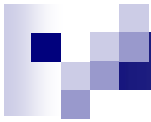




Compiler

Parsing: Bottom-Up

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Bottom-Up Parsing

- Bottom-up parsing is more general than top-down parsing
 - And just as efficient
 - Builds on ideas in top-down parsing
- Bottom-up is the preferred method in practice
- We'll explain the intuition, you should read the book to understand the algorithm



An Introductory Example

- Bottom-up parsers don't need left-factored grammars
- Hence we can revert to the “natural” grammar for our example:

$$E \rightarrow T + E \mid T$$

$$T \rightarrow \text{int} * T \mid \text{int} \mid (E)$$

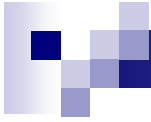
- Consider the string: `int * int + int`



The Idea

Bottom-up parsing *reduces* a string to the start symbol by inverting productions:

int * int + int	$T \rightarrow \text{int}$
int * T + int	$T \rightarrow \text{int} * T$
T + int	$T \rightarrow \text{int}$
T + T	$E \rightarrow T$
T + E	$E \rightarrow T + E$
E	



For You To Do

- **Question:** find the rightmost derivation of the string `int * int + int`

Observation

- Read the productions found by bottom-up parse in reverse (i.e., from bottom to top)
- This is a rightmost derivation!

int * int + int	$T \rightarrow \text{int}$
int * T + int	$T \rightarrow \text{int} * T$
T + int	$T \rightarrow \text{int}$
T + T	$E \rightarrow T$
T + E	$E \rightarrow T + E$
E	

A Bottom-up Parse

int * int + int

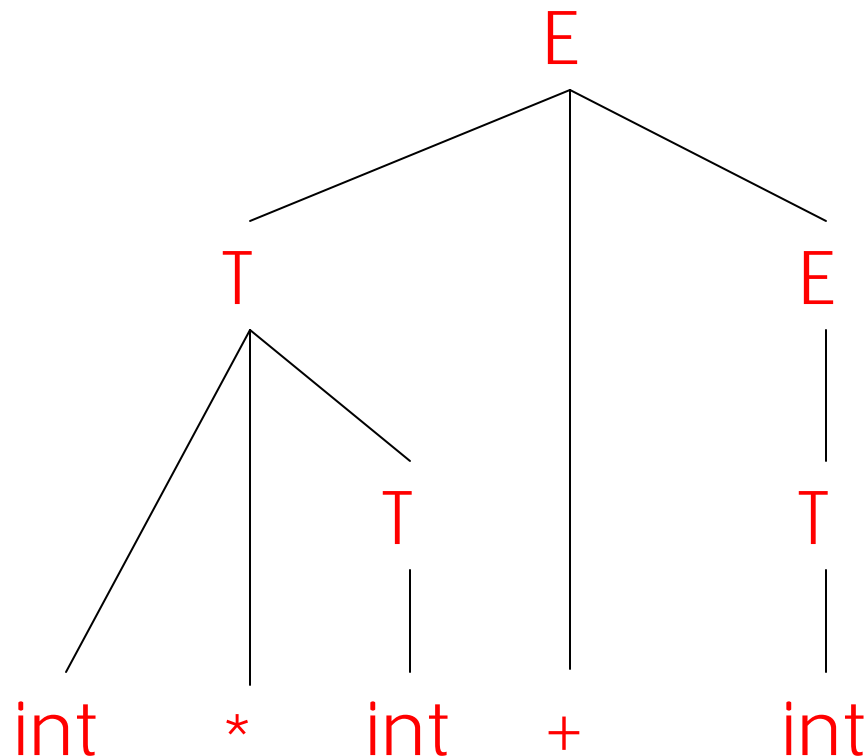
int * T + int

T + int

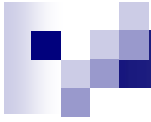
T + T

T + E

E



A bottom-up parser traces a rightmost derivation in reverse



A Bottom-up Parse in Detail (1)

int * int + int

int * int + int



A Bottom-up Parse in Detail (2)

int * int + int

int * T + int

int * int + int

T

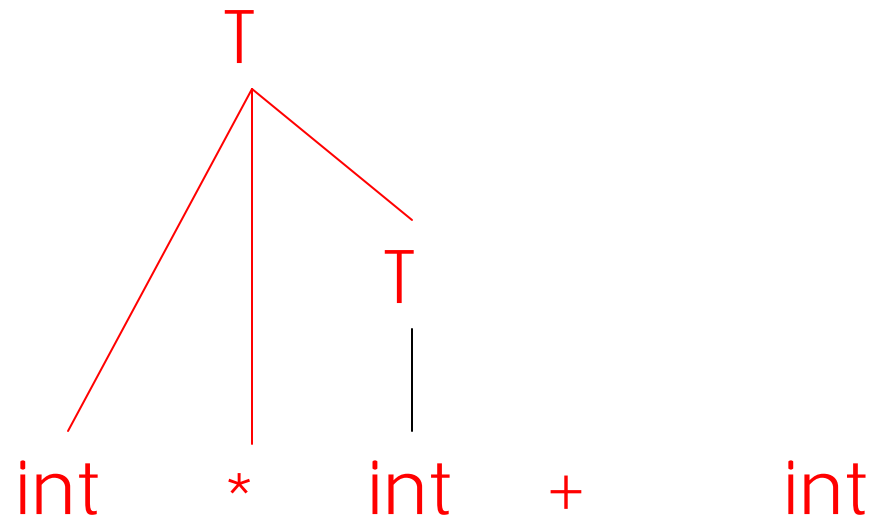
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A Bottom-up Parse in Detail (3)

int * int + int

int * T + int

T + int



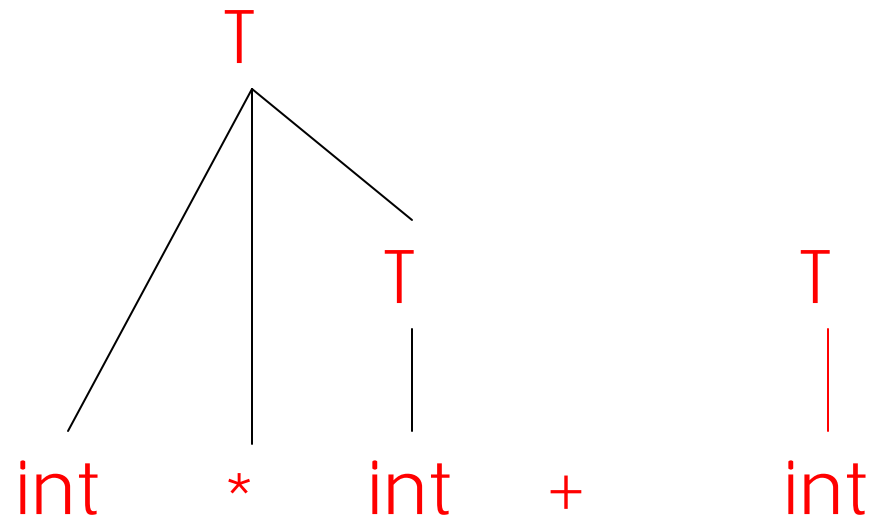
A Bottom-up Parse in Detail (4)

int * int + int

int * T + int

T + int

T + T



A Bottom-up Parse in Detail (5)

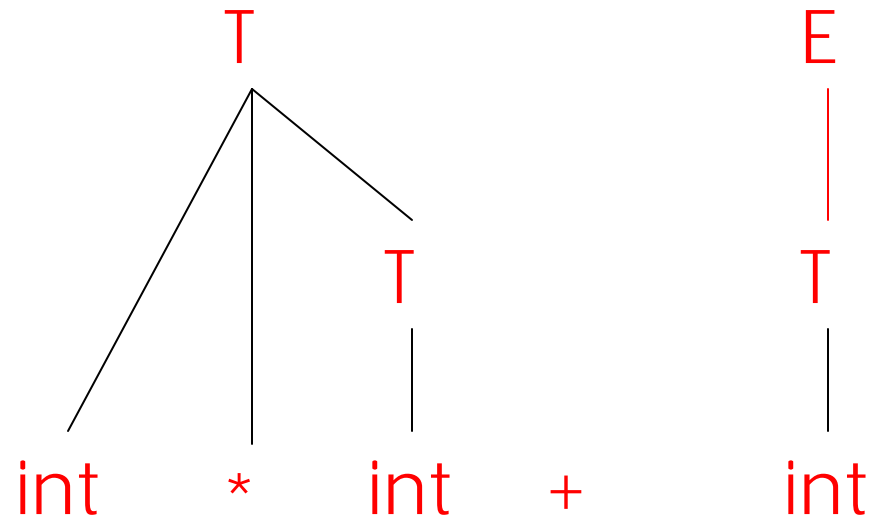
int * int + int

int * T + int

T + int

T + T

T + E



A Bottom-up Parse in Detail (6)

int * int + int

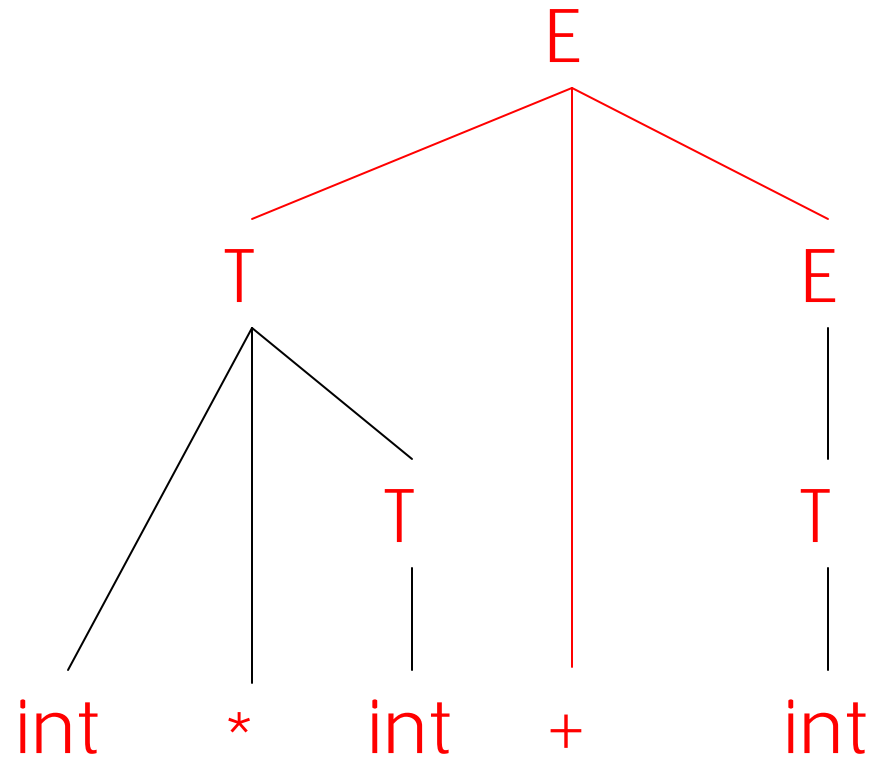
int * T + int

T + int

T + T

T + E

E





A Trivial Bottom-Up Parsing Algorithm

Let I = input string

repeat

 pick a non-empty substring β of I

 where $X \rightarrow \beta$ is a production

 if no such β , backtrack

 replace one β by X in I

until $I = "S"$ (the start symbol) or all

possibilities are exhausted



For You To Do

Do you see any problems with this algorithm?

Think about performance and completeness



Where Do Reductions Happen

Let $\alpha\beta\omega$ be a step of a bottom-up parse

- Assume the next reduction is by $X \rightarrow \beta$
- Then ω is a string of terminals

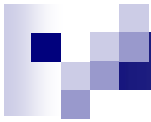
Why?

Because $\alpha X \omega \rightarrow \alpha \beta \omega$ is a step in a right-most derivation



Idea

- Split string into two substrings
 - Right substring : as yet unexamined by parsing (a string of terminals)
 - Left substring : has terminals and non-terminals
- The dividing point is marked by a |
 - The | is not part of the string
- Initially, all input is unexamined | $x_1 x_2 \dots x_n$



Shift-Reduce Parsing

Bottom-up parsing uses only two kinds of actions:

Shift

Reduce



Shift

- *Shift*: Move | one place to the right
 - Shifts a terminal to the left string

ABC|xyz \Rightarrow ABCx|yz



Reduce

- Apply an *inverse production* at the right end of the left string
 - If $A \rightarrow xy$ is a production, then

$$Cbxy|ijk \Rightarrow CbA|ijk$$

- xy is called a *handle*



The Example with Reductions

int * int | + int

int * T | + int

reduce $T \rightarrow \text{int}$

reduce $T \rightarrow \text{int} * T$

T + int |

T + T |

T + E |

E |

reduce $T \rightarrow \text{int}$

reduce $E \rightarrow T$

reduce $E \rightarrow T + E$

The Example with Shift-Reduce Parsing

int * int + int	shift
int * int + int	shift
int * int + int	shift
int * int + int	reduce $T \rightarrow \text{int}$
int * T + int	reduce $T \rightarrow \text{int} * T$
T + int	shift
T + int	shift
T + int	reduce $T \rightarrow \text{int}$
T + T	reduce $E \rightarrow T$
T + E	reduce $E \rightarrow T + E$
E	



A Shift-Reduce Parse in Detail (1)

|int * int + int

int * int + int
↑



A Shift-Reduce Parse in Detail (2)

|int * int + int
int | * int + int

int * int + int
↑



A Shift-Reduce Parse in Detail (3)

|int * int + int

int | * int + int

int * | int + int

int * int + int
 ↑



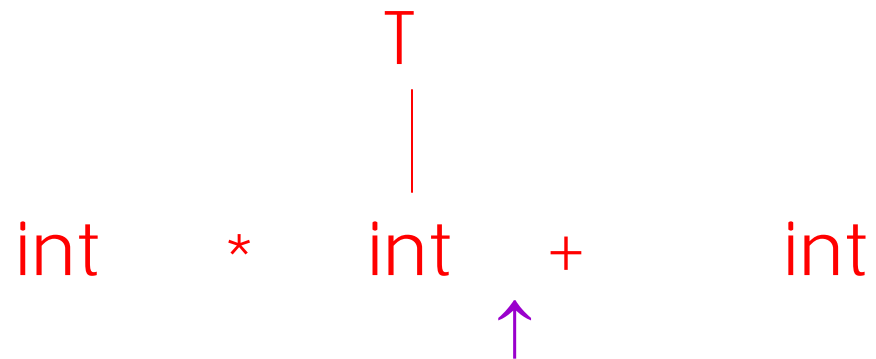
A Shift-Reduce Parse in Detail (4)

|int * int + int
int | * int + int
int * | int + int
int * int | + int

int * int + int
 ↑

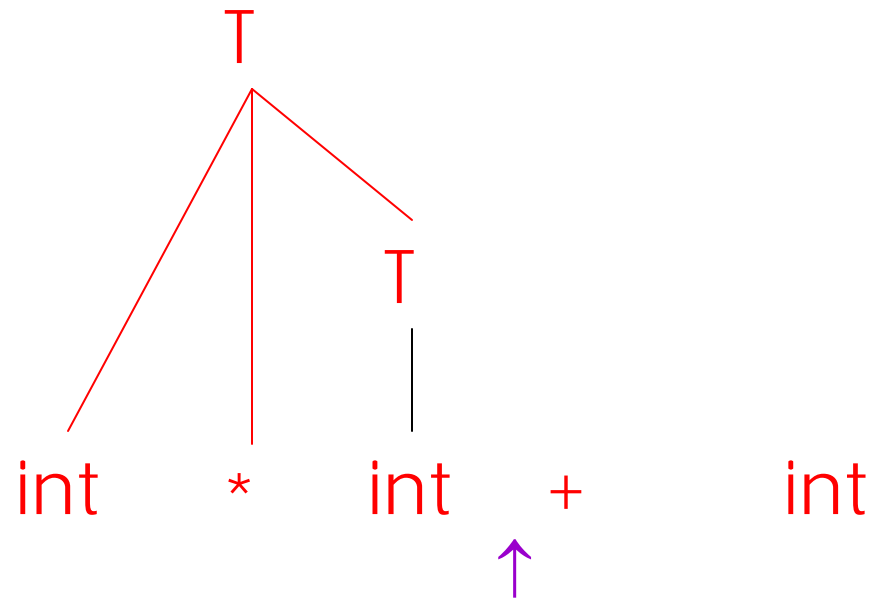
A Shift-Reduce Parse in Detail (5)

|int * int + int
int | * int + int
int * | int + int
int * int | + int
int * T | + int



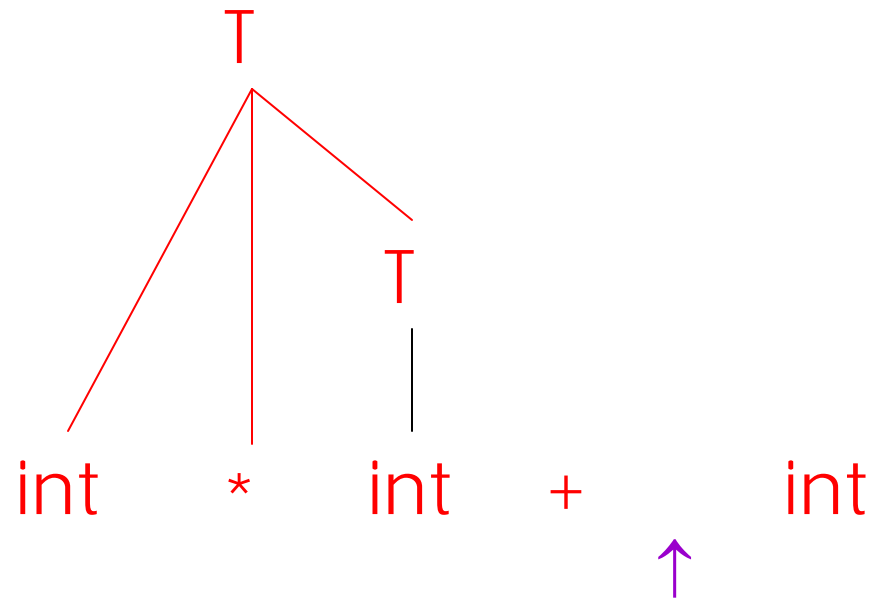
A Shift-Reduce Parse in Detail (6)

| int * int + int
int | * int + int
int * | int + int
int * int | + int
int * T | + int
T | + int



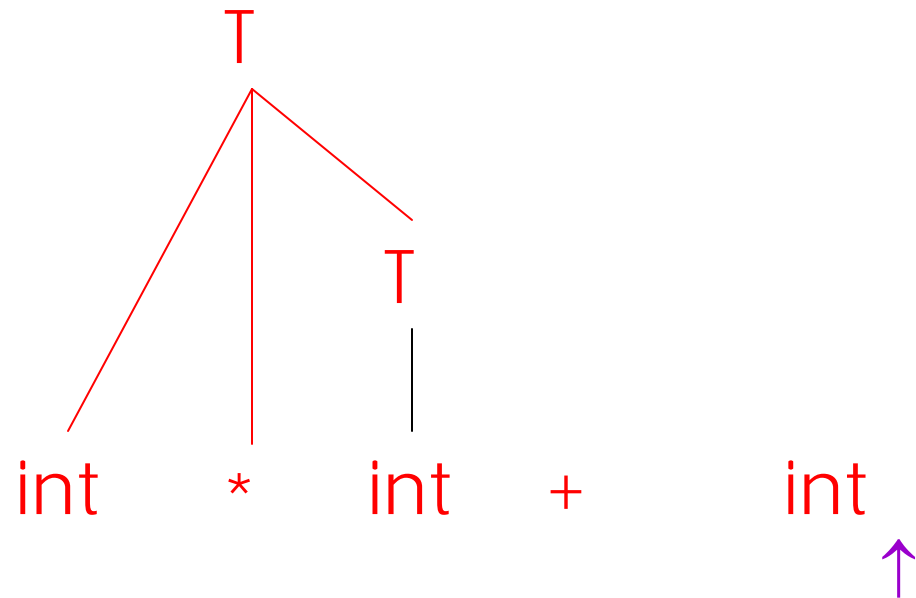
A Shift-Reduce Parse in Detail (7)

| int * int + int
int | * int + int
int * | int + int
int * int | + int
int * T | + int
T | + int
T + | int



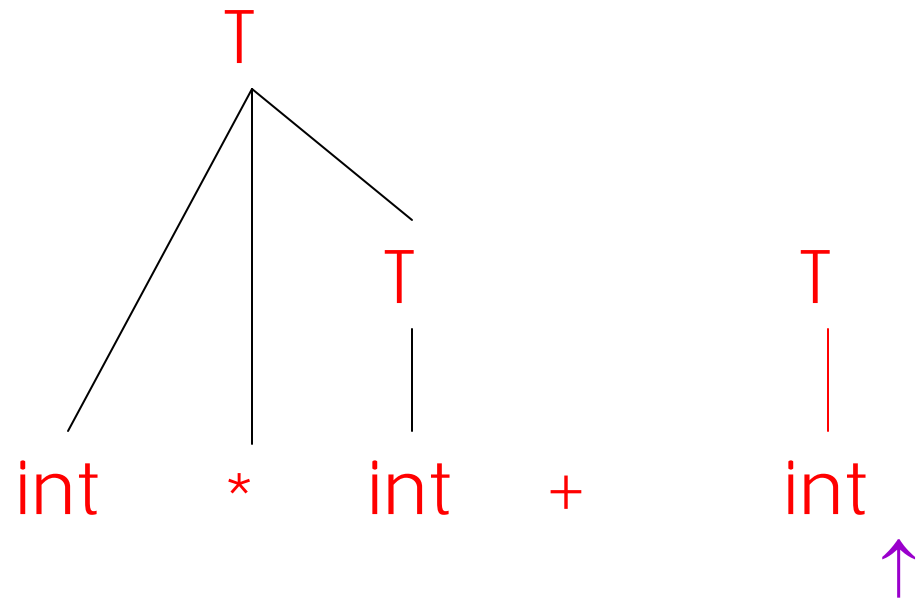
A Shift-Reduce Parse in Detail (8)

| int * int + int
int | * int + int
int * | int + int
int * int | + int
int * T | + int
T | + int
T + | int
T + int |



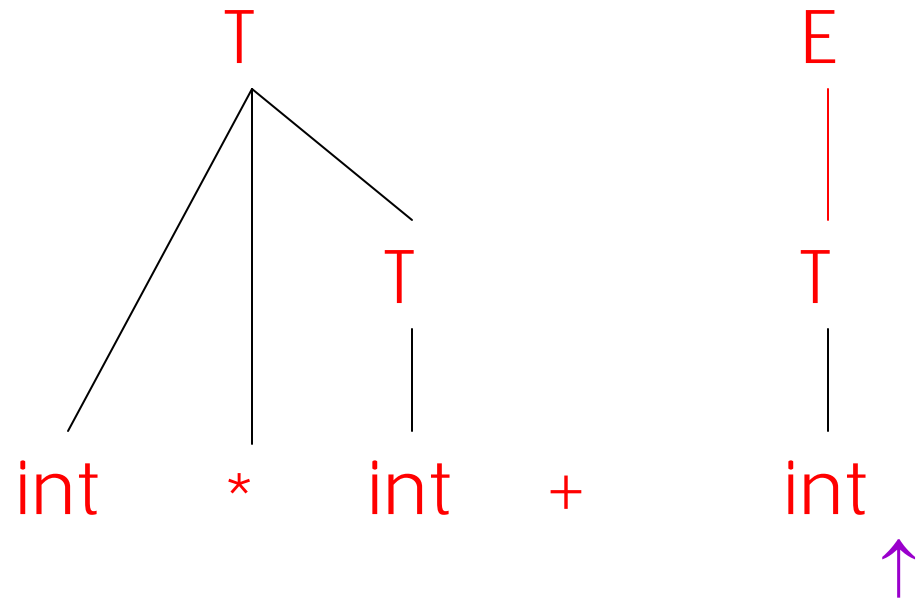
A Shift-Reduce Parse in Detail (9)

| int * int + int
int | * int + int
int * | int + int
int * int | + int
int * T | + int
T | + int
T + | int
T + int |
T + T |



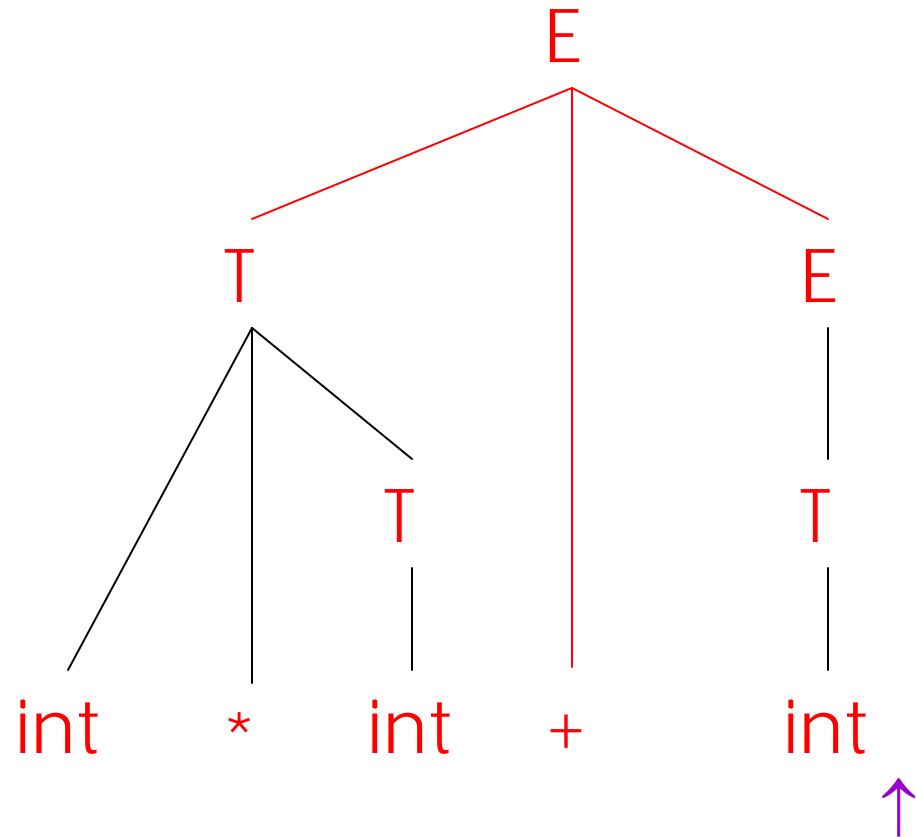
A Shift-Reduce Parse in Detail (10)

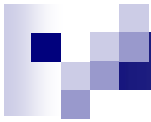
| int * int + int
int | * int + int
int * | int + int
int * int | + int
int * T | + int
T | + int
T + | int
T + int |
T + T |
T + E |



A Shift-Reduce Parse in Detail (11)

| int * int + int
int | * int + int
int * | int + int
int * int | + int
int * T | + int
T | + int
T + | int
T + int |
T + T |
T + E |
E |





The Stack

- Left string can be implemented by a stack
 - Top of the stack is the |
- Shift pushes a terminal on the stack
- Reduce pops 0 or more symbols off of the stack (production rhs) and pushes a non-terminal on the stack (production lhs)



Key Issue

- How do we decide when to shift or reduce?
 - Consider step `int | * int + int`
 - We could reduce by $T \rightarrow \text{int}$ giving `T | * int + int`
 - A fatal mistake: No way to reduce to the start symbol `E`
- This is resolved by various bottom-up parsing algorithms



Conflicts

- Generic shift-reduce strategy:
 - If there is a handle on top of the stack, reduce
 - Otherwise, shift
- But what if there is a choice?
 - If it is legal to shift or reduce, there is a *shift-reduce conflict*
 - If it is legal to reduce by two different productions, there is a *reduce-reduce conflict*



Source of Conflicts

- Ambiguous grammars always cause conflicts
- But beware, so do many non-ambiguous grammars



Conflict Example

Consider our favorite ambiguous grammar:

$$\begin{array}{lcl} E & \rightarrow & E + E \\ & | & E * E \\ & | & (E) \\ & | & \text{int} \end{array}$$

One Shift-Reduce Parse

|int * int + int

shift

...

...

E * E | + int

reduce $E \rightarrow E * E$

E | + int

shift

E + | int

shift

E + int|

reduce $E \rightarrow \text{int}$

E + E |

reduce $E \rightarrow E + E$

E |

Another Shift-Reduce Parse

|int * int + int

shift

...

...

E * E | + int

shift

E * E + | int

shift

E * E + int |

reduce $E \rightarrow \text{int}$

E * E + E |

reduce $E \rightarrow E + E$

E * E |

reduce $E \rightarrow E * E$

E |



Example Notes

- In the second step $E * E \mid + \text{int}$ we can either shift or reduce by $E \rightarrow E * E$
- Choice determines associativity of $+$ and $*$
- As noted previously, grammar can be rewritten to enforce precedence
- Precedence declarations are an alternative



Precedence Declarations Revisited

- Precedence declarations cause shift-reduce parsers to resolve conflicts in certain ways
- Declaring “ $*$ has greater precedence than $+$ ” causes parser to reduce at $E * E \mid + \text{int}$
- More precisely, precedence declaration is used to resolve conflict between reducing a $*$ and shifting a $+$



Precedence Declarations Revisited (Cont.)

- The term “precedence declaration” is a bit misleading
- These declarations do not define precedence; they define conflict resolutions
 - Not quite the same thing!