

SVM implementation

- `data=pd.read_csv('iris.csv')`
- `d={'Iris-setosa':0,'Iris-versicolor':1, 'Iris-virginica':2}`
- `data['species']=data['species'].map(d)`
- `X=data[['sepal_length','sepal_width']]`

```
svc_model = SVC(kernel='linear')
```

```
svc_model.fit(X_train, y_train)
```

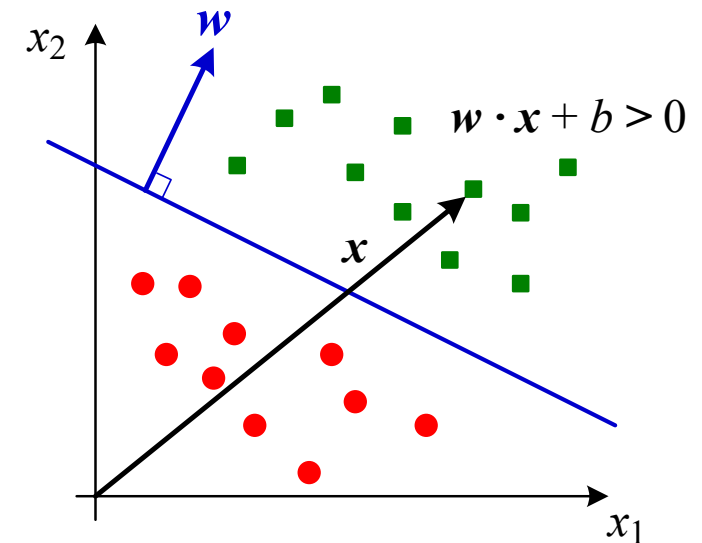
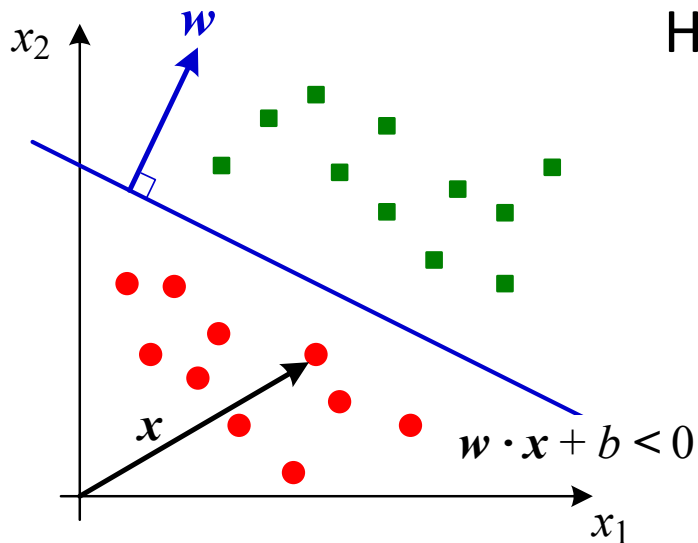
Linear Support Vector Machines

Hyperplane equation: $\mathbf{w} \cdot \mathbf{x} + b = 0$.

If \mathbf{x} is the position vector of a **negative** point then $\mathbf{w} \cdot \mathbf{x} + b < 0$.

If \mathbf{x} is the position vector of a **positive** point then $\mathbf{w} \cdot \mathbf{x} + b > 0$.

Hence the terminology.



Equations of the hyperplane

$$[x_1, x_2] \begin{bmatrix} w_1 \\ w_2 \end{bmatrix} + b = 0$$

$$x_1 w_1 + x_2 w_2 + b = 0$$

$$x_2 w_2 = -x_1 w_1 - b$$

$$x_2 = -\frac{w_1}{w_2} x_1 - \frac{b}{w_2}$$

Slope

Intercept

where, x_1 and x_2 are found *svc_model.coef_*

b is in *scv_model.intercept_*

```
w = svc_model.coef_[0] # w consists of 2 elements
```

```
b = svc_model.intercept_[0] # b consists of 1 element
```

```
x_points = np.linspace(4, 7) # generating x-points from 4 to 7
```

```
y_points = -(w[0] / w[1]) * x_points - b / w[1] # getting corresponding  
y-points
```

- # Plotting a red hyperplane
plt.plot(x_points, y_points, c='r');
- # Encircle support vectors
- **plt.scatter(svc_model.support_vectors[:, 0],
svc_model.support_vectors[:, 1], s=50,
facecolors='none',
edgecolors='k',
alpha=.5);**

The hyperplane classifier

Recall that the hyperplane classifier has equation

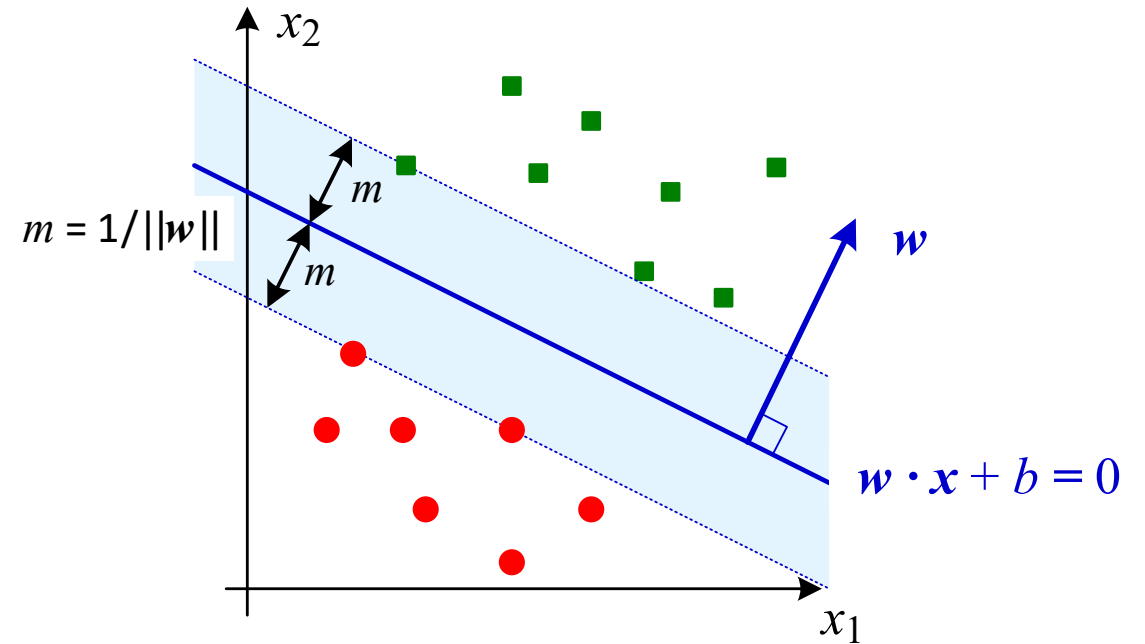
$$\mathbf{w} \cdot \mathbf{x} + b = 0.$$

The width of the margin is

$$d = \frac{2}{\|\mathbf{w}\|}.$$

Hence the distance from the hyperplane classifier to the positive and negative barriers is

$$m = \frac{1}{\|\mathbf{w}\|}.$$



The hyperplane classifier

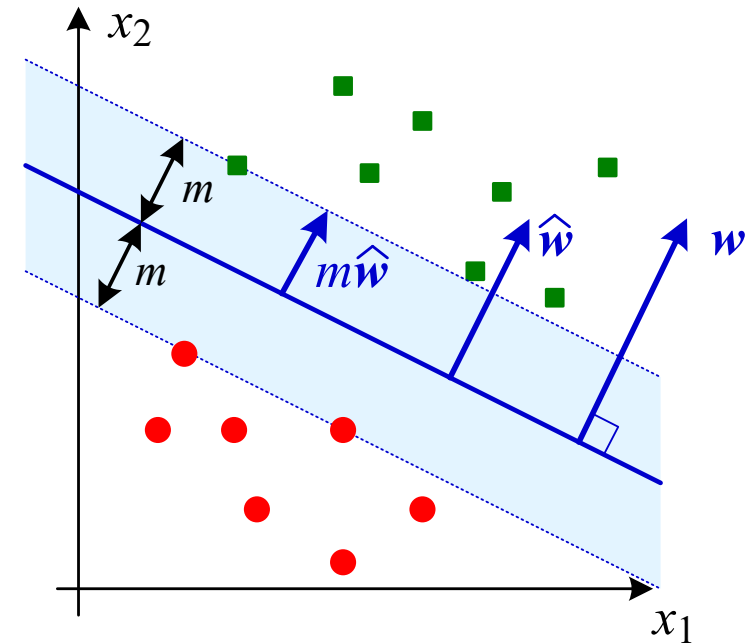
The vector \mathbf{w} is perpendicular to the hyperplane classifier.

Then

$$\hat{\mathbf{w}} = \frac{\mathbf{w}}{\|\mathbf{w}\|}$$

is a **unit** vector (length = 1) in the direction of \mathbf{w} .

Hence $m\hat{\mathbf{w}}$ has length m so is a vector from the hyperplane classifier to the positive barrier hyperplane.

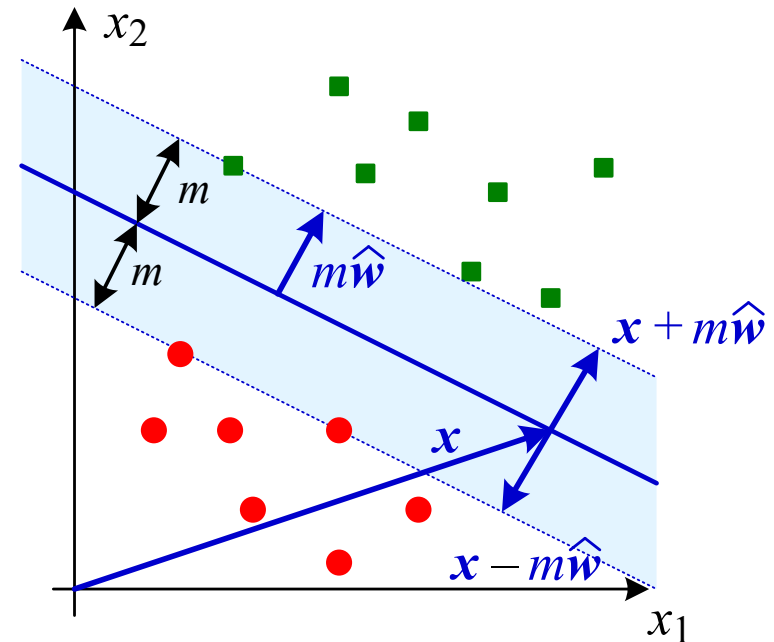


The hyperplane classifier

Let \mathbf{x} be the position vector of a point on the hyperplane classifier.

Then $\mathbf{x} + m\hat{\mathbf{w}}$ is the position vector of a point on the positive barrier hyperplane.

And $\mathbf{x} - m\hat{\mathbf{w}}$ is the position vector of a point on the negative barrier hyperplane.



```
w_hat = svc_model.coef_[0] / (np.sqrt(np.sum(svc_model.coef_[0] ** 2)))
```

```
margin = 1 / np.sqrt(np.sum(svc_model.coef_[0] ** 2))
```

```
decision_boundary_points = np.array(list(zip(x_points, y_points)))
```

```
points_of_line_above = decision_boundary_points + w_hat * margin  
points_of_line_below = decision_boundary_points - w_hat * margin
```

```
plt.plot(points_of_line_above[:, 0],  
points_of_line_above[:, 1], 'b--', linewidth=2)
```

```
plt.plot(points_of_line_below[:, 0], points_of_line_below[:, 1], 'g--',  
linewidth=2)
```

Output

