CodingLab4

May 18, 2025

Neural Data Science

Lecturer: Dr. Jan Lause, Prof. Dr. Philipp Berens

Tutors: Jonas Beck, Fabio Seel, Julius Würzler

Summer term 2025

Student names: Aakarsh Nair, Andreas Kotzur, Ahmed Eldably

LLM Disclaimer: *Did you use an LLM to solve this exercise? If yes, which one and where did you use it? Chat GPT 40, Google Gemini - Task Tracking, Template Code, Background Knowledge, Plotting

1 Coding Lab 4

In this notebook you will work with preprocessed 2 photon calcium recordings, that have already been converted into spike counts for a population of cells from the Macaque V1. During the experiment the animal has been presented with several drifting grating stimuli, in response to which the neural activity was recorded. In this exercise sheet we will study how you can visualize the activity of multiple neural spike trains and assess whether a neuron is selective to a specific stimulus type.

Download the data files nds_cl_4_*.csv from ILIAS and save it in the subfolder ../data/. We recommend you to use a subset of the data for testing and debugging, ideally focus on a single cell (e.g. cell number x). The spike times and stimulus conditions are read in as pandas data frames. You can solve the exercise by making heavy use of that, allowing for many quite compact computations. See documentation and several good tutorials on how to do this. Of course, converting the data into classical numpy arrays is also valid.

```
[1]: import pandas as pd
  import seaborn as sns
  import matplotlib.pyplot as plt
  import matplotlib as mpl
  import numpy as np
  import scipy.optimize as opt

from scipy import signal as signal
  from typing import Tuple

import itertools
```

```
import logging
    %matplotlib inline
    %load_ext jupyter_black
    %load_ext watermark
    %watermark --time --date --timezone --updated --python --iversions --watermark ∪
      ⊶-p sklearn
    Last updated: 2025-05-18 21:58:21CEST
    Python implementation: CPython
    Python version
                     : 3.11.11
    IPython version : 9.2.0
    sklearn: not installed
    pandas : 2.2.3
    seaborn : 0.13.2
    numpy : 1.26.4
    logging : 0.5.1.2
    matplotlib: 3.9.4
    scipy
           : 1.15.2
    Watermark: 2.5.0
[2]: # %%
    logging.basicConfig(
        format="%(asctime)s - %(levelname)s - %(message)s",
        level=logging.DEBUG,
    logger = logging.getLogger(__name__)
    logger.setLevel(logging.WARN)
    logger.info("Starting the script...")
     # --- Add these lines to suppress Matplotlib's DEBUG messages ---
    mpl_logger = logging.getLogger("matplotlib")
    mpl_logger.setLevel(logging.WARNING) # Or logging.INFO, logging.ERROR
    # You can also target specific noisy submodules if needed:
    # logging.getLogger('matplotlib.font_manager').setLevel(logging.WARNING)
     # logging.getLogger('matplotlib.pyplot').setLevel(logging.WARNING)
     # --- End of added lines ---
[3]: plt.style.use("../matplotlib_style.txt")
```

1.1 Load data

```
[4]: spikes = pd.read_csv("../data/nds_cl_4_spiketimes.csv") # neuron id, spike time stims = pd.read_csv("../data/nds_cl_4_stimulus.csv") # stimulus onset in ms, undirection

stimDur = 2000.0 # in ms
nTrials = 11 # number of trials per condition
nDirs = 16 # number of conditions
deltaDir = 22.5 # difference between conditions

stims["StimOffset"] = stims["StimOnset"] + stimDur
```

We require some more information about the spikes for the plots and analyses we intend to make later. With a solution based on dataframes, it is natural to compute this information here and add it as additional columns to the spikes dataframe by combining it with the stims dataframe. We later need to know which condition (Dir) and trial (Trial) a spike was recorded in, the relative spike times compared to stimulus onset of the stimulus it was recorded in (relTime) and whether a spike was during the stimulation period (stimPeriod). But there are many options how to solve this exercise and you are free to choose any of them.

```
[5]: # you may add computations as specified above
     spikes["Dir"] = np.nan
     spikes["relTime"] = np.nan
     spikes["Trial"] = np.nan
     spikes["stimPeriod"] = np.nan
     dirs = np.unique(stims["Dir"])
     trialcounter = np.zeros_like(dirs)
     for i, row in stims.iterrows():
         trialcounter[dirs == row["Dir"]] += 1
         i0 = spikes["SpikeTimes"] > row["StimOnset"]
         i1 = spikes["SpikeTimes"] < row["StimOffset"]</pre>
         select = i0.values & i1.values
         spikes.loc[select, "Dir"] = row["Dir"]
         spikes.loc[select, "Trial"] = trialcounter[dirs == row["Dir"]][0]
         spikes.loc[select, "relTime"] = spikes.loc[select, "SpikeTimes"] -
      →row["StimOnset"]
         spikes.loc[select, "stimPeriod"] = True
     spikes = spikes.dropna()
```

/var/folders/_q/911zk1853mv45phss2fsffd00000gn/T/ipykernel_80767/4012369867.py:2 1: FutureWarning: Setting an item of incompatible dtype is deprecated and will raise an error in a future version of pandas. Value 'True' has dtype

incompatible with float64, please explicitly cast to a compatible dtype first.
 spikes.loc[select, "stimPeriod"] = True

```
[6]: spikes.head()
```

```
[6]:
          Neuron
                     SpikeTimes
                                    Dir
                                             relTime
                                                      Trial stimPeriod
     514
                   15739.000000
                                  270.0
                                                        1.0
                1
                                         169.000000
                                                                   True
                   15776.566667
     515
                1
                                  270.0
                                         206.566667
                                                        1.0
                                                                   True
     516
                                  270.0
                   15808.466667
                                         238.466667
                                                        1.0
                                                                   True
     517
                   15821.900000
                                  270.0
                                         251.900000
                                                        1.0
                                                                   True
                1
                   15842.966667
                                  270.0
     518
                                         272.966667
                                                        1.0
                                                                   True
```

```
[7]: stims.head()
```

```
[7]:
        StimOnset
                       Dir
                            StimOffset
     0
             15570
                    270.0
                                17570.0
     1
             19022
                      45.0
                                21022.0
     2
             22592
                    112.5
                                24592.0
     3
             26095
                    225.0
                                28095.0
     4
             29431
                    180.0
                                31431.0
```

1.2 Task 1: Plot spike rasters

In a raster plot, each spike is shown by a small tick at the time it occurs relative to stimulus onset. Implement a function plotRaster() that plots the spikes of one cell as one trial per row, sorted by conditions (similar to what you saw in the lecture). Why are there no spikes in some conditions and many in others?

If you opt for a solution without a dataframe, you need to change the interface of the function.

Grading: 3 pts

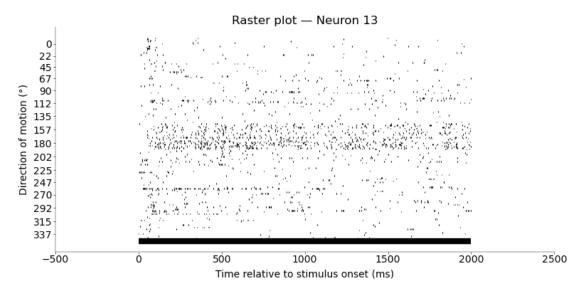
```
this function does not return anything, it just creates a plot!
# Write a raster plot function for the data (2 pts)
# -----
df = spikes[(spikes["Neuron"] == neuron) & (spikes["stimPeriod"])]
directions = np.sort(df["Dir"].unique())
fig, ax = plt.subplots(figsize=(8, 4))
y = 0
yticks, ylabels = [], []
for d in directions:
   sub = df[df["Dir"] == d]
   trials = np.sort(sub["Trial"].unique())
    # remember the center for this direction block
   yticks.append(y + len(trials) / 2)
   ylabels.append(int(d))
   for t in trials:
       times = sub[sub["Trial"] == t]["relTime"]
       ax.vlines(times, y, y + 1, linewidth=0.8, color="k")
    # small gap between direction blocks
   y += 0.5
# stimulus-on bar
ax.hlines(y + 0.5, xmin=0, xmax=stimDur, linewidth=6, color="k")
ax.set_yticks(yticks)
ax.set_yticklabels(ylabels)
ax.set_xlabel("Time relative to stimulus onset (ms)")
ax.set_ylabel("Direction of motion (°)")
ax.set_title(f"Raster plot - Neuron {neuron}")
\# show some pre- and post-stimulus window
ax.set_xlim(-500, stimDur + 500)
# if you want 0° at bottom, 360° at top:
ax.invert_yaxis()
plt.tight_layout()
plt.show()
```

```
[9]: # ------ # Find and explain examples? (1 pt) # -----
```

```
# average over the full O-stimDur window, per trial
rates = (
    spikes.query("stimPeriod")
     .groupby(["Neuron", "Dir", "Trial"])
    .size() # spike count
    .reset_index(name="count")
    .assign(rate=lambda df: df["count"] / (stimDur / 1000))
    .groupby(["Neuron", "Dir"])["rate"]
     .mean() # mean across trials
     .unstack() # rows=Neuron, cols=Dir
dsis = {}
osis = {}
for nm, row in rates.iterrows():
    pref = row.max()
    pref_dir = row.idxmax()
    null_dir = (pref_dir + 180) % 360
    perp_dirs = [(pref_dir + 90) % 360, (pref_dir - 90) % 360]
    R_null = row[null_dir]
    R_perp = row[perp_dirs].mean()
    dsis[nm] = (pref - R_null) / (pref + R_null + 1e-6)
    osis[nm] = (pref - R_perp) / (pref + R_perp + 1e-6)
# then:
# Using hueristic thresholds, permutation tests used later provide more robust _{\sqcup}
 →and accurate results
# to determine the selectivity of the neuron
dir_sel = [n for n in dsis if dsis[n] > 0.5] # [9, 13, 27]
ori_sel = [n \text{ for } n \text{ in osis if osis}[n] > 0.5 \text{ and dsis}[n] < 0.2] # [6, 7, 12]
non_sel = [n for n in dsis if abs(dsis[n]) < 0.1 and abs(osis[n]) < 0.1] # [1, ]
 →4]
print("Direction-selective examples:", dir_sel)
print("Orientation-selective examples:", ori_sel)
print("Non-selective examples:", non_sel)
for neuron in [dir_sel[1], ori_sel[3], non_sel[0]]:
    print(f"\nNeuron {neuron}:\n")
    plotRaster(spikes, neuron)
Direction-selective examples: [9, 13, 27, 29, 32, 37, 38]
Orientation-selective examples: [6, 7, 12, 16, 17, 21]
Non-selective examples: [1, 4]
```

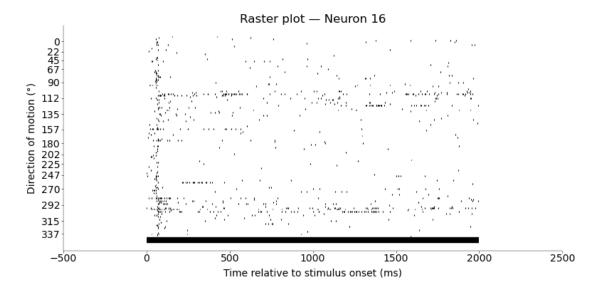
Neuron 13:

/var/folders/_q/911zk1853mv45phss2fsffd00000gn/T/ipykernel_80767/224280136.py:59
: UserWarning: The figure layout has changed to tight
 plt.tight_layout()



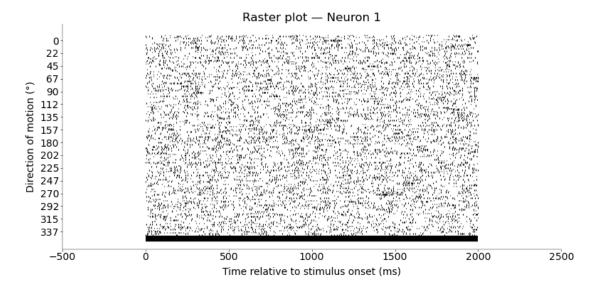
Neuron 16:

/var/folders/_q/911zk1853mv45phss2fsffd00000gn/T/ipykernel_80767/224280136.py:59
: UserWarning: The figure layout has changed to tight
 plt.tight_layout()



Neuron 1:

/var/folders/_q/911zk1853mv45phss2fsffd00000gn/T/ipykernel_80767/224280136.py:59
: UserWarning: The figure layout has changed to tight
 plt.tight_layout()



Why are there no spikes in some conditions and many in others? Answer: The primary reason why an individual neuron shows many spikes in some conditions and few or no spikes in others is because neurons themselves are intrinsically selective for specific stimulus features, such as particular orientations and directions of motion.

Each neuron in a sensory area like V1 is often 'tuned' to respond most strongly to its preferred stimulus. When a presented stimulus aligns with a neuron's preference, it fires vigorously (many spikes). When the stimulus does not match its preference, it fires weakly or not at all (few or no spikes).

In the experiment we are sub-sampling a population, and the specific neurons we happen to record will determine the range of preferences we observe in our dataset.

Find examples and and explain your choices:

1. A direction selective neuron:

Answer: We chose Neuron 13 as a possible example of a direction selective neuron. Observing the firing rate we find that there is a band between 140-180 degrees where the neuron is firing at a higher rate without a corresponding second direction to which it is selective.

2. An orientation selective neuron

Answer: We chose Neuron 16 as a possible example of orientation selective neuron. Observing that it fires for two directions roughly 180 degrees apart.

3. neither

Answer: We chose Neuron 1 as a possible example of a neuron which is not tuned to direction or orientation. It fires equally for all angles following stimulus.

1.3 Task 2: Plot spike density functions

Compute an estimate of the spike rate against time relative to stimulus onset. There are two ways:

* Discretize time: Decide on a bin size, count the spikes in each bin and average across trials. *

Directly estimate the probability of spiking using a density estimator with specified kernel width.

For full points, the optimal kernel- or bin-width needs to be computed.

Implement one of them in the function plotPSTH(). If you dont use a dataframe you may need to change the interface of the function.

Grading: 4 pts

```
[10]: from scipy.stats import norm
      nTrials = 11 # number of trials per direction
      def select_optimal_binwidth(
          rel times, T, n trials, delta min=1.0, delta max=None, n deltas=200
      ):
          11 11 11
          Shimazaki & Shinomoto (2007) algorithm to pick histogram bin width A,
          with log-spaced search capped at T/10 and a Freedman-Diaconis fallback.
          Parameters
          rel_times : array-like (ms)
              all spike times within [0, T]
          T: float (ms)
              total observation window
          n trials : int
              number of repeated trials
          delta_min : float (ms)
              smallest bin width to try
          delta_max : float (ms), optional
              largest bin width to try; defaults to T/10
              number of candidate widths in the log-spaced grid
          Returns
```

```
\Delta_opt_ms : float
        optimal bin width (ms)
    # convert to seconds
    rel_s = np.asarray(rel_times) / 1000.0
    T_s = T / 1000.0
    # cap delta_max at T/10 if not provided
    if delta max is None:
        delta_max = T / 20.0
    else:
        delta_max = min(delta_max, T / 20.0)
    # endpoints in seconds
    del_min_s = delta_min / 1000.0
    del_max_s = delta_max / 1000.0
    # log-spaced candidate \Delta_s
    deltas_s = np.logspace(np.log10(del_min_s), np.log10(del_max_s), n_deltas)
    # compute Shimazaki-Shinomoto cost for each \Deltas
    costs = np.zeros_like(deltas_s)
    for i, \Delta_s in enumerate(deltas_s):
        edges = np.arange(0, T s + \Delta s, \Delta s)
        kis, _ = np.histogram(rel_s, bins=edges)
        kis = kis.astype(float) / n_trials
        k bar = kis.mean()
        v = ((kis - k bar) ** 2).mean()
        costs[i] = (2 * k_bar - v) / (\Delta_s**2)
    # pick the \Delta_s that minimizes the cost
    idx = np.argmin(costs)
    \Delta_{\text{opt_ms}} = \text{deltas_s[idx]} * 1000.0
    # if the minimum is at the boundary, fallback to Freedman-Diaconis
    if idx == 0 or idx == len(deltas_s) - 1:
        x = np.asarray(rel_times)
        iqr = np.subtract(*np.percentile(x, [75, 25]))
        \Delta fd = 2 * iqr * (x.size ** (-1 / 3))
        \Delta_{\text{opt}_ms} = \text{np.clip}(\Delta_{\text{fd}}, \text{delta_min}, \text{delta_max})
    return ∆_opt_ms
def plotPSTH(spikes: pd.DataFrame, neuron: int, stimDur=2000.0, n_trials=11):
    """Plot PSTH for a single neuron sorted by condition
```

```
Parameters
_____
spikes: pd.DataFrame
    Pandas DataFrame with columns
        Neuron | SpikeTimes | Dir | relTime | Trial | stimPeriod
neuron: int
   Neuron ID
Note
this function does not return anything, it just creates a plot!
# Implement one of the spike rate estimates (3 pts)
# -----
# filter data
df = spikes[(spikes.Neuron == neuron) & spikes.stimPeriod]
dirs = np.sort(df.Dir.unique())
n_trials = df.groupby("Dir").Trial.nunique().iloc[0]
# compute optimal PSTH bin width \Delta *
Δ = select_optimal_binwidth(df.relTime.values, stimDur, n_trials)
# PSTH edges & centers
psth_edges = np.arange(0, stimDur + \Delta, \Delta)
psth_centers = psth_edges[:-1] + \Delta / 2
# time vector for SDF (±500 ms)
bg, ag = 500, 500
tvec = np.arange(-bg, stimDur + ag + 1)
# Gaussian kernel =20 ms
sigma = 20.0
kt = np.arange(-3 * sigma, 3 * sigma + 1)
gauss = norm.pdf(kt, 0, sigma)
gauss /= gauss.sum()
# 3) set up 4×4 grid
ncols = 4
nrows = int(np.ceil(len(dirs) / ncols))
fig, axes = plt.subplots(nrows, ncols, sharex=True, figsize=(14, 3 * nrows))
axes = axes.flatten()
```

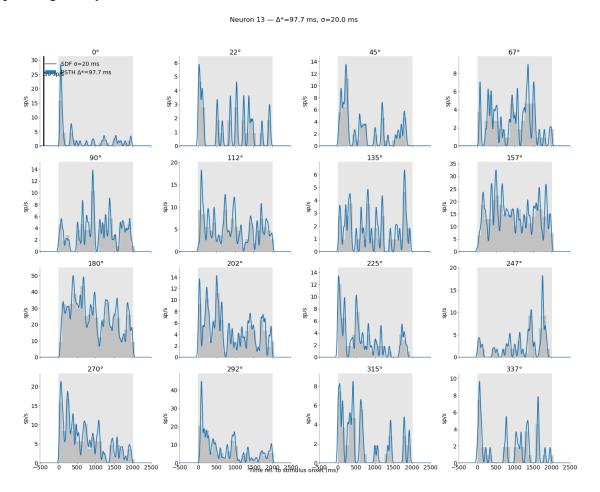
```
for ax, d in zip(axes, dirs):
       sub = df[df.Dir == d]
       # PSTH → spikes/sec
       trial_counts = []
       for t in range(1, n_trials + 1):
           st = sub[sub.Trial == t].relTime.values
           cnts, _ = np.histogram(st, bins=psth_edges)
           trial_counts.append(cnts)
       rate_hist = np.mean(trial_counts, axis=0) / (\Delta / 1000.0)
       # SDF → all-trial hist → sp/s → smooth
       hist1, _ = np.histogram(sub.relTime.values, bins=np.append(tvec,_
\hookrightarrowtvec[-1] + 1))
       rate1 = hist1 / n_trials * 1000.0
       sdf = np.convolve(rate1, gauss, mode="same")
       # plot
       ax.axvspan(0, stimDur, color="0.9", zorder=-1)
       ax.bar(
           psth_centers, rate_hist, width=\( \Delta\), color="0.7", edgecolor="none", \( \Delta\)
\Rightarrowalpha=0.7
       ax.plot(tvec, sdf, color="CO", lw=1.5)
       # format
       ax.set_xlim(-bg, stimDur + ag)
       ax.set_ylim(0, max(rate_hist.max(), sdf.max()) * 1.1)
       ax.set_title(f"{int(d)}")
       ax.set_ylabel("sp/s")
  # turn off any unused axes
  for ax in axes[len(dirs) :]:
       ax.axis("off")
   # shared legend & scale bar
  axes[0].bar([], [], color="0.7", alpha=0.7, label=f"PSTH \Delta *= \{\Delta : .1f\} ms")
  axes[0].plot([], [], color="CO", lw=1.5, label="SDF =20 ms")
  axes[0].legend(loc="upper left")
  axes[0].plot([-400, -400], [0, 50], "k", lw=2)
  axes[0].text(-390, 25, "50 sp/s", va="center")
  # global labels & title
  fig.text(0.5, 0.04, "Time rel. to stimulus onset (ms)", ha="center")
  fig.suptitle(f"Neuron {neuron} - \Delta *= \{\Delta : .1f\} ms, ={sigma:.1f} ms", y=0.98)
```

```
plt.tight_layout(rect=[0, 0.03, 1, 0.95])
plt.show()
```

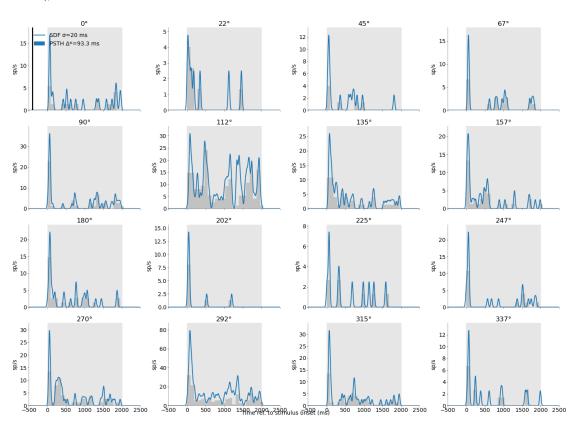
Plot the same 3 examples you selected in Task 1

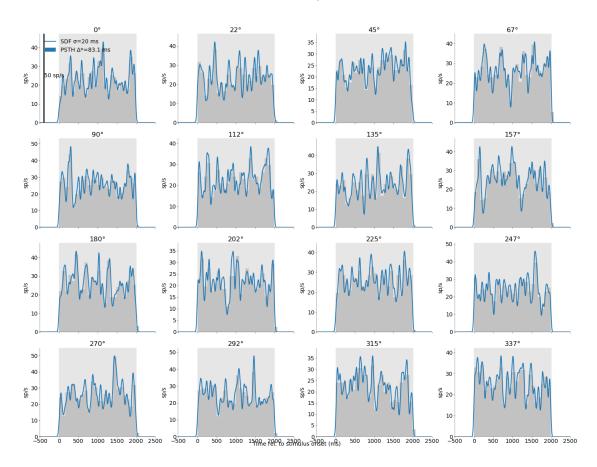
```
[11]: for neuron in [dir_sel[1], ori_sel[3], non_sel[0]]:
    plotPSTH(spikes, neuron)
```

/var/folders/_q/911zk1853mv45phss2fsffd00000gn/T/ipykernel_80767/24118823.py:169
: UserWarning: The figure layout has changed to tight
 plt.tight_layout(rect=[0, 0.03, 1, 0.95])









1.4 Task 3: Fit and plot tuning functions

The goal is to visualize the activity of each neuron as a function of stimulus direction. First, compute the spike counts of each neuron for each direction of motion and trial. The result should be a matrix \mathbf{x} , where x_{jk} represents the spike count of the j-th response to the k-th direction of motion (i.e. each column contains the spike counts for all trials with one direction of motion). If you used dataframes above, the groupby() function allows to implement this very compactly. Make sure you don't loose trials with zero spikes though. Again, other implementations are completely fine

Fit the tuning curve, i.e. the average spike count per direction, using a von Mises model. To capture the non-linearity and direction selectivity of the neurons, we will fit a modified von Mises function:

$$f(\theta) = \exp(\alpha + \kappa(\cos(2*(\theta - \phi)) - 1) + \nu(\cos(\theta - \phi) - 1))$$

Here, θ is the stimulus direction. Implement the von Mises function in vonMises() and plot it to understand how to interpret its parameters ϕ , κ , ν , α . Perform a non-linear least squares fit using a package/function of your choice. Implement the fitting in tuningCurve().

Plot the average number of spikes per direction, the spike counts from individual trials as well as your optimal fit.

Select two cells that show nice tuning to test your code.

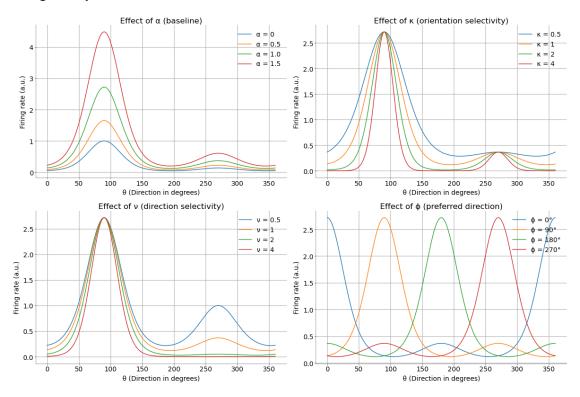
Grading: 5 pts

Plot the von Mises function while varying the parameters systematically.

```
theta_rad = np.deg2rad() # convert degrees to radians
   phi_rad = np.deg2rad() # convert degrees to radians
   fig, axs = plt.subplots(2, 2, figsize=(12, 8))
   axs = axs.ravel()
   # Vary (baseline)
   for a in [0, 0.5, 1.0, 1.5]:
       f = vonMises(theta_rad, =a, = , = phi_rad)
       axs[0].plot(, f, label=f" = {a}")
   axs[0].set_title("Effect of (baseline)")
   axs[0].legend()
   # Vary (orientation tuning sharpness)
   for k in [0.5, 1, 2, 4]:
       f = vonMises(theta_rad, = , =k, = , =phi_rad)
       axs[1].plot(, f, label=f" = {k}")
   axs[1].set_title("Effect of (orientation selectivity)")
   axs[1].legend()
   # Vary (direction tuning sharpness)
   for n in [0.5, 1, 2, 4]:
       f = vonMises(theta_rad, = , = , =n, =phi_rad)
       axs[2].plot(, f, label=f" = {n}")
   axs[2].set_title("Effect of (direction selectivity)")
   axs[2].legend()
    # Vary (preferred direction)
   for phi in [0, 90, 180, 270]:
       _rad = np.deg2rad(phi)
       f = vonMises(theta_rad, = , = , = _rad)
        axs[3].plot(, f, label=f" = {phi}^o")
   axs[3].set_title("Effect of (preferred direction)")
   axs[3].legend()
   for ax in axs:
       ax.set_xlabel(" (Direction in degrees)")
       ax.set_ylabel("Firing rate (a.u.)")
       ax.grid(True)
   plt.tight_layout()
   plt.show()
plot_vonMises_param_effects()
```

/var/folders/_q/911zk1853mv45phss2fsffd00000gn/T/ipykernel_80767/2235227151.py:57: UserWarning: The figure layout has changed to tight

plt.tight_layout()



Plot the von Mises function while varying the parameters systematically and explain what they do. The von Mises function used for fitting tuning curves is:

$$f(\theta) = \exp(\alpha + \kappa(\cos(2(\theta - \phi)) - 1) + \nu(\cos(\theta - \phi) - 1))$$

The parameters each distinctly describe the shape of the distribution: * α - Baseline/Amplitude is related to the neuron's baseline firing rate or the overall responsiveness. A larger alpha generally means the neuron fires more across all tested directions, or has a higher peak response. We see in the plot that going from a range of $\alpha=0$ to $\alpha=1.5$ all peaks show respective increase. * κ - Orientation Selectivity / Bimodal Component Strength - this term creates a response pattern that is 180° periodic (i.e., it has two peaks in a 360° range). kappa controls the strength and sharpness of this bimodal component. * ν - Direction Selectivity - Controls the strength and sharpness of this unimodal component. We see that $\nu=4$ has a flat bimodal peak. * ϕ - Preferred Direction/Orientation - ϕ is the neuron's preferred direction (if ν is dominant) or preferred orientation axis (if κ is dominant). It shifts the entire tuning curve horizontally along the direction axis. We note the shift in peak as we vary the ϕ above.

```
[14]: def compute_spike_count_matrix(counts: np.ndarray, dirs: np.ndarray) → np.

ondarray:

"""Compute the spike count matrix from the counts and dirs.

Parameters
```

```
counts: np.ndarray
              The spike counts for each trial.
          dirs: np.ndarray
              The stimulus directions for each trial.
          Returns
          spike_count_matrix: np.ndarray
              The computed spike count matrix.
          unique_stim_directions_deg = np.unique(dirs)
          num_unique_directions = len(unique_stim_directions_deg)
          logger.debug(f"Unique stimulus directions: {unique_stim_directions_deg}")
          logger.debug(f"Number of unique stimulus directions:
       →{num_unique_directions}")
          unique_stim_directions_deg = np.unique(dirs)
          num_unique_directions = len(unique_stim_directions_deg)
          spike_count_matrix_x = np.zeros((nTrials, num_unique_directions))
          for k_idx, direction_value in enumerate(unique_stim_directions_deg):
              counts_for_this_direction = counts[dirs == direction_value]
              if len(counts_for_this_direction) == nTrials:
                  spike_count_matrix_x[:, k_idx] = counts_for_this_direction
              else:
                  actual_trials_found = len(counts_for_this_direction)
                  if actual_trials_found >= nTrials:
                      spike_count_matrix_x[:, k_idx] = counts_for_this_direction[:
       ⇔nTrialsl
                  else: # actual trials found < nTrials</pre>
                      spike_count_matrix_x[:actual_trials_found, k_idx] = (
                          counts_for_this_direction
          return spike_count_matrix_x
[15]: def inital_von_mises_params(
          mean_counts_to_fit: np.ndarray, unique_dirs_rad: np.ndarray
      ) -> tuple:
          """Initial guess for the von Mises parameters based on mean counts.
          Parameters
          mean_counts_to_fit: np.ndarray
              The mean counts for each direction.
```

```
unique_dirs_rad: np.ndarray
              The unique directions in radians.
          Returns
          tuple: (alpha_guess, kappa_guess, nu_guess, phi_guess_rad)
              Initial guesses for the parameters of the von Mises function.
          if not np.any(mean_counts_to_fit > 1e-9):
              alpha_guess = np.log(1e-6)
              phi_guess_rad = 0.0
          else:
              # For alpha, use log of mean of positive counts, or log of max if all _{\sqcup}
       ⇔else fails
              positive_mean_counts = mean_counts_to_fit[mean_counts_to_fit > 1e-9]
              if len(positive_mean_counts) > 0:
                  alpha_guess = np.log(np.maximum(1e-6, np.
       →mean(positive_mean_counts)))
              else:
                  alpha_guess = np.log(np.maximum(1e-6, np.max(mean_counts_to_fit)))
              phi_guess_rad = unique_dirs_rad[np.argmax(mean_counts_to_fit)]
          kappa_guess = 1.0
          nu_guess = 1.0
          return alpha_guess, kappa_guess, nu_guess, phi_guess_rad
[16]: def plot_tuning_curve_fit(
          neuron_id: int,
          counts: np.ndarray,
          dirs: np.ndarray,
          mean_counts_to_fit: np.ndarray,
          p_opt: np.ndarray,
          r_squared: float = None,
      ) -> None:
          """Plot the tuning curve fit for a single neuron.
          Parameters
          _____
          neuron_id: int
              The ID of the neuron being plotted.
          counts: np.ndarray
              The spike counts for each trial.
          dirs: np.ndarray
              The stimulus directions for each trial.
          mean_counts_to_fit: np.ndarray
              The mean counts for each direction.
          p_opt: np.ndarray
              The optimized parameters from the von Mises fit.
```

```
r_squared: float, optional
       The R-squared value of the fit, if available.
  plt.figure(figsize=(10, 7))
  # 1. Plot individual trial spike counts (scatter plot)
  # Add some jitter to x-values for better visibility if many trials peru
\rightarrow direction
  unique_stim_directions_deg = np.unique(dirs)
  unique_dir_vals_plot = np.unique(dirs)
  dir_spacing = (
      np.min(np.diff(unique_dir_vals_plot)) if len(unique_dir_vals_plot) > 1__
⇔else 22.5
  jitter_strength = dir_spacing * 0.05 # Small jitter
  jittered_dirs = np.copy(dirs).astype(float)
  for ud in unique_dir_vals_plot:
      trials_for_dir_mask = dirs == ud
      num_trials_this_dir = np.sum(trials_for_dir_mask)
      if num_trials_this_dir > 1:
           jittered_dirs[trials_for_dir_mask] += np.random.uniform(
               -jitter_strength, jitter_strength, num_trials_this_dir
  plt.scatter(
      jittered_dirs,
      counts,
      alpha=0.3,
      s=25,
      color="darkgray",
      label="Individual Trial Counts",
      zorder=1,
  )
  # 2. Plot average spike counts per direction
  # Calculate standard error of the mean (SEM) for error bars if desired
  # sem_counts = np.std(spike_count_matrix_x, axis=0) / np.
⇒sqrt(spike_count_matrix_x.shape[0])
   # plt.errorbar(unique_stim_directions_deg, mean_counts_to_fit,_
⇔yerr=sem_counts,
                  fmt='o', color='dodgerblue', markersize=8, capsize=5,
                  label='Mean Counts (±SEM)', zorder=2)
  # Or simpler, just plot mean points:
  plt.plot(
      unique_stim_directions_deg,
      mean_counts_to_fit,
       "o",
```

```
color="dodgerblue",
      markersize=8,
      label="Mean Spike Count",
      zorder=2,
  )
  # 3. Plot the fitted von Mises curve (if fit was successful)
  if p_opt is not None:
      theta_plot_deg = np.linspace(0, 360, 361) # Smooth range of angles in_
\rightarrow degrees
      theta_plot_rad = np.deg2rad(
          theta_plot_deg
       ) # Convert to radians for vonMises function
      fitted_values = vonMises(theta_plot_rad, *p_opt)
      plt.plot(
          theta_plot_deg,
           fitted_values,
           0 - 0
           color="red",
          linewidth=2.5,
           label=(
              f"Von Mises Fit (R2={r_squared:.2f})"
               if r_squared is not None
              else "Von Mises Fit"
           ),
           zorder=3,
       )
  else:
      logger.info(f"Neuron {neuron_id if neuron_id else 'Unknown'}: No fit to∪
⇔plot.")
  plt.xlabel("Direction of motion (degrees)")
  plt.ylabel("Spike count")
  title_parts = ["Tuning Curve"]
  if neuron_id is not None:
      title_parts.append(f"Neuron {neuron_id}")
  if p_opt is None:
      title_parts.append("(Fit Failed)")
  plt.title(" - ".join(title_parts))
  plt.xticks(np.arange(0, 361, 45))
  plt.xlim(-10, 370) # Give a bit of space around 0 and 360
  # Adjust y-limits dynamically
  min_y_val = 0
```

```
if len(counts) > 0:
             min_y_val = min(0, np.min(counts) - 1)
             max_y_val = np.max(counts) + max(
                 1, np.std(counts) * 0.5
             ) # Ensure some space above max count
             if p_opt is not None: # Also consider fitted curve for ymax
                 max_y_val = max(max_y_val, np.max(fitted_values) * 1.1)
             plt.ylim(bottom=min_y_val, top=max_y_val)
         else:
             plt.ylim(bottom=0, top=1) # Default if no counts
         plt.legend(loc="upper right")
         plt.grid(True, linestyle="--", alpha=0.6)
         plt.tight_layout()
         plt.show()
[17]: def tuningCurve(
         counts: np.ndarray, dirs: np.ndarray, show: bool = True, neuron_id=None
     ) -> np.ndarray:
          """Fit a von Mises tuning curve to the spike counts in count with
          direction dir using a **least-squares fit**.
         Parameters
         counts: np.array, shape=(total n trials, )
             the spike count during the stimulation period
         dirs: np.array, shape=(total_n_trials, )
             the stimulus direction in degrees
         show: bool, default=True
             Plot or not.
         neuron_id: int, optional
             The ID of the neuron being fitted. Used for logging and plotting.
             If None, will be set to 'Unknown' in logs and plots.
         Return
         p: np.array or list, (4,)
             parameter vector of tuning curve function
         # Compute the spike count matrix (0.5 pts)
          # -----
         logger.info("Fitting tuning curve...")
```

logger.info(f"Counts: {counts.shape}")

```
logger.info(f"Dirs: {dirs.shape}")
      spike_count_matrix_x = compute_spike_count_matrix(counts, dirs)
     logger.info(f"Spike count matrix shape: {spike_count_matrix_x.shape}")
     logger.info(f"Spike count matrix: {spike_count_matrix_x}")
      # fit the von Mises tuning curve to the spike counts (0.5 pts)
      # 1. Calculate mean spike counts per direction
     mean_counts_to_fit = np.mean(spike_count_matrix_x, axis=0)
     logger.info(f"Mean counts to fit: {mean_counts_to_fit}")
     # 2. Get unique directions (degrees) and convert to radians
      # 'dirs' is the original 1D array of directions for all trials passed to_{\sqcup}
\hookrightarrow tuningCurve
     unique_stim_directions_deg = np.unique(dirs)
     unique_dirs_rad = np.deg2rad(unique_stim_directions_deg)
     logger.info(f"Unique directions (radians) for fitting: {unique dirs rad}")
      # Check if there's enough data to fit (at least as many points as u
⇒parameters)
      if len(unique_dirs_rad) < 4: # vonMises has 4 parameters</pre>
              logger.warning(
                       f"Not enough unique directions ({len(unique dire rad)}) to fit the
⇔von Mises model. Need at least 4. Skipping fit."
              p_opt = None # Indicate fit failed
     else:
              alpha_guess, kappa_guess, nu_guess, phi_guess_rad =_
⇔inital_von_mises_params(
                       mean_counts_to_fit, unique_dirs_rad
              p0 = [alpha_guess, kappa_guess, nu_guess, phi_guess_rad]
              logger.info(f"Initial parameter guesses (p0): {p0}")
               # Bounds: alpha, kappa>=0, nu>=0, phi in [0, 2*pi]
              bounds = ([-np.inf, 0, 0, 0], [np.inf, np.inf, np.inf, 2 * np.pi])
               # Fit the von Mises function to the mean counts
               # 4. Perform the non-linear least squares fit
              r_squared = None
              try:
                       p_opt, p_cov = opt.curve_fit(
                                f=vonMises, # Your vonMises function (make sure it's defined under the sure it's defi
→and accessible)
                                xdata=unique_dirs_rad,
```

```
ydata=mean_counts_to_fit,
               p0=p0,
               bounds=bounds,
               maxfev=5000, # Maximum number of function evaluations
          residuals = mean_counts_to_fit - vonMises(unique_dirs_rad, *p_opt)
           ss_res = np.sum(residuals**2)
           ss_tot = np.sum((mean_counts_to_fit - np.mean(mean_counts_to_fit))_
** 2)
           if ss_tot == 0: # Avoid division by zero if all mean_counts are_
→the same
              r squared = 1.0 if ss res < 1e-9 else 0.0
               r_squared = 1 - (ss_res / ss_tot)
          logger.info(
               f"Neuron {neuron_id if neuron_id else 'Unknown'}: R-squared =_

¬{r_squared:.3f}"

           logger.info(f"Optimized parameters (p_opt): {p_opt}")
      except RuntimeError:
           logger.warning(
               "RuntimeError: Optimal parameters not found during curve_fit._
⇔Fit failed."
          p_{opt} = (
              None # Or assign np.full(4, np.nan) if you prefer NaNs for
⇔failed fits
      except ValueError as e:
           logger.warning(f"ValueError during curve_fit: {e}. Fit failed.")
          p_opt = None
      if show:
           # plot the data and fitted tuning curve (1 pt)
          plot_tuning_curve_fit(
              neuron_id=neuron_id,
               counts=counts, # spike_count_matrix_x.flatten(),
               dirs=dirs,
               mean_counts_to_fit=mean_counts_to_fit,
               p_opt=p_opt,
               r_squared=r_squared, # Replace with actual R-squared value if_
\rightarrow available
```

```
# r_squared=1 - (np.sum((mean_counts_to_fit -u)

ovonMises(unique_dirs_rad, *p_opt))**2) / np.sum((mean_counts_to_fit - np.
omean(mean_counts_to_fit))**2))

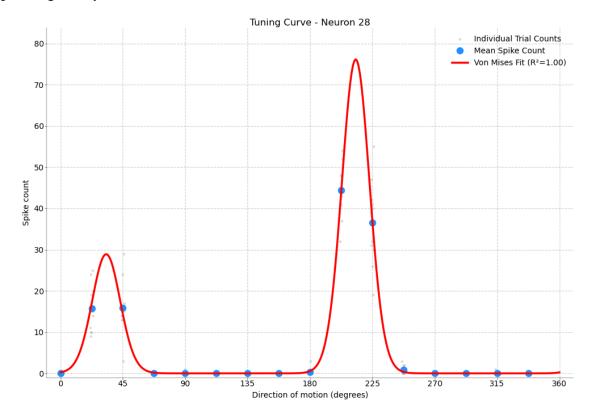
return p_opt
```

Plot tuning curve and fit for different neurons. Good candidates to check are 28, 29 or 37.

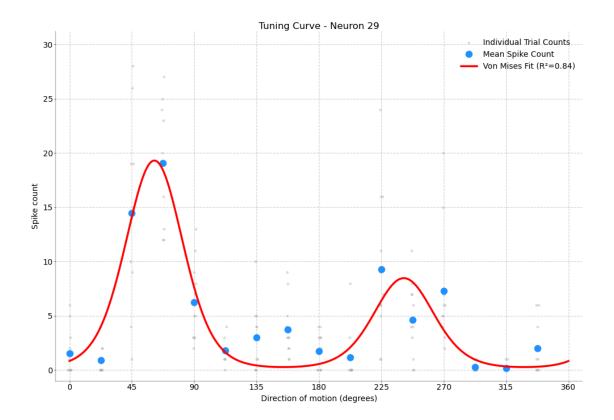
```
[18]: def get_data(spikes, neuron):
          spk_by_dir = (
              spikes[spikes["Neuron"] == neuron]
              .groupby(["Dir", "Trial"])["stimPeriod"]
              .sum()
              .astype(int)
              .reset_index()
          dirs = spk_by_dir["Dir"].values
          counts = spk_by_dir["stimPeriod"].values
          # because we count spikes only when they are present, some zero entries in
       → the count vector are missing
          for i, Dir in enumerate(np.unique(spikes["Dir"])):
              m = nTrials - np.sum(dirs == Dir)
              if m > 0:
                  dirs = np.concatenate((dirs, np.ones(m) * Dir))
                  counts = np.concatenate((counts, np.zeros(m)))
          idx = np.argsort(dirs)
          dirs sorted = dirs[idx] # sorted dirs
          counts_sorted = counts[idx]
          return dirs sorted, counts sorted
```

```
f"Neuron {neuron}: dirs_sorted.shape = {dirs_sorted.shape},__
counts_sorted.shape = {counts_sorted.shape}"
    )
else:
    print(f"Neuron {neuron}: No result from tuningCurve()")
```

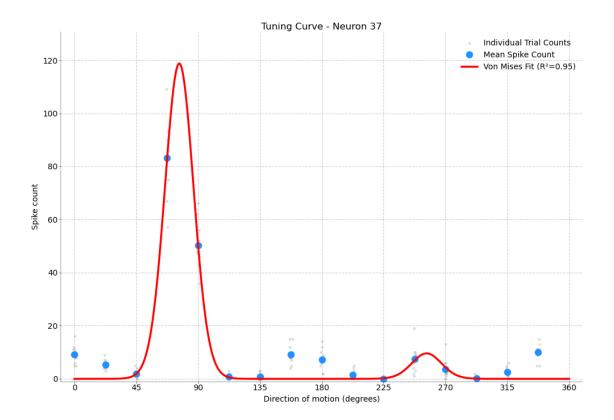
/var/folders/_q/911zk1853mv45phss2fsffd00000gn/T/ipykernel_80767/1305327222.py:1
07: UserWarning: The figure layout has changed to tight
 plt.tight_layout()



Neuron 28: dirs_sorted.shape = (176,), counts_sorted.shape = (176,)
/var/folders/_q/911zk1853mv45phss2fsffd00000gn/T/ipykernel_80767/1305327222.py:1
07: UserWarning: The figure layout has changed to tight
 plt.tight_layout()



Neuron 29: dirs_sorted.shape = (176,), counts_sorted.shape = (176,)
/var/folders/_q/9l1zk1853mv45phss2fsffd00000gn/T/ipykernel_80767/1305327222.py:1
07: UserWarning: The figure layout has changed to tight
 plt.tight_layout()



Neuron 37: dirs_sorted.shape = (176,), counts_sorted.shape = (176,)

1.4.1 Tuning Curves for neurons visualized

```
[20]: all_neuron_ids = spikes["Neuron"].unique()
   num_neurons = len(all_neuron_ids)
   ncols = 4
   nrows = int(np.ceil(num_neurons / ncols))

fig, axes = plt.subplots(
        nrows, ncols, figsize=(ncols * 5, nrows * 4), sharex=True, sharey="row"
)
   axes = axes.flatten()

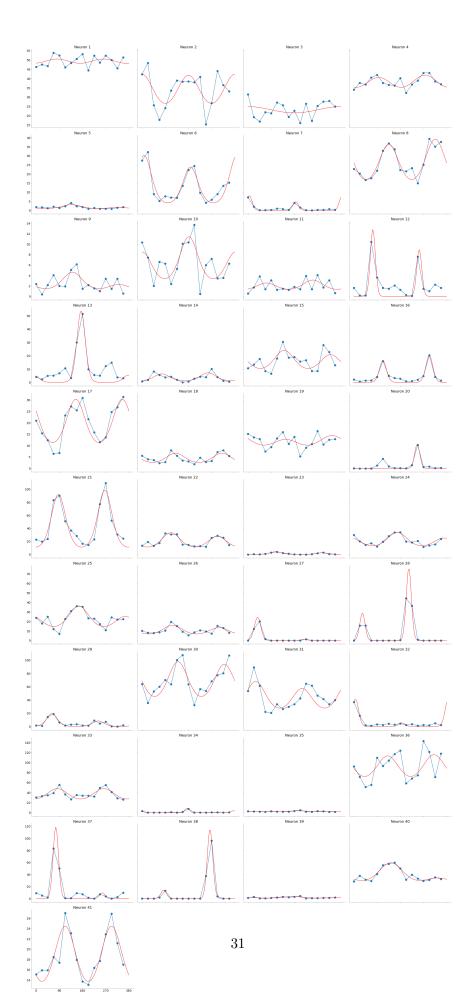
for i, neuron_id in enumerate(all_neuron_ids):
    if i >= len(axes):
        break
   ax = axes[i]
   dirs_sorted, counts_sorted = get_data(spikes, neuron_id)
   p_opt = None
```

```
r_sq = None
    try:
        p_opt = tuningCurve(counts_sorted, dirs_sorted, neuron_id=neuron_id,_u
 ⇔show=False)
    except Exception as e:
        logger.warning(f"Error fitting tuning curve for neuron {neuron id}:
 →{e}")
        p_opt = None
    # You'd also need mean_counts_to_fit and unique_stim_directions_deg here
    spike_count_matrix_x = compute_spike_count_matrix(counts_sorted,__

dirs_sorted)

    mean_counts_to_fit = np.mean(spike_count_matrix_x, axis=0)
    unique_stim_directions_deg = np.unique(dirs_sorted)
    ax.plot(unique_stim_directions_deg, mean_counts_to_fit, "o-")
    if p_opt is not None:
        theta_plot_deg = np.linspace(0, 360, 100)
        fitted_values = vonMises(np.deg2rad(theta_plot_deg), *p_opt)
        ax.plot(theta_plot_deg, fitted_values, "r-")
    ax.set_title(f"Neuron {neuron_id}")
    ax.set_xticks(np.arange(0, 361, 90))
for j in range(i + 1, nrows * ncols):
    if j < len(axes): # Check if axes[j] exists</pre>
        fig.delaxes(axes[j])
plt.tight_layout()
plt.show()
```

/var/folders/_q/911zk1853mv45phss2fsffd00000gn/T/ipykernel_80767/567795990.py:42
: UserWarning: The figure layout has changed to tight
 plt.tight_layout()



1.5 Task 4: Permutation test for direction tuning

Implement a permutation test to quantitatively assess whether a neuron is direction/orientation selective. To do so, project the vector of average spike counts, $m_k = \frac{1}{N} \sum_j x_{jk}$ on a complex exponential with two cycles, $v_k = \exp(\psi i \theta_k)$, where θ_k is the k-th direction of motion in radians and $\psi \in 1, 2$ is the fourier component to test (1: direction, 2: orientation). Denote the projection by $q = m^T v$. The magnitude |q| tells you how much power there is in the ψ -th fourier component.

Estimate the distribution of |q| under the null hypothesis that the neuron fires randomly across directions by running 1000 iterations where you repeat the same calculation as above but on a random permutation of the trials (that is, randomly shuffle the entries in the spike count matrix x). The fraction of iterations for which you obtain a value more extreme than what you observed in the data is your p-value. Implement this procedure in the function testTuning().

Illustrate the test procedure for one of the cells from above. Plot the sampling distribution of |q| and indicate the value observed in the real data in your plot.

How many cells are tuned at p < 0.01?

Grading: 3 pts

```
[21]: def compute null distribution(
          counts: np.ndarray,
          dirs: np.ndarray,
          v_k: np.ndarray,
          niters: int,
          rng: np.random.Generator,
      ) -> np.ndarray:
          """Compute the null distribution of |q| under the null hypothesis.
          Parameters
          _____
          counts: np.ndarray
              The spike counts for each trial.
          dirs: np.ndarray
              The stimulus directions for each trial.
          v k: np.ndarray
              The complex exponential vector for the specified psi.
          niters: int
              Number of iterations for the permutation test.
          rng: np.random.Generator
              Random number generator for reproducibility.
          Returns
```

```
q_distribution_null: np.ndarray
              The computed null distribution of |q|.
          11 11 11
          # Initialize an array to store the |q| values from each permutation
          q_distribution_null = np.zeros(niters)
          logger.info(f"Starting permutation test with {niters} iterations...")
          for i in range(niters):
              shuffled_trial_counts = rng.permutation(counts)
              permuted_spike_matrix =_
       →compute_spike_count_matrix(shuffled_trial_counts, dirs)
              m_k_permuted = np.mean(permuted_spike_matrix, axis=0)
              q_complex_permuted = np.dot(m_k_permuted, v_k)
              q_magnitude_permuted = np.abs(q_complex_permuted)
              q_distribution_null[i] = q_magnitude_permuted
          logger.info("Permutation test finished.")
          return q_distribution_null
[22]: def plot_null_distribution(
          q_distribution_null: np.ndarray,
          q_observed_magnitude: float,
          niters: int,
          title: str = "Null Distribution of |q|",
      ):
          """Plot the null distribution of |q| and the observed |q|.
          Parameters
          q_distribution_null: np.ndarray
              The computed null distribution of |q|.
          q_observed_magnitude: float
              The observed magnitude of |q| from the original data.
          niters: int
              Number of iterations for the permutation test.
          plt.figure(figsize=(8, 6))
```

Plot the histogram of the null distribution

q_distribution_null,

plt.hist(

bins=50,

```
density=True,
    alpha=0.7,
    color="skyblue",
    label=f"Null Distribution of |q|\n({niters} permutations)",
)
# Add a vertical line for the observed |q|
plt.axvline(
    x=q_observed_magnitude,
    color="red",
    linestyle="--",
    linewidth=2,
    label=f"Observed |q| = {q_observed_magnitude:.4f}",
)
plt.title(title)
plt.xlabel("|q|")
plt.ylabel("Density")
plt.legend()
plt.grid()
plt.show()
```

```
[23]: def testTuning(
          counts: np.ndarray,
          dirs: np.ndarray,
          psi: int = 1,
          niters: int = 1000,
          show: bool = False,
          random_seed: int = 2046,
         neuron: int = None,
      ) -> Tuple[float, float, np.ndarray]:
          """Plot the data if show is True, otherwise just return the fit.
          Parameters
          _____
          counts: np.array, shape=(total_n_trials, )
              the spike count during the stimulation period
          dirs: np.array, shape=(total_n_trials, )
              the stimulus direction in degrees
          psi: int
              fourier component to test (1 = direction, 2 = orientation)
          niters: int
              Number of iterations / permutation
```

```
show: bool
      Plot or not.
  random_seed: int
      Random seed for reproducibility.
  Returns
  _____
  p: float
     p-value
  q: float
      magnitude of second Fourier component
  qdistr: np.array
      sampling distribution of |q| under the null hypothesis
  # -----
  # Calculate m, nu \ and \ q \ (0.5 \ pts)
  \# m - This is the vector of average spike counts for each unique stimulus
\hookrightarrow direction.
  spike_count_matrix = compute_spike_count_matrix(counts, dirs)
  m_k = np.mean(spike_count_matrix, axis=0)
  \# Get unique directions and convert to radians for v_k
  unique_stim_directions_deg = np.unique(dirs)
  theta_k_rad = np.deg2rad(unique_stim_directions_deg)
  # v_k - This is the complex exponential vector for the specified psi.
  # It should be based on the unique radian directions theta_k_rad.
  v_k = np.exp(1j * psi * theta_k_rad)
  # q - This is the projection of m_k onto v_k.
  q_complex_observed = np.dot(m_k, v_k)
  q_observed_magnitude = np.abs(q_complex_observed)
  logger.debug(f"Observed q magnitude: {q_observed_magnitude}")
  logger.debug(f"Observed q complex: {q_complex_observed}")
  logger.debug(f"Observed m_k: {m_k}")
  logger.debug(f"Observed v_k: {v_k}")
  # Estimate the distribution of q under the HO and obtain the p value (1 pt)
  # -----
  # Ensure reproducibility using a random number generator
```

```
# Hint: Access random functions of this generator
          rng = np.random.default_rng(random_seed)
          q_distribution_null = compute_null_distribution(
              counts=counts, dirs=dirs, v_k=v_k, niters=niters, rng=rng
          )
          # Calculate the p-value.
               This is the proportion of permuted |q| values that are as extreme as,
               or more extreme than, the |q| observed from the original data.
          # We use smoothing to avoid p-values of 0 or 1.
          p_value = (np.sum(q_distribution_null >= q_observed_magnitude) + 1) / ___
       \hookrightarrow(niters + 1)
          # p value = np.sum(q distribution null >= q observed magnitude) / niters
          logger.info(
              f"Observed |q|: {q_observed_magnitude:.4f}, Calculated p-value:
       \hookrightarrow{p_value:.35f}"
          )
          if show:
              neuron_title_str = "" if neuron is None else f"Neuron: {neuron}"
              title = f"Null Distribution {neuron_title_str} $\Psi$ : {psi} P Value:

¬{p_value:.05f}"
              plot_null_distribution(
                  q_distribution_null, q_observed_magnitude, niters, title=title
          qdistr = q_distribution_null
          return p_value, q_observed_magnitude, qdistr
[24]: def test_neuron_tuning(all_neuron_ids, spikes, niters=1000):
          """Test the tuning of a neuron for direction and orientation."""
          tuning_results = []
          for i, neuron_id in enumerate(all_neuron_ids):
              logger.info(f"Processing neuron {i+1}/{len(all_neuron_ids)}: ID_ |
       →{neuron_id}...")
```

```
show=False,
        neuron=neuron_id,
    )
    # Test for orientation tuning (psi=2)
    p_orientation, q_orientation, _ = testTuning(
        counts_sorted,
        dirs_sorted,
        psi=2,
        niters=niters,
        show=False.
        neuron=neuron_id,
    )
    tuning_results.append(
            "neuron_id": neuron_id,
            "p_direction": p_direction,
            "q_direction": q_direction,
            "p_orientation": p_orientation,
            "q_orientation": q_orientation,
        }
    )
return pd.DataFrame(tuning_results)
```

```
[25]: def filter_tuning_results(tuning_results_df, alpha_threshold=0.01):
          """Filter the tuning results based on the significance level."""
          logging.debug(f"\n--- Tuning Selectivity Results (p < \{alpha\_threshold\})_{\sqcup}
       ---")
          direction_selective_neurons = tuning_results_df[
              tuning_results_df["p_direction"] < alpha_threshold</pre>
          orientation_selective_neurons = tuning_results_df[
              tuning_results_df["p_orientation"] < alpha_threshold</pre>
          1
          logging.debug(f"\nDirection Selective Neurons (psi=1, p <⊔
       →{alpha_threshold}):")
          if not direction_selective_neurons.empty:
              logging.debug(
                  direction_selective_neurons[["neuron_id", "p_direction", "

¬"q_direction"]]
              )
          else:
              logging.debug(
```

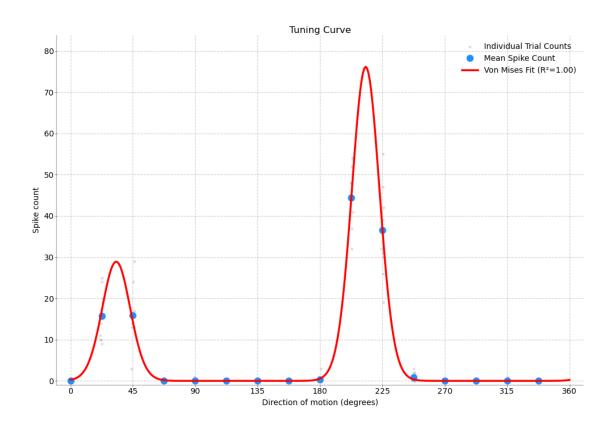
```
"No neurons found to be significantly direction selective at this...
\hookrightarrowthreshold."
       )
  logging.debug(f"\nOrientation Selective Neurons (psi=2, p <__

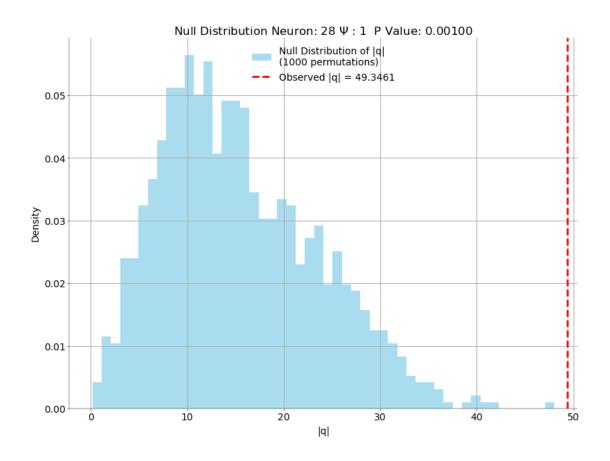
√{alpha threshold}):")
  if not orientation_selective_neurons.empty:
      logging.debug(
           orientation_selective_neurons[
               ["neuron_id", "p_orientation", "q_orientation"]
      )
  else:
       logging.debug(
           "No neurons found to be significantly orientation selective at this \sqcup
\hookrightarrowthreshold."
       )
  both_selective = tuning_results_df[
       (tuning_results_df["p_direction"] < alpha_threshold)</pre>
      & (tuning_results_df["p_orientation"] < alpha_threshold)
  1
  logging.debug(
       f"\nNeurons Selective for BOTH Direction and Orientation (p <_{\sqcup}
)
  if not both_selective.empty:
       logging.debug(both_selective[["neuron_id", "p_direction", u

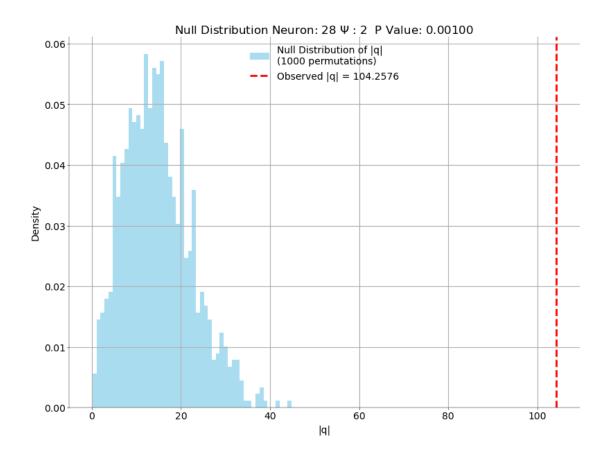
¬"p_orientation"]])
  else:
      logging.debug(
           "No neurons found to be significantly selective for both at this.
⇔threshold."
  strictly_direction_selective = tuning_results_df[
       (tuning results df["p direction"] < alpha threshold)</pre>
       & (tuning_results_df["p_orientation"] >= alpha_threshold)
  logging.debug(
       f"\nNeurons Strictly Direction Selective (p_dir < {alpha_threshold},__
→p_ori >= {alpha_threshold}):"
  )
  if not strictly_direction_selective.empty:
      logging.debug(
```

Show null distribution for the example cell:

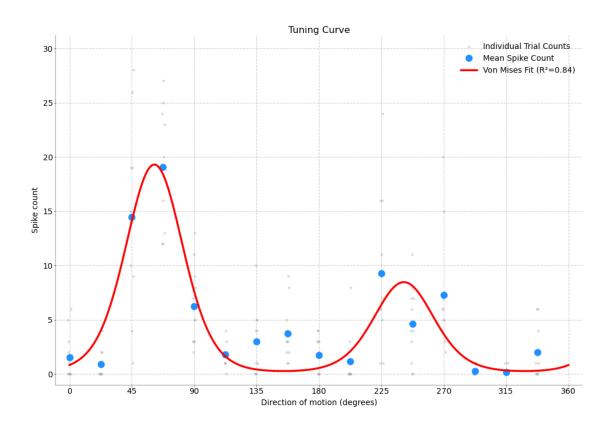
/var/folders/_q/911zk1853mv45phss2fsffd00000gn/T/ipykernel_80767/1305327222.py:1
07: UserWarning: The figure layout has changed to tight
 plt.tight_layout()

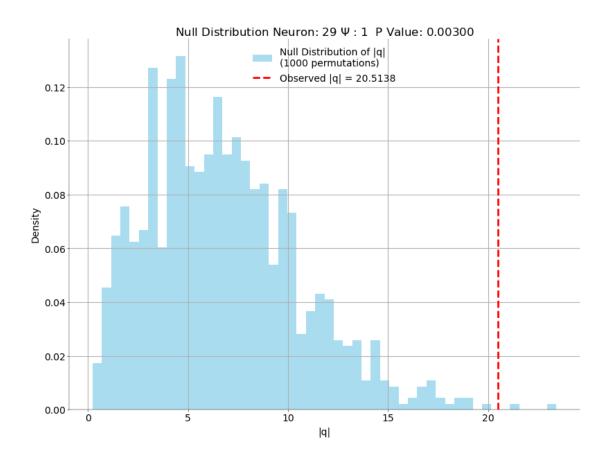


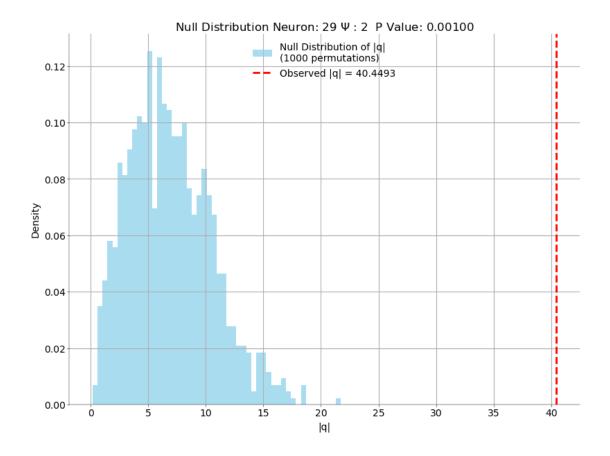




/var/folders/_q/911zk1853mv45phss2fsffd00000gn/T/ipykernel_80767/1305327222.py:1
07: UserWarning: The figure layout has changed to tight
 plt.tight_layout()







Test all cells for orientation and direction tuning

```
[28]: num_direction_tuned = len(direction_selective_neurons)
num_orientation_tuned = len(orientation_selective_neurons)
num_both_tuned = len(both_selective)
```

```
total_unique_tuned_cells = num_direction_tuned + num_orientation_tuned -_u

num_both_tuned

print(
    f"Total number of unique neurons showing any tuning (direction or_u

orientation, p < 0.01): {total_unique_tuned_cells}"
)
```

Total number of unique neurons showing any tuning (direction or orientation, p < 0.01): 34

Number of direction tuned neurons:

```
[29]: print(f"Number of direction selective neurons:

→{len(direction_selective_neurons)}")
```

Number of direction selective neurons: 12

Number of orientation tuned neurons:

```
[30]: print(f"Number of orientation selective neurons:

□

⟨-{len(orientation_selective_neurons)}")
```

Number of orientation selective neurons: 34

Number of neurons selective for both: 12 Number of strictly direction selective neurons: 0

```
[32]: print("List direction sensitive Neurons:")
    print(direction_selective_neurons)
    print("---")
    print("List orientation sensitive Neurons:---")
    print(orientation_selective_neurons)
    print("---")
```

List direction sensitive Neurons:

	neuron_id	$p_direction$	${ t q_direction}$	${ t p_orientation}$	${\tt q_orientation}$
12	13	0.000999	77.950288	0.000999	48.359041
19	20	0.000999	9.297844	0.000999	12.687638
23	24	0.001998	31.400913	0.000999	61.437416
24	25	0.003996	35.699993	0.000999	64.973538
26	27	0.000999	31.640129	0.000999	32.030661
27	28	0.000999	49.346055	0.000999	104.257627
28	29	0.002997	20.513794	0.000999	40.449320

30	31	0.000999	89.125639	0.000999	126.462049					
31	32	0.000999	43.971208	0.000999	47.458766					
36	37	0.000999	124.294759	0.000999	98.977689					
37	38	0.000999	119.906485	0.000999	142.278675					
39	40	0.000999	90.873419	0.000999	57.588171					
<i></i>		0.000999	90.073419	0.002991	57.500171					
List orientation sensitive Neurons:										
	neuron_id	p_direction	q_direction	p_orientation	q_orientation					
1	2	0.476523	13.188314	0.000999	69.584958					
2	3	0.063936	16.616565	0.001998	27.711406					
5	6	0.122877	19.423996	0.000999	79.765526					
6	7	0.277722	3.554301	0.000999	12.721692					
7	8	0.608392	12.447186	0.000999	81.147705					
9	10	0.339660	8.790470	0.002997	20.855551					
11	12	0.206793	5.174151	0.000999	14.809007					
12	13	0.000999	77.950288	0.000999	48.359041					
13	14	0.767233	2.969608	0.000999	24.945998					
14	15	0.239760	16.927466	0.000999	43.273723					
15	16	0.859141	3.880623	0.000999	42.754483					
16	17	0.025974	24.372216	0.000999	79.649865					
17	18	0.116883	7.239444	0.000999	14.349402					
19	20	0.000999	9.297844	0.000999	12.687638					
20	21	0.955045	9.478136	0.000999	285.435722					
21	22	0.070929	20.760966	0.000999	70.947070					
22	23	0.044955	4.684794	0.000999	11.984867					
23	24	0.001998	31.400913	0.000999	61.437416					
24	25	0.003996	35.699993	0.000999	64.973538					
25	26	0.582418	6.110360	0.000999	27.314082					
26	27	0.000999	31.640129	0.000999	32.030661					
27	28	0.000999	49.346055	0.000999	104.257627					
28	29	0.002997	20.513794	0.000999	40.449320					
29	30	0.881119	10.492633	0.000999	194.989028					
30	31	0.000999	89.125639	0.000999	126.462049					
31	32	0.000999	43.971208	0.000999	47.458766					
32	33	0.399600	15.009117	0.000999	76.786618					
33	34	0.010989	5.643544	0.000999	9.966181					
35	36	0.024975	79.275292	0.000999	191.295301					
36	37	0.000999	124.294759	0.000999	98.977689					
37	38	0.000999	119.906485	0.000999	142.278675					
38	39	0.043956	5.267488	0.001998	7.868793					
39	40	0.000999	90.873419	0.002997	57.588171					
40	41	0.900100	2.887781	0.000999	41.503439					
	-									