

**Department of Physics, Shiv Nadar Institution of Eminence**  
**Spring 2025**  
**PHY102: Introduction to Physics-II**  
**Tutorial – 13**

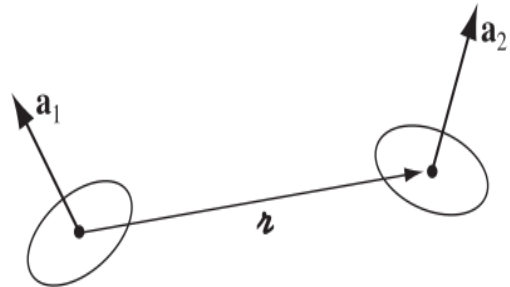
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1. Two tiny wire loops, with areas  $\mathbf{a}_1$  and  $\mathbf{a}_2$ , are situated as shown in the figure below.

(a) Find their mutual inductance.

[Hint: Treat them as magnetic dipoles]

(b) Suppose a current of magnitude  $I_1$  is flowing in loop 1, and we propose to turn on a current of magnitude  $I_2$  in loop 2. How much work must be done, against the mutually induced emf, to maintain the current magnitude  $I_1$  flowing in loop 1?



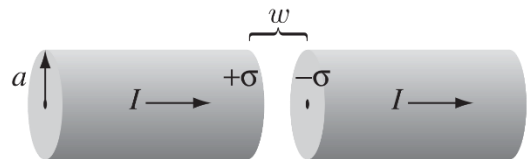
2. A sphere of radius  $a$  is so magnetized that its magnetization at any inside point  $(x,y,z)$  with respect to its Centre as origin is given by

$$\vec{M} = a_1 x^2 \hat{i} + (a_2 y^2 + b_2) \hat{j}$$

Find the magnetization current densities.

3. Suppose a long cylinder of radius  $a$  carries a magnetization  $\vec{M} = Kr^2 \hat{\theta}$ , where  $K$  is a constant,  $r$  is the distance from the axis and  $\hat{\theta}$  is the usual unit vector in  $(r, \theta, z)$  cylindrical coordinate system. Find the magnetic field due to  $\vec{M}$  both inside and outside the cylinder.

4. A fat wire, radius  $a$ , carries a constant current  $I$ , uniformly distributed over its cross section. A narrow gap in the wire, of width  $w \ll a$ , forms a parallel-plate capacitor, as shown in the figure. Find the magnetic field in the gap, at a distance  $s < a$  from the axis.



5. Suppose the circuit in the figure has been connected for a long time when suddenly, at time  $t = 0$ , switch  $S$  is thrown from  $A$  to  $B$ , bypassing the battery.

(a) What is the current at any subsequent time  $t$ ?

(b) What is the total energy delivered to the resistor?

(c) Show that this is equal to the energy originally stored in the inductor.

