

# Wine and Obesity Data Analysis

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## 1. Dataset Overview

### A. Wine Quality Dataset

- **Collection Year:** Dataset was collected in 2009.
- **Study Type:** The study is observational. Each wine was independently sampled.
- **Description:** Physiochemical properties for red and white Portuguese “Vinho Verde” wines.
- **Size:** 6497 rows, 12 columns
- **Variables:** fixed\_acidity, volatile\_acidity, citric\_acid, residual\_sugar, chlorides, free\_sulfur\_dioxide, total\_sulfur\_dioxide, density, ph, sulphates, alcohol, quality, color

Table 1: Dataset 1 Variables

Variable Name	Type	Description
fixed_acidity	Continuous	
volatile_acidity	Continuous	
citric_acid	Continuous	
residual_sugar	Continuous	
chlorides	Continuous	
free_sulfur_dioxide	Continuous	
total_sulfur_dioxide	Continuous	
density	Continuous	
pH	Continuous	
sulphates	Continuous	
alcohol	Continuous	
quality	Integer	score between 0 and 10
color	Categorical	red or white

### Sampling Distribution of Density

The following histogram shows the sampling distribution of the **sample mean of the density variable**.

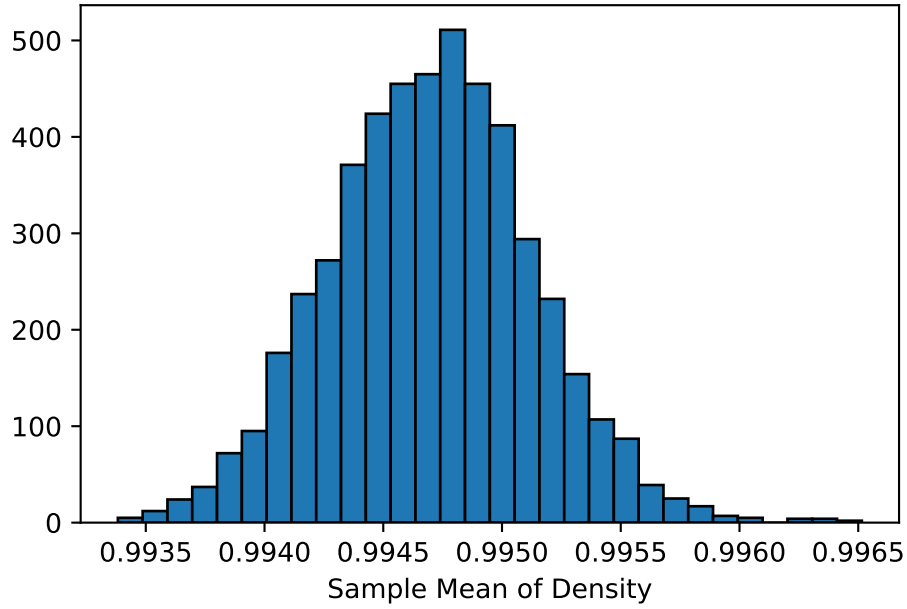


Figure 1: Sampling Distribution of Sample Mean (Density)

Figure 1 shows the sampling distribution of the sample mean of wine densities. There is a heavy clustering with similar frequencies from 0.9945 to 0.995 g/ml. The right tail appears thinner than the left tail but with small frequencies. The shape of the sampling distribution is approximately normal with little to no skew.

## B. Obesity Dataset

- **Collection Year:** The dataset was collected in 2019.
- **Study Type:** The study is observational, each person was measured independently.
- **Description:** Estimation of obesity levels in individuals from Mexico, Peru, and Colombia, based on eating habits and physical condition.
- **Size:** 2111 rows, 16 columns
- **Variables:** Gender, Age, Height, Weight, Family\_history\_with\_overweight, FAVC, FCVC, NCP, CAEC, SMOKE, CH20, SCC, FAF, TUE, CALC, MTRANS, NObeyesdad

Table 2: Dataset 2 Variables

Variable Name	Type	Description	Units
Gender	Categorical	Biological sex	-
Age	Continuous	Age in years	Years
Height	Continuous	Height	Meters
Weight	Continuous	Weight	Kg
Family_history_with_overweight	Binary	Family history of overweight	-
FAVC	Binary	Frequent high-calorie food intake	-
FCVC	Integer	Frequency of vegetable consumption	-
NCP	Continuous	Number of main meals per day	Count
CAEC	Categorical	Snacking between meals	-
SMOKE	Binary	Smokes or not	-
CH20	Binary	Monitors calorie intake	-
SCC	Continuous	Physical activity frequency	Hours/Week
FAF	Continuous	Daily screen/technology use	Hours
TUE	Continuous	Daily electronics use	Hours
CALC	Categorical	Alcohol consumption	-
MTRANS	Categorical	Mode of transportation	-
NObeyesdad	Categorical	Obesity classification	-

## Sampling Distribution of Weight

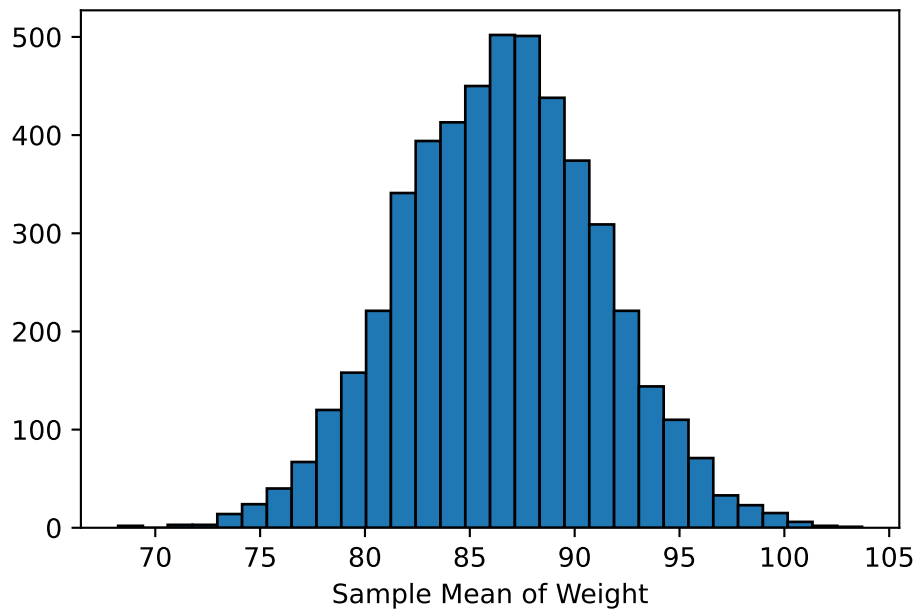


Figure 2: Sampling Distribution of Sample Mean (Weight)

Figure 2 shows the sampling distribution of the sample mean of individual weights. The histogram is approximately symmetric and bell-shaped, resembling the normal distribution. The sample clusters around 87 and 88 Kg, with a slightly larger frequency on the left of the center than the right. There is no noticeable skewness.

---

## 2. One-Sample T-Test: Wine Alcohol Content

### 2.1 Research Question and Hypothesis

**Research Question:** Is the average alcohol content of red and white wine greater than 10.5%?

**Hypotheses:** The null hypothesis states that the population mean alcohol content is equal to 10.5%, while the alternate hypothesis claims the population mean alcohol content of red and white wine is greater than 10.5%.

## 2.2 Assumptions

## 2.3 Test

### Results:

In the one-sample t-test, the sample mean was 10.492, with a corresponding t-statistic of  $-0.5541$ . At a significance level of  $\alpha = 0.05$ , the critical t-value for a one-tailed test was 1.6451. The resulting one-tailed p-value was 0.7102. Since the test statistic does not exceed the critical value and the p-value is greater than  $\alpha$ , there is insufficient evidence to reject the null hypothesis. Lastly, the 95% confidence interval for the population mean was (10.4628, 10.5208).

## 2.4 Conclusion:

Since the critical t-value was greater than  $\alpha$ , we fail to reject the null hypothesis. There is insufficient evidence that the mean alcohol content exceeds 10.5%.

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### 3. Bootstrap Approach: Wine pH

#### 3.1 Bootstrap Distribution

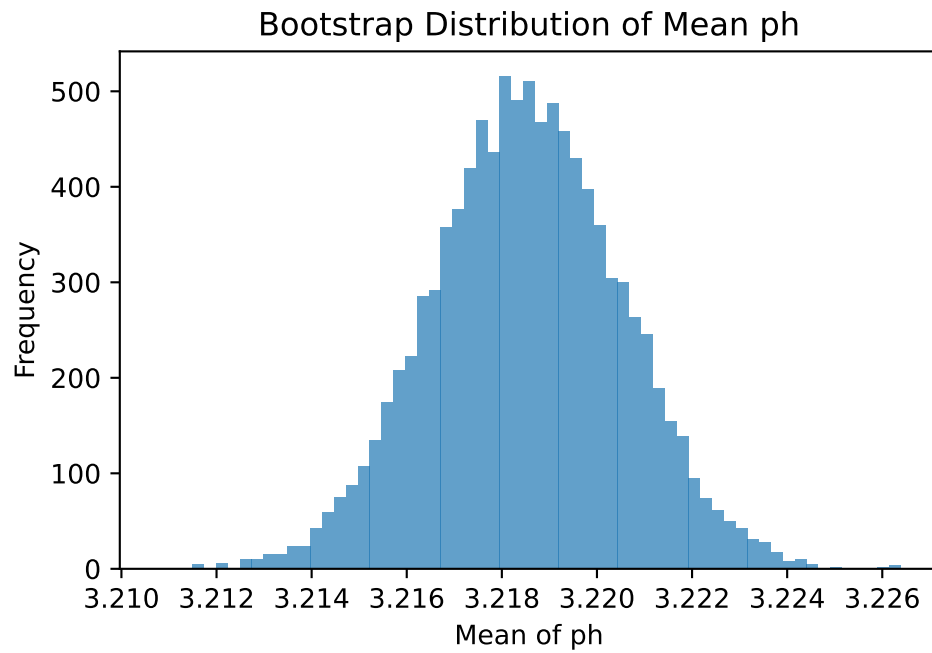


Figure 3: Bootstrap Distribution of Wine pH

### 3.2 QQ Plot for Bootstrap

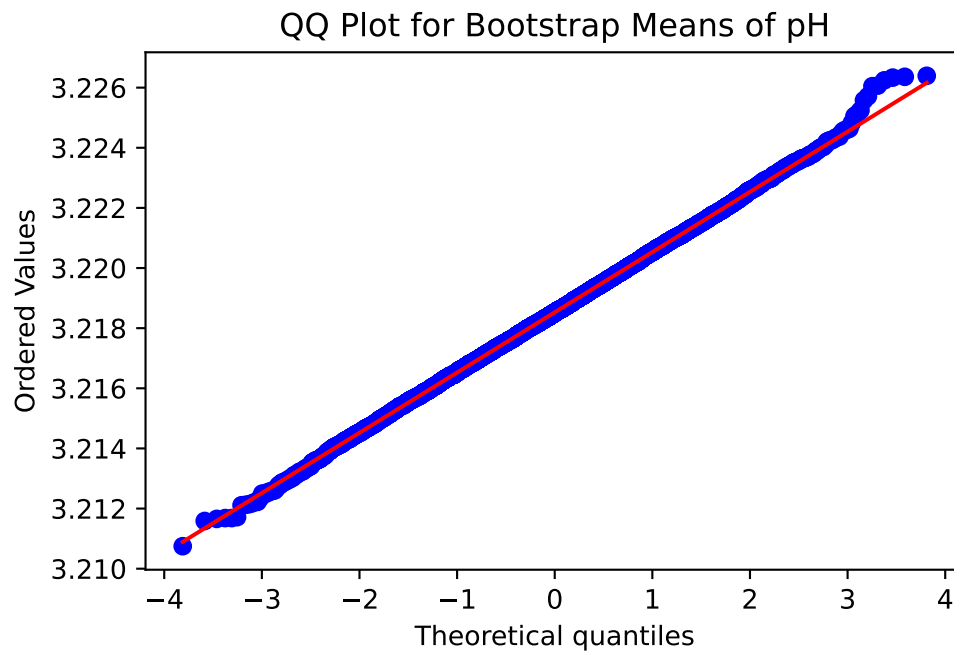


Figure 4: QQ Plot of Bootstrap Means (pH)

### 3.3 Bootstrap Confidence Interval

The bootstrap test CI was calculated to be (3.2146051639218105, 3.2224704863783282)

**Conclusion:** Using an  $\alpha$  of 0.05, We are 95% confident that the true population mean pH lies between 3.215 and 3.222.



## 4. Analysis of Variance (Wine Dataset)

### 4.1 F Test

### 4.2 ANOVA Table

### 4.3 AVOVA Assumptions Check

### 4.4 Conclusion

---

## 5. Multiple Comparisons (Obesity Dataset)

### 5.1 ANOVA Model and Assumptions

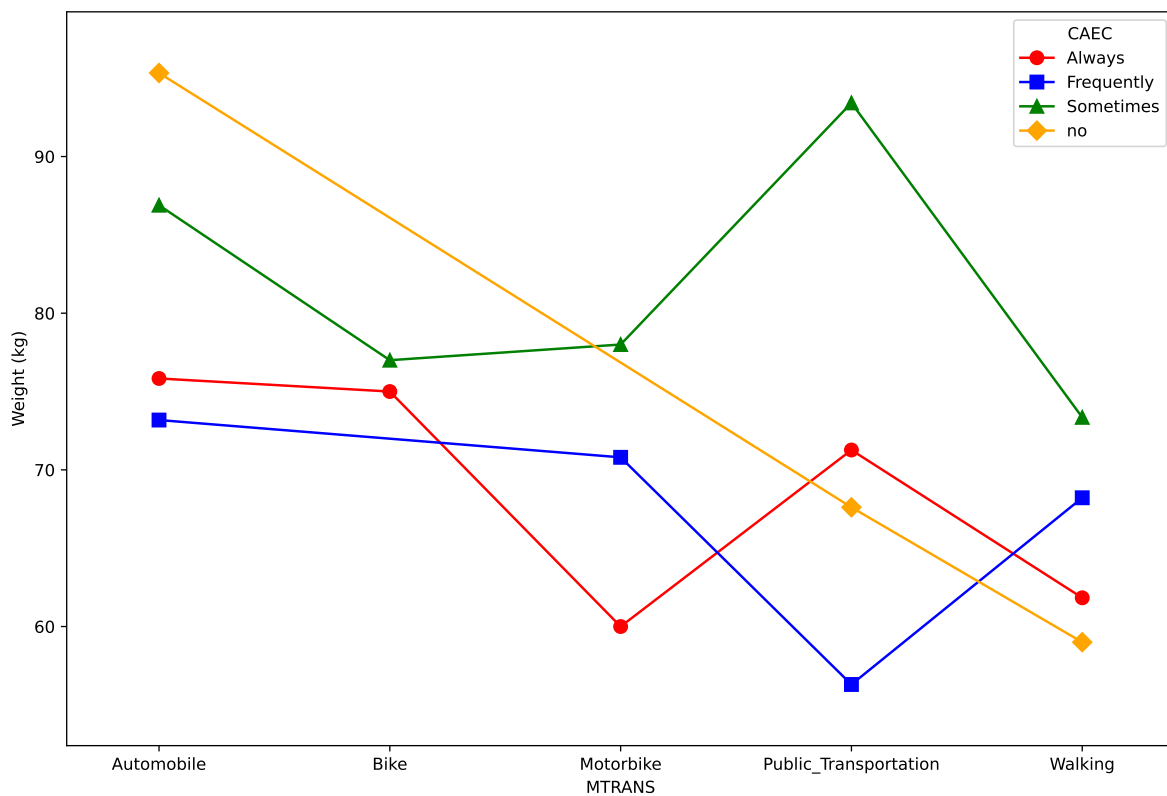


Figure 5: Two-way ANOVA with interaction:  $\text{Weight} \sim \text{MTRANS} * \text{CAEC}$

- **Interpretation:** Based on Figure 5, Weight differs across the different MTRANS (Method of Transportation) categories. The lines for different CAEC (Snacking between Meals) overlap, suggesting a relationship exists between MTRANS and CAEC levels.

## 5.2 QQ Plot and Residual Analysis:

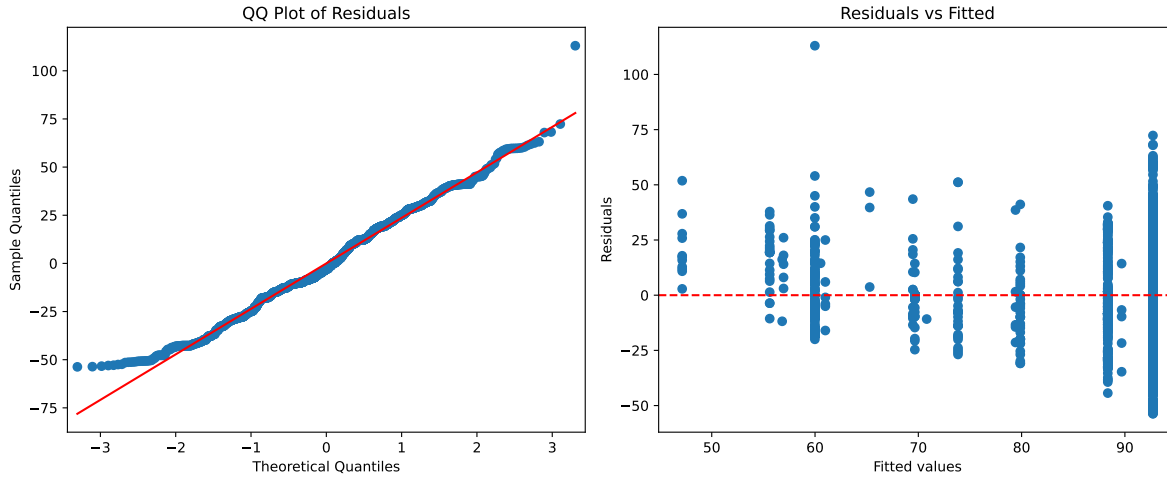


Figure 6: QQ Plot and Residual Plot

- The left plot in Figure 6 is the QQ plot, which shows approximate normality as the data falls around the line. There is a single datapoint on the far right tail that is deviated from the normal line, indicating a potential outlier. On the left end of the normal line, the datapoints appear to have a curvature away from the normal.
- The right plot in Figure 6 shows the corresponding residual plot. The datapoints shows no clear pattern, however there is a singular point that has an abnormally high residual around (60, 120), which is most likely the outlier that was observed in the QQ plot.
- **Conclusion:** Overall, the ANOVA assumptions of normality, independence, and equal variance are satisfied.

## 5.3 F-Tests for Factors

Table 3: ANOVA results for MTRANS and CAEC factors

Factor	F-statistic	F-critical	p-value	Conclusion
MTRANS	6.85	2.376	$1.78 \times 10^{-5}$	Reject H : At least one group mean differs
CAEC	149.69	2.609	$1.11 \times 10^{-16}$	Reject H : At least one group mean differs

**Interpretation:** Both MTRANS and CAEC significantly affect Weight; differences between group means are unlikely due to chance.

## 5.4 Pairwise Comparisons

Table 4: Tukey HSD Pairwise Comparison for MTRANS

	Transportion A	Transportion B	meandiff	p-adj	lower	upper	reject
0	Automobile	Bike	-9.1933	0.8866	-36.2772	17.8906	False
1	Automobile	Motorbike	-12.8167	0.4894	-34.5151	8.8817	False
2	Automobile	Public Transportation	1.5791	0.7845	-2.1981	5.3563	False
3	Automobile	Walking	-15.3115	0.0003	-25.3800	-5.2430	True
4	Bike	Motorbike	-3.6234	0.9985	-38.0069	30.7601	False
5	Bike	Public Transportation	10.7724	0.8109	-16.1659	37.7107	False
6	Bike	Walking	-6.1182	0.9772	-34.6275	22.3911	False
7	Motorbike	Public Transportation	14.3958	0.3584	-7.1206	35.9122	False
8	Motorbike	Walking	-2.4948	0.9984	-25.9482	20.9586	False
9	Public Transportation	Walking	-16.8906	0.0000	-26.5606	-7.2206	True

- **Transportion A, Transportion B:** The two transportation categories being compared.
- **meandiff:** Difference in group means (B minus A).
- **p-adj:** P-value adjusted for multiple comparisons to control the family-wise error rate.
- **lower, upper:** Lower and upper bounds of the 95% confidence interval for the mean difference.
- **reject:** Indicates whether the null hypothesis of equal means is rejected at  $\alpha = 0.05$ .

**Conclusion:** From Table 4, the Tukey HSD pairwise comparisons revealed a few significant differences between pairs of transportation methods. There were differences between Automobile vs. Walking and also Public Transportation vs. Walking. The mean difference in Weight were 15.3 and 16.9 respectively. These results suggest that walking is associated with a lower average weight.

Table 5: Tukey HSD Pairwise Comparison for CAEC

	CAEC A	CAEC B	meandiff	p-adj	lower	upper	reject
0	Always	Frequently	-12.2049	0.0041	-21.4825	-2.9273	True
1	Always	Sometimes	20.2698	0.0000	11.7416	28.7980	True
2	Always	no	-2.1881	0.9659	-14.1876	9.8115	False
3	Frequently	Sometimes	32.4747	0.0000	28.2813	36.6681	True
4	Frequently	no	10.0168	0.0322	0.5911	19.4425	True
5	Sometimes	no	-22.4579	0.0000	-31.1469	-13.7688	True

- **CAEC A, CAEC B:** The two frequencies of snacking categories being compared.
- **meandiff:** Difference in group means (B minus A).
- **p-adj:** P-value adjusted for multiple comparisons to control the family-wise error rate.
- **lower, upper:** Lower and upper bounds of the 95% confidence interval for the mean difference.
- **reject:** Indicates whether the null hypothesis of equal means is rejected at  $\alpha = 0.05$ .

**Conclusion:**

## 6. References

Cortez, Paulo, et al. "Wine Quality." UCI Machine Learning Repository, 2009, <https://doi.org/10.24432/C56S3T>.

"Estimation of Obesity Levels Based On Eating Habits and Physical Condition ." UCI Machine Learning Repository, 2019, <https://doi.org/10.24432/C5H31Z>.

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## 7. Code Appendix

```
from ucimlrepo import fetch_ucirepo
import pandas as pd
from scipy import stats
import numpy as np
import matplotlib.pyplot as plt
from statsmodels.graphics.factorplots import interaction_plot
import statsmodels.api as sm
import statsmodels.formula.api as smf
import seaborn as sns

# Fetch the Wine Quality dataset
wine_quality = fetch_ucirepo(id=186)

# Features and targets as pandas DataFrames
X = wine_quality.data.features
y = wine_quality.data.targets

estimation_of_obesity_levels_based_on_eating_habits_and_physical_condition = (
    fetch_ucirepo(id=544)
)
X2 = (
    estimation_of_obesity_levels_based_on_eating_habits_and_physical_condition.d
    ata.features
)
y2 = (
    estimation_of_obesity_levels_based_on_eating_habits_and_physical_condition.d
    ata.targets
)

# -----
# Sampling Distributions (Both Datasets)
# -----
def plot_histogram_q1():
    data = X["density"].values

    sample_size = 50
    num_samples = 5000

    sample_means = []
```

```

for i in range(num_samples):
    sample = np.random.choice(data, size=sample_size, replace=True)
    sample_means.append(np.mean(sample))

plt.hist(sample_means, bins=30, edgecolor="black")
plt.xlabel("Sample Mean of Density")
# plt.title("Sampling Distribution of Sample Mean (Density)")
plt.show()

def plot_histogram_q2():
    data = X2["Weight"].values
    sample_size = 30
    num_samples = 5000
    sample_means = []
    for i in range(num_samples):
        sample = np.random.choice(data, size=sample_size, replace=True)
        sample_means.append(np.mean(sample))
    plt.hist(sample_means, bins=30, edgecolor="black")
    plt.xlabel("Sample Mean of Weight")
    # plt.title("Sampling Distribution of Sample Mean (Weight)")
    plt.show()

# -----
# Bootstrap (Wine Quality Dataset)
# -----
def bootstrap():
    # wine_quality = fetch_ucirepo(id=186)
    X = wine_quality.data.features
    df = X["pH"].values

    iter = 10000
    runs = np.zeros(iter)

    for i in range(iter):
        sample = np.random.choice(df, size=len(df), replace=True)
        runs[i] = np.mean(sample)
    return runs

def plot_bootstrap(runs):

```

```

plt.hist(x=runs, bins="auto", alpha=0.7)
plt.xlabel("Mean of ph")
plt.ylabel("Frequency")
plt.title("Bootstrap Distribution of Mean ph")
plt.show()

def bootstrap_qq(vals):
    stats.probplot(vals, dist="norm", plot=plt)
    plt.title("QQ Plot for Bootstrap Means of pH")
    plt.show()

# -----
# ANOVA and Interaction Model (Obesity Dataset)
# -----
def mult_comparisons():
    # fetch dataset
    # estimation_of_obesity_levels_based_on_eating_habits_and_physical_condition
    = fetch_ucirepo(id=544)

    # data (as pandas dataframes)
    # X = estimation_of_obesity_levels_based_on_eating_habits_and_physical_condition.data.features
    # y = estimation_of_obesity_levels_based_on_eating_habits_and_physical_condition.data.targets

    # metadata
    # print(estimation_of_obesity_levels_based_on_eating_habits_and_physical_condition.metadata)

    # variable information
    # print(estimation_of_obesity_levels_based_on_eating_habits_and_physical_condition.variables)

    df = pd.concat([X2, y2], axis=1)
    df.columns = list(X2.columns) + list(y2.columns)

    df["MTRANS_str"] = df["MTRANS"].astype(str)
    df["CAEC_str"] = df["CAEC"].astype(str)

    # Interaction plot
    fig, ax = plt.subplots(figsize=(12, 8))

```

```

interaction_plot(
    df["MTRANS"],
    df["CAEC"],
    df["Weight"],
    colors=["red", "blue", "green", "orange"],
    markers=["o", "s", "^", "D"],
    ms=8,
    ax=ax, # pass axes to avoid auto (a)/(b)
)
ax.set_xlabel("MTRANS")
ax.set_ylabel("Weight (kg)")
# ax.set_title('Interaction Plot: Weight by MTRANS and CAEC')

plt.show()

model = smf.ols("Weight ~ C(MTRANS) + C(CAEC)", data=df).fit()

return model

def plot_resid_fitted(model):
    residuals = model.resid
    fitted = model.fittedvalues
    # Create plots
    fig, ax = plt.subplots(1, 2, figsize=(12, 5))

    # 1. Q-Q plot of residuals
    sm.qqplot(residuals, line="s", ax=ax[0])
    ax[0].set_title("QQ Plot of Residuals")

    # 2. Residuals vs Fitted plot
    ax[1].scatter(fitted, residuals)
    ax[1].axhline(0, color="red", linestyle="--")
    ax[1].set_xlabel("Fitted values")
    ax[1].set_ylabel("Residuals")
    ax[1].set_title("Residuals vs Fitted")

    plt.tight_layout()
    plt.show()

def hypothesis_test(model):
    anova_table = sm.stats.anova_lm(model, typ=2)

```



```

# 4. Hypothesis test for equality of means
# Calculate MSA and MSB
msa = anova_table["sum_sq"]["C(MTRANS)"] / anova_table["df"]["C(MTRANS)"]
msb = anova_table["sum_sq"]["C(CAEC)"] / anova_table["df"]["C(CAEC)"]
mse = anova_table["sum_sq"]["Residual"] / anova_table["df"]["Residual"]

# Calculate F-statistics
f_stat_a = msa / mse
f_stat_b = msb / mse
print(f"F-statistic for MTRANS: {f_stat_a}")
print(f"F-statistic for CAEC: {f_stat_b}")

# Critical F-value
alpha = 0.05
f_crit_a = stats.f.ppf(
    1 - alpha, anova_table["df"]["C(MTRANS)"], anova_table["df"]["Residual"]
)
f_crit_b = stats.f.ppf(
    1 - alpha, anova_table["df"]["C(CAEC)"], anova_table["df"]["Residual"]
)
print(f"Critical F-value for MTRANS: {f_crit_a}")
print(f"Critical F-value for CAEC: {f_crit_b}")

# p-values
p_value_a = 1 - stats.f.cdf(
    f_stat_a, anova_table["df"]["C(MTRANS)"], anova_table["df"]["Residual"]
)
p_value_b = 1 - stats.f.cdf(
    f_stat_b, anova_table["df"]["C(CAEC)"], anova_table["df"]["Residual"]
)
print(f"P-value for MTRANS: {p_value_a}")
print(f"P-value for CAEC: {p_value_b}")

# Conclusion
if f_stat_a > f_crit_a:
    print(
        "Reject null hypothesis for MTRANS: At least one group mean is
different."
    )
else:
    print(
        "Fail to reject null hypothesis for MTRANS: No significant
difference between group means."
    )

```

```

    )
    if f_stat_b > f_crit_b:
        print("Reject null hypothesis for CAEC: At least one group mean is
different.")
    else:
        print(
            "Fail to reject null hypothesis for CAEC: No significant difference
between group means."
        )

    return anova_table

def multiple_comparisons(model):
    from statsmodels.stats.multicomp import pairwise_tukeyhsd
    import pandas as pd

    # Extract dataframe used in the model
    df = model.model.data.frame.copy()

    # Convert factors to string for Tukey labels
    df["MTRANS_str"] = df["MTRANS"].astype(str)
    df["CAEC_str"] = df["CAEC"].astype(str)

    # --- Tukey for MTRANS ---
    tukey_mtrans = pairwise_tukeyhsd(
        endog=df["Weight"], groups=df["MTRANS_str"], alpha=0.05
    )

    # Convert Tukey result to DataFrame
    mtrans_df = pd.DataFrame(
        data=tukey_mtrans._results_table.data[1:], # skip header row
        columns=tukey_mtrans._results_table.data[0], # use header row
    )

    # --- Tukey for CAEC ---
    tukey_caec = pairwise_tukeyhsd(
        endog=df["Weight"], groups=df["CAEC_str"], alpha=0.05
    )

    caec_df = pd.DataFrame(
        data=tukey_caec._results_table.data[1:],
        columns=tukey_caec._results_table.data[0],
    )

```

```

    )
    return mtrans_df, caec_df

# -----
# Summary Statistics (Both Datasets)
# -----
def quantitative_summary(df, title):
    number_df = df.select_dtypes(include="number")

    # compute summary statistics
    summary = pd.DataFrame(
        {
            # Measures of Central Tendency
            "Mean": number_df.mean(), # find means
            "Median": number_df.median(), # find medians
            "Mode": number_df.mode().iloc[0], # find modes
            # Measures of Variability
            "Range": number_df.max() - number_df.min(), # find ranges
            "Variance": number_df.var(), # find variances
            "Standard Deviation": number_df.std(), # find standard deviations
            "IQR": number_df.quantile(0.75)
            - number_df.quantile(0.25), # find interquartile ranges
        }
    )

    # create figure and axes
    figure, axes = plt.subplots(figsize=(14, 6))
    axes.axis("off") # hide plot axes

    # create summary table
    summary_table = plt.table(
        cellText=summary.round(4).values, # round 4 decimal places
        rowLabels=summary.index, # label rows
        colLabels=summary.columns, # label columns
        loc="center", # center table
        cellLoc="center", # center text
    )

    # size table
    summary_table.scale(1, 2)

    # add title

```

```

plt.title(title)
plt.show()

def category_summary(df, title, wine_flag=False):
    # For wine quality dataset
    if wine_flag:
        category_columns = df.columns

    # For obesity dataset
    else:
        category_columns = df.select_dtypes(exclude="number").columns

    # categorical variable summary
    for col in category_columns:
        categorical_summary = pd.DataFrame(
            {
                "Quality Score": df[col]
                    .value_counts()
                    .sort_index()
                    .index, # find quality scores
                "Frequency": df[col].value_counts().sort_index(), # find
frequencies
                "Proportion": df[col]
                    .value_counts(normalize=True)
                    .sort_index(), # find proportions
            }
        )

        # create figure and axes
        figure, axes = plt.subplots(figsize=(14, 6))
        axes.axis("off") # hide plot axes

        # create summary table
        summary_table = plt.table(
            cellText=categorical_summary.round(4).values, # round 4 decimal
places
            colLabels=categorical_summary.columns, # label columns
            loc="center", # center table
            cellLoc="center", # center text
        )

        # size table

```

```

summary_table.scale(1, 3)

# add title
plt.title(f"{title}: {col}")
plt.show()

# -----
# One Sample Test (Wine Quality Dataset)
# -----
def alcohol_t_test():
    # get variable of interest
    alcohol_content = X["alcohol"].values

    # Hypothesized population mean
    pop_mean = 10.5

    # Sample statistics
    n = len(alcohol_content)
    df = n - 1
    sample_mean = np.mean(alcohol_content)
    sample_std = np.std(alcohol_content, ddof=1)

    # Compute t-statistic manually
    t_statistic = (sample_mean - pop_mean) / (sample_std / np.sqrt(n))

    # Find t-critical value for one-tailed test
    alpha = 0.05
    t_crit = stats.t.ppf(1 - alpha, df)

    # Print results
    print(f"Sample mean: {sample_mean:.4f}")
    print(f"T-statistic: {t_statistic:.4f}")
    print(f"T-critical (one-tailed, alpha={alpha}): {t_crit:.4f}")

    # Decision based on t-critical
    if t_statistic > t_crit:
        print("Reject the null hypothesis based on t-critical value.")
    else:
        print("Fail to reject the null hypothesis based on t-critical value.")

    # Also show p-value for reference
    t_stat, p_value_2tail = stats.ttest_1samp(a=alcohol_content,

```

```

popmean=pop_mean)

# find one-tailed p-value
if t_statistic > 0:
    p_value_1tail = p_value_2tail / 2
else:
    p_value_1tail = 1 - (p_value_2tail / 2)

print(f"\nOne-Tailed P-value: {p_value_1tail:.4f}")

if p_value_1tail < alpha:
    print("Reject the null hypothesis based on p-value.")
else:
    print("Fail to reject the null hypothesis based on p-value.")

# find 95% confidence interval
margin_error = (stats.t.ppf(1 - 0.05 / 2, df)) * (sample_std / np.sqrt(n))
low_interval = sample_mean - margin_error
high_interval = sample_mean + margin_error

print()
print(f"95% Confidence Interval:\n({low_interval:.4f},
{high_interval:.4f})")

# -----
# ANOVA (Wine Quality Dataset)
# -----
def anova_analysis():
    # combine X and Y dataframes
    combined_data = X.join(y)

    # Run ANOVA test
    anova_model = smf.ols("alcohol ~ C(quality)", data=combined_data).fit()
    anova_table = sm.stats.anova_lm(anova_model, typ=2)

    # print table
    print(anova_table)

    # create figure and axes
    figure, axes = plt.subplots(figsize=(14, 6))
    axes.axis("off") # hide plot axes

```

```

# create summary table
anova_table_output = plt.table(
    cellText=anova_table.round(4).values, # round 4 decimal places
    rowLabels=["Quality", "Residual Error"], # label rows
    colLabels=[
        "Sum of Squares",
        "Degrees of Freedom",
        "F-Statistic",
        "P-Value",
    ], # label columns
    loc="center", # center table
    cellLoc="center", # center text
)

# size table
anova_table_output.scale(1, 2)

# add title
plt.title("ANOVA Table: Alcohol Content by Wine Quality")
plt.show()

# find rejection region
alpha = 0.05
df1 = 6
df2 = 6490

f_critical_value = stats.f.ppf(1 - alpha, df1, df2)
print(f"F-Critical Value: {f_critical_value}")

print(f"\nReject H0 if F > {f_critical_value:.4f}")

# residual check with QQ-plot
sm.qqplot(anova_model.resid, line="45")
plt.title("QQ-Plot of ANOVA Residuals")
plt.show()

# equal variance check with boxplots
sns.boxplot(x="quality", y="alcohol", data=combined_data)
plt.title("Alcohol Content Through Alcohol Quality Levels")
plt.show()

```

```
# -----
```

```

# Main Execution (Both Datasets)
# -----
if __name__ == "__main__":

    # Sampling Distributions
    plot_histogram_q1()
    plot_histogram_q2()

    # Bootstrap
    runs = bootstrap()
    plot_bootstrap(runs)
    bootstrap_qq(runs)

    # Summary Statistics
    # Wine Quality
    quantitative_summary(X, "Wine Quality - Quantitative Summary")
    category_summary(y, "Wine Quality - Quality Score", wine_flag=True)

    # Obesity Dataset
    quantitative_summary(X2, "Obesity Dataset - Quantitative Summary")
    category_summary(X2, "Obesity Dataset - Categorical Variable")
    category_summary(y2, "Obesity Dataset - Target Variable")

    # Hypothesis Tests
    alcohol_t_test()

    # ANOVA and Interaction Model
    model = mult_comparisons()
    plot_resid_fitted(model)
    hypothesis_test(model)
    multiple_comparisons(model)
    pass

```