

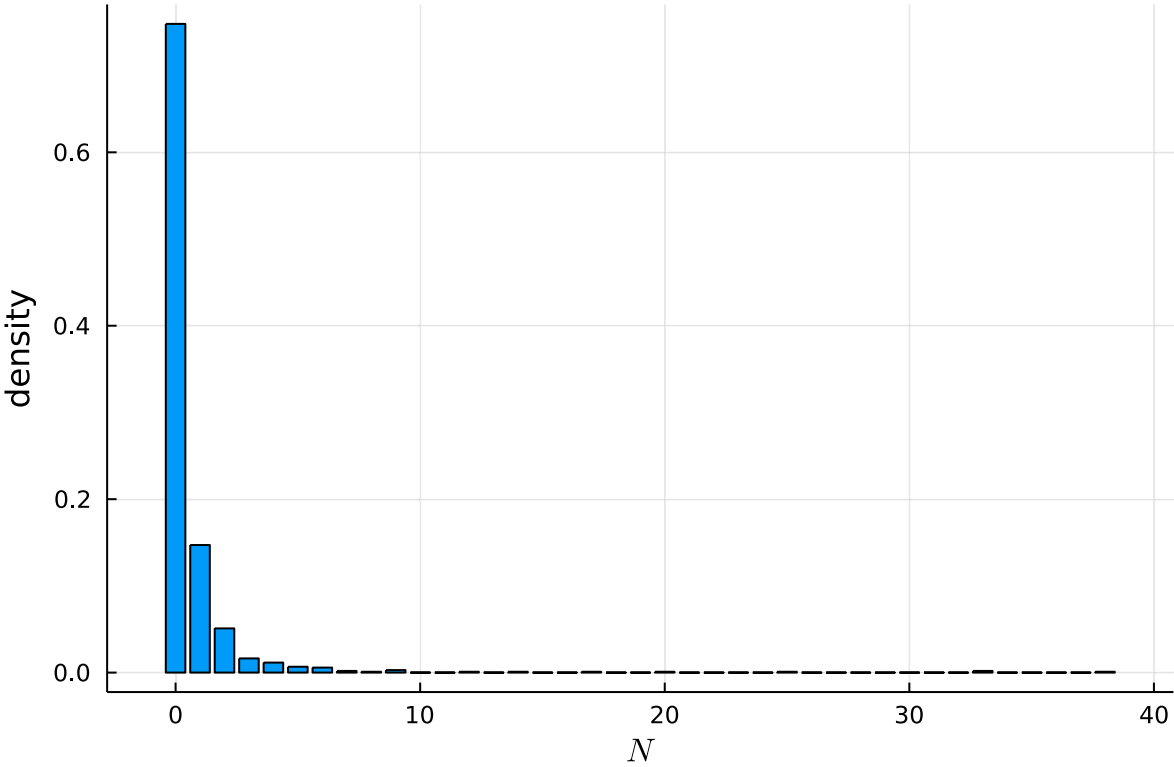


	value	counts	proportion
1	0	778	0.748077
2	1	153	0.147115
3	2	53	0.0509615
4	3	17	0.0163462
5	4	12	0.0115385
6	5	7	0.00673077
7	6	6	0.00576923
8	7	2	0.00192308
9	8	1	0.000961538
10	9	3	0.00288462
	more		
39	38	1	0.000961538

```
• begin # Frequency table
•   Nvalues = collect(0:maximum(Nobs))
•   Ncounts = zeros{Int, length(Nvalues)}
•   Ncounts[1] = 52*20 - nrows # number of cases when N = 0 (no claims)
•   for n ∈ Nobs
•     Ncounts[n+1] += 1
•   end
•   Nprop = Ncounts ./ sum(Ncounts)
•   NfreqTable = DataFrame{value = Nvalues, counts = Ncounts, proportion = Nprop}
• end
```

(1040, 1040, 1.0)

```
• sum(Ncounts), 52*20, sum(NfreqTable.proportion) # just checking
```



```
• bar(Nvalues, Nprop, xlabel = L"N", ylabel = "density", legend = false)
```

When the estimated probability  $\mathbb{P}(N = 0)$  is significantly higher than for  $N > 0$  sometimes it is better to try fitting a model for  $N|N > 0$ . *To be continued...*

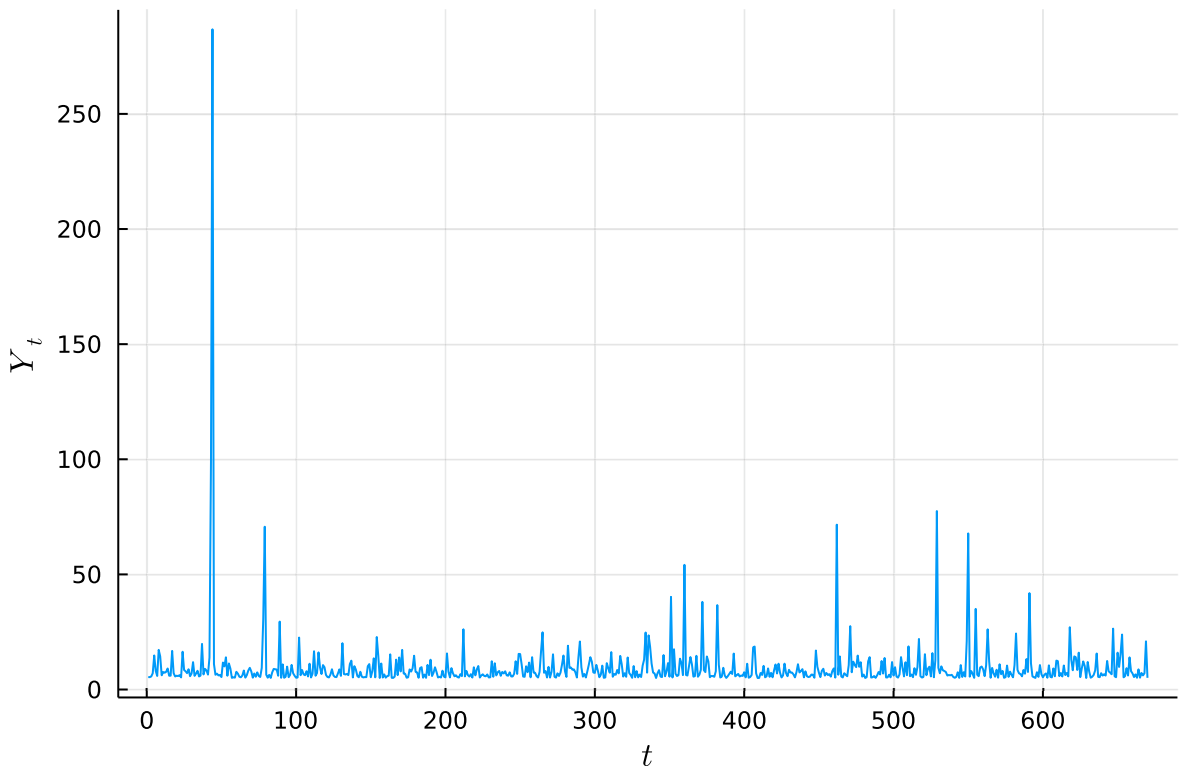
## Severity modeling

[5.411, 5.364, 5.664, 7.04, 14.799, 8.106, 5.883, 17.226, 14.412, 6.183, 7.598, 7.29, 7.693

```
begin
  Yobs = zeros(0)
  for i ∈ 1:nrows
    append!(Yobs, data[i])
  end
  println("Σ N_i = ", sum(Nobs))
  Yobs # vector of claims in chronological order
end
```

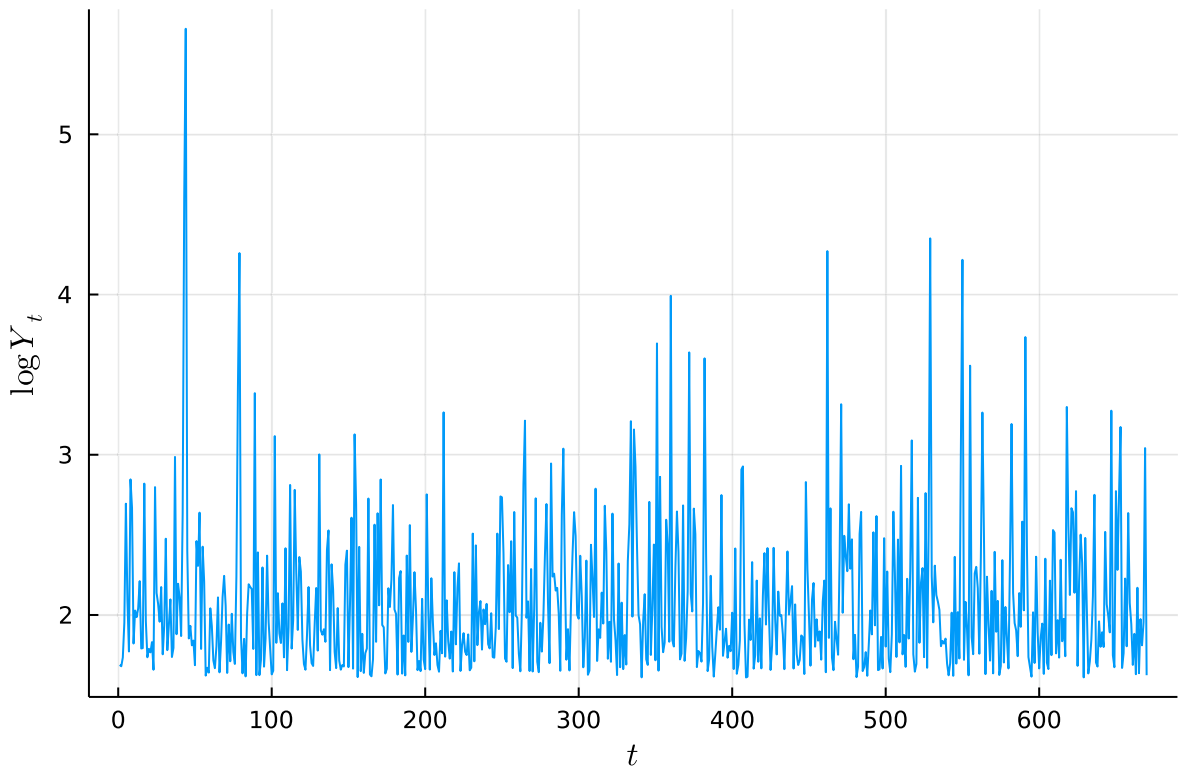
Σ N\_i = 670

Check for serial independence of  $Y_1, Y_2, \dots$

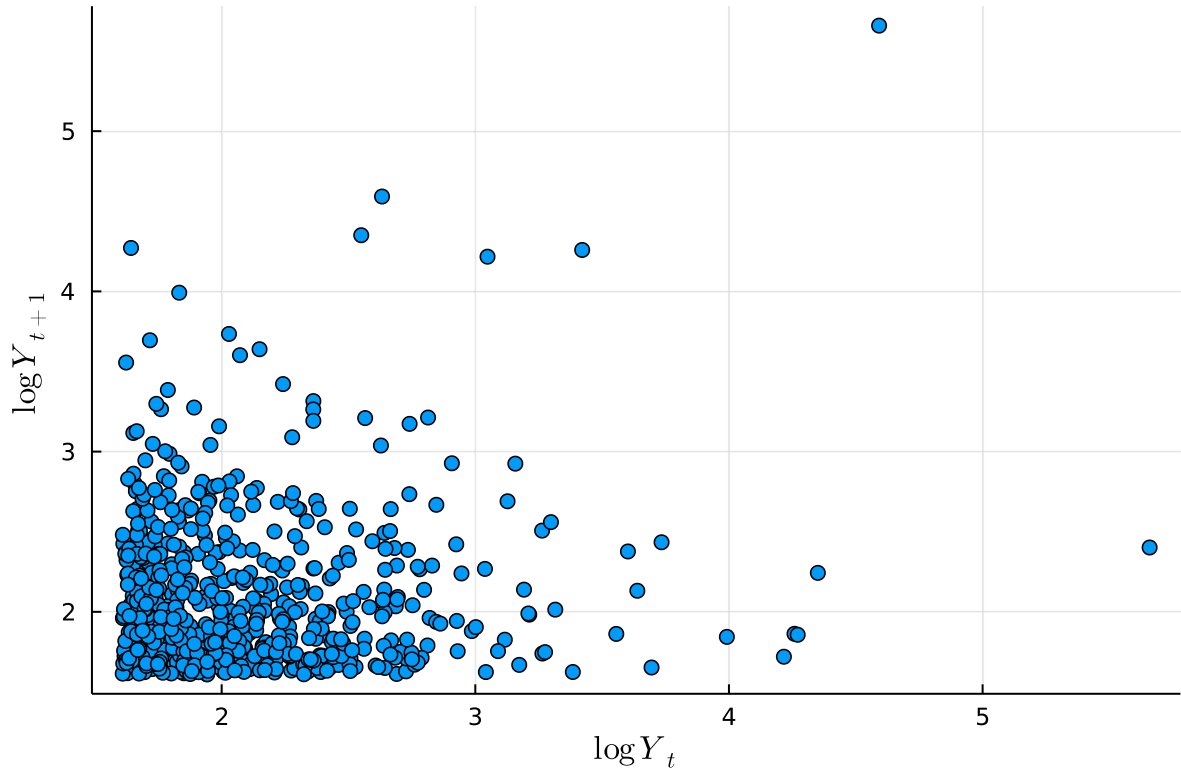


```
plot(Yobs, xlabel = L"t", ylabel = L"Y_t", legend = false)
```

For amounts of money a log-scale is preferred since vertical distances are proportional to % variations instead of absolute variations:



```
begin
  logYobs = log.(Yobs)
  plot(logYobs, xlabel = L"t", ylabel = L"\log\,Y_t", legend = false)
end
```



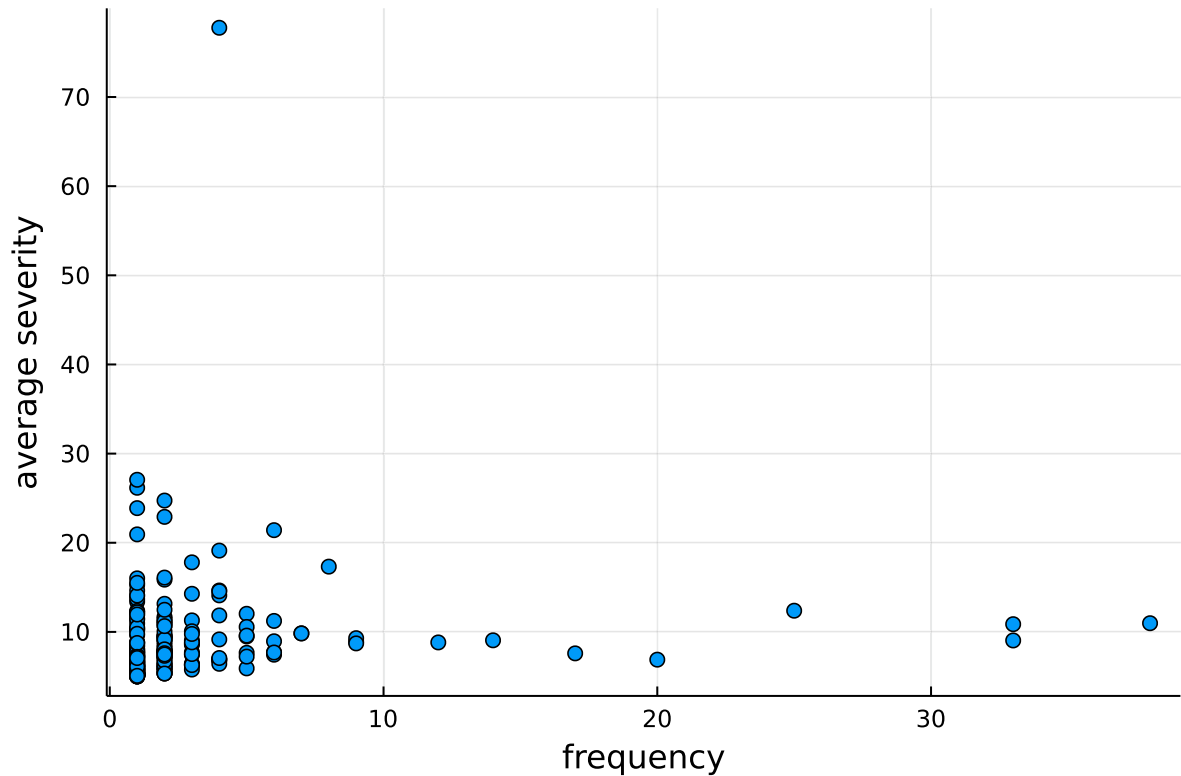
```
begin
  println("Spearman = ", corspearman(logYobs[1:(end-1)], logYobs[2:end])) #
  #Spearman's correlation
  scatter(logYobs[1:(end-1)], logYobs[2:end], xlabel = L"\log\,Y_t", ylabel =
    L"\log\,Y_{t+1}", legend = false)
end
```

Spearman = -0.00027283981672650856 ⓘ

A Spearman correlation close to zero does not necessarily imply independence between claims  $Y_1, Y_2, \dots$  so statistical procedures must be applied to verify. *To be continued...*

Check for possible dependence between claim severity and frequency:

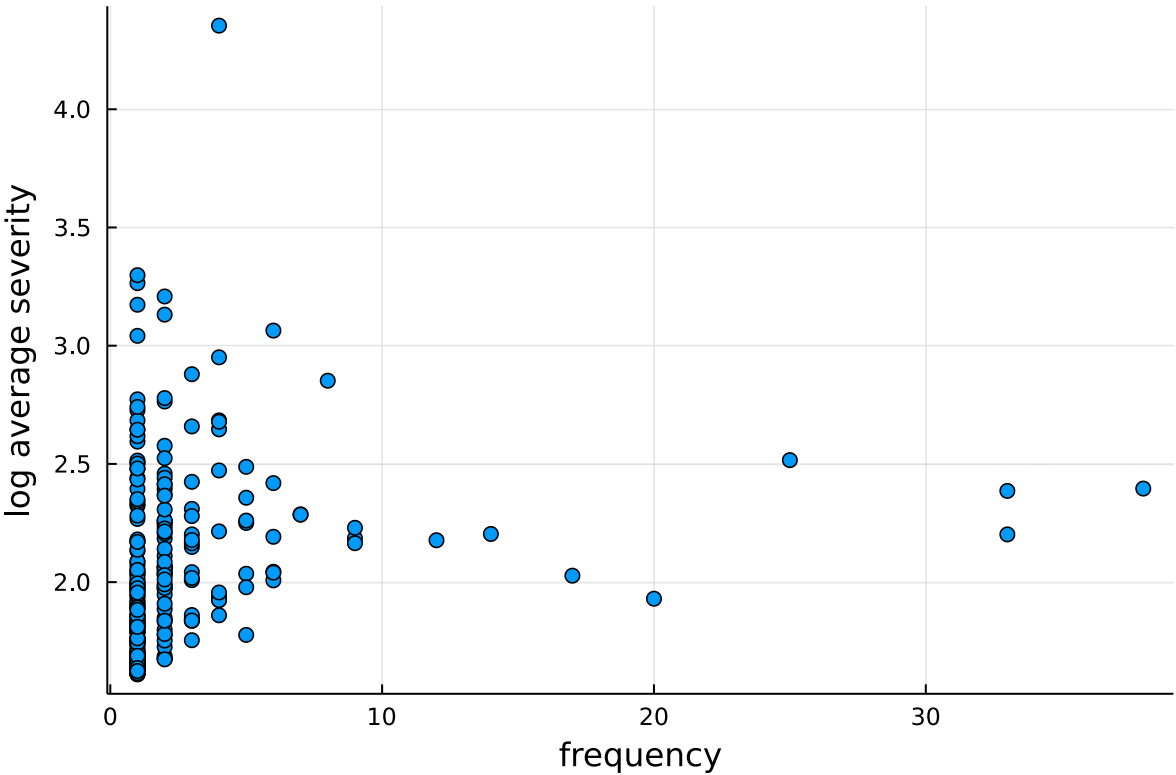
```
begin
  avgYobs = zeros(nrows)
  for i ∈ 1:nrows
    avgYobs[i] = mean(data[i])
  end
end
```



```
begin
  println("Spearman = ", corspearman(Nobs, avgYobs))
  scatter(Nobs, avgYobs, legend = false, xlabel = "frequency", ylabel = "average
    severity")
end
```

Spearman = 0.44433139528796955 ⓘ

The same as before but in log-scale:



```
• begin
•   println("Spearman = ", corspearman(Nobs, log.(avgYobs)))
•   scatter(Nobs, log.(avgYobs), legend = false, xlabel = "frequency", ylabel = "log
    average severity")
• end
```

Spearman = 0.44433139528796955 ?

Spearman's correlation clearly different from zero implies there is NO independence between frequency and severity, so in this case it is necessary to find a model for the severity conditional on the frequency. *To be continued...*