

$$(a) \quad V_0 = \frac{Z_2}{Z_1 + Z_2} V_i \quad Z_1 = R + jX_L \quad Z_2 = jX_C$$

$$\frac{V_0}{V_i} = \frac{-jX_C}{R + jX_L - jX_C} =$$

$$\frac{V_0}{V_i} = \frac{-j/\omega C}{R + j(\omega L - \frac{1}{\omega C})} = \frac{-j}{\omega C(R + j(\omega L - \frac{1}{\omega C}))}$$

$$\frac{V_0}{V_i} = \frac{-j}{\omega CR + j(\omega^2 LC - 1)} \times \frac{j}{j}$$

$$\frac{V_0}{V_i} = \frac{+1}{1 - \omega^2 LC + j\omega CR}$$

$$V_0 = \frac{V_i}{1 - \omega^2 LC + j\omega CR}$$

$$H(j\omega) = \frac{1}{1 - \omega^2 LC + j\omega CR} \quad \text{and} \quad |H(j\omega)| = \frac{1}{\sqrt{(1 - \omega^2 LC)^2 + (\omega CR)^2}}$$

Resonance occurs when the imaginary part of the denominator is zero

$$\omega L - \frac{1}{\omega C} = 0$$

$$\Rightarrow \omega_0 = \frac{1}{\sqrt{LC}} \quad \text{or} \quad f_0 = \frac{1}{2\pi\sqrt{LC}}$$

$$f_{\text{res}} = \frac{1}{1 - \omega^2 LC + j\omega CR}$$

$$\frac{\omega_0 R}{\sqrt{\omega_0^2 LC}}$$

at  $\omega = \omega_0$

$$\text{gain} = \frac{1}{1 - j\omega CR} = \frac{1}{j\omega CR}$$

$$\left| \frac{V_o}{V_i} \right| = \frac{1}{\omega CR}$$

(a)  $f_0 = \frac{1}{2\pi\sqrt{LC}} = \frac{1}{2\pi \times 10^{-3} \times 0.1 \times 10^{-6}} = 15923.566 \text{ Hz}$

gain at  $f_0$

$$\left| \frac{V_o}{V_i} \right| = \frac{1}{\omega_0 RC} = \frac{1}{2\pi \times 10^{-3} \times 0.1 \times 10^{-6} \times 6} = 265,392.78$$

$$\text{(b)} \quad Q = \frac{\chi_L}{R} = \frac{15923.566 \times 10^3}{6} = \underline{\underline{2.654}}$$

(b) For corner frequencies

$$|H(j\omega)| = \frac{1}{\sqrt{2}}$$

On applying this eqn  $\rightarrow \omega_{c1}, \omega_{c2}$

$$\omega_{c1,2} = \omega_0 \pm \frac{R}{2L}$$

and

$$\text{Band width } (\Delta\omega) = \frac{R}{L}$$

$$\omega_1 = \omega_0 + \frac{R}{2L}$$

$$= 10^5 + \frac{6}{2 \times 10^{-3}}$$

$\rightarrow$  convert into Hz

$$\omega_1 = 10.3 \times 10^3 \text{ rad/s}$$

$$\omega_2 = 97 \times 10^3 \text{ rad/s}$$

$$\text{Bandwidth} = \frac{R}{L} = \frac{6}{10^{-3}} = 6000 \text{ Hz}$$

$$(c) \quad \Theta = -\tan^{-1} \left( \frac{\omega CR}{1 - \omega^2 LC} \right) \quad CR = 6 \times 0.1 \times 10^{-6}$$

$$\Theta = -\tan^{-1} \left( \frac{\omega \times 6 \times 10^{-7}}{1 - \omega^2 \times 10^{-10}} \right) \quad LC = 0.1 \times 10^{-6} \times 10^{-3}$$

at higher cutoff frequency

$$\Theta = -\tan^{-1} \left( \frac{0.0618}{-0.0609} \right)$$

$$= \tan^{-1}(1.0147)$$

$$\Theta = 45.42^\circ \text{ (lag)}$$

at lower cutoff freq

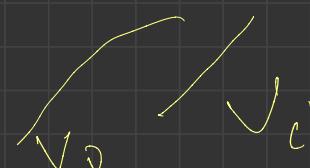
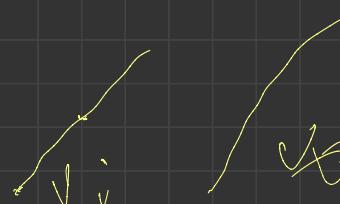
$$\Theta = -\tan^{-1} \left( \frac{47 \times 10^3 \times 6 \times 10^{-7}}{1 - (97 \times 10^3)^2 \times 10^{-10}} \right)$$

$$\Theta = -44.56^\circ \text{ (lag)}$$

in this configuration  
output voltage  
always lags after  
input voltage

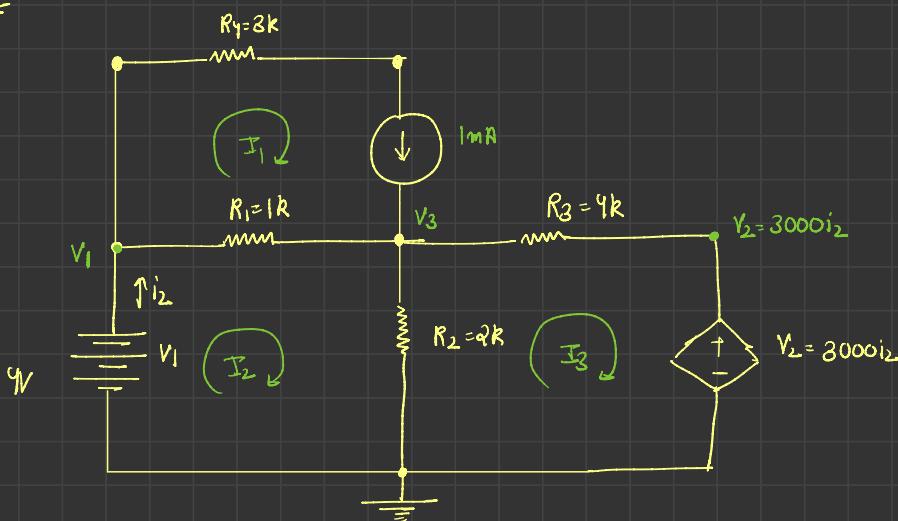
$\omega \rightarrow \infty$

$\omega \rightarrow 0$



Q2)

(a)



$$I_1 = 1\text{mA}$$

In mesh 2,

$$10^3(I_2 - I_1) - 2 \times 10^3(I_2 - I_3) + 4 = 0$$

$$I_2 - I_1 - 2I_2 + 2I_3 + 4 \times 10^{-3} = 0$$

$$-I_2 + 2I_3 + 3 \times 10^{-3} = 0 \quad \text{(i)}$$

In mesh 3,

$$4 \times 10^3 I_3 - 3000 I_2 - 2 \times 10^3(I_3 - I_2) = 0$$

$$4I_3 - 3I_2 - 2I_3 + 2I_2 = 0$$

$$-5I_2 + 2I_3 = 0 \quad \text{(iii)}$$

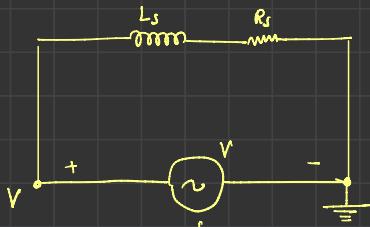
On solving (i) and (iii)

$$I_2 = -7.5 \times 10^{-4} \text{ A} \quad I_3 = -1.875 \times 10^{-3} \text{ A}$$

$$\text{Power dissipated in } R_s = (+1.875 \times 10^{-3} - 7.5 \times 10^{-4}) \times 2 \times 10^3$$

$$= 2.25 \text{ Watt}$$

(b)



Impedance of series LCR circuit

$$Z_1 = R_s + jX_s$$

$$Z_1 = R_s + jY_s$$

Converting admittance of parallel circuit into admittance

$$Y_b = \frac{1}{Z_1} = \frac{1}{R_s + jX_s} = \frac{R_s - jX_s}{R_s^2 + X_s^2} \quad (\text{on rationalizing})$$

$$Y_b = Z_2$$

$$\frac{R_s}{R_s^2 + X_s^2} - j\frac{X_s}{R_s^2 + X_s^2} = \frac{1}{R_p} + \frac{j}{jX_p}$$

$$\frac{R_s}{R_s^2 + X_s^2} + j\frac{X_s}{R_s^2 + X_s^2} = \frac{1}{R_p} + \frac{j}{jX_p}$$

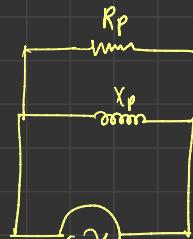
$$\Rightarrow R_p = \frac{R_s^2 + X_s^2}{R_s}$$

$$X_p = \frac{R_s^2 + X_s^2}{X_s}$$

$$\text{Moreover } X_s = \omega L_s$$

$$R_p = \frac{R_s^2 + (\omega L_s)^2}{R_s}$$

$$\omega L_p = \frac{R_s^2 + (\omega L_s)^2}{\omega L_s}$$

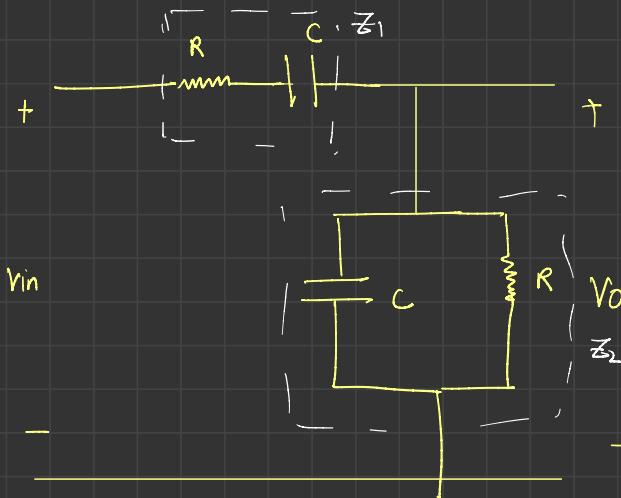


Impedance of parallel LCR circuit

$$Z_p = R_p \parallel jX_p$$

$$Z_p = \frac{1}{\frac{1}{R_p} + \frac{1}{jX_p}}$$

Q3



$$Z_1 = R + \frac{1}{j\omega C}$$

$$Z_2 = \frac{R(j\omega L)}{R + \frac{1}{j\omega C}}$$

$$Z_1 = \frac{1 + j\omega CR}{j\omega C}$$

$$Z_2 = \frac{-R}{j\omega CR + 1}$$

$$\frac{V_o}{V_{in}} = \frac{R}{1 + j\omega CR} \times \frac{1}{\frac{j\omega CR}{1 + j\omega CR} + \frac{R}{1 + j\omega CR}}$$

$$= \frac{R \times (1 + j\omega CR) \times j\omega C}{(1 + j\omega CR) ((1 + j\omega CR)^2 + j\omega C)}$$

$$= \frac{j\omega RC}{1 - \omega^2 C^2 R^2 + 2j\omega CR + j\omega CR} = \frac{1}{\frac{1}{j\omega RC} - \frac{\omega RC}{j} + 3} = \frac{1}{3 + \frac{j}{\omega RC} \left( \omega RC - \frac{1}{\omega RC} \right)}$$

$$H(j\omega) = \frac{j\omega RC}{1 - \omega^2 C^2 R^2 + 3j\omega CR}$$

$$|H(j\omega)| = \sqrt{\frac{\omega RC}{\left(1 - \omega^2 C^2 R^2\right)^2 + 9\omega^2 C^2 R^2}}$$

$$\theta = -\tan^{-1} \left( \frac{\omega RC - \frac{1}{\omega RC}}{3} \right)$$

For  $\theta=0^\circ$

$$\omega_{RC} = \frac{1}{RC}$$

$$\omega^2 = \frac{1}{R^2 C^2}$$

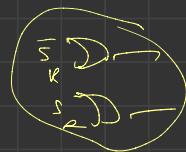
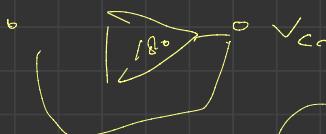
$$\omega = \frac{1}{RC} \quad \text{for max } \omega \quad \theta=0^\circ \quad = f = \frac{1}{2\pi RC}$$

### Wein bridge oscillator

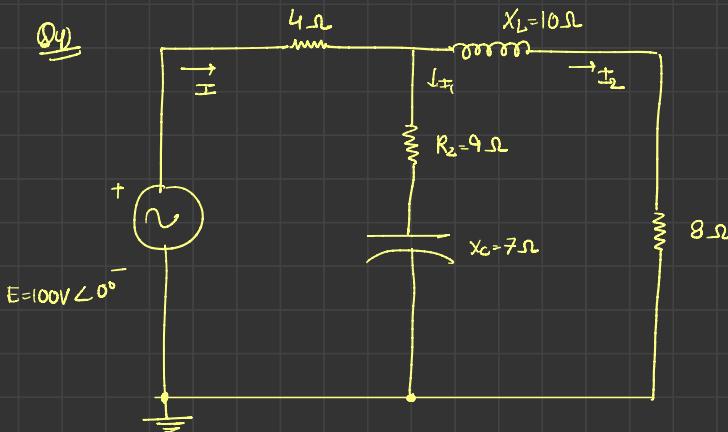
$$\text{At } \omega = \omega_0 = \frac{1}{RC}$$

$$\frac{V_o}{V_{in}} = \frac{1}{3}$$

$$Q = V_C \angle V_o \quad \text{lag}$$



Q4



$$(a) \quad Z_T = (8 + j10) \parallel (9 - j7) + 4$$

$$\frac{142 + 34j}{17 + j3} + 4$$

$$Z_T = 12.44 + 0.5j$$

$$(b) \quad I = \frac{V}{Z_T} = \frac{100 \angle 0^\circ}{12.45 \angle 2.87^\circ} = 8.032 A \angle -2.347^\circ$$

$$I_1 = \frac{8 + j10}{17 + j3} \times (8.032 \angle -2.347^\circ)$$

$$I_1 = 4.631 A \angle -8.7486^\circ$$

$$I_2 = \frac{9 - j7}{17 + j3} \times (8.032 \angle -2.347^\circ)$$

$$I_2 = 4.584 A \angle -2.669^\circ$$

$$(C) P = I_{\text{rms}}^2 \times R$$
$$= (4.584)^2 \times 8$$
$$= 168.104 \text{ Watt}$$

$$(d) |\text{Reactive Power}| = V_{\text{rms}} \times I_{\text{rms}} \times \sin \phi$$
$$= 100 \times 8.082 \times \sin 90^\circ (\pm 2.847)$$
$$|\text{Reactive Power}| = 82.892 \text{ Watt}$$

$$(e) \text{Power factor} = \cos(2.847)$$
$$= \underline{\underline{0.499}}$$

Q1 (d)

$$\underline{\text{Q2}} \quad P_{\max} = I_{\text{rms}}^2 \times R$$

$$= \frac{V_{\text{rms}}^2}{R} = \frac{100^2}{5}$$

$$= \frac{100 \times 100}{5} = 2000 \text{ Watt}$$

Q3 (c)

$$\frac{100 \times 5}{100 + 5} = \frac{100}{50} = 2$$

$$\underline{\text{Q4}} \quad \omega = \frac{1}{\sqrt{LC}}$$

Q5 (d)

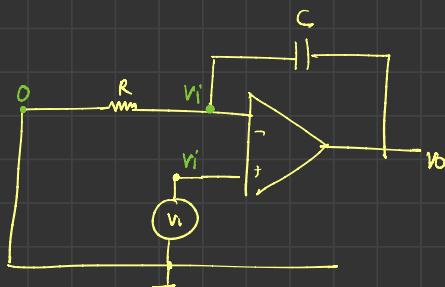
$$\underline{\text{Q5}} \quad E = 20 + j84 \angle 30^\circ$$

$$Z = j10$$

$$I = \frac{E}{Z} = 20.784 \angle -60^\circ$$

$$I_{\text{rms}} = 20.784 A$$

Q6



Applying nodal analysis

$$\frac{Vi - 0}{R} = \frac{Vi - V_o}{j\omega C}$$

$$\frac{Vi}{R} = (Vi - V_o)j\omega C$$

$$\frac{Vi}{j\omega CR} = Vi - V_o$$

$$V_o = (Vi - \frac{Vi}{j\omega CR})$$

$$V_o = Vi \left( 1 - \frac{1}{j\omega CR} \right)$$

$$V_o = Vi \left( j\omega CR - 1 \right)$$

$$\frac{V_o}{V_i} = \frac{j\omega CR - 1}{j\omega CR}$$

$$|H(j\omega)| = \sqrt{1 + \omega^2 C^2 R^2}$$

$$|H(j\omega)| = \sqrt{(\omega CR)^2 + 1}$$

$\omega$  is already static  $\omega = 0$

$$\omega = \frac{1}{RC} = \frac{\sqrt{2}}{y}$$

$$|H(j\omega)| =$$

Q3

$$5 + 10||5$$

$$5 + \frac{50 - 10}{15} =$$

$$\frac{15 + 10}{3} = \underline{\underline{25/3}}$$

Q4

10V