The objective of this exam is to test your understanding of week 7 of the CIS 194 Spring 2013 course (folds and monoids).

Name

1. (1 point) The foldr function, applied to a binary operator, a starting value, and a list, reduces the list using the binary operator, from right to left:

```
foldr :: (a \rightarrow b \rightarrow b) \rightarrow b \rightarrow [a] \rightarrow b
foldr f acc [] = acc
foldr f acc (x:xs) = f x (foldr f acc xs)
```

The filter function, applied to a predicate and a list, returns the list of those elements that satisfy the predicate:

Can you define filter in terms of foldr?

- 2. The fold1 function, applied to a binary operator, a starting value, and a list, reduces the list using the binary operator, from left to right.
 - (a) (1 point) Complete the definition of foldl:

```
foldl :: (b \rightarrow a \rightarrow b) \rightarrow b \rightarrow [a] \rightarrow b
foldl f acc [] = acc
foldl f acc (x:xs) =
```

- (b) (1 point (bonus)) What is the difference between the following expressions?
 - foldr (+) 0 [1..5]
 - foldl (+) 0 [1..5]

3. (1 point) A monoid is a type with an associative binary operation that has an identity:

```
class Monoid a where
  mempty :: a
  mappend :: a -> a -> a
```

Instances of Monoid should satisfy the following laws:

```
mappend mempty x = xmappend x mempty = x
```

```
• mappend x (mappend y z) = mappend (mappend x y) z
```

Remember the Maybe type?

```
data Maybe a = Nothing | Just a
```

Define an instance of Monoid for Maybe a:

```
instance Monoid a => Monoid (Maybe a) where
  mempty :: Maybe a
  mappend :: Maybe a -> Maybe a -> Maybe a
  mappend
```