

1.3

$$1. E_p = \frac{\lambda}{2\pi\epsilon_0 a} \sin\theta = \frac{\lambda}{2\pi\epsilon_0 a} \frac{\frac{1}{2}L}{\sqrt{a^2 + (\frac{1}{2}L)^2}}$$

Should state where this comes from. Your subscript is rho, but there is no rho in the equation.

Taylor series: $\frac{z}{\sqrt{z^2 + R^2}} = \left(1 + \frac{R^2}{z^2}\right)^{-1/2}$

Make sure that you review what a Taylor series is. This is simply an algebraic re-write.

$$\frac{\lambda}{2\pi\epsilon_0 a} \frac{\frac{1}{2}L}{\sqrt{a^2 + (\frac{1}{2}L)^2}} = \frac{\lambda}{2\pi\epsilon_0 a} \left(1 + \frac{a^2}{(\frac{1}{2}L)^2}\right)^{-1/2}$$

As $L \rightarrow \infty$,

$$\frac{\lambda}{2\pi\epsilon_0 a} (1 + 0) = \frac{\lambda}{2\pi\epsilon_0 a} = \frac{Q}{2\pi\epsilon_0 a L}$$

As $L \rightarrow \infty$, this goes to zero

$$2. E = \frac{\sigma_0}{\pi\epsilon_0} \tan^{-1}\left(\frac{\omega^2}{4z\sqrt{z^2 + \omega^2/2}}\right)$$

Taylor Series:

$$\frac{\sqrt{b^2}\pi}{2b} + O(z^2) + \left(-\frac{\sqrt{b^2}z}{b} + O(z^2)\right)$$

What is b?

At $z=0$,

$$E = \frac{\sigma_0}{\pi\epsilon_0} \left(\frac{\pi}{2}\right) = \frac{\sigma_0}{2\epsilon_0}$$

calculated using Wolfram Alpha