

Time series machine learning with shapelets

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A Hands-on Introduction to Time Series Classification and Regression

26/08/2024

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Notation one-stop shop

Before diving in, let us define some notations :

- a **time series** of length m and of dimension d as a vector $X = [\mathbf{x}_1, \dots, \mathbf{x}_m]$ with $\mathbf{x}_j \in \mathbb{R}^d$.
- a **time series dataset** $\mathcal{X} = [X_1, \dots, X_n]$, this is equivalent to an array 3D X of shape : (n_samples, n_channels, n_timepoints)
- an **annotation vector** $Y = [y_1, \dots, y_n]$. For example, in a regression context, $y_i \in \mathbb{R}$ would represent the label of X_i .

For simplicity, we'll consider time series with a fixed frequency.

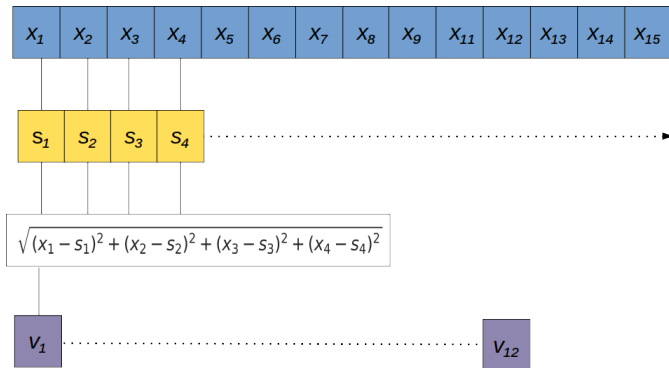
Additionally, we use:

- a blue color when talking about time series
- a yellow color when talking about shapelets
- a pink color when talking about annotation vectors
- a purple color when talking about distance vectors

What are shapelets ?

A shapelet [7] is a subsequence $S = \{s_1, \dots, s_l\} \in \mathbb{R}^{l,d}$ representing a pattern of interest. The similarity between S and X is quantified using a distance vector V . Example with $d = 1$ (univariate):

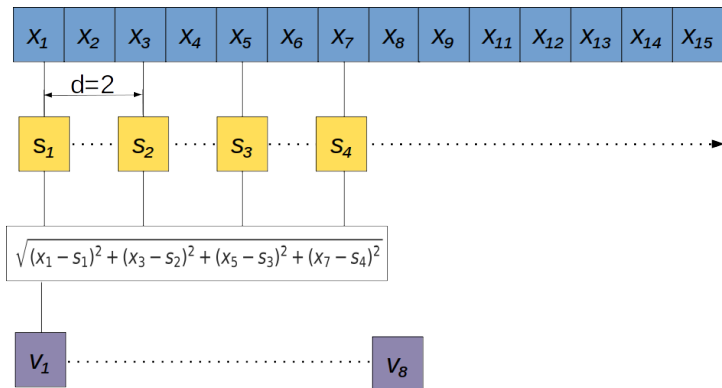
- $\text{dist}(X, S) = [v_1, \dots, v_{m-l+1}]$
- with $v_i = \sqrt{\sum_{j=1}^l (s_j - x_{i+j-1})^2}$. (or any distance function)



What are (dilated) shapelets ?

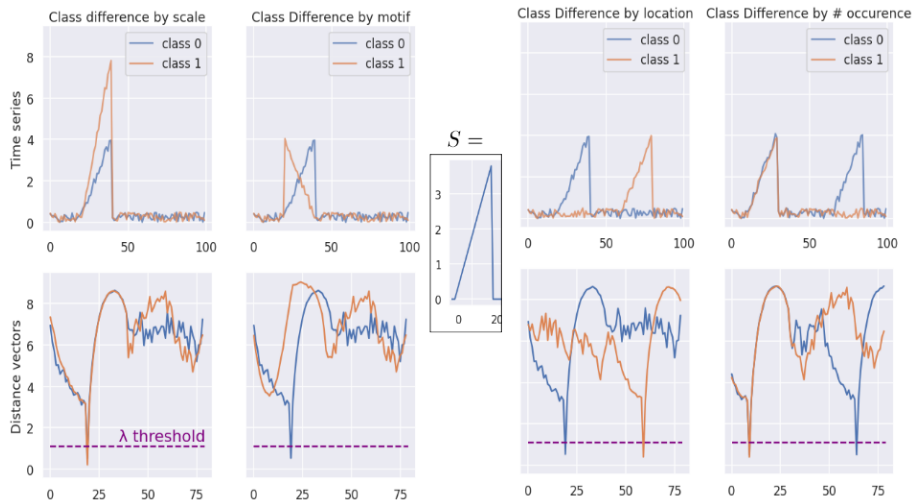
In [3], a parameter d is added to S . The intention is to :

- Allow matching non-contiguous, cyclic patterns (e.g. heartbeats)
- Increase receptive field.



What do we do with the distance vector ?

We want to identify discriminative characteristics between S and X:



What do we do with the distance vector ?

The following features are extracted to target these discriminative characteristics :

- **min** $d(X, S)$: the feature most shapelet-based methods use. It allows discriminating by **presence or absence of a pattern**.
- **argmin** $d(X, S)$: first used in [4] for shapelets, this allows to discriminate by **pattern location**.
- **Shapelet occurrence** [3]: $\sum_i I(v_i < \lambda)$, with I the identity function and a threshold λ , which is a shapelet parameter. It allows discriminating by **number of λ -close occurrence of the pattern**.

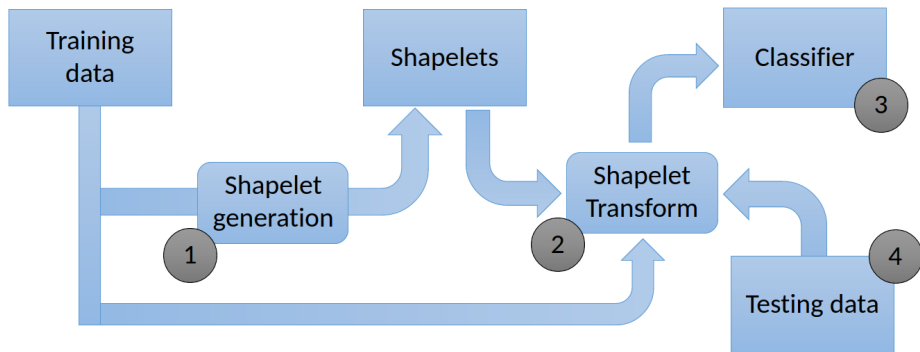
Standardizing S and every subsequence $[x_i, \dots, x_{i+(l-1)}]$ independently makes v_i , and thus $d(X, S)$ (and the extracted features), **scale invariant**.
Not standardizing makes them **scale sensitive**.

Shapelet-based classification and regression

All Shapelet classifiers or regressors use the same methodology, given

$\mathcal{X} = \{X_1, \dots, X_n\}$ and $Y = \{y_1, \dots, y_n\}$:

- 1 Generate $\mathcal{S} = \{S_1, \dots, S_k\}$ the set of Shapelets
- 2 Extract a matrix of features M , from \mathcal{X} using \mathcal{S}
- 3 Learn a classifier based on M and Y



How do we generate Shapelets ?

We can distinguish three approaches :

- **Exhaustive search** : extract all possible shapelet candidates and evaluate their quality to extract the best ones (information gain, F-statistic, ...)
- **Heuristic-based search**: random or semi-random extraction from the training data, statistical or rule-based methods for reducing the number of shapelet candidates.
- **Shapelet generation**: Use of optimization methods (gradient descent [2], evolutionary algorithm) to generate shapelet values instead of extracting them from the input.

What is the Shapelet Transform ?

Consider $\mathcal{X} = \{X_1, \dots, X_n\}$ and $\mathcal{S} = \{S_1, \dots, S_k\}$. The Shapelet Transform [6] algorithm is the same for all shapelet methods:

- 1 Create a matrix M of size (n, k) (or $(n, 3K)$ for RDST)
- 2 $\forall i \in [1, n]$, $\forall j \in [1, k]$, and extract features from $d(X_i, S_j)$

For example, if extracting the minimum value :

$$M = \begin{bmatrix} \min d(X_1, S_1) & \dots & \min d(X_n, S_1) \\ \vdots & \ddots & \vdots \\ \min d(X_1, S_k) & \dots & \min d(X_n, S_k) \end{bmatrix}$$

A column M_i of M describes X_i by the features extracted using \mathcal{S} . The argmin can also be extracted, giving a matrix M of size $(n, 2k)$.

Using the output of the transform

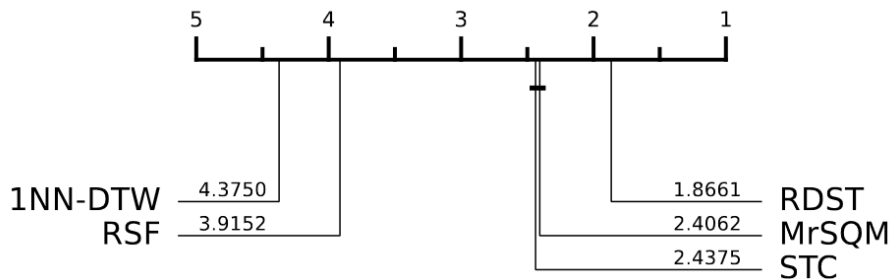
Given this matrix M of size (n, k) , we can use any tabular classification or regression model :

- Shapelet Transform Classifier [1] uses a Rotation Forest,
- Random Dilated Shapelet Transform [3] uses a linear model (Ridge),
- Learning Time Series Shapelets [2] uses a logistic regression layer as output of the network,
- Other models use shapelets as components of a model. For example, Random Shapelet Forest (RSF) [5] propose a random forest where tree nodes are producing splits based on the distance (min) to a specific shapelet.

The model using the output of the transform can often be switched with any other model, allowing to tune it for a specific task.

Current results for shapelet methods

The figure below gives the results of shapelet methods for the 112 dataset version of the classification archive :



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