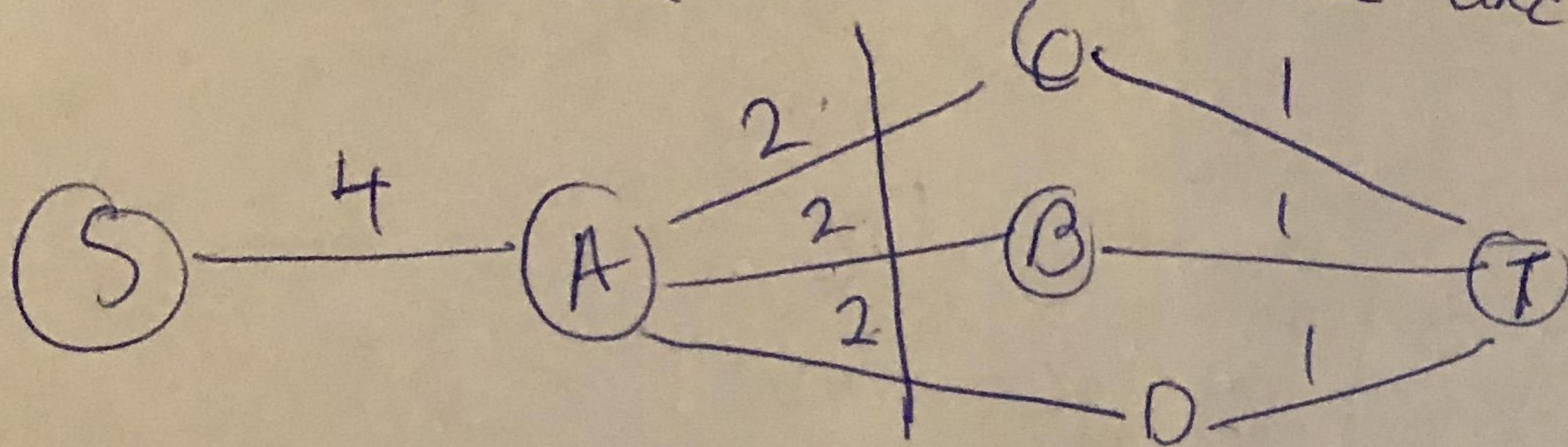
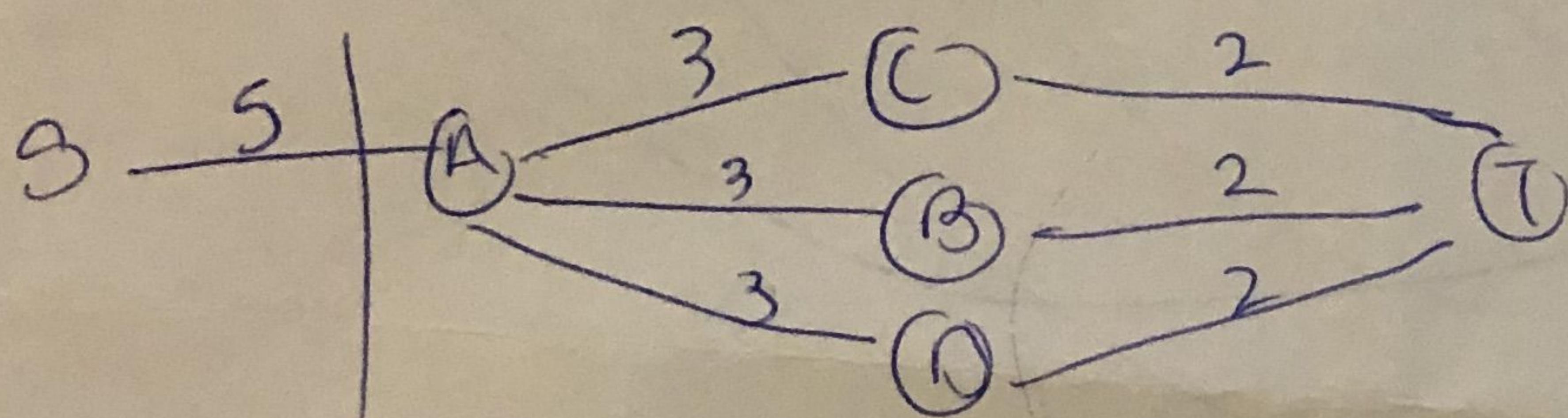


③ Consider a graph where S -source and $T \rightarrow$ sink



Proposition: we increase the capacity of each edge by 1 then (A β) must still be minimum cut.

The minimum cut gets changed when ~~it~~ contains edges different in capacity. The maximum cut above has capacity 6, increasing the capacity of each edges by 1 increases the cut to 9. So the new minimum cut from S to A with a capacity of 6.



When edges have the same capacity, increasing the capacity of every edge by 1 will not change the minimum cut.

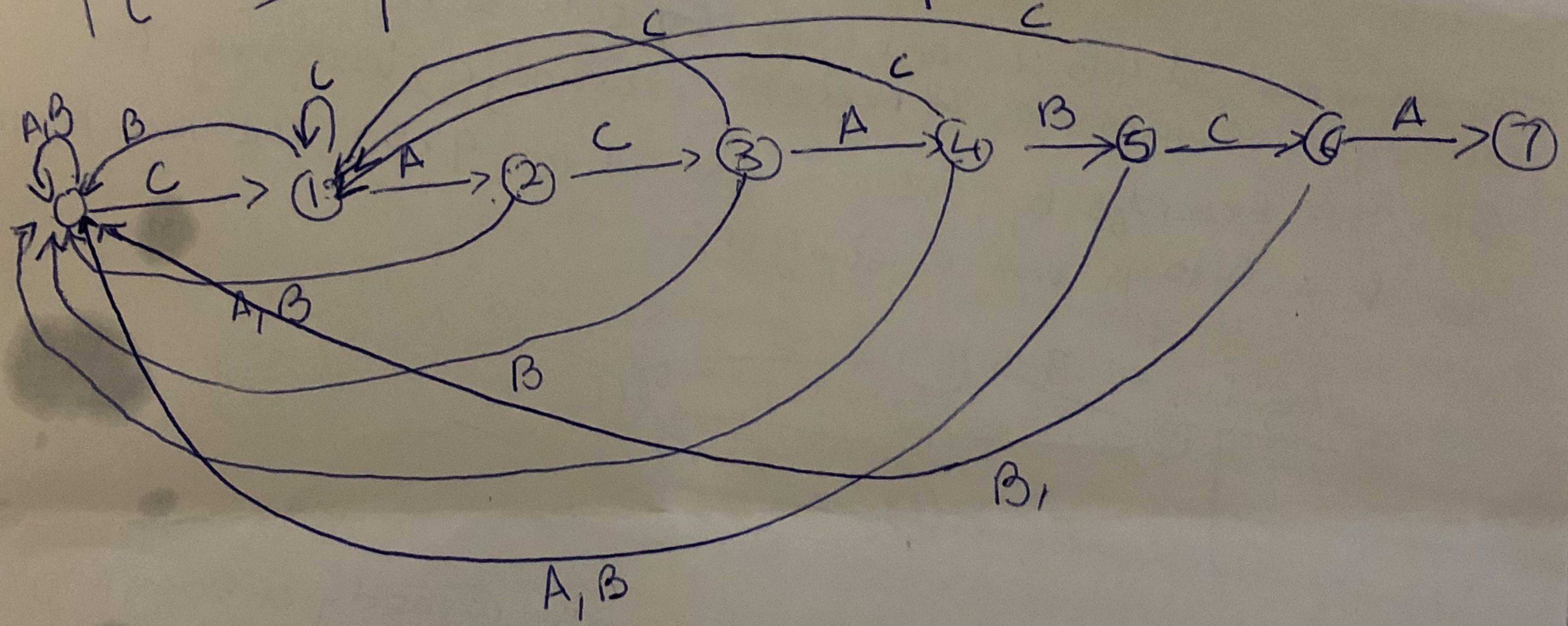
Let $N_c \rightarrow$ cut capacity
 $n \rightarrow$ number of edges
 $c \rightarrow$ constant
 $N \rightarrow$ minimum

If the capacity of each cut is increased by 1, we have $N(c+1)$ and the minimum cut is $N(c+1)$. Assuming a cut larger than ~~N(c+1)~~ exists, since all edges has weight $c+1$, such cut must be M -edge cut for some $M > N$. This would ~~prove~~ contradicting the original graph would have capacity $Nc > N$. So no such M -edge cut can exist because it contradicts the assumption that N edge cut is optimal.

④ CACABCAC

	0	1	2	3	4	5	6
0	C	A	C	A	B	C	A
1	G	2	0	4	0	0	7
2	0	0	0	0	5	0	0
3	0	1	3	1	1	6	1
4	0	1	1	1	1	6	1
5	0	0	0	0	0	0	0
6	0	0	0	0	0	0	0

dfac303



⑤

- ① for every ship full of k -comedians
 $2k$ -ordinary people
- * Each comedian has a boat
 - w * Each boat can carry two additional passengers
 - + certain non-comedians dislike certain comedians
- ~~\$600 - Sydney~~

Let a non-comedian be represented by NC

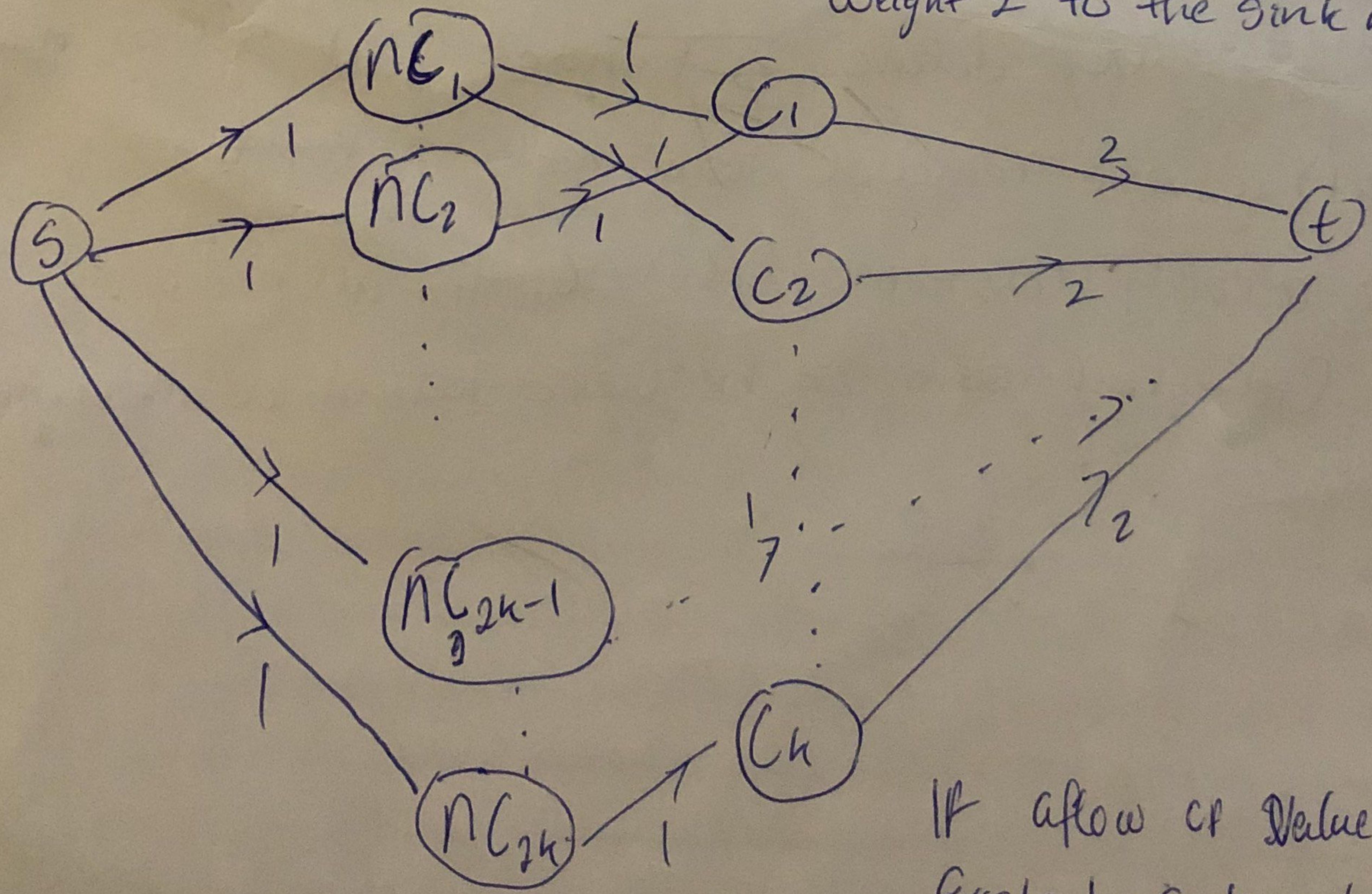
let a comedian be represented by C

Since certain non-comedians dislike certain comedians, we draw edges from a non-comedian node to all comedian nodes whose jokes they can tolerate and assign capacity 1.

+ Assign a source node s , and sink node t .

+ draw edges of capacity 1 to each non-comedian node

+ for each comedian node draw edges of weight 2 to the sink node.



If a flow of value $2k$ from source s exists to sink node then it is possible to evacuate everyone.

② Ford-Fulkerson algorithm has two main steps, first is labelling process that searches for a flow augmenting path

- * from s source to t sink for which $f \leq c$ along all forward arcs and $f > 0$ along all backward arcs

We start by ~~constructing a graph A where for every vertex v in G we would have vertices v_i to v_o~~

- * There is an edge from v_i to v_o of capacity c_v
- * the Max-flow Min-cut theorem for node capacity is the maximum capacity of an $s-t$ node capacity flow of graph G is equals to the minimum capacity of an $s-t$ node cut in G

- * use for each edge of G (v_i, v_o) with capacity c_v , any flow in h corresponds to flow in G and all node capacities are satisfied. We define $s-t$ node cut set of nodes $V' \subseteq V - (s+t)$ whose removal disconnects s from t .

The node capacity constraints $f_{in}(v) \leq c_v$ for all nodes
therefore Ford-Fulkerson can be used to find a maximum $s-t$ flow.

5 Using a wildcard token, given a pattern of length m , we hash it, we first start by hashing the first n characters of the, if they are not the same then it is impossible for the two strings to be the same, if they are the same then we ~~need~~ use the normal string for comparison or to check if they are hashed to the same value. If not we continue and shift over a character in the text string.