Tutorial 11 Solutions

PHY 101

Q1. One mole of a gas is contained in a cube of side 0.2m If these molecules, each of mass $5 \times 10^{-26} \text{kg}$, move with translational speed 483ms^{-1} , calculate the pressure exerted by the gas on the sides of the cube.

Sol:One mole of a gas is contained in a cube of side 0.2m If these molecules, each of mass kg, move

with translational speed 483m, calculate the pressure exerted by the gas on the sides of the cube.

Solution: The change in the momentum of the gaseous molecule between any two successive collisions with a wall of the container will be

$$\Delta p_x = 2mv_x = 2 \times (5 \times 10^{-26} \text{ kg}) \times (483 \text{ms}^{-1}) = 4.83 \times 10^{-23} \text{ Ns}$$

The time between successive collision on the same face

$$\triangle t = \frac{2L}{V_x} = -\frac{2 \times 0.2m}{483ms^{-1}} = 8.3 \times 10^{-4} s$$

Hence the rate of change of momentum of one molecule

$$\frac{\triangle p_x}{\triangle t} = \frac{4.83 \times 10^{-23} \text{ Ns}}{8.3 \times 10^{-4} \text{s}} = 0.582 \times 10^{-19} \text{ N}$$

Therefore, the total force exerted by all the molecules of the gas on a wall is

$$f_x = (0.582 \times 10^{-19} \text{ N}) \times (6 \times 10^{23}) = 3.49 \times 10^4 \text{ N}$$

Hence average pressure exerted by all the molecules of the gas on the walls of the container

$$P = \frac{3.49 \times 10^4 \text{ N}}{3 \times 4 \times 10^{-2} m^2} = 2.9 \times 10^5 Nm^{-2}$$

Q2. A gas is at temperature 80°C and pressure $5 \times 10^{-10} N$ m-2. What is the number of molecules per m³ if Boltzmann's constant is 1.38×10^{-23} J K-1.

Sol:

Temperature of gas
$$T = 80^{\circ}C = 80 + 273 = 353K$$

Pressure of gas $P = 5 \times 10^{-10} \text{ Nm}^{-2}$

Boltzmann's constant $k = 1.38 \times 10^{-23} \text{ J}k^{-1}$

Volume of gas $V = 1 \text{ m}^3$

No. of molecules n = ?

$$n = \frac{\text{PV}}{k\text{T}} = \frac{5 \times 10^{-10} \times 1}{1.38 \times 10^{-23} \times 353} = \frac{5 \times 10^{-10}}{487 \times 10^{-23}}$$

Ans: 1.02×10^{11}

Q3. If a mixture of n_1 moles of monatomic gas and n_2 moles of diatomic gas has $\gamma = 1.5$, then what will be the ratio of n_1 and n_2 ? Sol:

Sol. The average number of degrees of freedom per molecule

$$f = \frac{\text{total number of degrees of freedom}}{\text{total number of molecules}} = \frac{n_1 N_A f_1 + n_2 N_A f_2}{n_1 N_A + n_2 N_A}.....(1)$$

where N_A is the Avogadro constant, and f_1 and f_2 are degrees of freedoms of monatomic and diatomic gases

Hence,
$$f_1 = 3$$
, $f_2 = 5$

From Eq. (1) we can write

$$f = \frac{n_1 f_1 + n_2 f_2}{n_1 + n_2} = \frac{3n_1 + 5n_2}{n_1 + n_2} \dots (2)$$

Also,
$$\gamma = 1 + 2/f = 1.5$$

$$\Rightarrow f = 4$$

Using Eq. (2), we find

$$f = \frac{3n_1 + 5n_2}{n_1 + n_2} = 4$$

$$\rightarrow 3n_1 + 5n_2 = 4n_1 + 4n_2$$

$$\rightarrow n_1/n_2 = 1$$