

TOC Mid-2 Solutions.

Ans. 1: $S \rightarrow 00S1 \mid \epsilon$

Ans. 2: $S \rightarrow 0T \mid 1T$
 $T \rightarrow 0S \mid 1S \mid \epsilon$

Ans. 3: String \rightarrow ababba.

i) Left most Derivation.

$S \rightarrow aB$
 $S \rightarrow abS$
 $S \rightarrow abaB$
 $S \rightarrow ababs$
 $S \rightarrow ababbA$
 $S \rightarrow ababba.$

(ii) Right Most Derivation.

$S \rightarrow aB$
 $S \rightarrow abS$
 $S \rightarrow abaB$
 $S \rightarrow ababs$
 $S \rightarrow ababbA$
 $S \rightarrow ababba.$

Ans 4: Not possible. Take the language $L = \{a^n a^n\}$, having only one string whose length is two. The given grammar can not produce this. Since the grammar can only produce strings of length 1 or 3 and so on. It can not produce strings of length 2.

⑤ Given grammar $S \rightarrow aAa \mid bBb \mid \epsilon$

$A \rightarrow C \mid a$

$B \rightarrow C \mid b$

$C \rightarrow CDE \mid \epsilon$

$D \rightarrow A \mid B \mid ab$

(i) Eliminating ϵ -productions:-

Nullable symbols in the above grammar are $\{S, C, A, B, D\}$

$S \rightarrow aAa \mid aA \mid bBb \mid bb$

$A \rightarrow C \mid a$

$B \rightarrow C \mid b$

$C \rightarrow CDE \mid DE \mid CE \mid E$

$D \rightarrow A \mid B \mid ab$

(ii) Removing unit productions:-

From the above resultant grammar, we have unit pairs.

(A, A) (A, C) (A, E)

(B, B) (B, C) (B, E)

(C, C) (C, E)

(D, D) (D, A) (D, B) (D, C) (D, E)

Non unit productions.

$S \rightarrow aAa \mid aA \mid bBb \mid bb$

$A \rightarrow a$

$B \rightarrow b$

$C \rightarrow CDE \mid DE \mid CE$

$D \rightarrow a \mid b \mid ab$

+

$A \rightarrow CDE \mid DE \mid CE$

$B \rightarrow CDE \mid DE \mid CE$

$D \rightarrow CDE \mid DE \mid CE$

\therefore After removing the unit productions, grammar will have.

$S \rightarrow aAa \mid bBb \mid aA \mid bb$

$A \rightarrow CDE \mid DE \mid CE \mid a$

$B \rightarrow CDE \mid DE \mid CE \mid b$

$C \rightarrow CDE \mid DE \mid CE$

$D \rightarrow CDE \mid DE \mid CE \mid a \mid b \mid ab$

(iii) Removing useless symbols:-

(i) Find the ~~non~~ generating symbols:-

$\{a, b, S, A, B, D\}$

and non-generating symbols are $= \{C, E\}$
remove the productions involving C, E in their body.

$$S \rightarrow aAa / bBb / aa / bb$$

$$A \rightarrow a$$

$$B \rightarrow b$$

$$D \rightarrow a / b / ab$$

(ii) Find unreachable symbols. 'D' is unreachable

so, remove D productions.

the final grammar

$$S \rightarrow aAa / bBb / aa / bb$$

$$A \rightarrow a$$

$$B \rightarrow b$$

The resulting grammar will be.

$$S \rightarrow aAa / bBb / aa / bb$$

$$A \rightarrow a$$

$$B \rightarrow b$$

⑥ Given grammar G , $S \rightarrow AA / SB$

$$B \rightarrow AA$$

$$A \rightarrow a$$

(i) given string $aaaaa$

for substring aa

$$\begin{array}{c} A, A \\ \downarrow \\ \{B, S\} \end{array}$$

-				
{S}	{S}			
-	-	-		
{S, B}	{S, B}	{S, B}	{S, B}	
A	A	A	A	A
a	a	a	a	a

for substring aaa .

a	aa	aa	a
A	{S, B}	{S, B}	A
AS	AB	SA	BA
-	-	-	-

for substring $aaaa$

a	aaa	aa	aa	aaa	a
A	ϕ	{S, B}	{S, B}	{ ϕ }	{A}
-	-	SS	SB	BS	BB
-	-	-	S	-	-

for $aaaaa$

a	aaaa	aa	aaa	aaa	aa	aaaa	a
A	S	{S, B}	{ ϕ }	{ ϕ }	{S, B}	S	A
A	S	-	-	-	-	S	A

∴ The given string $a^5(aaaaa)$ is not in $L(G)$.

(ii) Given string aaaaaa

for substring aa
 $\downarrow \downarrow$
 $A \ A$
 \downarrow
 $\{S, B\}$

for substring aaa

a	aa		aa	a
A	$\{S, B\}$		$\{S, B\}$	A
AS	AB		SA	BA
-	-		-	-

for substring aaaa

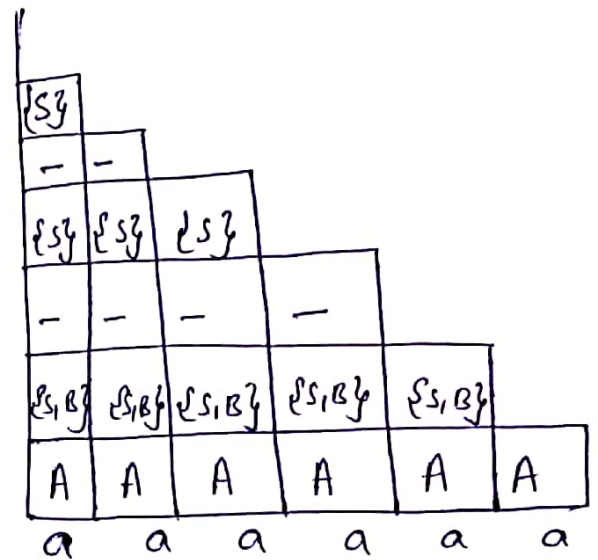
a	aaa		aa	aa
A	$\{\phi\}$		$\{S, B\}$	$\{S, B\}$
ϕ			SS	SB
-	-		-	S

for substring aaaaaa

a	aaaa		aa	aaa		aaa	aa		aaaa	a
$\{A\}$	$\{S\}$		$\{S, B\}$	$\{\phi\}$		$\{\phi\}$	$\{S, B\}$		$\{S\}$	$\{A\}$
AS			S	-		-			SA	
-	-		-	-		-	-		-	-

for substring aaaaaaa

a	aaaaa		aa	aaaa		aaa	aaa		aaaa	aa		aaaaa	a
A	ϕ		$\{S, B\}$	$\{S\}$		$\{\phi\}$	$\{\phi\}$		$\{S\}$	$\{S, B\}$		$\{\phi\}$	$\{A\}$
-	-		SS	BS		-	-		SS	SB		-	-
-	-		-	-		-	-		-	S		-	-



\therefore The given string aaaaaa is in $L(G)$.