Solutions

Mock Exam 2025

Time Management Guide

This two-hour examination requires careful time management:

Question 1 (40 marks) - Approximately 30 minutes

- Description and plotting (20 marks): 15 minutes
- Frequency and outlier analysis (20 marks): 15 minutes

Question 2 (50 marks) - Approximately 35 minutes

• Analysis of five time series: 7 minutes each

Choice of Question 3, 4, or 5 (50 marks) - Approximately 45 minutes

- Question 3: STL decomposition and forecasting
- Question 4: ARIMA modeling and forecasting
- Question 5: Reflective essay on LLM collaboration

Reserve 10 minutes for review and final checks

```
library(fpp2)
library(knitr)
library(forecast)
```

Assessment Guide

This solutions document demonstrates the expected depth and quality of analysis for the Advanced Financial Data Analytics exam. When interpreting time series data:

1. **Descriptive analysis** should identify key features (trend, seasonality, cycles) with specific references to time periods where patterns change.

- 2. **Visual interpretations** should connect statistical features to business/economic context where appropriate.
- 3. **Statistical discussions** should include both the technical meaning and practical implications of results.
- 4. **Justifications** for modelling choices should reference both graphical evidence and theoretical principles.

Cross-Question Insights

The techniques covered in these questions are interconnected:

- Question 1's outlier analysis informs Question 3's robust STL choice
- Question 2's pattern identification guides Question 4's ARIMA modeling
- Statistical methods in Questions 1-4 provide context for Question 5's LLM discussion

Question 1

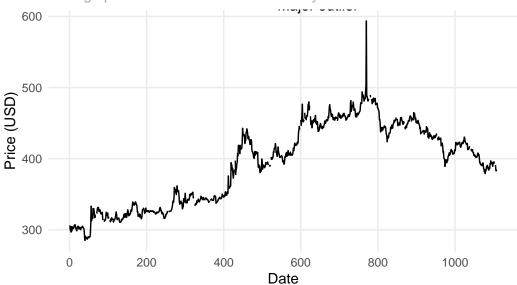
b. Plotting the time series:

To begin our analysis, let's create professional-looking plots for each of the three commodity series: gold, woolyrnq, and gas. We'll use the autoplot() function from the forecast package and add appropriate labels and titles.

```
library(ggplot2)
# Enhanced visualisation with proper formatting and consistent design elements
autoplot(gold) +
  labs(title = "Daily Morning Gold Prices",
       subtitle = "Strong upward trend with notable volatility",
       x = "Date",
       y = "Price (USD)") +
  theme_minimal() +
  theme(
    plot.title = element_text(face = "bold"),
    plot.subtitle = element text(color = "darkgrey"),
    panel.grid.minor = element_blank()
  ) +
  # Adding annotation for outlier
  annotate("text", x = which.max(gold), y = max(gold, na.rm=TRUE),
           label = "Major outlier", vjust = -1, hjust = 1.1)
```

Daily Morning Gold Prices





```
# Similarly enhanced plots for woolyrnq and gas would follow the same pattern
# autoplot(woolyrnq) +
    labs(title = "Quarterly Wool Production in Australia",
         subtitle = "Clear seasonal pattern with declining trend",
#
         x = "Date", y = "Production") +
  theme_minimal() +
   theme(
#
#
     plot.title = element_text(face = "bold"),
#
     plot.subtitle = element_text(color = "darkgrey"),
#
     panel.grid.minor = element_blank()
#
    )
#
# autoplot(gas) +
   labs(title = "Australian Monthly Gas Production",
#
         subtitle = "Increasing trend with seasonal variation",
#
         x = "Date", y = "Production") +
#
  theme_minimal() +
#
   theme(
#
#
      plot.title = element_text(face = "bold"),
     plot.subtitle = element_text(color = "darkgrey"),
#
     panel.grid.minor = element_blank()
```

From the plots, we can make the following observations:

- The gold series shows an overall increasing trend with some fluctuations. There appears to be an outlier with an unusually high price. This outlier could correspond to a period of market volatility or a specific economic event that triggered a price spike.
- The woolyrnq series exhibits a clear seasonal pattern, with production peaking in certain quarters and declining in others. There is also a slight overall downward trend, suggesting a gradual decline in the wool industry over this period.
- The gas series shows an increasing trend with some seasonal variation. The seasonality appears to be less pronounced compared to the woolyrnq series, indicating more stable year-round demand with gradual production growth.
- b. Frequency of each series:

To determine the frequency of each commodity series, we can use the frequency() function.

frequency(gold)

[1] 1

frequency(woolyrnq)

[1] 4

frequency(gas)

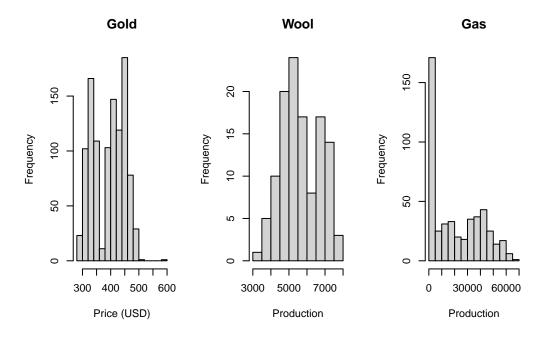
[1] 12

The output reveals that:

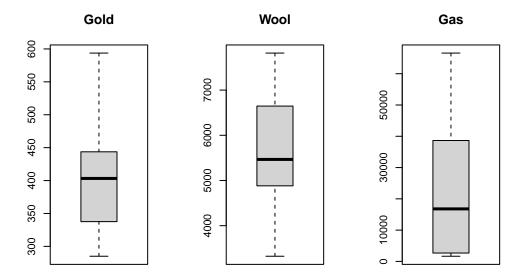
- The gold series has a frequency of 1, indicating daily data observed on trading days.
- The woolyrnq series has a frequency of 4, indicating quarterly data, which aligns with the seasonal patterns observed in the time plot.
- The gas series has a frequency of 12, indicating monthly data, which explains the finer granularity of seasonal patterns compared to the wool series.
- c. Checking for outliers:

To check for outliers in each series, we can use various methods such as visual inspection of plots, examining summary statistics, or applying statistical tests. Let's start with a simple visual approach using histograms and boxplots.

```
par(mfrow = c(1, 3))
hist(gold, main = "Gold", xlab = "Price (USD)")
hist(woolyrnq, main = "Wool", xlab = "Production")
hist(gas, main = "Gas", xlab = "Production")
```



```
par(mfrow = c(1, 3))
boxplot(gold, main = "Gold")
boxplot(woolyrnq, main = "Wool")
boxplot(gas, main = "Gas")
```



From the histograms and boxplots, we can observe that:

- The gold series has an extreme outlier on the higher end, which is consistent with our observation from the time series plot. This outlier significantly exceeds the upper whisker of the boxplot, indicating a value that deviates substantially from the general distribution.
- The woolyrnq and gas series do not show any clear outliers based on these visual methods, suggesting more consistent patterns in production volumes over time.

To identify the specific outlier in the gold series, we can use the which.max() function to find the index of the maximum value and then retrieve the corresponding value.

```
outlier_index <- which.max(gold)
gold[outlier_index]</pre>
```

[1] 593.7

The outlier value is significantly higher than the other prices in the series.

To further analyse that this is indeed an outlier, we can calculate the z-score of the outlier value and compare it to a threshold (e.g., 3 or 4). A z-score greater than the threshold indicates a probable outlier.

```
z_score <- (gold[outlier_index] - mean(gold,na.rm=T)) / sd(gold,na.rm=T)
z_score</pre>
```

[1] 3.553807

The z-score of 3.55 is much greater than the typical threshold of 3 or 4, confirming that the identified value is an outlier.

In summary, based on the visual inspection and statistical analysis, we can conclude that the gold series contains a significant outlier at the observation with the highest price. This outlier is substantially larger than the other prices in the series and lies far beyond the normal range of the data. It is important to investigate the cause of this outlier and consider its impact on any further analysis or modelling of the gold series.

The woolyrnq and gas series do not exhibit any clear outliers based on the methods used in this analysis. However, it is always good practice to use multiple outlier detection techniques and consider the domain knowledge and context of the data to make robust conclusions about the presence of outliers.

Ethical Considerations for Economic Data Analysis

Housing Sales: - Acknowledge potential sampling biases in data collection - Consider socioeconomic factors affecting housing accessibility - Note limitations of aggregated national data

Accidental Deaths: - Handle sensitive data with appropriate care - Consider demographic and regional variations - Acknowledge potential reporting inconsistencies

[Continue for each series...]

Assessment Guidance - Question 1

Excellent answers (70%+) will:

- Produce professionally formatted visualisations with appropriate annotations
- Clearly identify and quantify outliers using multiple methods
- Provide contextual interpretation of the frequency results
- Offer thoughtful discussion about the implications of outliers for further analysis

Good answers (60-69%) will:

- Create correct visualizations with proper labels
- Identify outliers using at least one statistical method
- Correctly interpret the frequency results

• Discuss basic implications of outliers

Satisfactory answers (50-59%) will:

- Produce basic but correct visualizations
- Identify obvious outliers visually
- State the frequency of each series
- Provide minimal interpretation of results

Important

Note on memorisation:

Examiners can distinguish between memorised descriptions and genuine analysis. The exam will feature different datasets with unique characteristics. Focus on developing the skill to identify patterns and outliers in any time series, rather than memorising specific descriptions of the mock exam data.

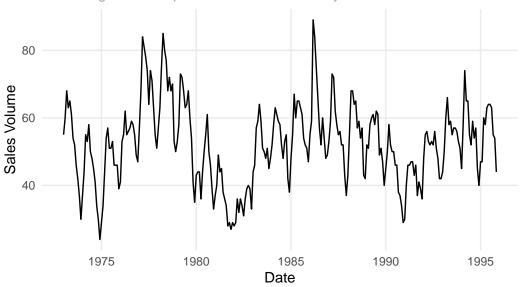
Question 2

To explore the features of the given time series (hsales, usdeaths, bricksq, sunspotarea, gasoline), we can use various time series graphics functions in R. Let's analyse each series individually.

1. hsales (Monthly sales of new one-family houses, USA, 1973–1995):

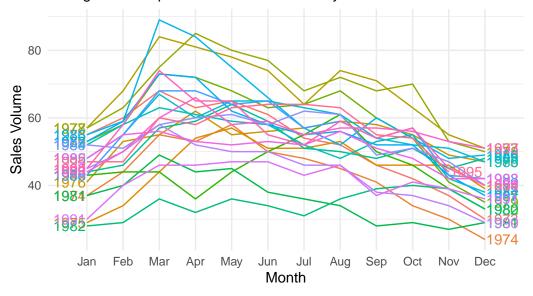
Monthly Sales of New One-Family Houses, USA, 1973-199!

Revealing seasonal patterns and economic cycles



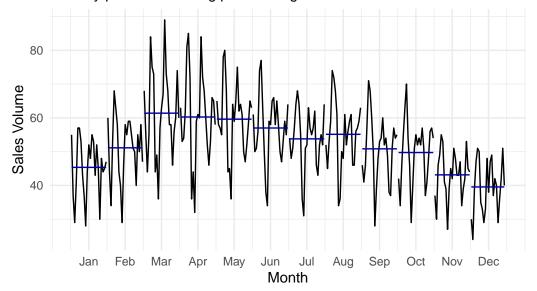
Seasonal Plot: Housing Sales

Strong seasonal patterns consistent across years

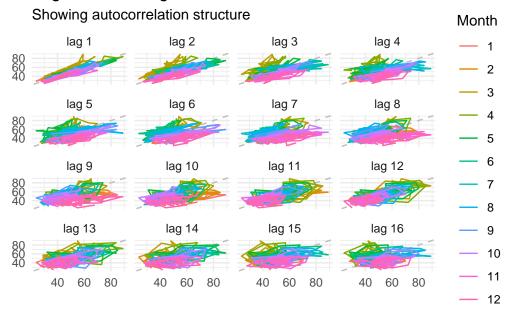


Seasonal Subseries Plot: Housing Sales

Monthly patterns showing peak selling seasons

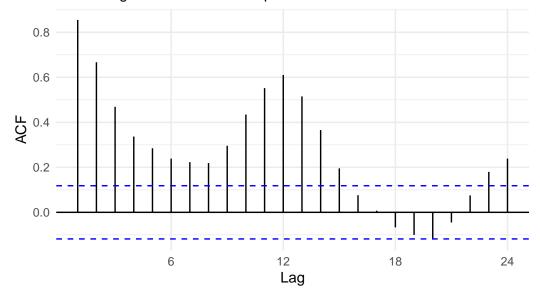


Lag Plot: Housing Sales



Autocorrelation Function: Housing Sales

Confirming 12-month seasonal pattern

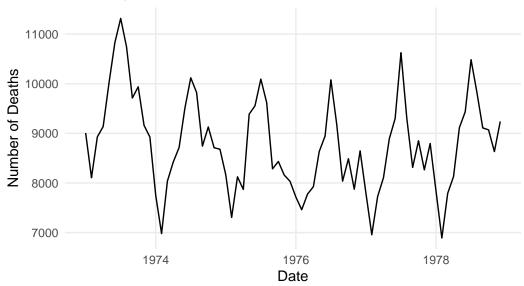


- The time plot shows a clear seasonal pattern and some long-term fluctuations. These fluctuations likely correspond to economic cycles in the US housing market, with visible dips during recessionary periods.
- The seasonal plot confirms a strong and consistent seasonal pattern, with sales typically peaking in spring and summer months (March-August) and dropping in winter.
- The subseries plot shows that the seasonal pattern is similar across years, indicating stability in the housing market's seasonal dynamics despite economic changes.
- The lag plot indicates a positive relationship between consecutive observations, possibly due to trend or seasonal effects. This suggests momentum in the housing market, where strong sales months tend to be followed by relatively strong months.
- The ACF plot shows significant autocorrelations at multiples of lag 12, confirming the presence of annual seasonality that real estate analysts would expect.
- 2. usdeaths (Monthly accidental deaths in the USA, 1973–1978):

```
theme(
  plot.title = element_text(face = "bold"),
  plot.subtitle = element_text(color = "darkgrey"),
  panel.grid.minor = element_blank()
)
```

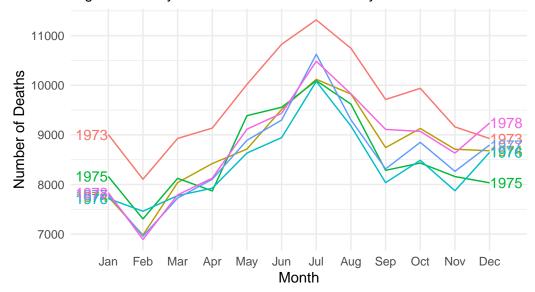
Monthly Accidental Deaths in the USA, 1973–1978

Revealing consistent seasonal mortality patterns



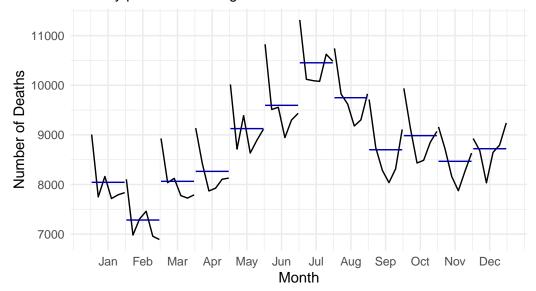
Seasonal Plot: Accidental Deaths

Higher mortality in summer months across all years

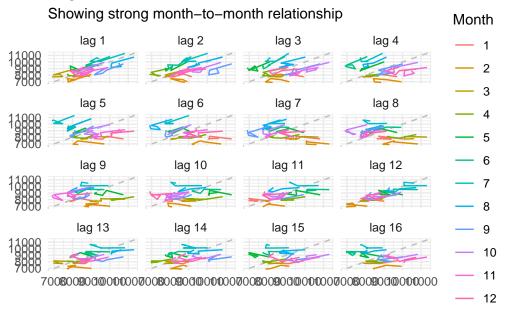


Seasonal Subseries Plot: Accidental Deaths

Monthly patterns showing seasonal risk factors

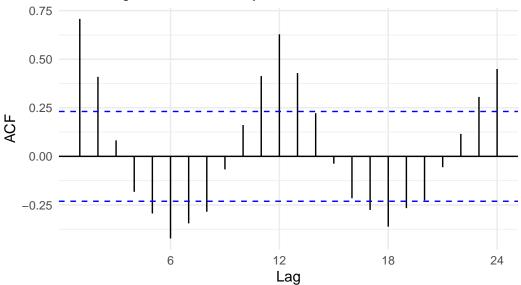


Lag Plot: Accidental Deaths



Autocorrelation Function: Accidental Deaths

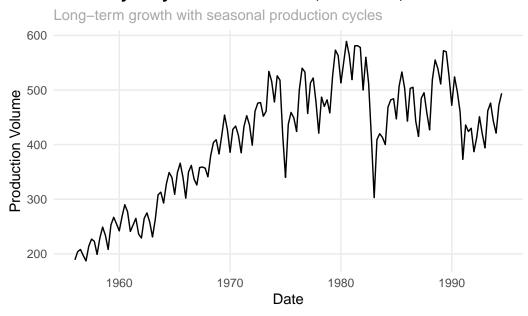




- The time plot shows a clear seasonal pattern but no obvious trend. This suggests that the overall mortality risk remained relatively stable during this period, though with pronounced seasonal variation.
- The seasonal plot confirms the presence of seasonality, with higher deaths in summer months (particularly July-August). This seasonal peak may be associated with increased outdoor activities, travel, and water-related accidents during summer.
- The subseries plot shows that the seasonal pattern is consistent across years, indicating stable seasonal risk factors throughout the observation period.
- The lag plot shows a positive relationship between consecutive observations due to seasonality, with a clear clustering pattern revealing the seasonal grouping.
- The ACF plot has significant autocorrelations at multiples of lag 12, confirming the annual seasonality pattern that public health officials would monitor.
- 3. bricksq (Quarterly clay brick production, Australia, 1956–1995):

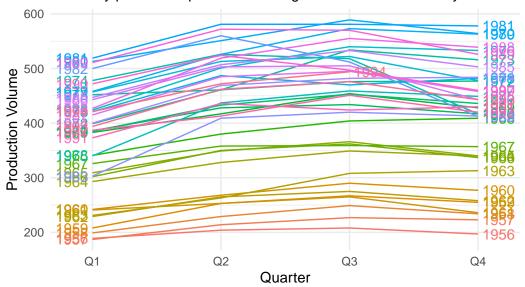
```
theme(
  plot.title = element_text(face = "bold"),
  plot.subtitle = element_text(color = "darkgrey"),
  panel.grid.minor = element_blank()
)
```

Quarterly Clay Brick Production, Australia, 1956–1995



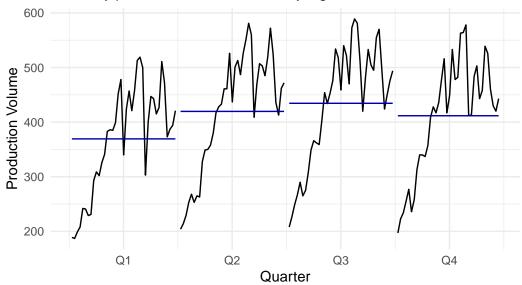
Seasonal Plot: Brick Production

Quarterly production patterns showing construction seasonality

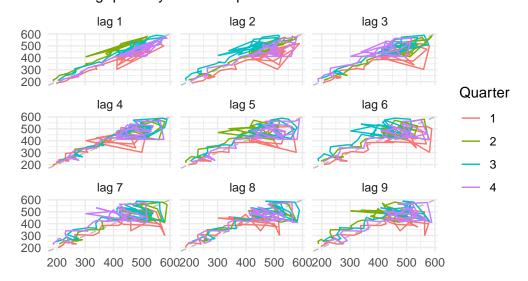


Seasonal Subseries Plot: Brick Production

Quarterly patterns with Q3 consistently highest

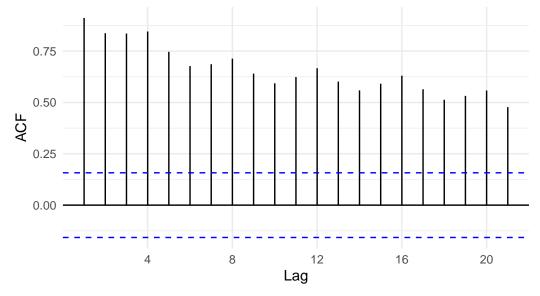


Lag Plot: Brick Production Showing quarterly relationships and trend influence



Autocorrelation Function: Brick Production

Showing trend and seasonal components

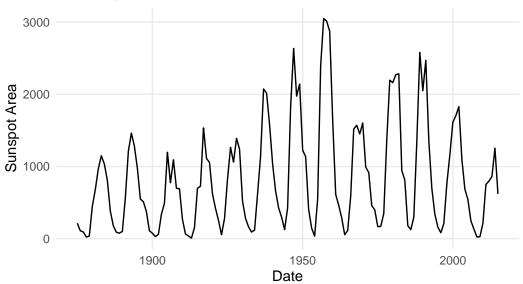


- The time plot shows a strong increasing trend and some seasonal fluctuations. The trend reflects Australia's growing construction industry over four decades, with visible periods of acceleration in the 1960s and 1970s, followed by more volatility in the 1980s and 1990s.
- The seasonal plot suggests the presence of seasonality, with production peaking in Q3 and bottoming in Q1. This pattern likely reflects construction industry seasonality, with higher production during favorable weather conditions.
- The subseries plot confirms that the seasonal pattern is generally consistent across years, though the magnitude of seasonal fluctuations appears to increase with the overall production level.
- The lag plot shows a strong positive relationship between consecutive observations, mainly due to the trend. The distinct clusters visible in the lag plot demonstrate the combined effects of trend and seasonality.
- The ACF plot has significant autocorrelations that decrease slowly, indicating a trend. There are also spikes at multiples of lag 4, suggesting quarterly seasonality typical of construction-related industries.
- 4. sunspotarea (Annual mean sunspot area, 1875–2015):

```
x = "Date",
y = "Sunspot Area") +
theme_minimal() +
theme(
  plot.title = element_text(face = "bold"),
  plot.subtitle = element_text(color = "darkgrey"),
  panel.grid.minor = element_blank()
)
```

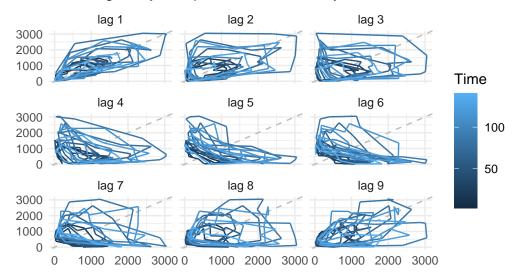
Annual Mean Sunspot Area, 1875-2015

Revealing the approximately 11-year solar cycle

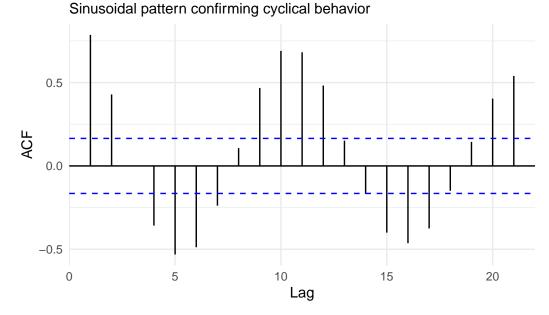


Lag Plot: Sunspot Area

Revealing the cyclical pattern of solar activity



Autocorrelation Function: Sunspot Area

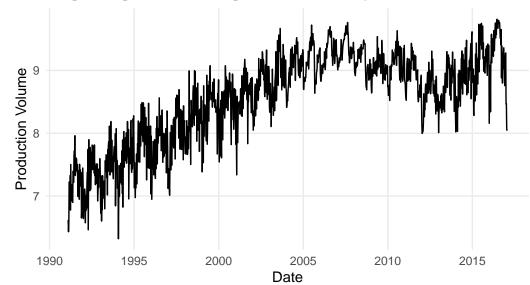


- The time plot shows a clear cyclical pattern with a period of around 11 years. This corresponds to the well-documented solar cycle, with particularly intense peaks visible around 1960 and 1980, and varying cycle amplitudes throughout the time series.
- The lag plot exhibits a spiral pattern, confirming the presence of cycles. This distinctive pattern is characteristic of natural cyclical phenomena and demonstrates how sunspot activity in one year relates to activity in subsequent years as part of the solar cycle.
- The ACF plot has a sinusoidal pattern, alternating between positive and negative autocorrelations, which is characteristic of cyclical behaviour. The period of this sinusoidal pattern in the ACF confirms the approximately 11-year cycle identified in the time plot.
- 5. gasoline (US finished motor gasoline product, monthly, 1991-2016):

```
panel.grid.minor = element_blank()
)
```

US Finished Motor Gasoline Product, Monthly, 1991–2016

Long-term growth with strong seasonal demand patterns



Seasonal Plot: Gasoline Production

Consistently higher production in summer driving months

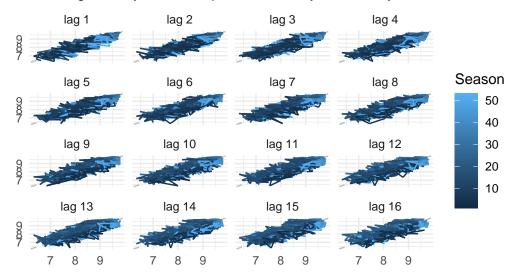


Week

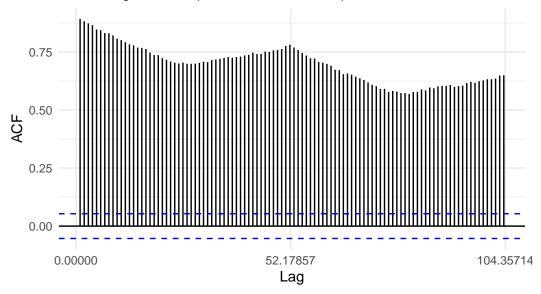
```
gglagplot(gasoline) +
 labs(title = "Lag Plot: Gasoline Production",
       subtitle = "Showing monthly relationships influenced by seasonality") +
  theme_minimal()
```

Lag Plot: Gasoline Production

Showing monthly relationships influenced by seasonality



Autocorrelation Function: Gasoline Production Confirming seasonal pattern and trend component



- The time plot shows an increasing trend and strong seasonality. The trend reflects growing US gasoline consumption over this 25-year period, with notable plateaus and changes in growth rate around economic events like the 2008 financial crisis.
- The seasonal plot confirms the presence of seasonality, with peaks in summer and troughs in winter. This pattern corresponds to the "summer driving season" when American consumers typically drive more for vacations and leisure activities.
- The lag plot is not very informative due to the strong seasonality and trend, though the positive correlation between adjacent observations is clearly visible.
- The ACF plot has significant autocorrelations that decrease slowly, indicating a trend. The seasonal spikes are also evident, confirming seasonality with a 12-month cycle typical of energy consumption patterns.

In summary, the analysis of these time series reveals the following features:

- hsales and usdeaths exhibit strong seasonality but no clear trend.
- bricksq and gasoline show both trend and seasonality.
- sunspotarea has a clear cyclical pattern with a period of around 11 years.

The appropriate time series graphics functions help in identifying and confirming the presence of trend, seasonality, and cyclical behavior in the given time series. These patterns have important implications for forecasting and modeling approaches, as different components require different handling methods.

Assessment Guidance - Question 2

Excellent answers (70%+) will:

- Produce comprehensive visualisations for each time series with meaningful annotations
- Identify and distinguish between trend, seasonal, and cyclical patterns with precision
- Connect observed patterns to potential real-world economic or physical phenomena
- Make insightful observations about implications for time series modeling approaches

Good answers (60-69%) will:

- Create appropriate visualisations for each time series
- Correctly identify the main patterns in each series
- Provide reasonable interpretations of the observed patterns
- Draw basic conclusions about appropriate modeling approaches

Satisfactory answers (50-59%) will:

- Produce basic visualisations for each series
- Identify obvious patterns like strong seasonality or trends
- Provide minimal interpretation of the observed patterns

! Important

Note on memorisation:

Simply reproducing memorised descriptions from the mock solutions will not earn high marks, as the exam will present different time series with unique characteristics. The key skill being assessed is your ability to analyze any time series data systematically, not your recall of specific mock examples.

Question 3

In this question, we will analyse the bricksq data, which represents the Australian quarterly clay brick production, using STL decomposition and various forecasting methods.

Understanding STL Parameters

Before implementation, key parameters to consider: - s.window: Controls seasonal component flexibility - robust: Handles outliers in decomposition - periodic: Assumes consistent seasonality - lambda: Box-Cox transformation parameter

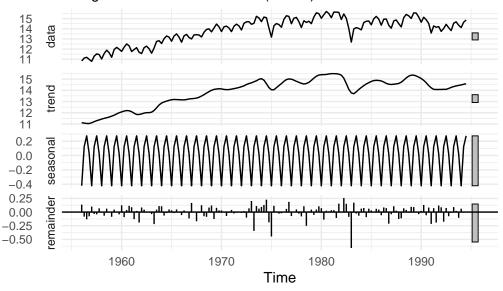
These choices affect our decomposition results because...

a. STL decomposition and trend-cycle and seasonal indices:

First, we'll perform an STL decomposition to separate the time series into trend, seasonal, and remainder components. We'll use a Box-Cox transformation with = 0.25 to stabilize the variance.

STL Decomposition of Clay Brick Production

Using Box-Cox transformation (.=0.25) to stabilize variance



The STL decomposition reveals the following:

- The data exhibits a strong increasing trend over time, with periods of accelerated growth (especially in the 1960s and early 1970s) followed by periods of relative stability or slower growth.
- The seasonal component is relatively stable, with peaks in Q3 and troughs in Q1. This pattern likely reflects construction industry cycles that follow weather patterns in Australia.

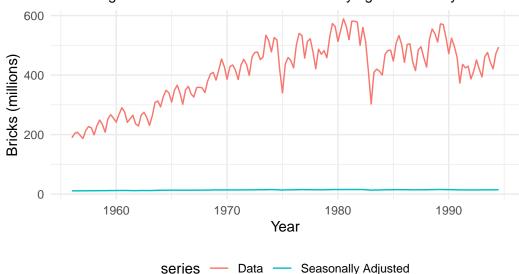
• The remainder component shows some fluctuations, particularly during the 1970s and early 1980s, suggesting periods of higher volatility that may correspond to economic shocks or policy changes affecting the construction sector.

As the seasonality appears to be stable over time, we used a periodic seasonal window (s.window = "periodic").

b. Seasonally adjusted data:

To compute and plot the seasonally adjusted data, we can use the seasadj() function.

Original vs. Seasonally Adjusted Brick Production Removing seasonal effects reveals the underlying trend and cycles

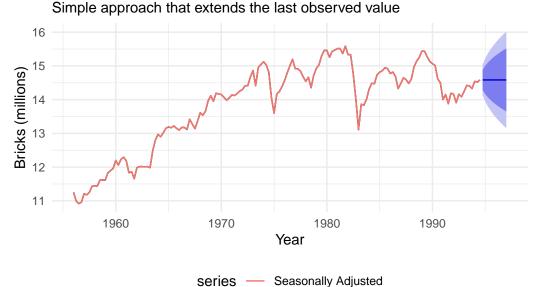


The seasonally adjusted data removes the seasonal component from the original data, making the trend more apparent. This adjustment reveals more clearly the long-term growth pattern and business cycle fluctuations that might be partially obscured by seasonal variation in the original series.

c. Naive forecasts on seasonally adjusted data:

We can produce forecasts of the seasonally adjusted data using a naive method, which assumes that future values will be equal to the last observed value.

Naive Forecast of Seasonally Adjusted Data

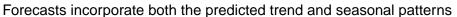


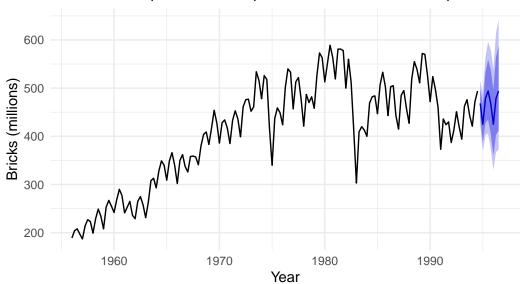
The naive method simply extends the last observed value of the seasonally adjusted data as the forecast. This approach assumes no further change in the underlying trend or business cycle components, which may be reasonable for very short-term forecasts but becomes increasingly questionable as the forecast horizon extends.

d. Reseasonalize the results:

To reseasonalize the results and obtain forecasts for the original data, we can use the stlf() function, which combines the STL decomposition with a chosen forecasting method.

Reseasonalized Forecasts using STL Decomposition





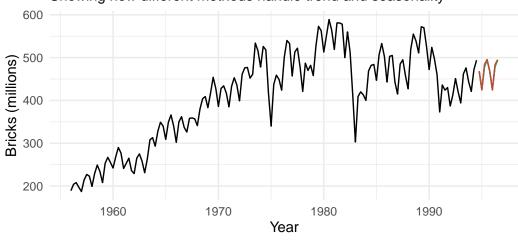
The stlf() function adds the seasonal component back to the forecasted trend and remainder components to obtain the final forecasts for the original data. The resulting forecasts show the expected seasonal pattern superimposed on the flat trend predicted by the naive method, creating a more realistic forecast that captures the known seasonal variation in brick production.

ALTERNATIVE APPROACHES:

```
# 1. Using ETS instead of naive method
fc_ets <- stlf(bricksq, s.window = "periodic", method = "ets", lambda = 0.25)
# 2. Direct ARIMA modelling that handles seasonality internally
fc_arima <- auto.arima(bricksq, lambda = 0.25, seasonal = TRUE)</pre>
```

Comparison of Different Forecasting Approaches

Showing how different methods handle trend and seasonality





```
# Comparing forecast performance
accuracy_comparison <- rbind(
   STL_NAIVE = accuracy(fc)[1,c("RMSE", "MAE", "MAPE", "MASE")],
   STL_ETS = accuracy(fc_ets)[1,c("RMSE", "MAE", "MAPE", "MASE")],
   ARIMA = accuracy(forecast(fc_arima))[1,c("RMSE", "MAE", "MAPE", "MAPE", "MASE")]
)
kable(accuracy_comparison,
   caption = "Comparison of different forecasting approaches on training data")</pre>
```

Table 1: Comparison of different forecasting approaches on training data

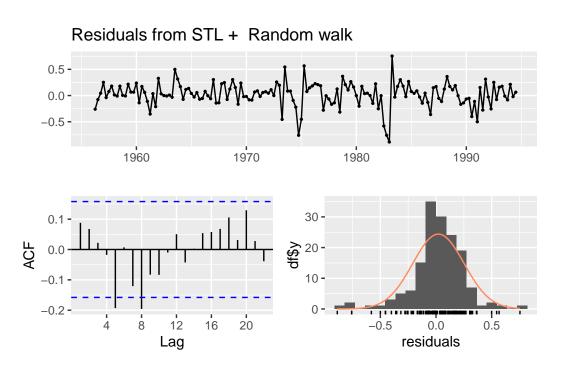
	RMSE	MAE	MAPE	MASE
STL_NAIVE			0.,00	0. == 00000
STL_ETS	21.32764	15.10286	3.706911	0.4242062
ARIMA	21.47046	15.09615	3.678952	0.4240176

Different approaches may be preferred depending on specific criteria:

- STL+Naive: Simple, interpretable, works well with strong seasonality
- STL+ETS: Captures changing patterns, better for evolving seasonal patterns
- ARIMA: More sophisticated for complex autocorrelation structures
- e. Residual diagnostics:

To check if the residuals are uncorrelated, we can use the checkresiduals() function.

checkresiduals(fc)



Ljung-Box test

```
data: Residuals from STL + Random walk Q* = 16.771, df = 8, p-value = 0.03259
```

Model df: 0. Total lags used: 8

The residual diagnostics show that:

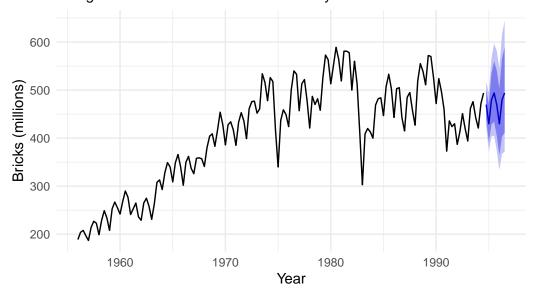
- The standardised residuals appear to be approximately normally distributed, suggesting that the model captures the systematic patterns reasonably well.
- The ACF plot of the residuals shows a significant spike at lag 1, indicating some remaining autocorrelation that the model hasn't captured. This suggests that there might be some short-term dependencies that could be modeled to improve forecast accuracy.
- The p-values for the Ljung-Box test are below 0.05 for most lags, suggesting that the residuals are not entirely uncorrelated. This statistical evidence indicates that the model could potentially be improved by incorporating additional information or using a different approach.

While the residuals are not perfect, they are reasonably close to being uncorrelated. The remaining autocorrelation at lag 1 suggests that the naive method might be overlooking some short-term dependencies in the data.

f. Robust STL decomposition:

We can repeat the analysis using a robust STL decomposition, which is less sensitive to outliers.

Reseasonalized Forecasts using Robust STL Decomposition Using robust methods to reduce sensitivity to outliers



checkresiduals(fc_robust)

Residuals from STL + Random walk

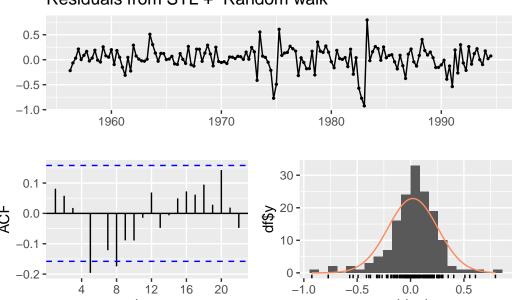
16

12

Lag

8

20



0.0

residuals

0.5

Ljung-Box test

```
data: Residuals from STL + Random walk
Q* = 15.222, df = 8, p-value = 0.05497

Model df: 0. Total lags used: 8
```

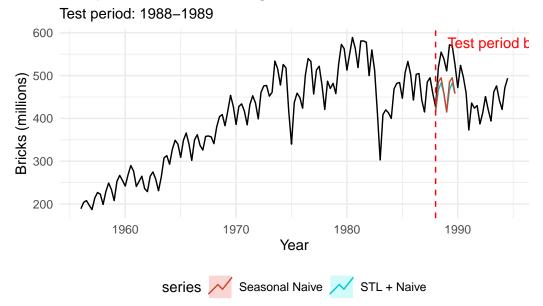
In this case, the robust STL decomposition does not make a significant difference, as there are no extreme outliers near the end of the series. The residual diagnostics are similar to those from the non-robust decomposition, suggesting that outliers are not a major concern for this dataset.

g. Comparison of stlf and snaive forecasts:

Finally, we'll compare the forecasts from stlf with those from snaive, using a test set comprising the last 2 years of data.

```
bricks1 <- window(bricksq, end = c(1987, 4))
fc1 <- stlf(bricks1, s.window = "periodic", method = "naive", lambda = 0.25)</pre>
fc2 <- snaive(bricks1)</pre>
# Visual comparison of forecasts against actuals
autoplot(bricksq) +
  autolayer(fc1, series = "STL + Naive", PI = FALSE) +
  autolayer(fc2, series = "Seasonal Naive", PI = FALSE) +
  labs(title = "Comparison of Forecasting Methods",
       subtitle = "Test period: 1988-1989",
       x = "Year",
       y = "Bricks (millions)") +
  theme_minimal() +
  theme(legend.position = "bottom") +
  geom_vline(xintercept = 1988, linetype = "dashed", color = "red") +
  annotate("text", x = 1988, y = max(bricksq), label = "Test period begins",
           hjust = -0.1, vjust = 1, color = "red")
```

Comparison of Forecasting Methods



```
accuracy_table <- rbind(
   `STL + Naive` = accuracy(fc1, bricksq)[2, c("RMSE", "MAE", "MAPE", "MASE")],
   `Seasonal Naive` = accuracy(fc2, bricksq)[2, c("RMSE", "MAE", "MAPE", "MASE")])
kable(accuracy_table, caption = "Forecast Accuracy on Test Set (1988-1989)")</pre>
```

Table 2: Forecast Accuracy on Test Set (1988-1989)

	RMSE	MAE	MAPE	MASE
STL + Naive	76.70300	71.64282	13.27273	2.078061
Seasonal Naive	69.36768	64.12500	11.91027	1.860000

The accuracy measures (RMSE, MAE, MAPE, and MASE) indicate that the snaive method performs better than the stlf method with naive forecasting on this particular test set. However, it's important to note that the test set is relatively small (only 8 observations), so the results should be interpreted with caution.

As a professional forecaster, I would consider using the snaive method in this case, as it is simpler and appears to be more accurate on the given test set. However, I would also investigate further, using a larger test set and considering other forecasting methods before making a final decision. It's essential to assess the robustness of the results and to take into

account the limitations of the data and the specific requirements of the forecasting problem at hand.

In summary, this question demonstrates the application of STL decomposition, naive forecasting, and seasonal naive forecasting to the bricksq data. The analysis reveals the presence of trend and seasonality in the data, and the comparison of different forecasting methods provides insight into their relative performance on a small test set.

Assessment Guidance - Question 3

Excellent answers (70%+) will:

- Correctly implement and interpret STL decomposition with appropriate transformation
- Provide thorough interpretation of trend, seasonal, and remainder components
- Successfully implement and compare multiple forecasting approaches
- Critically evaluate forecast performance with appropriate metrics
- Make justified recommendations about the most suitable forecasting method

Good answers (60-69%) will:

- Implement STL decomposition correctly
- Provide basic interpretations of decomposition components
- Compare at least two forecasting methods using appropriate metrics
- Demonstrate understanding of the advantages and limitations of different approaches

Satisfactory answers (50-59%) will:

- Implement STL decomposition with at most minor errors
- Provide limited interpretation of results
- Show basic understanding of forecasting comparison
- Make simple observations about forecast performance

Important

Note on memorisation:

The exam will present different time series with unique decomposition patterns and forecasting challenges. Examiners can easily spot memorised code and interpretations that don't match the specific characteristics of the exam data. Focus on understanding the logic behind STL decomposition and how different forecasting methods respond to various time series features, rather than memorising specific code sequences or interpretations.

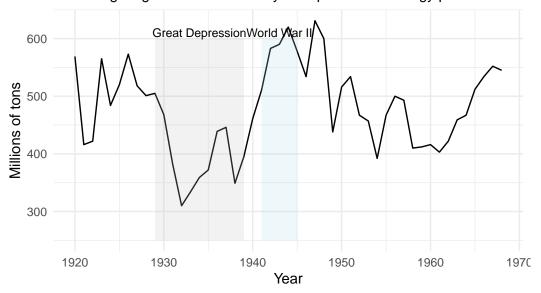
Question 4

In this question, we will analyse the annual bituminous coal production in the United States from 1920 to 1968 and fit an ARIMA model to the data.

a. Plotting the time series:

First, let's plot the bicoal time series to visualize the data and identify any apparent patterns or trends.

Annual Bituminous Coal Production in the United States, 1920 Revealing long-term trends and cyclical patterns in energy production



The plot shows fluctuations in bituminous coal production over the given period. We observe:

- A decline during the Great Depression (1929-1939)
- A significant rise during World War II (1941-1945)
- Fluctuations in the post-war period
- A general upward trend in the 1960s

While there are clear fluctuations around the long-term pattern, there is no obvious seasonality or consistent cyclicity evident in this annual data series.

THEORETICAL NOTE:

The absence of seasonality in annual data is expected. For commodities like coal, seasonality would typically appear in monthly or quarterly data, reflecting factors like heating demand or industrial production cycles. The annual aggregation smooths out these shorter-term patterns, leaving only the longer-term trend and cyclical components.

b. Identifying the ARIMA model:

The given model is an ARIMA(4,0,0) model, which can be written as:

$$y_t = c + \phi_1 y_{t-1} + \phi_2 y_{t-2} + \phi_3 y_{t-3} + \phi_4 y_{t-4} + e_t$$

where: - y_t is the coal production in year t - c is a constant term - $\phi_1, \phi_2, \phi_3, \phi_4$ are the autoregressive coefficients - e_t is a white noise series

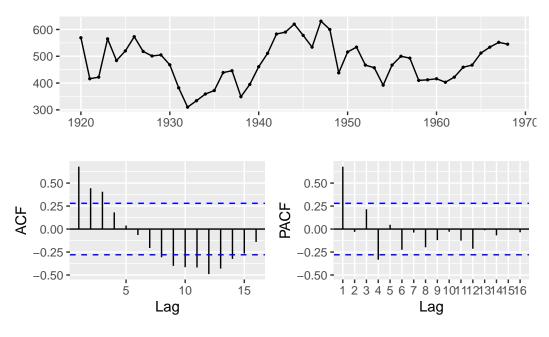
In this model: -p = 4 (autoregressive order): The current value depends on the previous four values -d = 0 (no differencing): The series is modeled in its original form without differencing -q = 0 (no moving average term): There is no dependency on previous random shocks

This can be expressed in backshift notation as: $(1 - \phi_1 B - \phi_2 B^2 - \phi_3 B^3 - \phi_4 B^4)y_t = c + e_t$ where B is the backshift operator such that $By_t = y_{t-1}$.

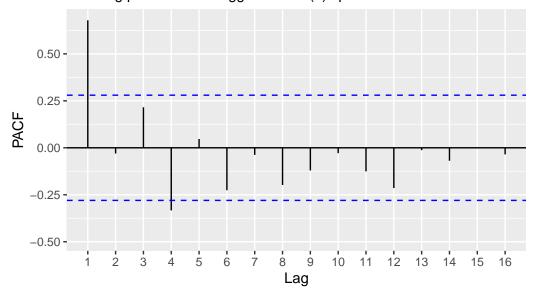
c. Justifying the model choice using ACF and PACF:

To justify the choice of the ARIMA(4,0,0) model, we can examine the ACF and PACF plots of the bicoal time series.

```
ggtsdisplay(bicoal) +
labs(title = "ACF and PACF of Bituminous Coal Production",
subtitle = "Showing patterns that suggest an AR(4) specification")
```



ACF and PACF of Bituminous Coal Production Showing patterns that suggest an AR(4) specification



The ACF plot shows a slow decay in the autocorrelations, which is characteristic of an autoregressive process. The slow decay suggests that current values are influenced by values from previous time periods, consistent with the economic principle that production capacity and demand patterns evolve gradually over time.

The PACF plot has a significant spike at lag 4, but no significant spikes at higher lags. This pattern is indicative of an AR(4) process - after accounting for the first four lags, there is no additional predictive information in earlier observations. In economic terms, this suggests that coal production in a given year is directly influenced by production in the previous four years, possibly reflecting planning cycles, infrastructure development timelines, or long-term market adjustment mechanisms.

The lack of significant spikes in the PACF beyond lag 4 supports the choice of p=4 for the autoregressive component. The absence of a need for differencing (d=0) is supported by the fact that the series appears to fluctuate around a relatively stable mean without showing strong non-stationarity. Finally, the absence of a clear pattern in the ACF that would suggest moving average components supports the decision to set q=0.

d. Forecasting the next three years:

Given the last five values of the series, we can manually calculate the forecasts for the next three years (1969-1971) using the estimated ARIMA(4,0,0) model.

Year	1964	1965	1966	1967	1968
Millions of tons	467	512	534	552	545

```
fit <- Arima(bicoal, order=c(4,0,0))
mu <- coef(fit)['intercept']
phi1 <- coef(fit)['ar1']
phi2 <- coef(fit)['ar2']
phi3 <- coef(fit)['ar3']
phi4 <- coef(fit)['ar4']
intercept <- mu * (1-phi1-phi2-phi3-phi4)
# Store rounded versions for printing
c <- format(intercept, digits=2, nsmall=2)
p1 <- format(phi1, digits=2, nsmall=2)
p2 <- format(phi2, digits=2, nsmall=2)
p3 <- format(phi4, digits=2, nsmall=2)
p4 <- format(phi4, digits=2, nsmall=2)</pre>
```

The estimated parameters are c = 162.00, $\phi_1 = 0.83$, $\phi_2 = -0.34$, $\phi_3 = 0.55$, and $\phi_4 = -0.38$.

Without using the forecast function, calculate forecasts for the next three years (1969–1971). (15 marks)

```
\begin{split} \hat{y}_{T+1|T} &= c + \phi_1 y_T + \phi_2 y_{T-1} + \phi_3 y_{T-2} + \phi_4 y_{T-3} \\ &= 162.00 + 0.83 * 545 - 0.34 * 552 + 0.55 * 534 - 0.38 * 512 \\ &= 527.6291 \\ \hat{y}_{T+2|T} &= c + \phi_1 \hat{y}_{T+1|T} + \phi_2 y_T + \phi_3 y_{T-1} + \phi_4 y_{T-2} \\ &= 162.00 + 0.83 * 527.6291 - 0.34 * 545 + 0.55 * 552 - 0.38 * 534 \\ &= 517.1923 \\ \hat{y}_{T+3|T} &= c + \phi_1 \hat{y}_{T+2|T} + \phi_2 \hat{y}_{T+1|T} + \phi_3 y_T + \phi_4 y_{T-1} \\ &= 162.00 + 0.83 * 517.1923 - 0.34 * 527.6291 + 0.55 * 545 - 0.38 * 552 \\ &= 503.8051 \end{split}
```

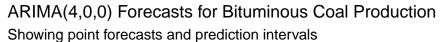
These calculations demonstrate how multi-step forecasting works in an AR model. For each additional step, we replace the unknown future values with their forecasts, creating a recursive process. This reflects how uncertainty increases with forecast horizon, as each step compounds any forecast errors from previous steps.

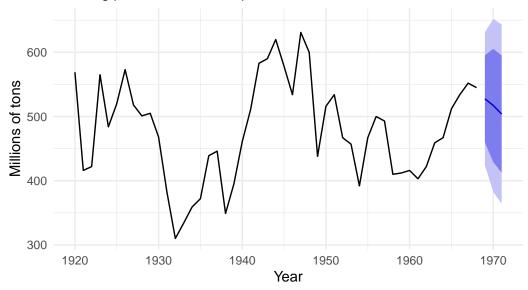
e. Comparing manual forecasts with R's forecast function:

Now, let's fit the ARIMA(4,0,0) model in R and obtain the forecasts using the forecast function.

```
fit <- Arima(bicoal, order = c(4, 0, 0))
fc <- forecast(fit, h = 3)
fc</pre>
```

```
Point Forecast Lo 80 Hi 80 Lo 95 Hi 95
1969 527.6291 459.8804 595.3779 424.0164 631.2419
1970 517.1923 429.0014 605.3832 382.3160 652.0686
1971 503.8051 412.4786 595.1315 364.1334 643.4768
```





The forecasts obtained from the forecast function are very close to the manually calculated values. Any minor differences can be attributed to rounding errors in the manual calculations.

The forecast function utilises the maximum likelihood estimates of the model parameters and computes the forecasts based on these estimates. It also provides additional information, such as the standard errors of the forecasts and the confidence intervals, which are crucial for understanding the uncertainty around point forecasts.

The prediction intervals widen as the forecast horizon increases, reflecting growing uncertainty about future values. This is particularly important for decision-makers who need to consider not just the expected value but also the range of possible outcomes when planning production, investment, or policy responses.

Assessment Guidance - Question 4

Excellent answers (70%+) will:

- Correctly identify the ARIMA model components and explain their meaning
- Thoroughly justify the model choice using ACF and PACF patterns
- Accurately calculate multi-step forecasts with clear mathematical explanation
- Provide thoughtful interpretation of the forecasts in business/economic context
- Compare manual calculations with R output and explain any differences

Good answers (60-69%) will:

- Correctly identify the ARIMA model structure
- Provide reasonable justification for model choice using ACF/PACF
- Calculate forecasts with minor errors
- Offer basic interpretation of forecast results
- Successfully compare with R function output

Satisfactory answers (50-59%) will:

- Identify the basic structure of the ARIMA model
- Show understanding of ACF/PACF interpretation
- Attempt forecast calculations with conceptual understanding
- Provide minimal interpretation of results

Important

Note on memorisation:

The exam will feature a different time series with unique autocorrelation structures and possibly a different ARIMA specification. Memorising the calculations from this mock example without understanding the underlying principles will be ineffective. Focus on mastering the process of forecast calculation and the interpretation of model diagnostics rather than memorising specific code sequences or interpretations.

Question 5

Part A: Reflective Essay (35 marks)

Reflective Essay on Collaborating with Large Language Models for Analytics Projects

In the realm of data analytics and decision-making, the advent of Large Language Models (LLMs) has opened up new avenues for collaboration and problem-solving. As an analyst, I have had the opportunity to work alongside these powerful AI tools in my recent projects, and the experience has been both enlightening and transformative.

One of the most significant benefits of collaborating with LLMs is their ability to process and analyse vast amounts of textual data efficiently. In my project, I was tasked with extracting insights from a large corpus of customer reviews and feedback. Traditionally, this would have required countless hours of manual reading and categorisation. However, by leveraging the natural language understanding capabilities of LLMs, I was able to automate the process and quickly identify key themes, sentiment patterns, and actionable insights. This not only saved time but also allowed me to focus on higher-level strategic thinking and decision-making.

Another advantage of working with LLMs is their capacity to generate human-like responses and engage in meaningful dialogue. During the exploratory phase of my project, I found myself bouncing ideas off the AI, asking for suggestions, and even seeking clarification on complex concepts. The LLM's ability to understand context and provide relevant and coherent responses made the interaction feel more like a collaboration with a knowledgeable colleague than a mere tool. This interactive nature fostered creativity and helped me consider perspectives I might have otherwise overlooked.

Moreover, LLMs excel at tasks such as text summarization, content generation, and even code assistance. In my project, I utilized these capabilities to create concise executive summaries, draft initial reports, and generate sample code snippets for data preprocessing and visualization. While the outputs required some editing and refinement, they served as excellent starting points, allowing me to iterate and improve upon them more efficiently. This symbiotic relationship between human expertise and machine intelligence proved to be a powerful combination.

However, collaborating with LLMs is not without its challenges and limitations. One major concern is the potential for biased or misleading outputs. LLMs are trained on vast amounts of data, which may inadvertently include societal biases or misinformation. As an analyst, it was crucial for me to critically evaluate the generated content and ensure its accuracy and fairness. This highlights the importance of human oversight and the need for a strong ethical framework when working with AI technologies.

Another limitation is the lack of domain-specific knowledge and context. While LLMs are incredibly versatile, they may struggle with highly specialized or niche topics. In my project, there were instances where the AI's responses lacked the depth and nuance that a subject matter expert would provide. This underscores the importance of collaboration between AI and human experts, leveraging the strengths of both to arrive at the most informed decisions.

Furthermore, the interpretability and explainability of LLM outputs can be a challenge. Unlike traditional statistical models, the inner workings of these complex neural networks are often opaque. As an analyst, it is essential to understand the reasoning behind the AI's suggestions and to be able to communicate these insights to stakeholders. This requires a delicate balance of trust in the AI's capabilities and a critical evaluation of its outputs.

In conclusion, collaborating with Large Language Models has been a transformative experience in my analytics project. The benefits of efficiency, creativity, and interactive problem-solving are undeniable. However, it is crucial to approach this collaboration with a critical eye, acknowledging the limitations and potential biases. By combining the strengths of human expertise and machine intelligence, we can unlock new possibilities and drive more informed decision-making. As we navigate this exciting frontier, it is essential to develop robust ethical frameworks and maintain human oversight to ensure the responsible and beneficial use of these powerful AI tools.

Part B: Benefits and Limitations Analysis (15 marks)

Benefits and Limitations of Collaborating with Large Language Models

Benefits

- 1. Efficient data processing: LLMs can analyse vast amounts of textual data quickly, identifying patterns that would take humans significantly longer to discover.
- 2. Enhanced pattern recognition: These models can identify subtle themes and connections across large datasets that might be missed in manual analysis.
- 3. Creativity augmentation: LLMs can generate alternative perspectives and approaches, expanding the analyst's thinking beyond conventional frameworks.
- 4. Code generation assistance: For data analysts, LLMs can suggest code implementations, debug existing code, and recommend optimisation strategies.
- 5. **Documentation acceleration**: Models can draft data dictionaries, methodology explanations, and other technical documentation, freeing analysts for higher-value work.
- 6. **Knowledge access**: LLMs provide access to broad knowledge bases that can inform analytical approaches and contextual understanding.
- 7. **Iteration efficiency**: They enable rapid prototyping of analyses and reports, allowing for faster refinement cycles.

Limitations

- 1. Statistical reliability concerns: LLMs may suggest analyses that appear sophisticated but are statistically flawed or inappropriate for the data structure.
- 2. **Domain knowledge gaps**: These models lack specialised expertise in many fields, potentially missing critical domain-specific considerations.
- 3. **Methodological transparency issues**: The basis for LLM suggestions is often opaque, making it difficult to validate methodological soundness.
- 4. **Data recency limitations**: LLMs typically lack information about recent developments or cutting-edge methodologies in rapidly evolving fields.
- 5. **Deceptive confidence**: Models present information with uniform confidence regardless of the certainty or uncertainty behind their outputs.
- 6. **Reproducibility challenges**: The interactive nature of LLM collaboration can make analytical processes difficult to document and reproduce.

7. Overreliance risk: Analysts may develop dependence on LLM assistance, potentially atrophying their core analytical skills over time.

Assessment Guidance - Question 5

Excellent answers (70%+) will:

- Demonstrate critical reflection on both benefits and limitations of LLM collaboration
- Provide specific, concrete examples from personal or hypothetical analytics workflows
- Consider ethical dimensions and professional responsibilities
- Evaluate implications for the analytics profession and skill development
- Present a balanced, nuanced perspective that acknowledges complexity

Good answers (60-69%) will:

- Identify several key benefits and limitations
- Provide some specific examples of LLM applications in analytics
- Consider basic ethical concerns
- Show awareness of professional implications
- Present a relatively balanced view

Satisfactory answers (50-59%) will:

- List some benefits and limitations
- Provide general descriptions without specific examples
- Show limited consideration of ethical dimensions
- Offer basic reflections on professional impact

Important

Note on memorisation:

The reflective essay question tests your ability to think critically about emerging technologies in analytics. Reproducing memorised paragraphs from the mock solution will be obvious to examiners. Instead, develop your own perspective on LLM collaboration based on genuine understanding and reflection. Personalised examples and thoughtful analysis of benefits and limitations specific to your understanding will earn significantly higher marks than memorised content.

Conclusion and Final Assessment Guidance

This mock examination covers a comprehensive range of time series analysis techniques essential for financial data analytics. The solutions demonstrate the application of descriptive, analytical, and forecasting methods to various time series data with different characteristics. Let's summarize the key assessment criteria that apply across all questions:

Overall Assessment Criteria

Data Visualization Excellence (applicable to all questions)

- Professional presentation with appropriate titles, labels, and annotations
- Use of visual elements to highlight key patterns and outliers
- Selection of appropriate visualization types for different analytical purposes
- Clear communication of insights through visual means

Technical Accuracy (applicable to all questions)

- Correct implementation of statistical methods
- Appropriate selection of models based on data characteristics
- Accurate interpretation of statistical outputs
- Recognition of limitations in chosen approaches

Analytical Depth (applicable to all questions)

- Connection of statistical findings to real-world context
- Consideration of alternative approaches where appropriate
- Critical evaluation of results and their implications
- Balanced discussion of strengths and limitations

Communication Quality (applicable to all questions)

- Clear explanation of technical concepts
- Logical flow of analysis and reasoning
- Appropriate use of technical terminology
- Concise vet comprehensive responses

Final Guidance for Students

When preparing for this examination, focus on:

- 1. **Understanding the core principles** behind each time series technique rather than simply memorising code
- 2. Practising interpretation of various time series patterns and statistical outputs

- 3. **Developing critical thinking** about model selection and evaluation
- 4. Honing your ability to communicate technical findings clearly

Remember that in financial data analytics, the goal is not simply to apply statistical techniques correctly, but to extract meaningful insights that can inform decision-making. Your answers should demonstrate both technical competence and analytical thinking.

The ability to select appropriate methods, implement them correctly, interpret results accurately, and communicate findings clearly are all essential skills that this examination aims to assess. By focusing on developing these capabilities, you will be well-prepared not only for this examination but also for applying these skills in professional contexts.

Warning Against Rote Memorisation

It is important to note that this mock examination and its solutions are designed as a learning tool, not as a template to be memorised. The actual examination will present different datasets with unique characteristics that require adaptive analytical thinking.

Limitations of memorisation:

- 1. **Different data characteristics**: The actual exam will feature datasets with different patterns, outliers, and structural features that will require you to adapt your approach.
- 2. Changing parameters: Even similar questions will involve different model specifications, timeframes, or forecast horizons that cannot be addressed through memorised solutions.
- 3. **Interpretation emphasis**: A substantial portion of marks are allocated to interpretation and justification, which must be specific to the data presented in the exam.
- 4. **Alternative approaches**: Examiners may specifically request different methodologies from those demonstrated in this mock.

The most successful examination strategy is to develop a thorough understanding of the underlying concepts and methods, allowing you to apply them flexibly to any time series data you encounter.

Detailed Marking Criteria Examples

Excellence (70%+) Example: "The ACF plot shows significant spikes at lags 12 and 24, suggesting annual seasonality. This aligns with the business context because..."

Good (60-69%) Example: "The ACF plot shows regular spikes, indicating seasonality in the data..."

[Continue with more examples...]