NCEA Level 2 Mathematics

Year 11 diagnostics

These questions are at the level required for NCEA Level 1 mathematics. At a bare minimum, students starting Y12 should be comfortable with those questions in part A. Students aiming for a merit or excellence in Level 2 should also revise the questions in part B.

Part A

A calculator isn't needed.

- 1. Write $\frac{3}{4} \frac{1}{3}$ as a single fraction.
- 2. If a = 5 and b = a 3, what is the value of 3a b?
- 3. What possible values of x make the equation 3x 8 = -4x + 34 true?
- 4. What possible values of y make the equation $x^2 x = 20$ true?
- 5. Write $\frac{x+1}{x-1} + \frac{x+1}{x-2}$ as a single fraction.
- 6. Give the equation of the line through the two points (0,1) and (2,3).
- 7. The two shorter sides of a right-angled triangle measure 2 m and 1 m. What are the measures of the three internal angles of the triangle?
- 8. Calculate the mean value of the following data: $\{2, 3, 6, 7, 9\}$.

Part B

A calculator might be useful here.

- 1. Because of inflation, the price of all homes for sale in a new subdivision are to be increased by 5%. If the new price for each lot is to be \$450,000, what is the current price of a lot?
- 2. A rectangular plot of land has area $28 \,\mathrm{km^2}$. If one side length is three kilometres more than the other side length, what are the dimensions of the plot?
- 3. Consider the following party trick.

Pick any number.

Add 11.

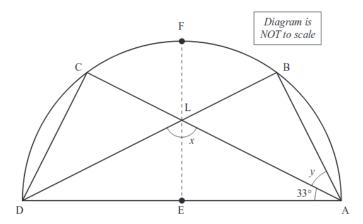
Divide by 2.

Multiply by 6.

Subtract 3 times your original number.

The magician (perhaps too strong a word) hands you a sealed envelope containing your final number. Why are you not surprised to find she is correct?

- 4. A chemist is mixing one container of a 7% solution of a chemical and another container of a 4% solution to produce 5 litres of a 5% solution. Calculate the volume of each solution needed.
- 5. A flagpole is known to be 10 m high. At a certain time, the length of the shadow cast by the flagpole is 0.5 m. At what angle are light rays from the top of the flagpole hitting the ground?
- 6. The following construction is made from a semicircle and two triangles.



The diameter of the semicircle is AD. The construction is symmetric about the line EF. Calculate the values of x and y.

7. Consider two lines. One passes through the points (0,3) and (2,5); the other passes through the points (3,4) and (5,6). Either find the point of intersection, or use precise mathematical reasoning to show that they do not intersect.