

Q3

$$\begin{aligned}\min Z &= x_1 + x_2 \\ \text{s.t.} \quad &x_1 + 2x_2 = 3 \\ &x_1 - 2x_2 \leq -5 \\ &x_1 + 5x_2 \leq 2 \\ &x_1, x_2 \geq 0\end{aligned}$$

∴ removing (-ve) from RHS and adding slack, surplus and artificial variables wherever required to convert it into standard L.P. format:

$$\begin{aligned}\therefore \min Z &= x_1 + x_2 - m a_1 - m a_2 = 0 \\ &x_1 + 2x_2 + a_1 = 3 \\ &-x_1 + 2x_2 - e_2 + a_2 = 5 \\ &x_1 + 5x_2 + s_3 = 2\end{aligned}$$

$$\text{where, } x_1, x_2, a_1, a_2, e_2, s_3 \geq 0.$$

∴ Creating tableau based on it for simplex LP:

	Z	x_1	x_2	a_1	e_2	a_2	S_3	RHS	BV	Ratio
R0	1	-1	-1	-M	0	-M	0	0	Z	
R1	0	1	2	1	0	0	0	3	a_1	
R2	0	-1	2	0	-1	1	0	5	a_2	
R3	0	1	5	0	0	0	1	2	S_3	

→ Removing $(-M)$ from (R0) to have a_1 coefficient as 0.

↓

$M \times R_1 + M \times R_2 \rightarrow R_0$	1	-1	$-1+4M$	0	-M	0	0	$8M$	Z	
R1	0	1	2	1	0	0	0	3	a_1	$3/2$
R2	0	-1	2	0	-1	1	0	5	a_2	$5/2$
← R3	0	1	5	0	0	0	1	2	S_3	2/5

→ Now, ~~enter~~ x_2 is entering variable based on its highest coefficient value in (R0).
 ∴ With ^{min} ratio test, we get S_3 as leaving variable.
 ∴ making x_2 column identity column, we get following table:

$\frac{-4M+1}{5} R_3 + R_0 \rightarrow R_0$	1	$-1+\frac{4M}{5}$	0	0	-M	0	$-\frac{4M}{5}$	$\frac{8M}{5}$	Z	
$\frac{2}{5} R_3 + R_1$	0	$1-\frac{2}{5}$	0	1	0	0	$-\frac{2}{5}$	$\frac{14}{5}$	a_1	$\frac{14}{5}$
$-\frac{2}{5} R_3 + R_2$	0	$-\frac{7}{5}$	0	0	-1	1	$-\frac{2}{5}$	$\frac{24}{5}$	a_2	$\frac{24}{5}$
$R_3 \Rightarrow R_3$	0	$1/5$	1	0	0	0	$1/5$	$2/5$	x_2	

∴ So, we don't have any feasible solution as we have a_1, a_2 still in solution but no further iteration.