

①

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Question 1:

$$\begin{array}{r}
 11110 \\
 00111 \\
 00000 \\
 11010 \\
 11011
 \end{array}
 \quad
 \begin{array}{r}
 141 \\
 021 \\
 242
 \end{array}$$

a) slide = 7

$$\text{Output} = \underline{\underline{5-3}} + 1 \\ = 3$$

$$\begin{array}{r}
 111141 \\
 00102+ \\
 000242
 \end{array}$$

$$(1+4+1+1) = 7, \quad = 3$$

$$\begin{array}{r}
 111 \\
 011 \\
 000
 \end{array}
 \quad (1+4+1)+2+1 = 9.$$

$$110 \quad (1+4+2) = 8.$$

$$\begin{array}{r}
 111 \\
 000 \\
 000
 \end{array}
 \quad \boxed{1798}$$

$$\begin{array}{r}
 001 \\
 000 \\
 110
 \end{array}
 \quad 1+2+4 = 7.$$

$$\begin{array}{r}
 011 \\
 000 \\
 101
 \end{array}
 \quad 4+1+2+2 = 9.$$

$$\begin{array}{r}
 111 \\
 000 \\
 010
 \end{array}
 \quad (1+4+1)+9 = 10. \quad \boxed{17910}$$

②

0 0 0

$$\begin{array}{r} 1 \ 1 \ 0 \\ 1 \ 1 \ 0 \end{array}$$

$$2 + 2 + 4 = 8$$

0 0 0

1 0 1

1 0 1

$$1 + 2 + 2 = 5$$

0 0 0

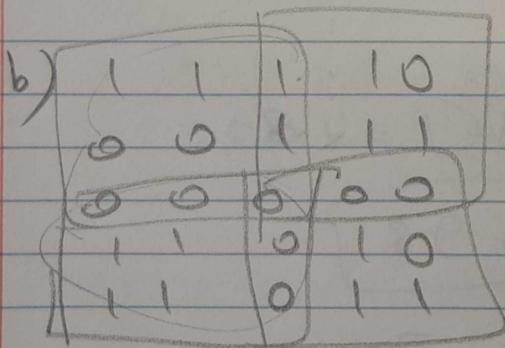
0 1 0

0 1 1

$$2 + 4 + 2 = 8.$$

output Qa

7	9	8
7	9	10
8	5	8



$$\begin{array}{r} 1 \ 4 \ 1 \\ 0 \ 2 \ 1 \\ 2 \ 4 \ 2 \end{array}$$

$$\begin{aligned} \text{Output} &= \frac{5-3}{2} + 1 \\ &= 2 \end{aligned}$$

$$\begin{array}{r} 1 \ 1 \ 1 \\ 0 \ 0 \ 1 \\ 0 \ 0 \ 0 \end{array}$$

$$1 + 4 + 1 + 1 = 7$$

$$\begin{array}{r} 1 \ 1 \ 0 \\ 1 \ 1 \ 1 \\ 0 \ 0 \ 0 \end{array}$$

$$1 + 1 + 2 + 1 = 5$$

(3)

0 0 0

1 1 0
1 1 0

$$2 + 2 + 4 = 8$$

0 0 0
0 1 0
0 1 1

$$2 + 1 + 2 = 5$$

output Q6

7	8
8	8

c) 1 pixel Padding, stride = 1

$$\text{output size} = \frac{7-3}{1} + 1 = 5.$$

0	0	0	0	0	0	0	1
0	1	1	1	0	0	0	141
0	0	0	1	1	1	0	021
0	0	0	0	0	0	0	242
0	1	1	0	1	0	0	
0	1	1	0	1	1	0	
0	0	0	0	0	0	0	

0 0 0

0 1 1
0 0 0

$$2 + 1 = 3$$

0 0 0

1 1 1
0 1 1

$$2 + 1 + 4 + 2 = 9$$

0 0 0

1 1 1
0 0 1

$$2 + 1 + 0 + 2 = 5$$

0 0 0

1 1 0
1 1 1

$$2 + 1 + 4 + 2 = 10$$

3,5,9,10,6

0 0 0

1 0 0
1 1 0

$$2 + 1 = 5$$

= 10

(4)

0	0	0	0	0	0	0	0
0	1	1	1	0	0	0	0
0	0	0	1	1	1	0	0
0	0	0	0	0	0	0	0
0	1	1	0	1	0	0	0
0	1	1	0	1	1	0	0
0	0	0	0	0	0	0	0

$$2+1=3$$

$$\begin{array}{r} 1 \ 1 \ 1 \\ 0 \ 0 \ 1 \\ 0 \ 0 \ 0 \end{array} \quad 1+4+1+1=7.$$

$$\begin{array}{r} 1 \ 1 \ 1 \\ 0 \ 1 \ 1 \\ 0 \ 0 \ 0 \end{array} \quad 2+1+1+4+1=9.$$

$$\begin{array}{r} 1 \ 1 \ 0 \\ 1 \ 1 \ 1 \\ 0 \ 0 \ 0 \end{array} \quad 1+4+2+1=8.$$

$$\begin{array}{r} 1 \ 0 \ 0 \\ 1 \ 1 \ 0 \\ 0 \ 0 \ 0 \end{array} \quad 1+2=3 \qquad \underline{1, 5, 7, 9, 8, 3}$$

(5)

$$\begin{array}{r} 000 \\ 000 \\ 011 \end{array}$$

$$\begin{array}{r} 001 \\ 000 \\ 110 \end{array}$$

$$\begin{array}{r} 011 \\ 000 \\ 101 \end{array}$$

$$9+9=6$$

$$1+2+1 = 4$$

$$9+1+2+2 = 9$$

$$\begin{array}{r} 111 \\ 000 \\ 010 \end{array}$$

$$\begin{array}{r} 110 \\ 000 \\ 100 \end{array}$$

$$1+4+1+4 = 10$$

$$1+4+2 = 7$$

76, 3, 9, 10, 7

$$\begin{array}{r} 000 \\ 011 \\ 011 \end{array}$$

$$\begin{array}{r} 000 \\ 110 \\ 110 \end{array}$$

$$\begin{array}{r} 000 \\ 101 \\ 101 \end{array}$$

$$\begin{array}{r} 000 \\ 010 \\ 011 \end{array}$$

$$2+1+9+2 = 9$$

$$0+2+2+4 = 8$$

$$1+2+2 = 5$$

$$2+9+2 = 8$$

$$\begin{array}{r} 100 \\ 110 \end{array}$$

$$2+4 = 6$$

9, 8, 5, 8, 6

$$\begin{array}{r}
 \begin{array}{ccccc}
 0 & 1 & 1 & 1 & 0 \\
 0 & 1 & 1 & 0 & \\
 0 & 0 & 1 & 0 & 0 \\
 \hline
 = 8 & & 1+9+2=7 & 3 & 4+2+1 \\
 1 & 0 & 0 & & \\
 \hline
 0 & 1 & 0 & 1+0+2=5 & \\
 0 & 0 & 0 & & \\
 \end{array}
 \end{array}$$

18, 7, 3, 7, 3

Max output Qc

3	5	9	10	6
5	7	9	?	3
6	7	9	10	7
9	8	5	8	6
8	7	3	7	5

d) Max Pooling size = 2
stride = 2

1	1	1	1	0
0	0	0	0	0
1	1	0	1	0
1	1	0	1	1

Output size =

$$\begin{aligned}
 N + 2P - F + 1 \\
 - S \\
 = 2.5
 \end{aligned}$$

We Need to use L2.5 aka 2×2

Output answer Qd

1	1
1	1

(P)

$$\begin{array}{r}
 \text{Q: } \begin{array}{cccc} 1 & 1 & 1 & 1 \\ 0 & 0 & 0 & 1 \\ 0 & 0 & 0 & 0 \\ 1 & 0 & 1 & 0 \\ 1 & 0 & 1 & 1 \end{array} \quad \begin{array}{r} 1 & - & 1 & - & 0 \\ - & - & - & - & \\ 0 & - & 0 & - & 0 \\ - & - & - & - & \\ 1 & - & 0 & - & 1 \end{array} \quad \begin{array}{r} 14 \\ 02 \\ 242 \end{array} \\
 \Rightarrow \quad \begin{array}{r} 1 & - & 1 & - & 0 \\ - & - & - & - & \\ 0 & - & 0 & - & 0 \\ - & - & - & - & \\ 1 & - & 0 & - & 1 \end{array} \quad \begin{array}{r} 14 \\ 02 \\ 242 \end{array}
 \end{array}$$

$$1+4+2+2 = 9$$

output $Q_C = [9]; 1 \times 1$

Question 2:

$$\theta = \left\lfloor \frac{I + 2P - K}{S} \right\rfloor + 1$$

We calculate for
W & H at
same time

Conv1: $\theta = \left\lfloor \frac{64 + 2 \times 1 - 3}{1} \right\rfloor + 1 = 64$

[Discard: $64 \times 64 \times 32$]

Conv2: $\theta = \left\lfloor \frac{64 + 2 - 7}{1} \right\rfloor + 1 = 58$

[Discard: $58 \times 58 \times 64$]

Pooling1: $\theta = \left\lfloor \frac{58 - 2}{2} \right\rfloor + 1 = 29$

[Discard: $29 \times 29 \times 64$]

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$$\text{Conv3: } O = \left\lfloor \frac{29+2(1)-3}{1} \right\rfloor + 1 = 29$$

Channels: 128

$$\boxed{\text{Dim: } 29 \times 29 \times 128}$$

$$\text{Conv4: } O = \left\lfloor \frac{29+0-7}{1} \right\rfloor + 1 = 23$$

$$\boxed{\text{Dim: } 23 \times 23 \times 256}$$

$$\text{Pool4: } O = \left\lfloor \frac{23-2}{2} \right\rfloor + 1 = 11$$

$$\boxed{\text{Dim: } 11 \times 11 \times 256}$$

$$\text{Dim of Flatten: } 11 \times 11 \times 256 = \boxed{30,976}$$

$$\text{Dim of Dense} = 10$$

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Question 5:

$$\begin{matrix} -7 & 0 & 1 \\ 2 & 3 & 4 \\ 5 & 6 & 3 \end{matrix} \quad \begin{matrix} 2 & 1 \\ 0 & -1 \end{matrix}$$

$$p=0 \\ s=1$$

then ReLU then
2x2 avg Pool

Conv → ReLU → Pool

$$-2 + (-3) = -5$$

$$1 - 4 = -3$$

$$2 \times 2 + 3 \times 1 - 6 = 1$$

$$3 \times 2 + 4 \times 1 - 7 = 3$$

output

$$5 \times 2 + 6 \times 1 + (-9) = 7$$

$$6 \times 2 + 7 \times 1 - 10 = 9$$

-5	-3
1	3
7	9

ReLU Operation: $\max(0, x)$

0	0
1	3
7	9

2x2 Pool Avg $(0+0+1+3)/4 = 1$

output of all Obs = [1]

Question 7:

In a transformer, the self attention mechanism calculates the output of x_i as follows:

1) Query: $q_i = w^Q x_i \in \mathbb{R}^{d_K}$

Key: $k_j = w^K x_i \in \mathbb{R}^{d_K}$

Value: $v_j = w^V x_i \in \mathbb{R}^{d_V}$

q_i is Query for x_i , k_j are all Keys for all inputs, & v_j are the values carrying the actual information.

2) Attention score: Q_i is compared with all keys to measure relevance

$$\text{Score}(x_i, x_j) = \frac{q_i \cdot k_j}{\sqrt{d_K}}$$

We need to maximize $\text{score}(x_i, x_i)$

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3) Softmax to get attention weights

$$\alpha_{ij} = \frac{\exp(score(x_i, x_j))}{\sum_l \exp(score(x_i, x_l))}$$

this gives how much x_i attends to each position in the sentence.

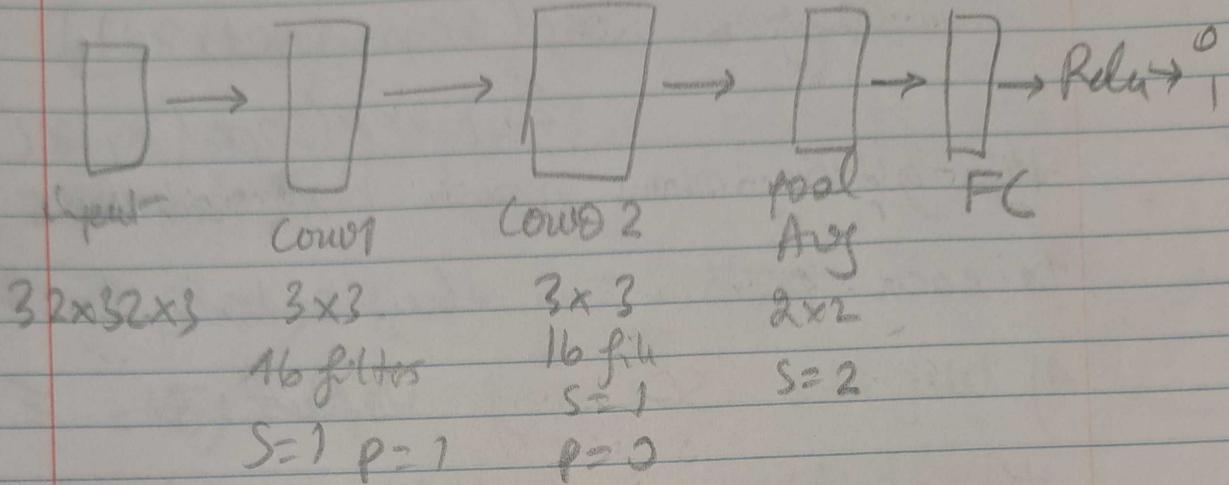
4) Weighted Sum of Values: $\tilde{x}_i = \sum_j \alpha_{ij} v_j$

This taking info from all tokens based on relevance to x_i .

Query \rightarrow look for Relevant Info in Sequence of Keys

then Gather Info (values) weighted by importance to produce a context-aware Representation \tilde{x}_i .

Question 3:



$$a) H_{out} = \lfloor \frac{32 + 2 \times 1 - 3}{1} \rfloor + 1 = 32$$

$$w_{out} = 32$$

$$\text{Depth} = 16$$

$$\text{total Neurons} = 32 \times 32 \times 16 = 16,384 \text{ Neurons}$$

Neurons = Height \times width \times Nb of Filters

$$b) \text{Weights per filter} = \underbrace{3 \times 3 \times 3}_{\substack{\text{filter} \\ \text{size}}} = 27$$

$$\text{total } W = 27 \times 16 = 432$$

$$\text{total } B = 16$$

$$\text{total } P = 5 = 448 \text{ parameters}$$

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$$c) H_{out} = \left\lfloor \frac{32 + 2 \times 0 - 3}{1} + 1 \right\rfloor = 30$$

$$w_{out} = 30$$

Depth = 16 (filters)

Nb of Neurons = 19,900 Neurons.

$$d) \underbrace{3 \times 3}_{\text{Filter size}} \times \underbrace{16}_{\text{Input depth}} = 144 \rightarrow \text{weight / Filter}$$

$$\text{total } W = 144 \times 16 = 2304$$

Total B = 16 (one per Filter)

$$\text{total } p_e = 2320$$

$$e) H_{out} = \left\lfloor \frac{(30 - 2)}{2} + 1 \right\rfloor = 15 = w_{out}$$

$$\text{Depth} = 16$$

After ReLU, No Chgs

$$\text{total features} = 15 \times 15 \times 16 = 3600 \text{ feat}$$

- g) -
 - fewer parameters
 - Non-linearity
 - better feature hierarchies
 - Improved Gradient Flow.

Question 4:

- 1) flatten the CNN output into a 10 vector.
- 2) Apply Logistic Regression: this will produce a prob for 2 classes
use if $\hat{y} \geq 0.5 \rightarrow \text{class 1}$
else class 0.

Dimensions: $15 \times 15 \times 16 = 3600$ features

Weights: 3600

Bias: 1

Total 3601 per vector

(15)

Question 6:

$$a) h_t = w_{in} x_t + w_{hh} h_{t-1}$$

$$b) x = [0.3, 0.4, 0.2], h_0 = 0.5, w_{in} = w_{hh} = \frac{why}{= 0.2}$$

$$h_1 = 0.2 \times 0.3 + 0.2 \times 0.5 = 0.16$$

$$h_2 = 0.2 \times 0.4 + 0.2 \times 0.16 = 0.112$$

$$h_3 = 0.2 \times 0.2 + 0.2 \times 0.112 = 0.0624$$

$$y = why h_3 = 0.2 \times 0.0624 = 0.01248$$

$$c) l = \frac{1}{2} (y - y_r)^2 \text{ let } e = y - y_r$$

$$\frac{\partial l}{\partial w_{hy}} = (y - y_r) h_3 = e h_3$$

$$h_3 = w_{in} (x_3 + w_{hh} x_2 + w_{hh}^2 x_1) + w_{hh}^3 h_0$$

$$\frac{\partial h_3}{\partial w_{in}} = x_3 + w_{hh} x_2 + w_{hh}^2 x_1 = \sum_{t=1}^{3-t} w_{hh}^{3-t} x^t$$

$$\frac{\partial l}{\partial w_{in}} = (y - y_r) w_{hy} \sum_{t=1}^3 w_{hh}^{3-t} x^t$$

$$\frac{\partial h_3}{\partial w_{hh}} = w_{in} (x_2 + 2w_{hh} x_1) + 3w_{hh}^2 h_0$$

$$\frac{\partial l}{\partial w_{hh}} = (y - y_r) w_{hy} (w_{in} (x_2 + 2w_{hh} x_1) + 3w_{hh}^2 h_0)$$

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$$d) y_1 = 0.4, \gamma = 0.15.$$

$$h_3 = 0.0624, y = 0.01248, e = -0.38752.$$

$$\frac{\partial L}{\partial w_{hy}} = -0.02418 = e \cdot h_3.$$

$$\begin{aligned} \frac{\partial L}{\partial w_{hh}} &= e \cdot w_{hy} (x_3 + w_{hh} x_2 + w_{hh}^2 x_1) \\ &= -0.38752 \times 0.2 (0.2 + 0.2 \times 0.4 + 0.2^2 \times 0.3) \\ &= -0.02263 \end{aligned}$$

$$\begin{aligned} \frac{\partial L}{\partial w_{hh}} &= e \cdot w_{hy} (w_{hh} (x_2 + 2w_{hh} x_1) + 3w_{hh}^2 h_0) \\ &= -0.38752 \times 0.2 (0.2 (0.4 + 0.2 \times 2 \cdot 0.3) \\ &\quad + 3 \times 0.2^2 \times 0.5) \end{aligned}$$

$$= -0.027606$$

$$w_k^{New} = w_k^{Old} - \eta \frac{\partial L}{\partial w_k}.$$

$$w_{in}^{New} = 0.2 - 0.15 (-0.0226 \dots)$$

$$= 0.20339$$

$$w_{hh}^{New} = 0.091906$$

$$w_{hy}^{New} = 0.203627$$