

Projet : Régressions pénalisées

Import des librairies utiles

```
library(mvtnorm)
library(palmerpenguins)
library(glmnet)

## Loading required package: Matrix
## Loaded glmnet 4.1-8

library(xtable)
library(stargazer)

##
## Please cite as:
## Hlavac, Marek (2022). stargazer: Well-Formatted Regression and Summary Statistics Tables.
## R package version 5.2.3. https://CRAN.R-project.org/package=stargazer

library(ggplot2)
library(gridExtra)
library(ordinal)
library(knitr)
library(dplyr)

##
## Attaching package: 'dplyr'

## The following object is masked from 'package:ordinal':
##
## slice

## The following object is masked from 'package:gridExtra':
##
## combine

## The following objects are masked from 'package:stats':
##
## filter, lag

## The following objects are masked from 'package:base':
##
## intersect, setdiff, setequal, union

library(kableExtra)

##
## Attaching package: 'kableExtra'

## The following object is masked from 'package:dplyr':
##
```

```
##      group_rows
library(corrplot)

## corrplot 0.92 loaded
library(pls)

##
## Attaching package: 'pls'
## The following object is masked from 'package:corrplot':
##
##      corrplot
## The following object is masked from 'package:stats':
##
##      loadings
library(pROC)

## Type 'citation("pROC")' for a citation.
##
## Attaching package: 'pROC'
## The following objects are masked from 'package:stats':
##
##      cov, smooth, var
```

Lecture des données

```
data=read.table("transportmod3.txt",h=T)
head(data)
```

##		CO2	Incid	CA	CA3	Port.Port.1	Port.Port.2	Port.Port.3	Port.Port.4	Port.Port.5
## 1	6.26	11	0	0	24.61	0.65	9.51	0.25	9.03	
## 2	7.51	8	0	1	24.43	1.84	12.94	0.56	8.04	
## 3	4.97	8	0	0	25.40	1.57	12.32	4.38	8.88	
## 4	6.27	9	0	1	27.41	2.54	12.20	1.23	9.57	
## 5	7.20	34	1	2	23.85	2.45	11.46	7.94	13.02	
## 6	6.81	22	0	1	24.61	2.11	12.16	6.85	12.32	
##	Port.Port.6	Port.Port.7	Port.Port.8	Port.Port.9	Port.Port.10	Port.Port.11				
## 1	0.71	15.22	18.33	19.99	21.24	7.47				
## 2	1.31	12.62	19.36	17.67	19.93	2.94				
## 3	5.90	14.58	17.83	17.52	18.59	5.71				
## 4	2.49	15.45	18.50	19.31	21.66	9.41				
## 5	4.96	15.04	17.77	12.99	20.52	2.81				
## 6	4.50	16.29	17.39	17.21	23.69	9.59				
##	Port.Port.12	Port.Port.13	Port.Port.14	Port.Port.15	Port.Port.16	Port.Port.17				
## 1	5.00	1.73	17.80	29.01	6.67	15.17				
## 2	5.24	3.55	16.19	30.09	8.86	14.78				
## 3	7.42	1.69	16.79	30.23	9.18	15.16				
## 4	6.59	2.05	19.74	29.41	8.52	14.20				
## 5	7.48	2.16	12.47	30.44	3.43	18.64				
## 6	9.78	3.15	17.65	30.89	8.01	17.16				
##	Port.Port.18	Port.Port.19	Port.Port.20	Port.Port.21	Port.Port.22	Port.Port.23				

## 1	0.61	28.62	4.27	20.73	12.86	4.56
## 2	3.70	26.90	7.34	25.08	8.39	1.61
## 3	0.28	28.31	10.12	17.94	12.73	0.67
## 4	2.75	29.99	5.48	23.85	9.06	5.65
## 5	0.25	24.90	9.59	20.20	13.80	1.49
## 6	3.52	27.16	9.44	21.28	9.26	5.50
##	Port.Port.24	Port.Port.25	Port.Port.26	Port.Port.27	Port.Port.28	Port.Port.29
## 1	1.09	10.99	22.48	4.34	21.84	0.85
## 2	9.96	9.07	23.33	5.95	22.71	5.79
## 3	2.94	8.51	23.62	4.30	24.88	4.11
## 4	4.19	11.43	22.56	6.03	19.47	2.98
## 5	2.08	5.56	23.32	6.55	25.57	7.83
## 6	3.92	10.38	23.53	7.13	23.42	5.00
##	Port.Port.30	Port.Port.31	Port.Port.32	Port.Port.33	Port.Port.34	Port.Port.35
## 1	13.83	2.09	10.58	22.06	15.57	11.34
## 2	7.18	2.67	8.43	17.61	12.13	9.34
## 3	14.20	0.06	12.98	29.33	16.37	13.41
## 4	10.73	1.67	5.53	17.74	14.02	13.18
## 5	11.58	2.59	11.65	24.67	18.42	16.19
## 6	17.87	4.00	12.50	25.82	16.04	17.55
##	Port.Port.36	Port.Port.37	Port.Port.38	Port.Port.39	Port.Port.40	Port.Port.41
## 1	6.81	10.44	6.36	4.86	8.65	4.16
## 2	0.07	11.57	9.58	4.78	2.49	4.92
## 3	3.28	12.30	8.64	7.86	4.89	2.73
## 4	4.64	15.74	9.96	5.25	6.00	2.94
## 5	4.11	12.31	5.52	8.78	6.50	5.05
## 6	4.22	17.43	10.77	6.83	6.15	6.62
##	Port.Port.42	Port.Port.43	Port.Port.44	Port.Port.45	Port.Port.46	Port.Port.47
## 1	8.23	4.18	0.86	10.33	1.69	10.05
## 2	11.30	6.46	2.71	13.28	5.60	9.83
## 3	9.71	6.00	2.59	4.05	1.02	11.28
## 4	10.52	9.50	1.72	9.60	8.42	14.22
## 5	8.73	2.90	3.59	10.54	1.61	9.63
## 6	7.26	2.88	4.95	16.28	0.24	5.82
##	Port.Port.48	Port.Port.49	Port.Port.50	Port.Port.51	Port.Port.52	Port.Port.53
## 1	0.25	2.02	7.09	15.17	6.83	6.16
## 2	4.73	4.78	7.43	10.85	5.95	6.82
## 3	4.51	5.42	3.25	10.10	2.38	8.97
## 4	1.91	5.10	11.50	9.38	1.71	8.04
## 5	6.86	3.67	4.06	15.79	5.93	6.70
## 6	0.10	0.18	10.82	10.63	6.84	5.33
##	Port.Port.54	Port.Port.55	Port.Port.56	Port.Port.57	Port.Port.58	Port.Port.59
## 1	18.91	10.60	14.74	18.42	16.27	13.34
## 2	19.10	10.29	12.02	16.95	16.63	14.57
## 3	15.14	8.57	15.61	14.38	7.92	13.26
## 4	15.97	10.47	12.99	15.60	12.39	12.41
## 5	18.09	11.76	14.07	23.97	18.75	14.56
## 6	18.05	12.00	8.52	18.96	17.94	10.34
##	Port.Port.60					
## 1	17.17					
## 2	19.50					
## 3	22.00					
## 4	24.49					
## 5	20.99					

```
## 6          22.67
```

Statistiques descriptives

Valeurs descriptives

```
# Sélection des colonnes à décrire
colonnes_a_analyser <- c("CO2", "Incid", "CA")
donnees_selectionnees <- data[colonnes_a_analyser]

# Affichage des statistiques descriptives
res_summary <- summary(donnees_selectionnees)
table_latex <- xtable(res_summary)

# Génération du code LaTeX
print(table_latex)

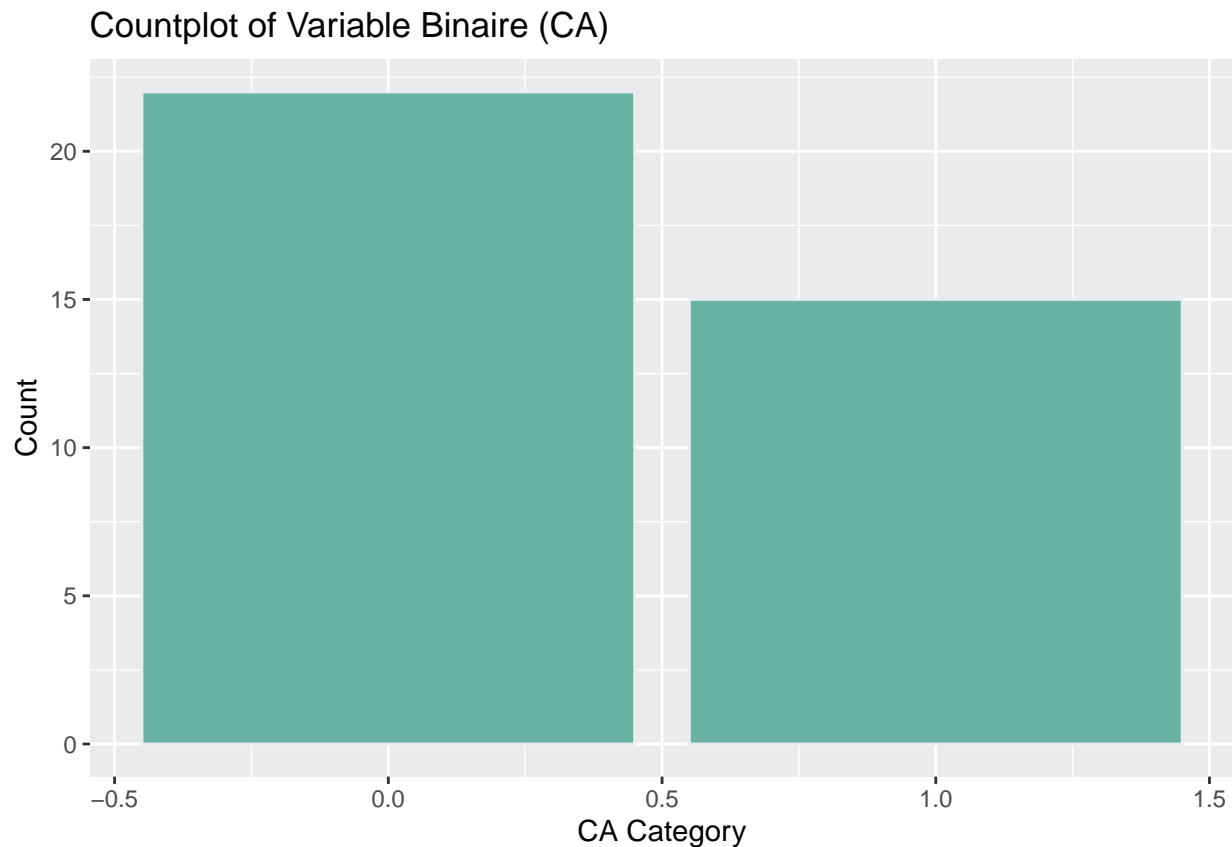
## % latex table generated in R 4.3.2 by xtable 1.8-4 package
## % Thu Dec 14 18:43:40 2023
## \begin{table}[ht]
## \centering
## \begin{tabular}{rlll}
## \hline
## & CO2 & Incid & CA \\
## \hline
## X & Min. : 4.970 & Min. : 3.0 & Min. : 0.0000 \\
## X.1 & 1st Qu.: 6.710 & 1st Qu.: 13.0 & 1st Qu.: 0.0000 \\
## X.2 & Median : 7.410 & Median : 27.0 & Median : 0.0000 \\
## X.3 & Mean : 7.465 & Mean : 34.7 & Mean : 0.4054 \\
## X.4 & 3rd Qu.: 8.290 & 3rd Qu.: 42.0 & 3rd Qu.: 1.0000 \\
## X.5 & Max. : 10.550 & Max. : 152.0 & Max. : 1.0000 \\
## \hline
## \end{tabular}
## \end{table}
```

Graphe des corrélations

```
# Définition un seuil pour les fortes corrélations
threshold <- 0.7
correlation_matrix <- cor(data)

# Récupérer les noms de lignes et de colonnes de corrélations fortes
strong_correlations <- as.data.frame(which(abs(correlation_matrix) > threshold, arr.ind = TRUE))

# Créer un graphique en violon
ggplot(data, aes(x = CA)) +
  geom_bar(fill = "#69b3a2", color = "#e9ecef") +
  labs(title = "Countplot of Variable Binaire (CA)",
       x = "CA Category",
       y = "Count")
```



Conditionnement de XX

```
X=as.matrix(data[,5:64])

# Calculer la matrice X'X
XTX <- t(X) %*% X

# Calculer les valeurs propres de X'X
eigen_XTX <- eigen(XTX)
cat("Valeurs propres de X'X:", eigen_XTX$values, "\n")

## Valeurs propres de X'X: 382245.6 1422.419 1215.233 1045.545 892.915 830.2399 743.8491 643.2138 570.9

# Calculer l'indice de conditionnement
condition_index <- max(eigen_XTX$values) / min(eigen_XTX$values)

# Afficher l'indice de conditionnement
cat("Indice de conditionnement:", condition_index, "\n")

## Indice de conditionnement: -2.591569e+16
```

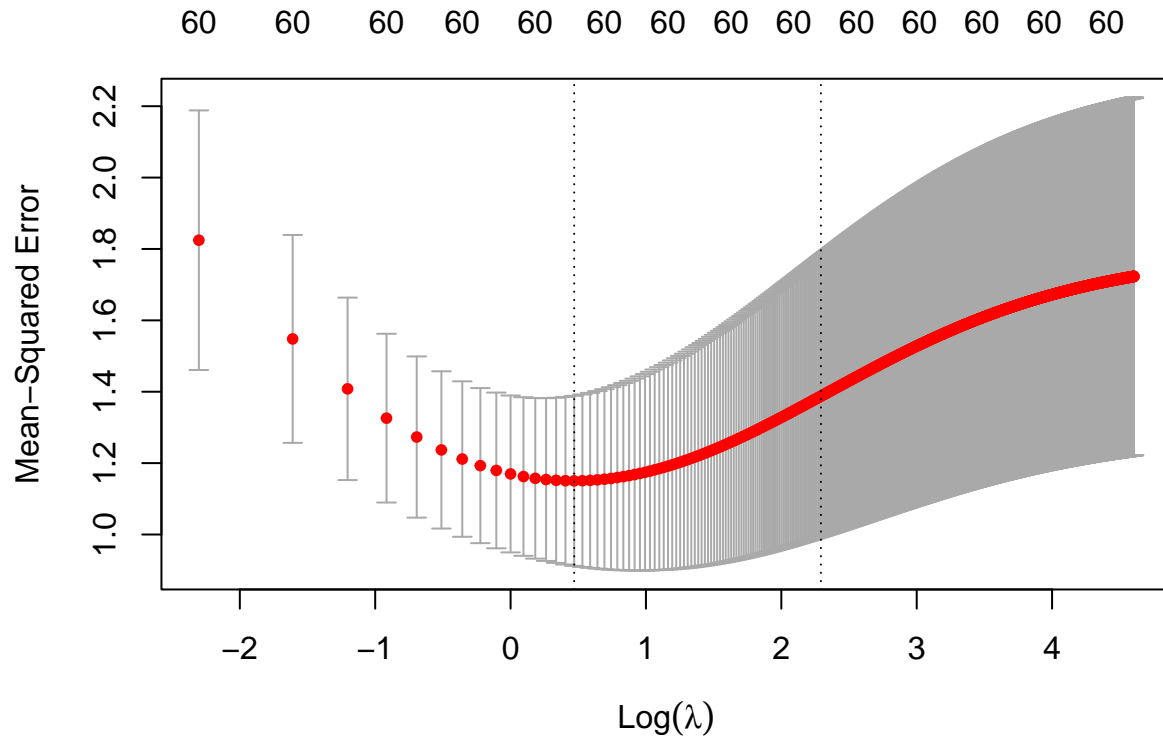
Modélisation du CO2

Standardisation de la donnée

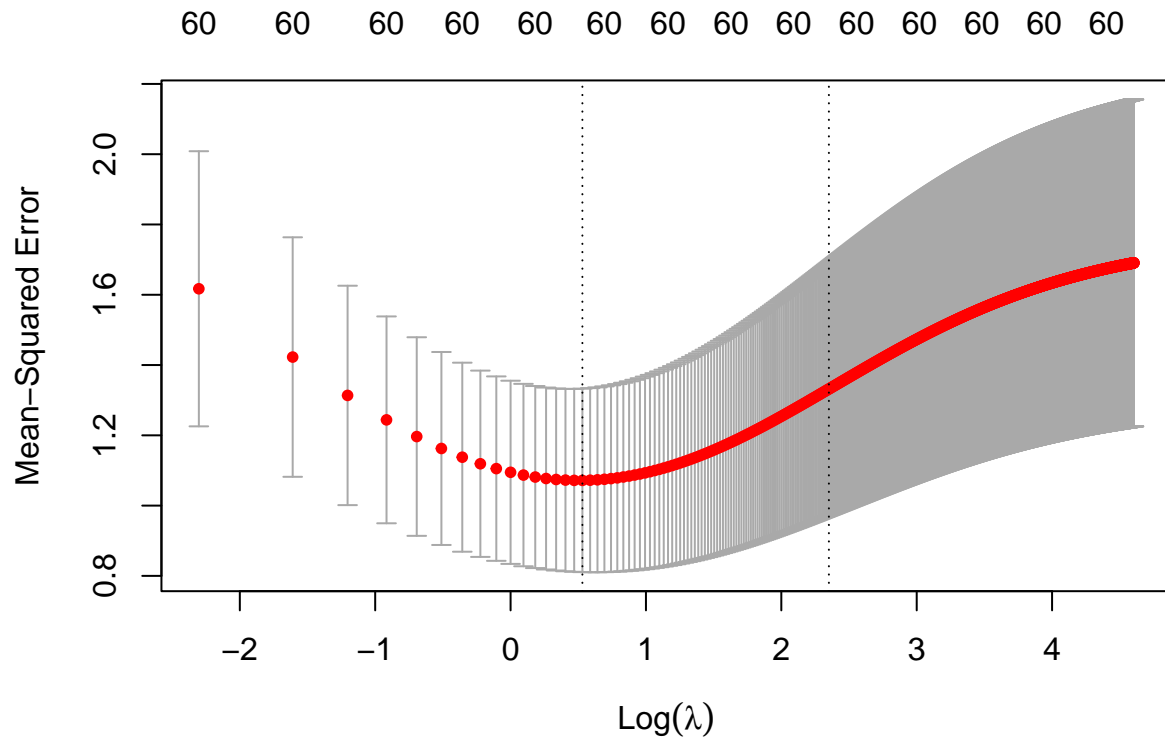
```
#Centrer et réduire les variables explicatives
Y=data$C02
X=as.matrix(data[,5:64])
XS=scale(X)
```

Modèle RIDGE

```
# On a un modèle linéaire. On va prendre family = 'gaussian'
rescv=cv.glmnet(XS,Y,family='gaussian',alpha=0, lambda=seq(0.1, 100, 0.1))
plot(rescv)
```



```
# Stabilisation du lambda avec une boucle
rescv=cv.glmnet(XS,Y,family='gaussian',alpha=0, lambda=seq(0.1, 100, 0.1))
plot(rescv)
```



```
lambda=rescv$lambda.min
lambda
```

```
## [1] 1.7
```

```
# Autre méthode
```

```
lambda=0
```

```
for (j in 1:10)
```

```
{
```

```
  rescv=cv.glmnet(XS,Y,family='gaussian',alpha=0, lambda=seq(0.1, 100, 0.1))
```

```
  print(rescv$lambda.min)
```

```
  lambda=lambda+rescv$lambda.min
```

```
}
```

```
## [1] 2.3
```

```
## [1] 1.9
```

```
## [1] 2.2
```

```
## [1] 1.9
```

```
## [1] 1.8
```

```
## [1] 2
```

```
## [1] 2
```

```
## [1] 2.2
```

```
## [1] 1.9
```

```
## [1] 2.3
```

Redéfinition du seuil

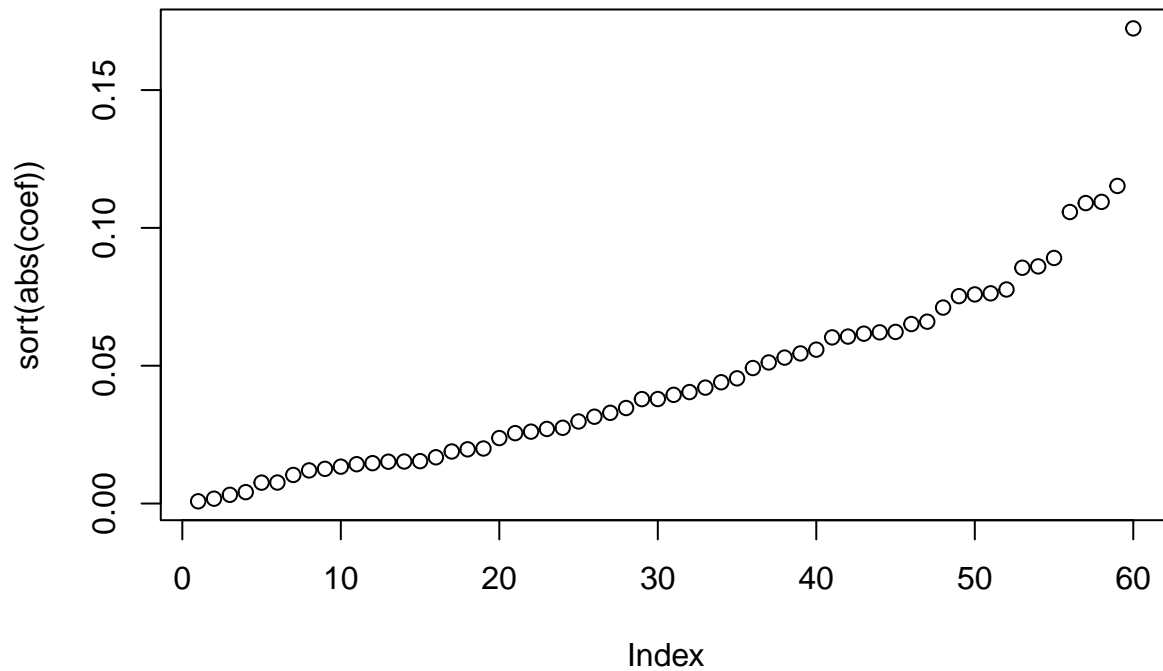
```
seuil=lambda/10
```

```
resridge=glmnet(XS,Y,family='gaussian',alpha=0, lambda=seuil)
```

```
#On retire le coefficient 1
```

```
coef=coefficients(resridge)[-1]
```

```
#On affiche
plot(sort(abs(coef)))
```



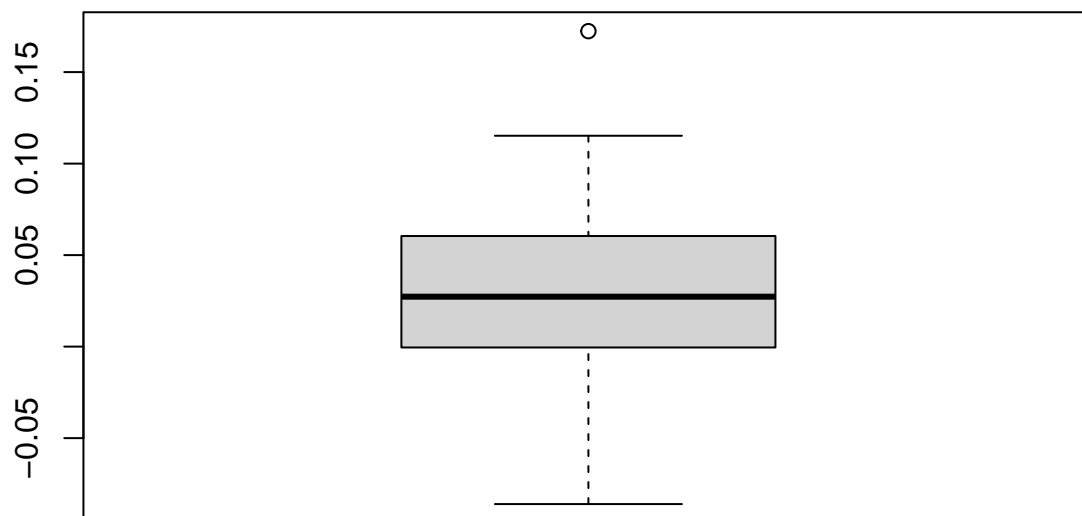
prend les 8 premiers qui se détachent du groupe.

Choix des ports

```
#En fonction du plot
which(abs(coef)>0.6)
```

```
## integer(0)
```

```
# A l'aide d'un boxplot
resbox=boxplot(coef)
```



```
which(coef>resbox$stats[5,])
```

```
## [1] 5
```



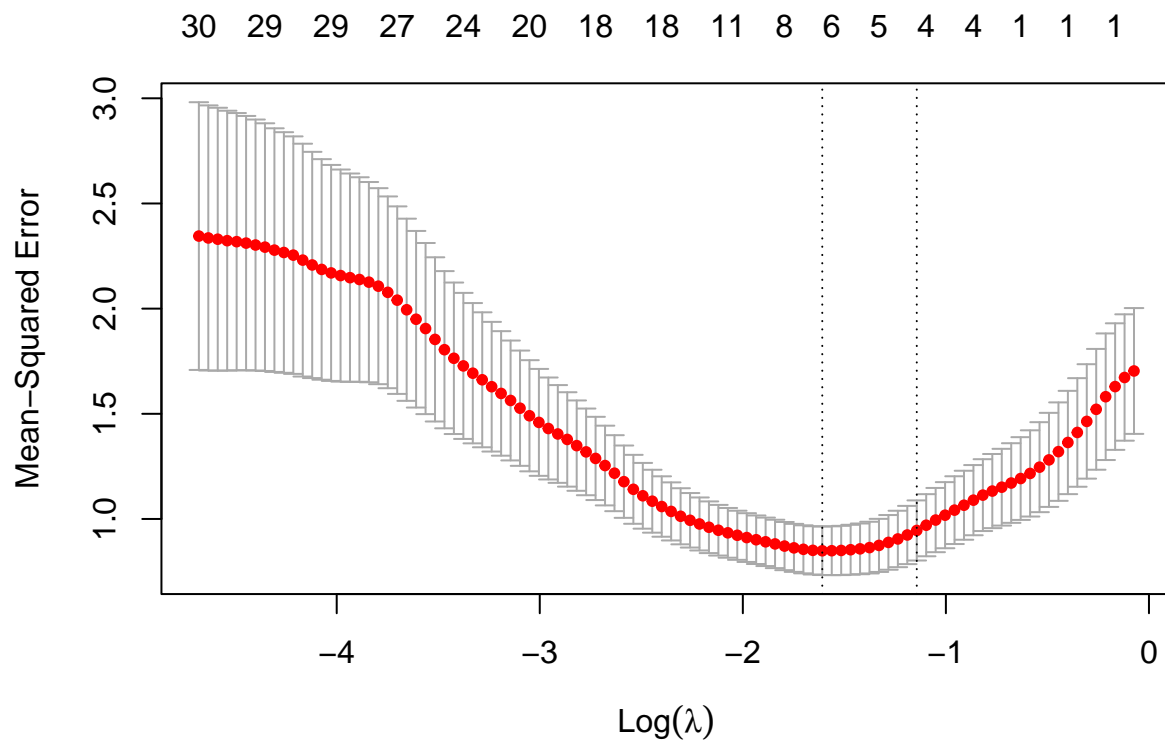
```
selecridge=order(coef,decreasing=TRUE)[1:5]
colnames(X[,selecridge])
```

```
## [1] "Port.Port.5" "Port.Port.3" "Port.Port.58" "Port.Port.34" "Port.Port.8"
```

Les ports retenus sont: 5 3 58 34 8.

Modèle LASSO

```
#Modèle LASSO
rescv=cv.glmnet(XS,Y,family='gaussian',alpha=1)
plot(rescv)
```



```
# Prenons le lambda_1se qui sélectionne un peu moins de variables
seuil=rescv$lambda.1se
reslasso=glmnet(XS,Y,family='gaussian',alpha=1,lambda=seuil)

#Boucle sur le lambda
lambda=0
for (j in 1:10)
{
  reslasso=cv.glmnet(XS,Y,family='gaussian',alpha=1, lambda=seq(0.1, 100, by = 0.1))
  print(reslasso$lambda.1se)
  lambda=lambda+reslasso$lambda.1se
}
```

```
## [1] 0.3
## [1] 0.3
## [1] 0.3
## [1] 0.3
## [1] 0.4
```

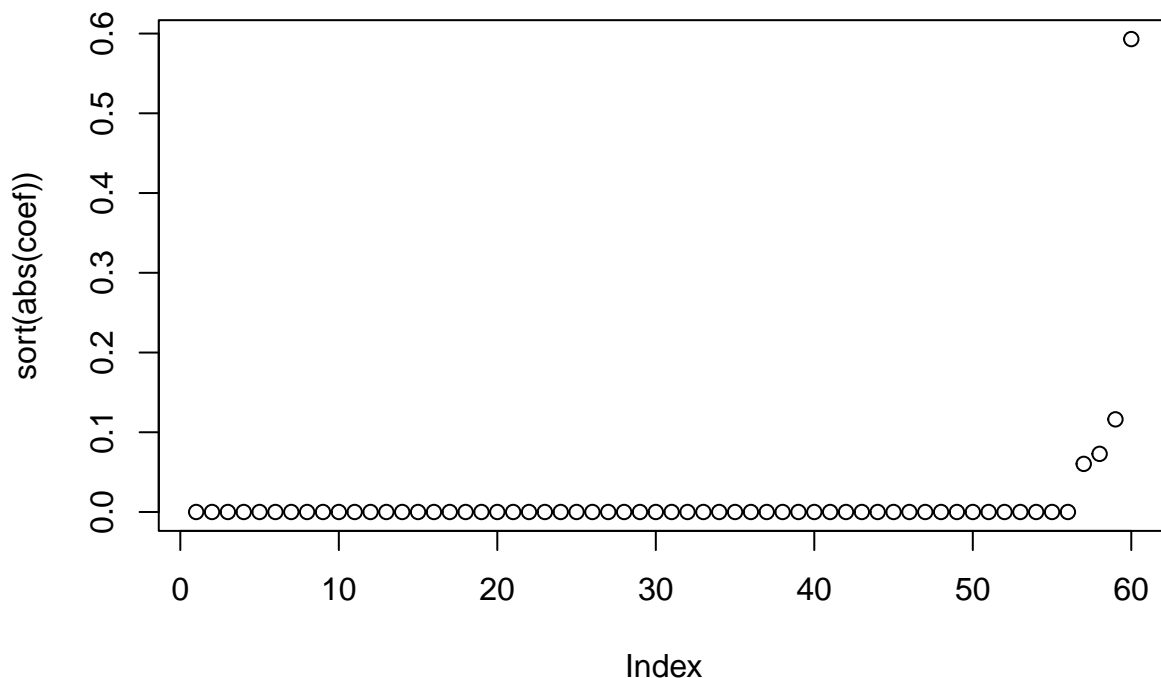
```
## [1] 0.3
## [1] 0.4
## [1] 0.3
## [1] 0.3
## [1] 0.3
```

#Définition du seuil

```
#Par calcul de la moyenne
seuil=lambda/10
seuil
```

```
## [1] 0.32
```

```
# On va alors redéfinir un meilleur seuil et relancer notre régression
reslasso=glmnet(XS,Y,family='gaussian',alpha=1, lambda=seuil)
coef=coefficients(reslasso)[-1]
plot(sort(abs(coef)))
```



sélectionne 4 variables

```
selected_va <- which(coef!=0)
selected_va
```

```
## [1] 3 5 7 58
```

On obtient les ports: 3 5 7 58.

Modèle Elasticnet

Modèle

```
"On procède de la même manière en stabilisant notre modèle sur un intervalle de test de valeur"
```

```
## [1] "On procède de la même manière en stabilisant notre modèle sur un intervalle de test de valeur"
```

```

lambda=0
for (j in 1:10)
{
  resenet=cv.glmnet(XS,Y,family='gaussian',alpha=0.5,lambda=seq(0.1, 100, 0.1))
  print(resenet$lambda.1se)
  lambda=lambda+resenet$lambda.1se
}

```

```

## [1] 0.5
## [1] 0.6
## [1] 0.7
## [1] 0.6
## [1] 0.6
## [1] 0.6
## [1] 0.5
## [1] 0.7
## [1] 0.7
## [1] 0.8

```

```

lambda.1se=lambda/10
lambda.1se

```

```

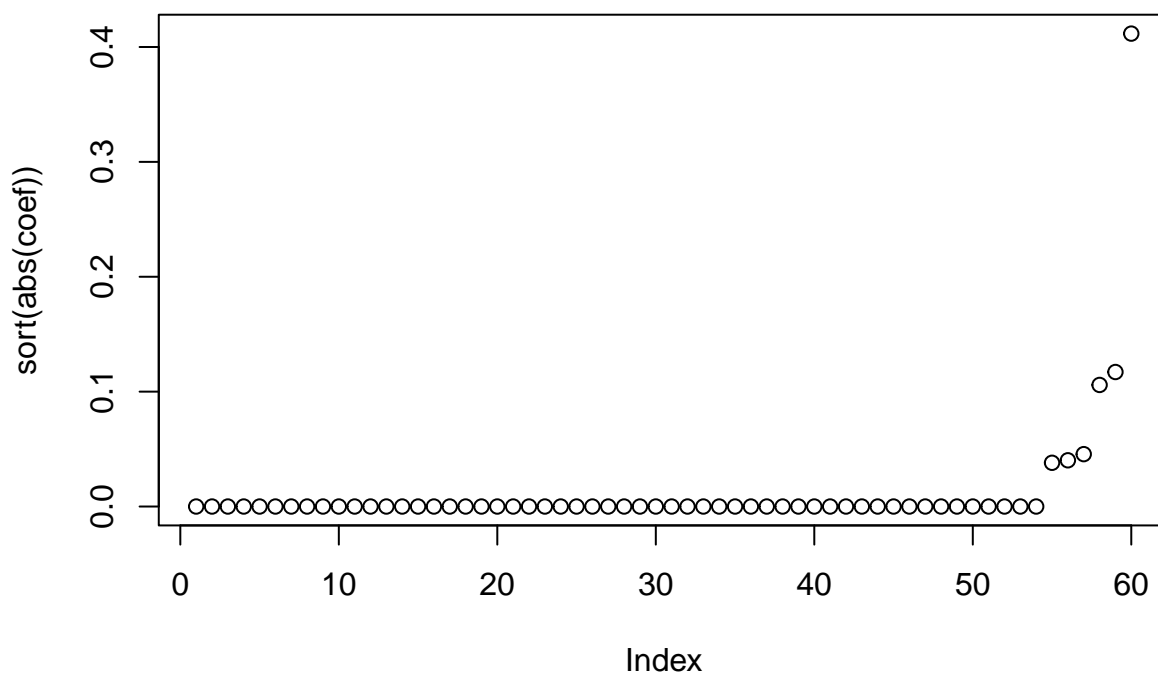
## [1] 0.63

```

```

resenet=glmnet(XS,Y,family='gaussian',alpha=0.5,lambda=lambda.1se)
coef=coefficients(resenet)[-1]
plot(sort(abs(coef)))

```



```

which(coef != 0)

```

```

## [1] 3 5 7 8 34 58

```

```

coef

```

```

## [1] 0.00000000 0.00000000 0.10582428 0.00000000 0.41164710 0.00000000

```

```
## [7] -0.04021975  0.03806654  0.00000000  0.00000000  0.00000000  0.00000000
## [13]  0.00000000  0.00000000  0.00000000  0.00000000  0.00000000  0.00000000
## [19]  0.00000000  0.00000000  0.00000000  0.00000000  0.00000000  0.00000000
## [25]  0.00000000  0.00000000  0.00000000  0.00000000  0.00000000  0.00000000
## [31]  0.00000000  0.00000000  0.00000000  0.04558936  0.00000000  0.00000000
## [37]  0.00000000  0.00000000  0.00000000  0.00000000  0.00000000  0.00000000
## [43]  0.00000000  0.00000000  0.00000000  0.00000000  0.00000000  0.00000000
## [49]  0.00000000  0.00000000  0.00000000  0.00000000  0.00000000  0.00000000
## [55]  0.00000000  0.00000000  0.00000000  0.11707652  0.00000000  0.00000000
```

Les ports: 3 5 7 8 34 58.

Modèle Linéaire

```
linear_model <- lm(Y ~ X[, selected_va])
stargazer(linear_model, title = "Linear Regression Results", out = "table.tex")

##
## % Table created by stargazer v.5.2.3 by Marek Hlavac, Social Policy Institute. E-mail: marek.hlavac@vse.cz
## % Date and time: Thu, Dec 14, 2023 - 18:43:49
## \begin{table}[!htbp] \centering
##   \caption{Linear Regression Results}
##   \label{}
##   \begin{tabular}{@{\extracolsep{5pt}}lc}
##     \hline
##     \hline
##     & \multicolumn{1}{c}{\textit{Dependent variable:}} & \\
##     \cline{2-2}
##     \hline
##     & Y & \\
##     \hline
##     X[, selected\_va]Port.Port.3 & 0.094 & \\
##     & (0.078) & \\
##     & & \\
##     X[, selected\_va]Port.Port.5 & 0.430$^{***}$ & \\
##     & (0.074) & \\
##     & & \\
##     X[, selected\_va]Port.Port.7 & $-0.313$^{***}$ & \\
##     & (0.093) & \\
##     & & \\
##     X[, selected\_va]Port.Port.58 & 0.060 & \\
##     & (0.040) & \\
##     & & \\
##     Constant & 5.065$^{***}$ & \\
##     & (1.792) & \\
##     & & \\
##     \hline
##     Observations & 37 & \\
##     R$^2$ & 0.729 & \\
##     Adjusted R$^2$ & 0.695 & \\
##     Residual Std. Error & 0.723 (df = 32) & \\
##     F Statistic & 21.555$^{***}$ (df = 4; 32) & \\
##     \hline
##     \hline
##     \textit{Note:} & \multicolumn{1}{r}{\textit{$^{*}$p} < 0.1; \textit{$^{**}$p} < 0.05; \textit{$^{***}$p} < 0.01} & \end{table}
```

```
## \end{tabular}
## \end{table}

print(selected_va)

## [1] 3 5 7 58

# Afficher le modèle linéaire
summary(linear_model)

##
## Call:
## lm(formula = Y ~ X[, selected_va])
##
## Residuals:
##      Min       1Q   Median       3Q      Max
## -1.09525 -0.63607  0.09453  0.57374  1.44511
##
## Coefficients:
##              Estimate Std. Error t value Pr(>|t|)
## (Intercept)      5.06467     1.79191   2.826  0.00805 **
## X[, selected_va]Port.Port.3  0.09383     0.07793   1.204  0.23742
## X[, selected_va]Port.Port.5  0.42989     0.07447   5.773  2.1e-06 ***
## X[, selected_va]Port.Port.7 -0.31274     0.09281  -3.370  0.00198 **
## X[, selected_va]Port.Port.58  0.06026     0.04019   1.499  0.14355
## ---
## Signif. codes:  0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
##
## Residual standard error: 0.7227 on 32 degrees of freedom
## Multiple R-squared:  0.7293, Adjusted R-squared:  0.6955
## F-statistic: 21.55 on 4 and 32 DF,  p-value: 1.052e-08
```

Modèle PCA

```
# Effectuez le PCR
pcr_model <- pcr(Y ~ XS, scale = TRUE)

# Résumé du modèle PCR
summary(pcr_model)

## Data:      X dimension: 37 60
## Y dimension: 37 1
## Fit method: svdpc
## Number of components considered: 36
## TRAINING: % variance explained
##      1 comps  2 comps  3 comps  4 comps  5 comps  6 comps  7 comps  8 comps
## X    11.91    21.74    30.67    38.54    45.42    51.98    57.54    62.55
## Y    10.07    15.90    24.69    40.01    50.56    53.59    54.61    63.65
##      9 comps 10 comps 11 comps 12 comps 13 comps 14 comps 15 comps
## X    67.17    71.21    75.09    78.12    80.87    83.17    85.12
## Y    64.96    66.15    67.54    67.90    69.36    75.77    76.02
##      16 comps 17 comps 18 comps 19 comps 20 comps 21 comps 22 comps
## X    87.02    88.73    90.30    91.63    92.82    93.88    94.88
## Y    78.59    78.80    78.87    78.99    80.46    80.49    80.50
##      23 comps 24 comps 25 comps 26 comps 27 comps 28 comps 29 comps
```

```
## X      95.77      96.45      97.10      97.64      98.16      98.55      98.89
## Y      80.51      82.61      82.77      82.82      89.36      89.38      89.65
##      30 comps 31 comps 32 comps 33 comps 34 comps 35 comps 36 comps
## X      99.20      99.43      99.58      99.71      99.83      99.92      100
## Y      91.38      92.27      96.67      97.66      98.64      98.72      100

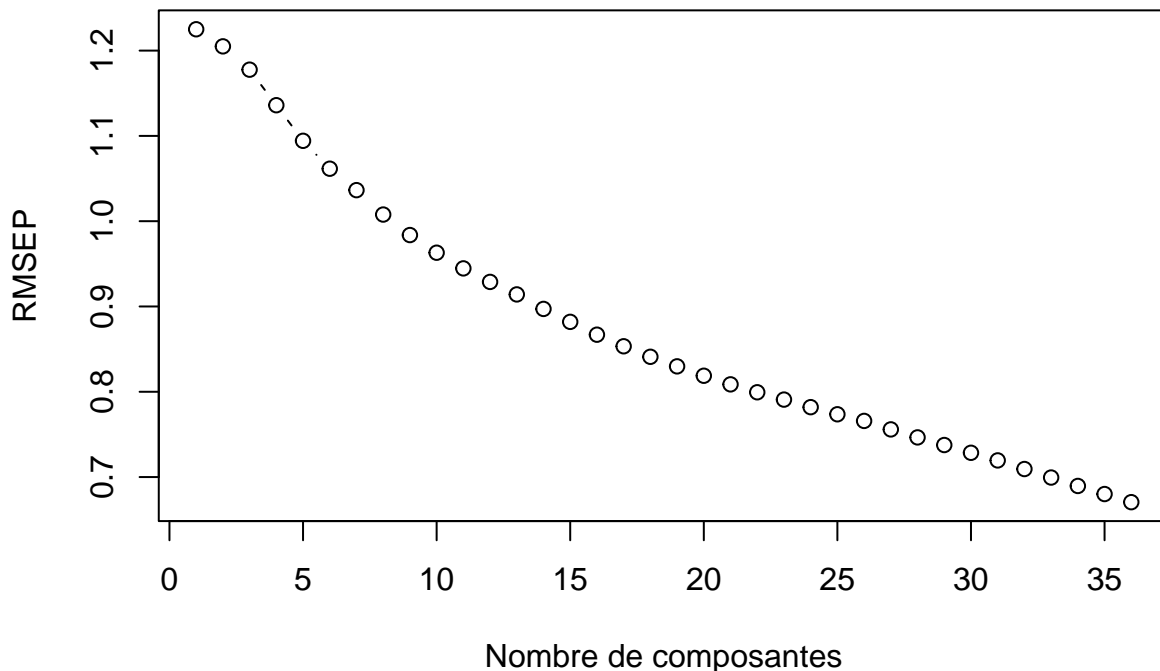
# Initialisation du vecteur pour stocker les RMSEP
rmsep_values <- numeric(36)

# Boucle sur le nombre de composantes
for (i in 1:36) {
  pcr_model <- pcr(Y ~ XS, ncomp = i, scale = TRUE)

  # Prédiction sur l'ensemble de données
  predicted_values <- predict(pcr_model, as.data.frame(X))

  # Calcul du RMSEP
  rmsep_values[i] <- sqrt(mean((Y - predicted_values)^2))
}

# Tracer le graphique du RMSEP
plot(1:36, rmsep_values, type = "b", xlab = "Nombre de composantes", ylab = "RMSEP")
```



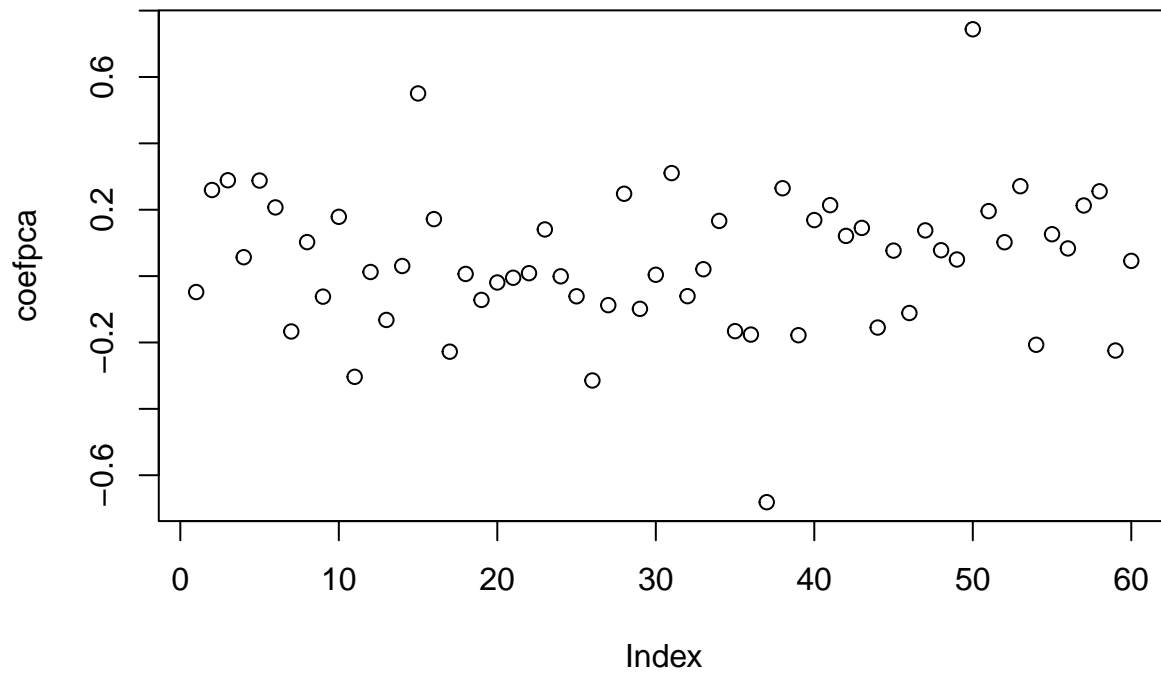
```
# Trouver le nombre optimal de composantes
optimal_components <- which.min(rmsep_values)

# Seuillage pour les coefficients
threshold <- 0.3 # Choisissez votre seuil
significant_coef <- abs(coef(pcr_model)) > threshold

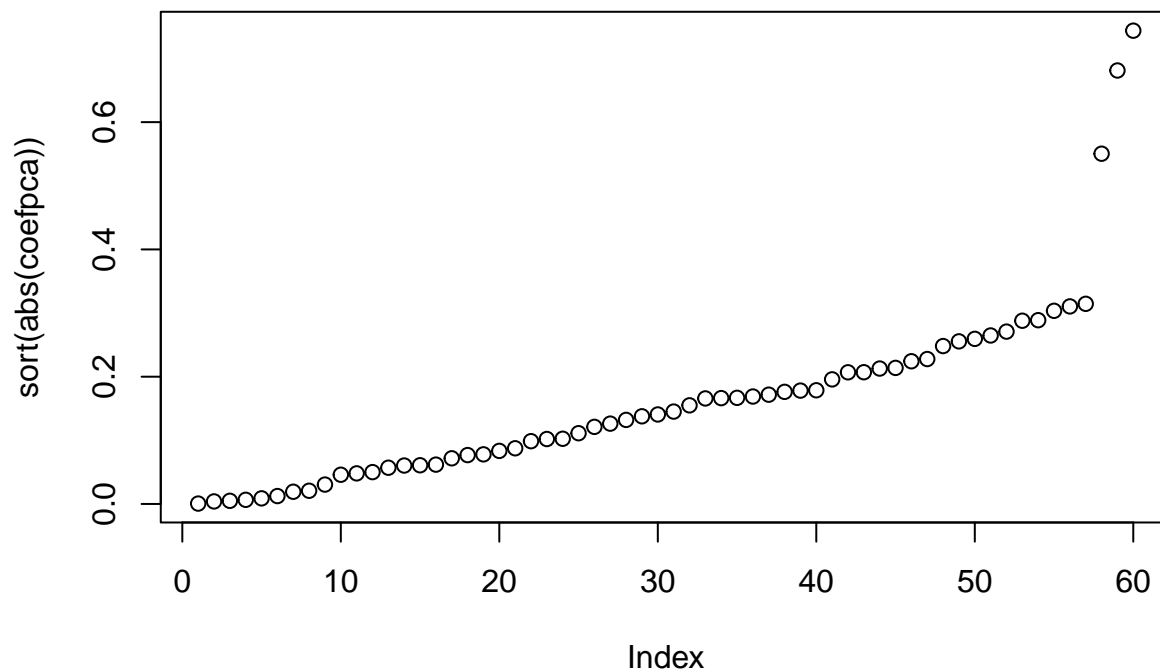
respca2=plsr(Y ~XS, ncomp=16)
summary(respca2)
```

```
## Data:      X dimension: 37 60
## Y dimension: 37 1
## Fit method: kernelppls
## Number of components considered: 16
## TRAINING: % variance explained
##      1 comps  2 comps  3 comps  4 comps  5 comps  6 comps  7 comps  8 comps
## X      9.075   17.28   23.17   28.79   34.25   38.51   44.43   49.21
## Y     69.775   80.21   86.23   89.98   92.86   95.56   96.56   97.35
##      9 comps 10 comps 11 comps 12 comps 13 comps 14 comps 15 comps
## X     54.01   57.50   60.37   64.54   67.84   71.85   74.51
## Y     98.11   98.85   99.39   99.62   99.76   99.82   99.89
##      16 comps
## X      77.17
## Y     99.93
```

```
coefpca=coef(respca2)
par(mfrow=c(1,1))
plot(coefpca) # on pourrait faire du seuillage ici
```



```
plot(sort(abs(coefpca)))
```



```
selecpc=order(abs(coefpca),decreasing=TRUE)[1:9]

colnames(X[,selecpc])

## [1] "Port.Port.50" "Port.Port.37" "Port.Port.15" "Port.Port.26" "Port.Port.31"
## [6] "Port.Port.11" "Port.Port.3" "Port.Port.5" "Port.Port.53"

##Modèle PLS
# Réaliser la régression PLS
pls_model <- plsr(Y ~ XS, ncomp = 16) # Vous pouvez ajuster ncomp selon votre analyse

# Afficher un résumé du modèle PLS
summary(pls_model)

## Data:      X dimension: 37 60
## Y dimension: 37 1
## Fit method: kernelpls
## Number of components considered: 16
## TRAINING: % variance explained
##      1 comps  2 comps  3 comps  4 comps  5 comps  6 comps  7 comps  8 comps
## X      9.075    17.28    23.17    28.79    34.25    38.51    44.43    49.21
## Y     69.775    80.21    86.23    89.98    92.86    95.56    96.56    97.35
##      9 comps 10 comps 11 comps 12 comps 13 comps 14 comps 15 comps
## X     54.01    57.50    60.37    64.54    67.84    71.85    74.51
## Y     98.11    98.85    99.39    99.62    99.76    99.82    99.89
##      16 comps
## X      77.17
## Y     99.93
# Visualiser les coefficients PLS
coef_pls <- coef(pls_model, ncomp = 16) # Vous pouvez ajuster ncomp ici aussi
print(coef_pls)

## , , 16 comps
```



```

##
##                                     Y
## Port.Port.1 -0.0480640114
## Port.Port.2  0.2594567631
## Port.Port.3  0.2887707800
## Port.Port.4  0.0569410378
## Port.Port.5  0.2879171414
## Port.Port.6  0.2070196206
## Port.Port.7 -0.1667723657
## Port.Port.8  0.1024610846
## Port.Port.9 -0.0618313286
## Port.Port.10 0.1786375903
## Port.Port.11 -0.3035112929
## Port.Port.12 0.0124025913
## Port.Port.13 -0.1320879834
## Port.Port.14 0.0304897491
## Port.Port.15 0.5504000094
## Port.Port.16 0.1717246771
## Port.Port.17 -0.2277282950
## Port.Port.18 0.0065216484
## Port.Port.19 -0.0717609931
## Port.Port.20 -0.0192261395
## Port.Port.21 -0.0049550482
## Port.Port.22 0.0088235516
## Port.Port.23 0.1406508179
## Port.Port.24 -0.0006142111
## Port.Port.25 -0.0608353876
## Port.Port.26 -0.3144918732
## Port.Port.27 -0.0874973000
## Port.Port.28 0.2481399271
## Port.Port.29 -0.0986739100
## Port.Port.30 0.0040104813
## Port.Port.31 0.3104189204
## Port.Port.32 -0.0604015128
## Port.Port.33 0.0207618401
## Port.Port.34 0.1663228307
## Port.Port.35 -0.1658395022
## Port.Port.36 -0.1761967634
## Port.Port.37 -0.6811737881
## Port.Port.38 0.2647416575
## Port.Port.39 -0.1781382938
## Port.Port.40 0.1688296535
## Port.Port.41 0.2137988165
## Port.Port.42 0.1211669439
## Port.Port.43 0.1451863711
## Port.Port.44 -0.1549744168
## Port.Port.45 0.0768054369
## Port.Port.46 -0.1111946686
## Port.Port.47 0.1377664477
## Port.Port.48 0.0779499755
## Port.Port.49 0.0500654422
## Port.Port.50 0.7437104125
## Port.Port.51 0.1957948988
## Port.Port.52 0.1020543766

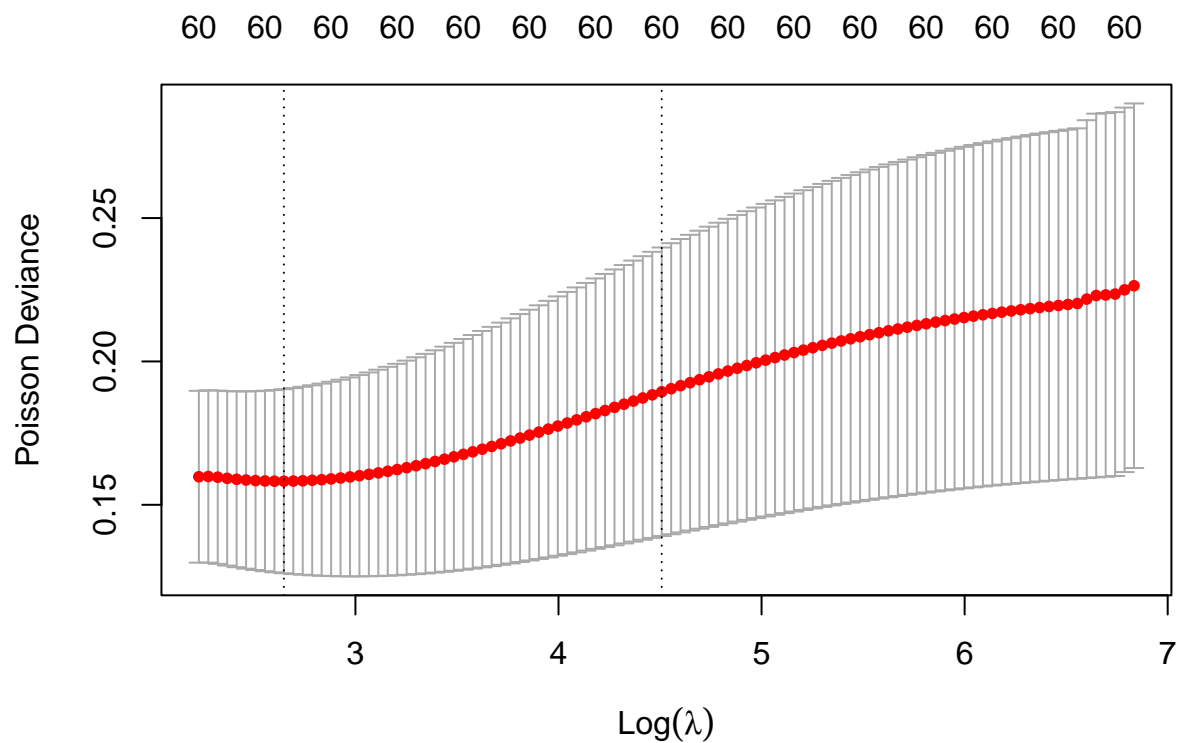
```

```
## Port.Port.53 0.2708461860
## Port.Port.54 -0.2068762343
## Port.Port.55 0.1262169362
## Port.Port.56 0.0834096003
## Port.Port.57 0.2127966093
## Port.Port.58 0.2555194380
## Port.Port.59 -0.2242603330
## Port.Port.60 0.0459284650
```

#Modélisation du nombre d'incidents

Modélisation Ridge de Poisson

```
#Modèle de Ridge de poisson
rescv_p <- cv.glmnet(XS, Y, family = "poisson", alpha = 0)
plot(rescv_p)
```



```
# Sélectionner le meilleur modèle en # utilisant la validation croisée
lambda=0
for (j in 1:10)
{
  rescv_poisson <- cv.glmnet(XS, Y, family = "poisson", alpha=0, lambda=seq(0.1, 100, 0.1))
  # Trouver le meilleur lambda (paramètre de régularisation)
  print(rescv_poisson$lambda.min)
  lambda=lambda+rescv_poisson$lambda.min
}
```

```
## [1] 13.8
## [1] 15
## [1] 10.4
## [1] 17.1
```

```

## [1] 11.4
## [1] 13.6
## [1] 15.1
## [1] 13.5
## [1] 15.8
## [1] 13.6

seuil=lambda/10

#On refait notre modèle avec le nouveau seuil trouvé
rescv_poisson <- glmnet(XS, Y, family = "poisson", alpha=0, lambda=seuil)

# Obtenir le vecteur des coefficients du meilleur modèle
best_coeffs <- coef(rescv_poisson)

# Sélectionner les variables non nulles du meilleur modèle
selected_vars <- which(best_coeffs != 0)

# Obtenez le nom des variables sélectionnées (en supposant que vous avez des noms de variables)
selected_var_names <- colnames(XS)[selected_vars]

# Deuxieme méthode
coef=coefficients(rescv_poisson)[-1] # on retire le coefficient 1
'la plupart de nos coeff sont différents de zéro donc une autre technique serait optimal
notamment un choix basé sur le seuillage ??'

## [1] "la plupart de nos coeff sont différents de zéro donc une autre technique serait optimal\nnotamm

#Lasso de Poisson
lambda=0
for (j in 1:10)
{
Lasso_poisson <- cv.glmnet(XS, Y, family = "poisson", alpha=1, lambda=seq(0.1, 100, 0.1))
# Trouver le meilleur lambda (paramètre de régularisation)
print(Lasso_poisson$lambda.1se)
lambda=lambda+Lasso_poisson$lambda.1se
}

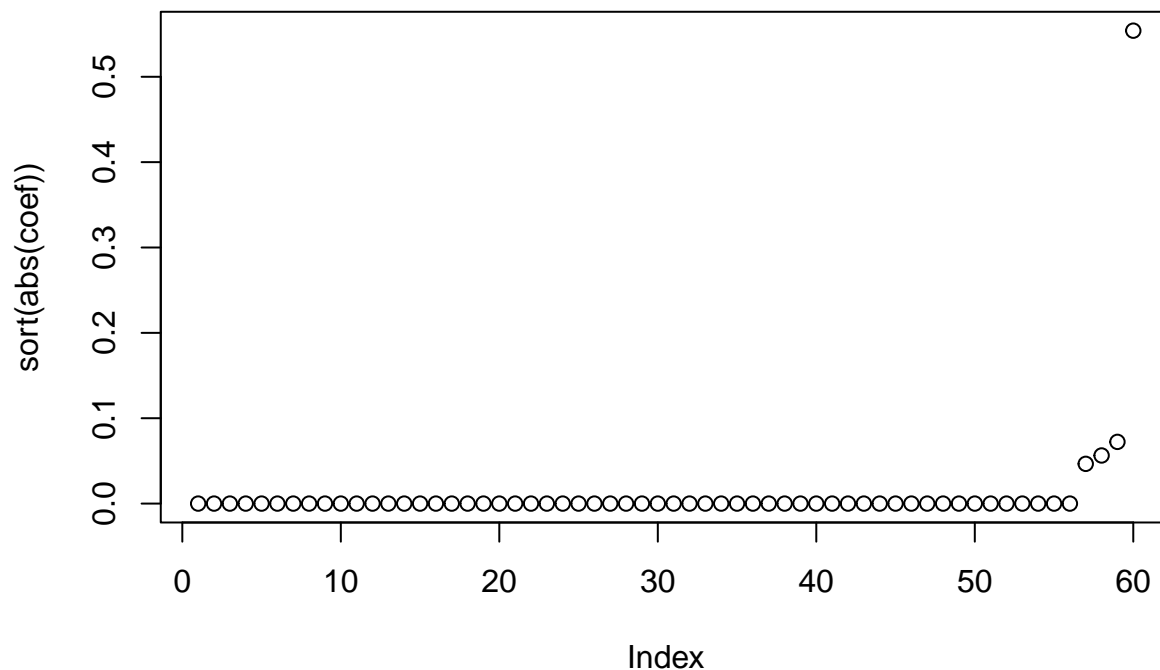
## [1] 0.6
## [1] 0.3
## [1] 0.3
## [1] 0.3
## [1] 0.3
## [1] 0.3
## [1] 0.3
## [1] 0.3
## [1] 0.3
## [1] 0.6
## [1] 0.3

seuil=lambda/10

Lasso_poisson=glmnet(XS,Y,family='gaussian',alpha=1, lambda=seuil)

coef=coefficients(Lasso_poisson)[-1]
plot(sort(abs(coef)))

```



```
which(coef!=0)
```

```
## [1] 3 5 7 58
```

```
# Extraire les coefficients du modèle Lasso (s = 0)
lasso_coefficients <- coef(Lasso_poisson, s = 0)
# Obtenir les indices des variables retenues
selected_indices <- which(lasso_coefficients != 0)
# Obtenir les noms des variables retenues
selected_variables <- colnames(lasso_coefficients)[selected_indices]
# Afficher les noms des variables retenues
print(selected_variables)
```

```
## [1] "s1" NA NA NA
```

Elasticnet de Poisson

```
lambda=0
for (j in 1:10)
{
  Elastinet_poisson <- cv.glmnet(XS, Y, family = "poisson", alpha=0.5, lambda=seq(0.1, 100, 0.1))
  # Trouver le meilleur lambda (paramètre de régularisation)
  print(Elastinet_poisson$lambda.1se)
  lambda=lambda+Elastinet_poisson$lambda.1se
}
```

```
## [1] 0.9
## [1] 0.7
## [1] 0.6
## [1] 0.8
## [1] 0.7
## [1] 0.7
## [1] 0.8
## [1] 0.7
```



```
## Warning in dpois(y, mu, log = TRUE): non-integer x = 6.270000
## Warning in dpois(y, mu, log = TRUE): non-integer x = 7.200000
## Warning in dpois(y, mu, log = TRUE): non-integer x = 6.810000
## Warning in dpois(y, mu, log = TRUE): non-integer x = 7.410000
## Warning in dpois(y, mu, log = TRUE): non-integer x = 8.410000
## Warning in dpois(y, mu, log = TRUE): non-integer x = 7.650000
## Warning in dpois(y, mu, log = TRUE): non-integer x = 6.330000
## Warning in dpois(y, mu, log = TRUE): non-integer x = 5.750000
## Warning in dpois(y, mu, log = TRUE): non-integer x = 10.550000
## Warning in dpois(y, mu, log = TRUE): non-integer x = 7.020000
## Warning in dpois(y, mu, log = TRUE): non-integer x = 7.320000
## Warning in dpois(y, mu, log = TRUE): non-integer x = 8.500000
## Warning in dpois(y, mu, log = TRUE): non-integer x = 5.010000
## Warning in dpois(y, mu, log = TRUE): non-integer x = 7.510000
## Warning in dpois(y, mu, log = TRUE): non-integer x = 6.590000
## Warning in dpois(y, mu, log = TRUE): non-integer x = 7.780000
## Warning in dpois(y, mu, log = TRUE): non-integer x = 5.040000
## Warning in dpois(y, mu, log = TRUE): non-integer x = 5.960000
## Warning in dpois(y, mu, log = TRUE): non-integer x = 7.060000
## Warning in dpois(y, mu, log = TRUE): non-integer x = 6.710000
## Warning in dpois(y, mu, log = TRUE): non-integer x = 7.670000
## Warning in dpois(y, mu, log = TRUE): non-integer x = 7.400000
## Warning in dpois(y, mu, log = TRUE): non-integer x = 9.740000
## Warning in dpois(y, mu, log = TRUE): non-integer x = 8.230000
## Warning in dpois(y, mu, log = TRUE): non-integer x = 9.520000
## Warning in dpois(y, mu, log = TRUE): non-integer x = 7.580000
## Warning in dpois(y, mu, log = TRUE): non-integer x = 8.500000
## Warning in dpois(y, mu, log = TRUE): non-integer x = 9.470000
## Warning in dpois(y, mu, log = TRUE): non-integer x = 7.120000
## Warning in dpois(y, mu, log = TRUE): non-integer x = 8.290000
## Warning in dpois(y, mu, log = TRUE): non-integer x = 7.250000
## Warning in dpois(y, mu, log = TRUE): non-integer x = 8.970000
## Warning in dpois(y, mu, log = TRUE): non-integer x = 8.830000
summary(model_poisson)
```

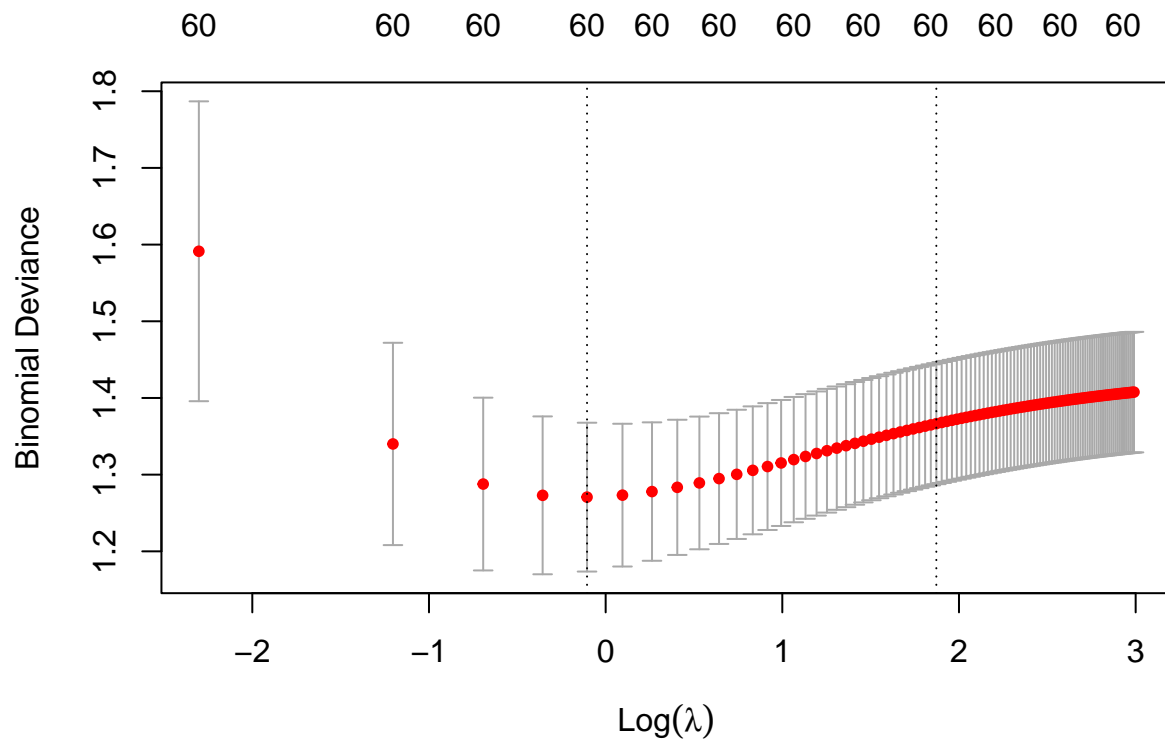
```
##
## Call:
## glm(formula = Y ~ ports_selectionnees, family = poisson)
##
## Coefficients:
##
##              Estimate Std. Error z value Pr(>|z|)
## (Intercept)      1.638705    0.921643   1.778  0.0754 .
## ports_selectionneesPort.Port.3  0.014696    0.039737   0.370  0.7115
## ports_selectionneesPort.Port.5  0.055896    0.036998   1.511  0.1308
## ports_selectionneesPort.Port.7 -0.039960    0.046935  -0.851  0.3946
## ports_selectionneesPort.Port.58  0.008395    0.020704   0.405  0.6851
## ---
## Signif. codes:  0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
##
## (Dispersion parameter for poisson family taken to be 1)
##
##      Null deviance: 8.3391  on 36  degrees of freedom
## Residual deviance: 2.3366  on 32  degrees of freedom
## AIC: Inf
##
## Number of Fisher Scoring iterations: 4
```

```
Y=data$CA
X=as.matrix(data[,5:64])
XS=scale(X)# Standardisation de la données

# Supposons que y est initialement une variable binaire (0 ou 1)
Y <- as.factor(Y)

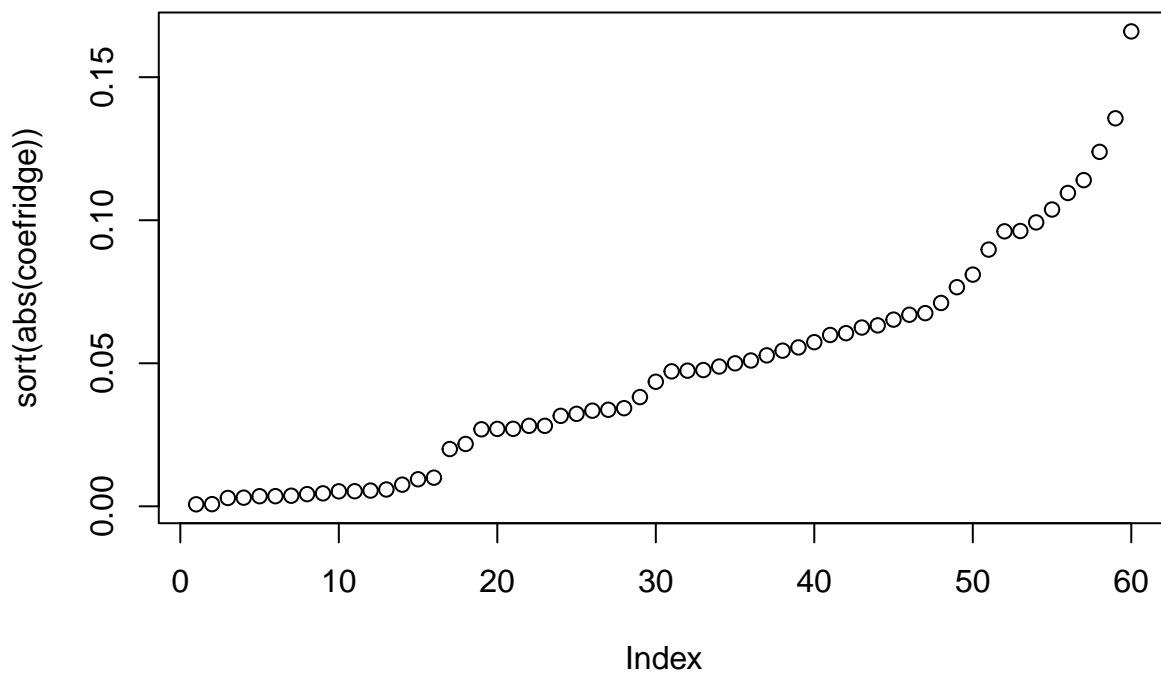
# Définir "1" comme le niveau par défaut
levels(Y) <- c("0", "1")

# Réalisez une régression logistique Ridge avec validation croisée
cv.ridge <- cv.glmnet(XS, Y, alpha = 0, family = "binomial",lambda=seq(0.1, 20, 0.2))
best_lambda <- cv.ridge$lambda.min # ou cv.ridge$lambda.1se selon votre choix
plot(cv.ridge)
```

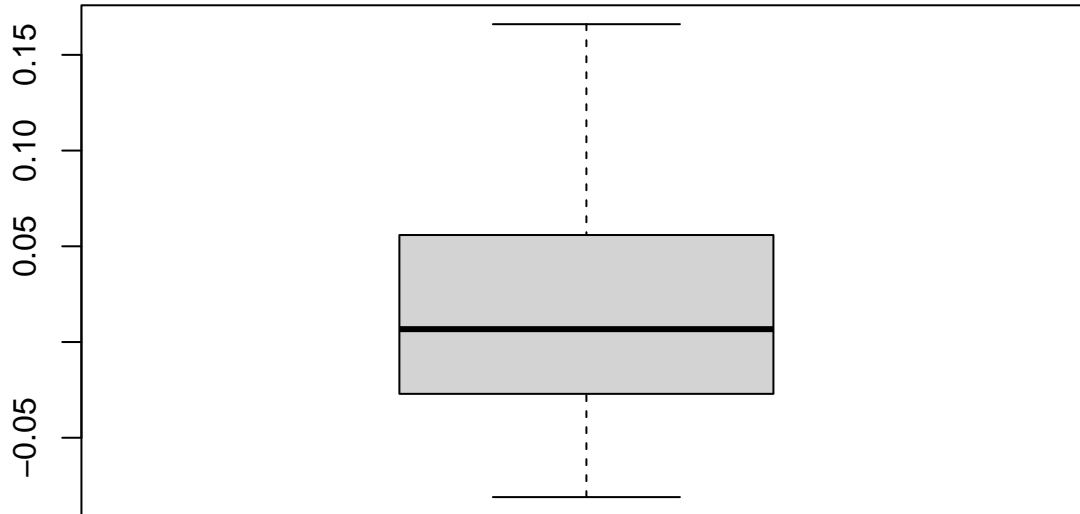



```
# Entraînez le modèle final avec le meilleur lambda
ridge_model <- glmnet(XS, Y, alpha = 0, lambda = best_lambda, family = "binomial")

# Sélection des variables
coefridge=coefficients(ridge_model)[-1]
plot(sort(abs(coefridge)))
```



```
boxplot(coefridge)
```



```
selec3=order(abs(coefridge),decreasing=TRUE)[1:3]  
selec3
```

```
## [1] 5 29 58
```

```
selec12=order(abs(coefridge),decreasing=TRUE)[1:6]  
selec12
```

```
## [1] 5 29 58 55 24 40
```

```
colnames(X[,selec3])
```

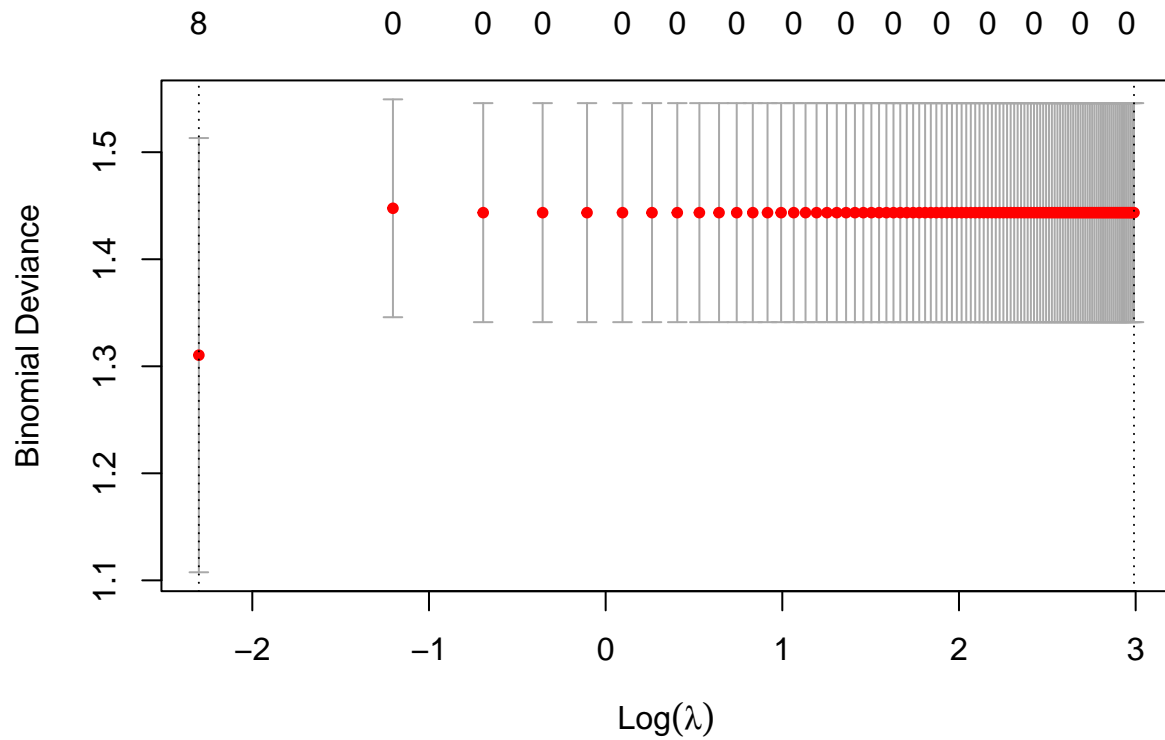
```
## [1] "Port.Port.5" "Port.Port.29" "Port.Port.58"
```

```
colnames(X[,selec12])
```

```
## [1] "Port.Port.5" "Port.Port.29" "Port.Port.58" "Port.Port.55" "Port.Port.24"  
## [6] "Port.Port.40"
```

Régression LASSO

```
rescv=cv.glmnet(XS,Y,family='binomial',alpha=1,lambda=seq(0.1, 20, 0.2))  
plot(rescv)
```



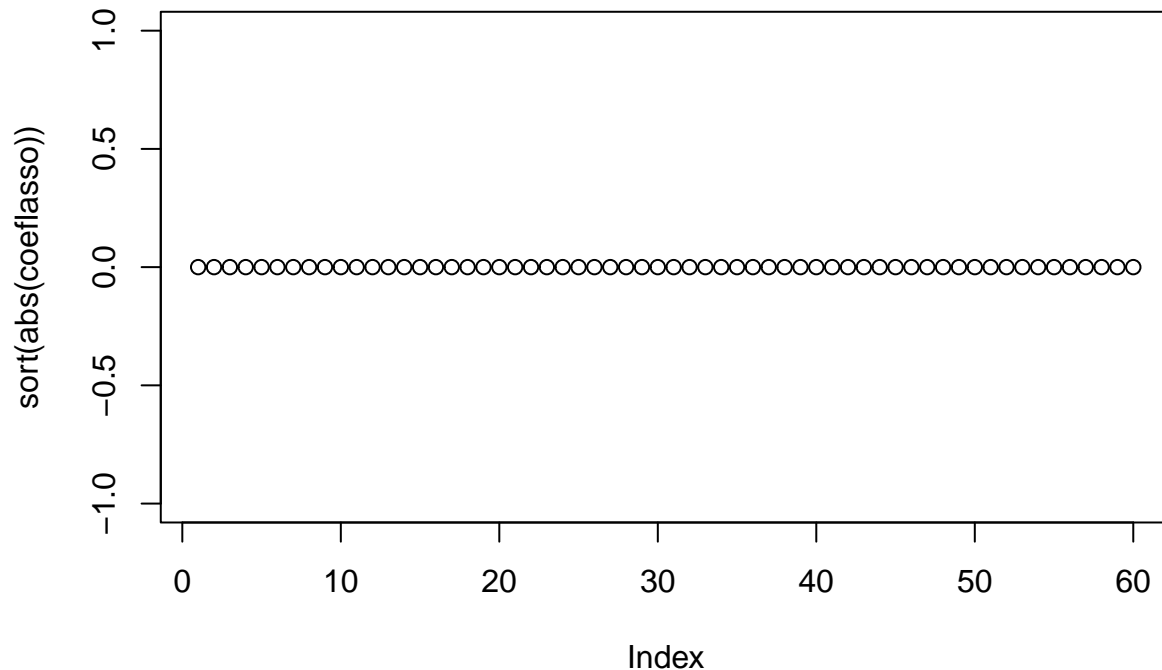
```

seuil=rescv$lambda.1se # sélection => lambda.1SE
# le lambda.1se varie car il d?pend de la partition utilis?e pour la CV
# l'id?al
reslasso=glmnet(X,Y,family='binomial',alpha=1,lambda=seuil)
reslasso

##
## Call:  glmnet(x = X, y = Y, family = "binomial", alpha = 1, lambda = seuil)
##
##      Df %Dev Lambda
## 1  0    0   19.9

coeflasso=coefficients(reslasso)[-1]
plot(sort(abs(coeflasso)))

```



```

selec6=order(abs(coeflasso),decreasing=TRUE)[1:6]
colnames(X[,selec6])

## [1] "Port.Port.1" "Port.Port.2" "Port.Port.3" "Port.Port.4" "Port.Port.5"
## [6] "Port.Port.6"

#AUC & Interprétation
# Obtenez les probabilités prédites
probas_lasso <- predict(reslasso, newx = as.matrix(XS), s = seuil, type = "response")

# Supposons que vous avez déjà les probabilités prédites dans une variable 'probas'
# et que 'Y' est votre variable de réponse binaire

roc_curve <- roc(Y, probas_lasso)

## Setting levels: control = 0, case = 1
## Warning in roc.default(Y, probas_lasso): Deprecated use a matrix as predictor.
## Unexpected results may be produced, please pass a numeric vector.
## Setting direction: controls < cases
roc_curve

##
## Call:
## roc.default(response = Y, predictor = probas_lasso)
##
## Data: probas_lasso in 22 controls (Y 0) < 15 cases (Y 1).
## Area under the curve: 0.5

auc_value <- auc(roc_curve)

# Obtenez les coefficients
coefficients_lasso <- coef(reslasso, s = seuil)

```

```
# Affichez les coefficients  
print(coefficients_lasso)
```

```
## 61 x 1 sparse Matrix of class "dgCMatrix"  
##                               s1  
## (Intercept) -0.3829923  
## Port.Port.1  0.0000000  
## Port.Port.2  .  
## Port.Port.3  .  
## Port.Port.4  .  
## Port.Port.5  .  
## Port.Port.6  .  
## Port.Port.7  .  
## Port.Port.8  .  
## Port.Port.9  .  
## Port.Port.10 .  
## Port.Port.11 .  
## Port.Port.12 .  
## Port.Port.13 .  
## Port.Port.14 .  
## Port.Port.15 .  
## Port.Port.16 .  
## Port.Port.17 .  
## Port.Port.18 .  
## Port.Port.19 .  
## Port.Port.20 .  
## Port.Port.21 .  
## Port.Port.22 .  
## Port.Port.23 .  
## Port.Port.24 .  
## Port.Port.25 .  
## Port.Port.26 .  
## Port.Port.27 .  
## Port.Port.28 .  
## Port.Port.29 .  
## Port.Port.30 .  
## Port.Port.31 .  
## Port.Port.32 .  
## Port.Port.33 .  
## Port.Port.34 .  
## Port.Port.35 .  
## Port.Port.36 .  
## Port.Port.37 .  
## Port.Port.38 .  
## Port.Port.39 .  
## Port.Port.40 .  
## Port.Port.41 .  
## Port.Port.42 .  
## Port.Port.43 .  
## Port.Port.44 .  
## Port.Port.45 .  
## Port.Port.46 .  
## Port.Port.47 .  
## Port.Port.48 .
```

```
## Port.Port.49 .
## Port.Port.50 .
## Port.Port.51 .
## Port.Port.52 .
## Port.Port.53 .
## Port.Port.54 .
## Port.Port.55 .
## Port.Port.56 .
## Port.Port.57 .
## Port.Port.58 .
## Port.Port.59 .
## Port.Port.60 .

# Supposons que vous avez déjà les coefficients dans une variable 'coefficients'
variable_significative <- names(coeflasso)[which.max(abs(coeflasso))]
cat("La variable la plus significative est :", variable_significative)
```

```
## La variable la plus significative est :
```

Modélisation de CA3

```
# Supposons que X soit votre matrice de variables explicatives et Y votre variable réponse CA3

# Convertir la variable réponse en facteur
Y=data$CA3
X=as.matrix(data[,5:64])
XS=scale(X)# Standardisation de la données
Y <- as.factor(Y)

# Appliquer la régression multinomiale pénalisée avec la validation croisée
cv_fit_multinom <- cv.glmnet(x = XS, y = Y, family = "multinomial", alpha = 1, lambda=seq(0.1, 20, 0.2))

## Warning in lognet(xd, is.sparse, ix, jx, y, weights, offset, alpha, nobs, : one
## multinomial or binomial class has fewer than 8 observations; dangerous ground

# Obtenir le meilleur lambda à partir de la validation croisée
best_lambda_multinom <- cv_fit_multinom$lambda.min

# Appliquer la régression multinomiale pénalisée avec le meilleur lambda
fit_multinom_best_lambda <- glmnet(x = XS, y = Y, family = "multinomial", alpha = 1, lambda = best_lambda_multinom)
fit_multinom_best_lambda

##
## Call:  glmnet(x = XS, y = Y, family = "multinomial", alpha = 1, lambda = best_lambda_multinom)
##
##   Df   %Dev Lambda
## 1 13 37.72   0.1

# Sélectionner les variables
selected_vars <- coef(fit_multinom_best_lambda)

# Afficher les variables sélectionnées
print(selected_vars)

## $`0`
## 61 x 1 sparse Matrix of class "dgCMatrix"
```

```

##                                     s0
##                                -0.26488018
## Port.Port.1      .
## Port.Port.2      -0.26869940
## Port.Port.3      .
## Port.Port.4      .
## Port.Port.5      .
## Port.Port.6      .
## Port.Port.7      .
## Port.Port.8      .
## Port.Port.9      .
## Port.Port.10     .
## Port.Port.11     .
## Port.Port.12     .
## Port.Port.13     .
## Port.Port.14     .
## Port.Port.15     .
## Port.Port.16     .
## Port.Port.17     .
## Port.Port.18     .
## Port.Port.19     .
## Port.Port.20     .
## Port.Port.21     .
## Port.Port.22     .
## Port.Port.23     .
## Port.Port.24     .
## Port.Port.25     .
## Port.Port.26     .
## Port.Port.27     -0.35282103
## Port.Port.28     .
## Port.Port.29     -0.01203646
## Port.Port.30     .
## Port.Port.31     .
## Port.Port.32     .
## Port.Port.33     0.10941111
## Port.Port.34     .
## Port.Port.35     .
## Port.Port.36     .
## Port.Port.37     .
## Port.Port.38     .
## Port.Port.39     .
## Port.Port.40     .
## Port.Port.41     .
## Port.Port.42     .
## Port.Port.43     .
## Port.Port.44     .
## Port.Port.45     .
## Port.Port.46     -0.34437403
## Port.Port.47     .
## Port.Port.48     .
## Port.Port.49     .
## Port.Port.50     .
## Port.Port.51     .
## Port.Port.52     .

```

```

## Port.Port.53 .
## Port.Port.54 .
## Port.Port.55 .
## Port.Port.56 .
## Port.Port.57 .
## Port.Port.58 -0.03163133
## Port.Port.59 .
## Port.Port.60 .
##
## $`1`
## 61 x 1 sparse Matrix of class "dgCMatrix"
##              s0
##      0.153760453
## Port.Port.1 .
## Port.Port.2 0.143987133
## Port.Port.3 .
## Port.Port.4 .
## Port.Port.5 .
## Port.Port.6 .
## Port.Port.7 .
## Port.Port.8 .
## Port.Port.9 .
## Port.Port.10 .
## Port.Port.11 .
## Port.Port.12 .
## Port.Port.13 .
## Port.Port.14 .
## Port.Port.15 .
## Port.Port.16 .
## Port.Port.17 .
## Port.Port.18 .
## Port.Port.19 .
## Port.Port.20 .
## Port.Port.21 .
## Port.Port.22 .
## Port.Port.23 .
## Port.Port.24 .
## Port.Port.25 .
## Port.Port.26 .
## Port.Port.27 .
## Port.Port.28 .
## Port.Port.29 .
## Port.Port.30 .
## Port.Port.31 .
## Port.Port.32 -0.056285411
## Port.Port.33 .
## Port.Port.34 .
## Port.Port.35 .
## Port.Port.36 .
## Port.Port.37 .
## Port.Port.38 .
## Port.Port.39 .
## Port.Port.40 .
## Port.Port.41 .

```



```

## Port.Port.42 0.007496989
## Port.Port.43 .
## Port.Port.44 .
## Port.Port.45 .
## Port.Port.46 .
## Port.Port.47 .
## Port.Port.48 .
## Port.Port.49 .
## Port.Port.50 .
## Port.Port.51 .
## Port.Port.52 .
## Port.Port.53 .
## Port.Port.54 .
## Port.Port.55 .
## Port.Port.56 .
## Port.Port.57 .
## Port.Port.58 .
## Port.Port.59 .
## Port.Port.60 .
##
## $`2`
## 61 x 1 sparse Matrix of class "dgCMatrix"
##              s0
##              0.111119730
## Port.Port.1 .
## Port.Port.2 .
## Port.Port.3 .
## Port.Port.4 .
## Port.Port.5 0.774572842
## Port.Port.6 .
## Port.Port.7 .
## Port.Port.8 .
## Port.Port.9 .
## Port.Port.10 .
## Port.Port.11 .
## Port.Port.12 .
## Port.Port.13 .
## Port.Port.14 .
## Port.Port.15 .
## Port.Port.16 .
## Port.Port.17 .
## Port.Port.18 .
## Port.Port.19 .
## Port.Port.20 .
## Port.Port.21 .
## Port.Port.22 .
## Port.Port.23 .
## Port.Port.24 0.144681561
## Port.Port.25 .
## Port.Port.26 .
## Port.Port.27 .
## Port.Port.28 .
## Port.Port.29 0.275670330
## Port.Port.30 .

```

```
## Port.Port.31 .
## Port.Port.32 .
## Port.Port.33 .
## Port.Port.34 .
## Port.Port.35 .
## Port.Port.36 .
## Port.Port.37 .
## Port.Port.38 .
## Port.Port.39 .
## Port.Port.40 0.217898160
## Port.Port.41 .
## Port.Port.42 .
## Port.Port.43 0.006916185
## Port.Port.44 .
## Port.Port.45 .
## Port.Port.46 .
## Port.Port.47 .
## Port.Port.48 .
## Port.Port.49 .
## Port.Port.50 .
## Port.Port.51 .
## Port.Port.52 .
## Port.Port.53 .
## Port.Port.54 0.031622876
## Port.Port.55 .
## Port.Port.56 .
## Port.Port.57 .
## Port.Port.58 .
## Port.Port.59 .
## Port.Port.60 .
```

Régression polytomique ordonnée

```
# Supposons que Y_ordered est votre variable réponse ordonnée et X_Select est votre matrice d'variables
# Convertir Y_ordered en une variable ordonnée si ce n'est pas déjà fait
Y_ordered <- as.ordered(Y)

# Créer une matrice X_Select (remplacez cela par votre propre matrice)
X_Select <- data[, c("Port.Port.5", "Port.Port.24", "Port.Port.29",
                    "Port.Port.40", "Port.Port.43", "Port.Port.54")]

# Appliquer la régression polytomique ordonnée
fit_ord <- clm(Y_ordered ~ ., data = cbind(X_Select, Y_ordered))

# Afficher les résultats
summary(fit_ord)

## formula:
## Y_ordered ~ Port.Port.5 + Port.Port.24 + Port.Port.29 + Port.Port.40 + Port.Port.43 + Port.Port.54
## data:      cbind(X_Select, Y_ordered)
##
## link threshold nobs logLik AIC niter max.grad cond.H
## logit flexible 37 -16.26 48.52 7(0) 4.86e-10 1.1e+06
```

```
##
## Coefficients:
##           Estimate Std. Error z value Pr(>|z|)
## Port.Port.5      1.2583     0.4529   2.778  0.00547 **
## Port.Port.24     0.6393     0.3278   1.951  0.05110 .
## Port.Port.29     0.6591     0.2594   2.541  0.01106 *
## Port.Port.40     0.6848     0.2503   2.736  0.00623 **
## Port.Port.43     0.3929     0.2070   1.898  0.05774 .
## Port.Port.54     0.9872     0.4832   2.043  0.04103 *
## ---
## Signif. codes:  0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
##
## Threshold coefficients:
##           Estimate Std. Error z value
## 0|1      39.76      13.63   2.918
## 1|2      44.70      14.78   3.024
```

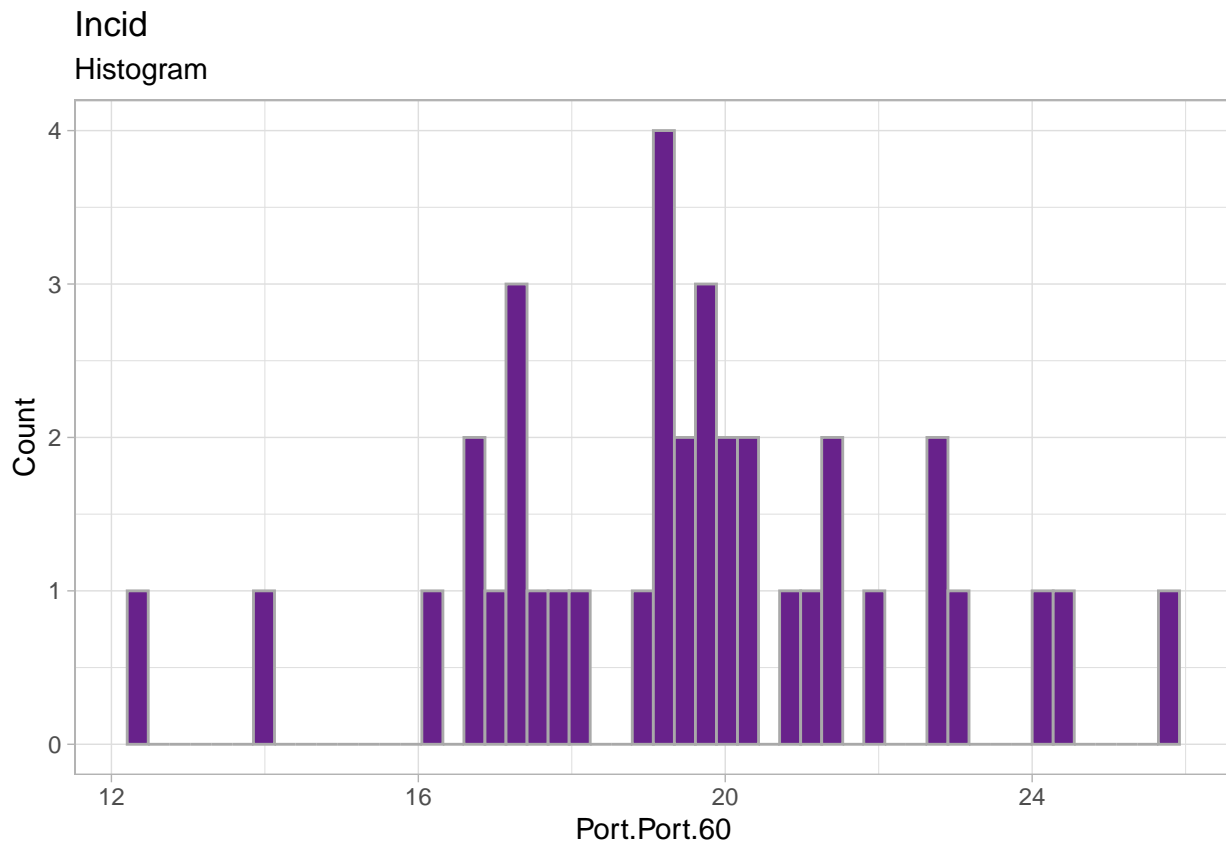
```
stargazer(fit_ord, title = "Régression polytomique ordonnée", out = "table.tex")
```

```
##
## % Table created by stargazer v.5.2.3 by Marek Hlavac, Social Policy Institute. E-mail: marek.hlavac@vse.cz
## % Date and time: Thu, Dec 14, 2023 - 18:43:59
## \begin{table}[!htbp] \centering
##   \caption{Régression polytomique ordonnée}
##   \label{}
##   \begin{tabular}{@{\extracolsep{5pt}}lc}
##     \hline
##     \hline \hline
##     & \multicolumn{1}{c}{\textit{Dependent variable:}} & \\
##     \cline{2-2}
##     \hline \hline & Y\_ordered & \\
##     \hline \hline
##     Port.Port.5 & 1.258$^{***}$ & \\
##     & (0.453) & \\
##     & & \\
##     Port.Port.24 & 0.639$^{*}$ & \\
##     & (0.328) & \\
##     & & \\
##     Port.Port.29 & 0.659$^{**}$ & \\
##     & (0.259) & \\
##     & & \\
##     Port.Port.40 & 0.685$^{***}$ & \\
##     & (0.250) & \\
##     & & \\
##     Port.Port.43 & 0.393$^{*}$ & \\
##     & (0.207) & \\
##     & & \\
##     Port.Port.54 & 0.987$^{**}$ & \\
##     & (0.483) & \\
##     & & \\
##     \hline \hline
##     Observations & 37 & \\
##     Log Likelihood & -$16.258 & \\
##     \hline
##     \hline \hline
```

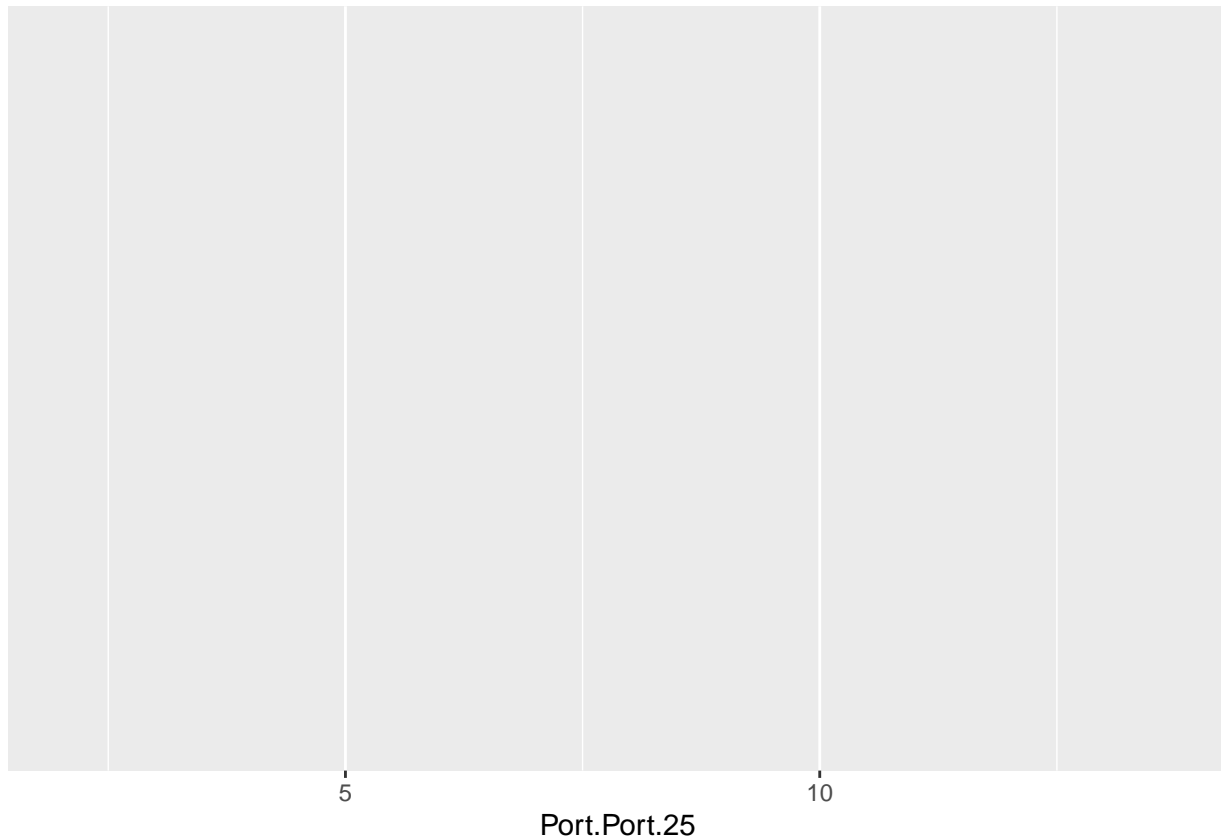
```
## \textit{Note:} & \multicolumn{1}{r}{\textit{\textsuperscript{*}}$p$<$0.1; \textit{\textsuperscript{*}}$p$<$0.05; \textit{\textsuperscript{***}}$p$<$0.01} \\\n## \end{tabular}\n## \end{table}
```

Histogramme

```
histo_mass <- ggplot(data)+\n  geom_histogram(aes(x=Port.Port.60), fill="darkorchid4", color="darkgray", bins=50)+\n  labs(title = "Incid", subtitle = "Histogram")+ \n  ylab("Count")+theme_light()\nhisto_mass
```



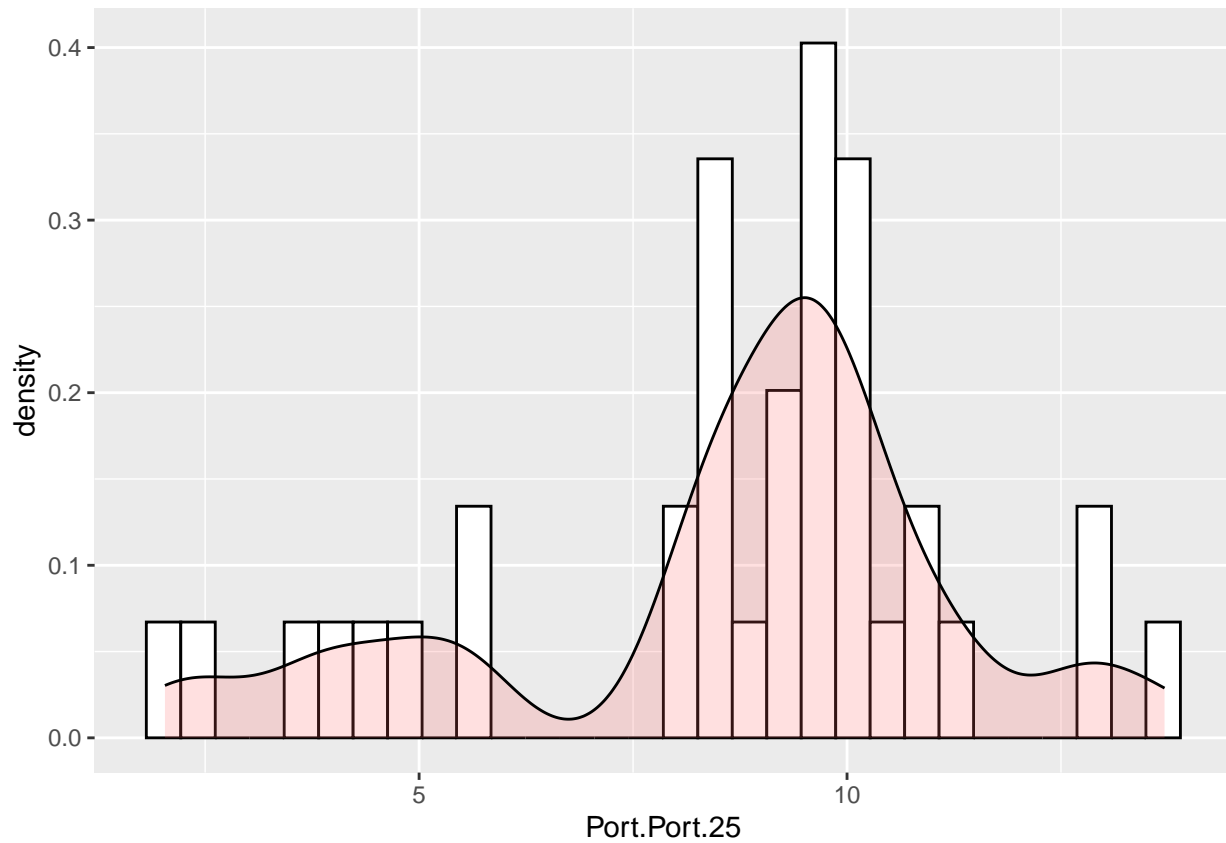
```
a <- ggplot(data, aes(x = Port.Port.25))\na
```



```
# Histogram with density plot
a + geom_histogram(aes(y = ..density..),
                   colour="black", fill="white") +
  geom_density(alpha = 0.2, fill = "#FF6666")
```

```
## Warning: The dot-dot notation (`..density..`) was deprecated in ggplot2 3.4.0.
## i Please use `after_stat(density)` instead.
## This warning is displayed once every 8 hours.
## Call `lifecycle::last_lifecycle_warnings()` to see where this warning was
## generated.

## `stat_bin()` using `bins = 30`. Pick better value with `binwidth`.
```



```
a + geom_histogram(aes(y = after_stat(density)), bins = 30, colour = "black", fill = "white") +  
  geom_density(alpha = 0.2, fill = "#FF6666")
```

