# Random forests STAT 471

**November 9, 2021** 

### Where we are

Unit 1: Intro to modern data mining

**Unit 2:** Tuning predictive models

Unit 3: Regression-based methods

Unit 4: Tree-based methods

Unit 5: Deep learning

Lecture 1: Growing decision trees

Lecture 2: Tree pruning and bagging

**Lecture 3:** Random forests

**Lecture 4:** Boosting

Lecture 5: Unit review and quiz in class

Homework 4 due the following Wednesday.

### **Recall: Bagging**

#### Bootstrap sample 1

Original training data

			1
Obs ID	X	Y	
1	X <sub>1</sub>	Y <sub>1</sub>	
2	<b>X</b> <sub>2</sub>	<b>Y</b> <sub>2</sub>	1
3	<b>X</b> 3	<b>Y</b> <sub>3</sub>	
4	<b>X</b> <sub>4</sub>	Y <sub>4</sub>	`
5	<b>X</b> <sub>5</sub>	<b>Y</b> <sub>5</sub>	

Obs ID	X	Y
5	<b>X</b> 5	<b>Y</b> <sub>5</sub>
3	<b>X</b> 3	<b>Y</b> <sub>3</sub>
2	<i>X</i> <sub>2</sub>	<b>Y</b> <sub>2</sub>
3	<b>X</b> 3	<b>Y</b> <sub>3</sub>
1	X <sub>1</sub>	Y <sub>1</sub>

 $\longrightarrow T^{*b}$ 

#### Bootstrap sample B

Obs ID	X	Υ
4	<i>X</i> <sub>4</sub>	<b>Y</b> <sub>4</sub>
1	X <sub>1</sub>	Y <sub>1</sub>
1	X <sub>1</sub>	Y <sub>1</sub>
5	<b>X</b> <sub>5</sub>	<b>Y</b> <sub>5</sub>
4	X <sub>4</sub>	Y <sub>4</sub>

Train one tree on the original data

Regression:

$$\hat{f}(X) = \frac{1}{B} \sum_{b=1}^{B} T^{*b}(X)$$

Classification:

$$\hat{f}(X) = \text{mode}(\{T^{*b}(X)\}_{b=1}^{B})$$

### Variance reduction of bagging

The bagging prediction is defined by  $\hat{f}(X) = \frac{1}{B} \sum_{b=1}^{B} T^{*b}(X)$ .

Suppose  $Corr[T^{*b_1}(X), T^{*b_2}(X)] = \rho \in [0,1]$ . Then, we can derive that

$$\mathrm{Var}[\hat{f}(X)] = \frac{1}{B^2} \sum_{b_1 = 1}^{B} \sum_{b_2 = 1}^{B} \mathrm{Cov}[T^{*b_1}(X), T^{*b_2}(X)] \approx \left(\frac{1}{B} + \frac{B-1}{B}\rho\right) \mathrm{Var}[T(X)] \approx \rho \cdot \mathrm{Var}[T(X)],$$

where T(X) is a single decision tree. Take-aways:

Variance of the bagging estimate is row time the variance of a single tree

- The variance is reduced by a factor of  $\rho = \text{Corr}[T^{*b_1}(X), T^{*b_2}(X)]$ , so the less correlated the bootstrapped trees prediction are, the better.
- ullet As long as B is large enough, the variance reduction is about the same.

The bootstrap tree predictions are better

Random forest is just like bagging but with extra step that reduces correlation among trees and further reduces variance

### **Random forests: More variance reduction**

Random forests are the same as bagging, but with one key modification:

At each split point of each tree:

- Randomly sample a subset of  $m \leq p$  features
- Split on the best feature among this subset

Intuition: Sampling features at each split decorrelates the trees, reducing variance and therefore boosting prediction performance.

Hopefully each individual tree is still roughly unbiased even though it has access to a smaller number of features at each split.

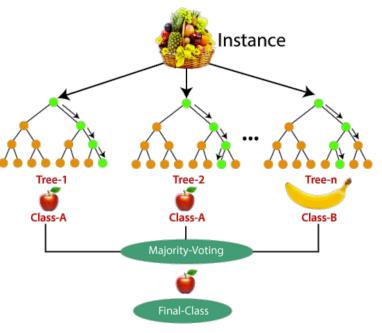


Image source: https://www.section.io/engineering-education/introduction-to-random-forest-in-machine learning/

Note that setting m = p recovers bagging. At every step would be including all features Have to decide which region should split and which

### **Random forests**

For each bootstrap sample, you randomly sample M candidate variables and grow a decision tree, and then you

Parameters: predict same way as bagging

• *B*: number of bootstrap samples

- *m*: number of variables to sample at each split
- criterion to stop splitting, like max number of nodes and/or min samples per node

#### Training:

- Extract *B* bootstrap samples from your training data
- For each bootstrap sample b = 1, ..., B,
  - Grow a decision tree based on the bootstrap sample, randomly sampling m candidate variable to split on at each step, until stopping criterion is met

#### **Prediction:**

• aggregate the decision trees using the mean (for regression) or mode (for classification)

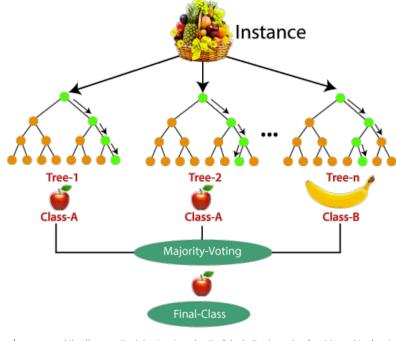


Image source: https://www.section.io/engineering-education/introduction-to-random-forest-in-machine-learni

### A bias-variance trade-off in choosing *m*

If m is larger, the random forest will have lower bias (it can better fit the underlying trend) but higher variance (more correlated trees).

The higher m is, the more similar the set of features the tree is considering

If m is smaller, the random forest will have higher bias (it might not be able to fit the underlying trend as well) but lower variance (less correlated trees).

If m is smaller, not allowing to use all features and trees will be less correlated

Default choices: m = p/3 for regression and  $m = \sqrt{p}$  for classification.

For best predictive performance, m should be tuned.

Random forest, in comparison to deep learning is more plug and play

Final tree is average of predictions of all trees. There is no "super" tree, but B trees that make up the "forest"

### Tuning random forests via out-of-bag error

We usually tune prediction methods via cross-validation. For random forests, there is a clever and computationally faster alternative: out-of-bag error.

The idea behind cross-validation is that we want to using parts of our training data as validation sets. By bootstrapping, random forests already do this!

For each bootstrap sample, define the "bag" to be the set of unique training observations in the sample. Then, predictions based on that tree can be made

Bootstrap sample b

on the out-of-bag (OOB) samples.

When we use bootstrapping, doing something very similar to CV

	•		_
Obs ID	X	Y	
5	<b>X</b> <sub>5</sub>	<b>Y</b> <sub>5</sub>	
3	<i>X</i> <sub>3</sub>	<b>Y</b> 3	$\longrightarrow T^{*b}$
2	<i>X</i> <sub>2</sub>	<b>Y</b> <sub>2</sub>	
3	<i>X</i> <sub>3</sub>	<b>Y</b> <sub>3</sub>	
1	X <sub>1</sub>	Y <sub>1</sub>	

# Tuning random forests via out-of-bag error

We usually tune prediction methods via cross-validation. For random forests, there is a clever and computationally faster alternative: out-of-bag error.

The idea behind cross-validation is that we want to using parts of our training data as validation sets. By bootstrapping, random forests already do this!

For each bootstrap sample, define the "bag" to be the set of unique training observations in the sample. Then, predictions based on that tree can be made

Rootstran sample h

on the out-of-bag (OOB) samples.

L	Jootstrap	Sampi		_
	Obs ID	X	Y	
	5	<b>X</b> 5	<b>Y</b> <sub>5</sub>	
	3	<b>X</b> 3	<b>Y</b> <sub>3</sub>	$T^{*b}$
	2	<i>X</i> <sub>2</sub>	<b>Y</b> <sub>2</sub>	
	3	<i>X</i> <sub>3</sub>	<b>Y</b> <sub>3</sub>	
	1	X <sub>1</sub>	Y <sub>1</sub>	
	4	<b>X</b> <sub>4</sub>	<b>Y</b> <sub>4</sub>	out-of-bag b

### Tuning random forests via out-of-bag error

We usually tune prediction methods via cross-validation. For random forests, there is a clever and computationally faster alternative: out-of-bag error.

The idea behind cross-validation is that we want to using parts of our training data as validation sets. By bootstrapping, random forests already do this!

For each bootstrap sample, define the "bag" to be the set of unique training observations in the sample. Then, predictions based on that tree can be made

on the out-of-bag (OOB) samples.

Bootstrap sample b Obs ID X 5  $X_5$  $Y_5$ 3  $X_3$  $\rightarrow T^{*b} \longrightarrow T^{*b}(X_A)$ Yo 2  $X_2$  $X_3$  $Y_3$  $X_1$  $Y_1$ out-of-bag b  $X_4$ 

Bootstrap sample 1

Obs ID	X	Y	
5	<b>X</b> <sub>5</sub>	<b>Y</b> <sub>5</sub>	
3	<b>X</b> 3	<b>Y</b> <sub>3</sub>	
2	<i>X</i> <sub>2</sub>	Y <sub>2</sub>	
3	<b>X</b> 3	<b>Y</b> <sub>3</sub>	
1	X <sub>1</sub>	Y <sub>1</sub>	

Original	training	data

Obs ID	X	Y
1	X <sub>1</sub>	Y <sub>1</sub>
2	<i>X</i> <sub>2</sub>	<b>Y</b> <sub>2</sub>
3	<b>X</b> 3	<b>Y</b> 3
4	<i>X</i> <sub>4</sub>	Y <sub>4</sub>
5	<b>X</b> <sub>5</sub>	<b>Y</b> <sub>5</sub>

Bootstrap sample B

Obs	ID	X	Y	
4		<i>X</i> <sub>4</sub>	Y <sub>4</sub>	
1		X <sub>1</sub>	Y <sub>1</sub>	*D
1		X <sub>1</sub>	Y <sub>1</sub>	$\longrightarrow T^{*B}$
5		<i>X</i> <sub>5</sub>	<b>Y</b> <sub>5</sub>	
4		<i>X</i> <sub>4</sub>	Y <sub>4</sub>	

Have a bunch of bootstrap samples

Each sample has its own out of bag sample

Bootstrap sample 1

Booton	ap can	י טיקי	
Obs ID	X	Y	
5	<b>X</b> 5	<b>Y</b> <sub>5</sub>	
3	<b>X</b> 3	<b>Y</b> <sub>3</sub>	$\longrightarrow T^{*1}$
2	<i>X</i> <sub>2</sub>	<b>Y</b> <sub>2</sub>	
3	<b>X</b> 3	<b>Y</b> <sub>3</sub>	
1	X <sub>1</sub>	Y <sub>1</sub>	
4	<b>X</b> <sub>4</sub>	<b>Y</b> <sub>4</sub>	out-of-bag

Original	training	data
----------	----------	------

Obs ID	X	Y
1	X <sub>1</sub>	Y <sub>1</sub>
2	<i>X</i> <sub>2</sub>	<b>Y</b> <sub>2</sub>
3	<b>X</b> 3	<b>Y</b> <sub>3</sub>
4	<i>X</i> <sub>4</sub>	Y <sub>4</sub>
5	<i>X</i> <sub>5</sub>	Y <sub>5</sub>

Bootstrap sample B

Obs ID	X	Y	
4	<i>X</i> <sub>4</sub>	Y <sub>4</sub>	
1	X <sub>1</sub>	Y <sub>1</sub>	* <i>p</i>
1	X <sub>1</sub>	Y <sub>1</sub>	$\longrightarrow T^{*B}$
5	<b>X</b> 5	<b>Y</b> <sub>5</sub>	
4	<i>X</i> <sub>4</sub>	Y <sub>4</sub>	

Bootstrap sample 1

	ipie i	ap san	DOOLST
	Y	X	Obs ID
	<b>Y</b> <sub>5</sub>	<b>X</b> 5	5
$T^{*1}$	<b>Y</b> <sub>3</sub>	<b>X</b> 3	3
	<b>Y</b> <sub>2</sub>	<b>X</b> 2	2
	<b>Y</b> 3	<b>X</b> 3	3
	Y <sub>1</sub>	X <sub>1</sub>	1
out-of-bag 1	Y <sub>4</sub>	X <sub>4</sub>	4
-		:	

Original	training	data
----------	----------	------

Obs ID	X	Y
1	X <sub>1</sub>	Y <sub>1</sub>
2	<i>X</i> <sub>2</sub>	<b>Y</b> <sub>2</sub>
3	<i>X</i> <sub>3</sub>	<b>Y</b> <sub>3</sub>
4	X <sub>4</sub>	Y <sub>4</sub>
5	<i>X</i> <sub>5</sub>	Y <sub>5</sub>

Bootstrap sample B

		•	•	
	Obs ID	X	Υ	
	4	<i>X</i> <sub>4</sub>	$Y_4$	
*	1	X <sub>1</sub>	Y <sub>1</sub>	*D
•	1	X <sub>1</sub>	Y <sub>1</sub>	$\longrightarrow T^{*B}$
	5	<b>X</b> <sub>5</sub>	<b>Y</b> <sub>5</sub>	
	4	<i>X</i> <sub>4</sub>	<b>Y</b> <sub>4</sub>	
	2	<b>X</b> <sub>2</sub>	<b>Y</b> <sub>2</sub>	out of box D
	3	<i>X</i> <sub>3</sub>	<b>Y</b> <sub>3</sub>	out-of-bag B

Original training data

 $X_1$ 

 $X_2$ 

*X*<sub>3</sub>

 $X_4$ 

 $X_5$ 

 $Y_1$ 

 $Y_2$ 

*Y*<sub>3</sub>

 $Y_4$ 

 $Y_5$ 

**Obs ID** 

3

4

5

### Bootstrap sample 1

	Y	X	Obs ID
	<b>Y</b> <sub>5</sub>	<b>X</b> 5	5
$\longrightarrow T^{*1}$	<b>Y</b> <sub>3</sub>	<b>X</b> 3	3
	<b>Y</b> <sub>2</sub>	<b>X</b> <sub>2</sub>	2
	<b>Y</b> <sub>3</sub>	<b>X</b> 3	3
	Y <sub>1</sub>	X <sub>1</sub>	1
out of boo	V.	ν,	1

Bootstrap sample B

		-	-	-
	Obs ID	X	Y	
	4	<i>X</i> <sub>4</sub>	Y <sub>4</sub>	
*	1	X <sub>1</sub>	Y <sub>1</sub>	* <i>D</i>
•	1	X <sub>1</sub>	Y <sub>1</sub>	$\longrightarrow T^{*B}$
	5	<b>X</b> 5	<b>Y</b> <sub>5</sub>	
	4	<i>X</i> <sub>4</sub>	<b>Y</b> <sub>4</sub>	
	2	<b>X</b> <sub>2</sub>	<b>Y</b> <sub>2</sub>	out of box P
	3	<i>X</i> <sub>3</sub>	<b>Y</b> <sub>3</sub>	out-of-bag B

#### OOB predictions

Obs ID	X	Y
1	<i>X</i> <sub>1</sub>	<b>Y</b> <sub>1</sub>
2	$X_2$	<b>Y</b> <sub>2</sub>
3	<b>X</b> 3	<b>Y</b> 3
4	<i>X</i> <sub>4</sub>	<b>Y</b> <sub>4</sub>
5	$X_5$	<b>Y</b> <sub>5</sub>

T*1(X)	 <b>T</b> *B( <b>X</b> )	у̂оов
_	 _	Ŷ <sub>1</sub> 008
_	 T*B(X2)	$\hat{\gamma}_2$ 008
_	 T*B(X3)	$\hat{\gamma}_3$ 008
T*1(X4)	 _	$\hat{\gamma}_4$ 008
_	 _	$\hat{\gamma}_5$ 008

#### Bootstrap sample 1

	•	•	
Obs ID	X	Y	
5	<b>X</b> <sub>5</sub>	<b>Y</b> <sub>5</sub>	
3	<b>X</b> 3	<b>Y</b> <sub>3</sub>	$T^{*1}$
2	<b>X</b> <sub>2</sub>	<b>Y</b> <sub>2</sub>	
3	<b>X</b> 3	<b>Y</b> 3	
1	X <sub>1</sub>	Y <sub>1</sub>	
4	<i>X</i> <sub>4</sub>	Y <sub>4</sub>	out-of-bag 1

**Obs ID**  $Y_1$  $X_1$ 

Original training data

2  $X_2$  $Y_2$ 3 *X*<sub>3</sub>  $Y_3$  $Y_4$ 4  $X_4$ 

 $X_5$ 

5

 $Y_5$ 

Bootstrap sample B

* D
$\rightarrow T^{*B}$
of boa D
of-bag B

#### OOB predictions

Obs ID	X	Y
1	$X_1$	<b>Y</b> <sub>1</sub>
2	$X_2$	<b>Y</b> <sub>2</sub>
3	<b>X</b> 3	<b>Y</b> 3
4	<i>X</i> <sub>4</sub>	<b>Y</b> <sub>4</sub>
5	$X_5$	<b>Y</b> <sub>5</sub>

T*1(X)	 <b>T</b> *B( <b>X</b> )	у̂оов
_	 _	$\hat{\gamma}_1$ 00B
_	 T*B(X2)	$\hat{\gamma}_2$ 008
_	 T*B(X3)	$\hat{\gamma}_3$ оов
$T^{*1}(X_4)$	 _	$\hat{\gamma}_4$ 00В
_	 _	$\hat{\gamma}_{5}$ оов

#### **Regression:**

$$\widehat{Y}_i^{OOB} = \text{mean}\{T^{*b}(X_i)\}_{i \in OOB_b}$$

$$\widehat{Y}_{i}^{OOB} = \text{mean}\{T^{*b}(X_{i})\}_{i \in OOB_{b}}$$

$$OOB \text{ err} = \frac{1}{n} \sum_{i=1}^{n} (Y_{i} - \widehat{Y}_{i}^{OOB})^{2}$$

#### Average across rows to get OOB predictions

### Out of bag error

#### Bootstrap sample 1

	•	•	
	Y	X	Obs ID
	<b>Y</b> <sub>5</sub>	<b>X</b> 5	5
$T^{*1}$	<b>Y</b> <sub>3</sub>	<i>X</i> <sub>3</sub>	3
	<b>Y</b> <sub>2</sub>	<b>X</b> <sub>2</sub>	2
	<b>Y</b> <sub>3</sub>	<b>X</b> 3	3
	Y <sub>1</sub>	X <sub>1</sub>	1
out-of-bag 1	<b>Y</b> <sub>4</sub>	X <sub>4</sub>	4

Obs ID	X	Y
1	X <sub>1</sub>	Y <sub>1</sub>
2	<i>X</i> <sub>2</sub>	<b>Y</b> <sub>2</sub>
3	<b>X</b> 3	<b>Y</b> <sub>3</sub>
4	<i>X</i> <sub>4</sub>	Y <sub>4</sub>
5	X <sub>5</sub>	Y <sub>5</sub>

Original training data

Bootstrap sample B

	•	•	
Obs ID	X	Y	
4	X <sub>4</sub>	Y <sub>4</sub>	
1	X <sub>1</sub>	Y <sub>1</sub>	*D
1	X <sub>1</sub>	Y <sub>1</sub>	$\longrightarrow T^{*B}$
5	<b>X</b> <sub>5</sub>	<b>Y</b> <sub>5</sub>	
4	<i>X</i> <sub>4</sub>	<b>Y</b> <sub>4</sub>	
2	<b>X</b> <sub>2</sub>	Y <sub>2</sub>	
3	<b>X</b> <sub>3</sub>	<b>Y</b> <sub>3</sub>	out-of-bag E
	4 1 1 5 4	$ \begin{array}{c cccc} 4 & X_4 \\ 1 & X_1 \\ 1 & X_1 \\ 5 & X_5 \\ 4 & X_4 \\ \hline 2 & X_2 \end{array} $	$\begin{array}{c ccccccccccccccccccccccccccccccccccc$

#### **OOB** predictions

Obs ID	X	Y
1	$X_1$	<b>Y</b> <sub>1</sub>
2	$X_2$	<b>Y</b> <sub>2</sub>
3	<b>X</b> 3	<b>Y</b> 3
4	<i>X</i> <sub>4</sub>	<b>Y</b> <sub>4</sub>
5	$X_5$	<b>Y</b> <sub>5</sub>

T*1(X)	 <b>T</b> *B( <b>X</b> )	у̂оов
_		$\hat{\gamma}_1$ 00B
_	 $T^{*B}(X_2)$	$\hat{\gamma}_2$ 008
_	 T*B(X3)	$\hat{\gamma}_3$ оов
$T^{*1}(X_4)$	 -	$\hat{\gamma}_4$ 00В
_	 1	$\mathbf{\hat{\gamma}}_{5}$ оов

#### **Regression:**

$$\hat{Y}_i^{OOB} = \text{mean}\{T^{*b}(X_i)\}_{i \in OOB_b}$$

OOB err = 
$$\frac{1}{n} \sum_{i=1}^{n} (Y_i - \widehat{Y}_i^{OOB})^2$$

#### **Classification:**

$$\widehat{Y}_i^{OOB} = \mathsf{mode}\{T^{*b}(X_i)\}_{i \in OOB_b}$$

OOB err = 
$$\frac{1}{n} \sum_{i=1}^{n} I(Y_i \neq \widehat{Y}_i^{OOB})$$

### Parameters to tune (or not)

Random forests generally work pretty well even if not tuned (i.e. if default parameter choices are used).

However, parameters can be tuned using OOB error to improve performance:

- m: most important tuning parameter
- criteria to stop splitting: can be tuned but growing trees about as deep as possible generally works pretty well
- B: least necessary to tune; just choose a large value like 100-1000.

Recommendation is to tune on M

### Interpretability and variable importance measures

Compared to trees, main drawback of random forests is reduced interpretability.

However, variable importance measures can help improve the interpretability.

Two types of variable importance measures are used for random forests:

- purity based importance: how much improvement in node purity results from splitting on a feature
- OOB prediction based importance: how much deterioration in prediction accuracy results from scrambling a feature out of bag

### **Purity-based variable** importance

Consider the construction of one tree. For each split, note the feature that was split on and resulting reduction in RSS or Gini index (i.e. improvement in purity).

Define the importance of each feature in this single tree by summing up the improvement in purity for all splits based on this feature.

For random forests, we can average this quantity over all of the trees to get a purity-based variable importance metric.

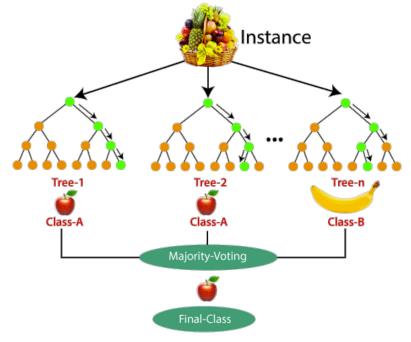


Image source: https://www.section.io/engineering-education/introduction-to-random-forest-in-machine-learning

Recall the OOB error introduced a few slides ago.

For each feature j and each tree, consider making predictions on the OOB data after first scrambling feature j. We can therefore get a scrambled OOB error.

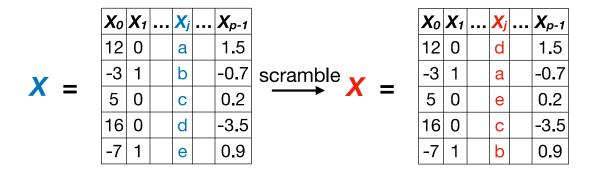
For each feature j, we can define an OOB-prediction-based variable importance by the difference in OOB error when this feature is scrambled and when it is not.

		<b>X</b> o	<b>X</b> <sub>1</sub>	 Χj	 <b>X</b> <sub>p-1</sub>
<b>X</b> =		12	0	а	1.5
		-3	1	b	-0.7
	=	5	0	С	0.2
	16	0	d	-3.5	
		-7	1	е	0.9

Recall the OOB error introduced a few slides ago.

For each feature j and each tree, consider making predictions on the OOB data after first scrambling feature j. We can therefore get a scrambled OOB error.

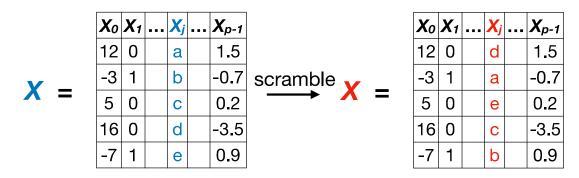
For each feature j, we can define an OOB-prediction-based variable importance by the difference in OOB error when this feature is scrambled and when it is not.



Recall the OOB error introduced a few slides ago.

For each feature j and each tree, consider making predictions on the OOB data after first scrambling feature j. We can therefore get a scrambled OOB error.

For each feature j, we can define an OOB-prediction-based variable importance by the difference in OOB error when this feature is scrambled and when it is not.



#### Regular OOB predictions

T*1(X)	 <b>T</b> *B( <b>X</b> )	Ŷоов	
_	 _	Ŷ <sub>1</sub> 00B	
_	 T*B(X2)	Ŷ <sub>2</sub> 00B	Regular
_	 T*B(X3)	$\hat{\gamma}_3$ 00B	OOB error
$T^{*1}(X_4)$	 _	$\hat{\gamma}_4$ 00B	
_	 _	$\hat{\gamma}_5$ OOB	

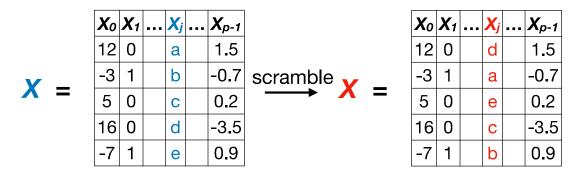
#### Scrambled OOB predictions

T*1(X)	 <b>T</b> *B( <b>X</b> )	у̂оов	
_	 _	Ŷ <sub>1</sub> 00B	
_	 T*B(X2)	$\hat{\gamma}_2$ 00B	Scrambled
_	 T*B(X3)	$\hat{\gamma}_3$ 008	OOB error
$T^{*1}(X_4)$	 _	$\hat{\gamma}_4$ 008	
	 _	$\hat{\gamma}_{5}$ 008	

Recall the OOB error introduced a few slides ago.

For each feature j and each tree, consider making predictions on the OOB data after first scrambling feature j. We can therefore get a scrambled OOB error.

For each feature j, we can define an OOB-prediction-based variable importance by the difference in OOB error when this feature is scrambled and when it is not.



#### Regular OOB predictions

T*1(X)	 <b>T</b> *B( <b>X</b> )	у̂оов	
_	 _	Ŷ <sub>1</sub> 00B	
_	 T*B(X2)	Ŷ <sub>2</sub> 00B	Regular
_	 T*B(X3)	Ŷ <sub>3</sub> 00B	OOB erro
$T^{*1}(X_4)$	 _	$\hat{\gamma}_4$ 00B	
_	 _	$\hat{\gamma}_5$ 00B	

#### Scrambled OOB predictions

T*1(X)	 <b>T</b> *B( <b>X</b> )	Ŷоов	
_	 _	Ŷ <sub>1</sub> 00B	
_	 T*B(X2)	$\hat{\gamma}_2$ 00B	Scrambled
_	 T*B(X3)	$\hat{\gamma}_3$ 008	OOB error
T*1(X4)	 _	$\hat{\gamma}_4$ 008	
_	 _	$\hat{\gamma}_5$ OOB	

Var. Imp. = scrambled OOB err - regular OOB err

### **Summary**

- Random forests are a fancier version of bagging based on random subsampling of m features at each split point.
- They improve on bagging by de-correlating the bootstrapped decision trees and therefore reducing the variance of the method.
- OOB error is a nice alternative to cross-validation error for random forests, and can be used to tune parameters such as m.
- Random forests usually give much better prediction performance than individual decision trees, but at the cost of interpretability.
- Nevertheless, there are a couple ways to measure variable importance in random forests, giving us some interpretability.

Random forests are a state-of-the-art tool for predictive modeling.