A Computable Expression for the Spatial Distribution of Extracellular Spike Waveforms Enables in Silico Localization of Neurons

Alexander Olsson alexander.olsson@bme.lth.se

I. INTRODUCTION

With implanted electrodes, it is possible to record the aggregate activity of demarcated populations of neurons within the central nervous system for extensive periods of time [1]. In a process typically referred to as *spike sorting*, recordings obtained in this way can (assuming sufficient signal quality) blindly be decomposed into contributions originating from individual neurons by exploiting inter-neuronal variation in extracellular spike waveforms arising from the spatial dependency of waveform morphology [2]. Such techniques can be invaluable for researchers that wish to study neuronal behaviours both at the individual and network level.

As most assays that involve invasive neural recordings are aimed at uncovering neuronal firing behaviour, processing pipelines for spike sorting typically do not give any explicit information on the geometry of the latent neuronal signal sources that are found. Notably, extracting this information is not trivial, as it requires solving an *inverse problem*. On the other hand, the ability to infer the relative positions of individual neurons by processing extracelluar recordings could enable some interesting applications—conjectured examples include electrode drift detection [3] and high-resolution monitoring of neuronal density [4].

If one has knowledge of the process that generates extracellular recordings, it is tempting to treat the inverse problem of localizing individual neurons as an optimization problem. Specifically, if one as access to an explicit formulation of the so-called forward mapping $f:G\longrightarrow R$ that transforms the geometry G to a recording R it is possible to formulate the inverse problem as finding a candidate geometry G that minimizes $D(f(\tilde{G}), \hat{R})$, where \hat{R} is a recording obtained from the true geometry and $D(\cdot, \cdot)$ is some appropriate distance metric. In this paper, I present and evaluate a rudimentary method based on this reasoning for solving the inverse problem of neuron localization by using a computationally efficient model of the forward mapping introduced in [5].

II. METHODS

In this section, I give an overview of (1) the proposed algorithmic framework for neuron localization and (2) a selection of *in silico* experiments performed for the purpose of evaluating the framework. The entirety of the current study was performed using custom Python 3.5 code¹.

If not otherwise specified, the sampling rate is assumed to be $f_s = 25000$ samples/s and the durations of recordings is assumed to be to be $D = f_s \cdot 60s = 1500000$ samples.

A. Neuronal Model

As the aim of this work was to simulate and subsequently locate neurons, a necessary first step was to define a suitable model of individual neurons. For the purposes of this study, a neuron was conceptualized as having 3 free parameters:

- 1) A spatial *position* $\mathbf{P}_n \in \mathbb{R}^3$, to be interpreted as the location of the soma in some 3D coordinate system. Succinctly, the aim of this study is to be able to derive this value from observations of extracelluar recordings.
- 2) A constant firing rate $F \in \mathbb{R}^+$, to be interpreted as the expected number of action potentials that the neuron fires per unit of time. While a constant firing rate is not necessarily a biologically reasonable assumption, it is arguably a justifiable simplification in sufficiently short recordings.
- 3) A categorical *type T*. This auxiliary variable is intended to encode all inter-neuronal morphological variation, e.g. shape, size, and bioelectrical idiosyncrasies.

To use (populations of) this neuronal model to simulate extracellular voltage recordings, a computable expression for the extracellular spike waveform, dependent on the relative positions of neurons and electrodes, is needed. For this purpose, let $\mathcal{W}_T(\mathbf{P}_e, \mathbf{P}_n) \in \mathbb{R}^L$ denote the L equitemporal voltages sampled by a hypothetical electrode located at $\mathbf{P}_e = (x_e, y_e, z_e)$ over a time of $\frac{L}{f_s}$ seconds following the onset an action potential fired by a neuron of type T at position $\mathbf{P_n} = (x_n, y_n, z_n)$. Whereas the localization framework presented in this paper is agnostic to the choice of mathematical formulation for \mathcal{W}_T , the model introduced in [5] was used in all parts of the current study for practical reasons. This specific formulation, wherein $T \in [1, 4]$, has several desirable properties for my aims here, most saliently its computationally simplicity and full translation-invariance, i.e. $\mathcal{W}_T(\mathbf{P}_e, \mathbf{P}_n) = \mathcal{W}_T(\mathbf{P}_e - \mathbf{P}_n)$. To be able to make

¹All code written for this paper is available at www.github.com/aeolsson/neuron_localization

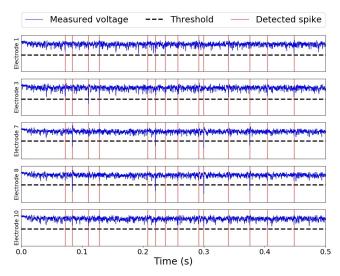


Fig. 1: A simulated recording, comprised of 5 randomly selected electrode channels, with appertaining spike detections.

straightforward use of preimplemented .mat files from [5], the duration of the waveform was in this study always set as L=100 samples.

To quantify the aggregate effect a single neuron has on an electrode over the course of an entire recording, knowing the spatial distribution of waveforms associated with each of its firings is not sufficient; it is also necessary to simulate at what times the neuron actually fires. For this, a gamma distribution [6] with shape parameter k = 5 and scale parameter $\theta = \frac{1}{kF}$ was used to sample neuron-specific interspike intervals (ISIs) that could subsequently used to derive a neuron-specific spike train S, where $S_t = 1$ if the neuron fires at time t and $\mathbf{S}_t = 0$ otherwise. The signal $\mathbf{X} \in \mathbb{R}^D$ originating from a neuron of type T located at \mathbf{P}_n observed by an electrode located at P_e can then be obtained by convolving S with $\mathcal{W}_T(\mathbf{P}_e, \mathbf{P}_n)$. For a geometry with N neurons with types $T_1,...,T_N$ at positions $\mathbf{P}_n^1,...,\mathbf{P}_n^N$, each with an associated simulated spike train, the voltage signal observed by an electrode can be obtained by summation over the contributions of all neurons. I here assume linearity (i.e. adding an additional electrode never affects the recordings of any other electrode)—the signal observed by each electrode in a multi-electrode system can be thus computed independently by following the aforementioned procedure electrodewise.

B. Data Synthesis

To simulate extracellular neural recordings, a measurement geometry (i.e. a set of neurons and a set of electrode location) was first created. The neurons of the geometry consisted of (1) a population of *target neurons* and (2) a population of *noise neurons*. As has already been alluded to, the aim of the experiments of the current study was to locate, i.e. infer the positions of, all target neurons. Conversely, the purpose of the noise neurons was to realistically represent background noise that an electrode would be subjected to.

For all experiments in this study, the population of noise neurons was constructed by defining a hollowed-out cylinder centered on the origin with outer radius $r_o = 250 \mu m$, inner radius $r_i = 100 \mu m$, height $h = 500 \mu m$, and neuronal density $\rho = 9.5 \cdot 10^6$ neurons/ μm^3 . With this, a homogeneous population of noise neurons was generated as follows:

- 1) The expected number of noise neurons $\rho \pi (r_o^2 r_i^2)(h) \approx 705.1$ was computed and rounded to the nearest integer $N_{noise} = 705$.
- 2) For all $i \in [1, N_{noise}]$:
 - a) Sample ξ_1 from the uniform distribution $\mathcal{U}(\frac{r_i^2}{r^2},1)$, ξ_2 and ξ_2 from the uniform distribution $\mathcal{U}(0,1)$.
 - b) Set $r = r_0 \cdot \sqrt{\xi_1}$, $\theta = 2\pi \cdot \xi_2$, and $z = \xi_3 \cdot h \frac{h}{2}$.
 - c) Set the position of the *i*:th noise neuron to $\mathbf{P}_n = (r\cos\theta, r\sin\theta, z)$.

Each noise neuron was randomly assigned a type between 1 and 4, and a firing rate between 1 Hz and 50 Hz.

The population of target neurons and the numbers and positions of electrodes differed between specific experiments and is discussed in sections II-G, II-H, and II-I. In the sections following, \mathbf{P}_n^i and T_i refer to the true position and type, respectively, of the ith target neuron.

Once a geometry had been constructed, a recording matrix $\mathbf{X} \in \mathbb{R}^{E \times D}$, where E is the number of electrodes, was simulated by superimposing the contributions of all neurons as described in section II-A. As preprocessing, the electrodewise sample mean was always subtracted from the recording.

C. Spike Detection

For the *i*th electrode of the recording, a spike detection threshold was set to $-8 \cdot MAD_i$, where MAD_i is median absolute deviation of $\mathbf{X}_{i,*}$ (the recording of the *i*th electrode). Firing events (not yet specific to any target neuron) were assigned to all samples where the recorded voltage fell below this threshold. A first-order difference filter was used to ensure that only the first sample of a continuous sequence of samples below the threshold was counted as a detection. Spike times obtained in this way were lastly aligned by shifting them forward in time to the peak value reached by the signal within 10 samples.

To obtain a total estimate of firing times, the spike times detected from all electrodes separately were simply pooled. A refractory period of 25 samples was assumed, meaning that spike events detected within $25/f_s=1$ ms after a previously detected spike were discarded. A global list of firing times was thusly obtained, each representing the firing time of any target neuron. While this procedure sometimes underestimates the firing rates of neurons (true spikes will not be detected if they occur during the refractory period of another neuron), this is of minimal consequence for the purpose of localization. An example of a recording with firing times detected can be viewed in Figure 1.

From each of the S detected firing times t_sD , $s \in [1, S]$, a spike waveform matrix $\mathbf{W}^s \in \mathbb{R}^{E \times L}$ was constructed by extracting the L/4 preceding samples and succeeding 3L/4 samples from all electrodes of the recording.

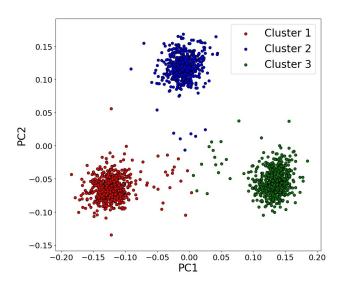


Fig. 2: An example of results from waveform source attribution in a case with N=3 target neurons. Each point represents a single extracted waveform and is colored according to what neuron it was attributed to. Note that the full $E \cdot L$ -dimensional waveform feature space was used as the basis for clustering; principal component analysis was used only for dimensionality reduction to allow for two-dimensional visualization.

D. Spike sorting

Using the sequence of spike times $t_1,...,t_S$, each with an appertaining waveform matrix $\mathbf{W}^1,...,\mathbf{W}^S$, a spike sorting procedure was used to determine from which of the neurons each spike originated. Specifically, KMeans clustering (SKLearn [7] implementation) applied on the full $E \cdot L$ -dimensional waveform feature space was used to assign a neuronal membership $M_s \in [1,N]$ (N is the number of target neurons) to each waveform and spike time. The number of clusters was set to the number of target neurons in the geometry, and as such the method currently requires prior knowledge on the true number of target neurons. An example of the result of this clustering is shown in Figure 2.

E. Estimation of Waveform Morphology

Even when their neuronal affiliations are known, the individually extracted waveform matrices make for poor proxies for the true action potential-triggered waveform matrices (too much interference from other neurons). Instead, for the ith detected target neuron, an archetypal waveform matrix $\bar{\mathbf{W}}^i \in \mathbb{R}^{E \times L}$ was computed by averaging over the all waveform matrices assigned as originating from that neuron. Incidentally, $\bar{\mathbf{W}}^i$ is also the centroid of the ith cluster found during spike sorting. Under the assumption that all electrode-channels are zero-mean (enforced as per section II-B), $\bar{\mathbf{W}}^i$ is an unbiased estimate of the true, recording-generating extracellular waveform matrix $[\mathcal{W}_{T_i}(\mathbf{P}_e^1, \mathbf{P}_n^i), ..., \mathcal{W}_{T_i}(\mathbf{P}_e^E, \mathbf{P}_n^i)]^T$. An example of archetypal waveform morhologies estimated by this approach is shown in Figure 3.

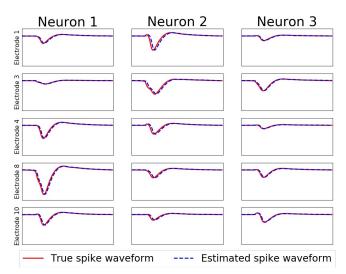


Fig. 3: An example of true (from geometry) and estimated (by spike-triggered averaging) waveforms. To generate this image, pairings between target neurons and detected clusters were made manually on the basis of waveform similarity.

F. Source Localization

Recall from section II-A that $\mathcal{W}_T(\mathbf{P}_e,\mathbf{P}_n) \in \mathbb{R}^L$ is the waveform that an electrode at position $\mathbf{P}_e = (x_e,y_e,z_e)$ would observe if a neuron at position $\mathbf{P}_n = (x_n,y_n,z_n)$ with type T fired (in this study approximated using the model from [5]). Now, let $\tilde{\mathbf{P}} = (\tilde{x},\tilde{y},\tilde{z})$ denote a candidate neuron position and \tilde{T} denote a candidate neuron type. Define the loss function $\mathcal{L}_i(\tilde{\mathbf{P}},\tilde{T}) \in \mathbb{R}^+$ pertaining to the ith target neuron as:

$$\mathcal{L}_{i} = \mathcal{L}_{i}(\tilde{\mathbf{P}}, \tilde{T}) = \frac{1}{E} \sum_{i=1}^{E} \frac{\|\mathcal{W}_{\tilde{T}}(\mathbf{P}_{e}^{j}, \tilde{\mathbf{P}}) - \bar{\mathbf{W}}_{j,*}^{i}\|_{2}^{2}}{\|\bar{\mathbf{W}}_{j,*}^{i}\|_{2}^{2}}$$

where $\|\cdot\|_2$ is the Euclidean norm, \mathbf{P}_e^j is the position of the jth electrode, and $\bar{\mathbf{W}}_{j,*}^i$ is the jth row of the archetypal waveform matrix pertaining to the ith detected neuron. In words, the value of $\mathcal{L}_i(\tilde{\mathbf{P}},\tilde{T})$ represents how dissimilar the archetypal waveform matrix is from the waveform matrix that would be observed by the electrodes if the ith target neuron had been located at $\tilde{\mathbf{P}}$ and had type \tilde{T} .

Importantly, $\mathcal{L}_i(\mathbf{P}_n^i,T_i)=0$, i.e. the loss is zero if the candidate position and candidate type are the true position and true type, respectively, of the ith target neuron². As $\mathcal{L}_i(\tilde{\mathbf{P}},\tilde{T})\geq 0$, it follows that this is a global minimum of the loss function. Thus, if this minimum is unique (not true for all geometries!), then the position and type of the ith neuron are the solution to the minimization problem:

$$\mathbf{P}_n^i, T_i = \operatorname*{argmin}_{\tilde{\mathbf{P}}, \tilde{T}} \mathcal{L}_i(\tilde{\mathbf{P}}, \tilde{T})$$

For geometries where N > 1, this minimization problem can be solved independently for each target neuron.

²Assuming that the waveform morphology estimation has zero errors, i.e. that $\bar{\mathbf{W}}_{j,*}^i = \mathcal{W}_{T_i}(\mathbf{P}_e^j, \mathbf{P}_n^i)$. If the waveform morphology estimation result is slightly noisy, we instead expect $\mathcal{L}_i(\mathbf{P}_n^i, T_i)$ to be small but nonzero

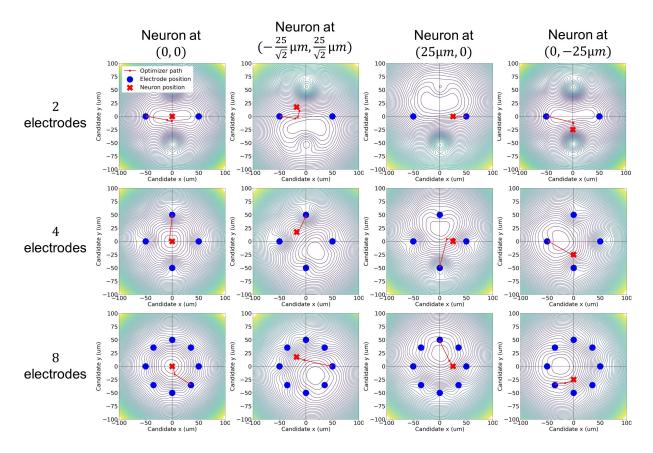


Fig. 4: Level curves of the loss function for the localization problem for different electrode setups and neuron locations. For illustration purposes, the loss function is here set as $\mathcal{L}^*_{2D}(\tilde{x},\tilde{y}) = \mathcal{L}^*(\tilde{x},\tilde{y},0)$ and it is thus not necessarily representative of the full 3-dimensional problem formulation. As can be seen from the optimizer path, conjugate gradient optimization starting from a random electrode position successfully converges on the true neuron position in all depicted cases.

From here on, I explicitly assume that all target neurons are of type T=1. Needless to say, this assumption entails a significant loss of generality, but was practically necessary to keep the project within time limits. With this assumption, the minimization problem for the *i*th neuron reduces to finding the candidate location that minimizes $\mathcal{L}_i^*(\tilde{\mathbf{P}}) = \mathcal{L}_i(\tilde{\mathbf{P}}, 1)$.

Any number of optimization algorithms could be applied to approximate the minimum of \mathcal{L}_i^* . In this study, the conjugate gradient method [8] (SciPy implementation [9]) was selected, as the success or failure this method would give an indication of whether or not the aforementioned minimization problem is convex. The gradient $\mathbf{g}_i = \nabla \mathcal{L}_i \in \mathbb{R}^3$ and Hessian $\mathbf{H}_i = \nabla \mathbf{g}_i \in \mathbb{R}^{3\times 3}$ were approximated by the central finite difference method with $\epsilon = 10^{-8}$. The algorithm was assumed to have converged once $\|\mathbf{g}_i\|_2 < 10^{-9}$. Examples of this localization method running in two dimensions with different geometries are illustrated in Figure 4.

G. Experiment 1: Cylindrical Electrode Array

The geometry of the first experiment is shown in Figure 5. 3 target neurons, all of type T=1 and with firing rate F=10 Hz, were placed at coordinates $\mathbf{P}_n^1 = (25\mu m, 0, 0), \mathbf{P}_n^2 = (0, -25\mu m, 25\mu m),$ and $\mathbf{P}_n^3 = (\frac{-25}{\sqrt{2}}\mu m, \frac{25}{\sqrt{2}}\mu m, -25\mu m).$ A population of 705 noise neurons was initialized as per the description in section II-B. A cylinder-shaped 3×5 electrode array centred about the origin with height $100\mu m$ and radius $50\mu m$ (5 electrodes placed equidistantly along the circumference of a circle with radius $50\mu m$ at each of the 3 heights $z=-50\mu m, z=0$, and $z=50\mu m$) was used to simulate recordings. Spike detection, sorting, and waveform morphology estimation was carried out in accordance with sections II-C, II-D, and II-E, respectively. Once archetypal waveform matrices had been established for each neuron in this way, the iterative localization algorithm from section II-F was initialized at the coordinates of a randomly selected electrode (independently for each of the $N\,=\,3$ neuron localization problems) and allowed to run until convergence or until 1000 iterations had passed, whichever came first. To be able to evaluate the accuracy of estimated neuron positions, each estimated neuron position was compared to the closest true neuron position in the geometry.

 $^{^3}$ As I have access to a closed-form expression of \mathcal{W}_T from [5], I could compute the gradient analytically. By instead assuming that I have no knowledge of the gradient, the localization method can straightforwardly be used with other extracellular waveform models that are more difficult to differentiate analytically.

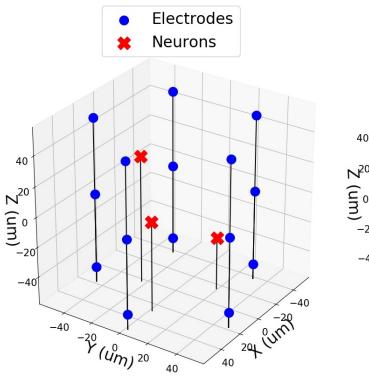


Fig. 5: Measurement geometry of the first experiment (cylindrical electrode array).

H. Experiment 2: Linear Electrode Array

The geometry of the second experiment is shown in Figure 6. Target neurons and noise neurons were initialized identically to experiment 1. A linear electrode array of length 8 electrode, equidistantly placed along the line connecting the end points $(0,0,-50\mu m)$ and $(0,0,50\mu m)$, was used to simulate recordings. Spike detection, sorting, and waveform morphology estimation was carried out in accordance with sections II-C, II-D, and II-E, respectively. Once archetypal waveform matrices had been established for each neuron in this way, the iterative localization algorithm from section II-F was initialized at the origin (0,0,0) and allowed to run until convergence or until 1000 iterations had passed, whichever came first. To be able to evaluate the accuracy of estimated neuron positions, each estimated neuron position was compared to the closest true neuron position in the geometry.

Due to the apparent symmetry of the geometry in this experiment, I hypothesized that it would be impossible to locate neurons, i.e. the solution to the minimization problem of section II-F would not be unique. The reasoning behind this conjecture was that the archetypal waveforms would look the same irrespective of the relative angle (but not distance!) between the source neuron and the electrode array—this would make exact localization by waveform dissimilarity minimization impossible.

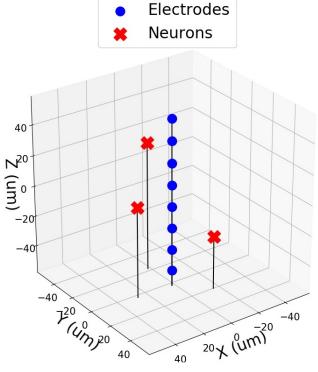


Fig. 6: Measurement geometry of the second experiment (linear electrode array).

I. Experiment 3: Sensitivity Analysis

In the work presented so far, the same waveform model $\mathcal{W}_T = \mathcal{W}_1$ (from [5]) has been used both to simulate recordings and to evaluate the quality of candidate neuron positions. Arguably, this casts doubt on the practical efficacy of the proposed localization method: Neural recording acquired *in vivo* would not neatly decompose into spike waveforms exactly equal to those predicted by any (tractable) computable model. Thus, an important question to ask is this: would the localization framework outlined in section II-F perform adequately if there was some small but nonzero bias separating empirically estimated archetypal waveforms from waveforms predicted by the computable expression for the spatial distribution of waveforms used to define the loss function?

To investigate the robustness of the localization framework to such systematic model-reality discrepancies, a small sensitivity analysis was carried out. The same electrode setup as the one from in experiment 1 (cylindrical) was used, but with only a single target neuron located at the origin. Once archetypal waveforms had been estimated, they were corrupted with Brownian noise (intended to represent a discrepancy between modelled waveforms and empirically estimated waveforms). This procedure was repeated 11 times with noise standard deviation ranging linearly between 0 and $5\mu V$. The neuron localization problem via loss minimization was solved 100 times at each such noise level and the accuracy of the final result saved.

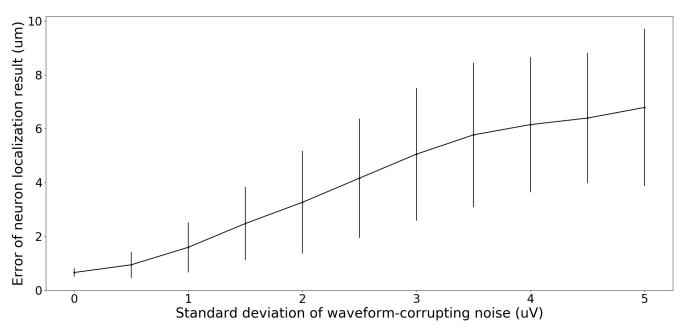


Fig. 7: Mean and standard deviation of localization error for different levels of Brownian noise added to the archetypal waveform matrices $\bar{\mathbf{W}}^1,...,\bar{\mathbf{W}}^N$ before starting the iterative localization algorithm.

TABLE I: Localization results for experiment 1 (cylindrical electrode array). All quantities are presented in μm .

Target Neuron #	True Position	Estimated Position
1	(25,0,0)	(24.20, -0.87, -4.24)
2	(0, -25, 25)	(0.70, -23.54, 26.50)
3	$(\frac{-25}{\sqrt{2}}, \frac{25}{\sqrt{2}}, -25)$	(-17.00, 15.96, -26.35)

III. RESULTS

A. Experiment 1: Cylindrical Electrode Array

Estimated neuron positions from the geometry with a cylindrical electrode array (experiment 1) paired with actual positions of target neurons are presented in Table I. These results correspond to Euclidean distances between true and estimated neurons of $4.41\mu m$, $2.20\mu m$, and $2.29\mu m$. As these distances are all smaller than the diameter of a typical soma, this result arguably constitutes reasonably accurate localization.

B. Experiment 2: Linear Electrode Array

Estimated neuron positions from the geometry with a linear electrode array (experiment 2) paired with actual positions of target neurons are presented in Table II. These results correspond to Euclidean distances between true and estimated neurons of $29.00\mu m$, $7.18\mu m$, and $8.98\mu m$. With errors of this size, the localization must be viewed as a failure for this geometry (as was hypothesized). However, the distances from the estimated locations to the electrode array center was very similar to the distances between the true neuron locations and the electrode array center, indicating that in this geometry, the method can still successfully estimate the distance to, but not the exact positions of, neurons.

TABLE II: Localization results for experiment 2 (linear electrode array). All quantities are presented in μm .

Target Neuron #	True Position	Estimated Position
1	(25,0,0)	(13.42, -26.13, -4.75)
2	(0, -25, 25)	(5.59, -26.85, 29.11)
3	$\left(\frac{-25}{\sqrt{2}}, \frac{25}{\sqrt{2}}, -25\right)$	(-12.14, 24.56, -26.63)

C. Experiment 3: Sensitivity Analysis

A plot if the relationship between Brownian noise variance and localization error is shown in Figure 7. Interestingly, the mean error of the localization method increases quite slowly with waveform corruption, indicating that localization can be successful even in cases when the spatial distribution model \mathcal{W}_T employed by the loss function does not exactly correspond to the latent waveform model that generated the recording.

IV. DISCUSSION

In this study, I have assumed that all target neuron are of the same type T=1. This is a major limitation, as the spatial distribution of spike waveforms surrounding a neuron can differ radically based on neuron morphology, such as the direction of the axon. The most pressing next step in developing this framework would thus be to incorporate some search over the space of candidate neuron types in order to find the best fit before starting the gradient-based localization step. Furthermore, the number of target neurons N to be located should ideally not have to be provided ex-ante, but instead be estimated by processing the recording. Fortunately, methods to estimate the number of target neurons in a recording already exist [3].

On a similar note, I have assumed exact knowledge of all electrode positions. This is clearly not a realistic assumption for many types of recordings. An interesting research question could thus be to expand the framework introduced here to simultaneously estimate electrode and neuron locations. Given that the positions of at least some electrodes and/or neurons can be provided to the algorithm (in order to counteract complete rotational and translational invariance), I conjecture that expanding the framework introduced in this paper could be as simple as expanding the search space for candidate positions from \mathbb{R}^3 to \mathbb{R}^{3I} in the case of I unknown electrode and/or neuron positions.

Whereas the results of the sensitivity analysis are at least encouraging, simulating model error as Brownian noise is clearly insufficient for establishing validity. To continue this line of inquiry, one would need more theoretically sound way to perturb archetypal waveforms in order to convincingly model the discrepancy between real extracellular spike waveforms and those generated by the simplified model. Unavoidably, the localization framework investigated in the current paper would need to be validated on real (i.e. not simulated) neural recordings with known geometry in order to be of any practical value whatsoever.

An interesting theoretical question (and one towards which no effort at all was directed in this study) is this: for what configurations of waveform models and recording geometries is localization theoretically possible? For instance, localization would clearly not be possible if spatial distribution is uniform, i.e. waveform is independent of the relative position of the neuron and the electrode. On the other hand, for a waveform distribution were the waveform amplitude is scaled down linearly with distance 3 electrodes would typically be sufficient, as simple triangulation could be used.

REFERENCES

- G. Buzsáki, "Large-scale recording of neuronal ensembles.," Nat. Neurosci. 2004, vol. 7, no. 5, pp. 446-51.
- [2] M. S. Lewicki, "A review of methods for spike sorting: the detection and classification of neural action potentials.," *Network* 1998, vol. 9, no. 4, pp. 53-78.
- [3] P. T. Thorbergsson, M. Garwicz, J. Schouenborg, and A. J. Johansson, "Spike-Feature Based Estimation of Electrode Position in Extracellular Neural Recordings," in *Int. Conf. IEEE EMBC* 2012.
- [4] T. Kubo, N. Katayama, A. Karashima, and M. Nakao. (2008). "The 3D position estimation of neurons in the hippocampus based on the multi-site multi-unit recordings with silicon tetrodes," in *Int. Conf.* IEEE EMBC 2008.
- [5] P. T. Thorbergsson, M. Garwicz, J. Schouenborg, and A. J. Johansson, "Computationally efficient simulation of extracellular recordings with multielectrode arrays," *J. Neurosci. Methods*, 2012, vol 211, issue 1, pp. 133-44.
- [6] D. Heeger, "Poisson model for spike generation," 2000, available from cns.nyu.edu/ david/handouts/poisson.pdf
- [7] F. Pedregosa, G. Varoquaux, A. Gramfort, V. Michel, B. Thirion, O. Grisel et al., "Scikit-learn: machine learning in Python," J. Mach. Learn. Res. 2011, vol. 12, pp. 2825–30.
- Learn. Res., 2011, vol. 12, pp. 2825–30.
 [8] J Nocedal and S. Wright, "Numerical Optimization," 1999, pp. 120-2.
- [9] Documentation available at
 - $docs.scipy.org/doc/scipy/reference/generated/scipy.optimize.fmin_cg.html$

V. REFLECTION ON ETHICS

In this project I have attempted, with moderate success, to locate individual neurons in space by processing simulated extracellular neural recordings. All parts of the study were conducted entirely in silico and did not involve neither moral agents nor moral subjects, at least not in a contemporary understanding of these terms. Thus, if one ignores questions of opportunity cost (counterfactually, how I could have spent my time and resources if I had refrained from doing this project?), I find it difficult to see how any of the standard normative theories (consequentialism, deontology, virtue ethics, care ethics, etc.) could ascribe any moral significance to my current project in and of itself. To find anything of interest for a discussion of ethics related to the project, I will move to consider ethical concerns related to continued work on neuron localization, as well as to neural interfacing considered more broadly.

To validate the algorithmic framework presented here *in vivo*, live subjects (animals or people) would doubtlessly have to be involved. As with all experiments involving autonomous agents capable of suffering, issues related to the 4 principles of biomedical ethics—autonomy, justice, beneficence, and non-maleficence—would arise. As such experiments would concern the central nervous system—the proverbial seat of the soul—these issues would arguably become significantly more poignant. All risks, such as those of violating autonomy or causing bodily or psychological harm, would have to be weighted against any and all potential short- and long-term benefits, both medical and scientific, of the technology.

More generally, this work can be considered a contribution (admittedly negligible) towards the pursuit of methods that allow for influencing the central nervous system exogenously. Here, I will very briefly consider some ethical implications of highly functional neural engineering of this kind. Given that our current understanding of neuroscience is at least approximately correct, it seems plausible to assume that psychological qualities could be modified at will with the appropriate technology. In a world where any and all forms of vice are reduced to illnesses, curable at the press of a button, can virtue really be said to have any more moral significance than bodily health? After all, few are willing to give moral praise to those not currently afflicted by a cold. Interestingly, this implication does not seem to logically require that highprecision neural engineering becomes practically feasible soon or even ever—we would probably not feel tempted to blame patients suffering from a bacterial infection even in a world were antibiotics did not exist. Out of the standard moral theories, only utilitarianism seems to survive in a world where moral desert is an incoherent concept. With this in mind, I believe those of us that put normative value on phenomena beyond hedonic tone (art, courageous action, virtuous societies, etc.) should probably feel compelled to provide definitions of such goods that do not require an agentic conception of ethics.