# Static Program Analysis Part 9 – pointer analysis

http://cs.au.dk/~amoeller/spa/

Anders Møller & Michael I. Schwartzbach Computer Science, Aarhus University

#### Agenda

- Introduction to points-to analysis
- Andersen's analysis
- Steensgaards's analysis
- Interprocedural points-to analysis
- Null pointer analysis
- Flow-sensitive points-to analysis

#### **Analyzing programs with pointers**

How do we perform e.g. constant propagation analysis when the programming language has pointers? (or object references?)

```
*x = 42;
*y = -87;
z = *x;
// is z 42 or -87?
```

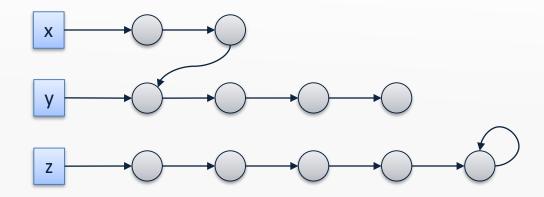
```
E → &X
| alloc E
| *E
| null
| ...
```

$$S \rightarrow *X = E;$$
| ...

$$E \rightarrow E(E, ..., E)$$

#### **Heap pointers**

- For simplicity, we ignore records
  - alloc then only allocates a single cell
  - only linear structures can be built in the heap



- Let's at first also ignore function pointers
- We still have many interesting analysis challenges...

#### **Pointer targets**

- The fundamental question about pointers:
   What locations can they point to?
- We need a suitable abstraction
- The set of (abstract) cells, Cells, contains
  - alloc-i for each allocation site with index i
  - X for each program variable named X
- This is called *allocation site abstraction*
- Each abstract cell may correspond to many concrete memory cells at runtime

#### Points-to analysis

- Determine for each pointer variable X the set pt(X) of the cells X may point to
- A conservative ("may points-to") analysis:
  - the set may be too large
  - can show absence of aliasing:  $pt(X) \cap pt(Y) = \emptyset$
- We'll focus on *flow-insensitive* analyses:
  - take place on the AST
  - before or together with the control-flow analysis

\*x = 42:

\*y = -87;

// is z 42 or -87?

#### **Obtaining points-to information**

- An almost-trivial analysis (called address-taken):
  - include all alloc-i cells
  - include the X cell if the expression &X occurs in the program
- Improvement for a typed language:
  - eliminate those cells whose types do not match
- This is sometimes good enough
  - and clearly very fast to compute

#### **Pointer normalization**

- Assume that all pointer usage is normalized:
  - X =alloc P where P is null or an integer constant
  - X = &Y
  - X = Y
  - X = \*Y
  - \*X = Y
  - X = null
- Simply introduce lots of temporary variables...
- All sub-expressions are now named
- We choose to ignore the fact that the cells created at variable declarations are uninitialized

#### Agenda

- Introduction to points-to analysis
- Andersen's analysis
- Steensgaards's analysis
- Interprocedural points-to analysis
- Null pointer analysis
- Flow-sensitive points-to analysis

# Andersen's analysis (1/2)

- For every cell c, introduce a constraint variable  $[\![c]\!]$  ranging over sets of locations, i.e.  $[\![\cdot]\!]$ : Cells  $\rightarrow 2^{Cells}$
- Generate constraints:

• 
$$X = \text{alloc } P$$
: alloc- $i \in [X]$ 

• 
$$X = \&Y$$
:  $Y \in \llbracket X \rrbracket$ 

• 
$$X = Y$$
:  $[Y] \subseteq [X]$ 

• 
$$X = {}^*Y$$
:  $\alpha \in [\![Y]\!] \Rightarrow [\![\alpha]\!] \subseteq [\![X]\!]$  for each  $\alpha \in Cells$ 

• \*
$$X = Y$$
:  $\alpha \in [X] \Rightarrow [Y] \subseteq [\alpha]$  for each  $\alpha \in Cells$ 

• 
$$X = null$$
: (no constraints)

# Andersen's analysis (2/2)

The points-to map is defined as:

$$pt(X) = [X]$$

- The constraints fit into the cubic framework ©
- Unique minimal solution in time  $O(n^3)$
- In practice, for Java:  $O(n^2)$
- The analysis is flow-insensitive but directional
  - models the direction of the flow of values in assignments

#### **Example program**

```
var p,q,x,y,z;
p = alloc null;
x = y;
X = Z;
*p = z;
p = q;
q = &y;
x = *p;
p = \&z;
```

#### **Applying Andersen**

Generated constraints:

```
alloc-1 \in [p]
[y] \subseteq [x]
[z] \subseteq [x]
\alpha \in [p] \Rightarrow [z] \subseteq [\alpha]
[q] \subseteq [p]
y \in [q]
\alpha \in [p] \Rightarrow [\alpha] \subseteq [x]
z \in [p]
```

Smallest solution:

#### Agenda

- Introduction to points-to analysis
- Andersen's analysis
- Steensgaards's analysis
- Interprocedural points-to analysis
- Null pointer analysis
- Flow-sensitive points-to analysis

## Steensgaard's analysis

- View assignments as being bidirectional
- Generate constraints:

• 
$$X = \text{alloc } P$$
:  $\text{alloc-} i \in [X]$ 

• 
$$X = \&Y$$
:  $Y \in \llbracket X \rrbracket$ 

• 
$$X = Y$$
:  $[X] = [Y]$ 

• 
$$X = *Y$$
:  $\alpha \in [Y] \Rightarrow [\alpha] = [X]$ 

• 
$$*X = Y$$
:  $\alpha \in [X] \Rightarrow [Y] = [\alpha]$ 

Extra constraints:

$$t_1, t_2 \in [\![t]\!] \Rightarrow [\![t_1]\!] = [\![t_2]\!]$$
 and  $[\![t_1]\!] \cap [\![t_2]\!] \neq \emptyset \Rightarrow [\![t_1]\!] = [\![t_2]\!]$  (whenever a cell may point to two cells, they are effectively merged into one)

• Steensgaard's original formulation uses conditional unification for X = Y:  $\alpha \in [Y] \Rightarrow [X] = [Y]$  (avoids unifying if Y is never a pointer)

### Steensgaard's analysis

- Reformulate as term unification
- Generate constraints:

• 
$$X = alloc P$$
:  $[X] = &[alloc - i]$ 

• 
$$X = \&Y$$
:  $[X] = \&[Y]$ 

• 
$$X = Y$$
:  $[X] = [Y]$ 

• 
$$X = *Y$$
:  $[Y] = & \alpha \land [X] = \alpha$  where  $\alpha$  is fresh

• 
$$*X = Y$$
:  $[X] = & \alpha \land [Y] = \alpha$  where  $\alpha$  is fresh

- Terms:
  - term variables, e.g. [X], [alloc-i],  $\alpha$  (each representing the possible values of a cell)
  - a single (unary) term constructor &t (representing the location of the cell that t represents)
  - $\|X\|$  is now a term variable, not a constraint variable holding a set of cells
- Fits with our unification solver! (union-find...)
- The points-to map is defined as  $pt(X) = \{ c \in Cells \mid [X] = \&[c] \}$
- Note that there is only one kind of term constructor, so unification never fails<sub>16</sub>

## **Applying Steensgaard**

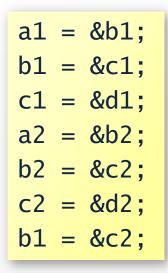
Generated constraints:

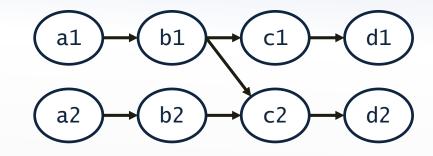
```
alloc-1 \in [p]
[y] = [x]
[z] = [x]
\alpha \in [\![p]\!] \Rightarrow [\![z]\!] = [\![\alpha]\!]
[q] = [p]
y \in [q]
\alpha \in [\![p]\!] \Rightarrow [\![\alpha]\!] = [\![x]\!]
z \in [p]
+ the extra constraints
```

• Smallest solution:

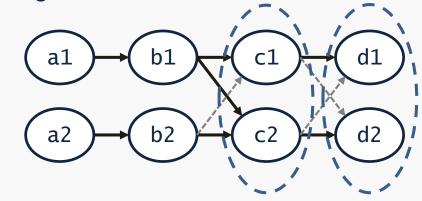
#### **Another example**

#### Andersen:





#### Steensgaard:



#### Recall our type analysis...

- Focusing on pointers...
- Constraints:

Implicit extra constraint for term equality:

$$\&t_1 = \&t_2 \Rightarrow t_1 = t_2$$

 Assuming the program type checks, is the solution for pointers the same as for Steensgaard's analysis?

#### **Agenda**

- Introduction to points-to analysis
- Andersen's analysis
- Steensgaards's analysis
- Interprocedural points-to analysis
- Null pointer analysis
- Flow-sensitive points-to analysis

#### Interprocedural points-to analysis

- If function pointers are distinct from heap pointers:
  - first run a CFA
  - then run Andersen or Steensgaard
- But in TIP both kinds may be mixed together:

$$(***x)(1,2,3)$$

• In this case the CFA and the points-to analysis must happen *simultaneously*!

#### **Function call normalization**

Assume that all function calls are of the form

$$x = y(a_1, ..., a_n)$$

- y may be a variable whose value is a function pointer
- Assume that all return statements are of the form

- As usual, simply introduce lots of temporary variables...
- Include all function names in Cells

#### **CFA** with Andersen

For the function call

$$x = y(a_1, ..., a_n)$$
  
and every occurrence of

Andersen's analysis is already closely connected to control-flow analysis!

 $f(x_1, ..., x_n)$  { ... return z; } add these constraints:

$$f \in \llbracket f \rrbracket$$
 $f \in \llbracket y \rrbracket \Rightarrow (\llbracket a_i \rrbracket \subseteq \llbracket x_i \rrbracket \text{ for i=1,...,} n \land \llbracket z \rrbracket \subseteq \llbracket x \rrbracket)$ 

- (Similarly for simple function calls)
- Fits directly into the cubic framework!

#### **CFA** with Steensgaard

For the function call

$$x = y(a_1, ..., a_n)$$
  
and every occurrence of

$$f(x_1, ..., x_n) \{ ... return z; \}$$

add these constraints:

$$f \in \llbracket f \rrbracket$$

$$f \in \llbracket y \rrbracket \Rightarrow (\llbracket a_i \rrbracket = \llbracket x_i \rrbracket \text{ for i=1,...,} n \land \llbracket z \rrbracket = \llbracket x \rrbracket)$$

- (Similarly for simple function calls)
- Fits into the unification framework, but requires a generalization of the ordinary union-find solver

- Generalize the abstract domain  $Cells \rightarrow 2^{Cells}$  to  $Contexts \rightarrow Cells \rightarrow 2^{Cells}$  (or equivalently:  $Cells \times Contexts \rightarrow 2^{Cells}$ ) where Contexts is a (finite) set of call contexts
- As usual, many possible choices of Contexts
  - recall the call string approach and the functional approach
- Also need to track the set of reachable contexts for each function (like the use of lifted lattices earlier)
- Does this still fit into the cubic solver?

```
foo(a) {
  return *a;
bar() {
  x = alloc null; // alloc-1
  y = alloc null; // alloc-2
  *x = alloc null; // alloc-3
  *y = alloc null; // alloc-4
  q = foo(x);
 W = foo(y);
```

```
mk() {
  return alloc null; // alloc-1
baz() {
 var x,y;
 x = mk();
  y = mk();
```

Are x and y aliases?

- We can go one step further and introduce context-sensitive heap (a.k.a. heap cloning)
- Let each abstract cell be a pair of
  - alloc-i (the alloc with index i) or X (a program variable)
  - a heap context from a (finite) set HeapContexts
- This allows abstract cells to be named by the source code allocation site and (information from) the current context
- One choice:
  - set HeapContexts = Contexts
  - at alloc, use the entire current call context as heap context

#### Agenda

- Introduction to points-to analysis
- Andersen's analysis
- Steensgaards's analysis
- Interprocedural points-to analysis
- Null pointer analysis
- Flow-sensitive points-to analysis

### **Null pointer analysis**

- Decide for every dereference \*p, is p different from null?
- (Why not just treat null as a special location in an Andersen or Steensgaard-style analysis?)
- Use the monotone framework
  - assuming that a points-to map pt has been computed
- Let us consider an intraprocedural analysis
   (i.e. we ignore function calls)

### A lattice for null analysis

• Define the simple lattice *Null*:



where NN represents "definitely **n**ot **n**ull" and ? represents "maybe null"

Use for every program point the map lattice:

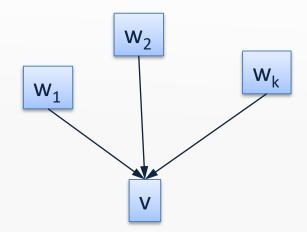
Cells 
$$\rightarrow$$
 Null

#### Setting up

- For every CFG node, v, we have a variable [[v]]:
  - a map giving abstract values for all cells at the program point after v
- Auxiliary definition:

$$JOIN(v) = \coprod [w]$$
  
 $w \in pred(v)$ 

(i.e. we make a forward analysis)



### **Null analysis constraints**

For operations involving pointers:

$$||v|| = ???$$

• 
$$X = \&Y$$
:

• 
$$X = Y$$
:

• 
$$X = *Y$$
:

• 
$$*X = Y$$
:

For all other CFG nodes:

where *P* is null or an integer constant

#### **Null analysis constraints**

- For a heap store operation \*X = Y we need to model the change of whatever X points to
- That may be multiple abstract cells (i.e. the cells pt(X))
- With the present abstraction, each abstract heap cell alloc-i may describe multiple concrete cells
- So we settle for weak update:

\*
$$X = Y$$
:  $\llbracket v \rrbracket = store(JOIN(v), X, Y)$   
where  $store(\sigma, X, Y) = \sigma[\alpha \mapsto \sigma(\alpha) \sqcup \sigma(Y)]$ 

#### **Null analysis constraints**

- For a heap load operation  $X = {}^*Y$  we need to model the change of the program variable X
- Our abstraction has a single abstract cell for X
- That abstract cell represents a single concrete cell
- So we can use strong update:

$$X = *Y$$
:  $\llbracket v \rrbracket = load(JOIN(v), X, Y)$   
where  $load(\sigma, X, Y) = \sigma[X \mapsto \bigsqcup_{\alpha \in pt(Y)} \sigma(\alpha)]$ 

#### Strong and weak updates

```
mk() {
  return alloc null; // alloc-1
a = mk();
b = mk();
*a = alloc null; // alloc-2
n = null;
*b = n; // strong update here would be unsound!
c = *a;
```

is C null here?

The abstract cell alloc-1 corresponds to multiple concrete cells

#### Strong and weak updates

```
a = alloc null; // alloc-1
b = alloc null; // alloc-2
*a = alloc null; // alloc-3
*b = alloc null; // alloc-4
if (...) {
 x = a;
} else {
  x = b:
n = null;
*x = n; // strong update here would be unsound!
c = *x;
```

is C null here?

The points-to set for x contains *multiple abstract cells* 

## **Null analysis constraints**

```
    X = alloc P: [v] = JOIN(v)[X → NN, alloc-i → ?]
    X = &Y: [v] = JOIN(v)[X → NN]
    X = Y: [v] = JOIN(v)[X → JOIN(v)(Y)]
    X = null: [v] = JOIN(v)[X → ?]
```

- In each case, the assignment modifies a program variable
- So we can use strong updates, as for heap load operations

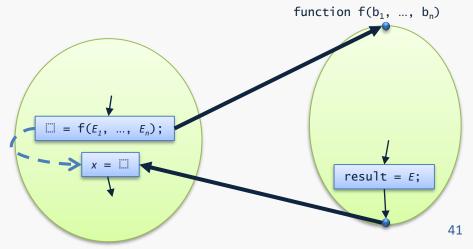
## Strong and weak updates, revisited

- Strong update:  $\sigma[c \mapsto new-value]$ 
  - possible if c is known to refer to a single concrete cell
  - works for assignments to local variables
     (as long as TIP doesn't have e.g. nested functions)

- Weak update:  $\sigma[c \mapsto \sigma(c) \sqcup new-value]$ 
  - necessary if c may refer to multiple concrete cells
  - bad for precision, we lose some of the power of flow-sensitivity
  - required for assignments to heap cells (unless we extend the analysis abstraction!)

## Interprocedural null analysis

- Context insensitive or context sensitive, as usual...
  - at the after-call node, use the heap from the callee
- But be careful!
   Pointers to local variables may escape to the callee
  - the abstract state at the after-call node cannot simply copy the abstract values for local variables from the abstract state at the call node



# Using the null analysis

The pointer dereference \*p is "safe" at entry of v if
 JOIN(v)(p) = NN

• The quality of the null analysis depends on the quality of the underlying points-to analysis

#### **Example program**

```
p = alloc null;
q = &p;
n = null;
*q = n;
*p = n;
```

#### Andersen generates:

```
pt(p) = {alloc-1}
pt(q) = {p}
pt(n) = Ø
```

#### **Generated constraints**

#### Solution

- At the program point before the statement \*q=n
   the analysis now knows that q is definitely non-null
- ... and before \*p=n, the pointer p is maybe null
- Due to the weak updates for all heap store operations, precision is bad for alloc-i locations

#### **Agenda**

- Introduction to points-to analysis
- Andersen's analysis
- Steensgaards's analysis
- Interprocedural points-to analysis
- Null pointer analysis
- Flow-sensitive points-to analysis

#### Points-to graphs

- Graphs that describe possible heaps:
  - nodes are abstract cells
  - edges are possible pointers between the cells
- The lattice of points-to graphs is  $2^{Cells \times Cells}$  ordered under subset inclusion (or alternatively,  $Cells \rightarrow 2^{Cells}$ )
- For every CFG node, v, we introduce a constraint variable \[v\] describing the state after v
- Intraprocedural analysis (i.e. ignore function calls)

#### **Constraints**

For pointer operations:

```
• X = \text{alloc } P: [v] = JOIN(v) \downarrow X \cup \{ (X, \text{alloc} - i) \}

• X = \&Y: [v] = JOIN(v) \downarrow X \cup \{ (X, Y) \}

• X = Y: [v] = assign(JOIN(v), X, Y)

• X = *Y: [v] = load(JOIN(v), X, Y)

• *X = Y: [v] = store(JOIN(v), X, Y)

• X = \text{null}: [v] = JOIN(v) \downarrow X
```

- For all other CFG nodes:
  - \[ \v \] = JOIN(\v)

# **Auxiliary functions**

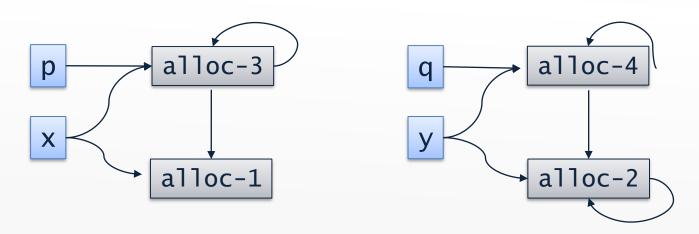
- $\sigma \downarrow X = \{ (s,t) \in \sigma \mid s \neq X \}$
- $assign(\sigma, X, Y) = \sigma \downarrow X \cup \{ (X, t) \mid (Y, t) \in \sigma \}$
- $load(\sigma, X, Y) = \sigma \downarrow X \cup \{ (X, t) \mid (Y, s) \in \sigma, (s, t) \in \sigma \}$
- $store(\sigma, X, Y) = \sigma \cup \{ (s, t) \mid (X, s) \in \sigma, (Y, t) \in \sigma \}$ 
  - note: weak update!

#### Example program

```
var x,y,n,p,q;
x = alloc null; y = alloc null;
*x = null; *y = y;
n = input;
while (n>0) {
  p = alloc null; q = alloc null;
  *p = x; *q = y;
 x = p; y = q;
 n = n-1;
```

## Result of analysis

After the loop we have this points-to graph:



We conclude that x and y will always be disjoint

## Points-to maps from points-to graphs

A points-to map for each program point v:

$$pt(X) = \{ t \mid (X,t) \in \llbracket v \rrbracket \}$$

- More expensive, but more precise:
  - Andersen:  $pt(x) = \{ y, z \}$
  - flow-sensitive:  $pt(x) = \{z\}$

# Improving precision with abstract counting

- The points-to graph is missing information:
  - alloc-2 nodes always form a self-loop in the example
- We need a more detailed lattice:

$$2^{Cell \times Cell} \times (Cell \rightarrow Count)$$

where we for each cell keep track of how many concrete cells that abstract cell describes

$$Count = 0 1 > 1$$

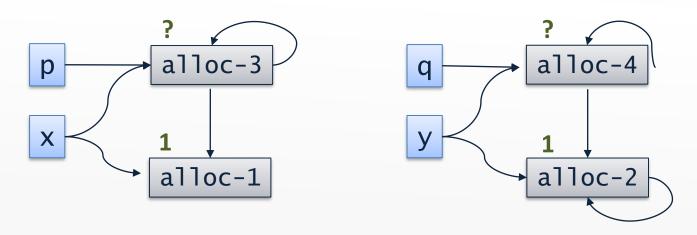
 This permits strong updates on those that describe precisely 1 concrete cell

#### **Constraints**

- X= alloc P: ...
- \*X = Y: ...
- •

#### **Better results**

After the loop we have this extended points-to graph:



Thus, alloc-2 nodes form a self-loop

# Interprocedural shape analysis

#### New issues to consider:

- parameter passing etc.
- weak updates to stack cells
- escaping of stack cells

#### **Escape analysis**

- Perform a points-to analysis
- Look at return expression
- Check reachability in the points-to graph to arguments or variables defined in the function itself

None of those

no escaping stack cells

```
baz() {
  var x;
  return &x;
main() {
  var p;
  p=baz();
  *p=1;
  return *p;
```