c'}(\mathbf{x}_j; \theta) \right\rangle$$

Then the NTK has a block structure, where each diagonal block has the “regular” NTK for each class and the off-diagonal blocks are cross terms.



# Trace NTK: a proxy for the eNTK

Much lower computational overhead needed

We look at a simplification of the NTK:

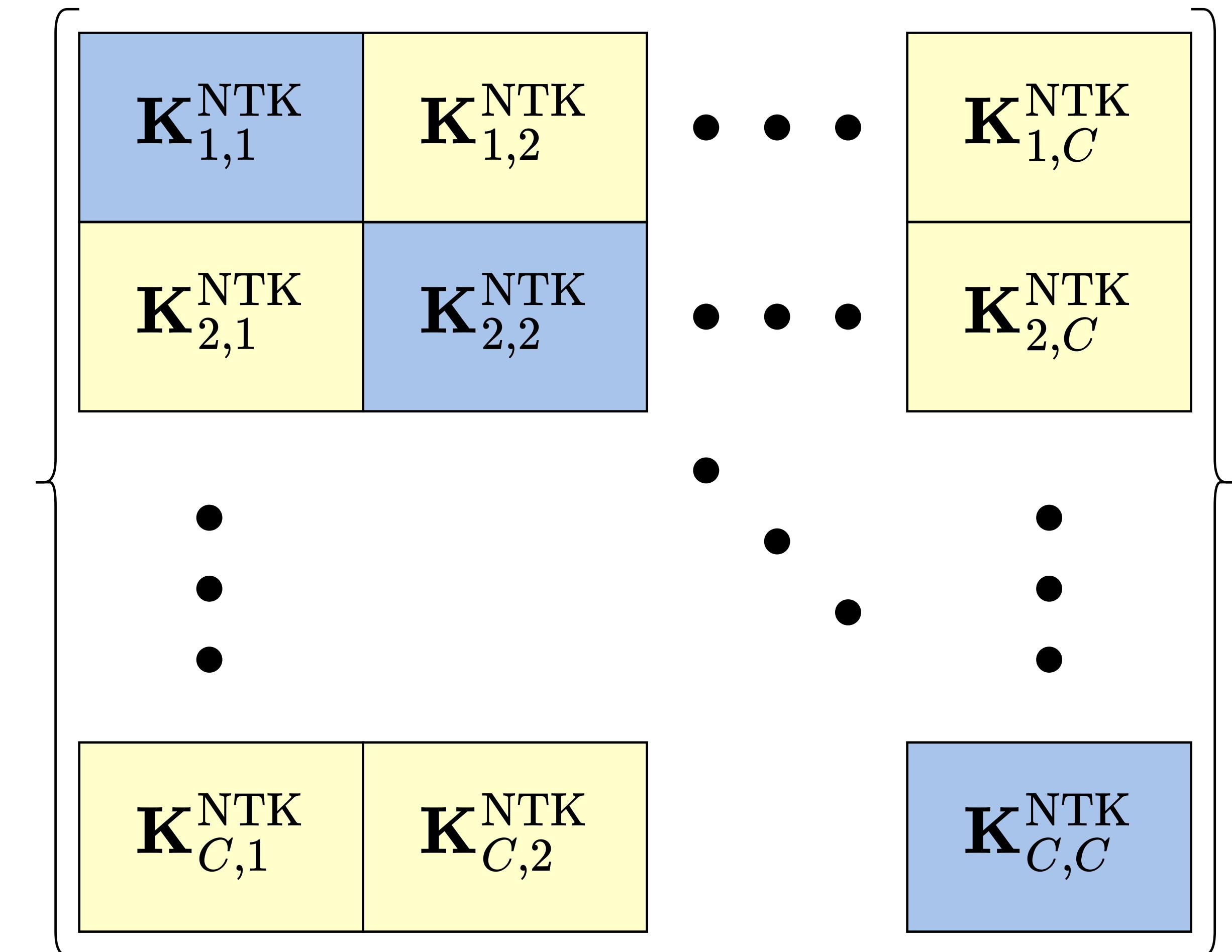
$$K^{\text{trNTK}}(x_i, x_j) = \frac{\sum_{c=1}^C \left\langle \nabla_{\theta} f^c(x_i; \theta), \nabla_{\theta} f^c(x_j; \theta) \right\rangle}{\left( \sum_{c=1}^C \|f^c(x_i; \theta)\|^2 \right)^{1/2} \left( \sum_{c=1}^C \|f^c(x_j; \theta)\|^2 \right)^{1/2}}$$

This is **different from other surrogate kernels**: the pseudo NTK (pNTK) (Mohamadi & Sutherland, 2022), things based on the CK (Fan & Wang, 2020; Yeh et al., 2018), the un-normalized trNTK, and the embedding kernel (Akyürek et al., 2023).

**Fast to compute**, also with random projections (Novak et al., 2022, Park et al., 2023))

# Some takeaways from the setup

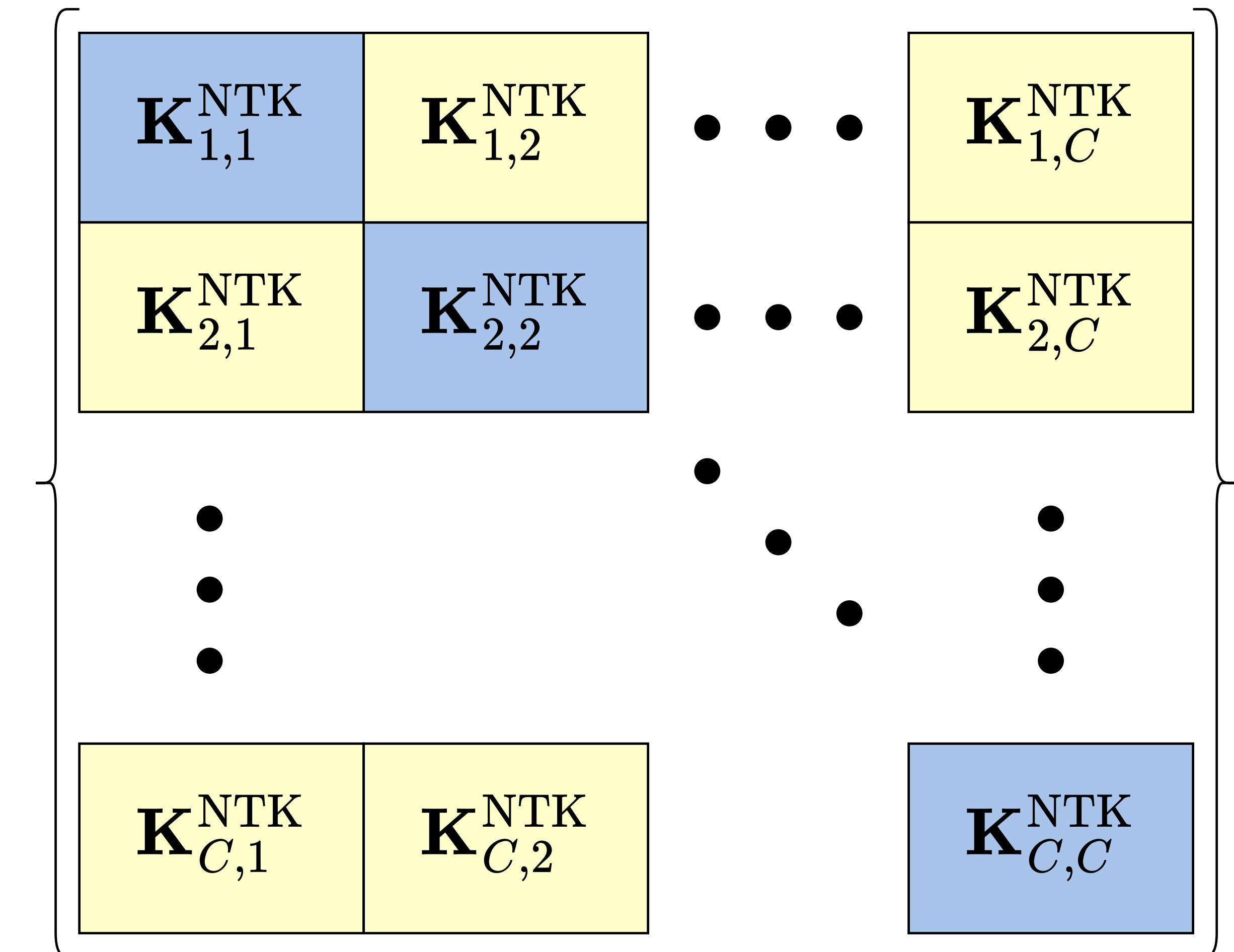
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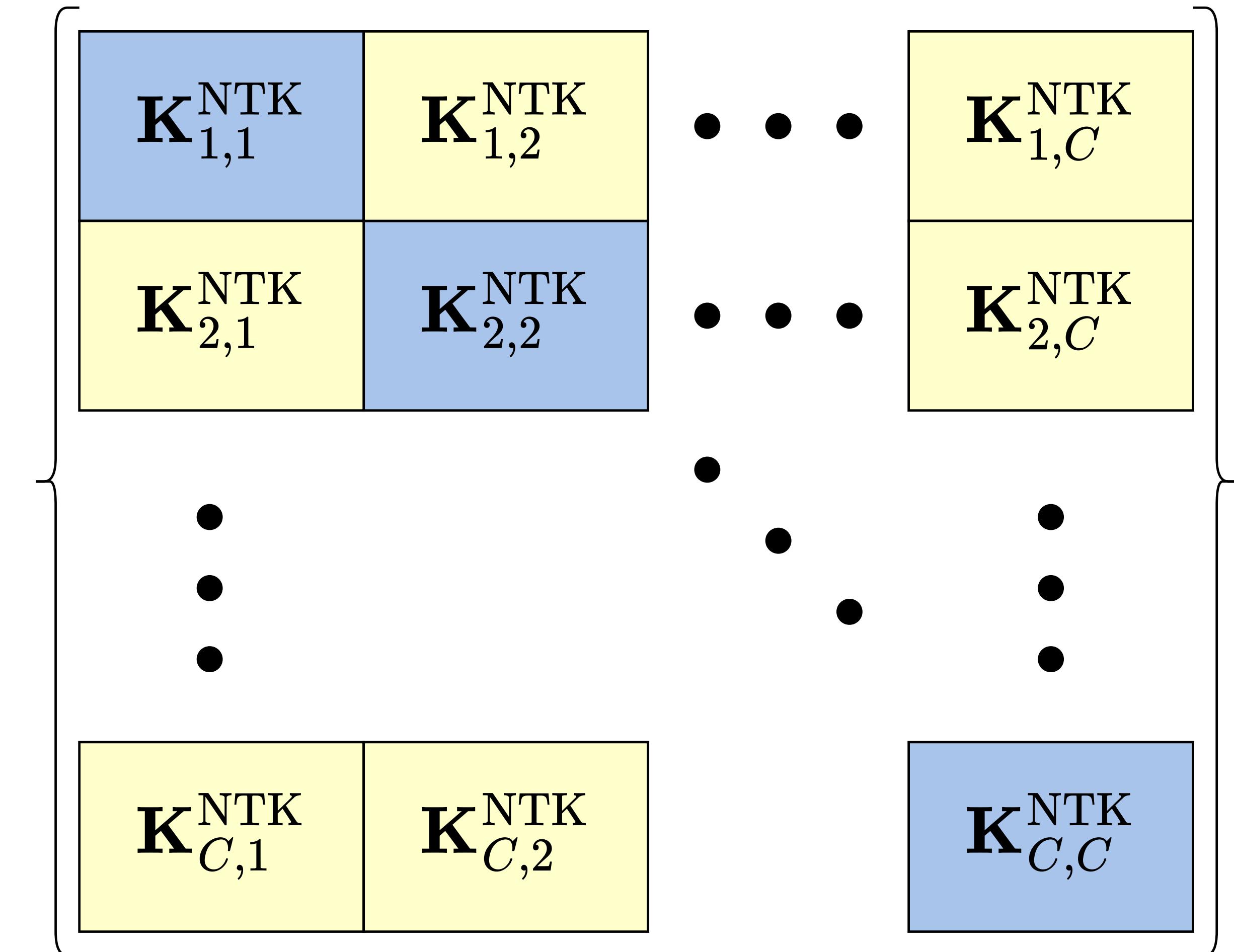


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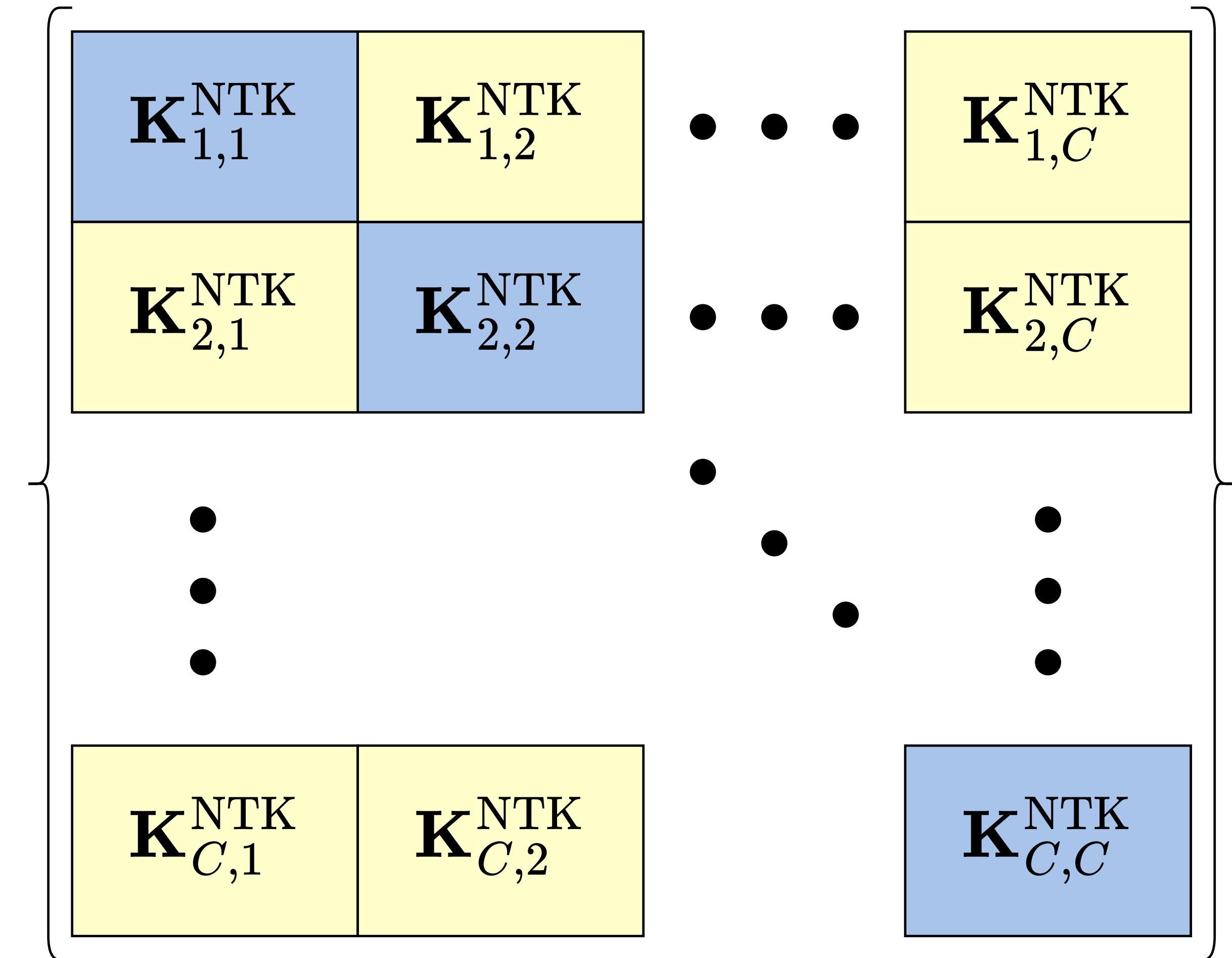


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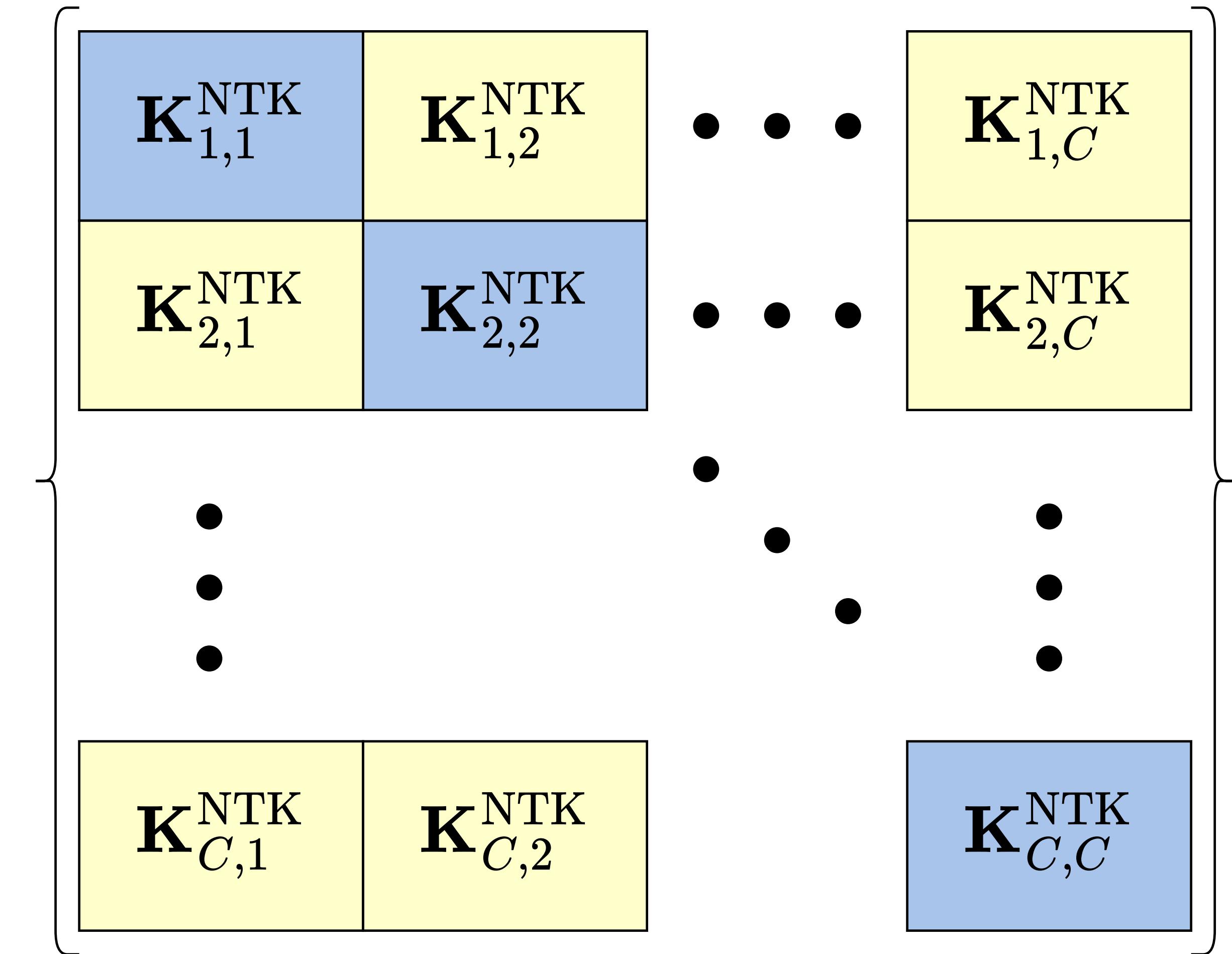


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- Much easier if you have access to the training corpora.
- Challenging because of invariants.



# Embedding spaces and model comparisons



Rm Palaniappan, *Alien Planet-B*  
Viscosity, pencil colour and ink on handmade paper

# A question of interoperability

Challenges in collaborating with AI instruments



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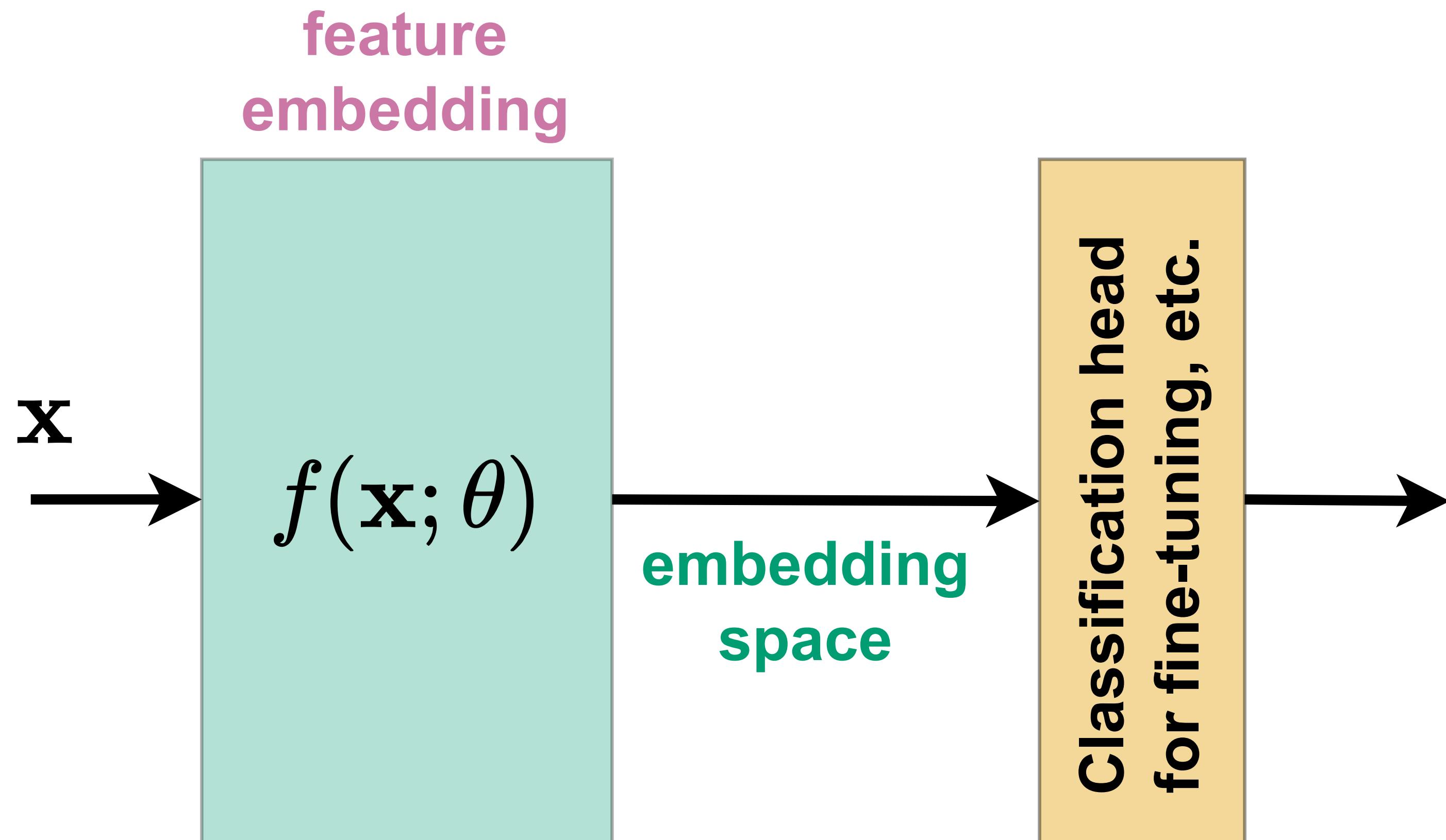
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- Can we quantitatively see if they are different?

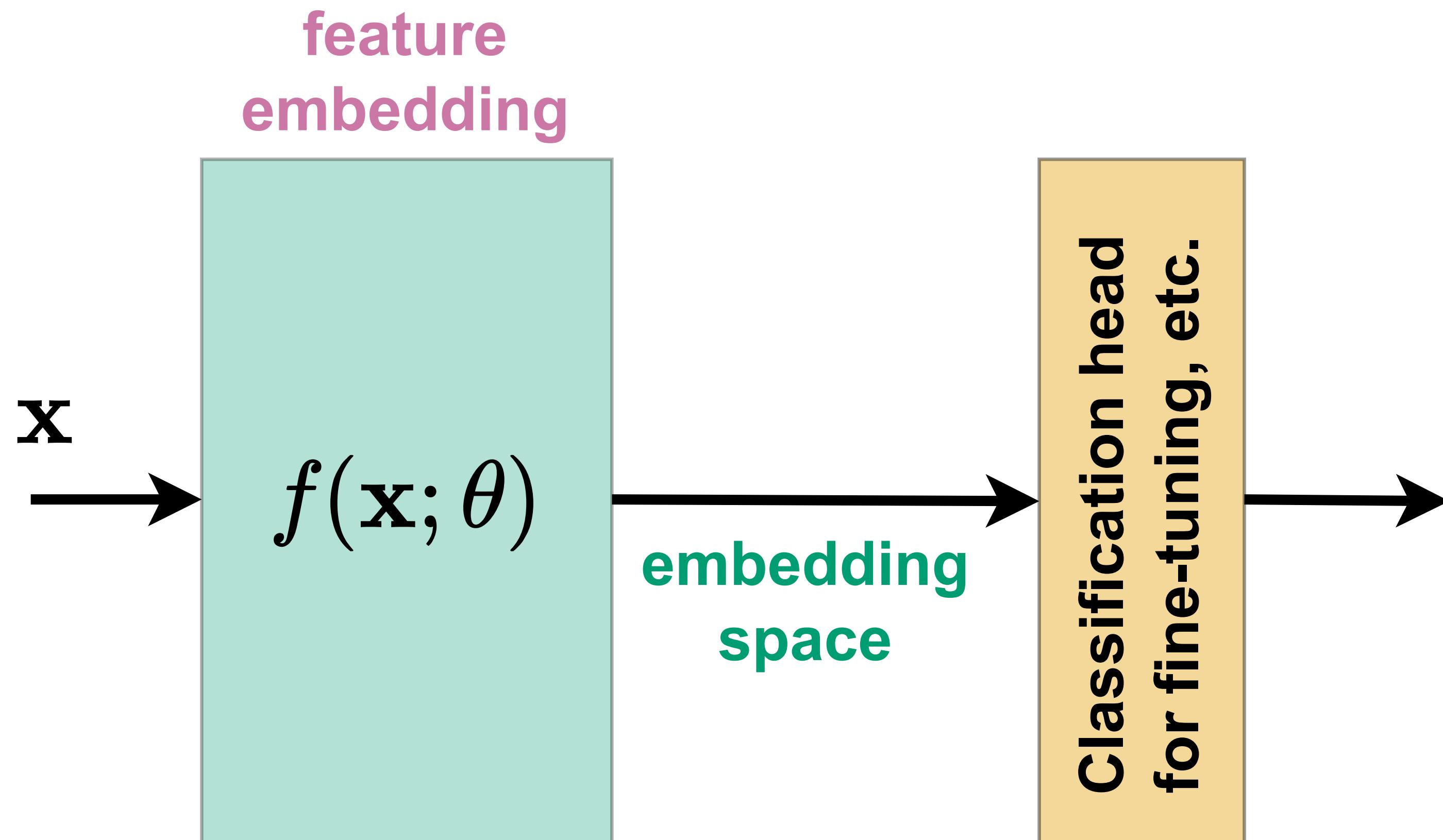
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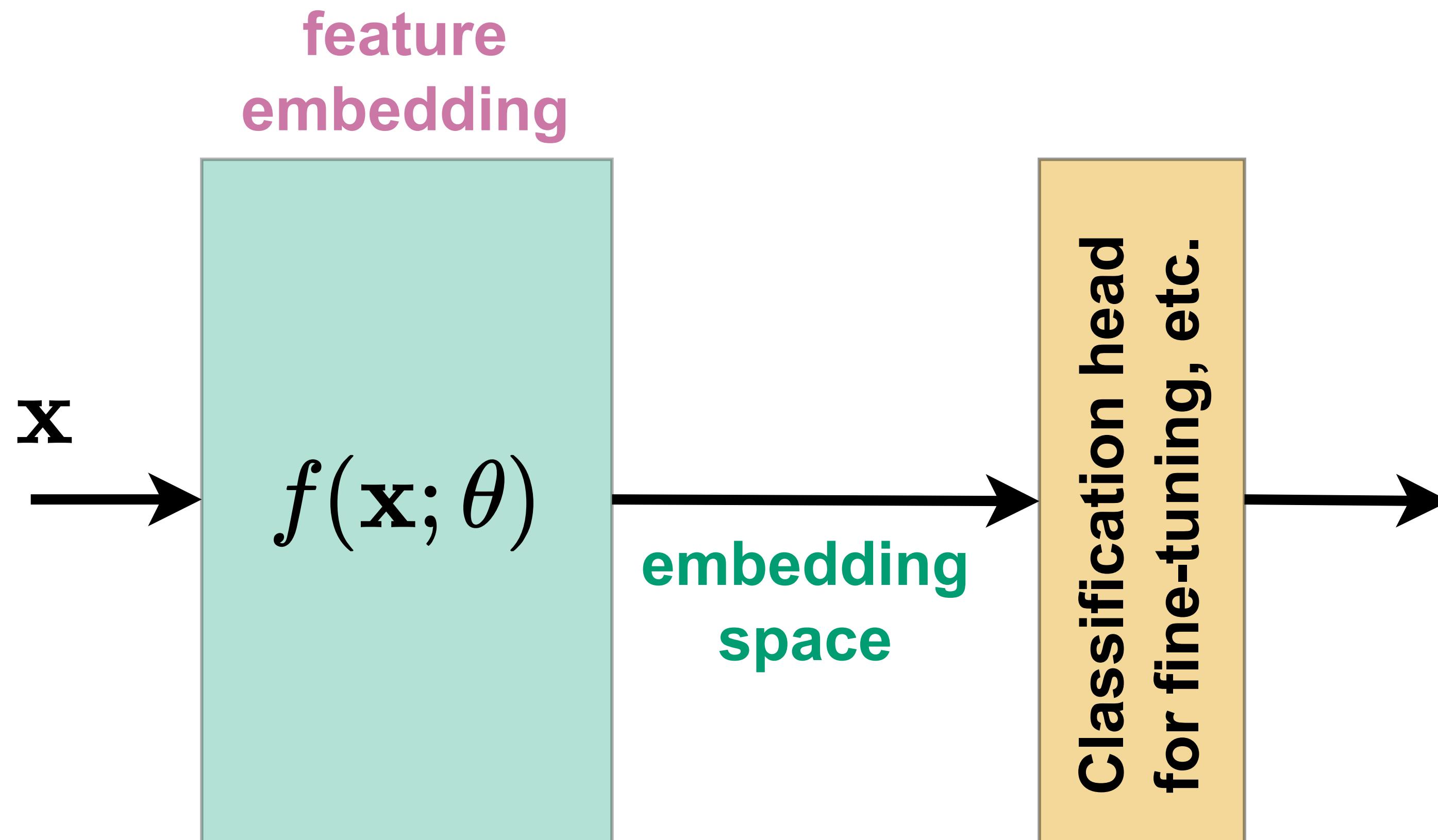
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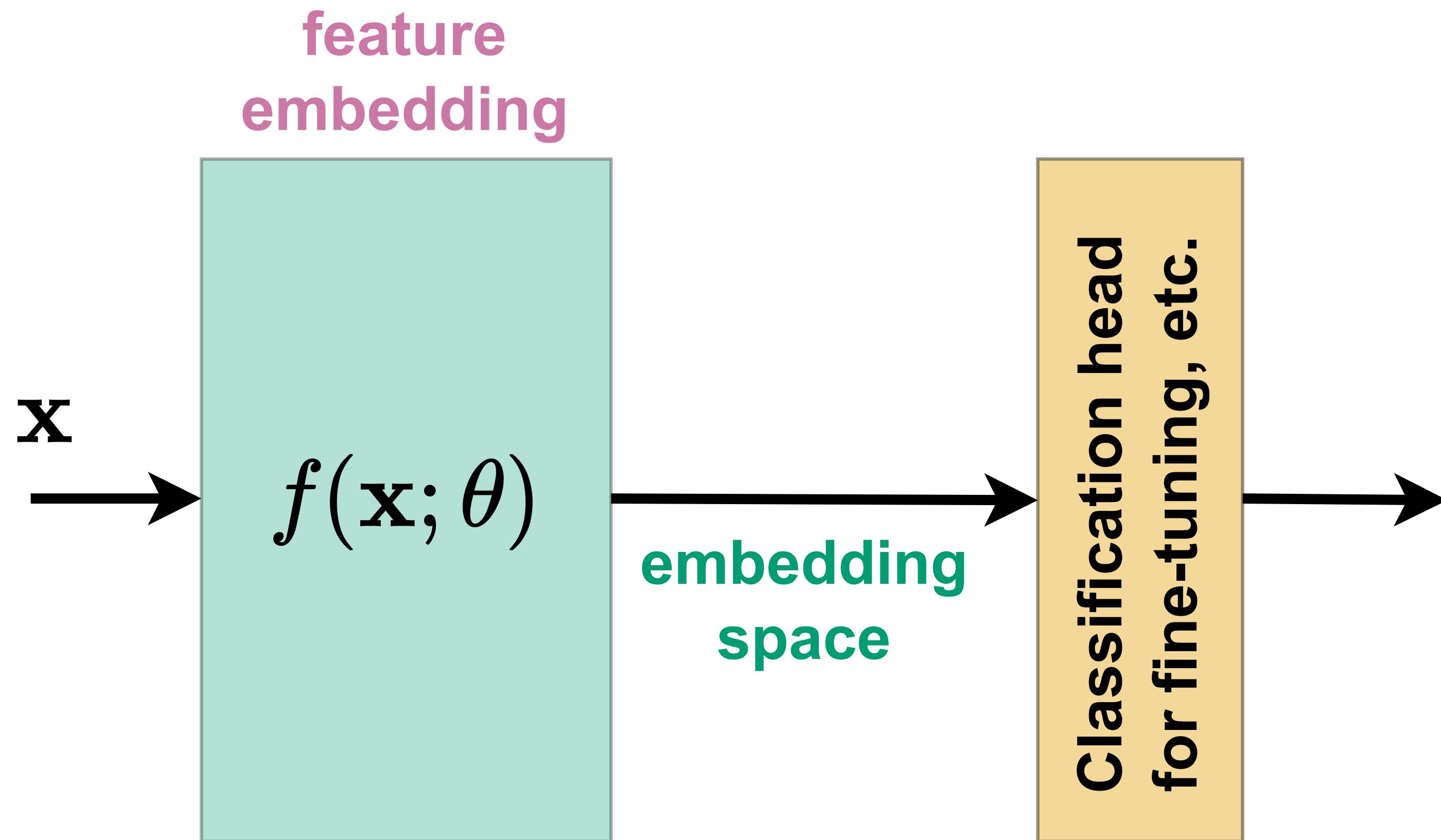


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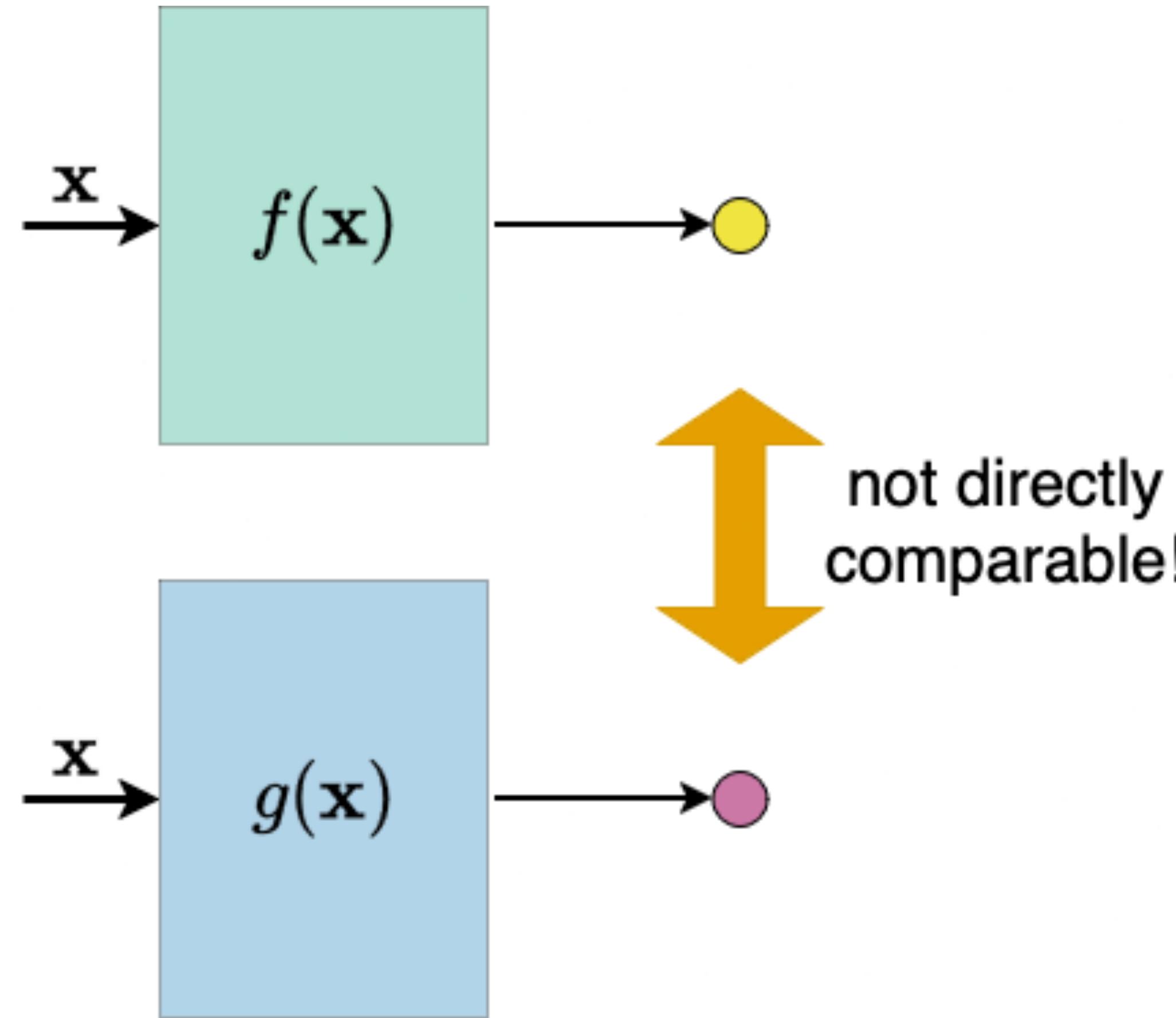
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**Idea:** can we compare the embedding spaces of models to tell the difference between them?

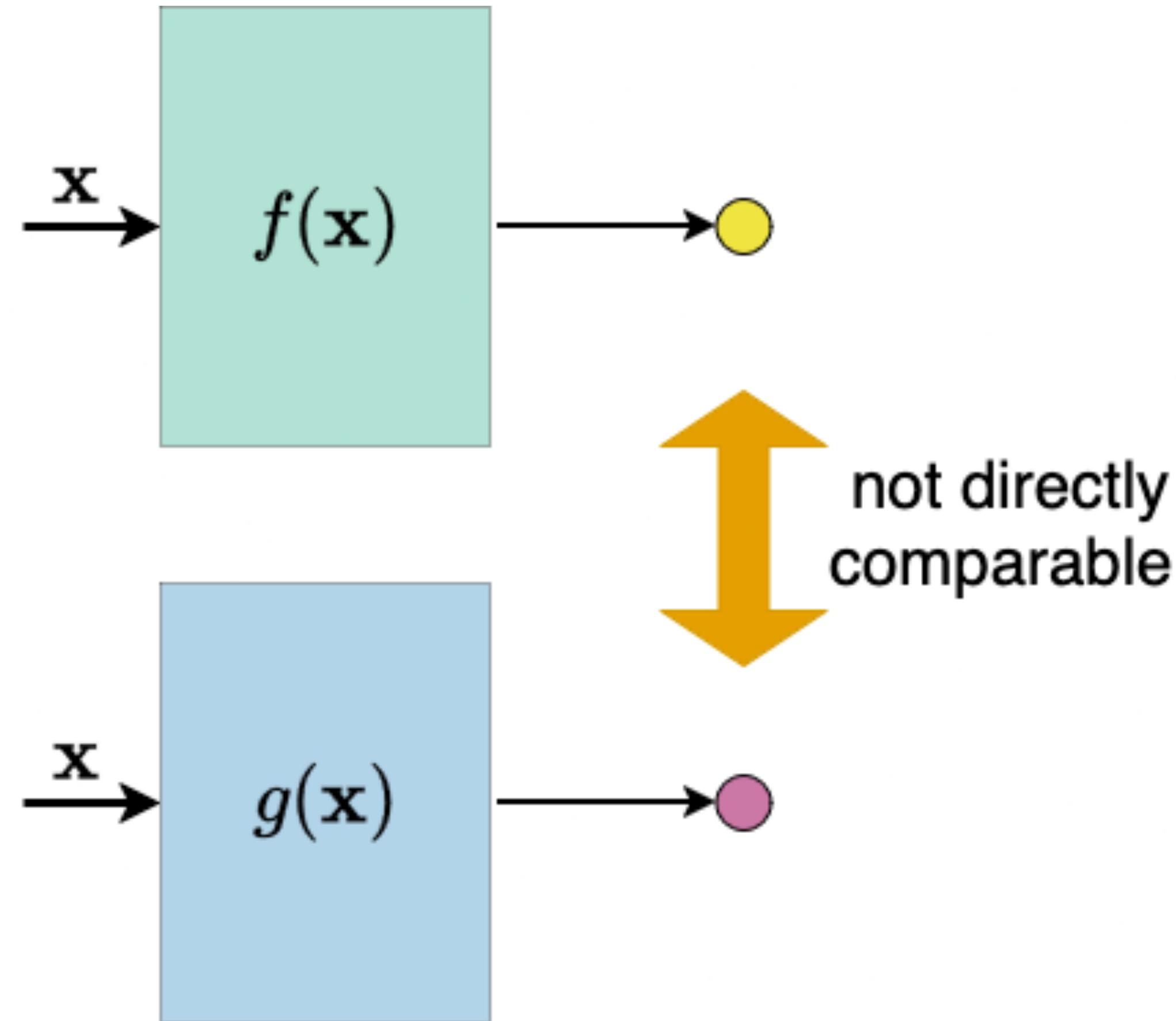
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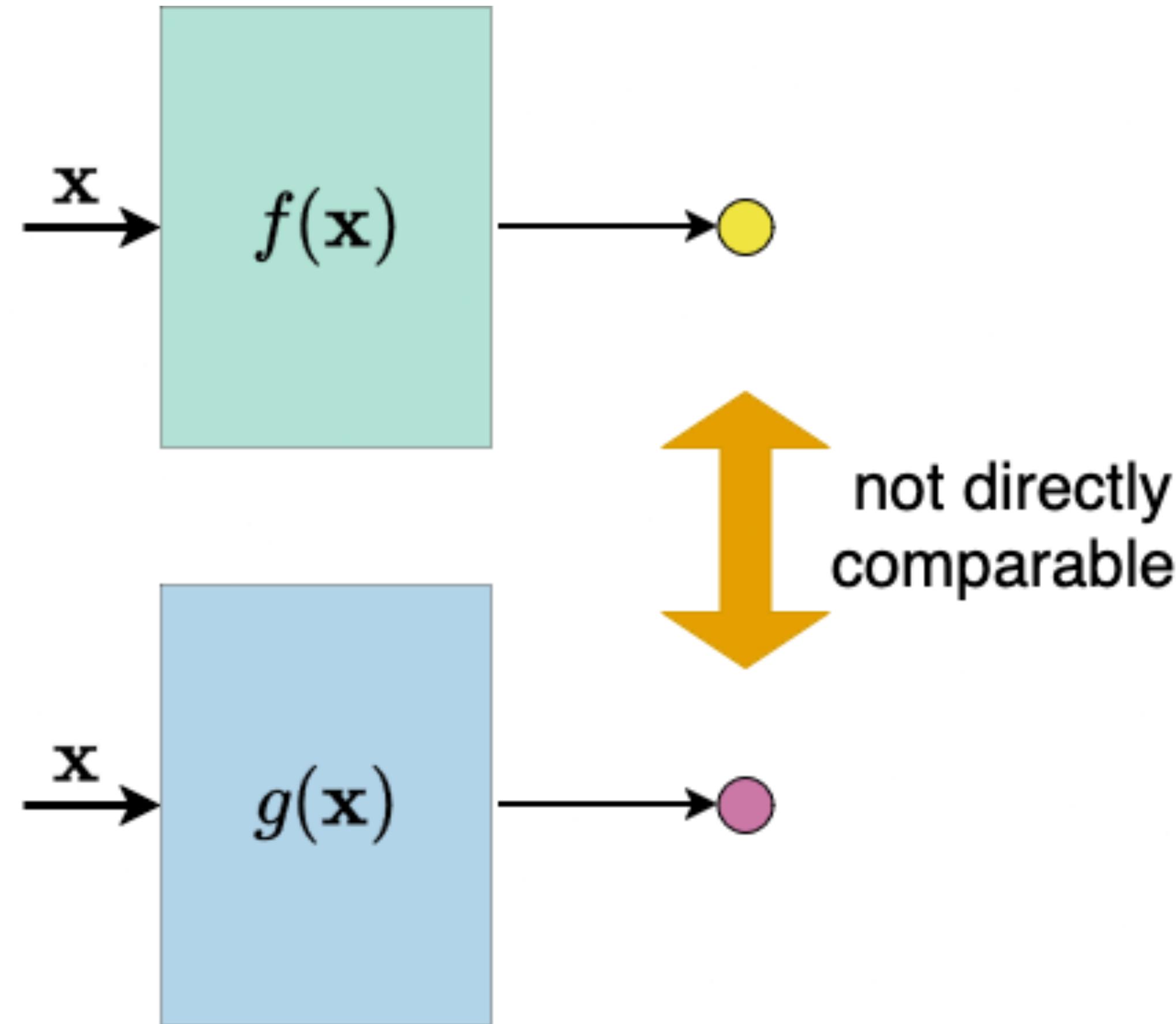
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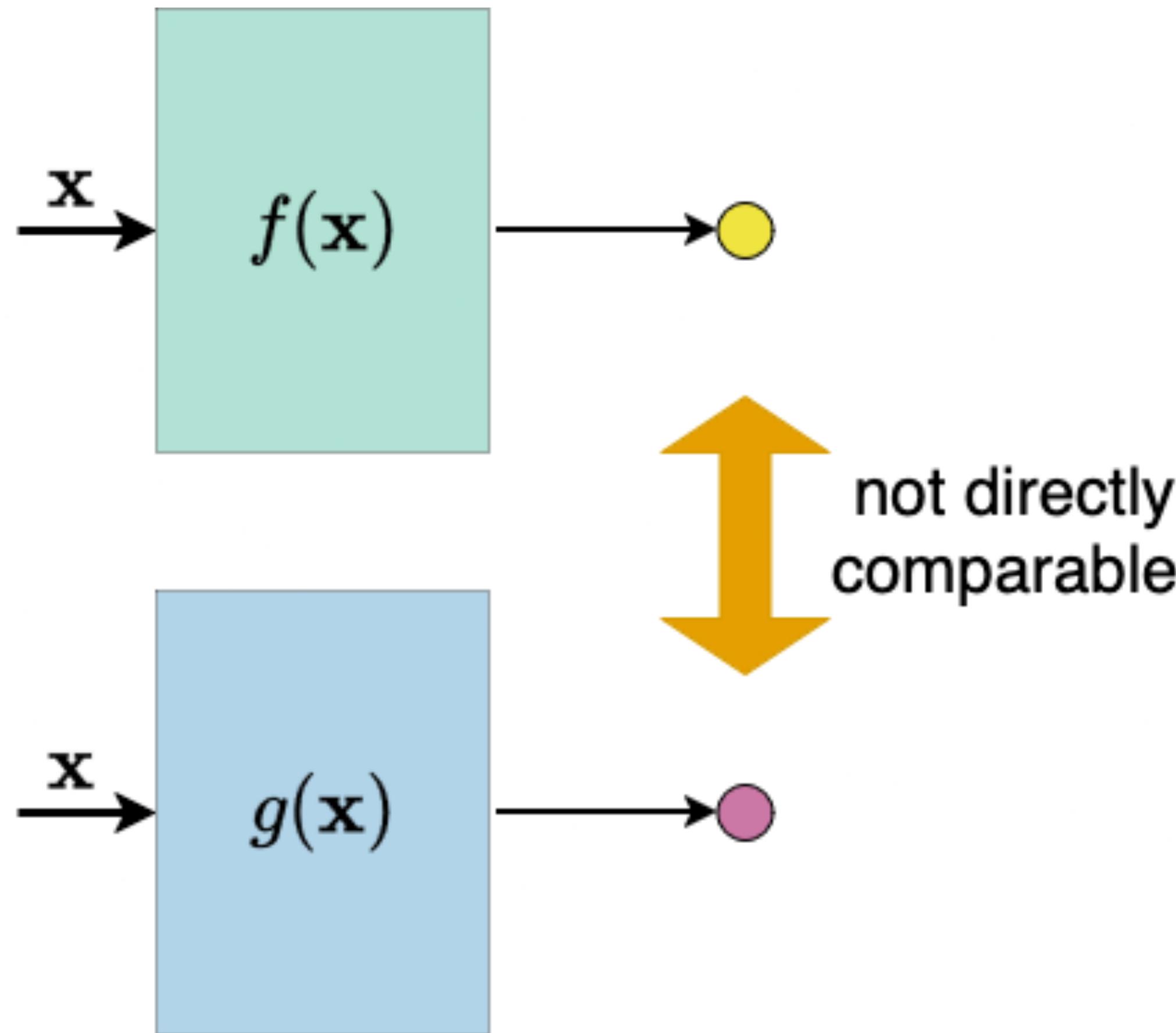


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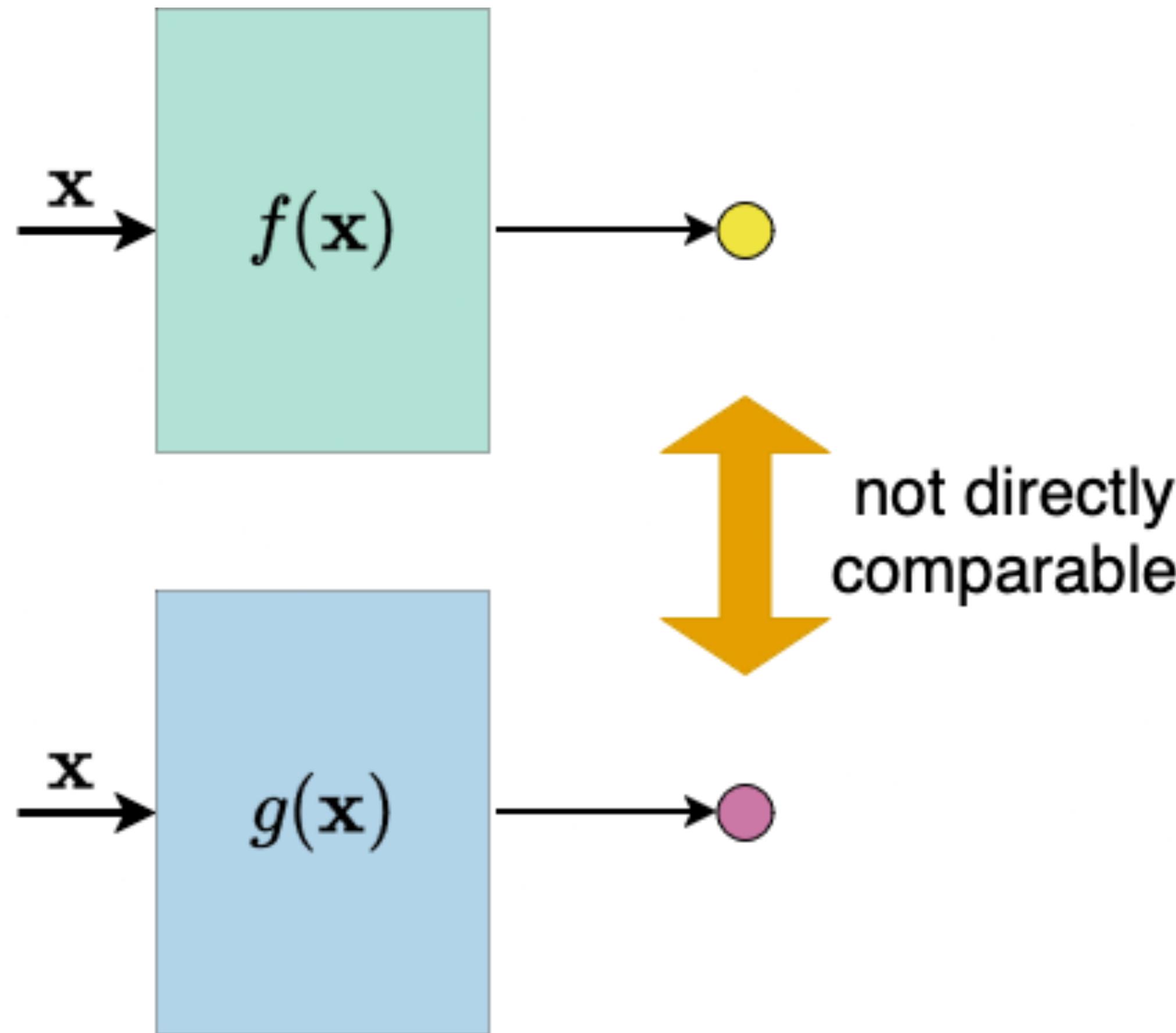


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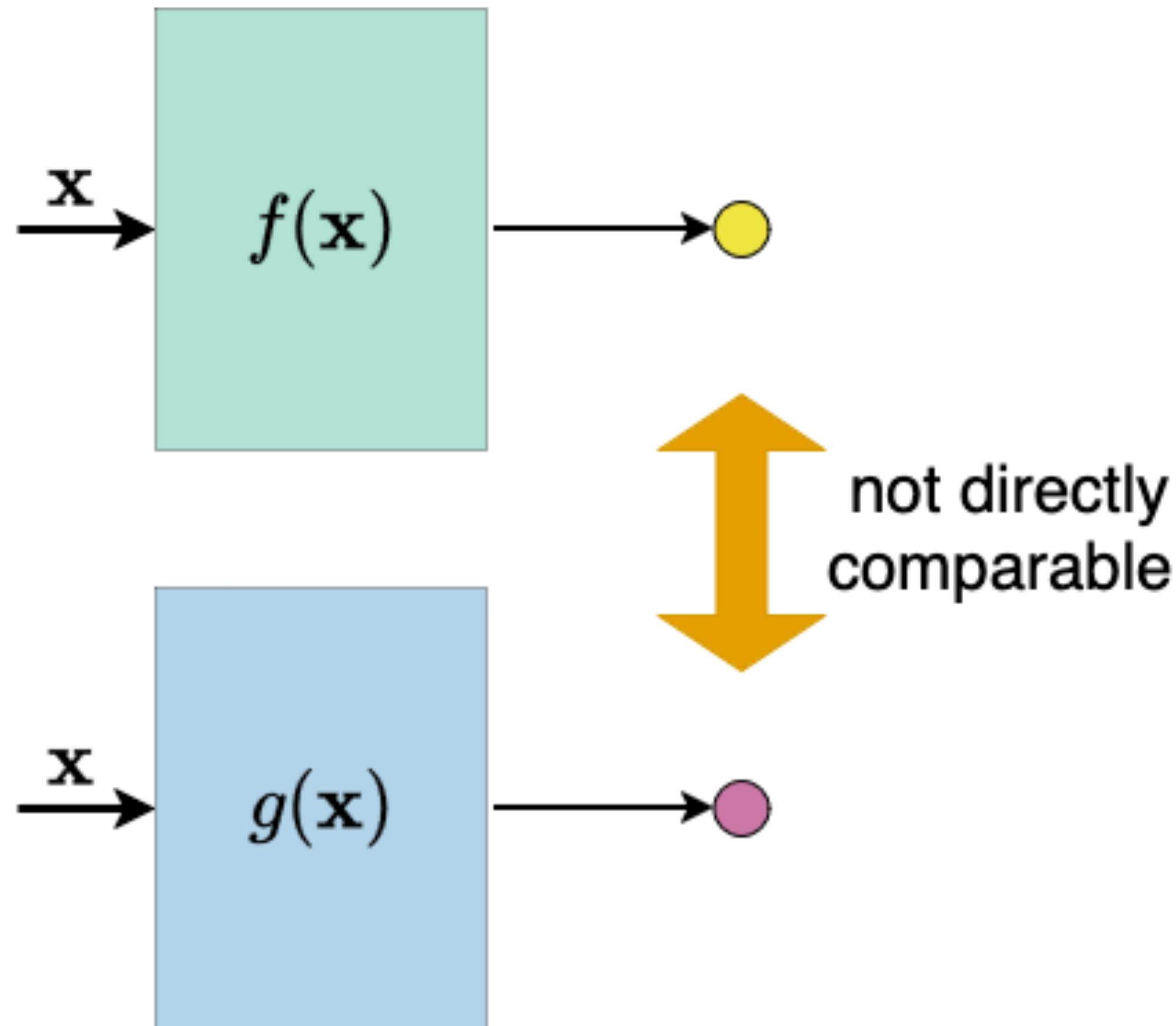


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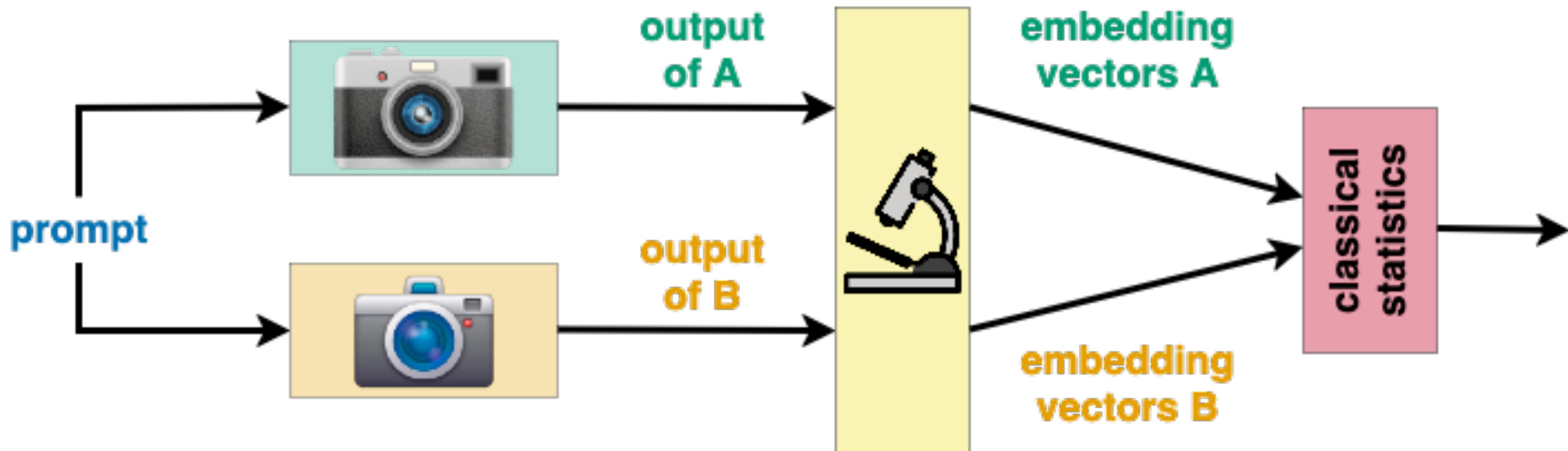
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Unlike with classification, we need to compare the outputs of the generative models.

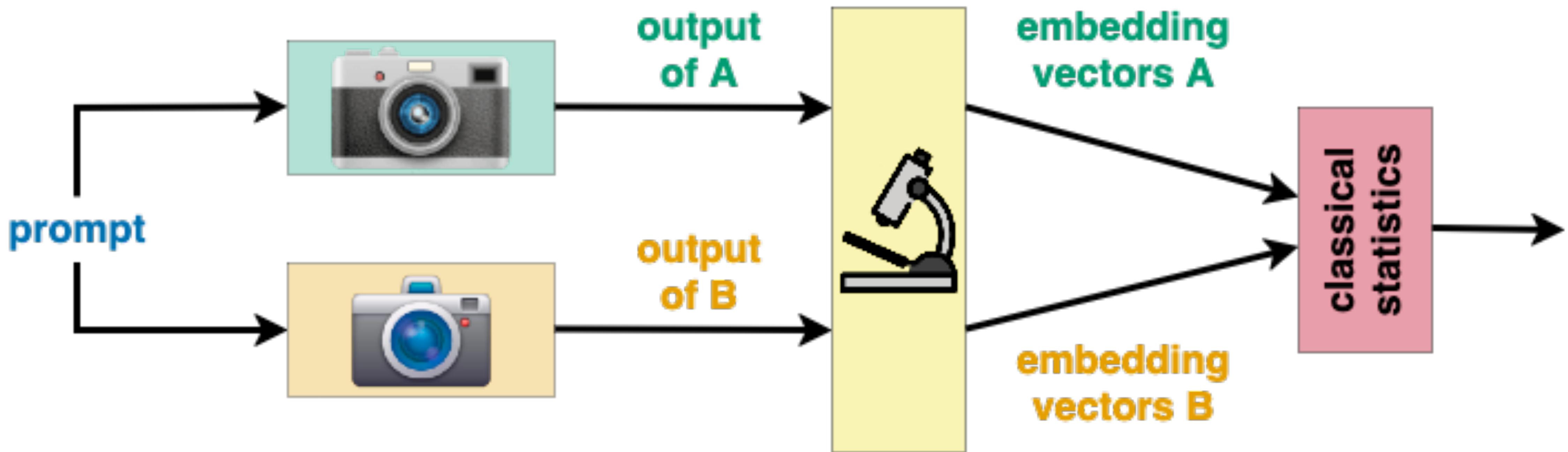
# Using a pre-trained model to distinguish

Use the embedding space to compare outputs of models



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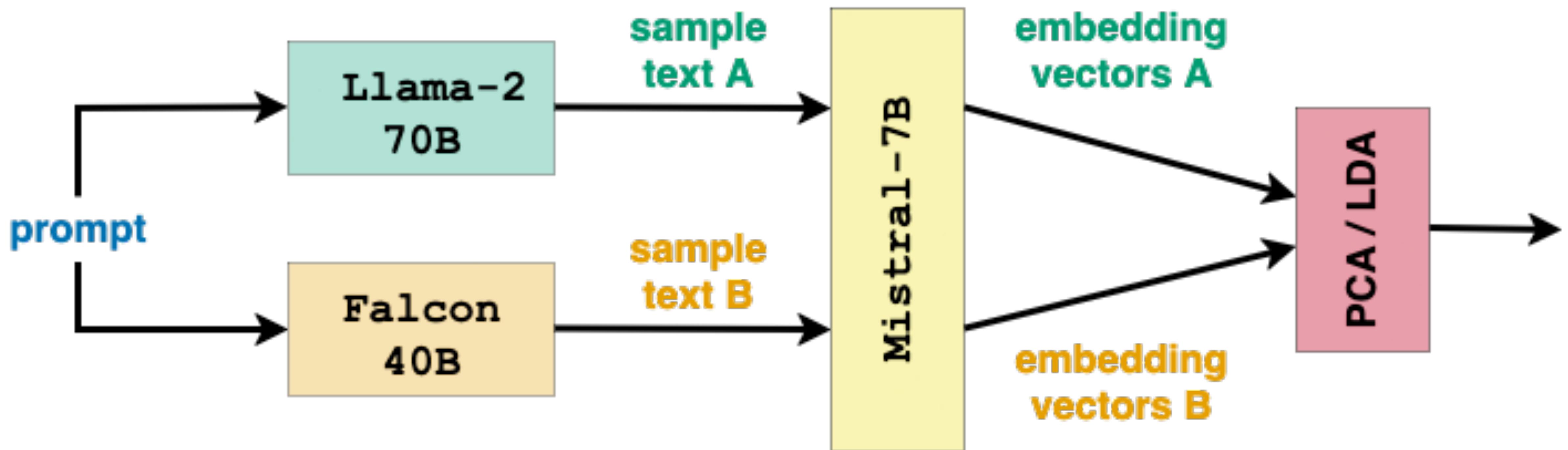
## Use the embedding space to compare outputs of models



**New idea:** use the embedding space of a **third AI model** as a “microscope” to compare the outputs of two AI models.s

# A specific example for GenAI

Compare the outputs using a 3rd model for embedding



# Using a large model as an instrument

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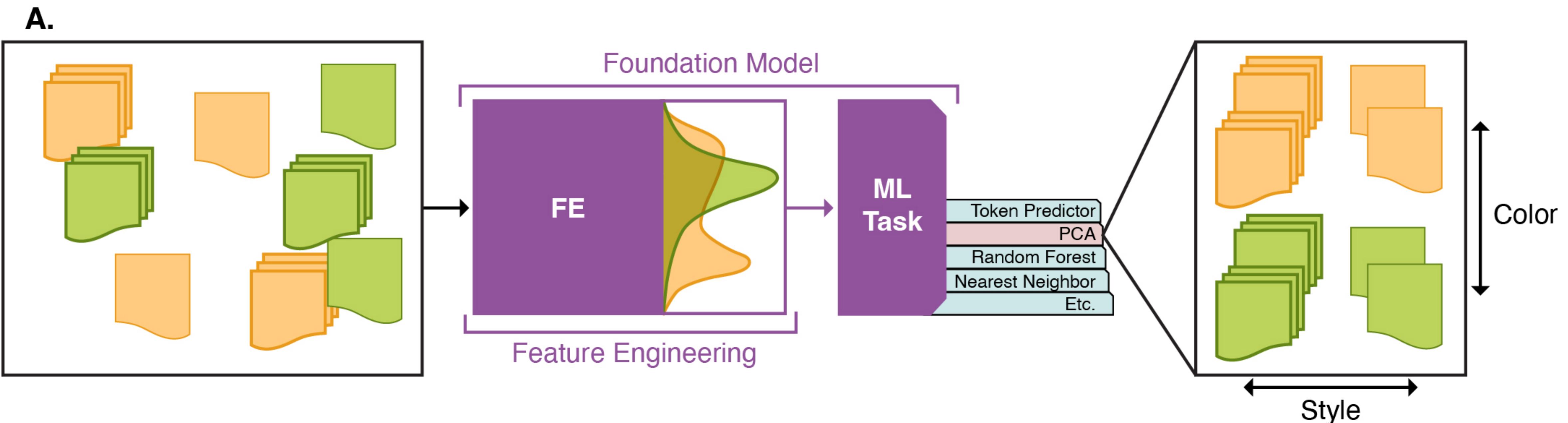
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- **Data Filtering Network**: a CLIP model trained on 5B images that were filtered from an uncurated dataset of image-text pairs. It has 1B parameters and can be used to encode both text and images.

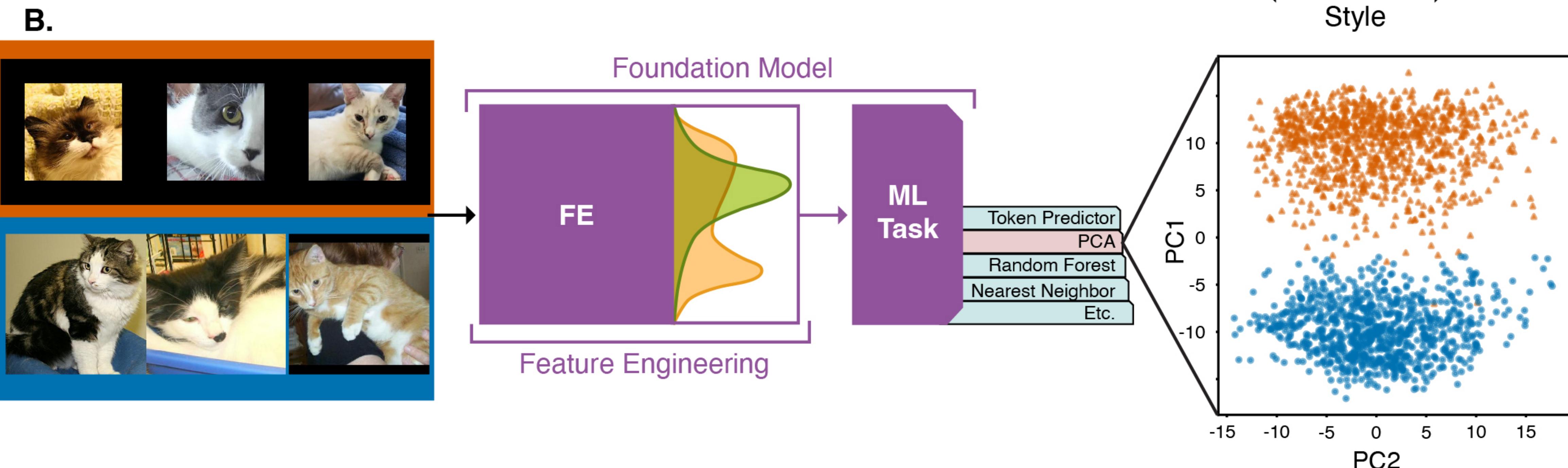
# The generic approach in different contexts

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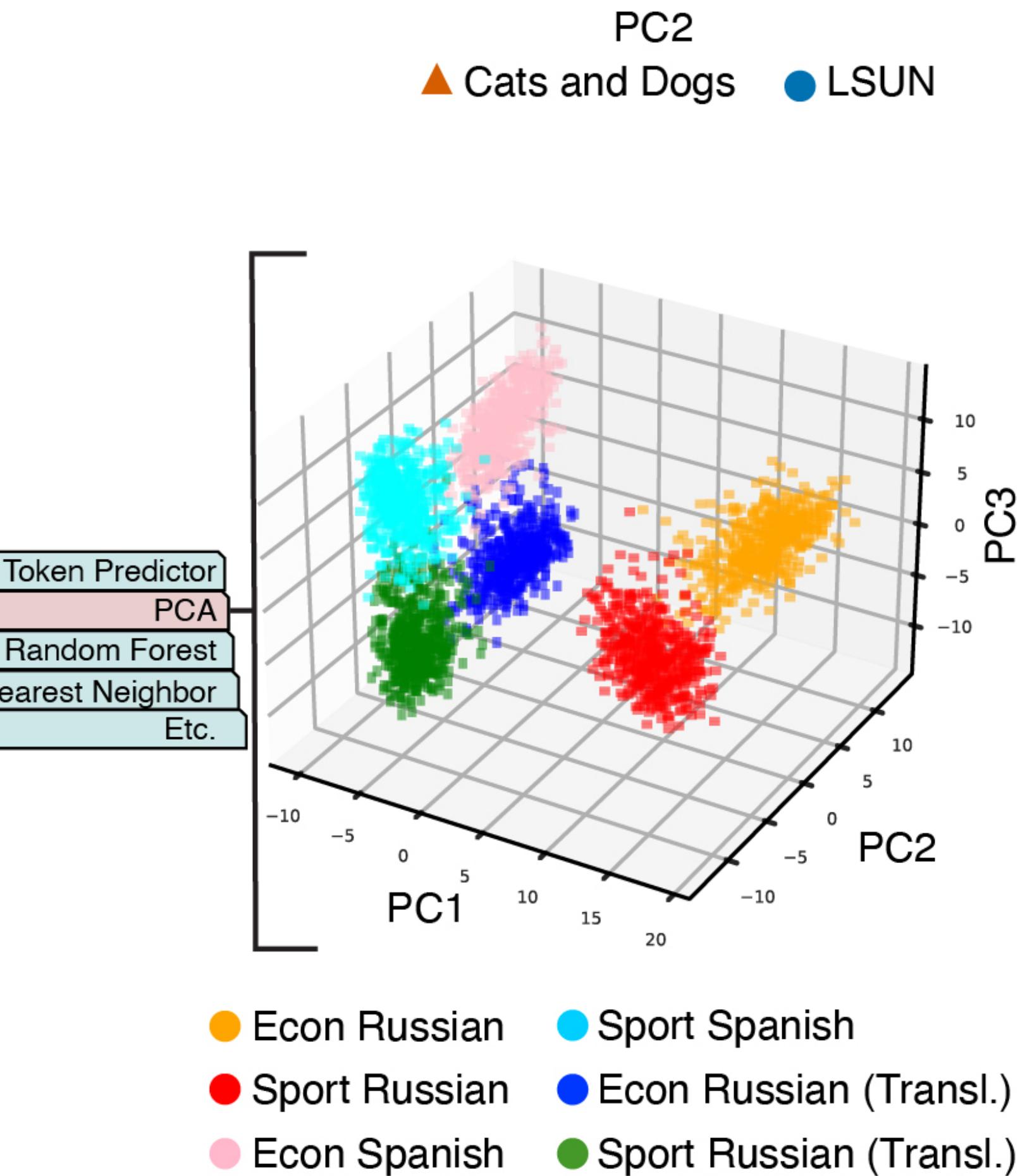
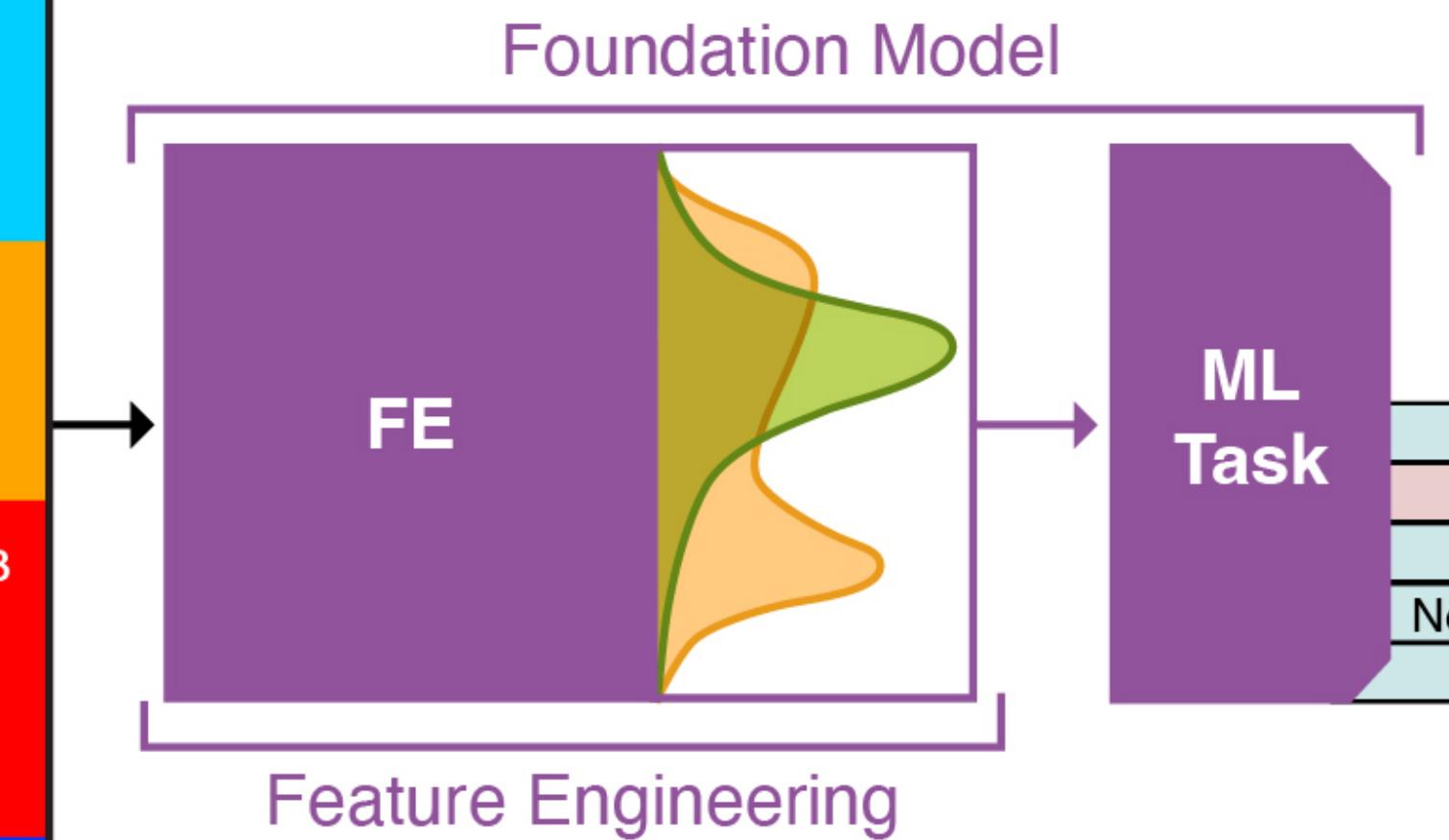
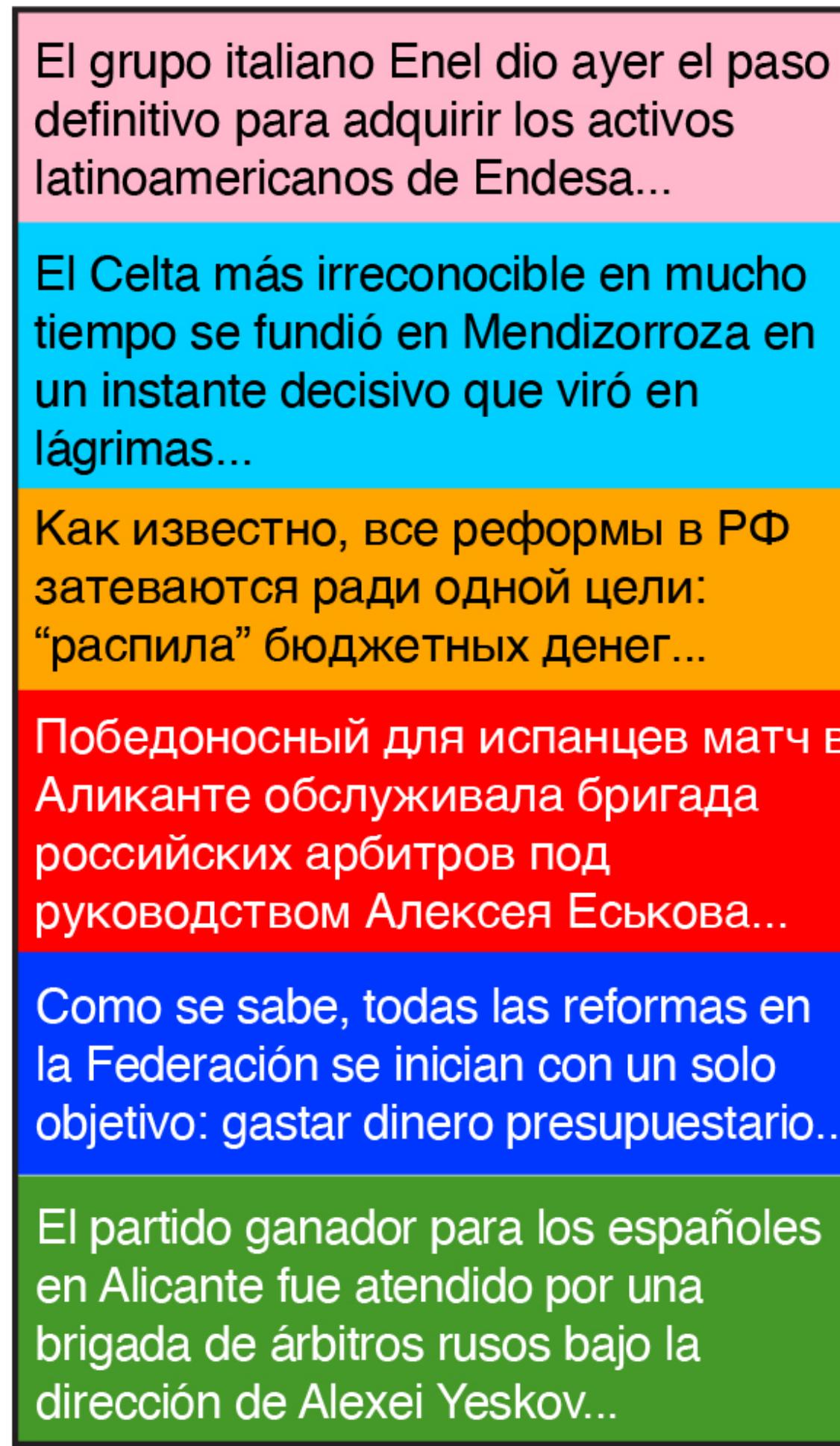
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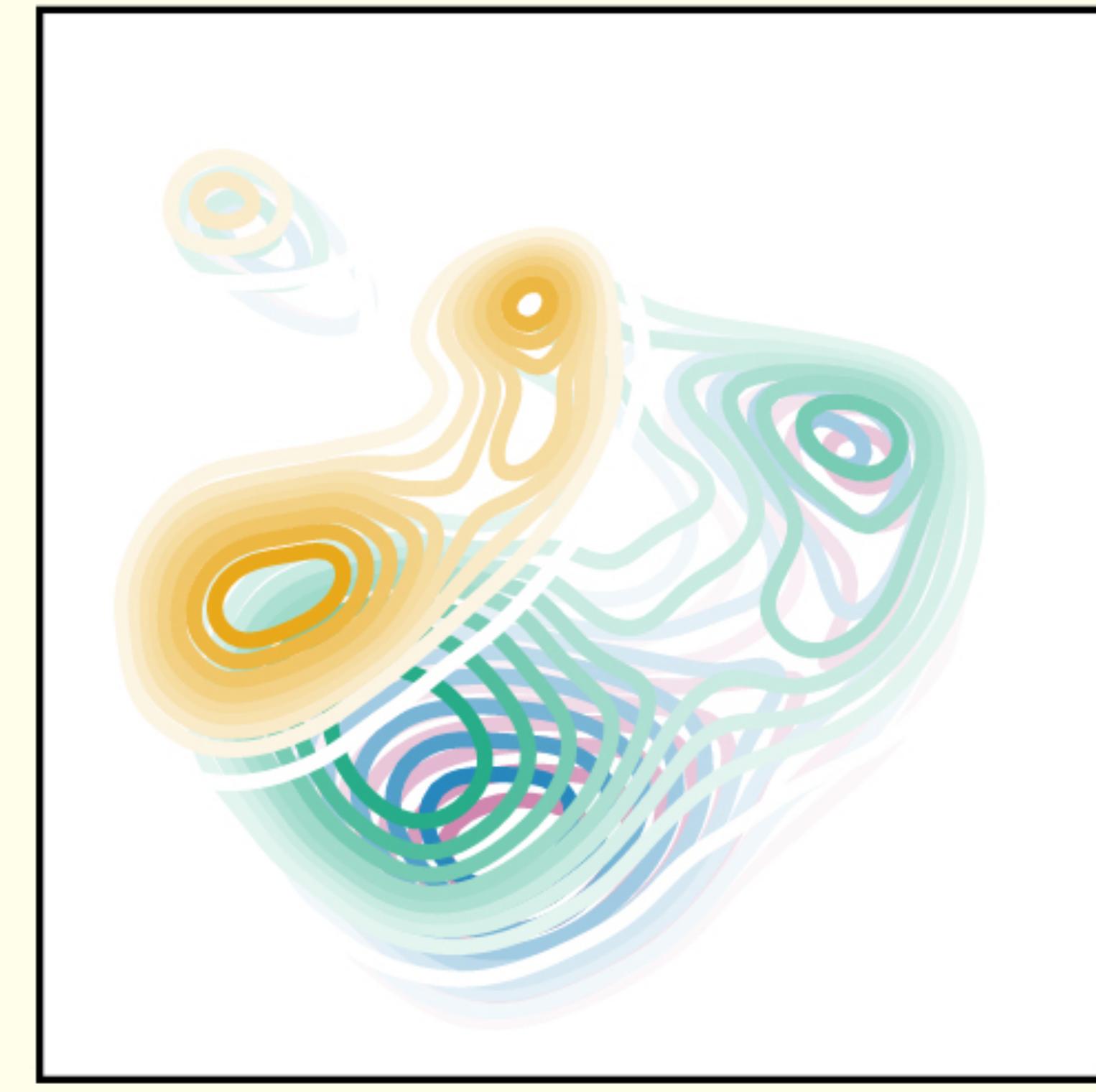
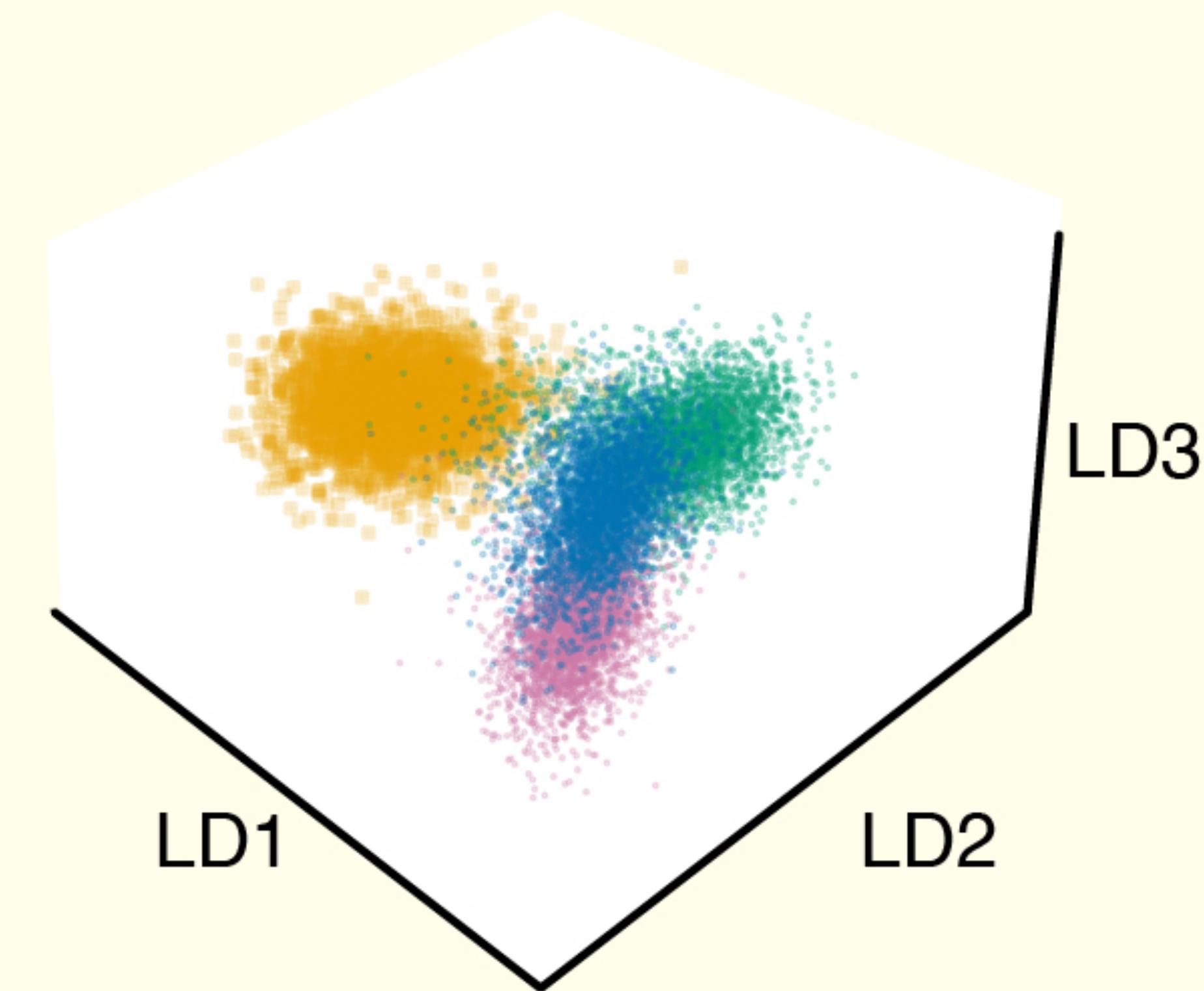
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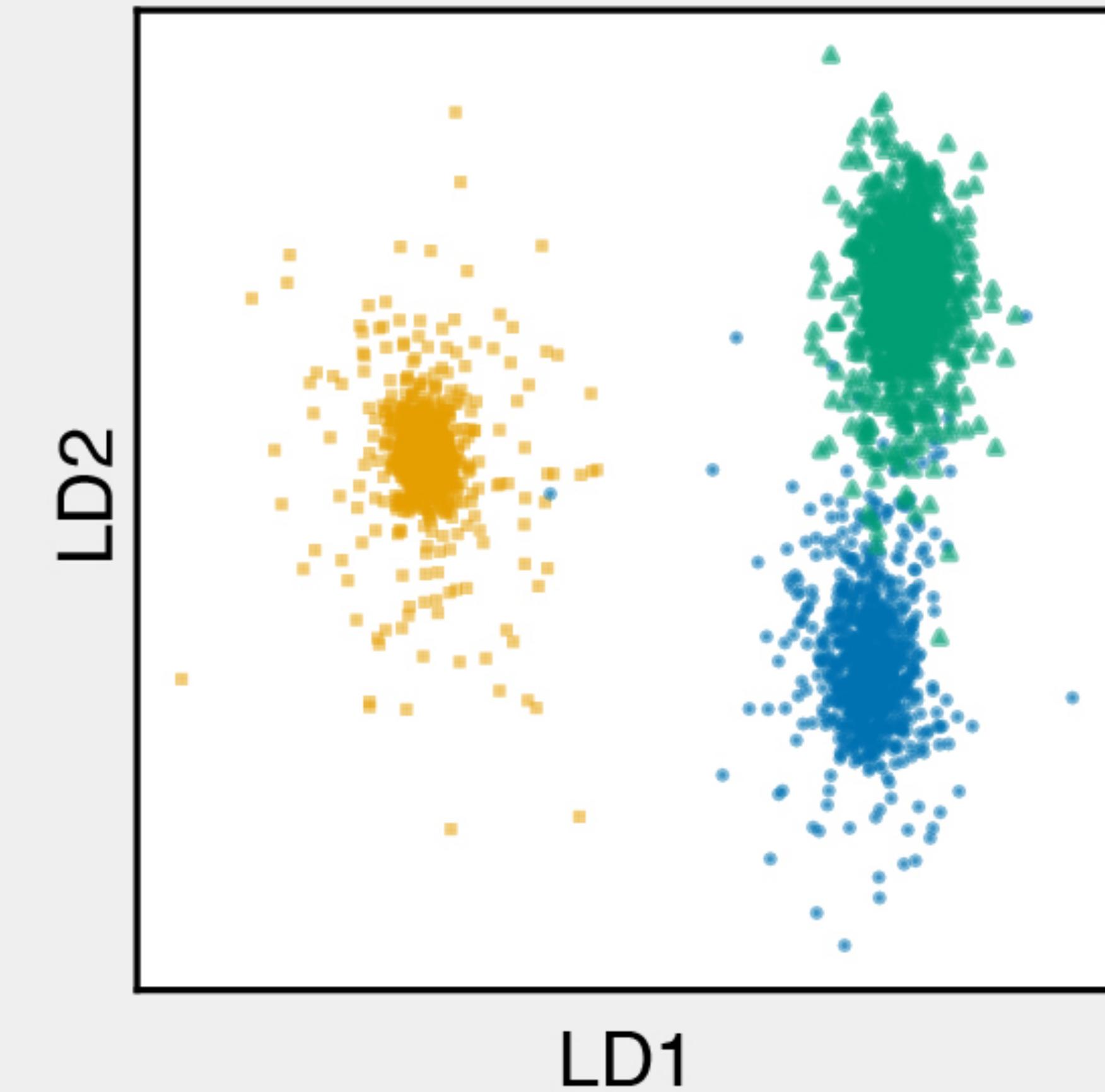
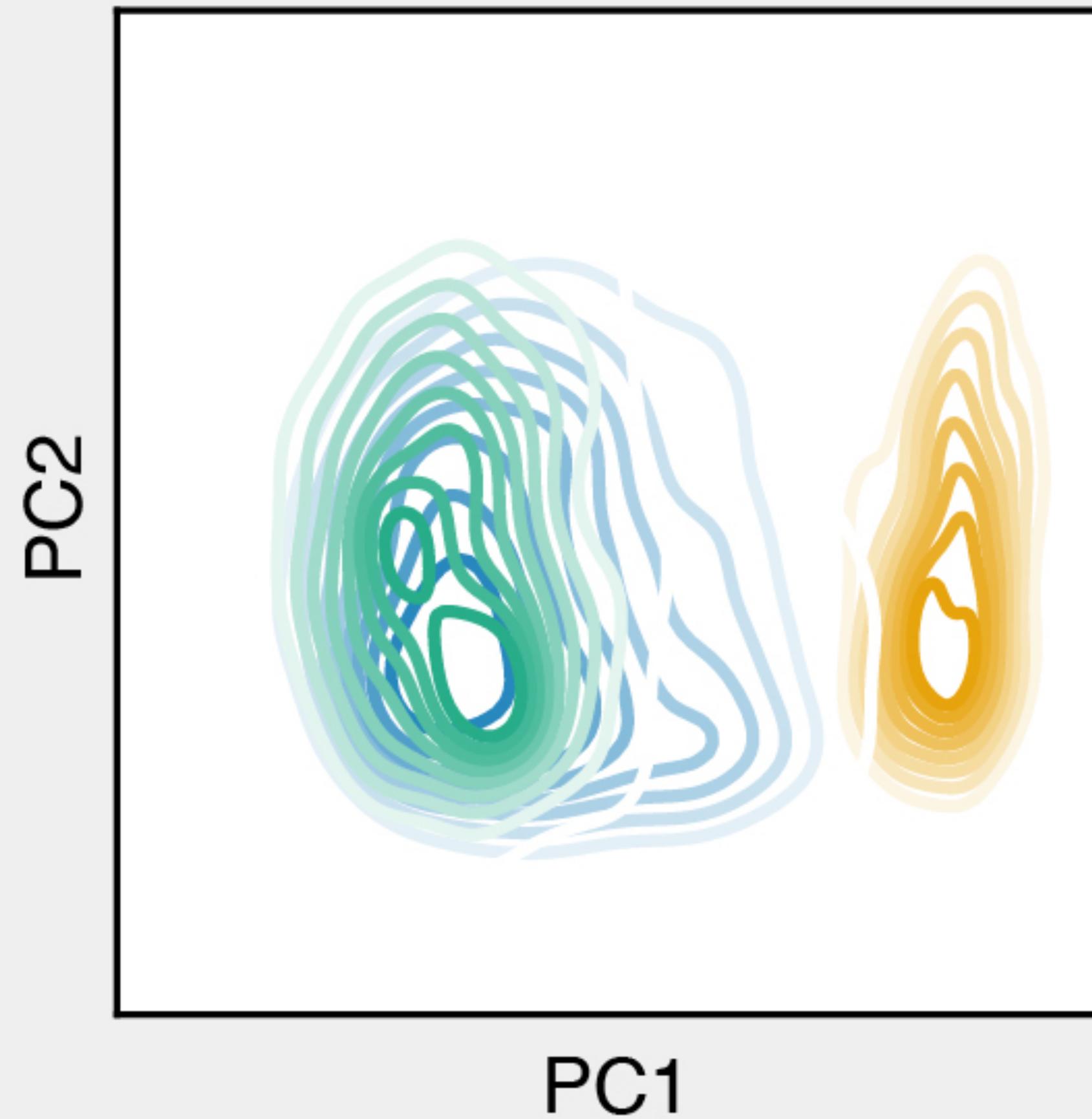
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1. Embed real data and AI-generated data to see if the embedding vectors cluster.
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3. Detect the difference between real and machine-translated data.

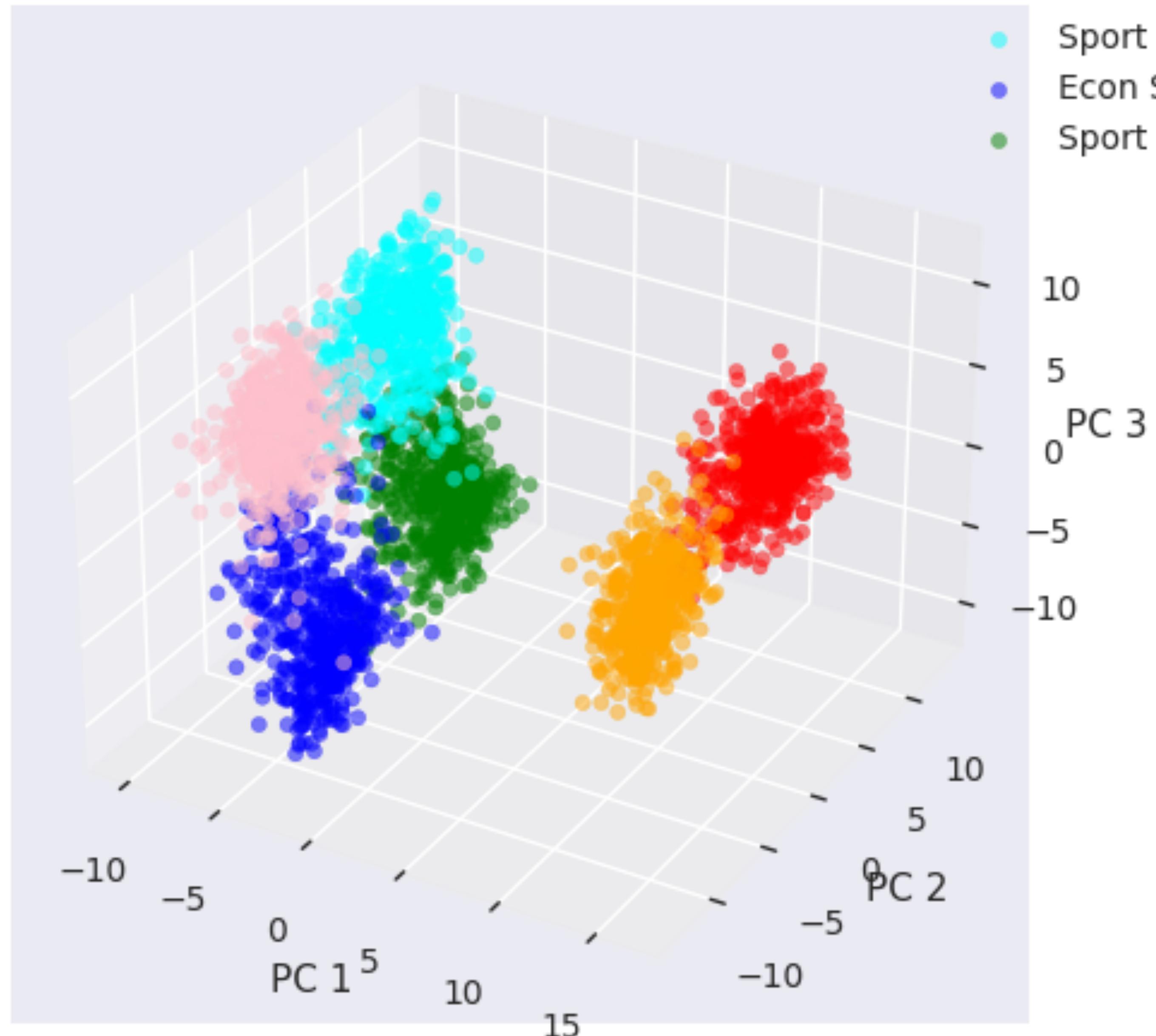
**A.****PCA****Stack exchange****PC1****LDA****LD1****LD2****LD3****Real****Mixtral 8x7B****Falcon 40B****Llama-2 70B**

C.

Economics abstracts



● Real   ● Prompt 1   ● Prompt 2



- Econ Spanish
- Sport Spanish
- Econ German
- Sport German
- Econ Spanish (Transl.)
- Sport Spanish (Transl.)

**Claim:** PCs reflect interpretable features/known hidden labels.

Took news articles in Spanish and German in two topics, economics and sports.

Used a ML translator to translate German to Spanish.

Translating news articles helps reduce the variation in one dimension (language).

# Some takeaways and ongoing work

## Model forensics and model evolution



HarmonyOS 4.0



Samsung UI 7.0

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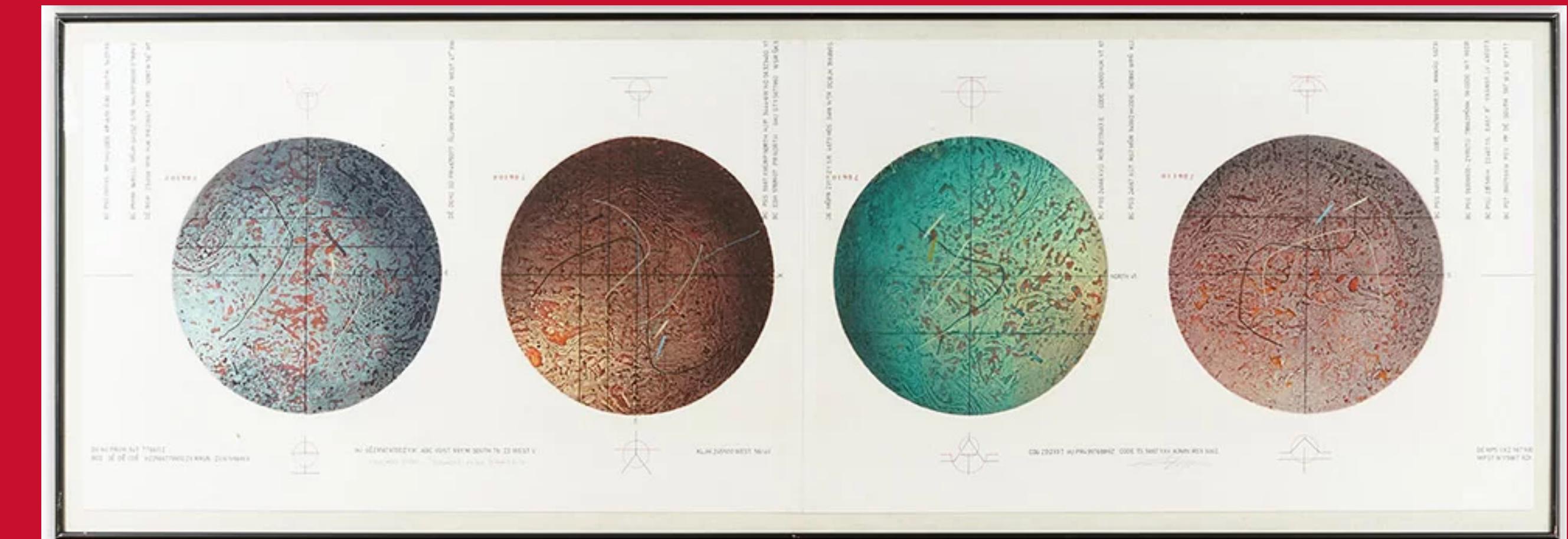
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- Forensics applications: comparing models, detecting deepfakes, etc.
- “Model DNA”: fine-tuned or “lightly modified” models make minor modifications to the embeddings.
- Use post processing to “align” embeddings for calibration, ensembling, federated learning, etc.



Samsung UI 7.0

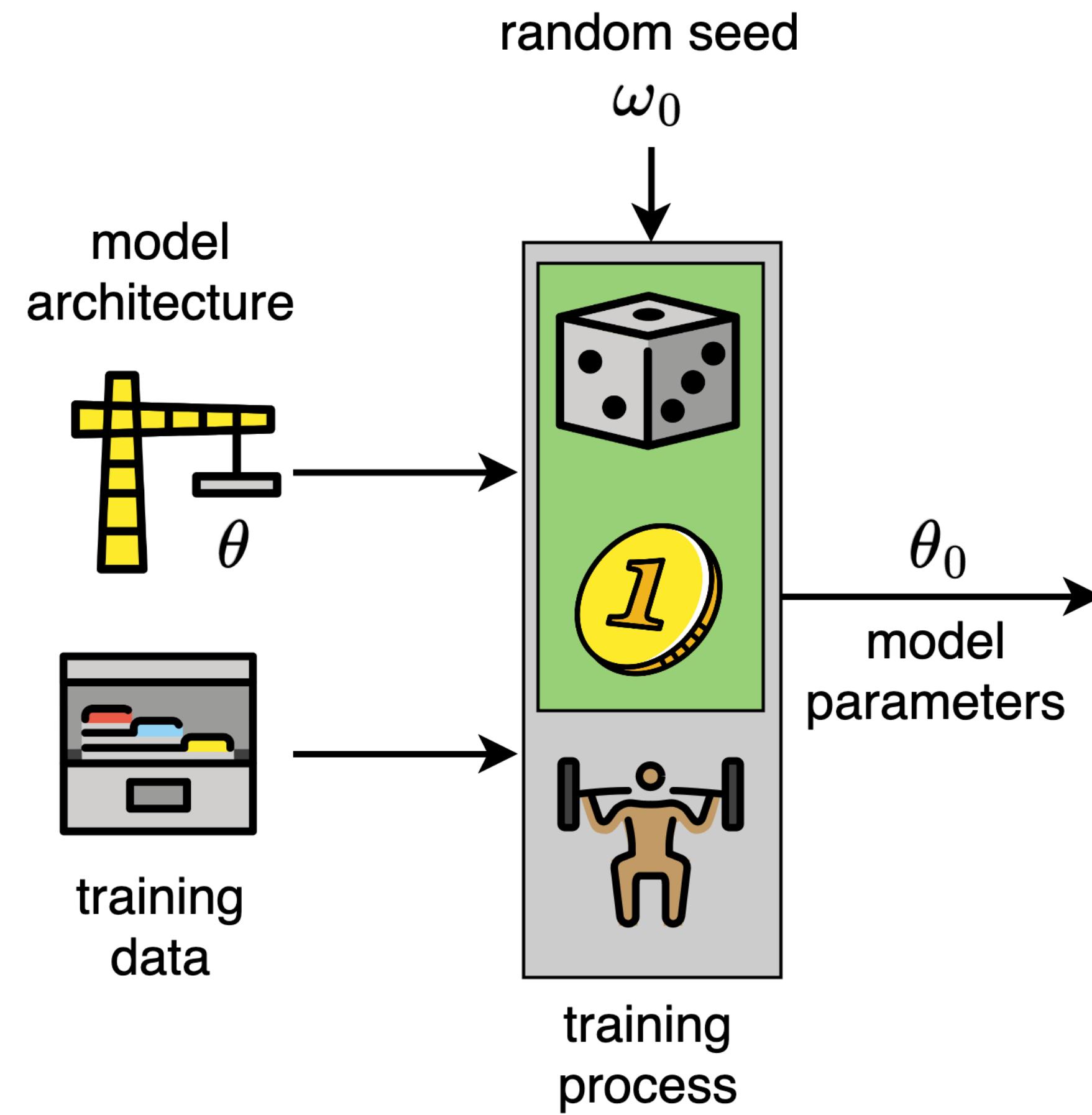
# Model comparisons in training



Rm Palaniappan, *Alien Planet-D*  
Viscosity, pencil colour and ink on handmade paper

# Variability in the training process

Is training reliable?



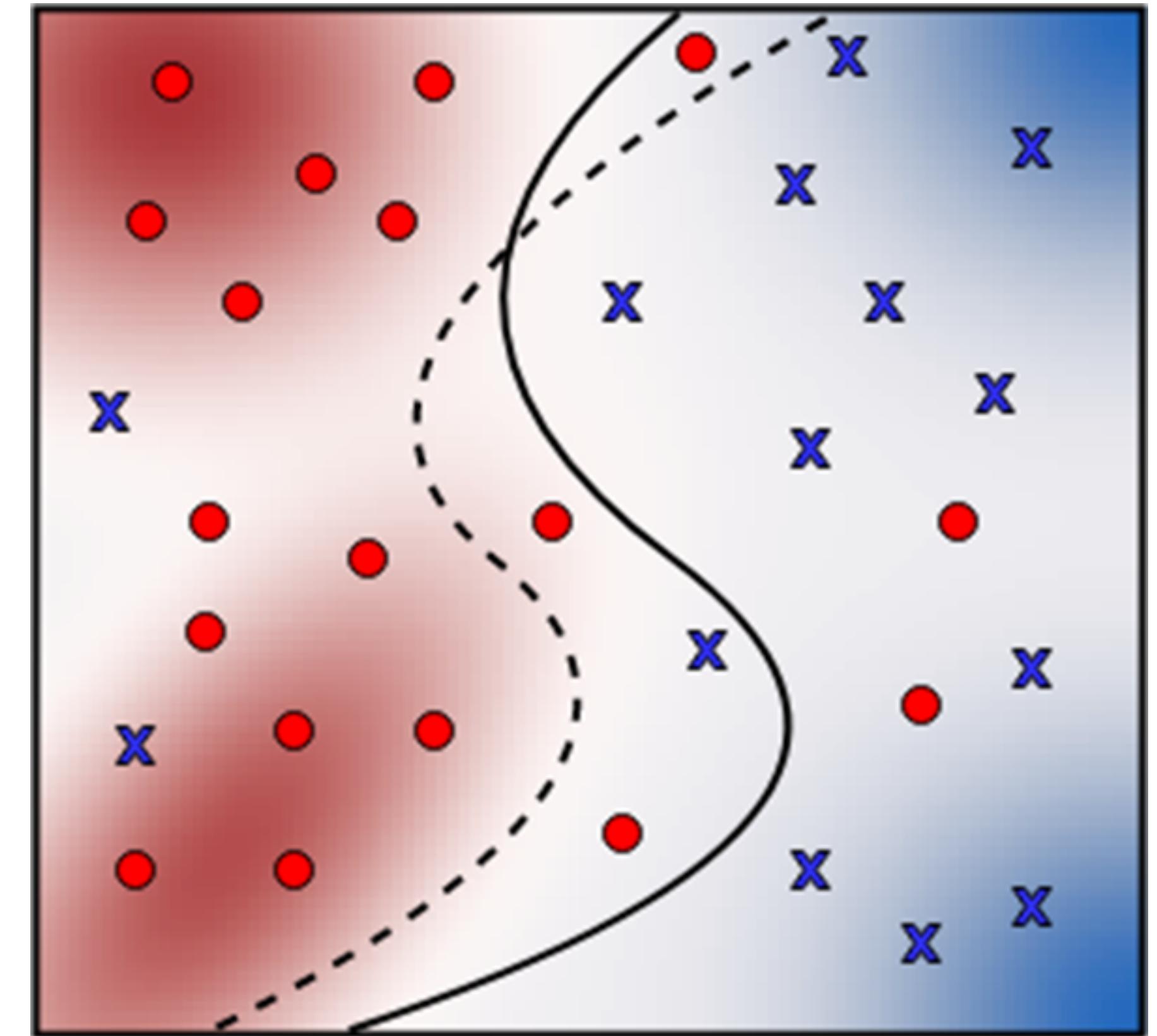
Each time we run the training algorithm on the **same training set, same architecture, same algorithm**, we still use (pseudo-)**independent randomness**.

- Each training run is a **sample** from  $\mathcal{F}$ .
- Given samples  $f_1, f_2, \dots, f_M$  are they similar to each other or different?

This is related to how **reproducible** a model is.

# Comparing two runs of training

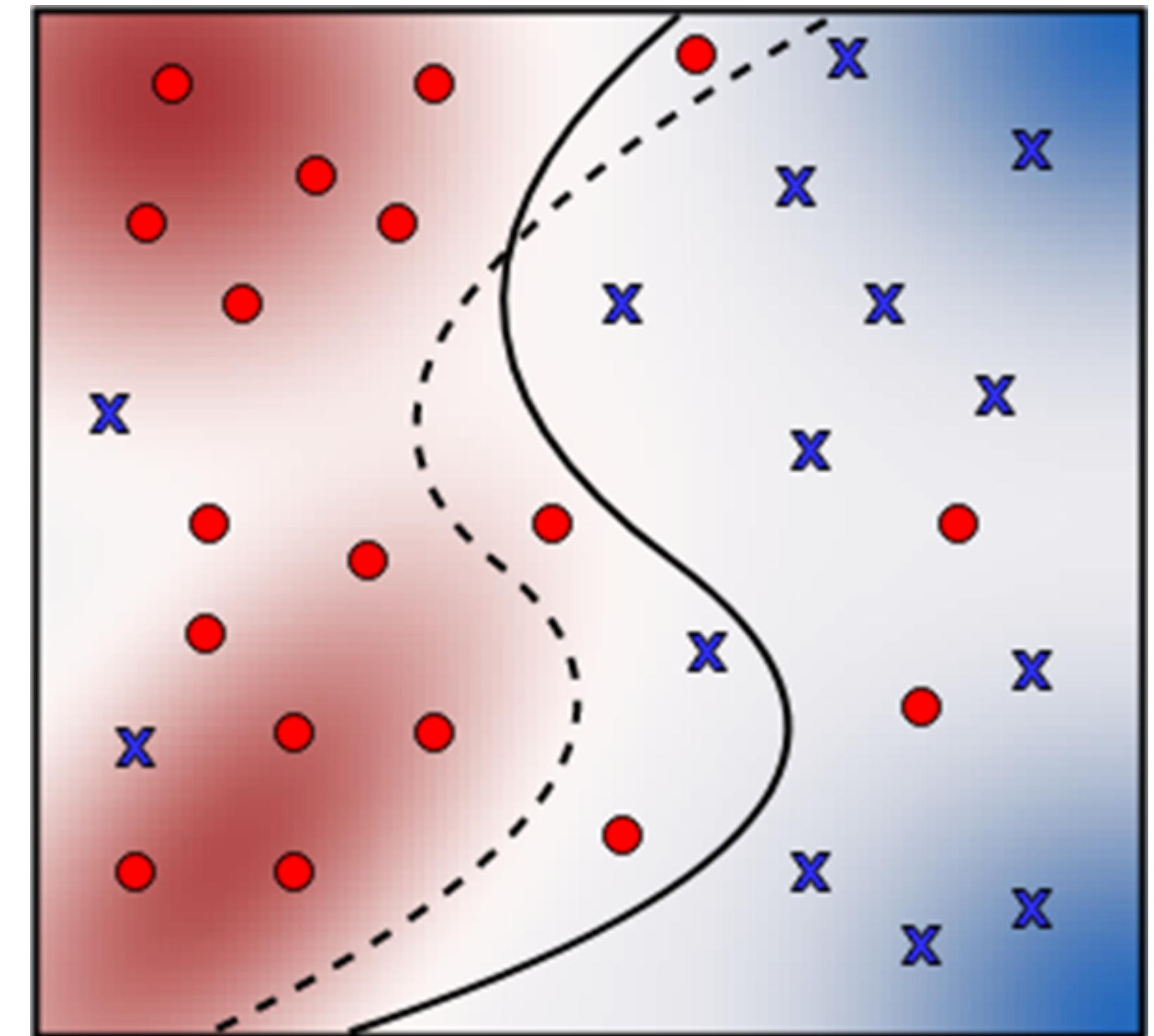
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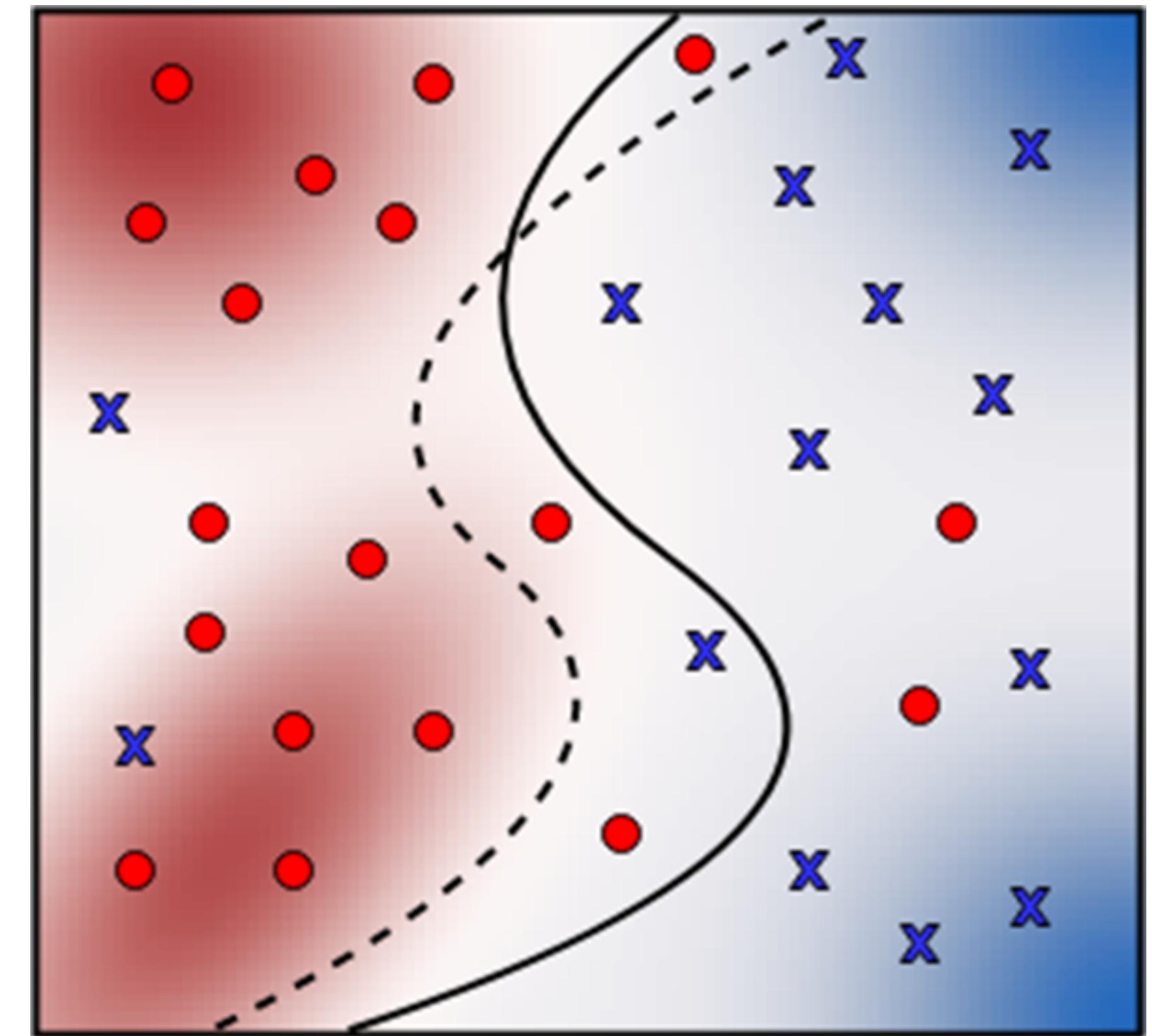
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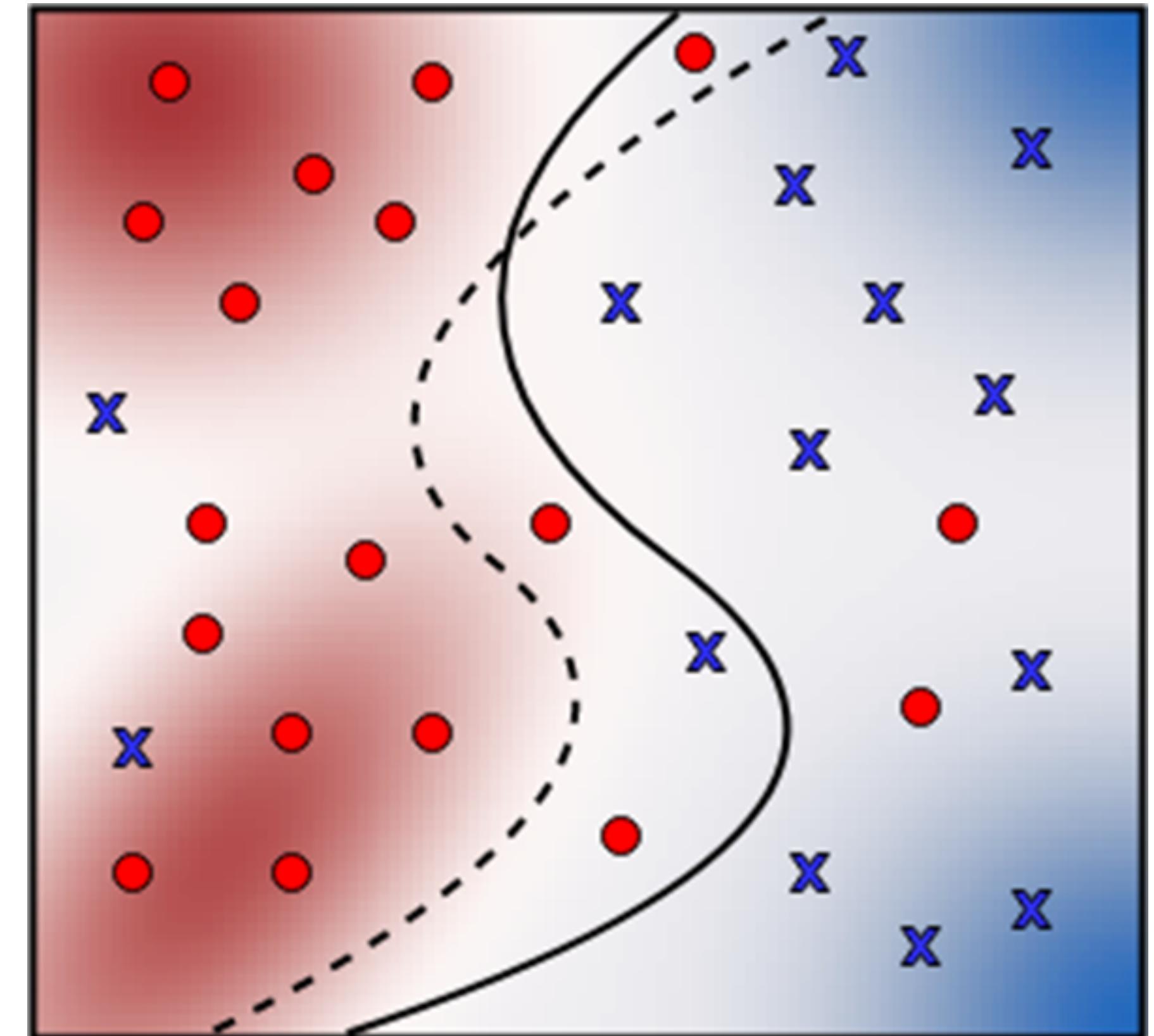


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Terms like the **Rashomon effect**<sup>[1][2][3]</sup>, **predictive multiplicity**<sup>[4]</sup>, or **prediction churn**<sup>[5]</sup> have been used to describe this phenomena.



[1] Breiman, L. (2001). Statistical modeling: The two cultures (with comments and a rejoinder by the author). *Statistical science*, 16(3), 199-231

[2] Fisher, A., Rudin, C., & Dominici, F. (2019). All models are wrong, but many are useful: Learning a variable's importance by studying an entire class of prediction models simultaneously. *Journal of Machine Learning Research*, 20(177), 1-81.

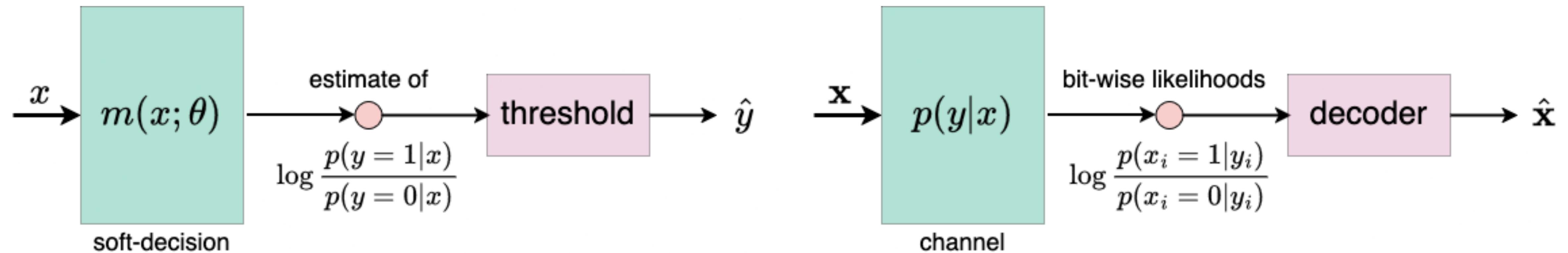
[3] Hsu, H., & Calmon, F. (2022). Rashomon capacity: A metric for predictive multiplicity in classification. *Advances in Neural Information Processing Systems*, 35, 28988-29000.

[4] Milani Fard, M., Cormier, Q., Canini, K., & Gupta, M. (2016). Launch and iterate: Reducing prediction churn. *Advances in Neural Information Processing Systems*, 29.

[5] Marx, C., Calmon, F., & Ustun, B. (2020, November). Predictive multiplicity in classification. In *International Conference on Machine Learning* (pp. 6765-6774). PMLR.

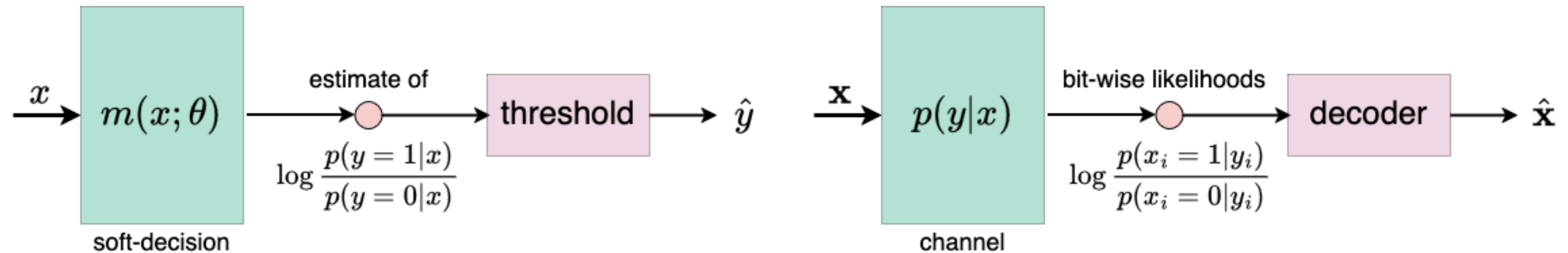
# Hard decisions vs. soft decisions

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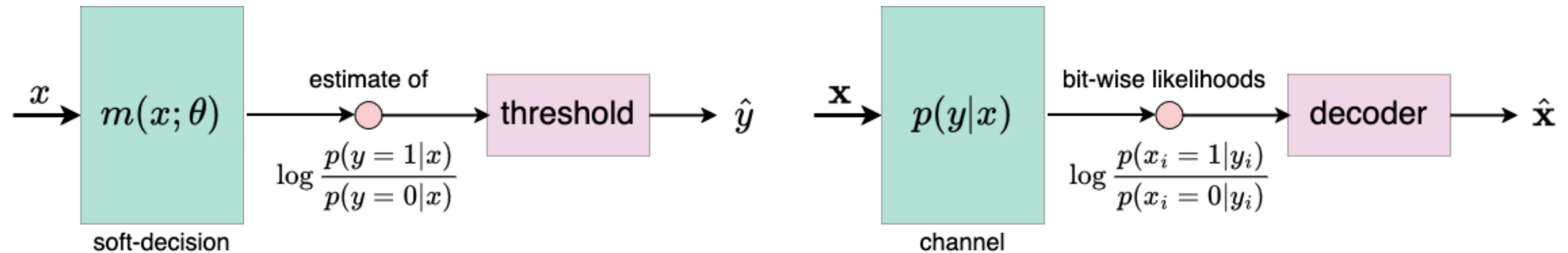
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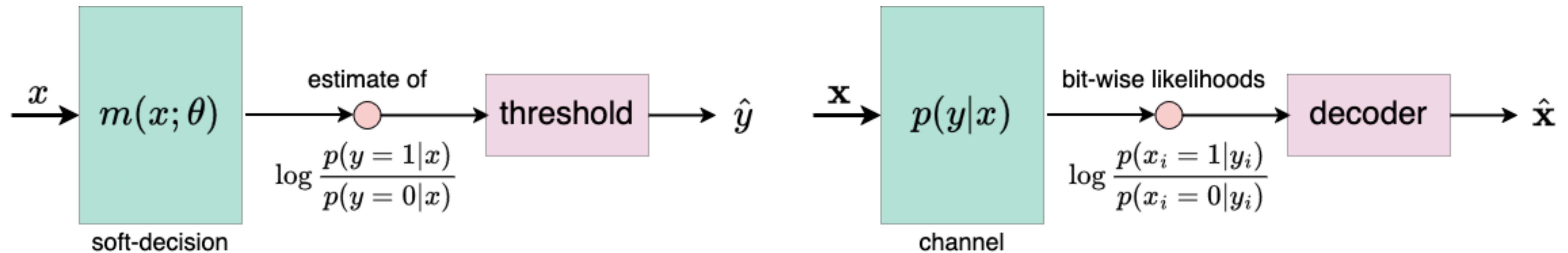


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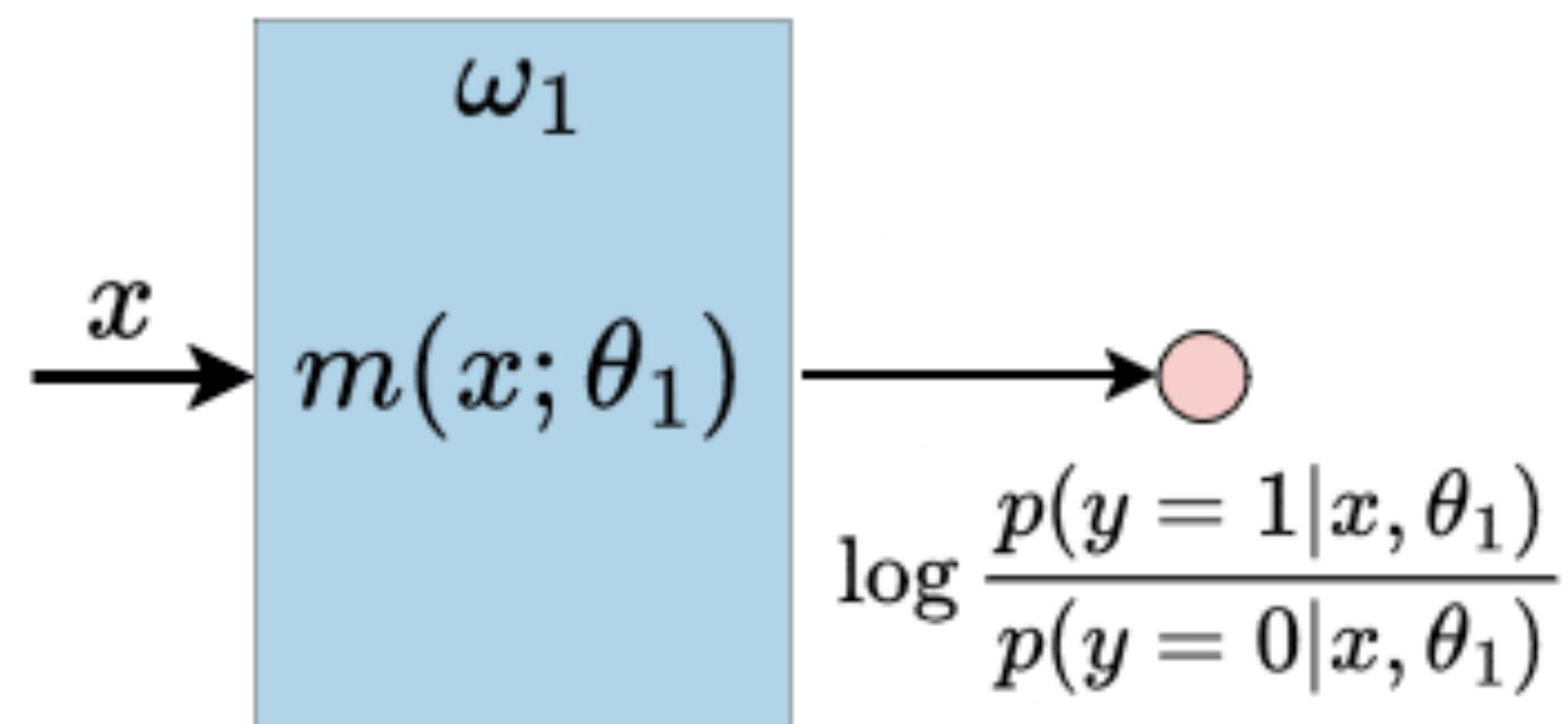
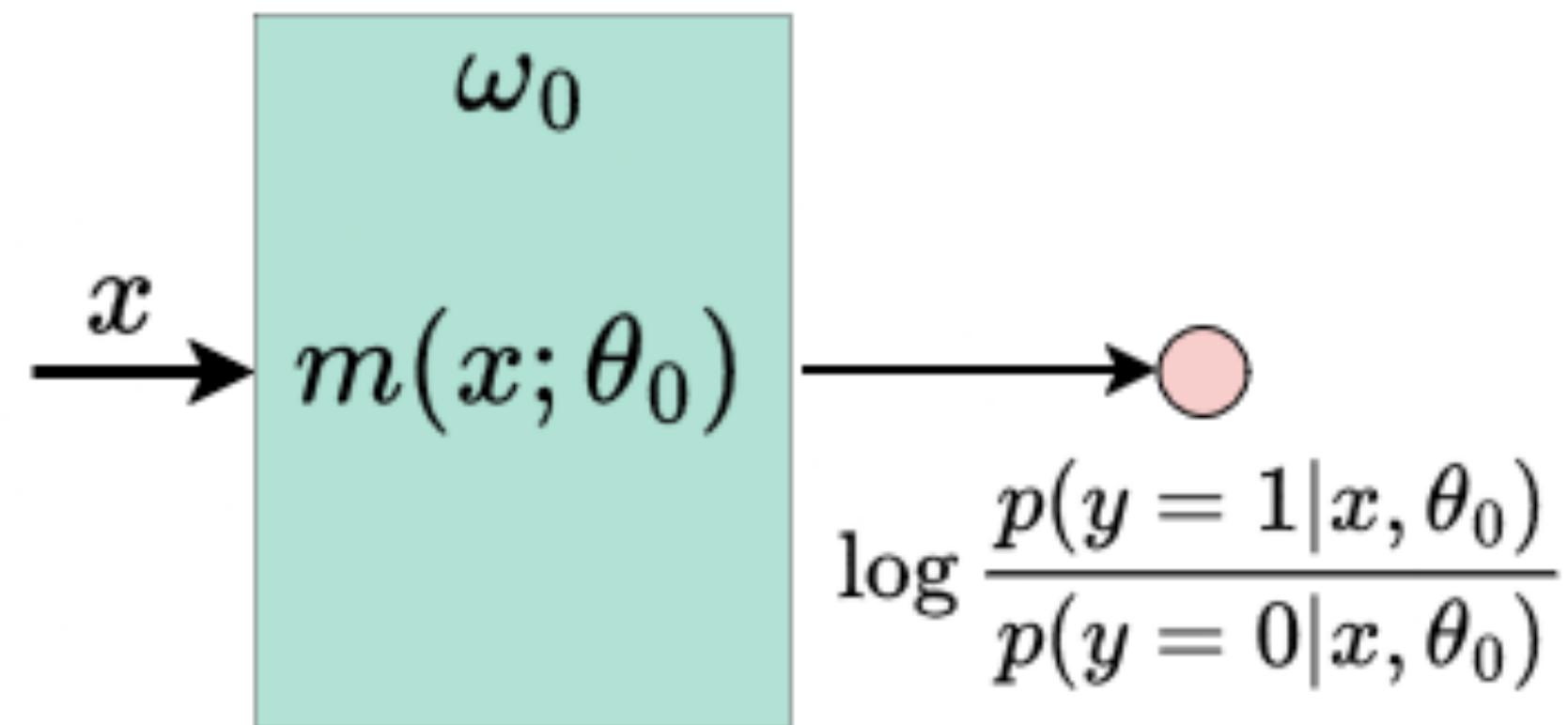


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- These are usually made using (softmax) probability estimates  $\hat{p}(y|x, \theta)$ .
- Instead look at **pre-threshold “soft decision”**  $m(x|\theta)$  for the model.

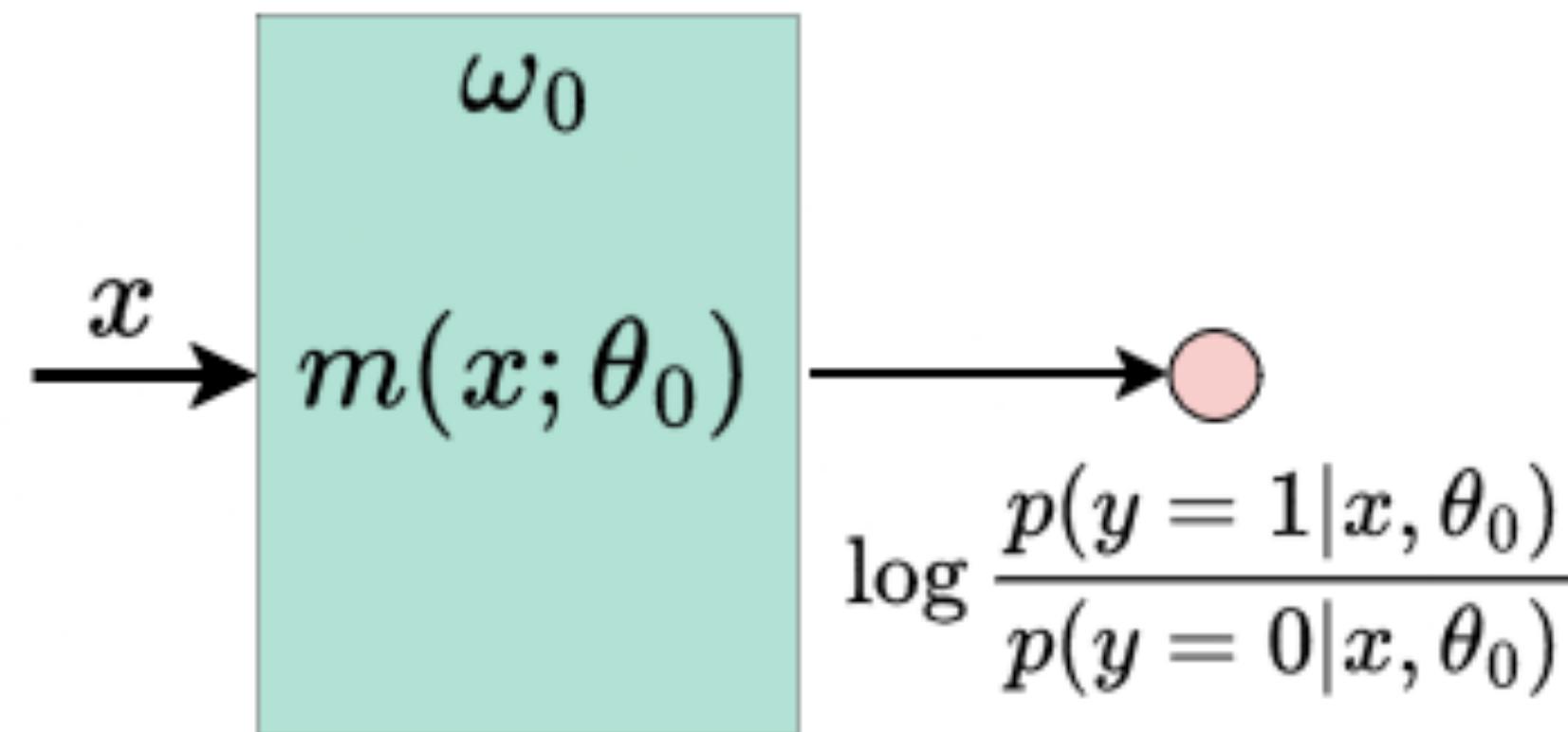
# Comparing two binary classifiers

Soft decisions are different even if decisions are the same

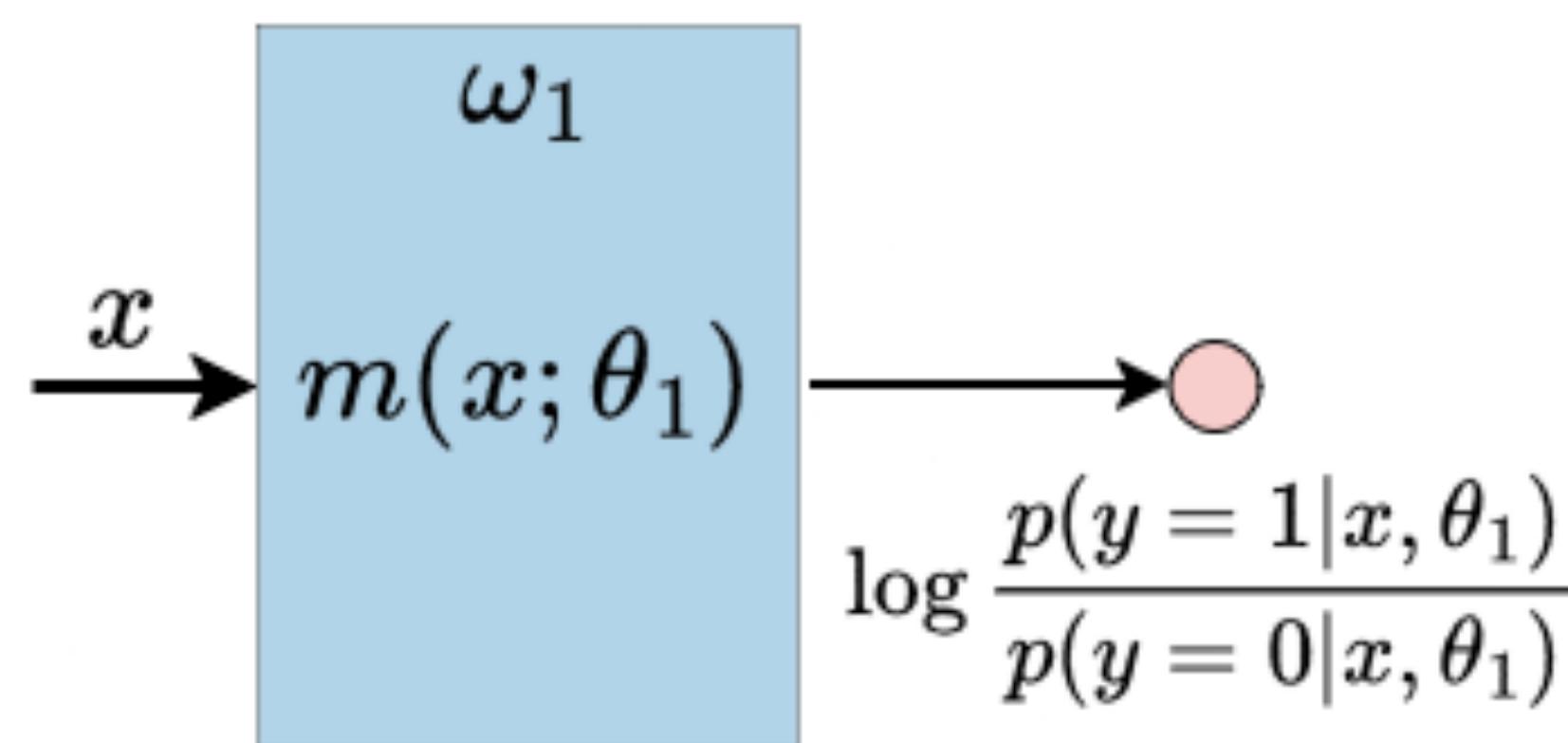


# Comparing two binary classifiers

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Measure the difference between the **soft decisions/LLRs**.



Assume the test set is made of i.i.d. draws from the input distribution.

Turn this into a **hypothesis testing problem!**

# Two-sample tests for model similarity

Back to simple tools: hypothesis testing



VS.



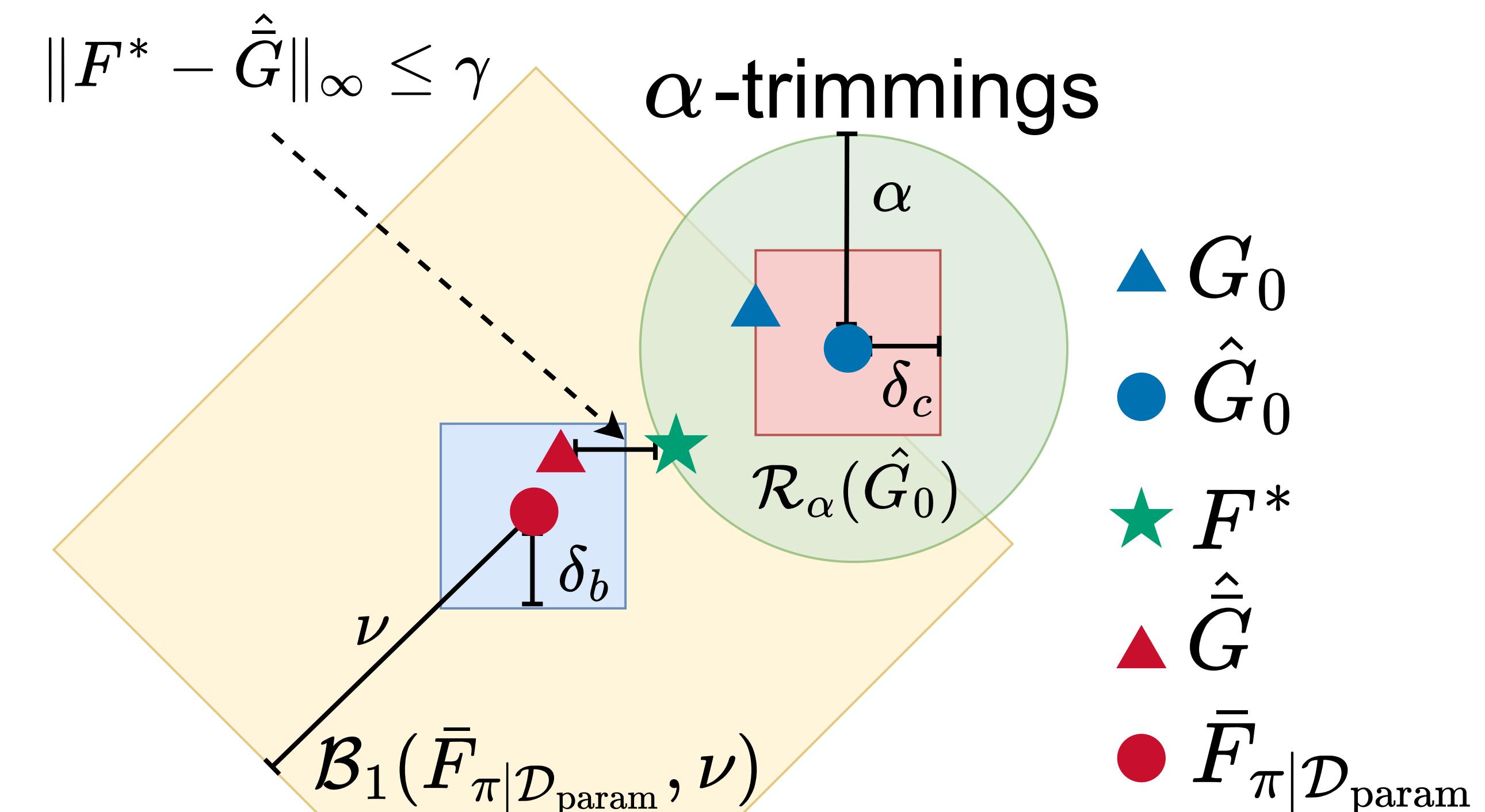
Are the models the same or different? Answer this by testing:

$$\mathcal{H}_0 : m(x; \theta_0) = m(x; \theta_1)$$

$$\mathcal{H}_1 : m(x; \theta_0) \neq m(x; \theta_1)$$

# Hypothesis testing for model comparisons

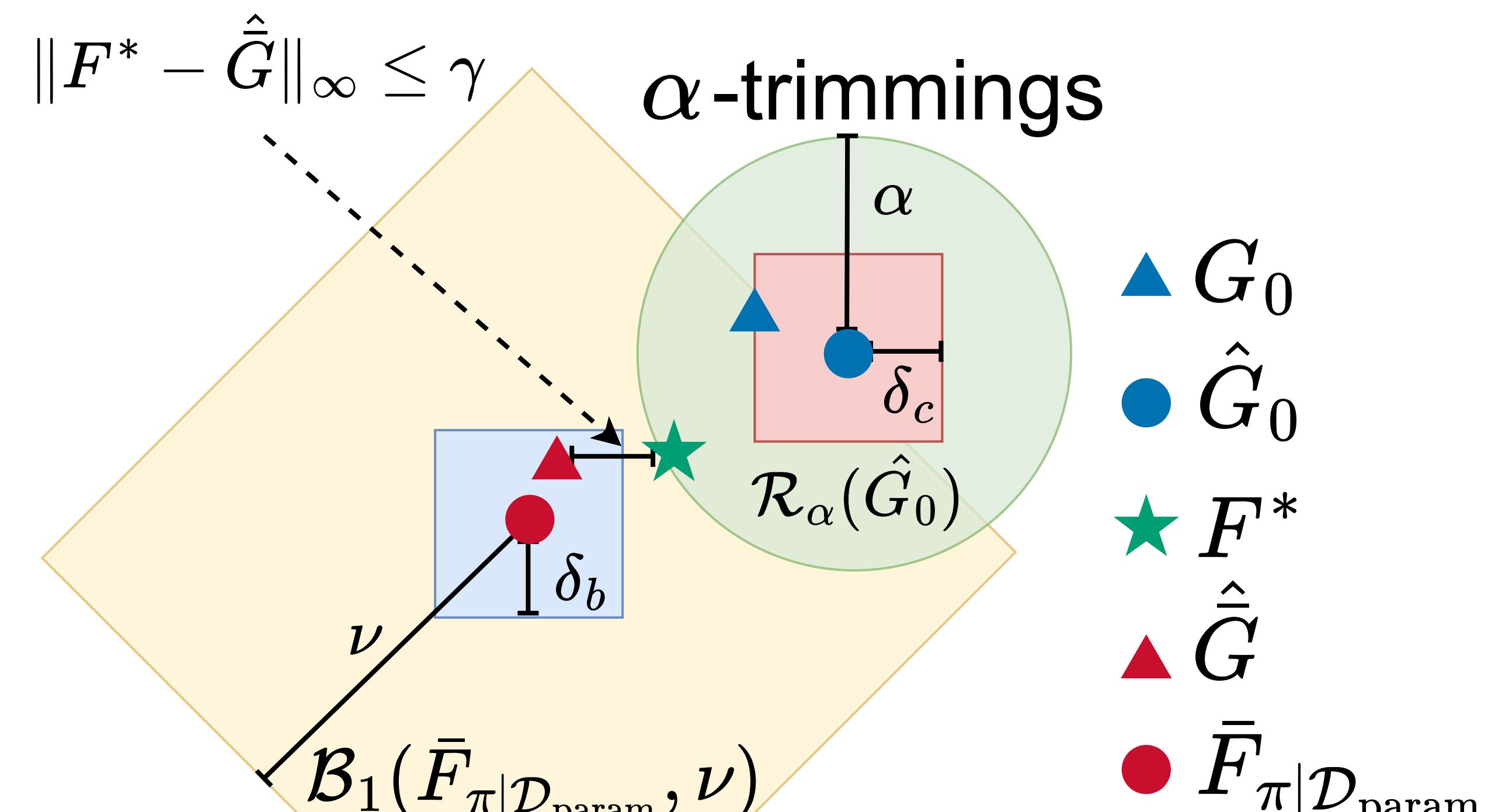
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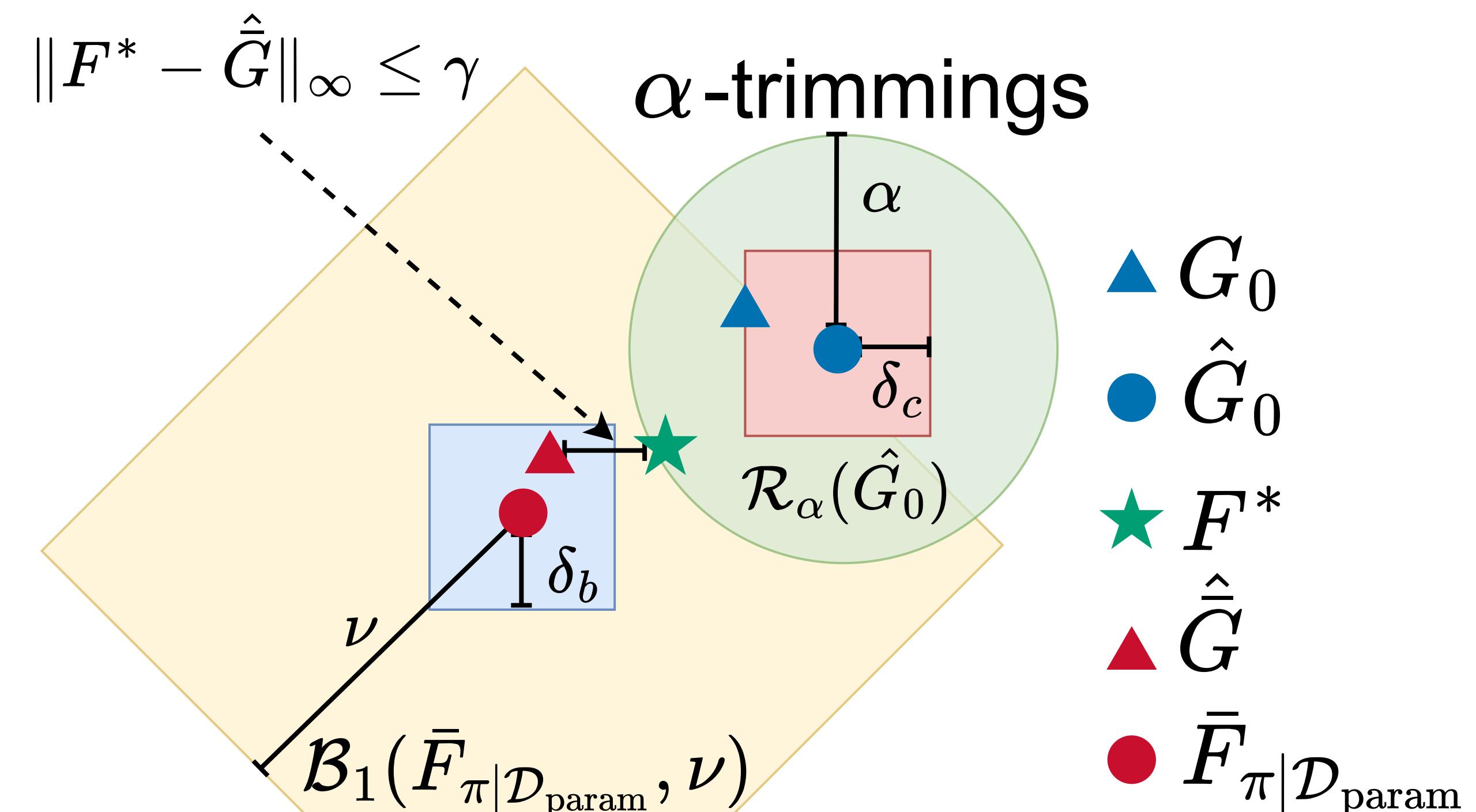


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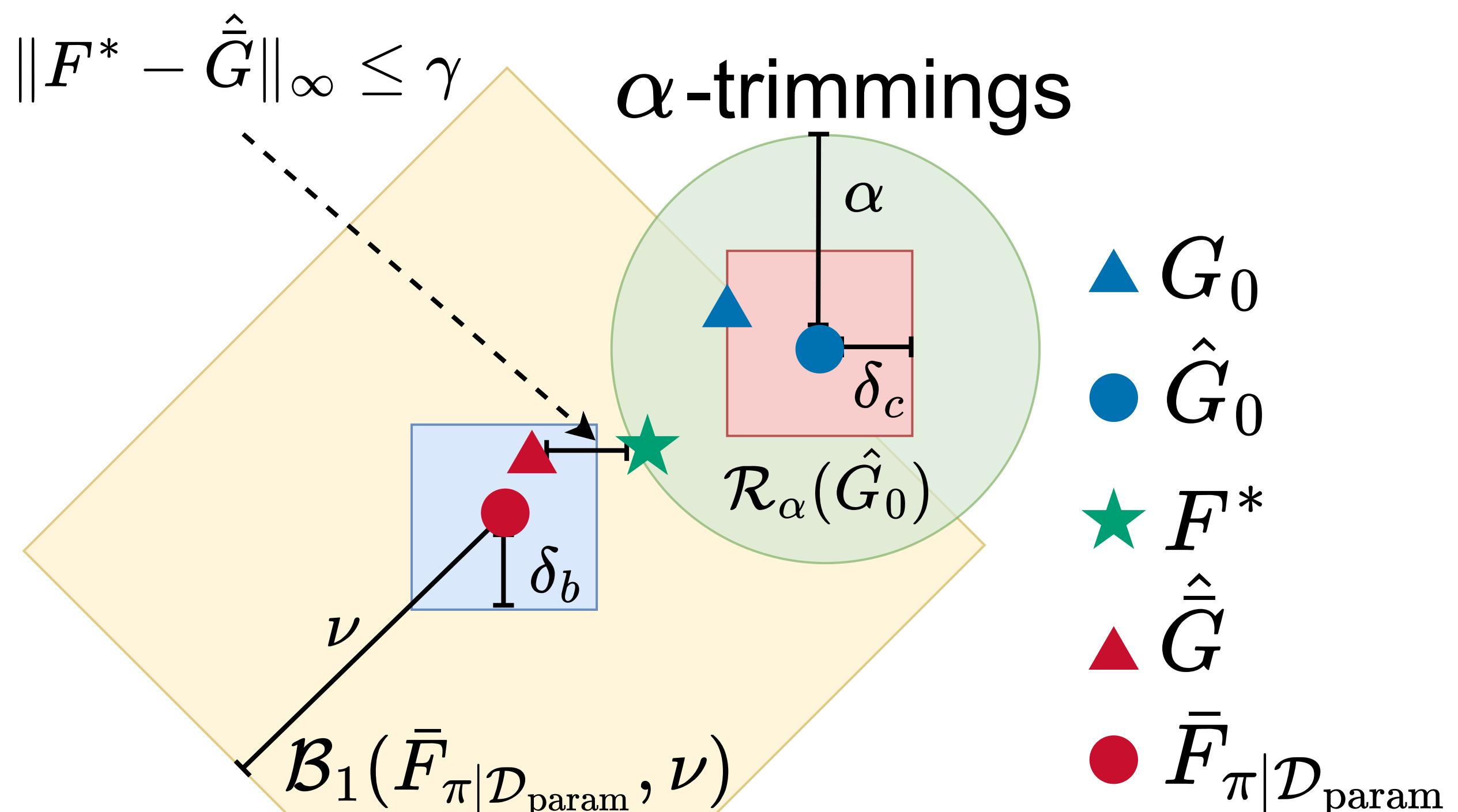
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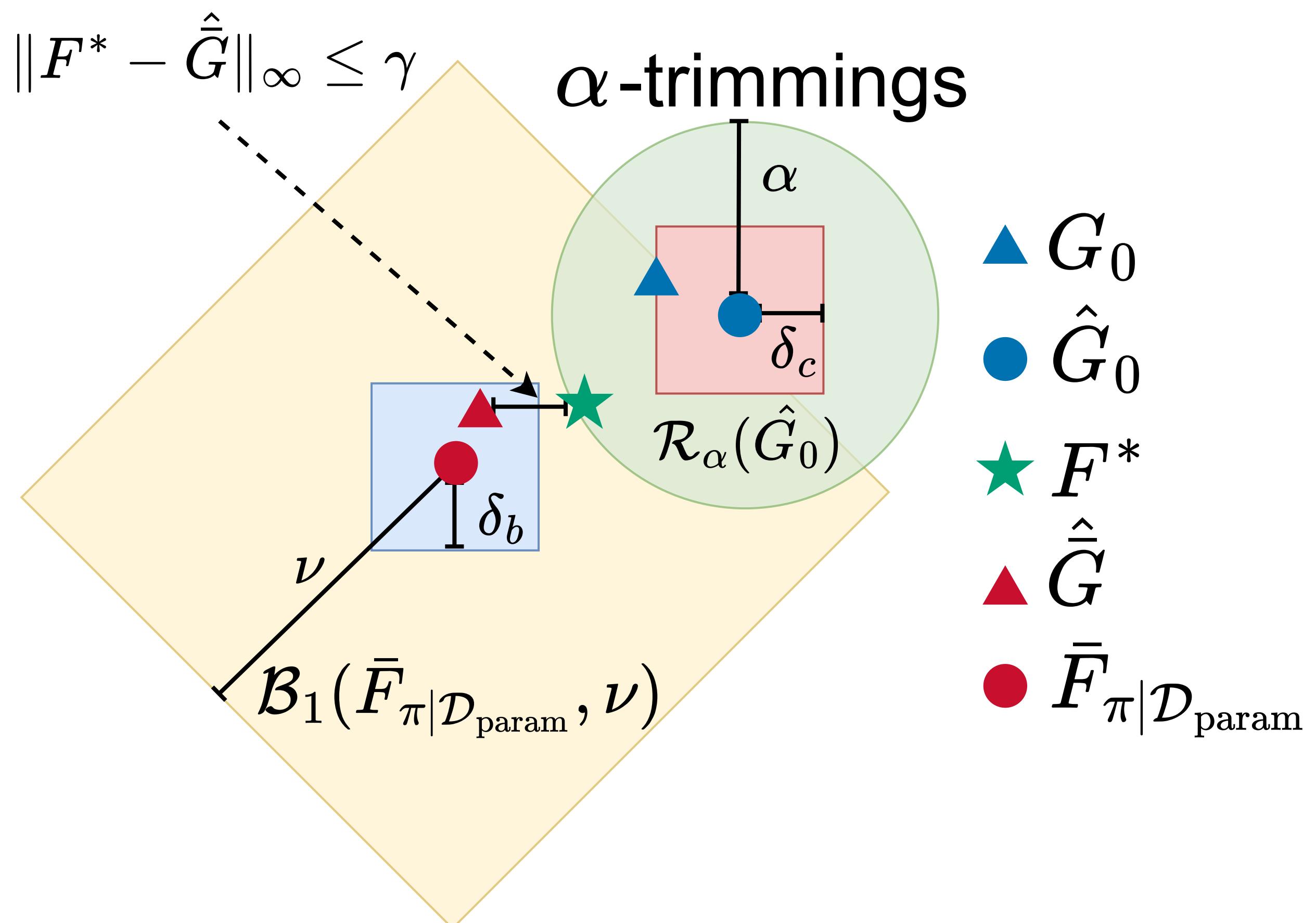
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Define a new discrepancy measure  $\hat{\alpha}$  as the minimum level for the test (= radius of the ball) to accept.



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- Models with small  $\hat{\alpha}$  are generally low on all the other metrics as well.

# Connecting back to our story

“Reliable” training algorithm should produce “typical” models



iOS 8.3



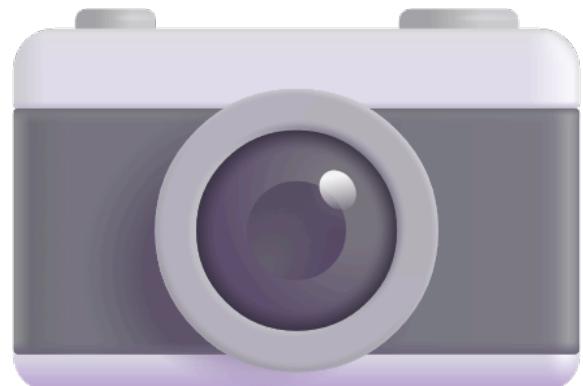
iOS 18.4



HarmonyOS 4.0



Samsung UI 7.0



MS 3D Fluent



SerenityOS

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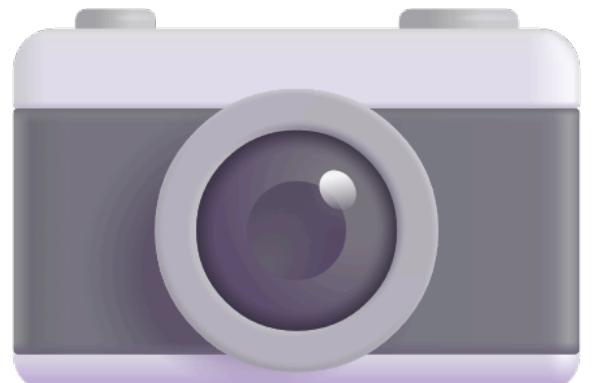
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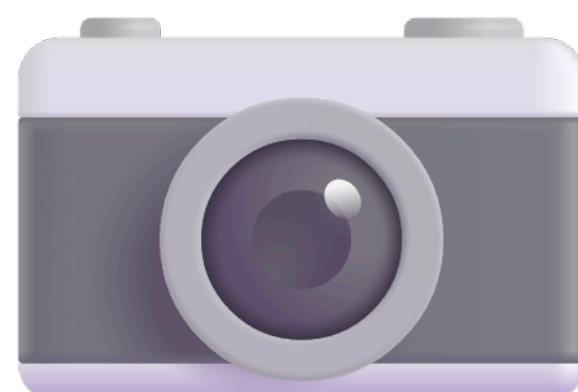
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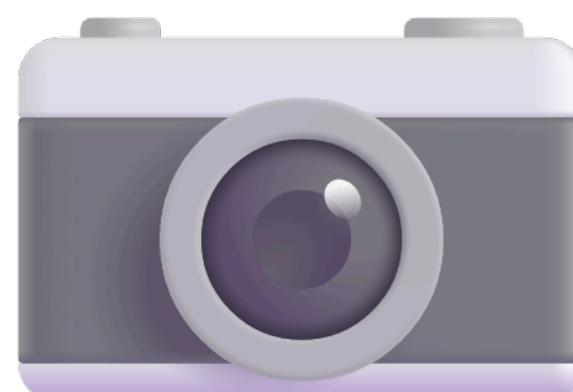
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- Use this to design **new methods for model ensembling.**
- Apply it to **other features of trained models** (e.g. NTK spectra) to find model differences.

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iOS 8.3



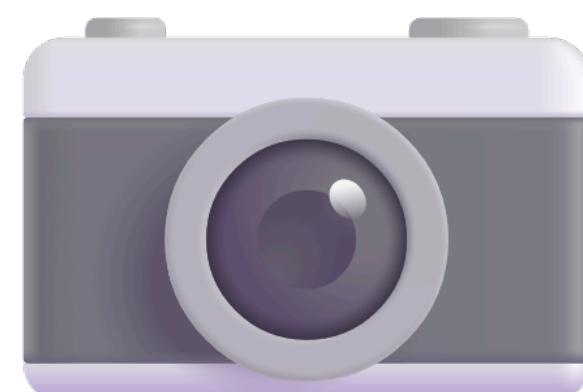
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Samsung UI 7.0



MS 3D Fluent

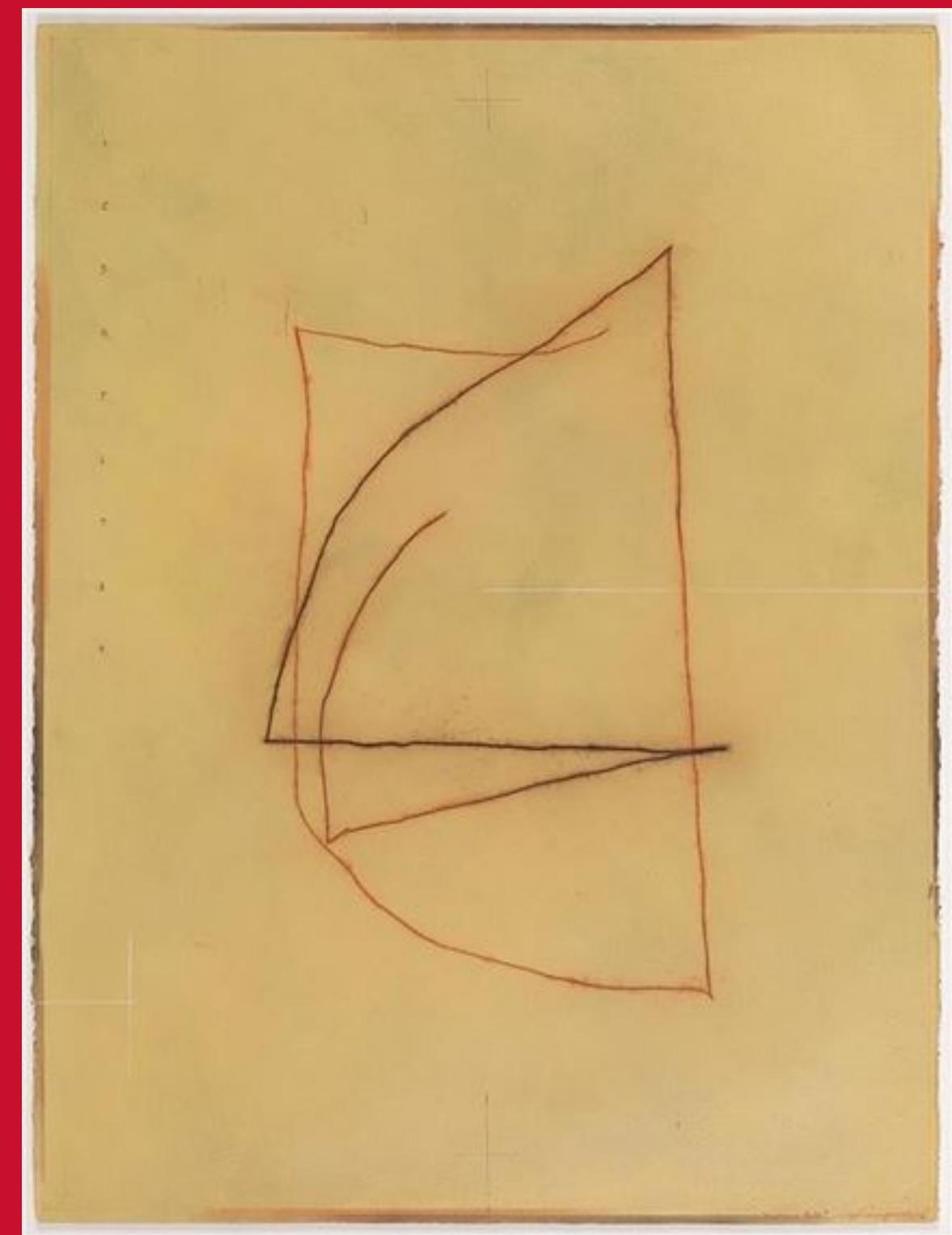


SerenityOS

Measures like  $\hat{\alpha}$  (using  $\ell_1$  balls, Wasserstein balls, etc.) can let us **measure “atypicality.”**

- Use this to design **new methods for model ensembling**.
- Apply it to **other features of trained models** (e.g. NTK spectra) to find model differences.
- Connect it to **process engineering** and other industrial production ideas.

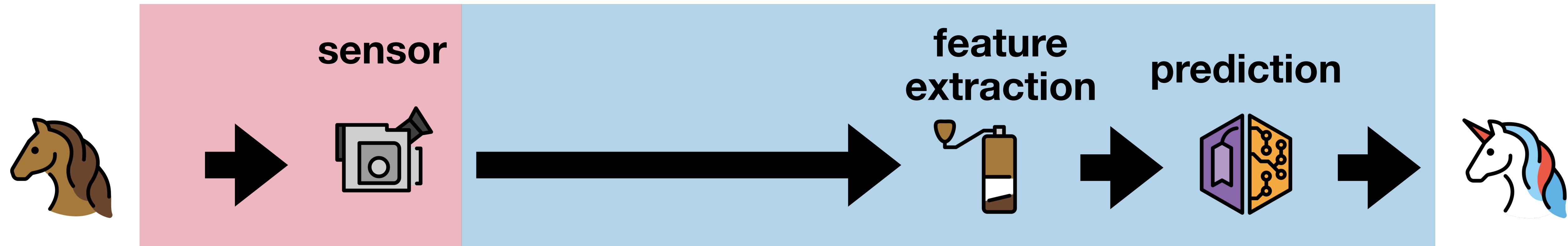
# Some final remarks



Rm Palaniappan, *Intense Talk*  
Mixed media on paper pasted on mount board

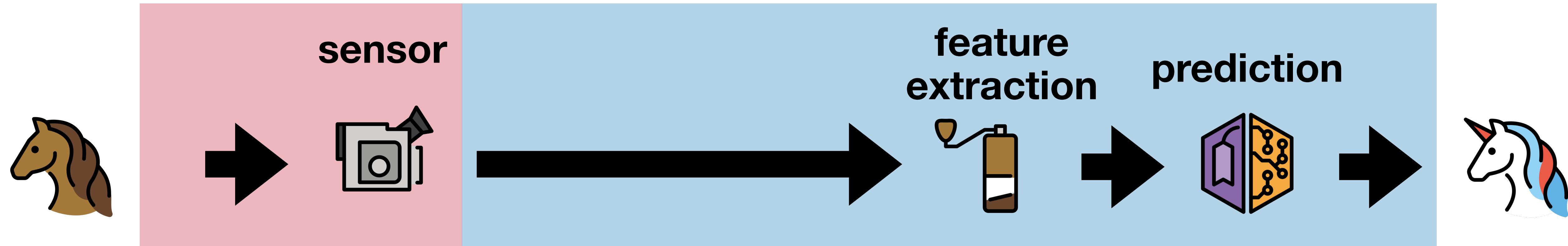
# Back to the original question

What does any of this mean for “AI for Science”?



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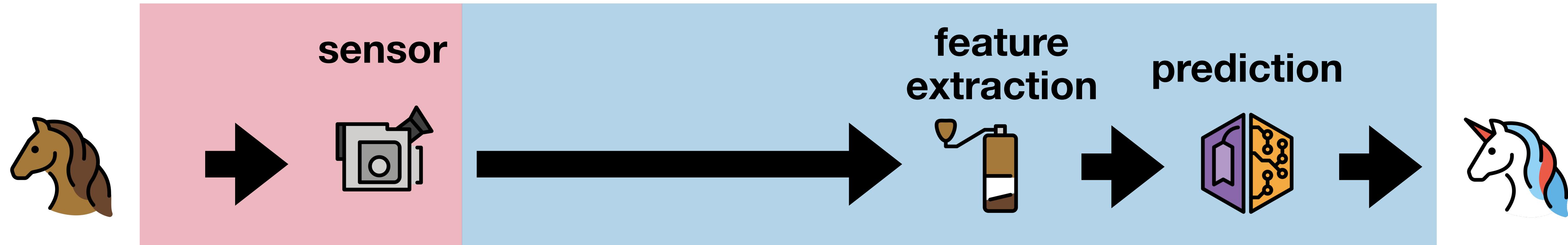
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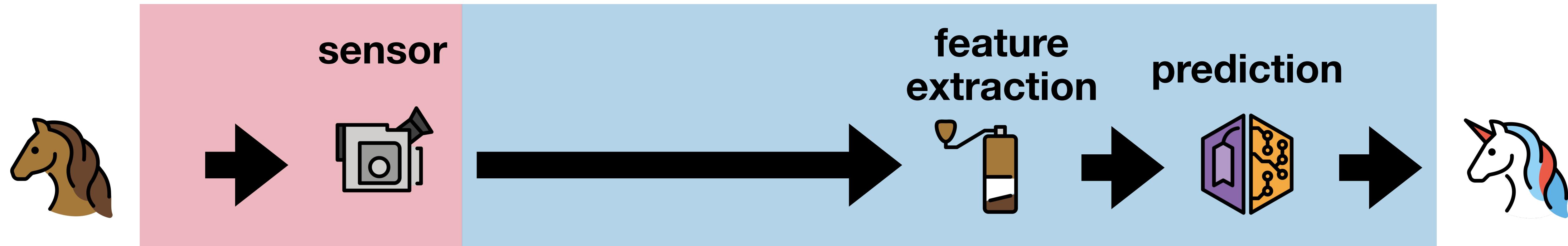


To use large ML/AI models as part of a scientific workflow, we need “interpretability” and “reliability.”

We also need to understand “reliability” for the training/fine-tuning processes.

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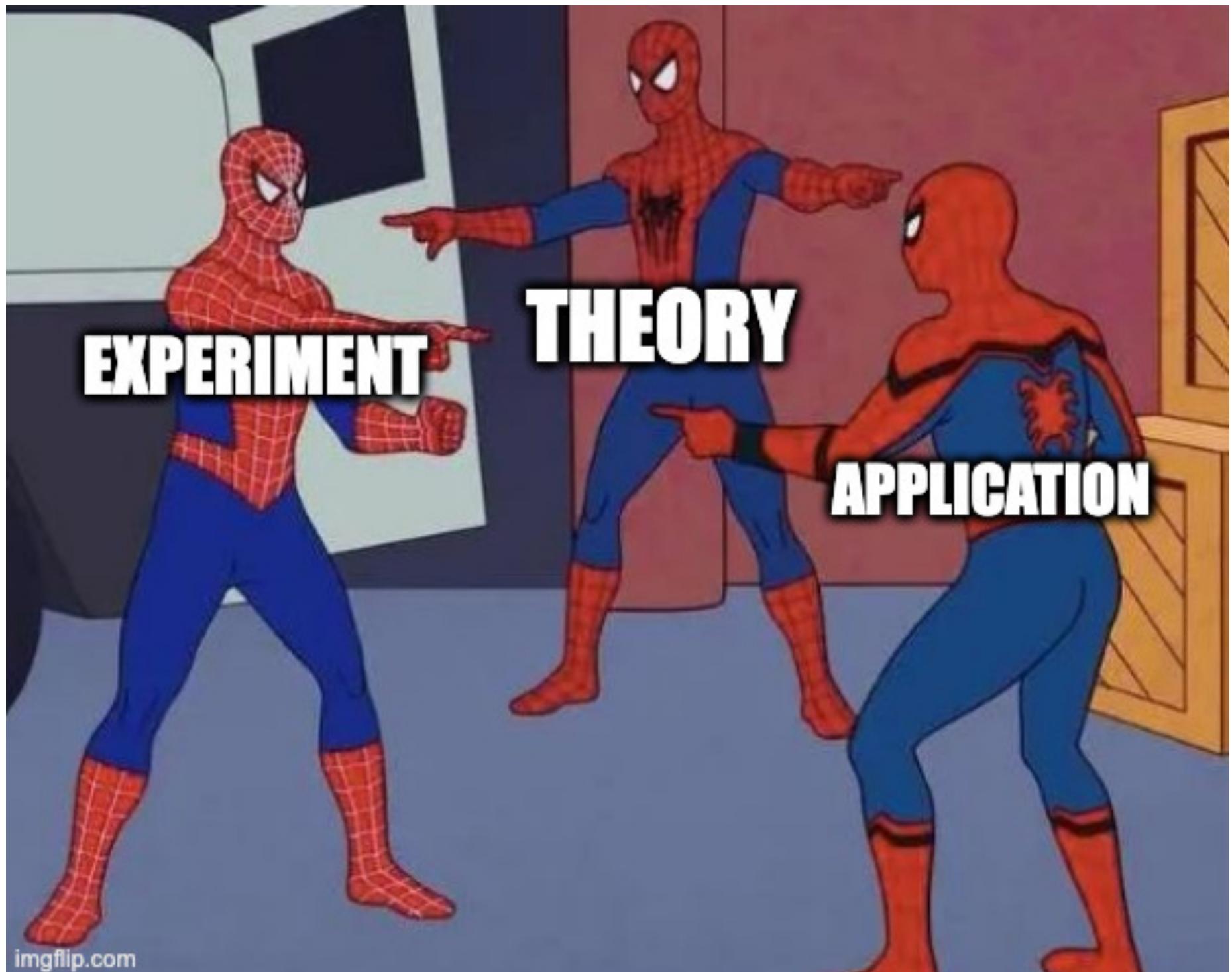
We also need to understand “reliability” for the training/fine-tuning processes.

It’s more important to **compare models directly** and not just their **performance**.

# Where is this all going?

Maybe some strange new worlds

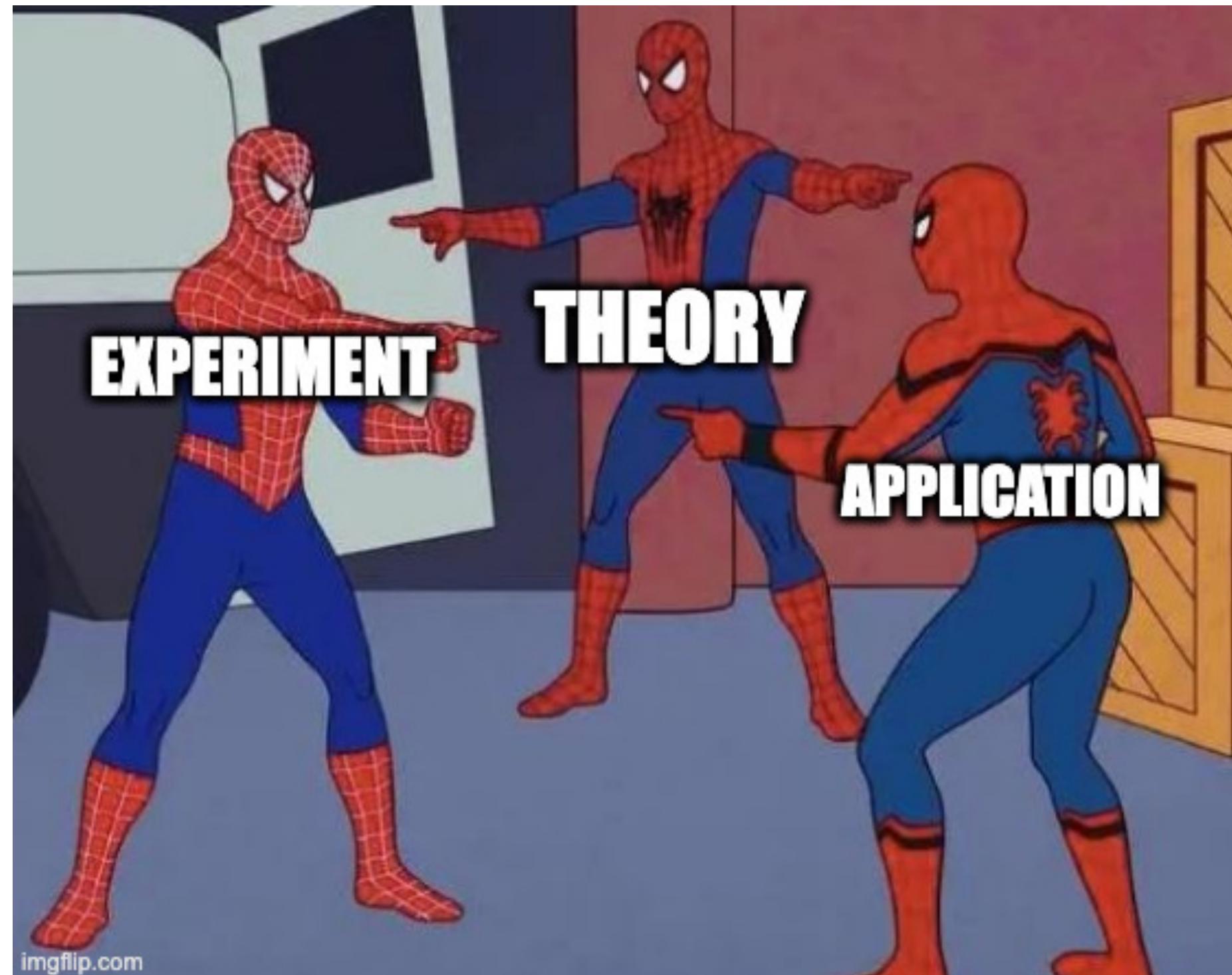
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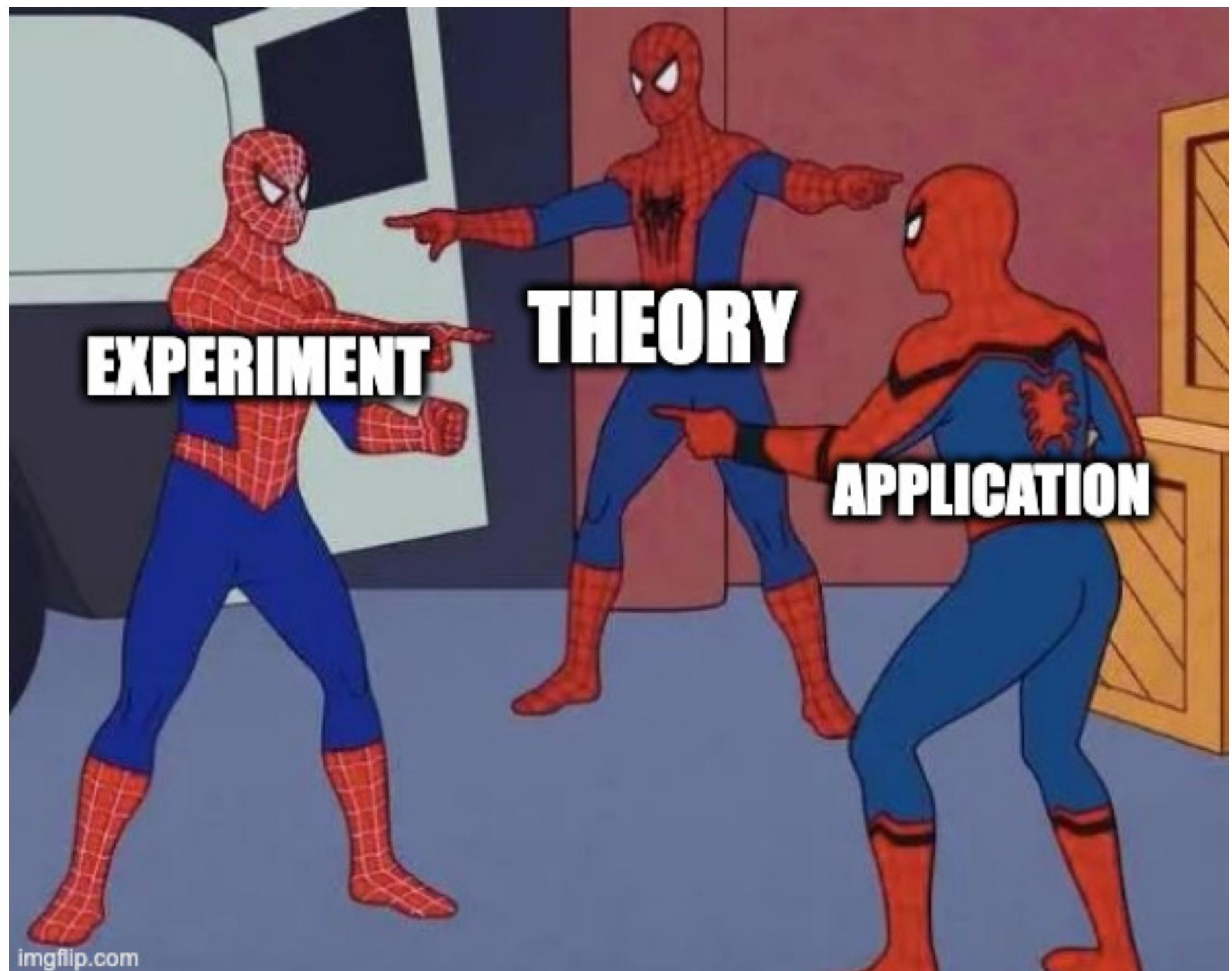


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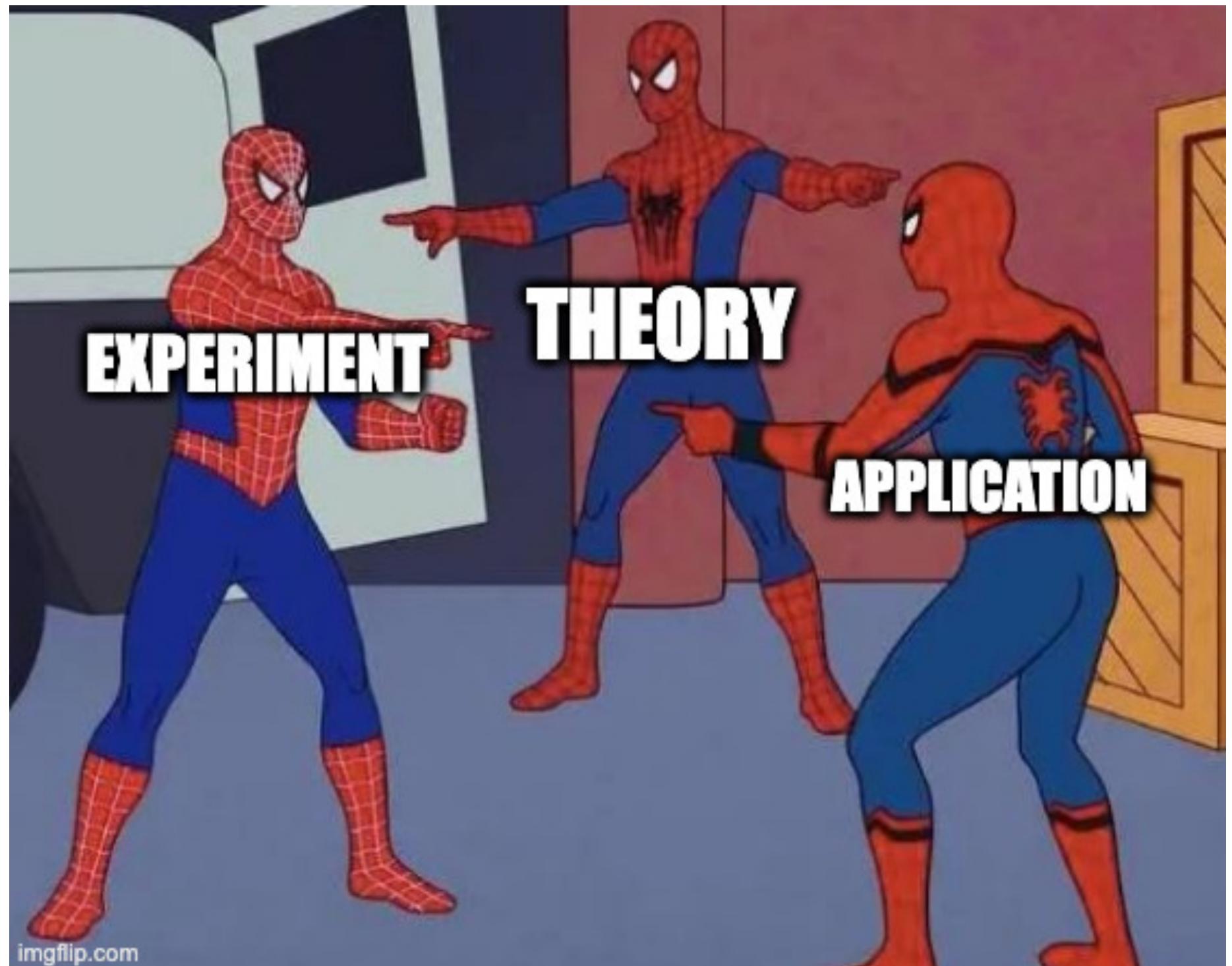


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- **Theory:** can we instead compare surrogate models like “faithful” NTK representations (Engel et al. 2024)?
- **Experiment:** can we do these comparisons cheaply (e.g. using academic-level resources)?
- **Application:** how do we use model comparisons in forensics, process engineering, ensembling, and beyond?

**谢谢大家的关注!**