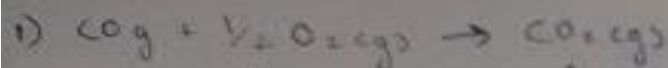


## THERMODYNAMICS CHAPTER PRACTICE PROBLEMS

1. Show that the reaction  $\text{CO(g)} + \frac{1}{2}\text{O}_2\text{(g)} \longrightarrow \text{CO}_2\text{(g)}$  at 300 K is spontaneous and exothermic. When standard entropy change is  $-0.094 \text{ KJ/mol}^\circ$ ? The standard Gibbs free energy of formation for  $\text{CO}_2$  and  $\text{CO}$  are  $-394.4$  and  $-137.2 \text{ KJ mol}^{-1}$ , respectively.



$\Delta G^\circ$  can be calculated as follows

$$\begin{aligned}\Delta G^\circ &= \Delta G^\circ_{\text{PRODUCTS}} - \Delta G^\circ_{\text{REACTANTS}} \\ &= [\Delta G^\circ_{\text{CO}_2} - \frac{1}{2} \Delta G^\circ_{\text{O}_2} - \Delta G^\circ_{\text{CO}}] \\ &= -394 - (\frac{1}{2} \times 0) - (-137.2) \\ &= -257.2 \text{ KJ mol}^{-1}\end{aligned}$$

Since  $\Delta G^\circ = \Delta H^\circ - T\Delta S^\circ$

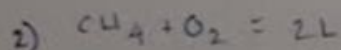
$$\Rightarrow -257.2 = \Delta H^\circ - 300(-0.094)$$

$$\Rightarrow \Delta H^\circ = -255.4 \text{ KJ/mol}$$

$\rightarrow \Delta H^\circ$  is negative Hence Reaction is Exothermic

$\rightarrow \Delta G^\circ$  is negative Hence Reaction is Spontaneous

2. A 1.00 L sample of a mixture of methane gas and oxygen, measured at  $25^\circ\text{C}$  and 740 torr pressure, was allowed to react at constant pressure in a calorimeter which together with its contents, had a heat capacity of 1260 cal/K. The complete combustion of the methane to carbon dioxide and liquid water caused a temperature rise in the calorimeter of 0.667 K. What was the mol percent of  $\text{CH}_4$  in the original mixture? [ $\Delta H_{\text{comb}}$  for  $\text{CH}_4\text{(g)} = -210.8 \text{ kcal/mol}$ .]



$$T = 25^\circ\text{C} = 298 \text{ K}$$

$$P = 740 \text{ torr} = \frac{740}{760} \text{ atm} \quad \left\{ \frac{x \text{ torr}}{760} = y \text{ atm} \right\}$$

$$S = 1260 \text{ cal/K}$$

$$\begin{aligned}\text{Total No. of moles of gas} &= \frac{PV}{RT} = \frac{\frac{740}{760} \times 1}{0.0821 \times 298} \\ &= 3.98 \times 10^{-2} \text{ moles}\end{aligned}$$

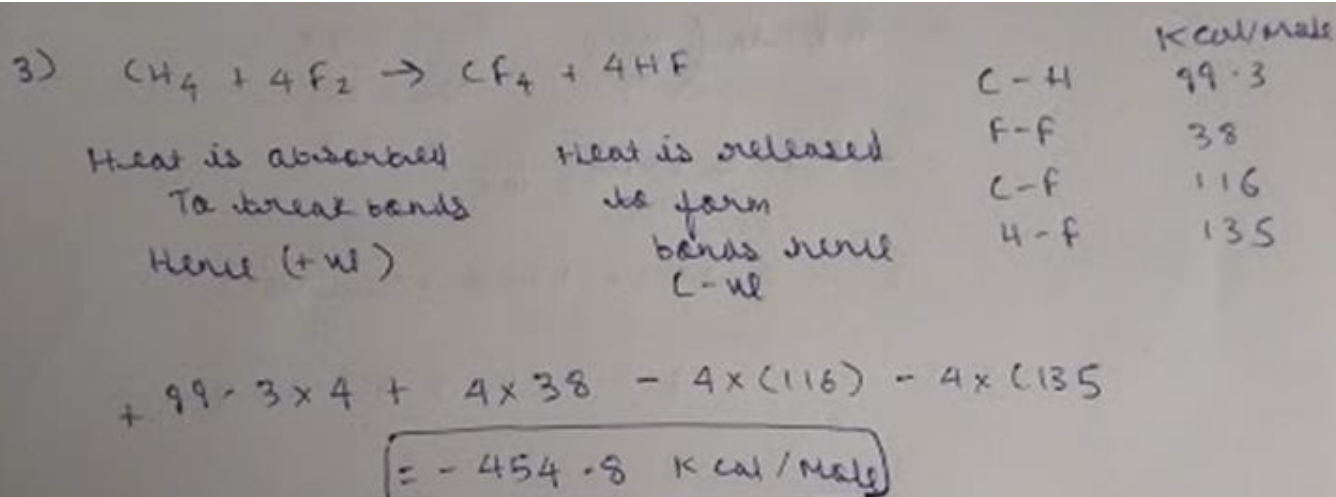
$$\begin{aligned}\Delta H &= 1260 \times 0.667 \text{ K} \quad (\Delta H = \text{Heat} \times S \times \Delta T) \\ &= 840.4 \text{ cal}\end{aligned}$$

$$\begin{aligned}\text{No. of Moles} &= \frac{\text{Heat produced by CH}_4}{\text{Heat produced in 1 mole}} = \frac{840.4 \text{ cal}}{210.8 \times 10^3} \\ &= 3.99 \times 10^{-3} \text{ moles}\end{aligned}$$

$$\% \text{ of Molecules} = \frac{3.94 \times 10^{-3}}{3.98 \times 10^{-3}} \{ \text{moles of } \text{CH}_4 \}$$

$$= 10\%$$

3. Calculate the heat of following gaseous reaction  $\text{CH}_4 + 4\text{F}_2 \rightarrow \text{CF}_4 + 4\text{HF}$  the bond energy of C-H, F-F, C-F and H-F bonds are 99.3, 38, 116 and 135 KCal/mole respectively



4. The heat of reaction for  $\text{N}_2 + 3\text{H}_2 \rightarrow 2\text{NH}_3$  at  $27^\circ\text{C}$  is  $-91.94 \text{ KJ}$ . What will be its value at  $50^\circ\text{C}$ ? The molar heat capacities at constant pressure and  $27^\circ\text{C}$  for  $\text{N}_2$ ,  $\text{H}_2$  and  $\text{NH}_3$  are 28.45, 28.32 and 37.07 joule respectively.

4)  $\Delta H(T_2) = \Delta H(T_1) + C_p(T_2 - T_1)$

$T_1 = 27^\circ\text{C}$

$T_2 = 50^\circ\text{C}$

$C_p(\text{NH}_3) = 37.07$   
 $C_p(\text{N}_2) = 28.45$   
 $C_p(\text{H}_2) = 28.32$

$$\Delta H(T_1) = -91.94 \text{ KJ/mol}$$

$$\Delta C_p = 2 \times C_p(\text{NH}_3) - C_p(\text{N}_2) - C_p(\text{H}_2) \times 3$$

$$= 2 \times 37.07 - 28.45 - 3 \times 28.32$$

$$= -39.27 \text{ KJ/mol} \times 10^{-3}$$

$$\Delta H(T_2) = -91.94 + [-0.03927 \times (50 - 27)]$$

$$= -91.94 - (0.90)$$

$$= -92.84 \text{ KJ/mol}$$

5. Calculate  $W$  and  $q$  for the isothermal reversible expansion of one mole of an ideal gas from an initial pressure of 1.0 bar to a final pressure of 0.1 bar at a constant temperature of 273 K.

$$\begin{aligned}
 5) \quad w_{\text{rev}} &= - \int_{V_1}^{V_2} P dV & n &= 1 \\
 & & R &= 8.303 \sim 8.3 \\
 &= -nRT \ln \left( \frac{V_2}{V_1} \right) & T &= 273 \text{ K} \\
 & & V_2 &= 0.1 \\
 & & V_1 &= 1 \\
 &= - (1) \times 8.3 \times \ln \left( \frac{1}{10} \right) \times 273 \\
 &= - 2.303 \times (1) \times 8.3 \times \log 10^{-1} \times 273 \\
 &= + 2.303 \times 8.3 \times 273
 \end{aligned}$$

$$w_{\text{rev}} = -nRT \log \left( \frac{P_1}{P_2} \right) \times 2.303$$

$$n = 1$$

$$R = 8.3$$

$$T = 273 \text{ K}$$

$$P_1 = 1$$

$$P_2 = 0.1$$

$$\begin{aligned}
 \Rightarrow w_{\text{rev}} &= -1 \times 8.3 \times \log 10 \times 2.303 \times 273 \\
 &= 8.3 \times 2.303 \times 273 \\
 &= \boxed{5212.7}
 \end{aligned}$$

$$W = -q \quad \left\{ \begin{array}{l} \text{Isothermal} \\ \text{Reversible} \end{array} \right\}$$

$$\Rightarrow q = \boxed{+ 5212.7}$$

