

## HW 5 (IQB w18)

Due date: 19/2/18

1. Open and closed states of an ion channel is a prominent example of two state biological systems. Suppose  $P_o$  and  $P_c$  denote the probability of finding a given channel in open and closed states, respectively. Master equations describing open to close transitions in this two state system can be given by

$$\frac{dP_o}{dt} = -k_{-1}P_o + k_1P_c \quad \text{and} \quad \frac{dP_c}{dt} = k_{-1}P_o - k_1P_c$$

(a) (1 pt) Show that in the steady state (equilibrium) ratio of probabilities are given by:

$$\frac{P_o}{P_c} = \frac{k_1}{k_{-1}}$$

(b) (1 pt) Analyze the single channel recording data provided in the next page and estimate  $P_o/P_c$ .

(c) (1 pt) Suppose  $P_{\text{Open} \rightarrow \text{Close}} = 2/5$  and  $P_{\text{Close} \rightarrow \text{Open}} = 1/5$  using time-step of  $\Delta t = 1$  msec. Use computer simulation (kinetic Monte Carlo) to capture dynamics of opening / closing of a single ion channel; show 2 plots of current ~ time (as shown in the graph next page) between  $t=0$  to  $t=100$  msec. (assume fixed / constant current when a channel is open).

Challenge question: Estimate  $P_o/P_c$  from current ~ time graphs generated in part 1(c) and verify the relation proved in part 1(a).

state of  
channel:

closed

open

closed

open

closed

open

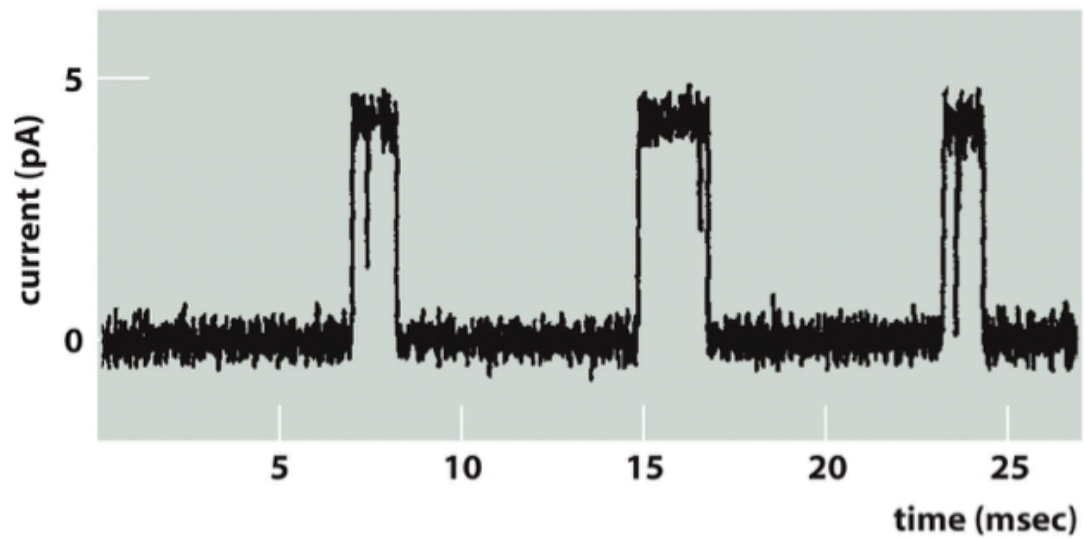


Figure 12-25 Essential Cell Biology, 4th ed. (© Garland Science 2014)

Ref:

Essential Cell Biology (by Alberts et al)

Physical Biology of the Cell (by Philips et al)