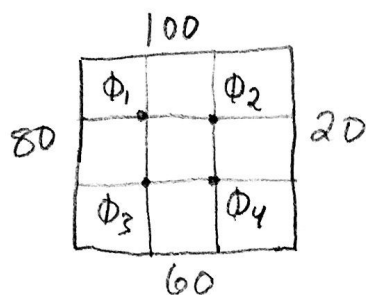


2.2.1.



For $\phi_1 (x,y) = (1/3, 2/3)$, $(a,b) = (1,1)$ at $n=1$

$$V_L = \frac{4(80)}{\pi} \frac{\sinh\left(\frac{\pi(1-1/3)}{1}\right) \sin\left(\frac{\pi(2/3)}{1}\right)}{(1) \sin(\pi(1/1))} = 30.54$$

$$V_b = \frac{4(60)}{\pi} \frac{\sinh\left(\frac{\pi(1-2/3)}{1}\right) \sinh\left(\frac{\pi(1/3)}{1}\right)}{(1) \sinh(\pi(1))} = 7.16$$

$$V_t = \frac{4(100)}{\pi} \frac{\sinh(\pi(2/3)) \sin(\pi(1/3))}{\sinh(\pi)} = 38.18$$

$$V_r = \frac{4(20)}{\pi} \frac{\sinh(\pi(1/3)) \sinh(\pi(2/3))}{\sinh(\pi)} = 2.39$$

$$\phi_1 = V_L + V_b + V_t + V_r = 30.54 + 7.16 + 38.18 + 2.39 = 78.27$$

Repeating for $\phi_2 (x,y) = (2/3, 2/3)$, $(a,b) = (1,1)$

$$V_L = 9.54 \quad V_b = 7.16 \quad V_t = 38.18 \quad V_r = 7.64$$

$$\phi_2 = 62.52$$

$\phi_3 (x,y) = (1/3, 1/3)$, $(a,b) = (1,1)$

$$V_L = 30.54 \quad V_b = 22.91 \quad V_t = 11.93 \quad V_r = 2.39$$

$$\phi_3 = 67.77$$

$\phi_4 (x,y) = (2/3, 1/3)$, $(a,b) = (1,1)$

$$V_L = 9.54 \quad V_b = 22.91 \quad V_t = 11.93 \quad V_r = 7.64$$

$$\phi_4 = 52.02$$

The way it's done in the book:

$$\phi_1 = (100 + 80 + 65 + 65)/4 = 77.5$$

$$\phi_2 = (100 + 20 + 77.5 + 65)/4 = 65.63$$

$$\phi_3 = (77.5 + 80 + 65 + 60)/4 = 70.63$$

$$\phi_4 = (20 + 60 + 65.63 + 70.63)/4 = 54.06$$