

⊛ Experiment : Rolling a six-face dice.

6 possible outcomes : $\{1, 2, 3, 4, 5, 6\} \rightarrow$ sample space

Subset of sample space $\{1, 3, 5\}$ called events.

⊛ Given the sample space S of an experiment, probability of an event $E \subseteq S$ is $P(E)$

where impossible events are probability 0,

certain events are probability 1

$$\rightarrow P(\emptyset) = 0$$

$$P(S) = 1$$

⊛ Calculating P for event $E \subseteq$ sample space S

$$P(E) = \frac{|E|}{|S|} = \frac{\text{Num. in events}}{\text{Num. in sample space}}$$

⊛ If events are mutually exclusive i.e. $E_1 \cap E_2 = \emptyset$

$$P(E_1 \cup E_2) = P(E_1) + P(E_2)$$

⊛ Ex: Two dice are rolled. P of each sum?

$$|E| = 6 \times 6 = 36$$

$$1 \text{ way of } 2 (1+1) \rightarrow P(2) = \frac{1}{36}$$

$$2 \text{ way of } 3 (1+2, 2+1) \rightarrow P(3) = \frac{2}{36}$$

...

$$1 \text{ way of } 12 (6+6) \rightarrow P(12) = \frac{1}{36}$$

⊗ Misconceptions: Gambler's fallacy

If events are independent, results are independent

E.g. After getting 5 tails in a row,

$P(\text{tail})$ is $\frac{1}{2}$, not less.