

## Tutorial 3

### Monsoon 2024 PHY-101

**Q1:** A bead moves along the spoke of a wheel at constant speed 'u' m/s. The wheel rotates with uniform angular velocity  $\dot{\theta} = \Omega$  radians per second about an axis fixed in space. At  $t = 0$  the spoke is along the x axis and the bead is at the origin. Find the velocity of the bead at time  $t$  in both polar and cartesian coordinates.

**Q2.** Consider a particle which feels the angular acceleration of the form  $a_\theta = 3\dot{r}\dot{\theta}$ . Show that

$\dot{r} = \sqrt{Ar^4 + B}$  where A and B are constants.

**Q3** A particle moves so that its position vector is given by  $\mathbf{r} = \cos\omega t\hat{i} + \sin\omega t\hat{j}$  where  $\omega$  is a constant. Show that (a) the velocity  $\mathbf{v}$  of the particle is perpendicular to  $\mathbf{r}$ . (b) the acceleration  $\mathbf{a}$  is directed towards the origin and has a magnitude proportional to the origin, (c)  $\mathbf{r} \times \mathbf{v} = \text{Constant vector}$ .

**Q4** In planar polar co-ordinates, an object's position at time  $t$  is given as  $(r, \theta)$   
 $= (e^t \text{ meter}, \sqrt{8} t \text{ radian})$

(a) Find radial velocity, tangential velocity and speed of particle at  $t=0$

(b) Find radial acceleration, tangential acceleration and magnitude of acceleration at  $t=0$