

Q2

min<sup>m</sup> cost assignment of persons of jobs using hungarian method can be done in following way:  $\min w = \sum_{i=1}^3 \sum_{j=1}^5 c_{ij} x_{ij}$ ,  $x_{ij} = \begin{cases} 1 & \text{if assigned} \\ 0 & \text{if not assigned} \end{cases}$

→ As person 2 and 3 can do ~~more~~ two jobs we have added extra rows for 2' and 3'.  
also, as we need no. of rows = no. of columns for balancing we will add dummy column '5' of 0 values.

	1	2	3	4	5	min <sup>m</sup> of row
1	50	46	42	40	0	0
2	51	48	44	*	0	0
3	*	47	45	45	0	0
2'	51	48	44	*	0	0
3'	*	47	45	45	0	0

min<sup>m</sup> of column 50 46 42 40 0

∴ We get on subtracting min<sup>m</sup> of column from each column element,

	1	2	3	4	5	
1	0	0	0	0	0	①
2	1	2	2	*	0	
3	*	1	3	5	0	
2' → 4	1	2	2	*	0	
3' → 5	*	1	3	5	0	

as, lines = ② but matrix (5x5) ②

∴ now, min<sup>m</sup> = 1 ∴ adding that at intersection of ① and ② and subtracting it from all other, ②



	1	2	3	4	5
1	0	0	0	0	1
2	0	1	1	*	0
3	*	0	2	4	0
4	0	1	1	*	0
5	*	0	2	4	0

lines = 3, matrix (5x5)

∴ next iteration.

(minim = 1)

	1	2	3	4	5	<u>zeros</u>
1	1	1	0	<span style="border: 1px solid black;">0</span>	2	2
2	<span style="border: 1px solid black;">0</span>	1	0	*	0	2
3	*	<span style="border: 1px solid black;">0</span>	1	3	0	2
4	0	1	<span style="border: 1px solid black;">0</span>	*	0	2
5	*	0	1	3	<span style="border: 1px solid black;">0</span>	2
<u>zeros</u>	2	2	2	1	4	

now, lines = 5 = matrix size.

∴ optimal table.

now, looking at no. of zeros and allocating for least zero rows and columns, we get,

optimal solution  $\Rightarrow x_{21} = x_{32} = x_{23} = x_{35}$   
 $= x_{14} = 1$ , other  $x_{ij} = 0$

$$\therefore \text{minim cost} = (40 \times 1) + (51 \times 1) + (47 \times 1) + (44 \times 1)$$

$$= \boxed{182}$$