

# Cross Validation

- How to find appropriate  $k$  value for  $k$ -NNC.
- Some improvements to  $k$ -NNC

# Cross Validation

- *r-fold cross validation:*
  1. Partition the training set into  $r$  blocks. Let these are  $D_1, D_2, \dots, D_r$ .
  2. For  $i = 1$  to  $r$  do
    - I. Consider  $D - D_i$  as the training set and  $D_i$  as the validation set.
    - II. For a range of  $k$  values (say from 1 to  $m$ ) find the error rates on the validation set.
    - III. Let these error rates are  $e_{i1}, e_{i2}, \dots, e_{im}$
  3. Take  $e_i = \text{mean of } \{e_{i1}, e_{i2}, \dots, e_{im}\}$ , for  $i = 1$  to  $m$ .
  4.  $k \text{ value} = \underset{j}{\operatorname{argmin}} \{e_1, e_2, \dots, e_j, \dots, e_m\}$

# Cross validation

- One should not use *the test set* to decide the value of  $k$ .
- Test set should be used only after fixing  $k$ , to get the final *error-rate* for the classifier.
- Cross validation is only to fix the value of parameters like  $k$ . So the error rates on validation sets should be called *validation error rates*.

# k-NNC

- Since k-NNC is a simple classifier, it attracted many researchers.
- First k-NNC is invented in 1952. Since then people tried to improve it in various ways.
- k-NNC is often not seen as a related classifier to Bayes classifier. This is because, distributions are not explicitly calculated.

# An improvement of k-NNC

- k-NNC gives equal importance to the first NN and to the last NN.
- *S.A. Dudani (1976)* has given a method where we give *weights* to the NNs.
- Voting is done according to these weights.
- Let the distances (with given pattern) of k NNs be an ordered set =  $\{d_1, d_2, \dots, d_k\}$
- For  $i^{\text{th}}$  NN the weight is,  $w_i = (d_k - d_i) / (d_k - d_1)$
- Use these weights as vote values and classify accordingly.
- This is called *modified k-NNC* or *weighted k-NNC*, and is found to improve the performance in almost all cases.

# Bootstrapping

- Another promising improvement is to regenerate the training set, so that the training patterns belonging to different classes are separated well.
- *Hamamoto(1997)* proposed the following:
- For each training pattern  $y$  do:
  1. Find  $r$  NNs of  $y$  in the training set that belongs to the same class as  $y$ .
  2. Find the mean of these  $r$  NNs. Let this is  $y_r$
  3. Replace  $y$  by  $y_r$

# Other improvements

- Let  $n$  be the number of training patterns.
- Let  $k$  be a small constant when compared with  $n$
- The time and space complexity of k-NNC are both equal to  $O(n)$ .
- To reduce the computational burden of k-NNC is another important direction of research.
  - Prototype selection.
  - Not all training patterns are important for k-NNC, so remove those which are unimportant.

# Condensed k-NNC

- *Cover and Hart (1967)* gave the following procedure to reduce the training set size.
- The new reduced training set is called the *condensed training set*.
  - Start with empty condensed set.
  - Let  $x$  be a training pattern.
  - Classify  $x$  using condensed set as the training set.
  - If  $x$  is misclassified then add  $x$  to the condensed set.
  - Repeatedly do this for all training patterns until no more changes to the condensed set.
- Training error using only the condensed set is zero.



# Some other ways ...

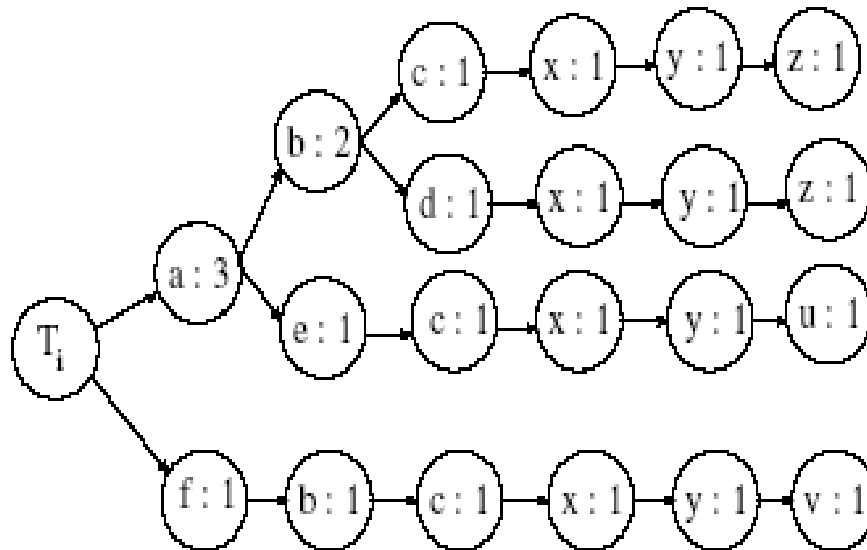
- Building an *index* over the training set can reduce the search time.
- Similar to *B+ trees* there are indexing methods for high dimensional data like *R-tree index*, *KD tree index*, etc.

## Some more ...

- To reduce the space, a compact representation for the training set can be found.
- *Anantanarayana (2001)* gave a compact representation called PC-tree. And also he gave nearest neighbor search method directly over PC-tree representations. So actually the search time also is reduced.

# PC-tree

Let the training patterns for a class are:  $(a,b,c,x,y,z)^t$ ,  
 $(a,b,c,x,y,z)^t$ ,  $(a,e,c,x,y,u)^t$ ,  $(f,b,c,x,y,v)^t$



# You too can ...

- It is easy to find some other ways to improve on k-NNC.
- What one can do:
  1. Do a closer study of existing improvements.
  2. Propose your improvement.
  3. Experiment on some datasets and hence show it really improves.
- One can closely study k-NNC along with SVM or MLP and find ways to speedup SVM or MLP learning.

# Next class

- We will go back to Bayes classifiers.