

# Tutorial 9

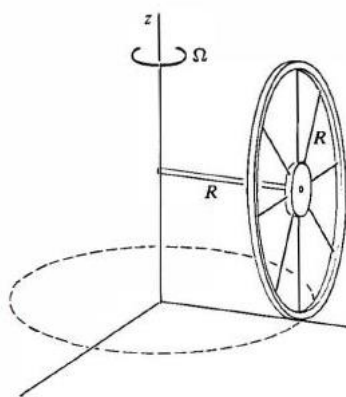
## PHY 101

Q1. A thin hoop of mass  $M$  and radius  $R$  rolls without slipping about the  $z$  axis. It is supported by an axle of length  $R$  through its centre, as shown. The hoop circles around the  $z$  axis with angular velocity  $\Omega$ .

(a) What is the instantaneous angular velocity  $\omega$  of the hoop?

(b) What is the angular momentum  $L$  of the hoop? Is  $L$  parallel to  $\omega$ ?

(Note: the moment of inertia of the hoop for an axis along its diameter is  $\frac{1}{2}MR^2$ .)



Q2. A bowling ball of mass  $4.0\text{ kg}$ , a moment of inertia of  $1.6 \times 10^{-2} \text{ kgm}^2$  and a radius of  $0.10\text{ m}$ . If it rolls down the lane without slipping at a linear speed of  $4\text{ m/s}$ , what is its total energy?

Q3. A  $0.250\text{-kg}$  object ( $m_1$ ) is slid on a frictionless surface into a dark room, where it strikes an initially stationary object with mass of  $0.400 \text{ kg}$  ( $m_2$ ). The  $0.250\text{-kg}$  object emerges from the room at an angle of  $45.0^\circ$  with its incoming direction. The speed of the  $0.250\text{-kg}$  object is originally  $2.00 \text{ m/s}$  and is  $1.50 \text{ m/s}$  after the collision. Calculate the magnitude and direction of the velocity ( $v_2'$  and  $\vartheta_2$ ) of the  $0.400\text{-kg}$  object after the collision.

Q4. A meteor enters Earth's atmosphere as shown in fig. and is observed by someone on the ground before it burns up in the atmosphere. The vector  $\vec{r} = 25 \text{ km } \hat{i} + 25 \text{ km } \hat{j}$  gives the position of the meteor with respect to the observer. At the instant the observer sees the meteor, it has linear momentum  $\vec{p} = (15.0 \text{ kg})(-2.0 \text{ km/s } \hat{j})$ , and it is accelerating at a constant  $2.0 \text{ m/s}^2 (-\hat{j})$  along its path, which for our purposes can be taken as a straight line. What is the angular momentum of the meteor about the origin, which is at the location of the observer?

