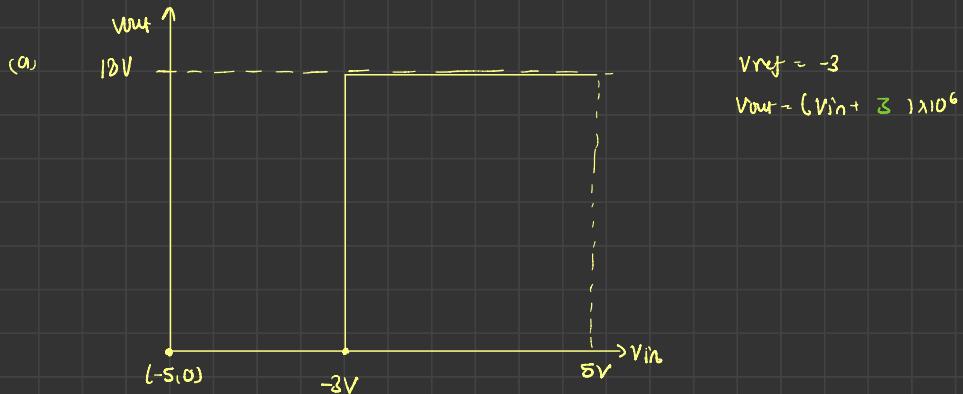


Q1

$$V_{out} = (V_+ - V_-) A$$

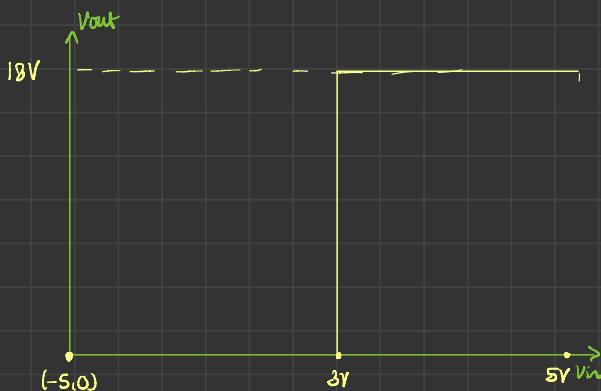
$$= (V_{in} - V_{ref}) \times 10^6$$

$$V_{out} = (V_{in} - V_{ref}) \times 10^6 \quad -5V \leq V_{in} \leq +5V$$

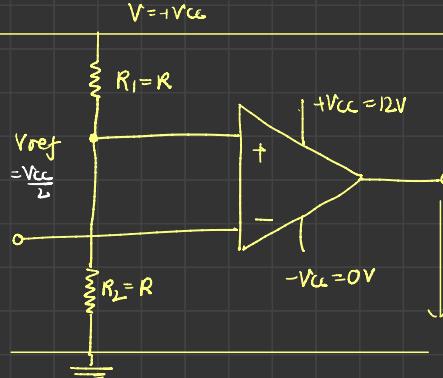


(b)  $V_{out} = (V_{in} - 3) \times 10^6$

$$-5V \leq V_{in} \leq +5V$$



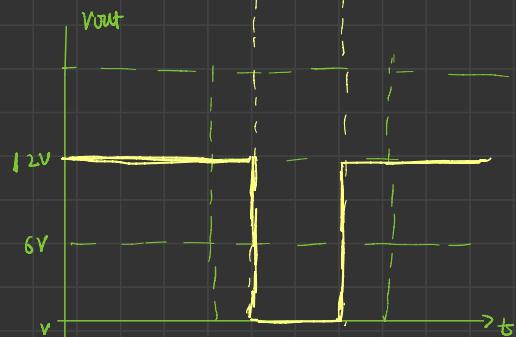
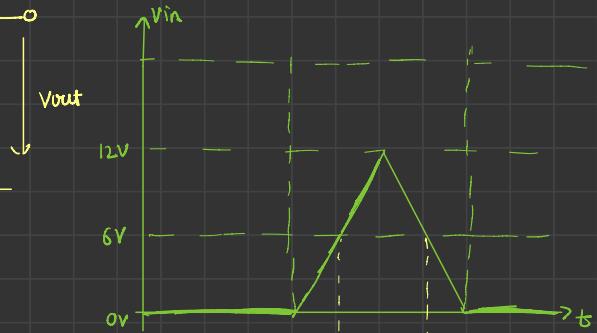
Q2



$$V_{out} = (V_{ref} - V_{in}) \times A_{vA}$$

$$V_{out} = (V_{ref} - V_{in}) \times 10^6$$

$$V_{out} = (6 - V_{in}) \times 10^6$$



Q2

$$T_{ON} = 0.693(R_A + R_B) \times C_{ext}$$

$$= 0.693(2.2 + 4.7) \times 10^3 \times 0.022 \times 10^{-6}$$

$$= 1.052 \times 10^{-4} \text{ s}$$

$$T_{OFF} = 0.693 R_B \times C_{ext}$$

$$= 0.693 \times 4.7 \times 10^3 \times 0.022 \times 10^{-6}$$

$$T_{OFF} = 7.165 \times 10^{-5} \text{ s}$$

$$T = T_{ON} + T_{OFF} = 1.052 \times 10^{-4} + 7.165 \times 10^{-5}$$

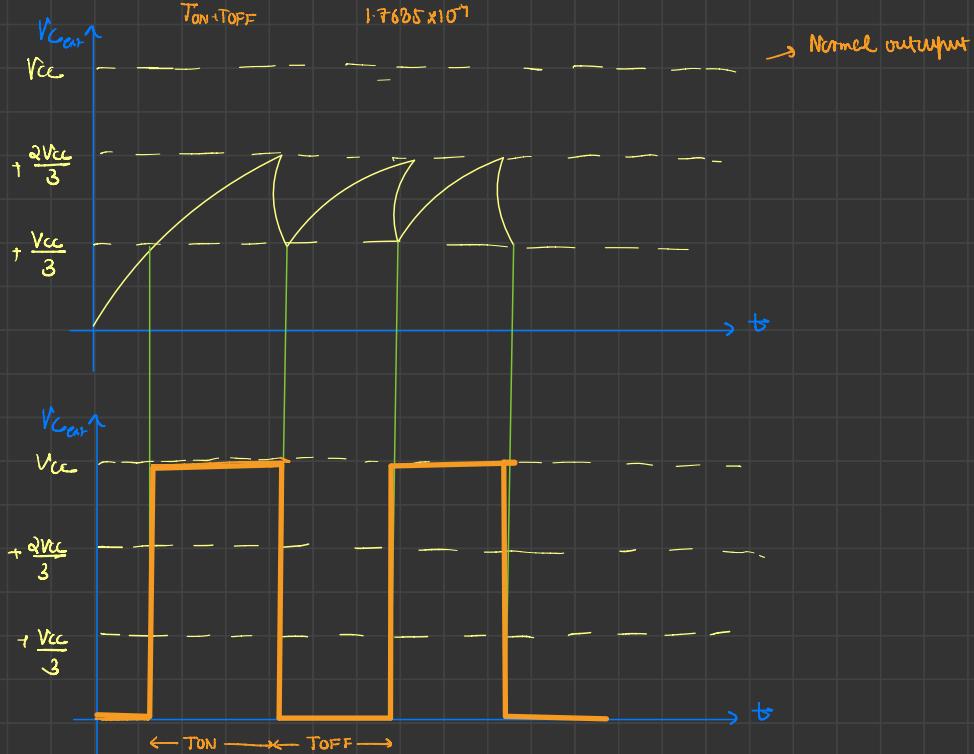
$$= 1.7685 \times 10^{-4} \text{ s}$$

$$f = \frac{1}{T} = 5654.311 \text{ Hz}$$

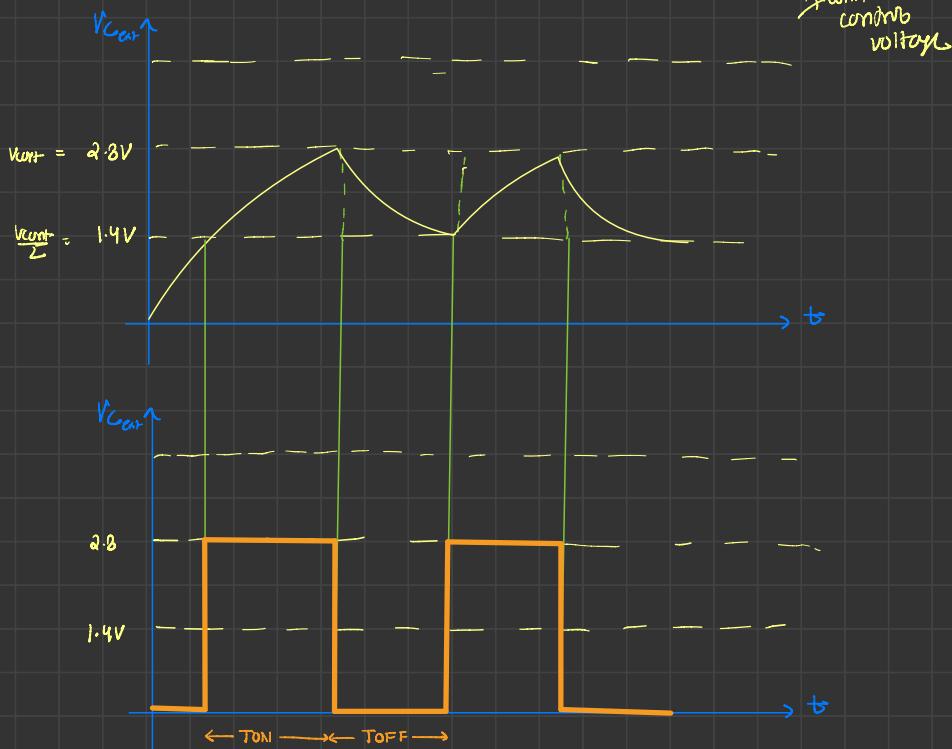
T

$$= 5.6 \text{ kHz}$$

$$\text{Duty cycle} = \frac{T_{ON}}{T_{ON} + T_{OFF}} \times 100 = \frac{1.052 \times 10^{-4}}{1.7685 \times 10^{-4}} \times 100 = 59.48\%$$



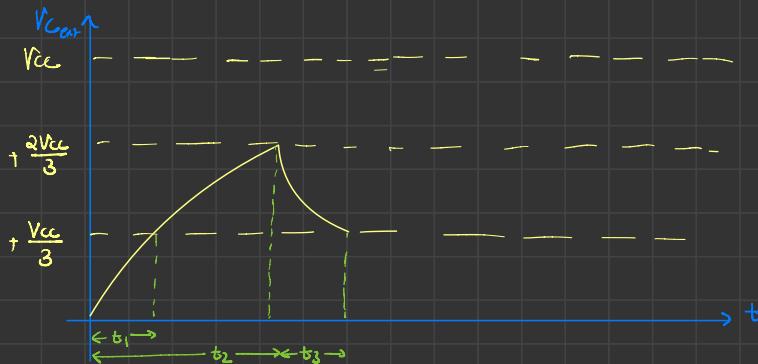
With control pin at 2.8V



## Charging of a capacitor

$$\text{Charging} = V_C(t) = V_{CC} \left[ 1 - \exp(-t/\tau_2) \right] \quad \begin{matrix} \nearrow \text{max voltage} \\ \downarrow \text{charging} \end{matrix}$$

$$V_d(t) = V_{max} \exp(-t/\tau_d) \quad \begin{matrix} \circ \\ \downarrow \text{discharging} \end{matrix}$$



$$T_C = (R_A + R_B)C$$

$$T_d = R_B C$$

Charging

For  $t_1$ ,

$$\frac{V_{CC}}{3} = V_{CC} \left[ 1 - \exp\left(\frac{t_1}{T_C}\right) \right]$$

For  $t_2$ ,

$$\frac{2V_{CC}}{3} = V_{CC} \left[ 1 - \exp\left(\frac{-t_2}{T_C}\right) \right]$$

$$\frac{1}{3} = 1 - \exp\left(\frac{-t_1}{T_C}\right)$$

$$\frac{2}{3} = 1 - \exp\left(\frac{-t_2}{T_C}\right)$$

$$\exp\left(\frac{-t_1}{T_C}\right) = 2/3$$

$$\exp\left(\frac{-t_2}{T_C}\right) = 1/3$$

Taking log on both sides

For discharging,

$$\frac{V_{CC}}{3} = \frac{2V_{CC}}{3} \exp\left(-\frac{t_3}{T_d}\right)$$

$$\frac{1}{3} = \frac{2}{3} \exp\left(-\frac{t_3}{T_d}\right)$$

$$\frac{1}{2} = \exp\left(-\frac{t_3}{T_d}\right)$$

$$+\ln 2 = -\frac{t_3}{T_d}$$

$$t_3 = T_d \ln 2$$

$$t_3 = \ln 2 R_B C$$

$$T_d = R_B C$$

$$-\frac{t_1}{T_C} = \ln(2/\beta)$$

$$-\frac{t_2}{T_C} = \ln(1/\beta)$$

$$t_1 = T_C \ln(2/\beta)$$

$$t_2 = T_C \ln(1/\beta)$$

$$T_{ON} = t_2 - t_1 = T_C (\ln(2) - \ln(1/\beta))$$

$$= T_C \ln(2\beta)$$

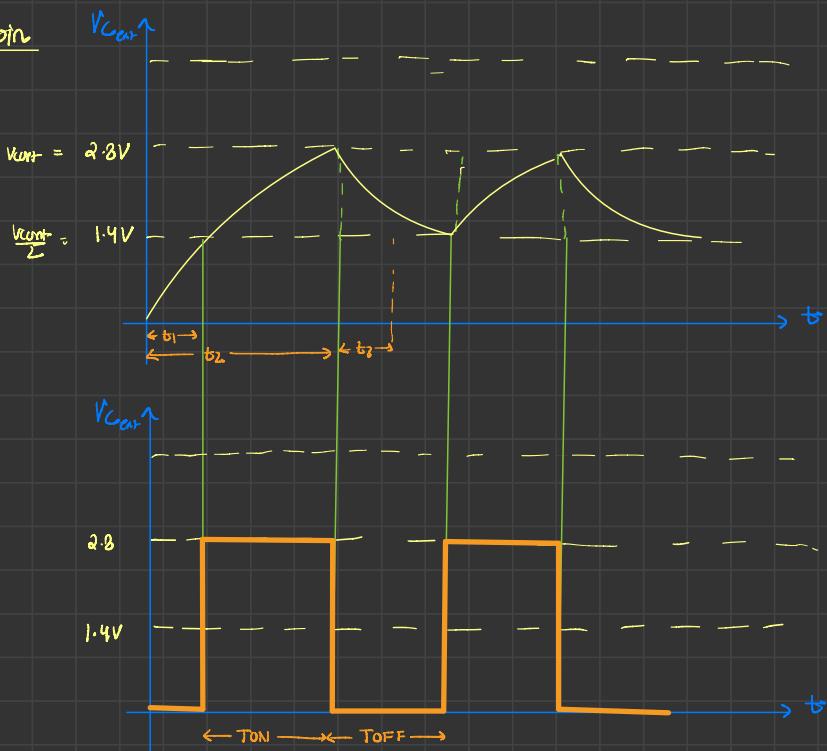
=

$$T_{ON} = T_C \ln(2\beta)$$

$$T_{ON} = \ln 2 (R_A + R_B) C$$

$$T_C = (R_A + R_B) C$$

For control pin



For charging of capacitor

$$t_1 = 0 \rightarrow \frac{V_{\text{final}}}{2}$$

$$V(t_1) = V_{\text{CC}} \left[ 1 - \exp\left(-\frac{t_1}{T_C}\right) \right]$$

$$\frac{V_{\text{final}}}{2} = V_{\text{CC}} \left[ 1 - \exp\left(-\frac{t_1}{T_C}\right) \right]$$

$$1.4 = 5.5 \left[ 1 - \exp\left(-\frac{t_1}{T_C}\right) \right]$$

$$0.2545 = 1 - \exp\left(-\frac{t_1}{T_C}\right)$$

$$\exp\left(-\frac{t_1}{T_C}\right) = 0.7454$$

$$-\frac{t_1}{T_C} = \ln(0.7454)$$

$$-\frac{t_1}{T_C} = -0.2937$$

$$t_1 = 0.2937 T_C$$

For  $t_2$

$$V(t) = V_{\text{CC}} \left[ 1 - \exp\left(-\frac{t}{T_C}\right) \right]$$

$$2.8 = 5.5 \left[ 1 - \exp\left(-\frac{t_2}{T_C}\right) \right]$$

$$0.509 = 1 - \exp\left(-\frac{t_2}{T_C}\right)$$

$$\exp\left(-\frac{t_2}{T_C}\right) = 0.491$$

$$-\frac{t_2}{T_C} = -0.711$$

$$t_2 = 0.711 T_C$$

$$T_{\text{ON}} = t_2 - t_1 = 0.711 T_C - 0.2937 T_C$$

$$= 0.418 T_C$$

$$T_C = (R_A + R_B) C$$

$$\boxed{T_{\text{ON}} = 0.418(R_A + R_B)C}$$

For discharging,

$$V(t) = V_{\text{max}} \left( \exp\left(-\frac{t_3}{T_D}\right) \right)$$

$$1.4 = 2.8 \left( \exp\left(-\frac{t_3}{T_D}\right) \right)$$

$$\frac{1}{2} = \exp\left(-\frac{t_3}{T_D}\right)$$

$$-\ln 2 = -t_3/T_D$$

$$\text{new duty cycle} = \frac{T_{\text{ON}}}{V}$$

$$t_3 = \ln 2 \tau_d$$

$$\tau_d = R_B C$$

$$t_3 = 0.693 R_B C$$

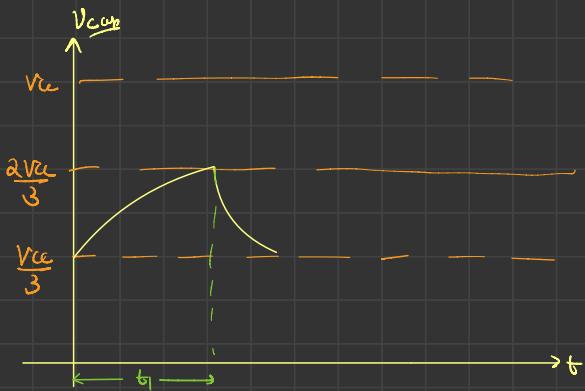
For monostable multivibrator

For charging

$$V(t) = V_{cc} \left[ 1 - \exp\left(-\frac{t}{\tau_c}\right) \right]$$

$$\text{here } \tau_c = RC$$

$$\frac{2V_{cc}}{3} = V_{cc} \left( 1 - \exp\left(-\frac{t_1}{\tau_c}\right) \right)$$



$$\exp\left(-\frac{t_1}{\tau_c}\right) = \frac{1}{3}$$

Taking log on both sides

$$-\frac{t_1}{\tau_c} = -\ln 3$$

$$t_1 = \tau_c \ln 3$$

$$\tau_{on} \approx 1.1 \tau_c$$

