

SMEFT (at NLO) : EW, Higgs, and Top

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Plan for today's lecture

- SMEFT essentials
- The SMEFT precision frontier
- Example: Fitting in the Top (with Higgs/EW) sector
- Bringing lessons home

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SMEFT Lagrangian: Dim=6

[Buchmuller and Wyler, 86] [Grzadkowski et al, 10]

| X^3 | | φ^6 and $\varphi^4 D^2$ | | $\psi^2 \varphi^3$ | |
|--------------------------|--|---------------------------------|---|-----------------------|---|
| Q_G | $f^{ABC} G_\mu^{A\nu} G_\nu^{B\rho} G_\rho^{C\mu}$ | Q_φ | $(\varphi^\dagger \varphi)^3$ | $Q_{e\varphi}$ | $(\varphi^\dagger \varphi)(\bar{l}_p e_r \varphi)$ |
| $Q_{\tilde{G}}$ | $f^{ABC} \tilde{G}_\mu^{A\nu} G_\nu^{B\rho} G_\rho^{C\mu}$ | $Q_{\varphi \square}$ | $(\varphi^\dagger \varphi) \square (\varphi^\dagger \varphi)$ | $Q_{u\varphi}$ | $(\varphi^\dagger \varphi)(\bar{q}_p u_r \tilde{\varphi})$ |
| Q_W | $\varepsilon^{IJK} W_\mu^{I\nu} W_\nu^{J\rho} W_\rho^{K\mu}$ | $Q_{\varphi D}$ | $(\varphi^\dagger D^\mu \varphi)^* (\varphi^\dagger D_\mu \varphi)$ | $Q_{d\varphi}$ | $(\varphi^\dagger \varphi)(\bar{q}_p d_r \varphi)$ |
| $Q_{\tilde{W}}$ | $\varepsilon^{IJK} \tilde{W}_\mu^{I\nu} W_\nu^{J\rho} W_\rho^{K\mu}$ | | | | |
| $X^2 \varphi^2$ | | $\psi^2 X \varphi$ | | $\psi^2 \varphi^2 D$ | |
| $Q_{\varphi G}$ | $\varphi^\dagger \varphi G_{\mu\nu}^A G^{A\mu\nu}$ | Q_{eW} | $(\bar{l}_p \sigma^{\mu\nu} e_r) \tau^I \varphi W_{\mu\nu}^I$ | $Q_{\varphi l}^{(1)}$ | $(\varphi^\dagger i \overleftrightarrow{D}_\mu \varphi)(\bar{l}_p \gamma^\mu l_r)$ |
| $Q_{\varphi \tilde{G}}$ | $\varphi^\dagger \varphi \tilde{G}_{\mu\nu}^A G^{A\mu\nu}$ | Q_{eB} | $(\bar{l}_p \sigma^{\mu\nu} e_r) \varphi B_{\mu\nu}$ | $Q_{\varphi l}^{(3)}$ | $(\varphi^\dagger i \overleftrightarrow{D}_\mu^I \varphi)(\bar{l}_p \tau^I \gamma^\mu l_r)$ |
| $Q_{\varphi W}$ | $\varphi^\dagger \varphi W_{\mu\nu}^I W^{I\mu\nu}$ | Q_{uG} | $(\bar{q}_p \sigma^{\mu\nu} T^A u_r) \tilde{\varphi} G_{\mu\nu}^A$ | $Q_{\varphi e}$ | $(\varphi^\dagger i \overleftrightarrow{D}_\mu \varphi)(\bar{e}_p \gamma^\mu e_r)$ |
| $Q_{\varphi \tilde{W}}$ | $\varphi^\dagger \varphi \tilde{W}_{\mu\nu}^I W^{I\mu\nu}$ | Q_{uW} | $(\bar{q}_p \sigma^{\mu\nu} u_r) \tau^I \tilde{\varphi} W_{\mu\nu}^I$ | $Q_{\varphi q}^{(1)}$ | $(\varphi^\dagger i \overleftrightarrow{D}_\mu \varphi)(\bar{q}_p \gamma^\mu q_r)$ |
| $Q_{\varphi B}$ | $\varphi^\dagger \varphi B_{\mu\nu} B^{\mu\nu}$ | Q_{uB} | $(\bar{q}_p \sigma^{\mu\nu} u_r) \tilde{\varphi} B_{\mu\nu}$ | $Q_{\varphi q}^{(3)}$ | $(\varphi^\dagger i \overleftrightarrow{D}_\mu^I \varphi)(\bar{q}_p \tau^I \gamma^\mu q_r)$ |
| $Q_{\varphi \tilde{B}}$ | $\varphi^\dagger \varphi \tilde{B}_{\mu\nu} B^{\mu\nu}$ | Q_{dG} | $(\bar{q}_p \sigma^{\mu\nu} T^A d_r) \varphi G_{\mu\nu}^A$ | $Q_{\varphi u}$ | $(\varphi^\dagger i \overleftrightarrow{D}_\mu \varphi)(\bar{u}_p \gamma^\mu u_r)$ |
| $Q_{\varphi WB}$ | $\varphi^\dagger \tau^I \varphi W_{\mu\nu}^I B^{\mu\nu}$ | Q_{dW} | $(\bar{q}_p \sigma^{\mu\nu} d_r) \tau^I \varphi W_{\mu\nu}^I$ | $Q_{\varphi d}$ | $(\varphi^\dagger i \overleftrightarrow{D}_\mu \varphi)(\bar{d}_p \gamma^\mu d_r)$ |
| $Q_{\varphi \tilde{W}B}$ | $\varphi^\dagger \tau^I \varphi \tilde{W}_{\mu\nu}^I B^{\mu\nu}$ | Q_{dB} | $(\bar{q}_p \sigma^{\mu\nu} d_r) \varphi B_{\mu\nu}$ | $Q_{\varphi u d}$ | $i(\tilde{\varphi}^\dagger D_\mu \varphi)(\bar{u}_p \gamma^\mu d_r)$ |

SMEFT Lagrangian: Dim=6

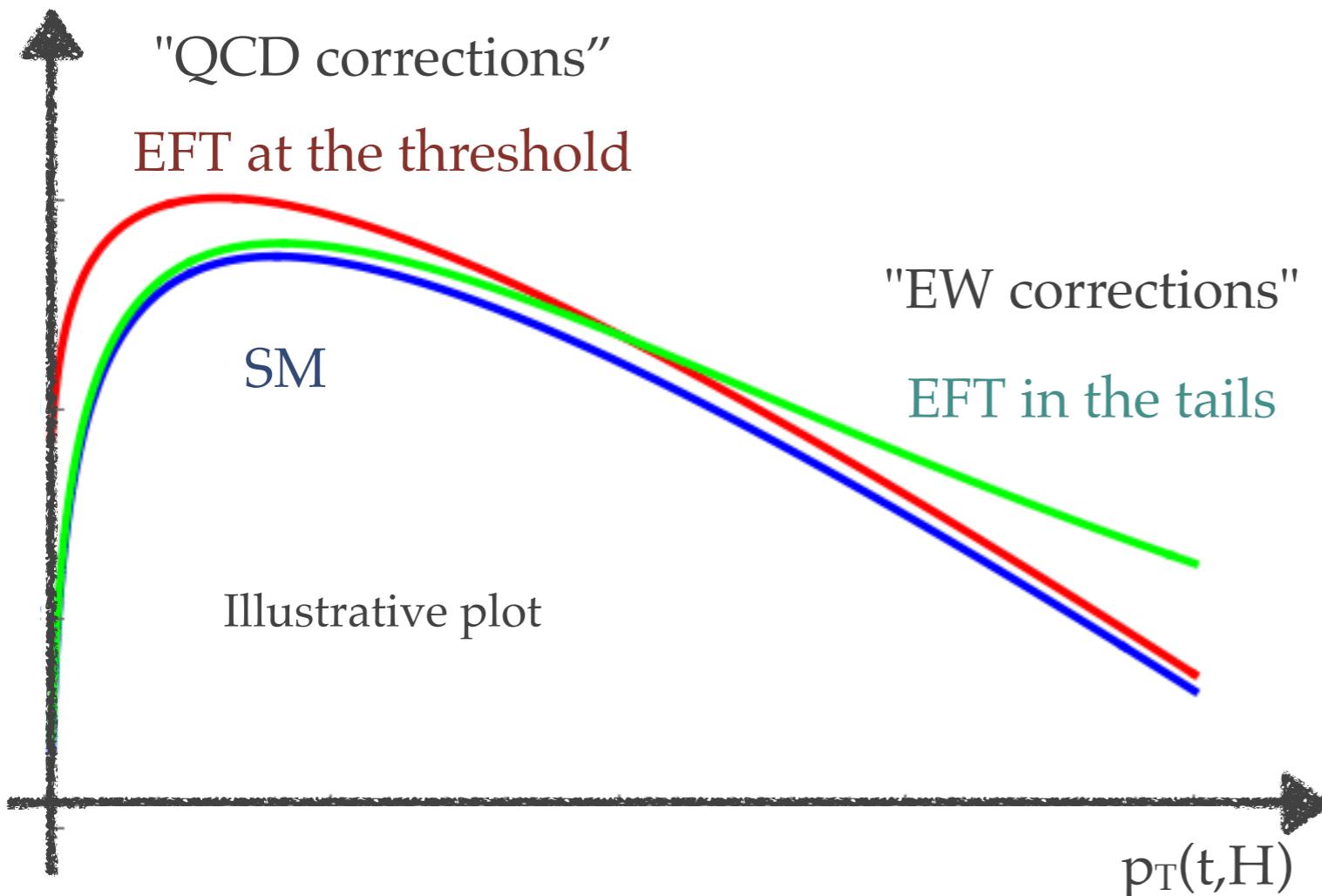
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| $(\bar{L}L)(\bar{L}L)$ | | $(\bar{R}R)(\bar{R}R)$ | | $(\bar{L}L)(\bar{R}R)$ | |
|---|--|------------------------|---|------------------------|--|
| Q_{ll} | $(\bar{l}_p \gamma_\mu l_r)(\bar{l}_s \gamma^\mu l_t)$ | Q_{ee} | $(\bar{e}_p \gamma_\mu e_r)(\bar{e}_s \gamma^\mu e_t)$ | Q_{le} | $(\bar{l}_p \gamma_\mu l_r)(\bar{e}_s \gamma^\mu e_t)$ |
| $Q_{qq}^{(1)}$ | $(\bar{q}_p \gamma_\mu q_r)(\bar{q}_s \gamma^\mu q_t)$ | Q_{uu} | $(\bar{u}_p \gamma_\mu u_r)(\bar{u}_s \gamma^\mu u_t)$ | Q_{lu} | $(\bar{l}_p \gamma_\mu l_r)(\bar{u}_s \gamma^\mu u_t)$ |
| $Q_{qq}^{(3)}$ | $(\bar{q}_p \gamma_\mu \tau^I q_r)(\bar{q}_s \gamma^\mu \tau^I q_t)$ | Q_{dd} | $(\bar{d}_p \gamma_\mu d_r)(\bar{d}_s \gamma^\mu d_t)$ | Q_{ld} | $(\bar{l}_p \gamma_\mu l_r)(\bar{d}_s \gamma^\mu d_t)$ |
| $Q_{lq}^{(1)}$ | $(\bar{l}_p \gamma_\mu l_r)(\bar{q}_s \gamma^\mu q_t)$ | Q_{eu} | $(\bar{e}_p \gamma_\mu e_r)(\bar{u}_s \gamma^\mu u_t)$ | Q_{qe} | $(\bar{q}_p \gamma_\mu q_r)(\bar{e}_s \gamma^\mu e_t)$ |
| $Q_{lq}^{(3)}$ | $(\bar{l}_p \gamma_\mu \tau^I l_r)(\bar{q}_s \gamma^\mu \tau^I q_t)$ | Q_{ed} | $(\bar{e}_p \gamma_\mu e_r)(\bar{d}_s \gamma^\mu d_t)$ | $Q_{qu}^{(1)}$ | $(\bar{q}_p \gamma_\mu q_r)(\bar{u}_s \gamma^\mu u_t)$ |
| | | $Q_{ud}^{(1)}$ | $(\bar{u}_p \gamma_\mu u_r)(\bar{d}_s \gamma^\mu d_t)$ | $Q_{qu}^{(8)}$ | $(\bar{q}_p \gamma_\mu T^A q_r)(\bar{u}_s \gamma^\mu T^A u_t)$ |
| | | $Q_{ud}^{(8)}$ | $(\bar{u}_p \gamma_\mu T^A u_r)(\bar{d}_s \gamma^\mu T^A d_t)$ | $Q_{qd}^{(1)}$ | $(\bar{q}_p \gamma_\mu q_r)(\bar{d}_s \gamma^\mu d_t)$ |
| | | | | $Q_{qd}^{(8)}$ | $(\bar{q}_p \gamma_\mu T^A q_r)(\bar{d}_s \gamma^\mu T^A d_t)$ |
| $(\bar{L}R)(\bar{R}L)$ and $(\bar{L}R)(\bar{L}R)$ | | B -violating | | | |
| Q_{ledq} | $(\bar{l}_p^j e_r)(\bar{d}_s q_t^j)$ | Q_{duq} | $\varepsilon^{\alpha\beta\gamma} \varepsilon_{jk} [(d_p^\alpha)^T C u_r^\beta] [(q_s^\gamma)^T C l_t^k]$ | | |
| $Q_{quqd}^{(1)}$ | $(\bar{q}_p^j u_r) \varepsilon_{jk} (\bar{q}_s^k d_t)$ | Q_{qqu} | $\varepsilon^{\alpha\beta\gamma} \varepsilon_{jk} [(q_p^\alpha)^T C q_r^{\beta k}] [(u_s^\gamma)^T C e_t]$ | | |
| $Q_{quqd}^{(8)}$ | $(\bar{q}_p^j T^A u_r) \varepsilon_{jk} (\bar{q}_s^k T^A d_t)$ | $Q_{qqq}^{(1)}$ | $\varepsilon^{\alpha\beta\gamma} \varepsilon_{jk} \varepsilon_{mn} [(q_p^\alpha)^T C q_r^{\beta k}] [(q_s^\gamma)^T C l_t^n]$ | | |
| $Q_{lequ}^{(1)}$ | $(\bar{l}_p^j e_r) \varepsilon_{jk} (\bar{q}_s^k u_t)$ | $Q_{qqq}^{(3)}$ | $\varepsilon^{\alpha\beta\gamma} (\tau^I \varepsilon)_{jk} (\tau^I \varepsilon)_{mn} [(q_p^\alpha)^T C q_r^{\beta k}] [(q_s^\gamma)^T C l_t^n]$ | | |
| $Q_{lequ}^{(3)}$ | $(\bar{l}_p^j \sigma_{\mu\nu} e_r) \varepsilon_{jk} (\bar{q}_s^k \sigma^{\mu\nu} u_t)$ | Q_{duu} | $\varepsilon^{\alpha\beta\gamma} [(d_p^\alpha)^T C u_r^\beta] [(u_s^\gamma)^T C e_t]$ | | |

The EFT approach: managing unknown unknowns

- Very powerful model-independent approach.
- A **global constraining strategy** needs to be employed:
 - assume all* couplings not be zero at the EW scale.
 - identify the operators entering predictions for each observable (LO, NLO,..)
 - find enough observables (cross sections, BR's, distributions,...) to constrain all operators.
 - solve the linear (+quadratic)* system.
- Use to constrain UV-complete* models.
- The final reach on the scale of New Physics crucially depends on the THU.

SMEFT at the LHC



The expected effects can be both at threshold as well as in the tails. Some operators can affect distributions at the threshold. Some operators just lead to global rescaling of the distributions. Other induce an energy growth in the tails. The latter are the most characteristic EFT effects that are looked for.

The sensitivity to new interactions depends on a crucial way to our ability to make accurate/precise predictions for the SM observables. The reach of our interpretations will also depend on the accuracy/precision on the SMEFT predictions.

SMEFT at the LHC

S is a generic scale, which is process and operator dependent

- Large number of operators, yet a plethora of observables and final states to measure.
- Precision observables in the bulk of the distributions while tails provide sensitivity through the energy growth.
- Validity issues arise, as well as for the interpretation in terms of models.

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$$\text{Obs}_i = \text{Obs}_i^{\text{SM}} + M_{ij} \cdot \frac{S}{\Lambda^2} c_j$$

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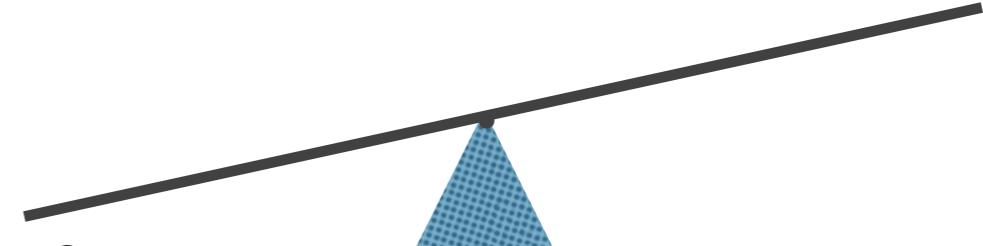
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$$\Lambda > \sqrt{s} \sqrt{|c_i|} / \delta$$

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$$|c_i|s/\Lambda^2 < \delta$$



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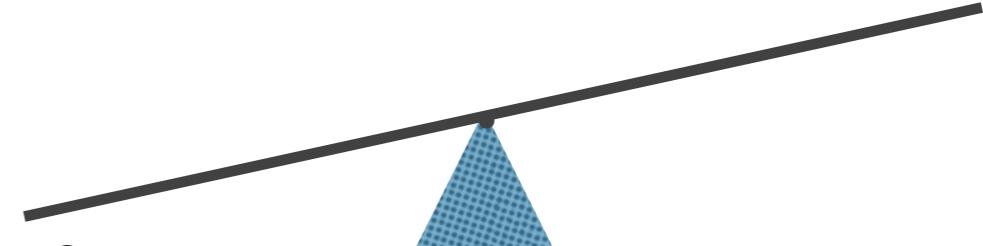
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- Validity issues arise, as well as for the interpretation in terms of models.

$$\sqrt{s} < \Lambda$$

Top-quark operators and processes

[Willenbrock and Zhang 2011, Aguilar-Saavedra 2011, Degrade et al. 2011]

$$O_{\varphi Q}^{(3)} = i \frac{1}{2} y_t^2 \left(\varphi^\dagger \overleftrightarrow{D}_\mu^I \varphi \right) (\bar{Q} \gamma^\mu \tau^I Q)$$

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$$O_{\varphi t} = i \frac{1}{2} y_t^2 \left(\varphi^\dagger \overleftrightarrow{D}_\mu \varphi \right) (\bar{t} \gamma^\mu t)$$

$$O_{tW} = y_t g_w (\bar{Q} \sigma^{\mu\nu} \tau^I t) \tilde{\varphi} W_{\mu\nu}^I$$

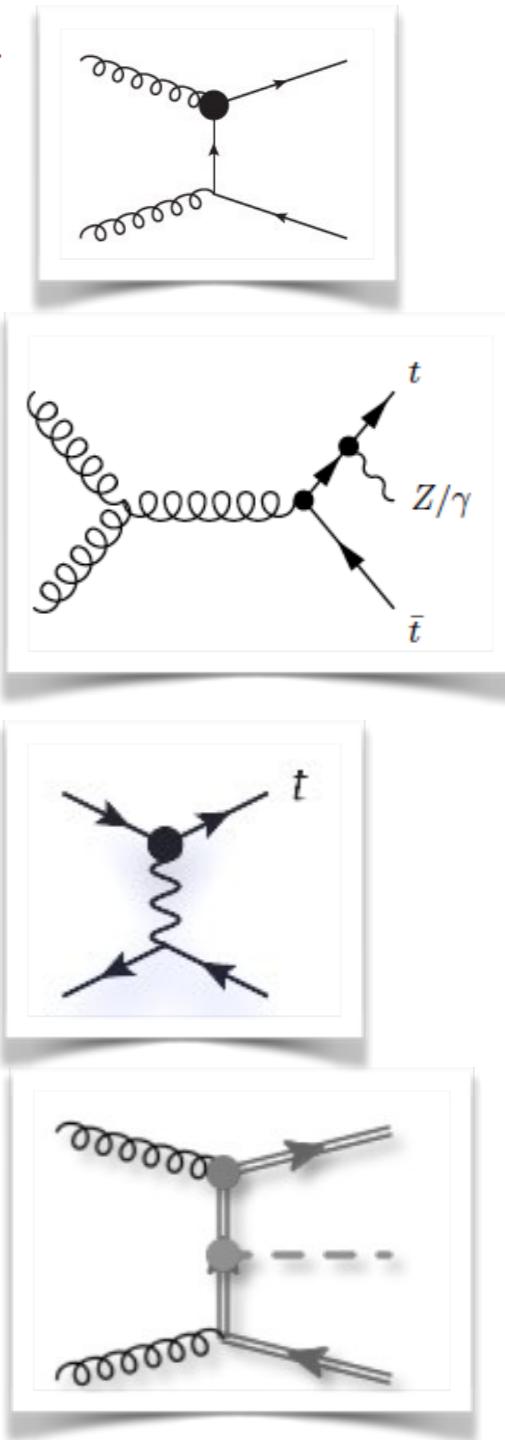
$$O_{tB} = y_t g_Y (\bar{Q} \sigma^{\mu\nu} t) \tilde{\varphi} B_{\mu\nu}$$

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+ four-fermion operators

+ operators that do not feature a top,
but contribute to the procs...



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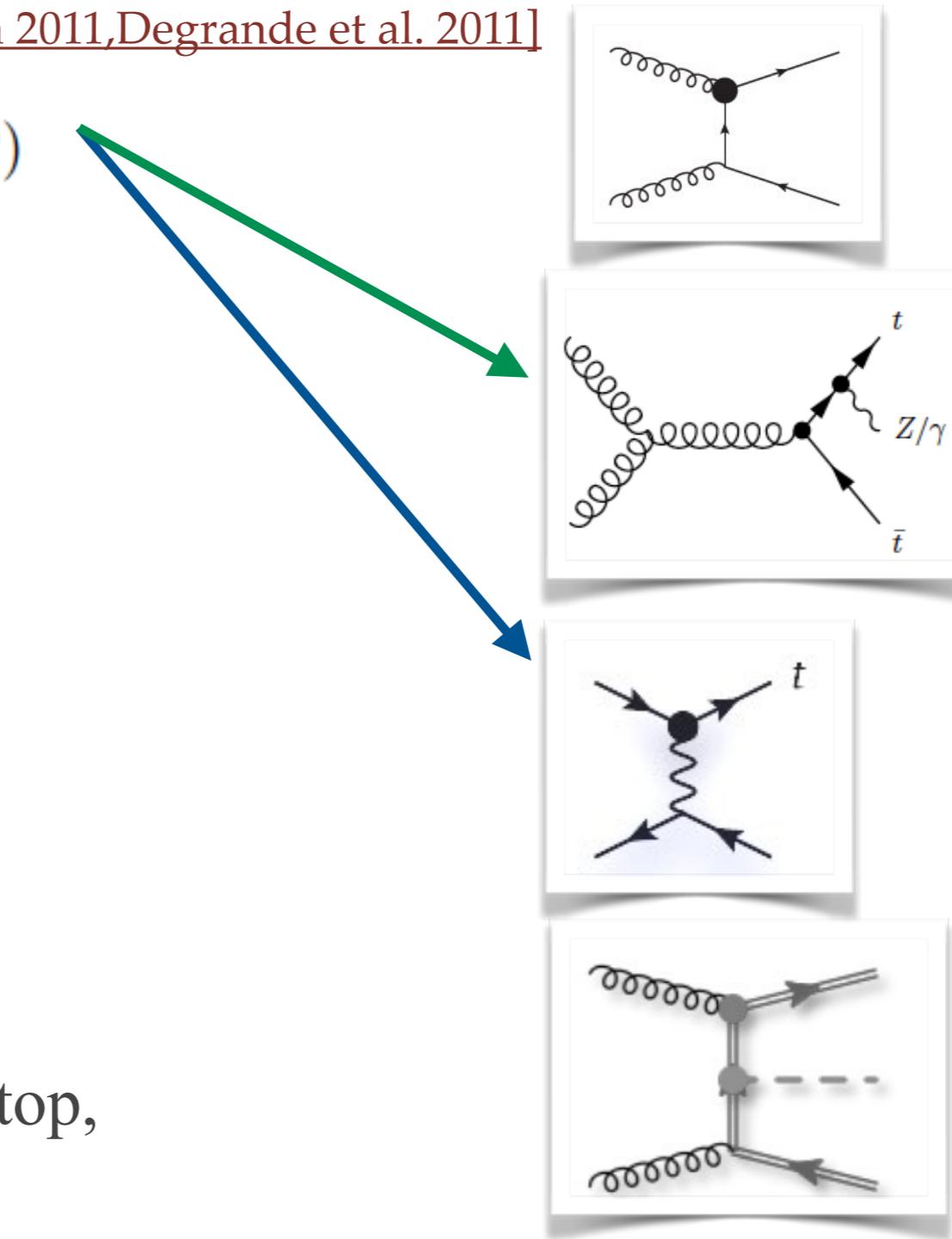
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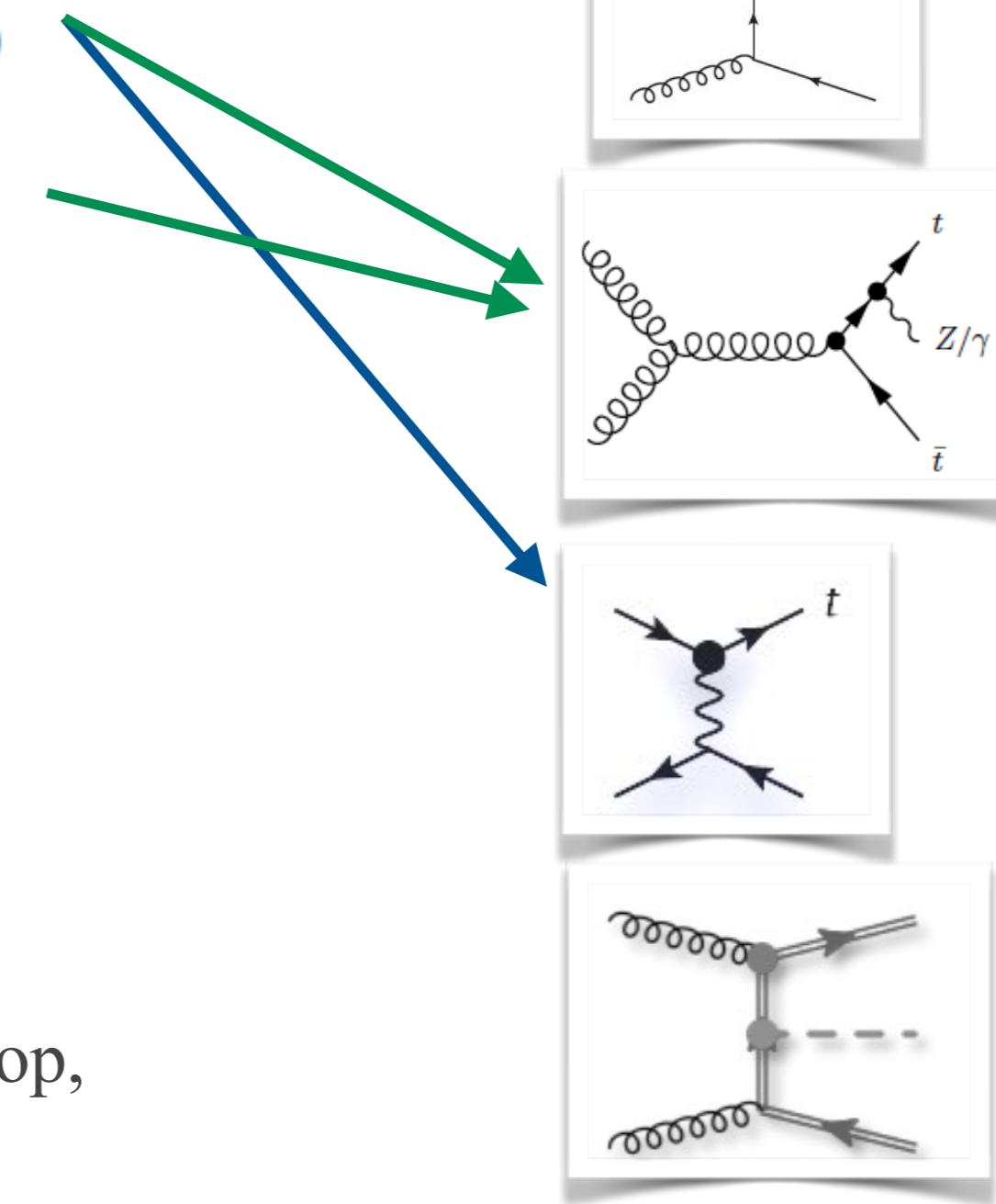
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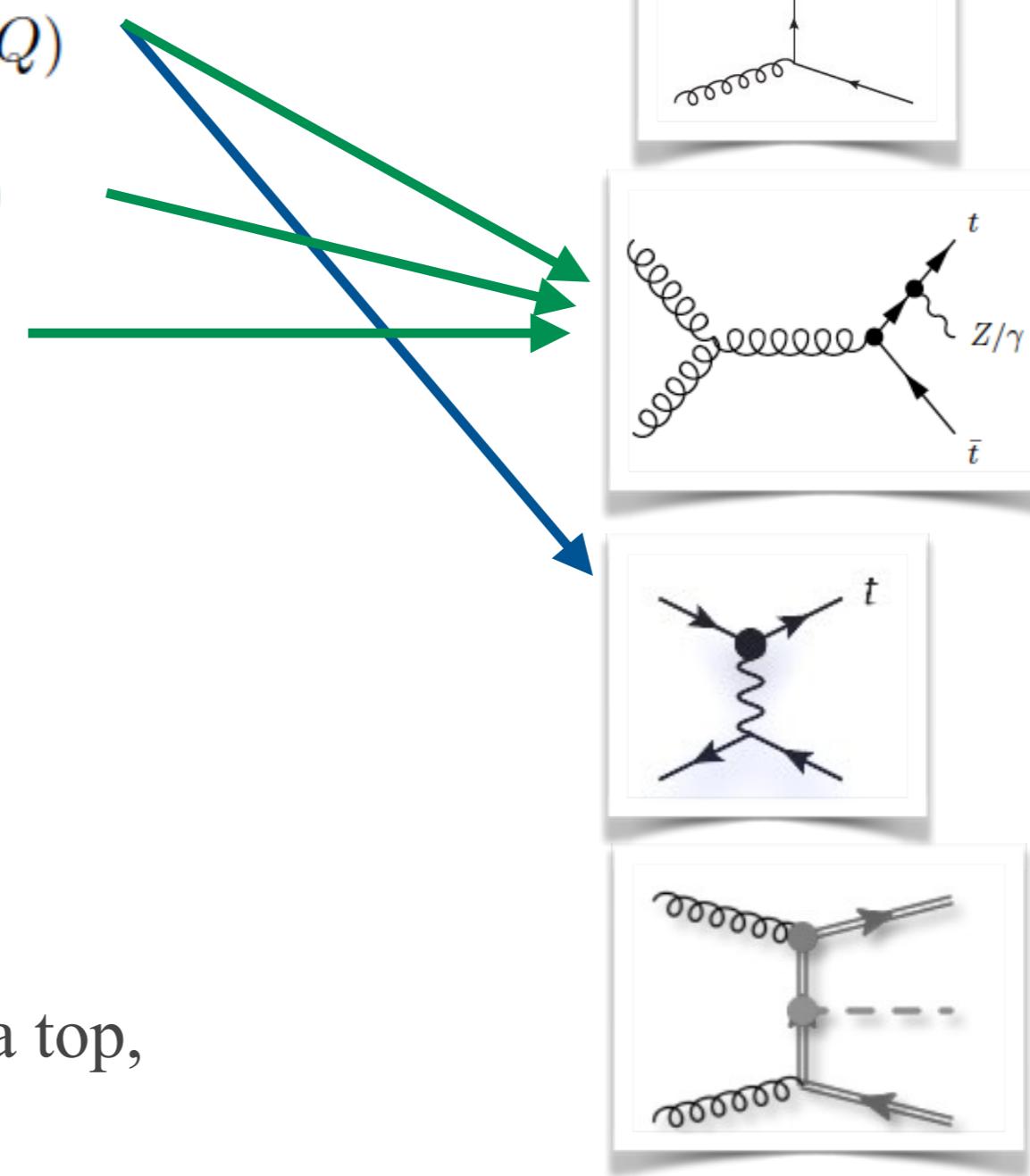
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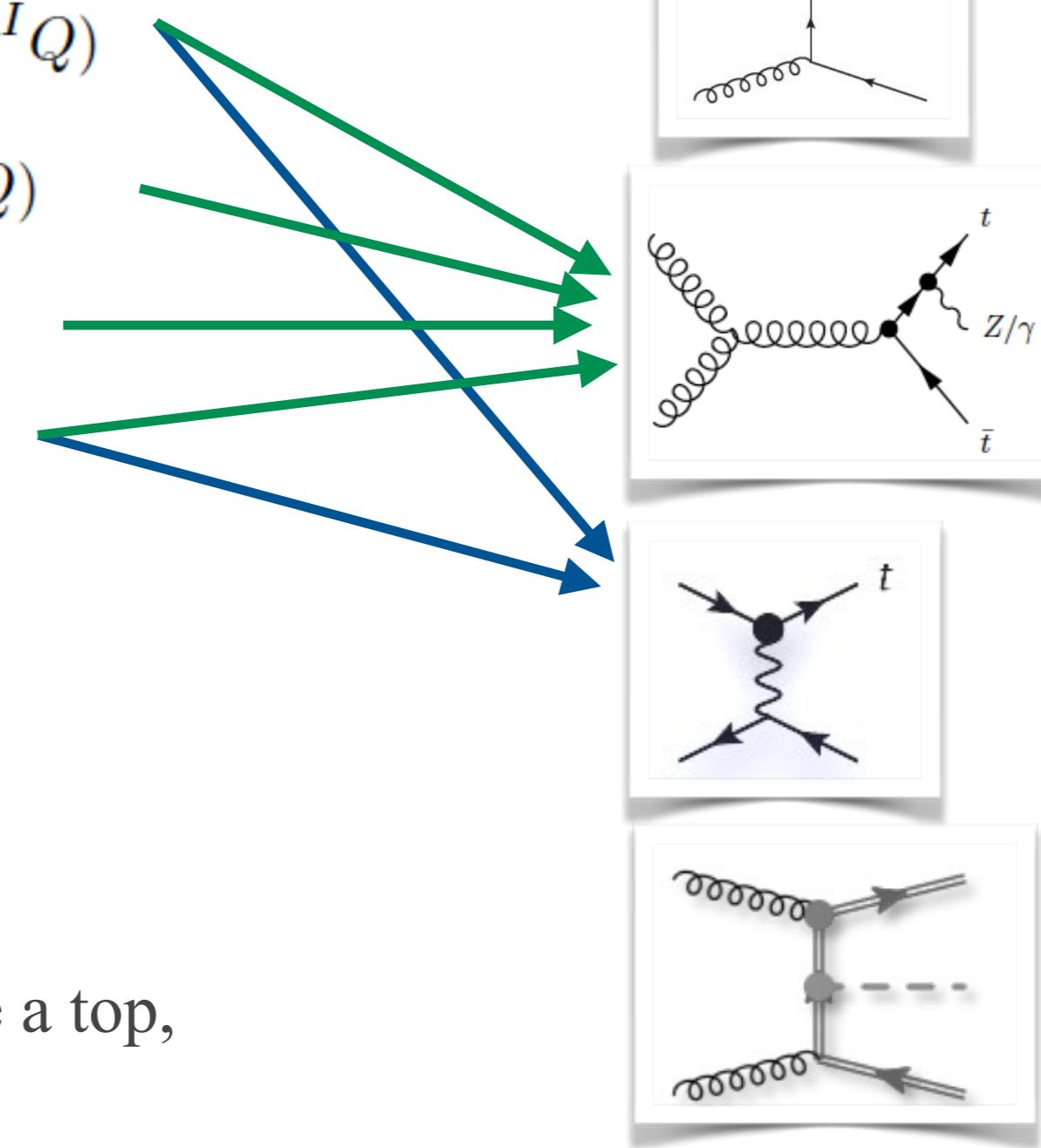
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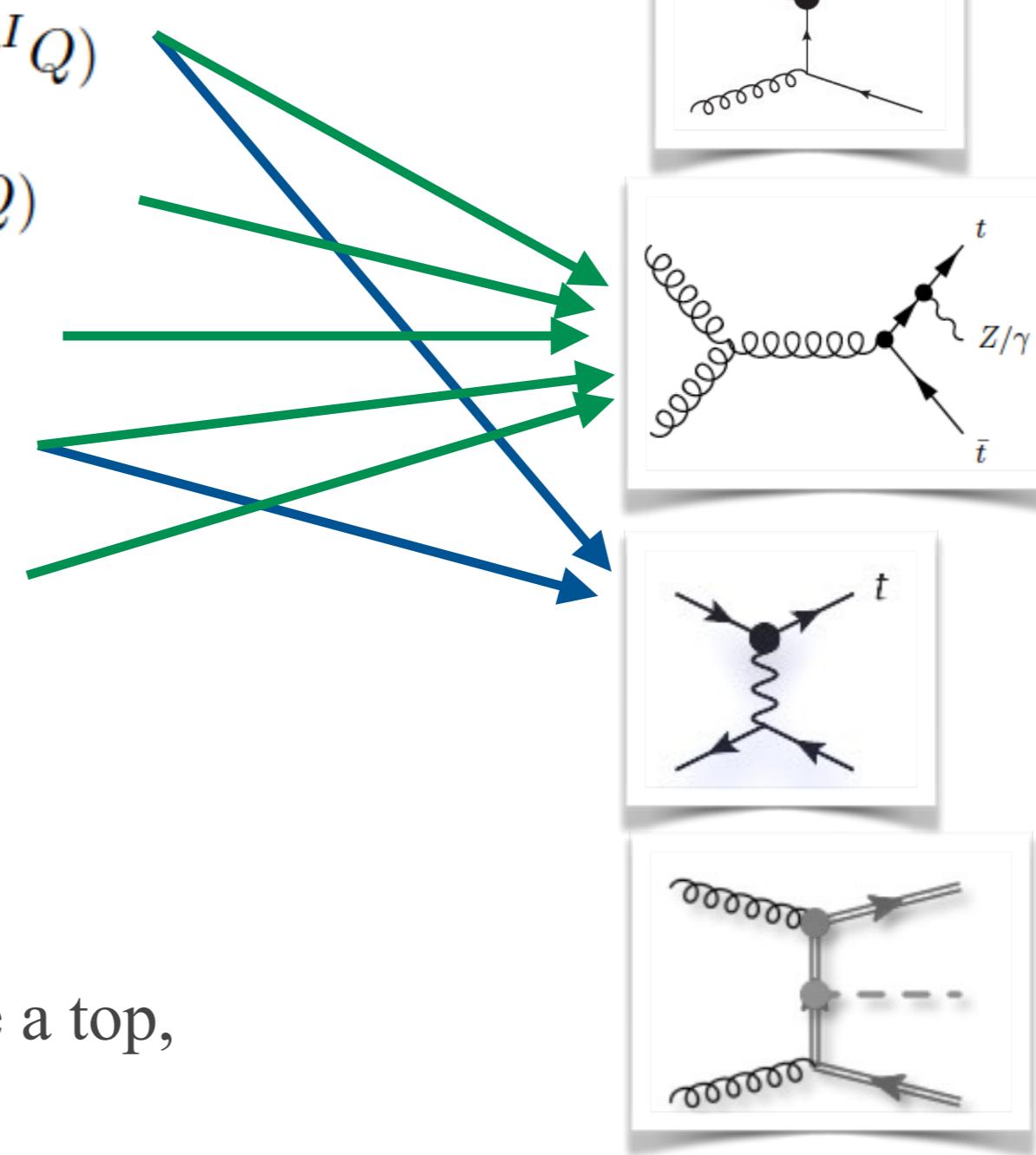
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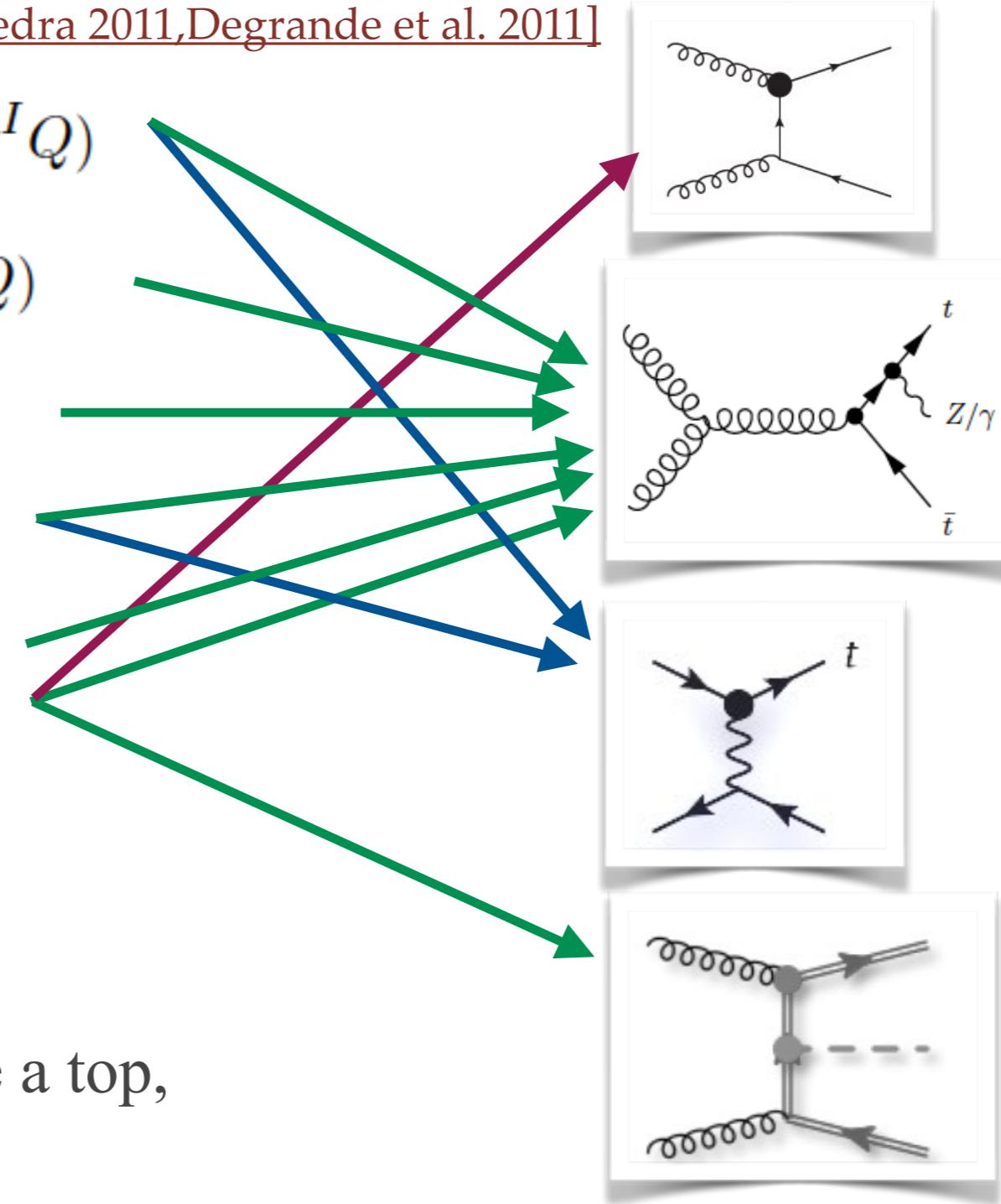
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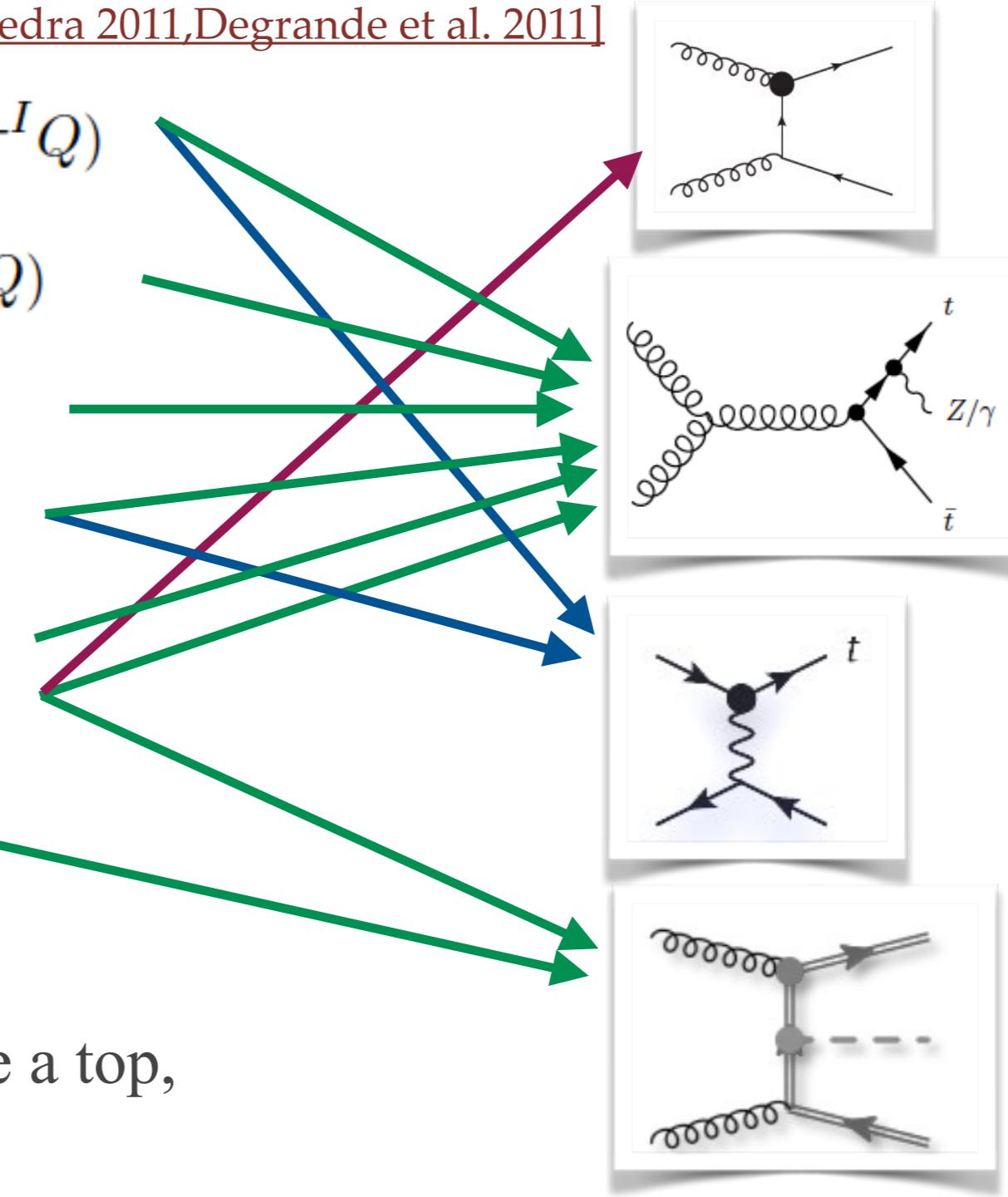
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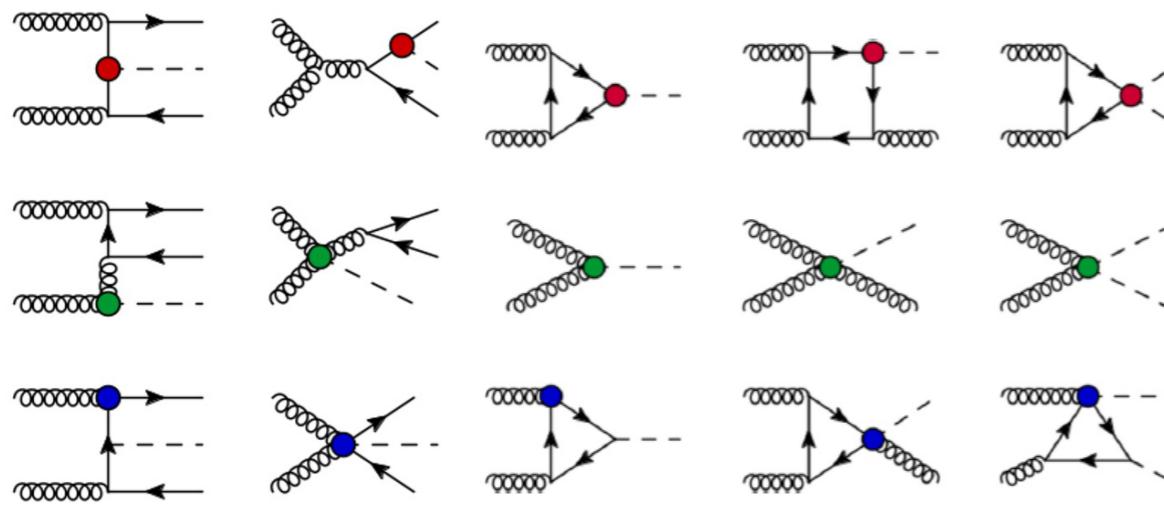


Top/Higgs operators and processes

Several operators typically enter each process at LO (or at LO²) and

| NLO (no) | Process | O_{tG} | O_{tB} | O_{tW} | $O_{\varphi Q}^{(3)}$ | $O_{\varphi Q}^{(1)}$ | $O_{\varphi t}$ | $O_{t\varphi}$ | O_{bW} | $O_{\varphi tb}$ | O_{4f} | O_G | $O_{\varphi G}$ |
|-------------|--|----------|----------|----------|-----------------------|-----------------------|-----------------|----------------|----------|------------------|----------|-------|-----------------|
| ✓ | $t \rightarrow bW \rightarrow bl^+\nu$ | N | | L | L | | | | L^2 | L^2 | $1L^2$ | | |
| ✓ | $pp \rightarrow tj$ | N | | L | L | | | | L^2 | L^2 | $1L$ | | |
| ✓ | $pp \rightarrow tW$ | L | | L | L | | | | L^2 | L^2 | $1N$ | N | |
| ✓ | $pp \rightarrow t\bar{t}$ | L | | | | | | | | | $2L-4N$ | L | |
| ✓ | $pp \rightarrow t\bar{t}j$ | L | | | | | | | | | $2L-4N$ | L | |
| ✓ | $pp \rightarrow t\bar{t}\gamma$ | L | L | L | | | | | | | $2L-4N$ | L | |
| ✓ | $pp \rightarrow t\bar{t}Z$ | L | L | L | L | L | L | | | | $2L-4N$ | L | |
| ✓ | $pp \rightarrow t\bar{t}W$ | L | | | | | | | L | | $1L-2L$ | | |
| ✓ | $pp \rightarrow t\gamma j$ | N | L | L | L | | | | L^2 | L^2 | $1L$ | | |
| ✓ | $pp \rightarrow tZj$ | N | L | L | L | L | L | | L^2 | L^2 | $1L$ | | |
| ✓ | $pp \rightarrow t\bar{t}t\bar{t}$ | L | | | | | | | | | $2L-4L$ | L | |
| ✓ | $pp \rightarrow t\bar{t}H$ | L | | | | | | L | | | $2L-4L$ | L | L |
| ✓ | $pp \rightarrow tHj$ | N | | L | L | | | L | L^2 | L^2 | $1L$ | | N |
| ○✓ | $gg \rightarrow H$ | L | | | | | | L | | | | N | L |
| ○✗ | $gg \rightarrow Hj$ | L | | | | | | L | | | | L | L |
| ○✗ | $gg \rightarrow HH$ | L | | | | | | L | | | | N | L |
| ○✗ | $gg \rightarrow HZ$ | L | | | L | L | L | L | | | | N | L |

Top/Higgs operators and processes



ttH

H

H+j

HH

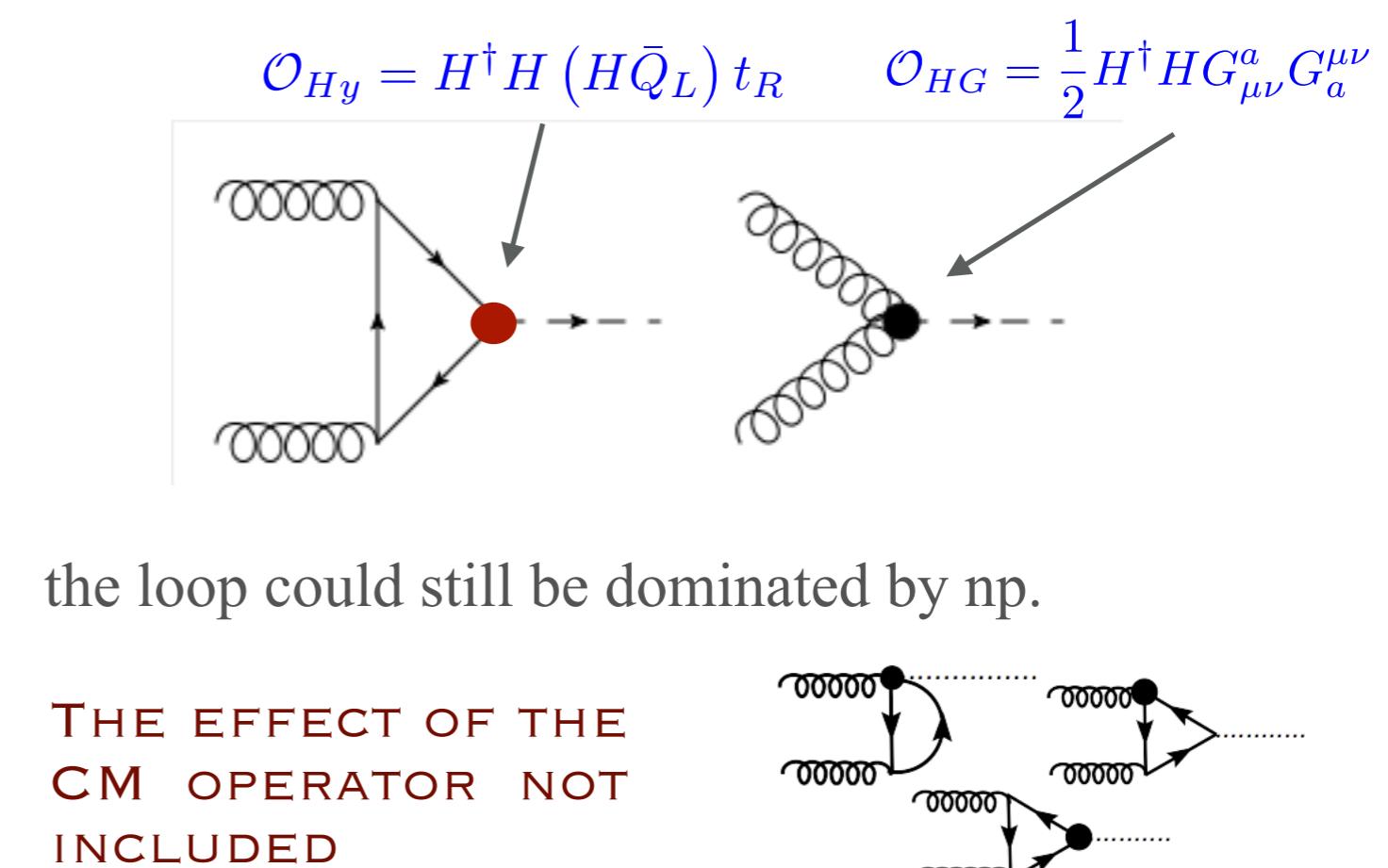
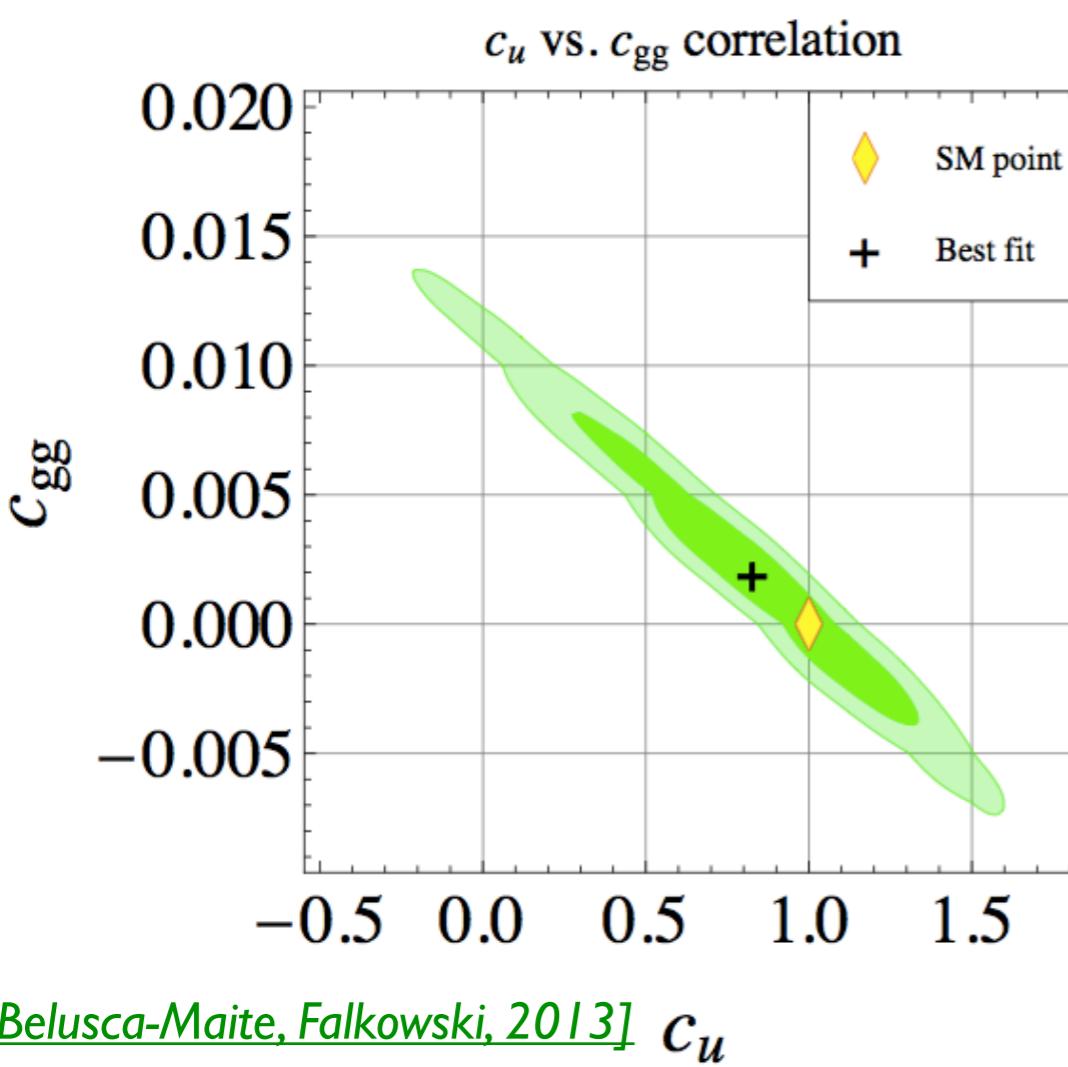
$$\begin{aligned}
 O_{t\phi} &= y_t^3 (\phi^\dagger \phi) (\bar{Q} t) \tilde{\phi} \\
 O_{\phi G} &= y_t^2 (\phi^\dagger \phi) G_{\mu\nu}^A G^{A\mu\nu} \\
 O_{tG} &= y_t g_s (\bar{Q} \sigma^{\mu\nu} T^A t) \tilde{\phi} G_{\mu\nu}^A
 \end{aligned}$$

Top-Higgs interactions: constraints

From a global fit the coupling of the higgs to the top is poorly determined.

$$\frac{\sigma_{ggh}}{\sigma_{ggh}^{\text{SM}}} \simeq \left| 1 + \frac{\hat{c}_{gg}}{c_{gg}^{\text{SM}}} \right|^2$$

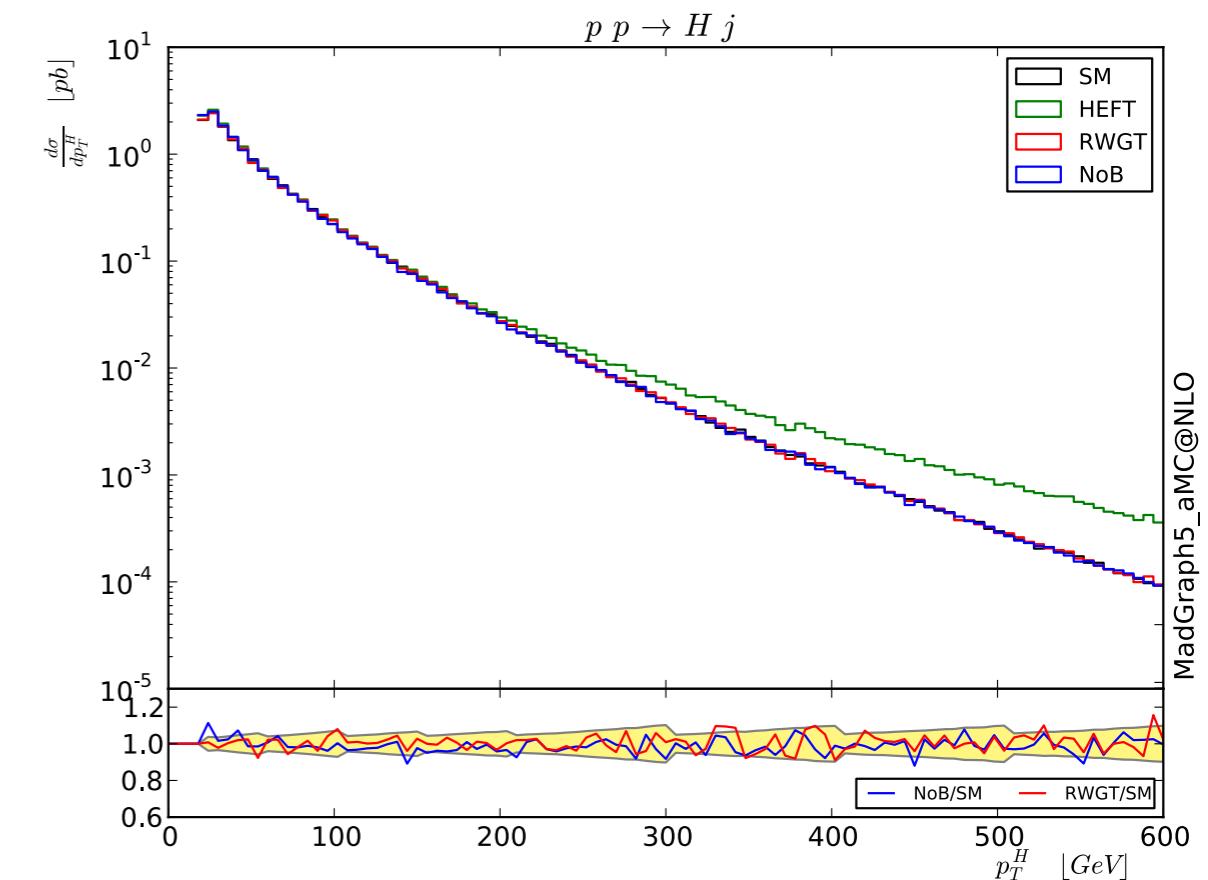
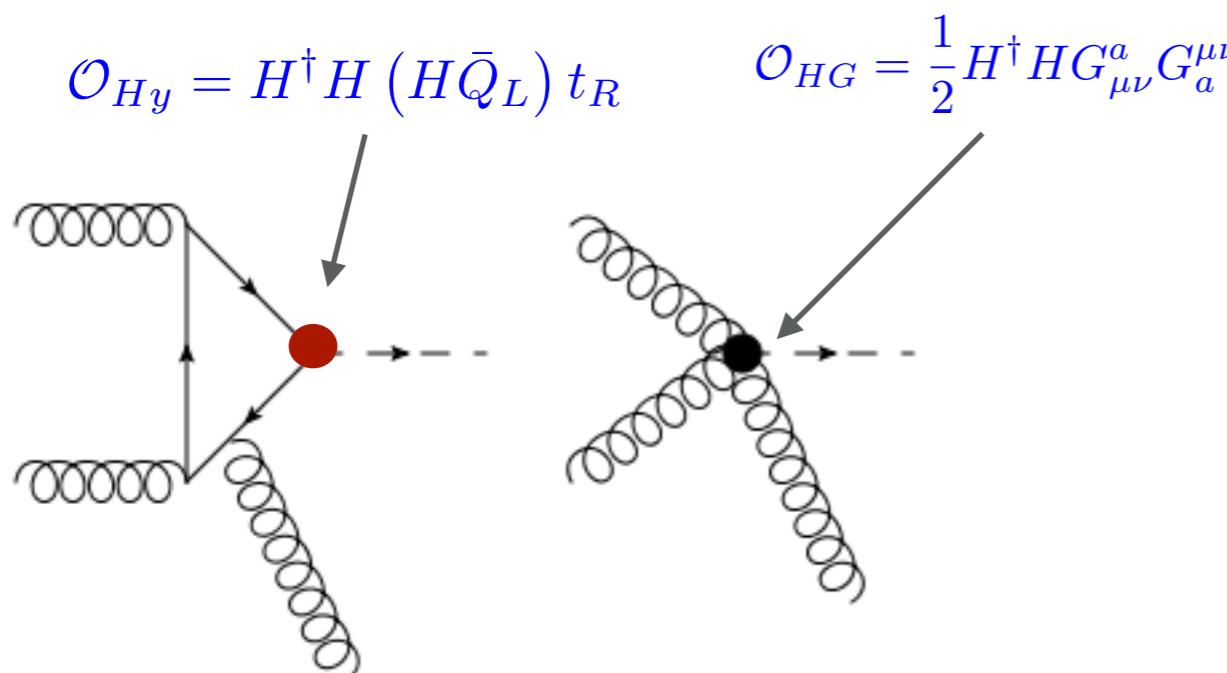
$$\frac{\sigma_{ggh}}{\sigma_{ggh}^{\text{SM}}} \simeq 1 + 237c_{gg} + 2.06\delta y_u - 0.06\delta y_d.$$



Top-Higgs interactions: high-pt

From a global fit the coupling of the higgs to the top is poorly determined: the loop could still be dominated by np.

[\[Grojean et al., 2013\]](#) [\[Banfi et al. 2014\]](#) [\[Buschmann, et al. 2014\]](#)

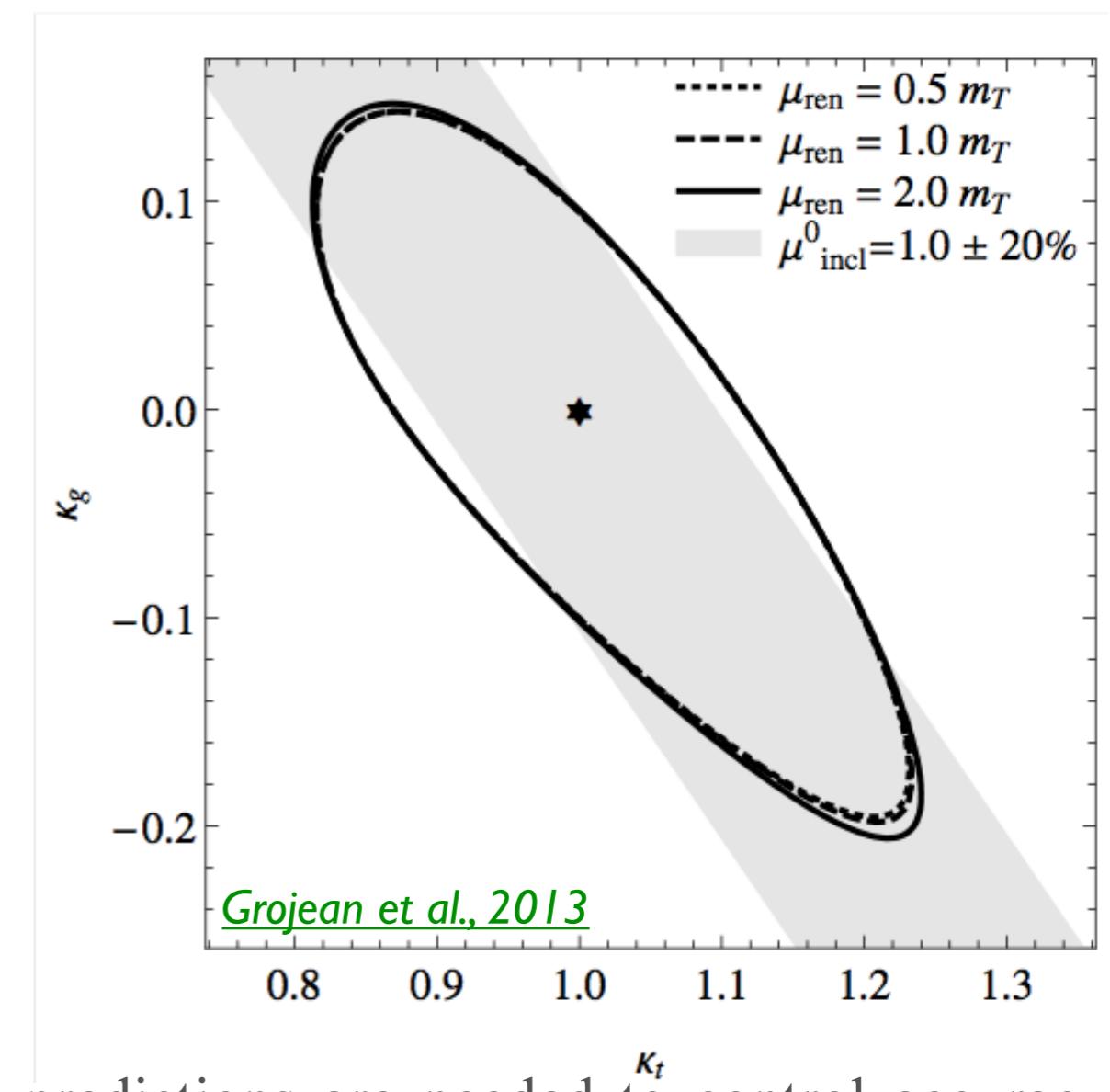
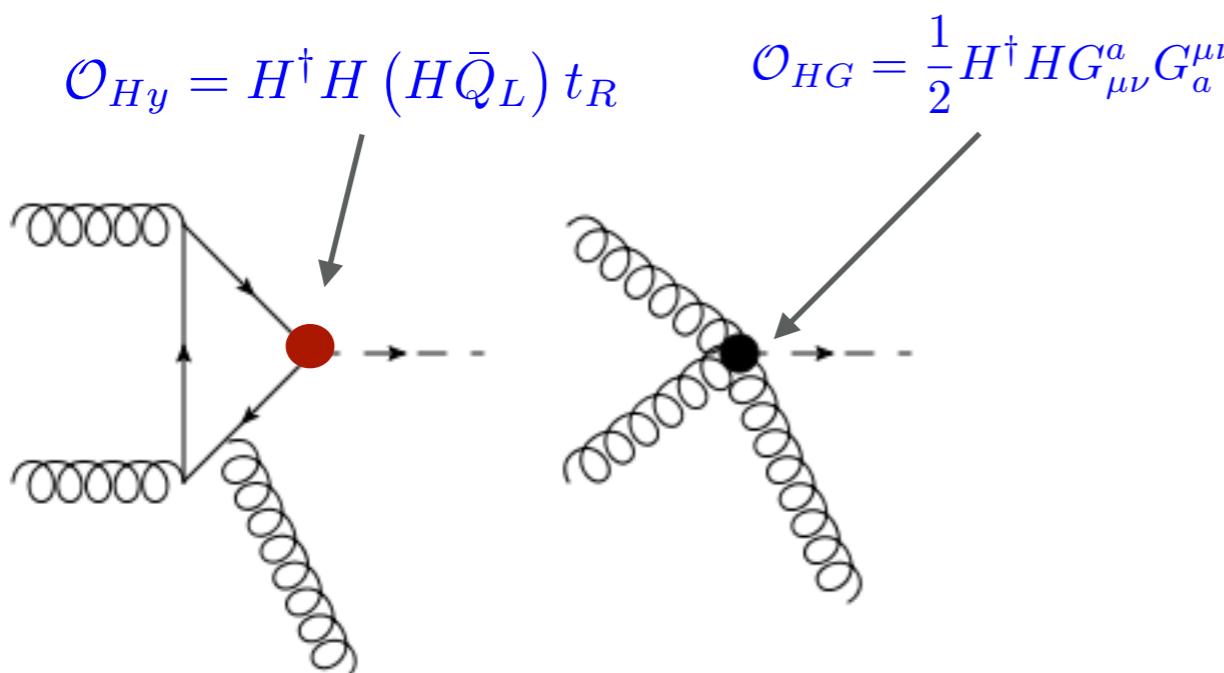


EFT at NLO predictions available, yet SM NLO predictions are needed to control accuracy and precision.

Top-Higgs interactions: high-pt

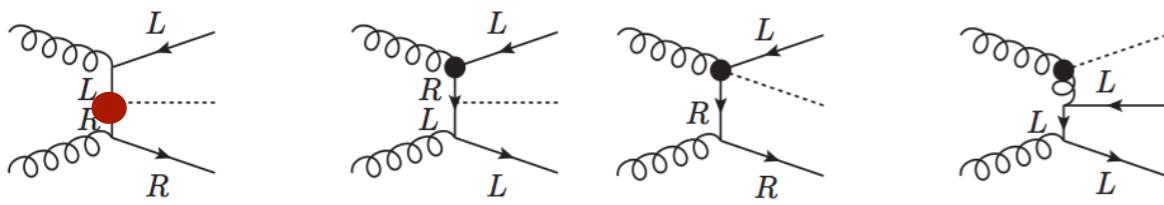
From a global fit the coupling of the higgs to the top is poorly determined: the loop could still be dominated by np.

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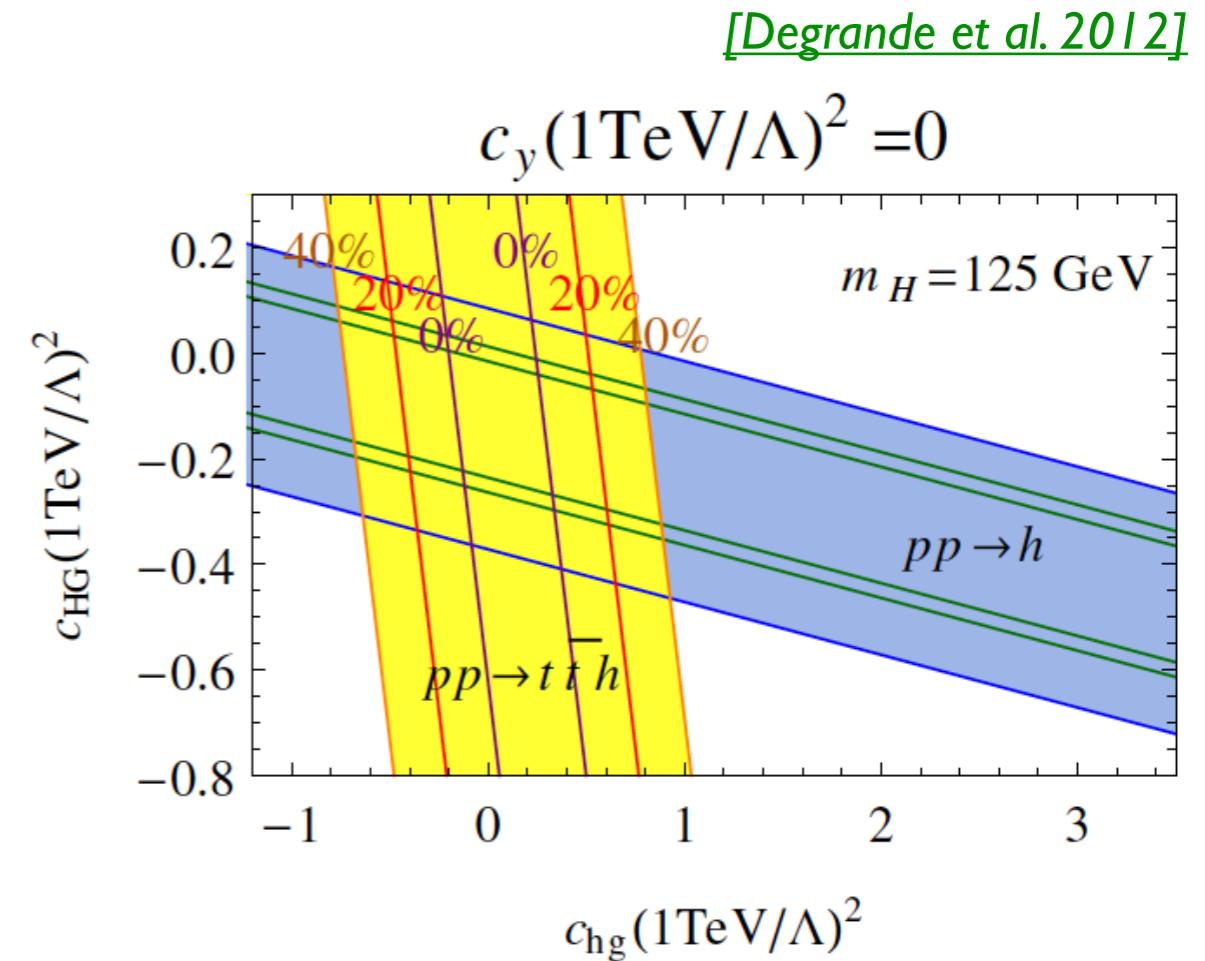


EFT at NLO predictions available, yet SM NLO predictions are needed to control accuracy and precision.

Top-Higgs interactions: ttH

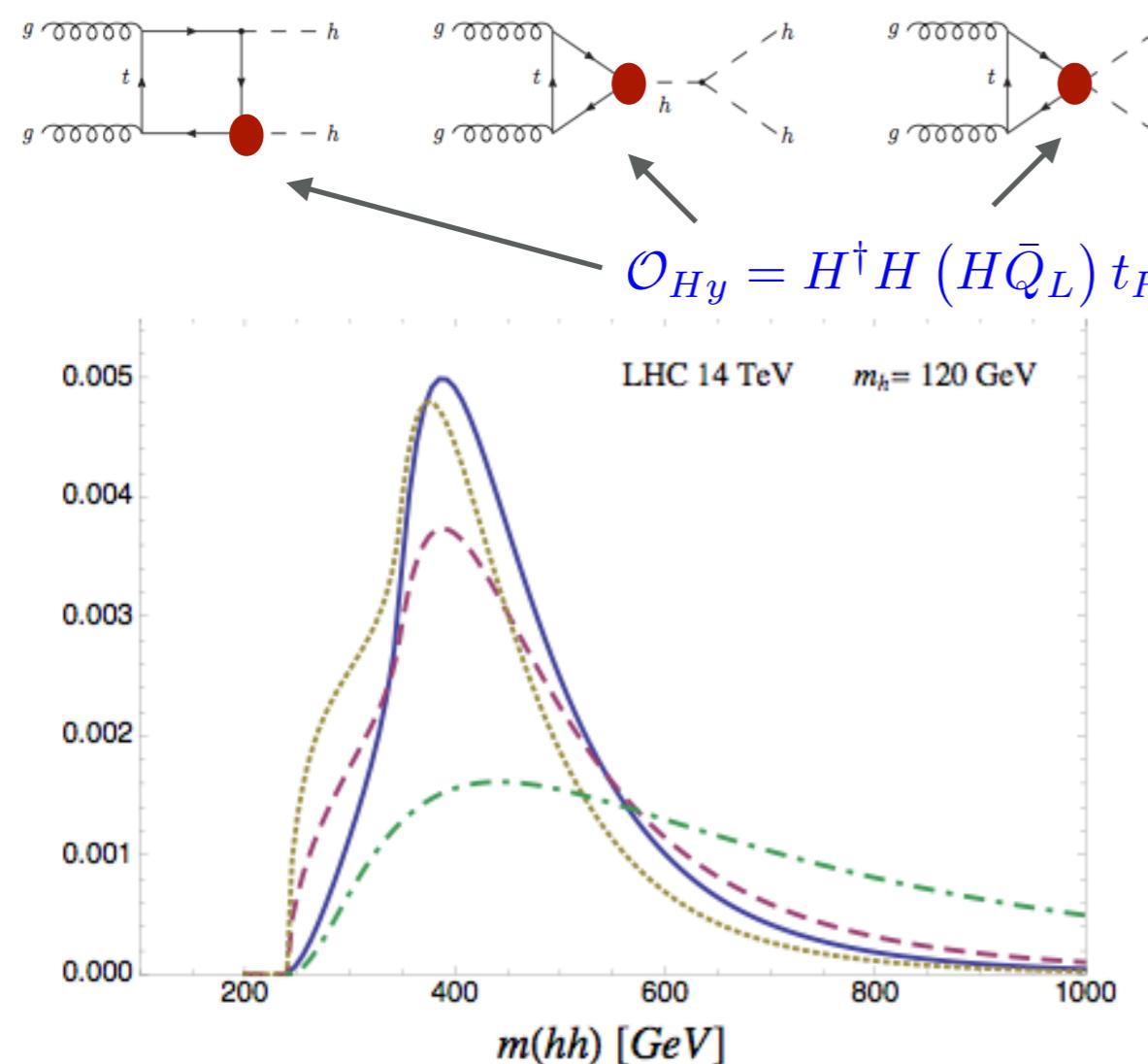


$$\begin{aligned}
 \frac{\sigma(pp \rightarrow t\bar{t}h)}{\text{fb}} = & 611_{-110}^{+92} + [457_{-91}^{+127} \Re c_{hg} - 49_{-10}^{+15} c_G \\
 & + 147_{-32}^{+55} c_{HG} - 67_{-16}^{+23} c_y] \left(\frac{\text{TeV}}{\Lambda} \right)^2 \\
 & + [543_{-123}^{+143} (\Re c_{hg})^2 + 1132_{-232}^{+323} c_G^2 \\
 & + 85.5_{-21}^{+73} c_{HG}^2 + 2_{-0.5}^{+0.7} c_y^2 \\
 & + 233_{-144}^{+81} \Re c_{hg} c_{HG} - 50_{-14}^{+16} \Re c_{hg} c_y \\
 & - 3.2_{-8}^{+8} \Re c_{Hy} c_{HG} - 1.2_{-8}^{+8} c_H c_{HG}] \left(\frac{\text{TeV}}{\Lambda} \right)^4
 \end{aligned}$$



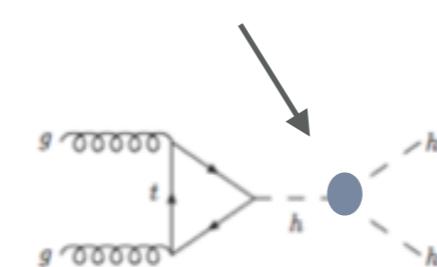
Top-Higgs interactions: HH

$pp \rightarrow hh$

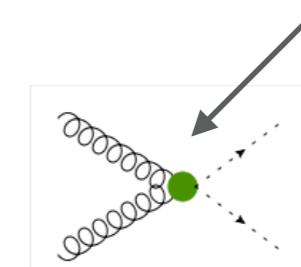


[Contino et al. 2012]

$$\mathcal{O}_6 = (H^\dagger H)^3$$



$$\mathcal{O}_{HG} = \frac{1}{2} H^\dagger H G_{\mu\nu}^a G_a^{\mu\nu}$$

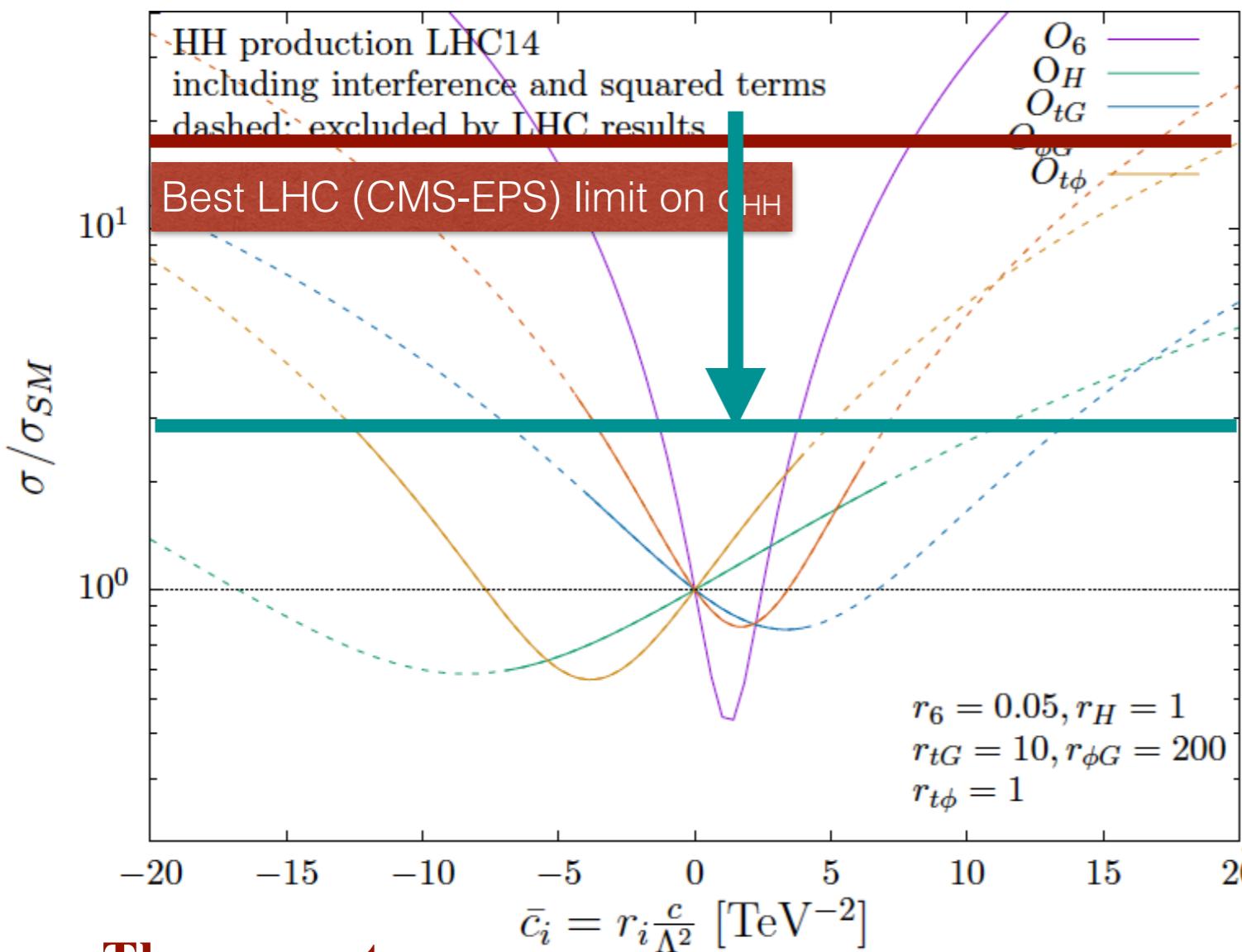


The strong destructive interference gives extra sensitivity of $pp \rightarrow HH$ to dim=6 operators.

The HHH coupling is modified by two operators of dim=6.

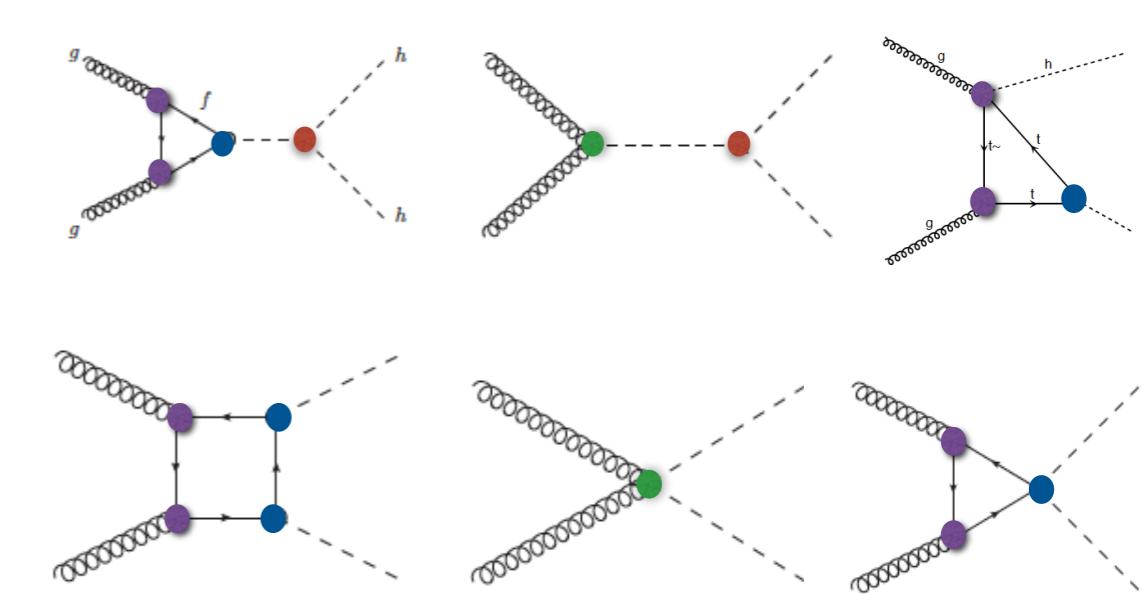
Only a global approach will allow to accurately measure the HHH coupling from HH .

How to extract λ_{HHH} from HH?



The present

Given the current constraints on $\sigma(\text{HH})$, $\sigma(\text{H})$ and the fresh $t\bar{t}\text{H}$ measurement, the Higgs self-coupling can be currently constrained “ignoring” other couplings



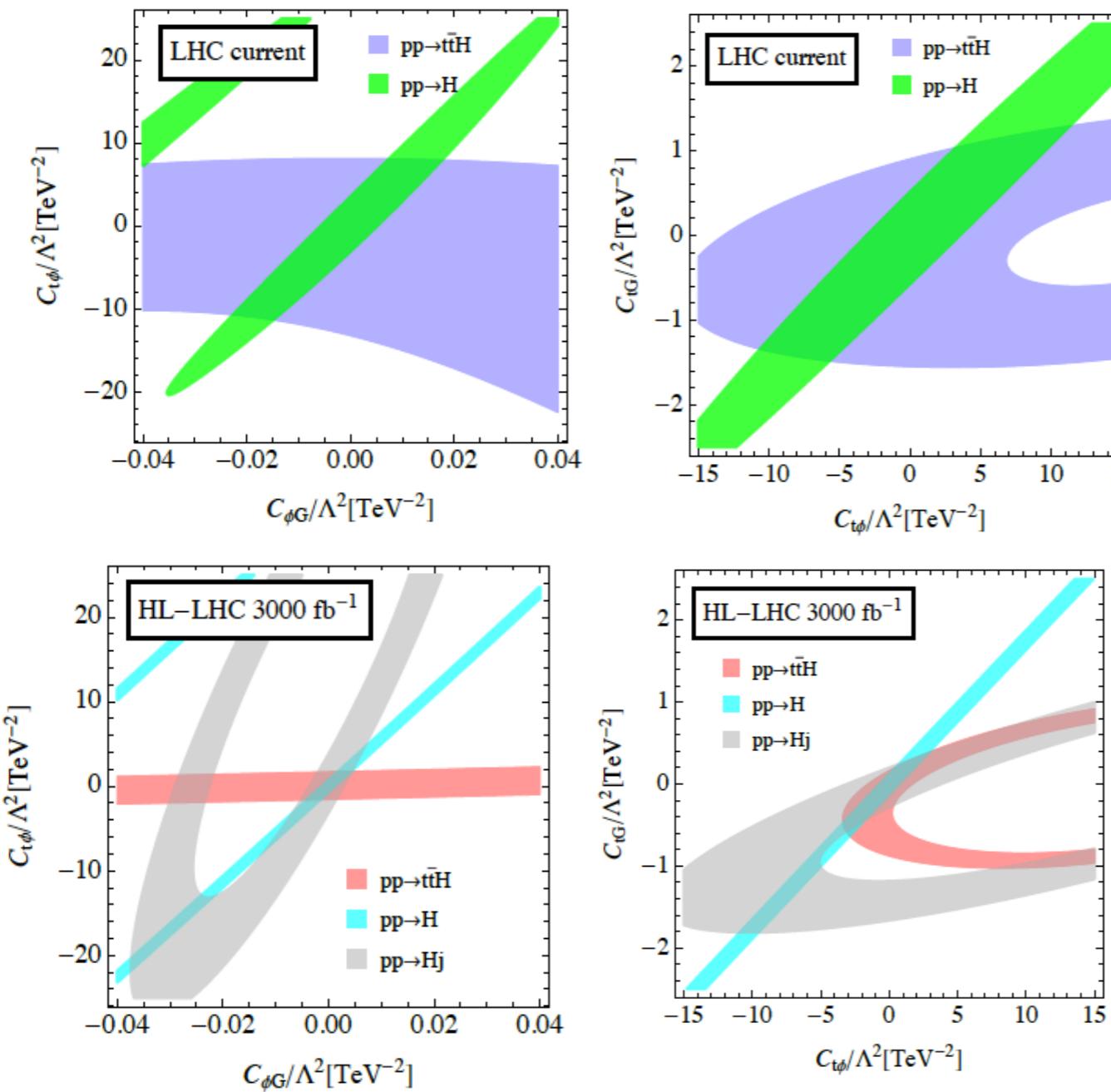
Other couplings enter in the same process: top Yukawa, ggh(h) coupling, top-gluon interaction

The future

Precise knowledge of other Wilson coefficients will be needed to bound λ as the bound gets closer to SM. Differential distributions will also be necessary

Constraints from ttH and Higgs production

[FM, Vryonidou, Zhang, 16]



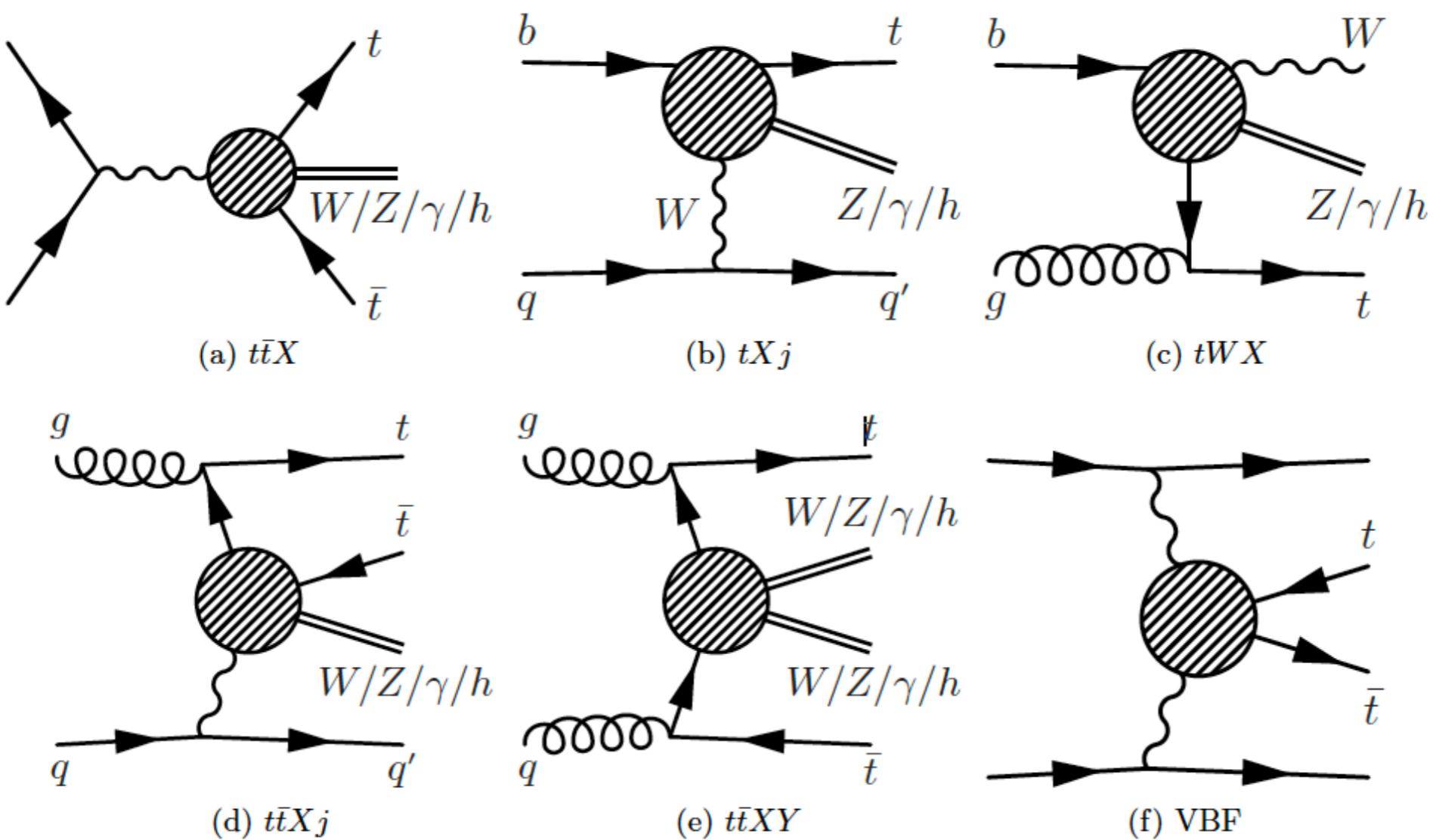
Current limits using LHC measurements

$$\begin{aligned}
 O_{t\phi} &= y_t^3 \left(\phi^\dagger \phi \right) (\bar{Q} t) \tilde{\phi} \\
 O_{\phi G} &= y_t^2 \left(\phi^\dagger \phi \right) G_{\mu\nu}^A G^{A\mu\nu} \\
 O_{tG} &= y_t g_s (\bar{Q} \sigma^{\mu\nu} T^A t) \tilde{\phi} G_{\mu\nu}^A
 \end{aligned}$$

14TeV projection

3000 fb-1

EW/Higgs top couplings sensitivity



See work at e^+e^- : [\[Durieux et al. 2018\]](#) [\[Durieux, Matsedonsky, 2018\]](#) [\[Riva, Grojean et al., 2018\] wip.](#)

Energy growths

gauge/higgs operators \longleftrightarrow top operators

| | $\mathcal{O}_{\varphi D}$ | $\mathcal{O}_{\varphi \square}$ | $\mathcal{O}_{\varphi B}$ | $\mathcal{O}_{\varphi W}$ | $\mathcal{O}_{\varphi WB}$ | \mathcal{O}_W | $\mathcal{O}_{t\varphi}$ | \mathcal{O}_{tB} | \mathcal{O}_{tW} | $\mathcal{O}_{\varphi Q}^{(1)}$ | $\mathcal{O}_{\varphi Q}^{(3)}$ | $\mathcal{O}_{\varphi t}$ | $\mathcal{O}_{\varphi tb}$ |
|--------------------------|---------------------------|---------------------------------|---------------------------|---------------------------|----------------------------|-----------------|--------------------------|--------------------|--------------------|---------------------------------|---------------------------------|---------------------------|----------------------------|
| $bW \rightarrow tZ$ | E | — | — | — | E | E^2 | — | E^2 | E^2 | E | E^2 | E | E^2 |
| $bW \rightarrow t\gamma$ | — | — | — | — | E | E^2 | — | E^2 | E^2 | — | — | — | — |
| $bW \rightarrow th$ | — | — | — | E | — | — | E | — | E^2 | — | E^2 | — | E^2 |

single-top

| | $\mathcal{O}_{\varphi D}$ | $\mathcal{O}_{\varphi \square}$ | $\mathcal{O}_{\varphi B}$ | $\mathcal{O}_{\varphi W}$ | $\mathcal{O}_{\varphi WB}$ | \mathcal{O}_W | $\mathcal{O}_{t\varphi}$ | \mathcal{O}_{tB} | \mathcal{O}_{tW} | $\mathcal{O}_{\varphi Q}^{(1)}$ | $\mathcal{O}_{\varphi Q}^{(3)}$ | $\mathcal{O}_{\varphi t}$ |
|-------------------------------|---------------------------|---------------------------------|---------------------------|---------------------------|----------------------------|-----------------|--------------------------|--------------------|--------------------|---------------------------------|---------------------------------|---------------------------|
| $tW \rightarrow tW$ | E | E | — | E | E | E^2 | E | E | E^2 | E^2 | E^2 | E^2 |
| $tZ \rightarrow tZ$ | E | E | E | E | E | — | E | E^2 | E^2 | E | E | E |
| $tZ \rightarrow t\gamma$ | — | — | E | E | E | — | — | E^2 | E^2 | — | — | — |
| $t\gamma \rightarrow t\gamma$ | — | — | E | E | E | — | — | E | E | — | — | — |

two-top
w/o Higgs

| | $\mathcal{O}_{\varphi D}$ | $\mathcal{O}_{\varphi \square}$ | $\mathcal{O}_{\varphi B}$ | $\mathcal{O}_{\varphi W}$ | $\mathcal{O}_{\varphi WB}$ | \mathcal{O}_W | $\mathcal{O}_{t\varphi}$ | \mathcal{O}_{tB} | \mathcal{O}_{tW} | $\mathcal{O}_{\varphi Q}^{(1)}$ | $\mathcal{O}_{\varphi Q}^{(3)}$ | $\mathcal{O}_{\varphi t}$ | $\mathcal{O}_{\varphi tb}$ |
|--------------------------|---------------------------|---------------------------------|---------------------------|---------------------------|----------------------------|-----------------|--------------------------|--------------------|--------------------|---------------------------------|---------------------------------|---------------------------|----------------------------|
| $tZ \rightarrow th$ | E | — | E | E | E | — | E | E^2 | E^2 | E^2 | E^2 | E^2 | — |
| $t\gamma \rightarrow th$ | — | — | E | E | E | — | — | E^2 | E^2 | — | — | — | — |
| $th \rightarrow th$ | E | E | — | — | — | — | E | — | — | — | — | — | — |

two-top
w/ Higgs

Energy growths

gauge/higgs operators \longleftrightarrow top operators Energy-growing interference

| | $\mathcal{O}_{\varphi D}$ | $\mathcal{O}_{\varphi \square}$ | $\mathcal{O}_{\varphi B}$ | $\mathcal{O}_{\varphi W}$ | $\mathcal{O}_{\varphi WB}$ | \mathcal{O}_W | $\mathcal{O}_{t\varphi}$ | \mathcal{O}_{tB} | \mathcal{O}_{tW} | $\mathcal{O}_{\varphi Q}^{(1)}$ | $\mathcal{O}_{\varphi Q}^{(3)}$ | $\mathcal{O}_{\varphi t}$ | $\mathcal{O}_{\varphi tb}$ |
|--------------------------|---------------------------|---------------------------------|---------------------------|---------------------------|----------------------------|-----------------|--------------------------|--------------------|--------------------|---------------------------------|---------------------------------|---------------------------|----------------------------|
| $bW \rightarrow tZ$ | E | — | — | — | E | E^2 | — | E^2 | E^2 | E | E^2 | E | E^2 |
| $bW \rightarrow t\gamma$ | — | — | — | — | E | E^2 | — | E^2 | E^2 | — | — | — | — |
| $bW \rightarrow th$ | — | — | — | E | — | — | E | — | E^2 | — | E^2 | — | E^2 |

single-top

| | $\mathcal{O}_{\varphi D}$ | $\mathcal{O}_{\varphi \square}$ | $\mathcal{O}_{\varphi B}$ | $\mathcal{O}_{\varphi W}$ | $\mathcal{O}_{\varphi WB}$ | \mathcal{O}_W | $\mathcal{O}_{t\varphi}$ | \mathcal{O}_{tB} | \mathcal{O}_{tW} | $\mathcal{O}_{\varphi Q}^{(1)}$ | $\mathcal{O}_{\varphi Q}^{(3)}$ | $\mathcal{O}_{\varphi t}$ | |
|-------------------------------|---------------------------|---------------------------------|---------------------------|---------------------------|----------------------------|-----------------|--------------------------|--------------------|--------------------|---------------------------------|---------------------------------|---------------------------|--|
| $tW \rightarrow tW$ | E | E | — | E | E | E^2 | E | E | E^2 | E^2 | E^2 | E^2 | |
| $tZ \rightarrow tZ$ | E | E | E | E | E | — | E | E^2 | E^2 | E | E | E | |
| $tZ \rightarrow t\gamma$ | — | — | E | E | E | — | — | E^2 | E^2 | — | — | — | |
| $t\gamma \rightarrow t\gamma$ | — | — | E | E | E | — | — | E | E | — | — | — | |

two-top
w/o Higgs

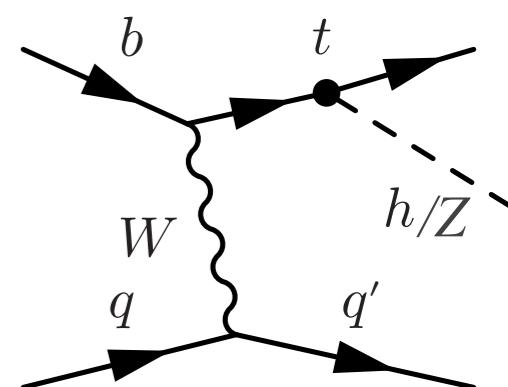
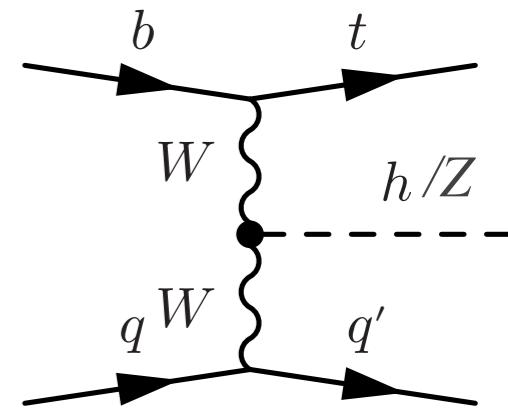
| | $\mathcal{O}_{\varphi D}$ | $\mathcal{O}_{\varphi \square}$ | $\mathcal{O}_{\varphi B}$ | $\mathcal{O}_{\varphi W}$ | $\mathcal{O}_{\varphi WB}$ | \mathcal{O}_W | $\mathcal{O}_{t\varphi}$ | \mathcal{O}_{tB} | \mathcal{O}_{tW} | $\mathcal{O}_{\varphi Q}^{(1)}$ | $\mathcal{O}_{\varphi Q}^{(3)}$ | $\mathcal{O}_{\varphi t}$ | $\mathcal{O}_{\varphi tb}$ |
|--------------------------|---------------------------|---------------------------------|---------------------------|---------------------------|----------------------------|-----------------|--------------------------|--------------------|--------------------|---------------------------------|---------------------------------|---------------------------|----------------------------|
| $tZ \rightarrow th$ | E | — | E | E | E | — | E | E^2 | E^2 | E^2 | E^2 | E^2 | — |
| $t\gamma \rightarrow th$ | — | — | E | E | E | — | — | E^2 | E^2 | — | — | — | — |
| $th \rightarrow th$ | E | E | — | — | — | — | E | — | — | — | — | — | — |

two-top
w/ Higgs

- Interfering growth rare, only in longitudinal configurations (c.f. helicity selection)

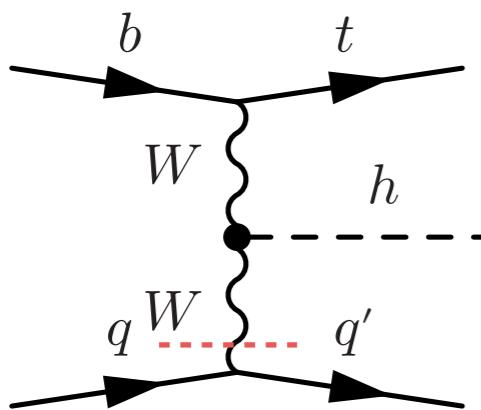
Example: tZj/tHj

- Single top rate about 1/4 of QCD $t\bar{t}$
- Purely EW processes \Rightarrow no QCD contribution
- Sensitive to 2 four-fermion and 3 top/EW operators that modify tbW vertex
- Requiring the presence of an additional Z or Higgs
 - Unique possibility of probing full set of top/Higgs/EW operators at once
 - Higher thresholds may enhance EFT effects
 - Recent LHC measurement of tZj cross section at 4.2σ



Example: tZj/tHj

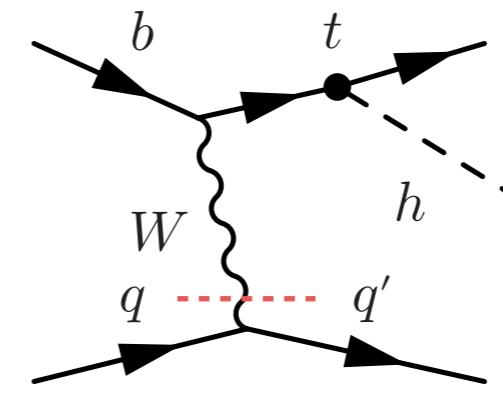
tHj ($tZj = h \rightarrow Z$) : classes of operators



$$\mathcal{O}_{\varphi_W} : \varphi^\dagger \varphi W_i^{\mu\nu} W_{\mu\nu}^i$$

HWW
TGC

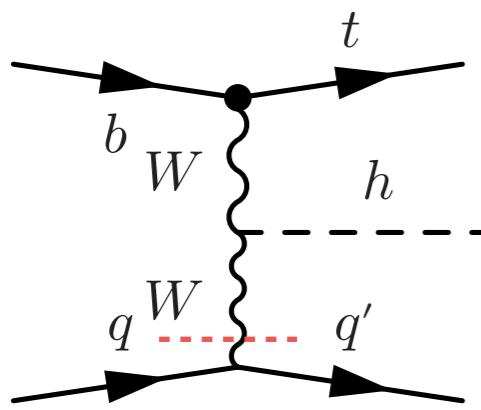
$$\mathcal{O}_W : \epsilon^{ijk} W_{i,\mu\nu} W_{j,\nu\rho}^{\nu\rho} W_{k,\rho}^{\mu}$$



$$\mathcal{O}_{t\varphi} : (\varphi^\dagger \varphi) (\bar{Q} t) \tilde{\varphi}$$

top Yukawa
ttZ coupling

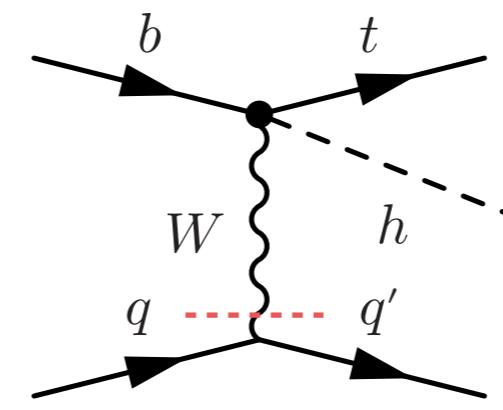
$$\mathcal{O}_{\varphi_t} : i(\varphi^\dagger \overleftrightarrow{D}_\mu \varphi) (\bar{t} \gamma^\mu t)$$



$$\mathcal{O}_{\varphi_Q}^{(3)} : i(\varphi^\dagger \overleftrightarrow{D}_\mu^i \varphi) (\bar{Q} \gamma^\mu \sigma_i Q)$$

Wtb vertex

$$\mathcal{O}_{\varphi_{tb}} : i(\tilde{\varphi} D_\mu \varphi) (\bar{b} \gamma^\mu t)$$

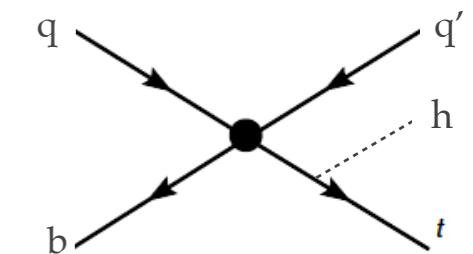


$$\mathcal{O}_{\varphi_Q}^{(3)} : i(\varphi^\dagger \overleftrightarrow{D}_\mu^i \varphi) (\bar{Q} \gamma^\mu \sigma_i Q)$$

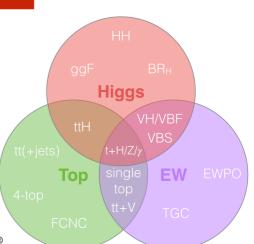
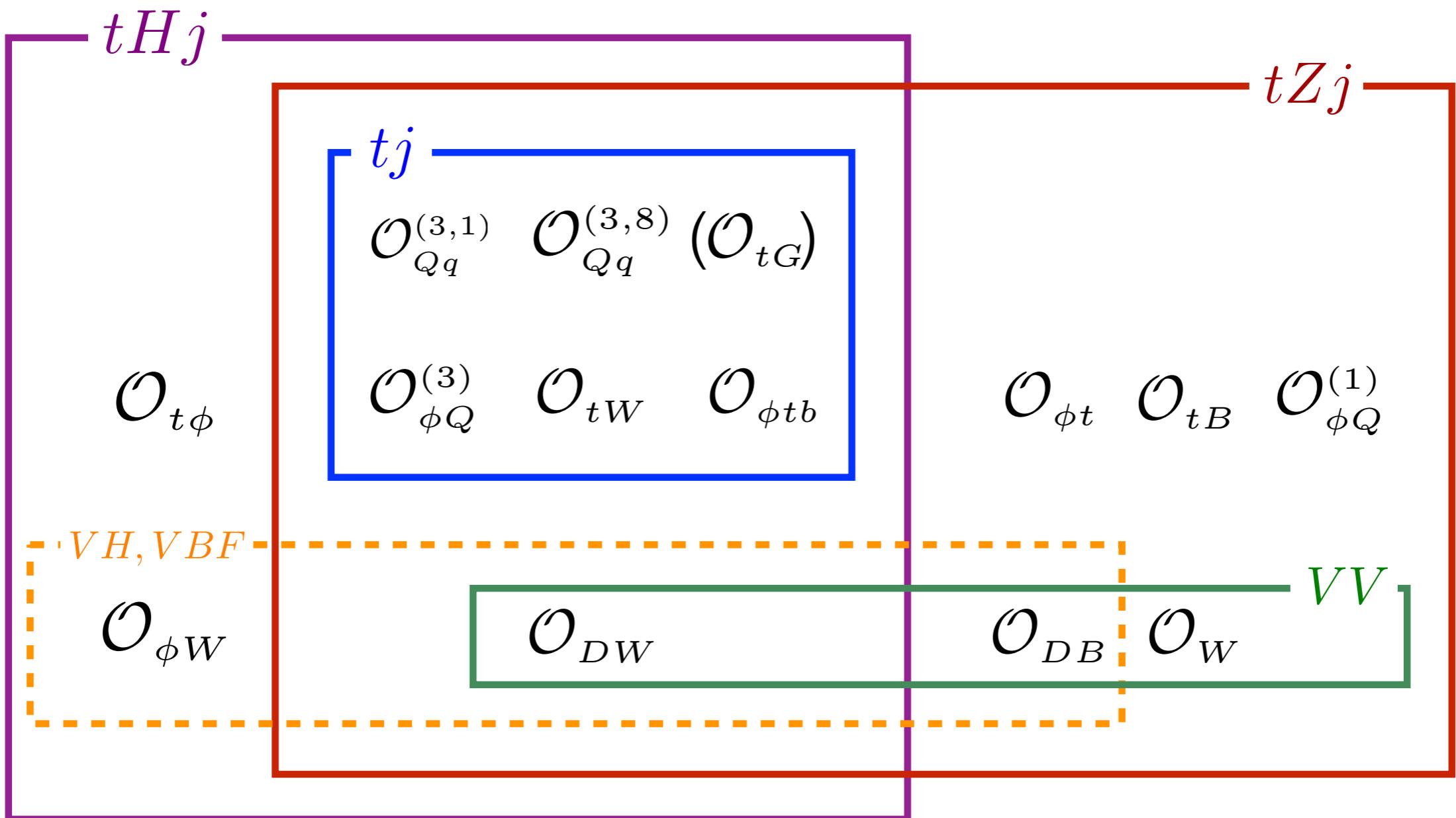
Contact terms

$$\mathcal{O}_{tB} : (\bar{Q} \sigma_{\mu\nu} t) \tilde{\varphi} B^{\mu\nu}$$

- Accessing the $bW \rightarrow tH$ & $bW \rightarrow tZ$ sub-amplitudes
 - Rich interplay between EFT operators from different sectors
 - Different energy growth and interference with the SM
 - Four fermion interactions also present

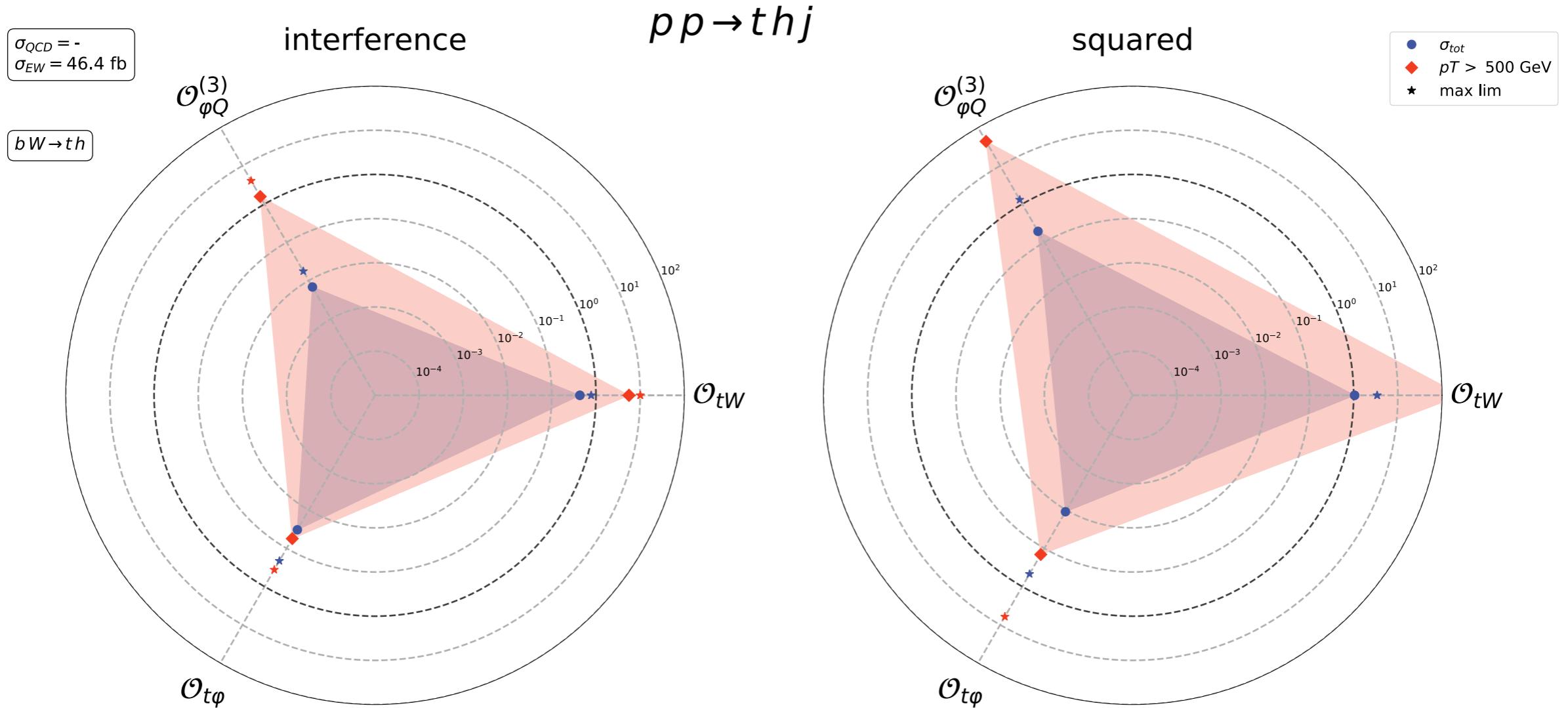


Example: tZj/tHj



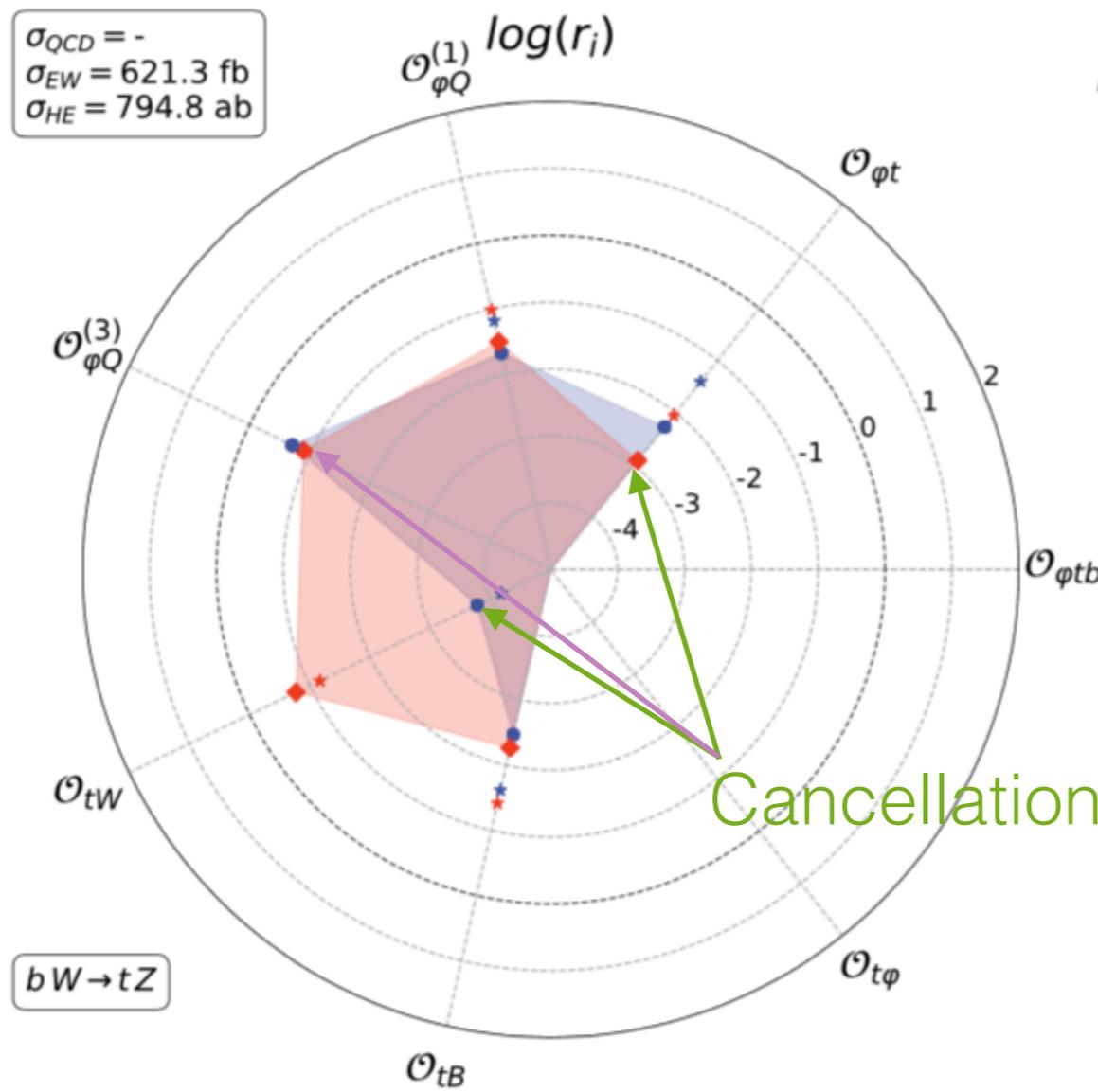
tHj

[FM, Mantani, Mimasu, 2018]



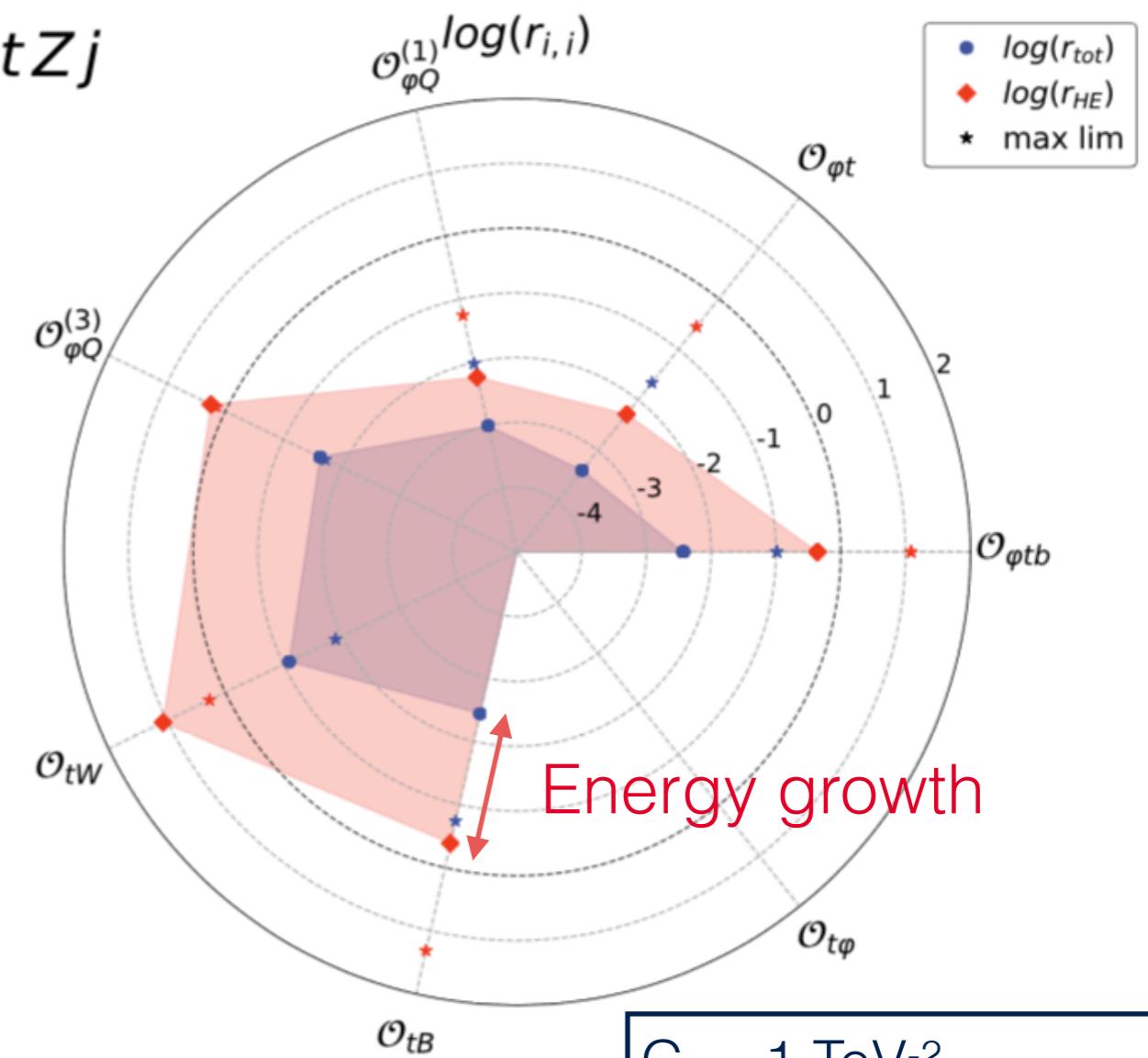
tZj

interference/SM



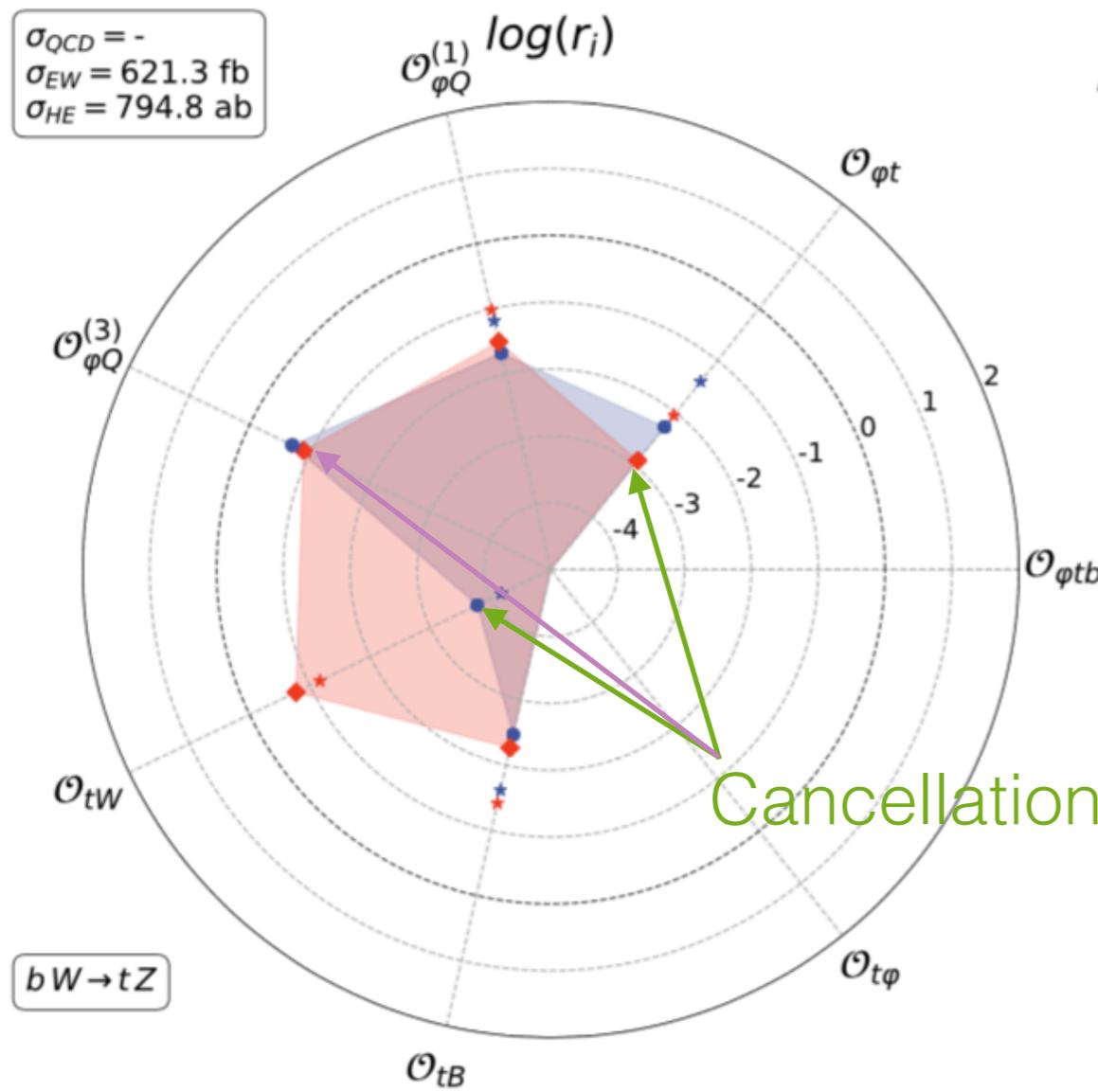
$pp \rightarrow tZj$

square/SM



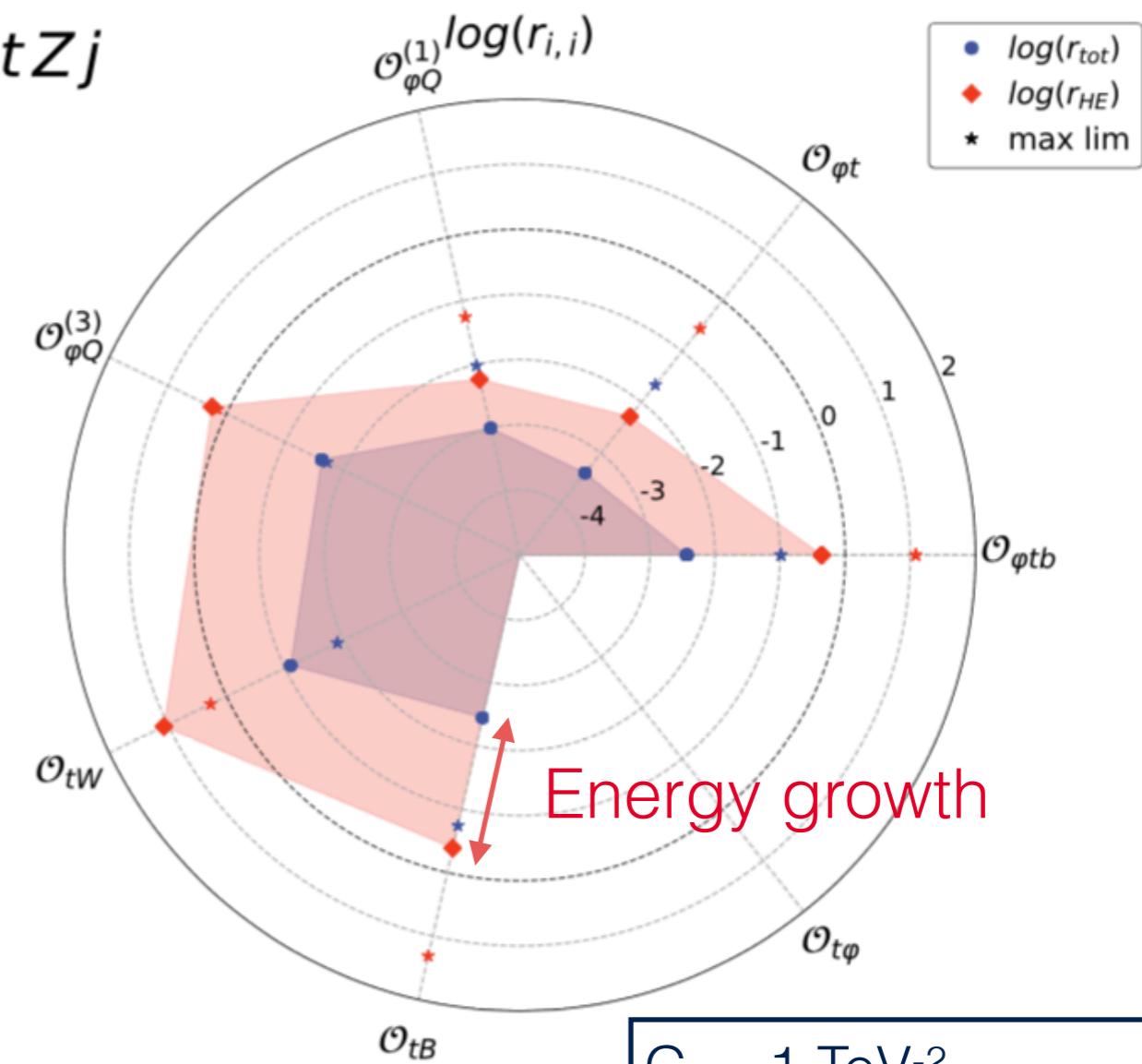
tZj

interference/SM



$pp \rightarrow tZj$

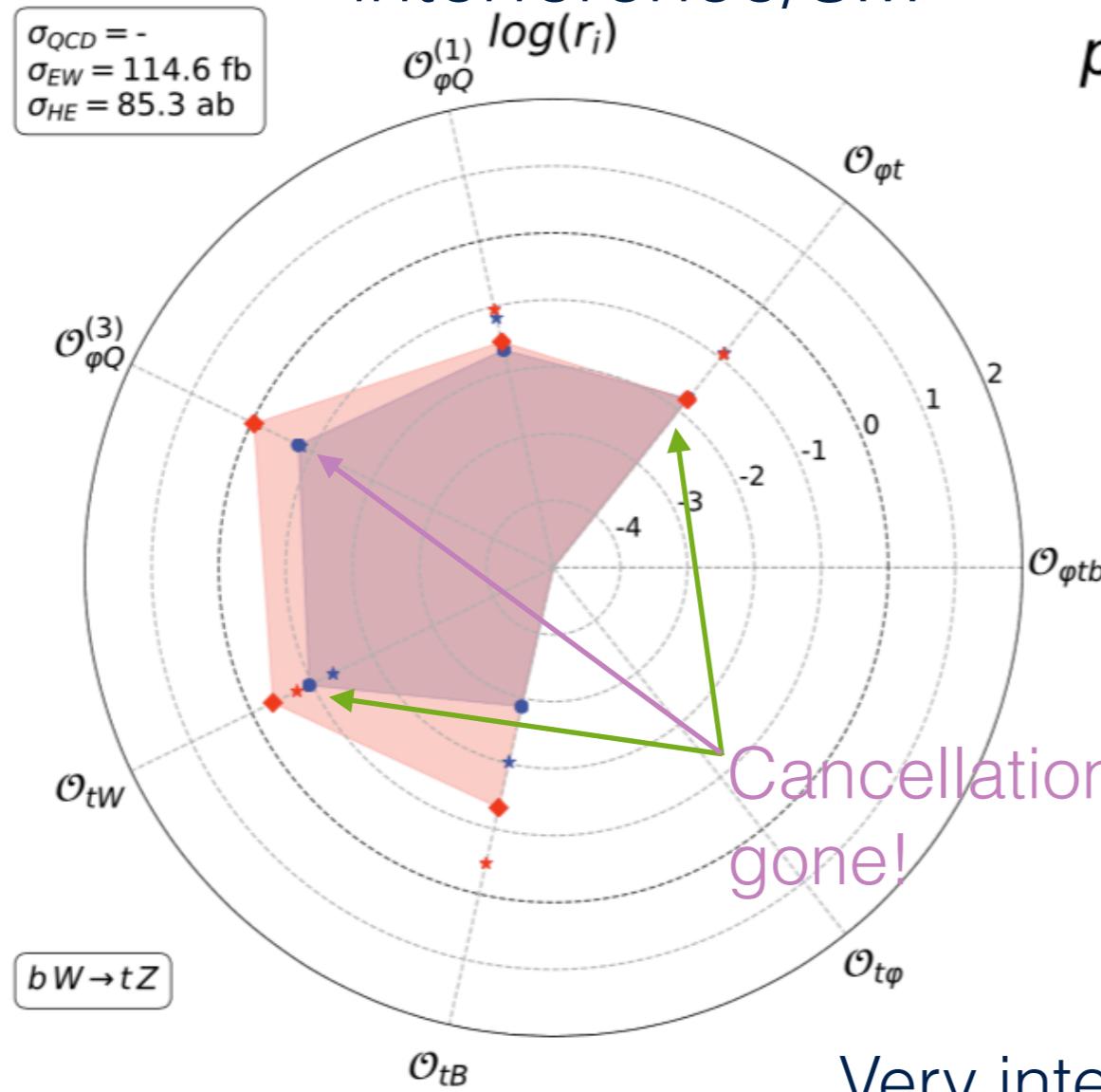
square/SM



Expected growth from $2 \rightarrow 2$ absent!

tZW

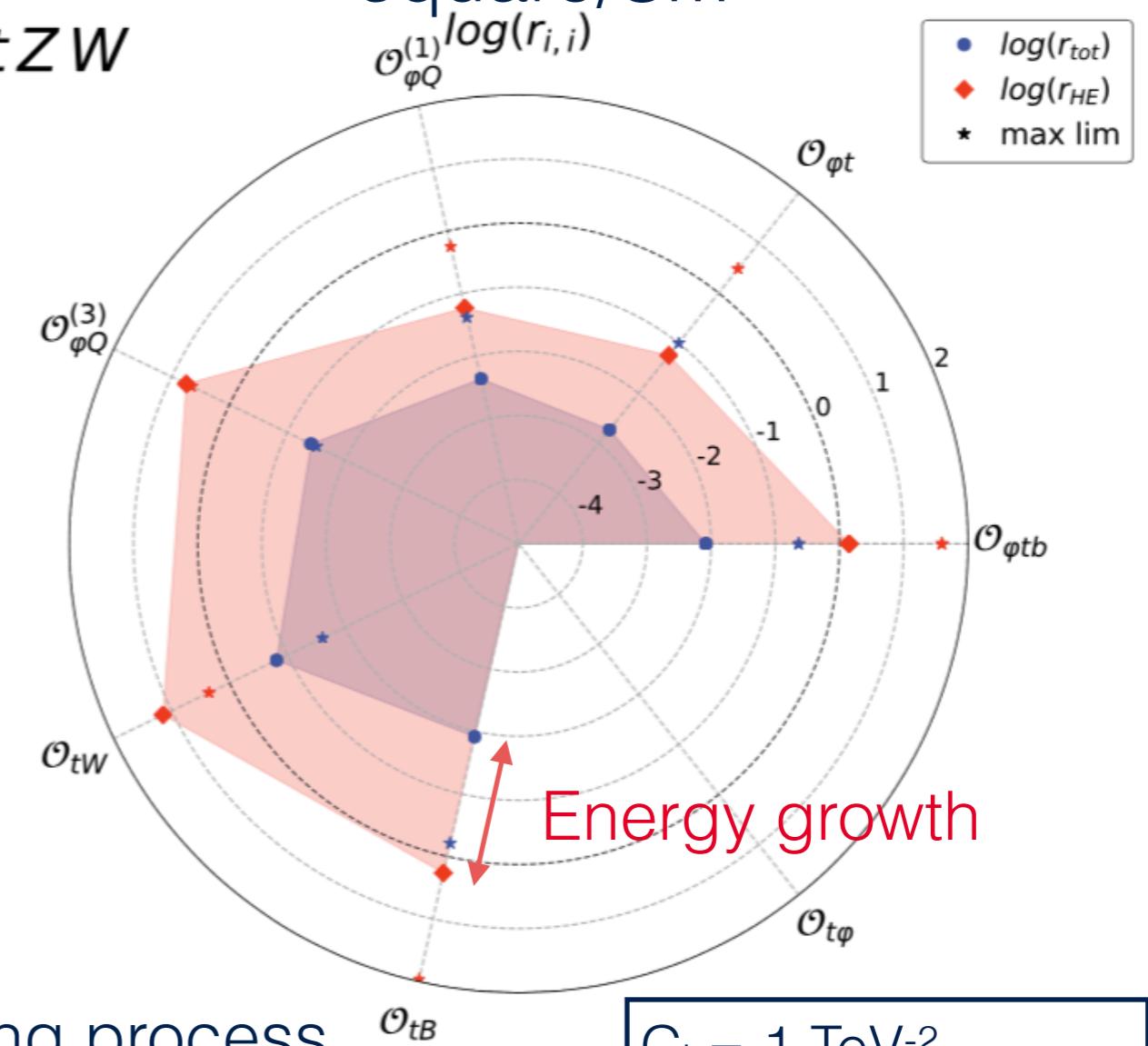
interference/SM



Expected growth is there!

$p p \rightarrow tZW$

square/SM



Very interesting process
that should be
measured at the LHC

$C_i = 1 \text{ TeV}^{-2}$
Inclusive
 $p_T(W,Z) > 500 \text{ GeV}$

Plan for today's lecture

- SMEFT essentials
- The SMEFT precision frontier
- Example: Fitting in the Top (with Higgs/EW) sector
- Bringing the lesson home

Plan for today's lecture

- SMEFT essentials
- The SMEFT precision frontier
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Need for NLO

- 1. Operators run and mix under RGE**
- 2. EFT scale dependence**
- 3. Genuine NLO corrections (finite terms) are important**
- 4. New operators arise**

Need for NLO

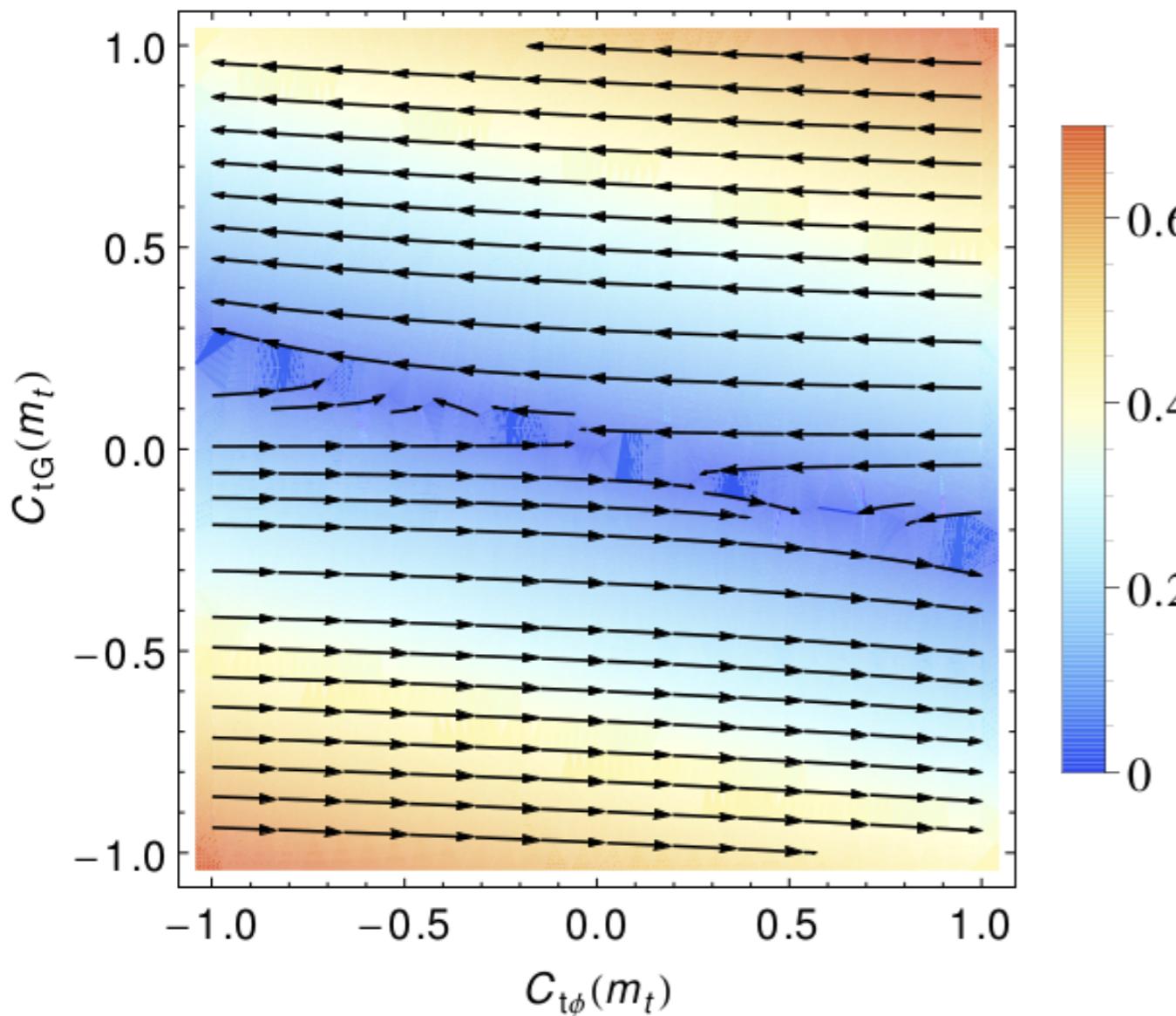
1. Operators run and mix under RGE

Running means that the Wilson coefficients depend on the scale where they are measured (as the couplings in the SM). Note that this introduces also an additional uncertainty in the perturbative computations.

Mixing means that in general the Wilson coefficients at low scale (=where the measurements happen) are related. One immediate consequence is that assumptions about some coefficients being zero at low scales are in general not valid (and in any case have to be consistent with the RGEs). Note also that operator mixing is not symmetric: Op1 can mix into Op2, but not viceversa.

Need for NLO

1. Operators run and mix under RGE



Scale corresponds to the change from m_t to 2 TeV.

$$\begin{aligned}
 O_{t\phi} &= y_t^3 (\phi^\dagger \phi) (\bar{Q} t) \tilde{\phi}, \\
 O_{\phi G} &= y_t^2 (\phi^\dagger \phi) G_{\mu\nu}^A G^{A\mu\nu}, \\
 O_{tG} &= y_t g_s (\bar{Q} \sigma^{\mu\nu} T^A t) \tilde{\phi} G_{\mu\nu}^A.
 \end{aligned}$$

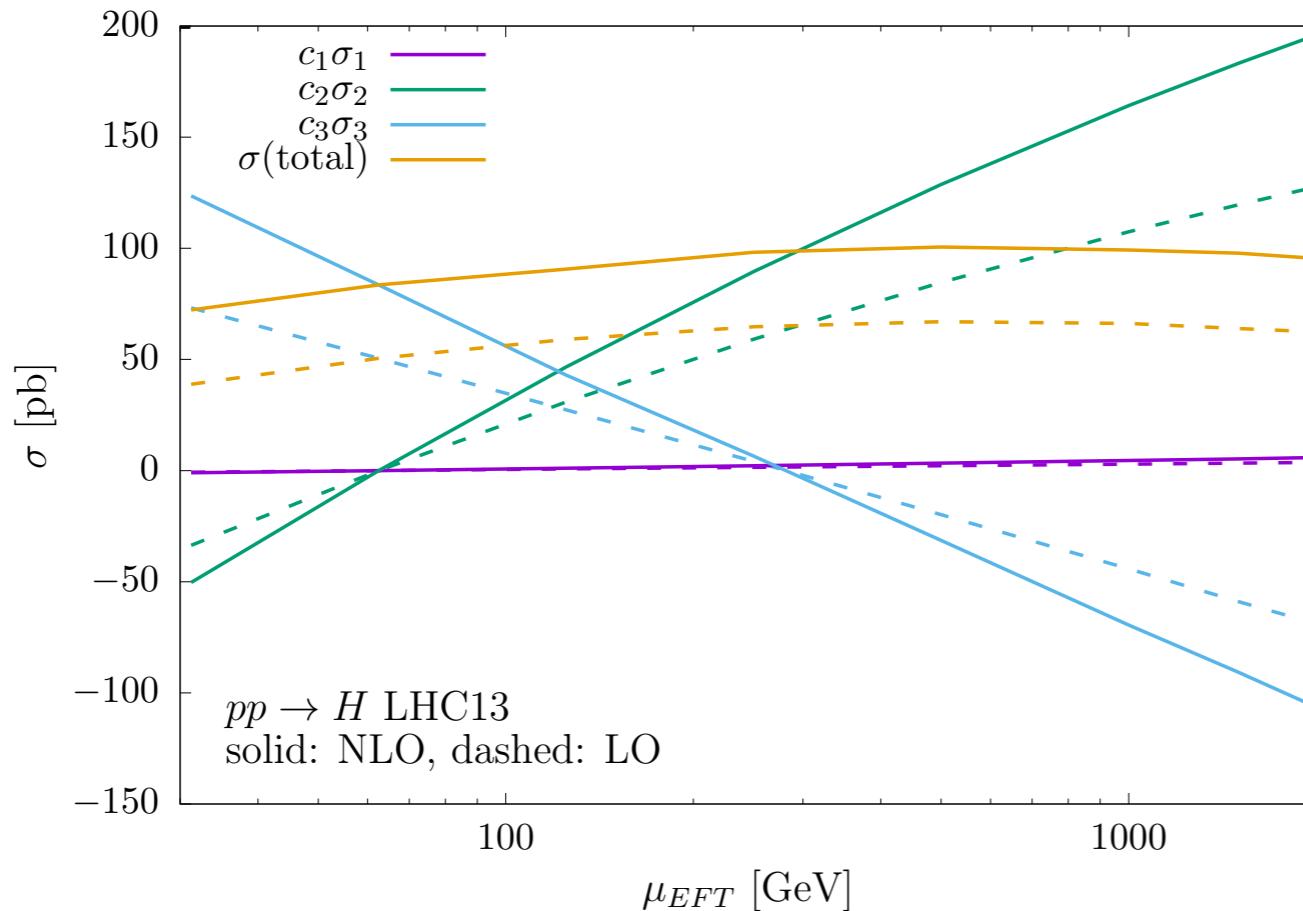
$$\frac{dC_i(\mu)}{d \log \mu} = \frac{\alpha_s}{\pi} \gamma_{ij} C_j(\mu), \quad \gamma = \begin{pmatrix} -2 & 16 & 8 \\ 0 & -7/2 & 1/2 \\ 0 & 0 & 1/3 \end{pmatrix}$$

At $\mu = 1$ TeV: $C_{tG} = 1, C_{t\phi} = 0$;

At $\mu = 173$ GeV: $C_{tG} = 0.98, C_{t\phi} = 0.45$

Need for NLO

2. EFT scale dependence



By including the mixing, the overall scale dependence at LO, is very much reduced with respect to the single ones. A global point of view is required: contribution from each coupling may not make sense; only their sum is meaningful.

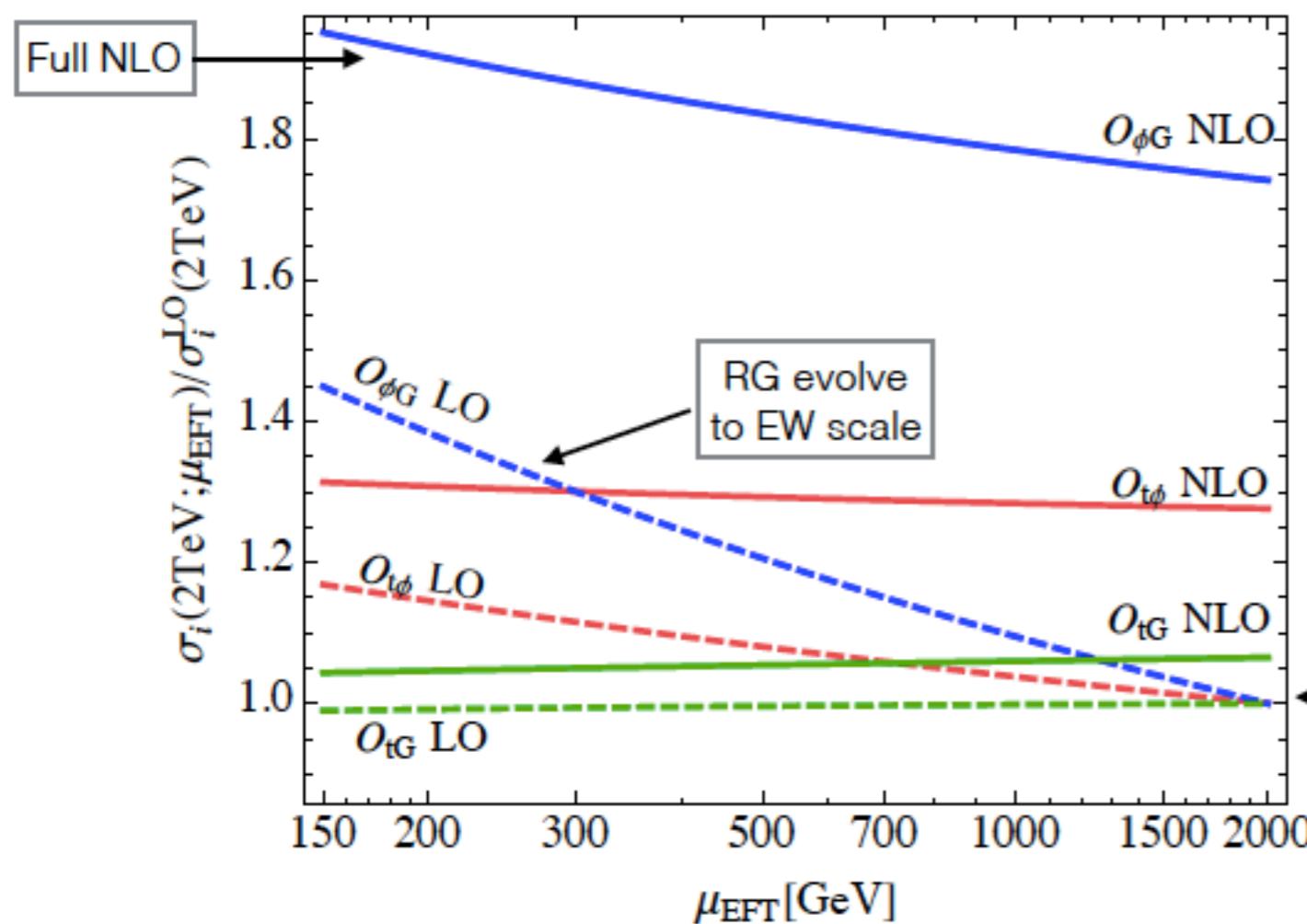
$$\begin{aligned}
 O_{t\phi} &= y_t^3 (\phi^\dagger \phi) (\bar{Q} t) \tilde{\phi}, \\
 O_{\phi G} &= y_t^2 (\phi^\dagger \phi) G_{\mu\nu}^A G^{A\mu\nu}, \\
 O_{tG} &= y_t g_s (\bar{Q} \sigma^{\mu\nu} T^A t) \tilde{\phi} G_{\mu\nu}^A.
 \end{aligned}$$

$$\frac{dC_i(\mu)}{d \log \mu} = \frac{\alpha_s}{\pi} \gamma_{ij} C_j(\mu),$$

$$\gamma = \begin{pmatrix} -2 & 16 & 8 \\ 0 & -7/2 & 1/2 \\ 0 & 0 & 1/3 \end{pmatrix}$$

Need for NLO

3. Genuine NLO corrections (finite terms) are important



- $\text{pp} \rightarrow \text{tH}$

$$O_{tφ} = y_t^3 \left(φ^\dagger φ \right) (Q t) φ̃,$$

$$O_{φG} = y_t^2 \left(φ^\dagger φ \right) G_{μν}^A G^{Aμν},$$

$$O_{tG} = y_t g_s (Q̃ σ^{μν} T^A t) φ̃ G_{μν}^A.$$
- EFT scale uncertainties are very much reduced at NLO.
- RG are sometimes thought to be an approximation for full NLO, but it is often not the case.

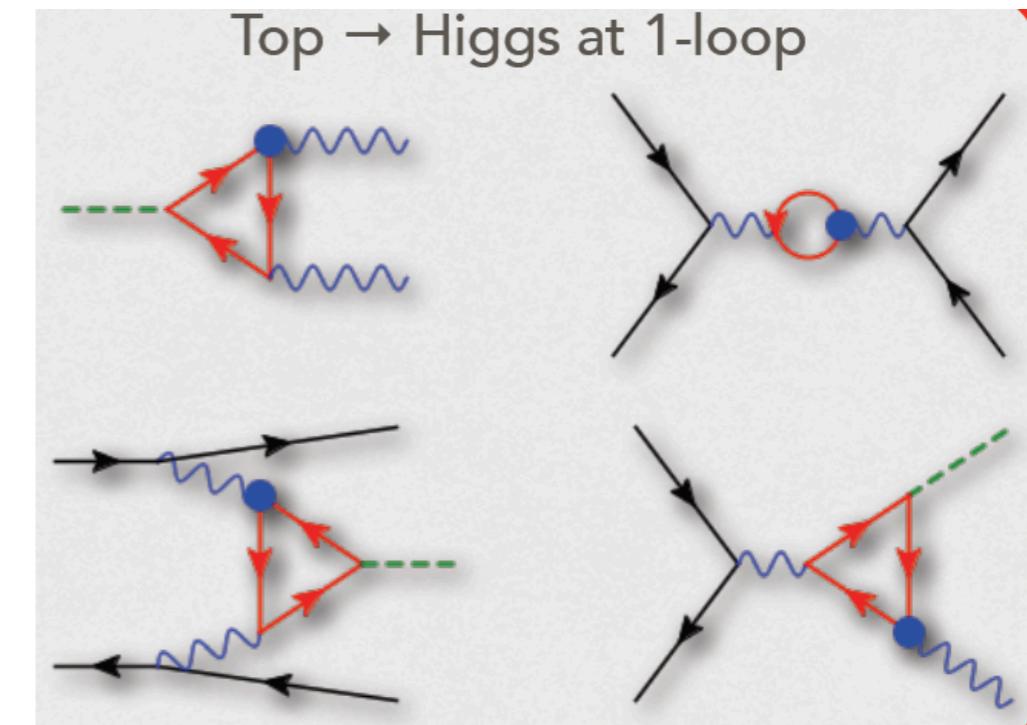
Need for NLO

4. New operators arise

New operators can arise at one-loop or via real corrections.

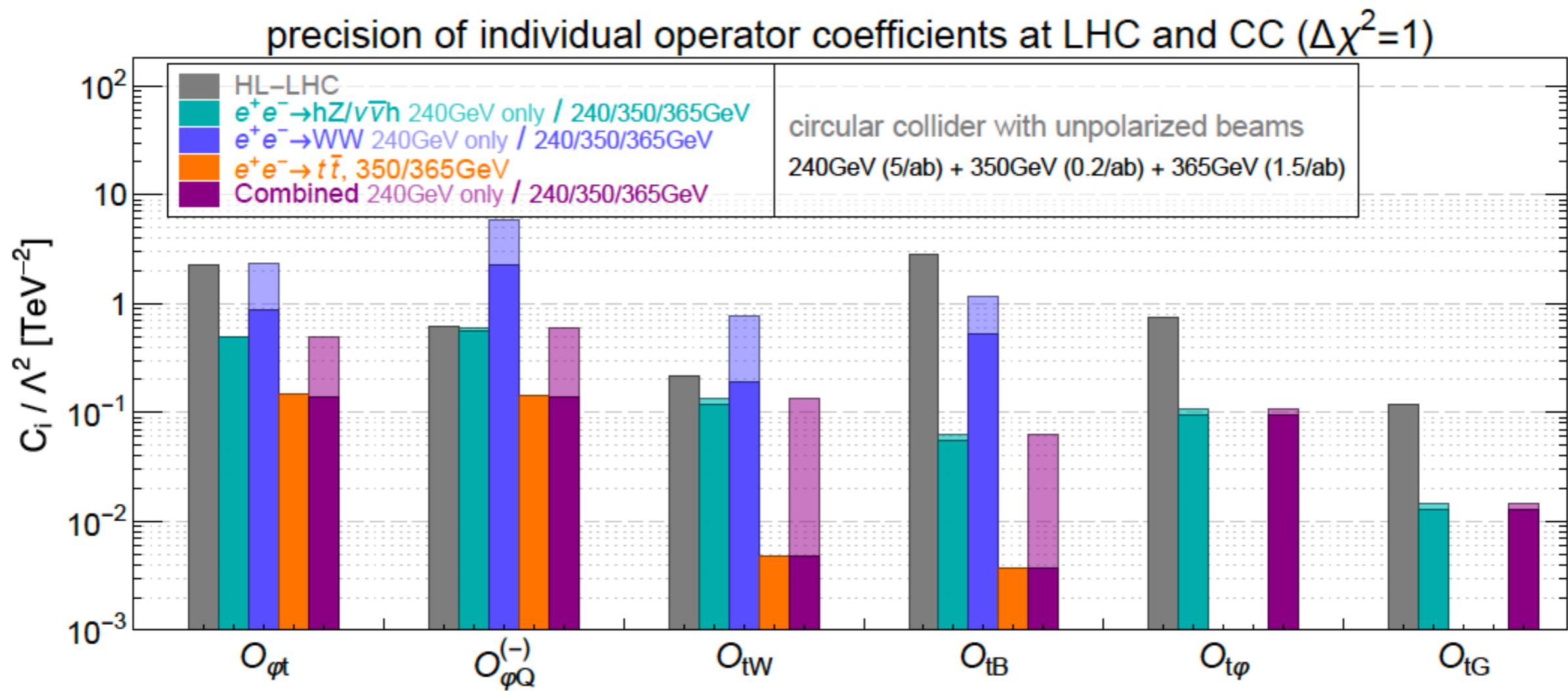
- At variance with the SM, loop-induced processes might not be finite.
- Including the full set of operators at a given order implies that no extra UV divergences appear (closure check).
- Use tree-level, loop-level, hierarchy but not gauge couplings.

- [\[Ghezzi, Gomez-Ambrosio, Passarino, Uccirati, 15a\]](#)
[\[Hartmann and Trott, 15\]](#)
[\[Ghezzi, Gomez-Ambrosio, Passarino, Uccirati, 15b\]](#)
[\[Dawson, Giardino, 2018, 2019\]](#)
[\[Dedes et al, 2018\]](#)
[\[Vryonidou and Zhang, 2018\]](#)



Need for NLO

4. New operators arise



[Durieux, Gu, Vryonidou and Zhang, 2018]

SMEFT codes

- ❖ Single & double Higgs (partial SMEFT)
 - ❖ HiGlu, SusHi, HPAIR, HiggsPair
 - ❖ eHDECAY for BR
 - ❖ HAWK
 - ❖ VBF and VH @ NLO in QCD & EW for SM + 2 anomalous couplings
 - ❖ VBFNLO
 - ❖ General (FO) tool for Higgs/weak boson production @ NLO in QCD
 - ❖ POWHEG-BOX/MCFM
 - ❖ VH NLO QCD + PS for Higgs/EW operators (SILH) [KM et al.; JHEP 1608 (2016) 039]
 - ❖ Drell-Yan & EW Higgs production with more operators [Alioli et al.; JHEP 08 (2018) 205]
 - ❖ WW with TGC & quark vertex operators [Baglio et al.; PRD 99 (2019) 035029]
- [Spira; arXiv:hep-ph/9510347]
 [Harlander, Liebler & Mantler; arXiv:
 1605.03190]
 [Dawson, Dittmaier & Spira; Phys. Rev.
 D58:115012]
 [Goertz et al.; JHEP 1504 (2015) 167]
 [Contino et al.; Comp. Phys. Comm. 185 (2014) 3412-3423]
<https://www.itp.kit.edu/~maggie/eHDECAY/>
 [Denner et al.; JHEP 1203 (2012) 075]
<http://omnibus.uni-freiburg.de/~sd565/programs/hawk/hawk>
 [Baglio et al.; arXiv:1404.3940]
<https://www.itp.kit.edu/vbfnlo>
<http://powhegbox.mib.infn.it>
 [KM et al.; JHEP 1608 (2016) 039]
 [Alioli et al.; JHEP 08 (2018) 205]
 [Baglio et al.; PRD 99 (2019) 035029]

SMEFT models

- ❖ HEL
 - ❖ Flavor universal SILH basis @ LO [Alloul et al.; JHEP 1404 (2014) 110]
<http://feynrules.irmp.ucl.ac.be/wiki/HEL>
 - ❖ Higgs/EW operators in SILH basis @ NLOQCD (HELatNLO) [Degrade, et al.; EPJC 77 (2017) 4, 262]
<http://feynrules.irmp.ucl.ac.be/wiki/HELatNLO>
- ❖ SMEFTsim
 - ❖ Complete Warsaw basis (2499!) @ LO with flavor restriction options [Brivio et al.; JHEP 1712 (2017) 070]
<http://feynrules.irmp.ucl.ac.be/wiki/SMEFT>
- ❖ SMEFTfr
 - ❖ FeynRules for Warsaw basis @ LO in R_ξ -gauge [Dedes et al.; JHEP 1706 (2017) 143]
[Misiak et al.; JHEP 1902 (2019) 051]
<https://www.few.edu.pl/smeft>
- ❖ dim6top
 - ❖ top sector @ LO, several flavor symmetry scenarios (LH top WG) [Aguilar-Saavedra et al.; arXiv:1802.07237]
<http://feynrules.irmp.ucl.ac.be/wiki/dim6top>
- ❖ SMEFTatNLO
 - ❖ top/Higgs/EW sector @ NLOQCD (4F operators now validated) [Degrade et al.; in preparation]
<http://feynrules.irmp.ucl.ac.be/wiki/SMEFTatNLO>

SMEFT at NLO

Aim to fully automate NLO calculations in the SMEFT within public Monte Carlo generators based on:

- Warsaw basis of dimension-6 operators

Current status:

- 73 degrees of freedom (top, Higgs, gauge):
 - CP-conserving
 - Flavour assumption: $U(2)_Q \times U(2)_u \times U(3)_d \times U(3)_L \times U(3)_e$
- Successful validation with LO implementations
- 0/2F@NLO operators validated (with previous partial NLO implementations)
<http://feynrules.irmp.ucl.ac.be/wiki/SMEFTatNLO>
- 4F@NLO operators validation: completed

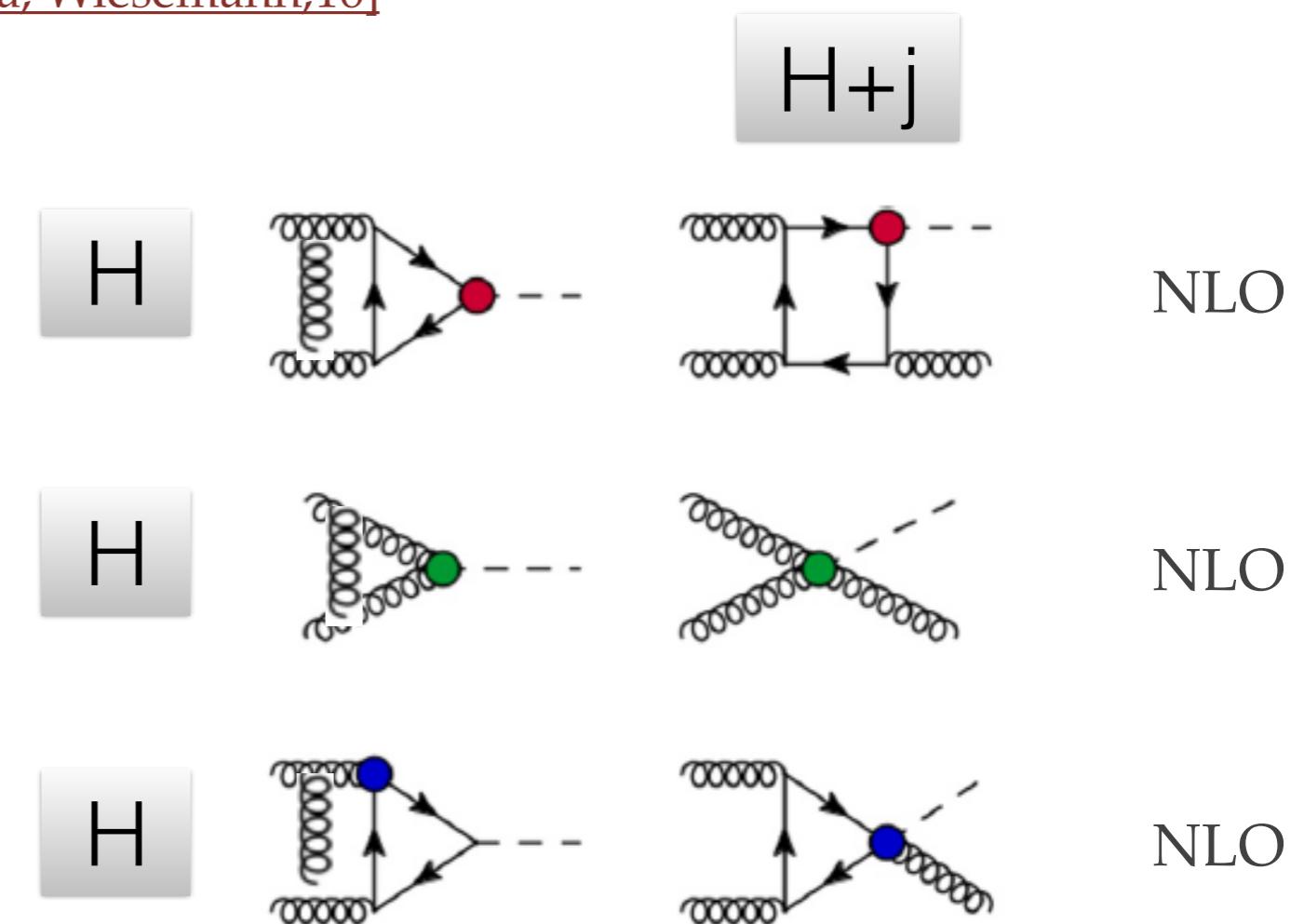
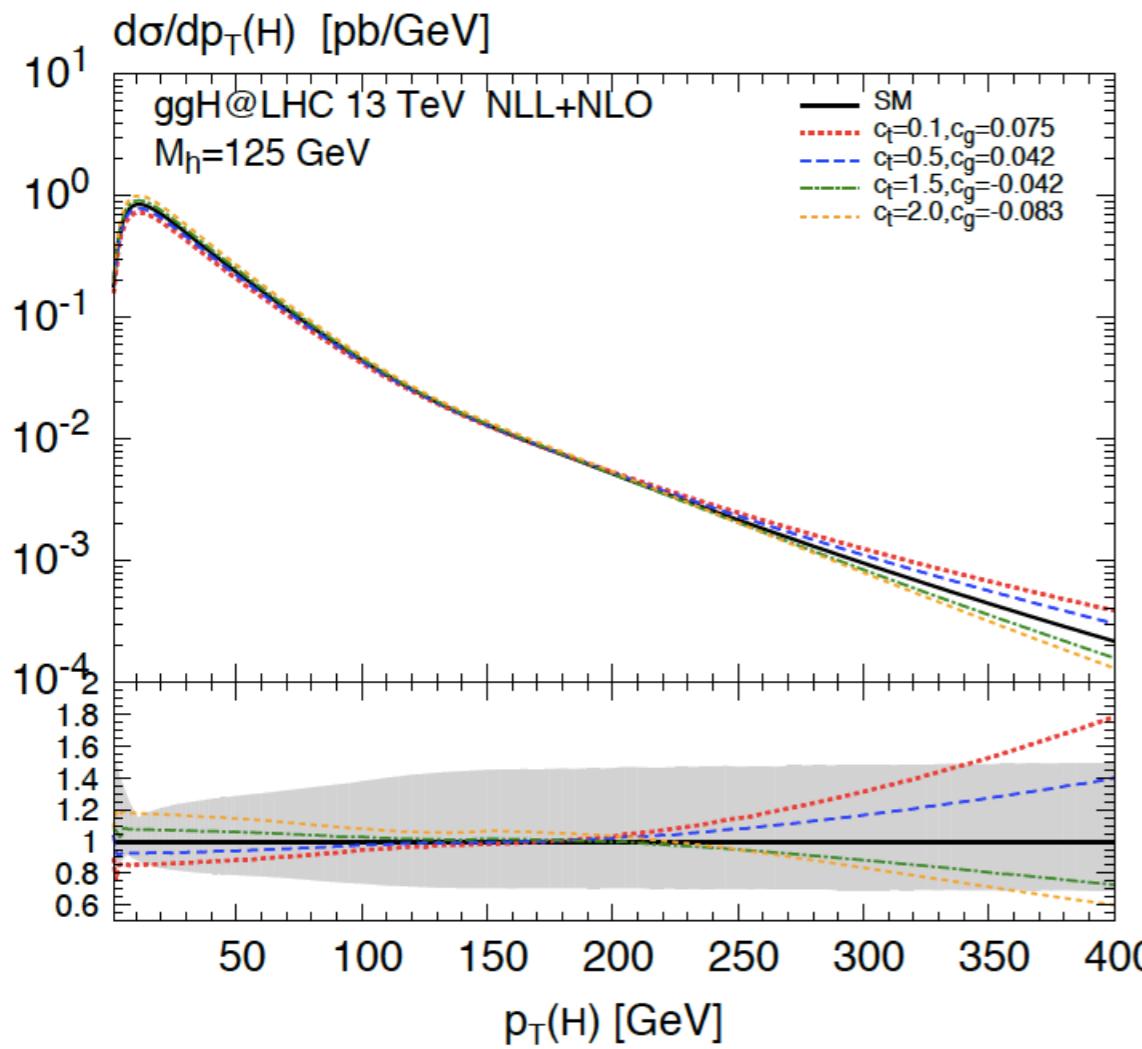
Paves the way for a precise SMEFT programme at the LHC

[In collaboration with: C. Degrande, G. Durieux, K. Mimasu, E. Vryonidou, C. Zhang]

ggH at NLO

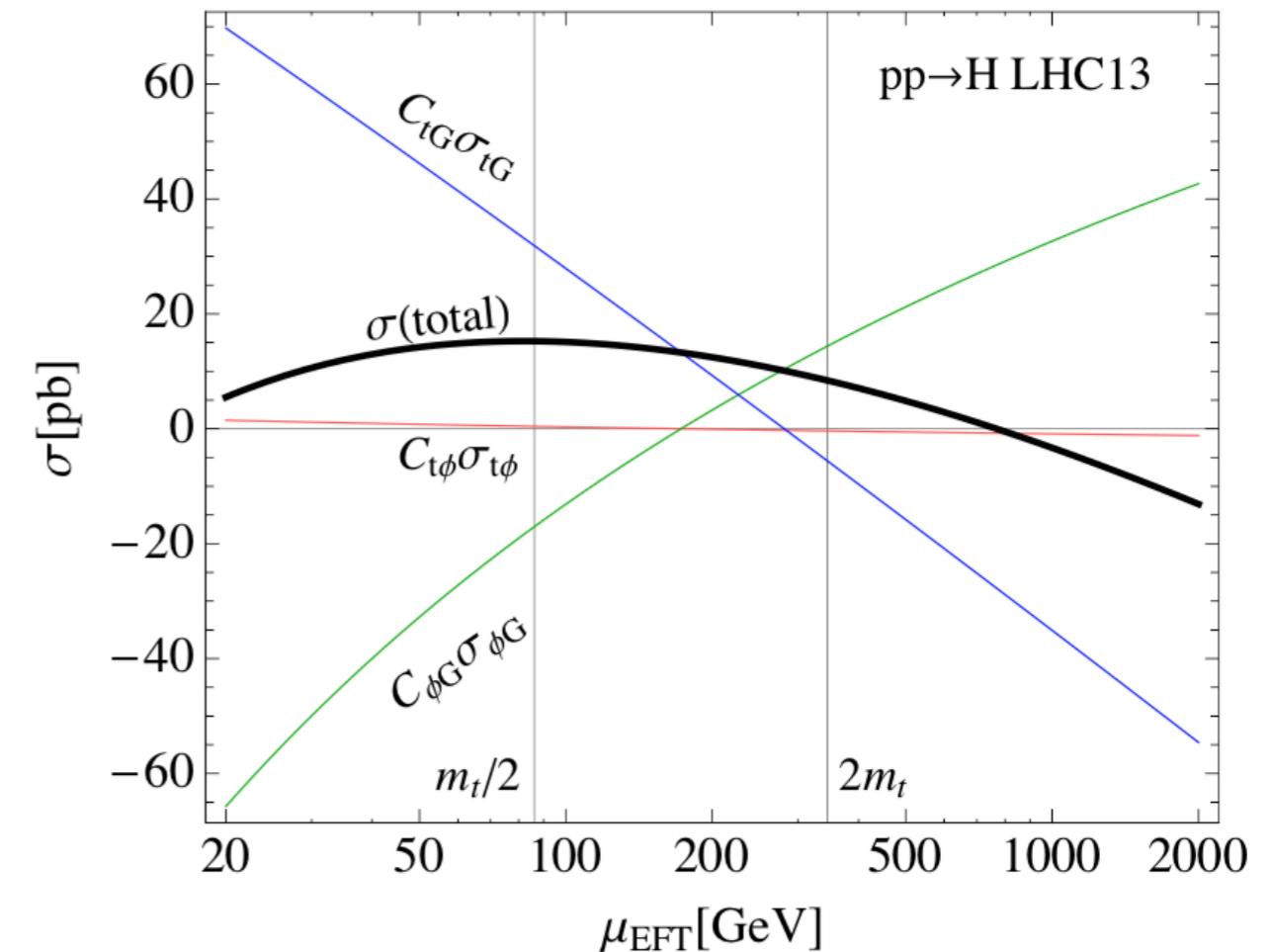
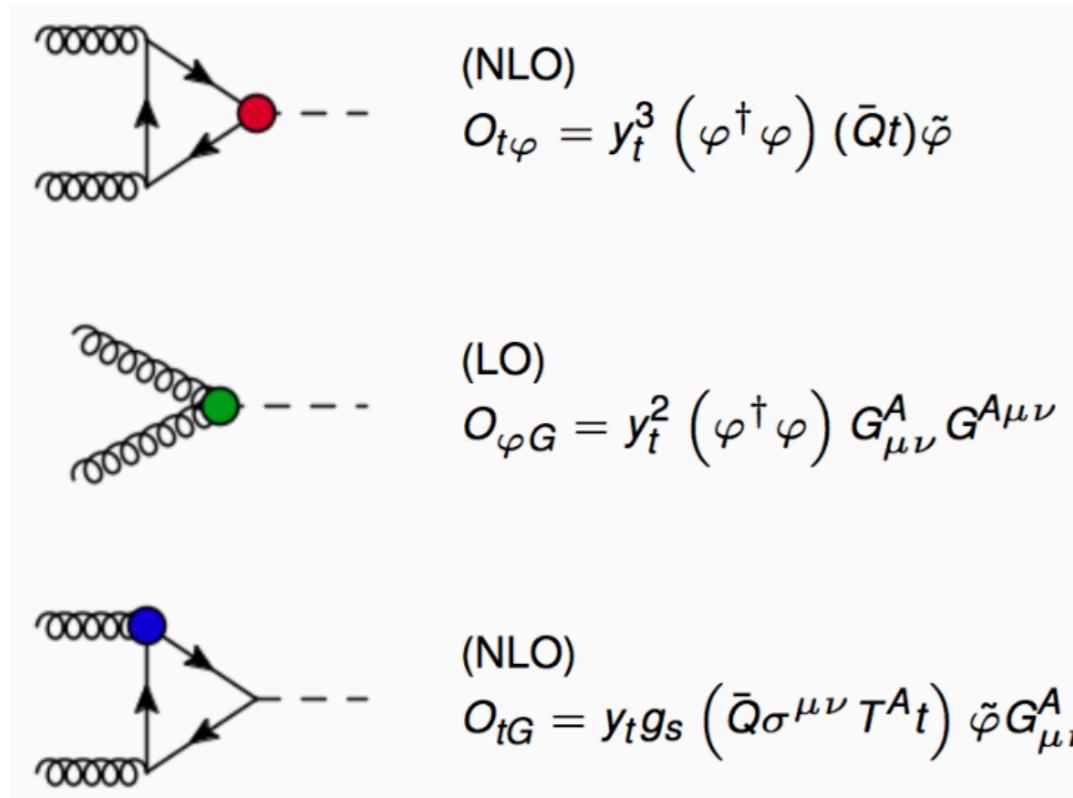
Earlier studies of ggH in the SMEFT [\[Degrande et al. 12\]](#) [\[Grojean et al. 13\]](#)

More recently, [\[Grazzini, Ilnicka, Spira, Wiesemann,16\]](#)



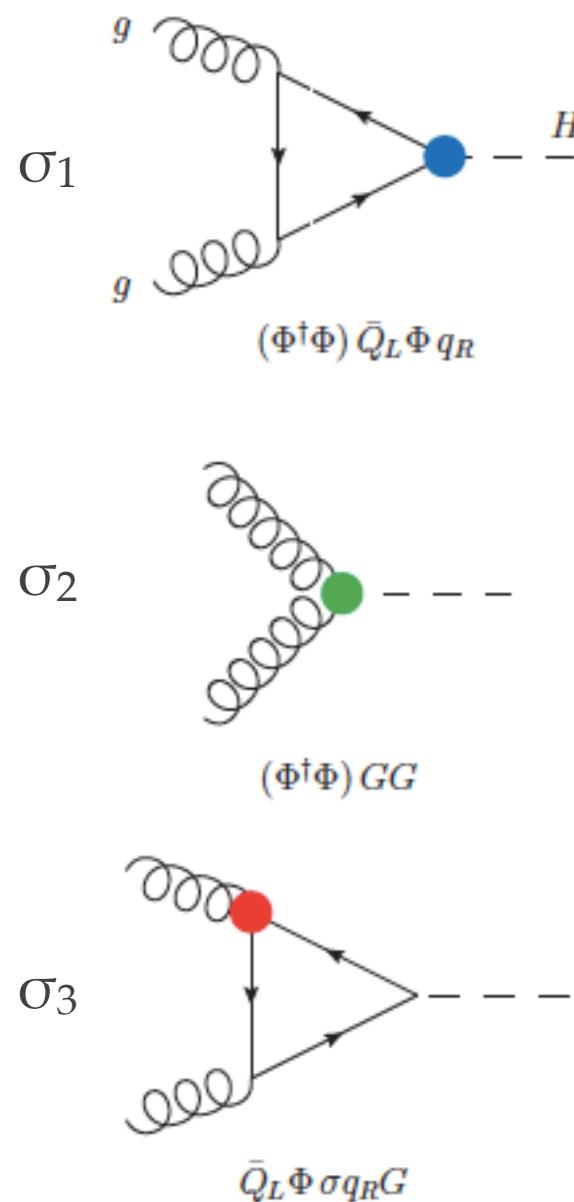
[\[Deutschmann, Duhr, FM, Vryonidou, 17\]](#)

ggH at NLO



- Scale dependence of (LO) $O_{\varphi G}$, from running coef., cancels that of (NLO) O_{tG} , from the loop.
 - Only global point of view could make sense. To estimate TH uncertainty, must sum all operators.
- $C_{tG} = 1, C_{t\varphi} = C_{\varphi G} = 0$ at m_t

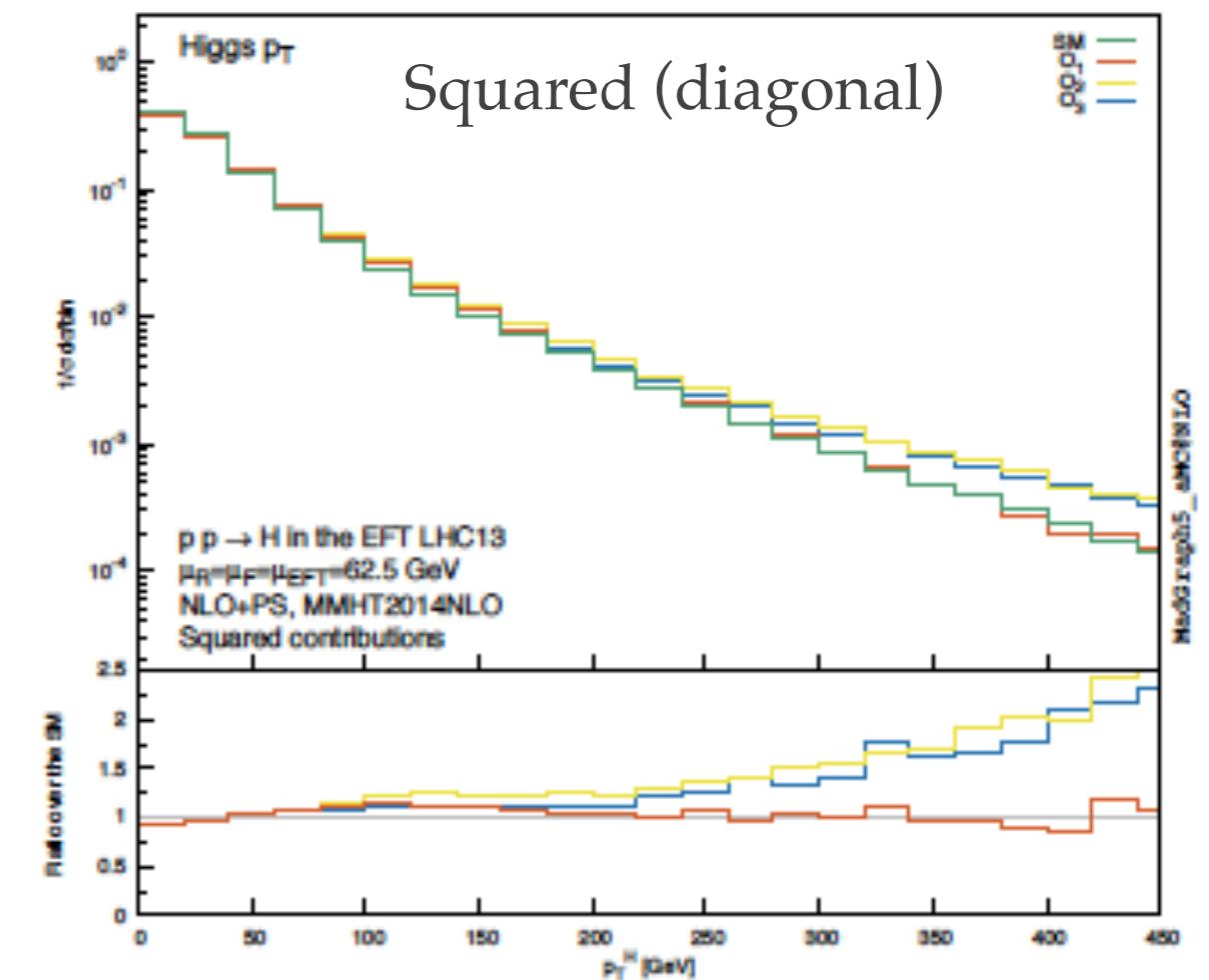
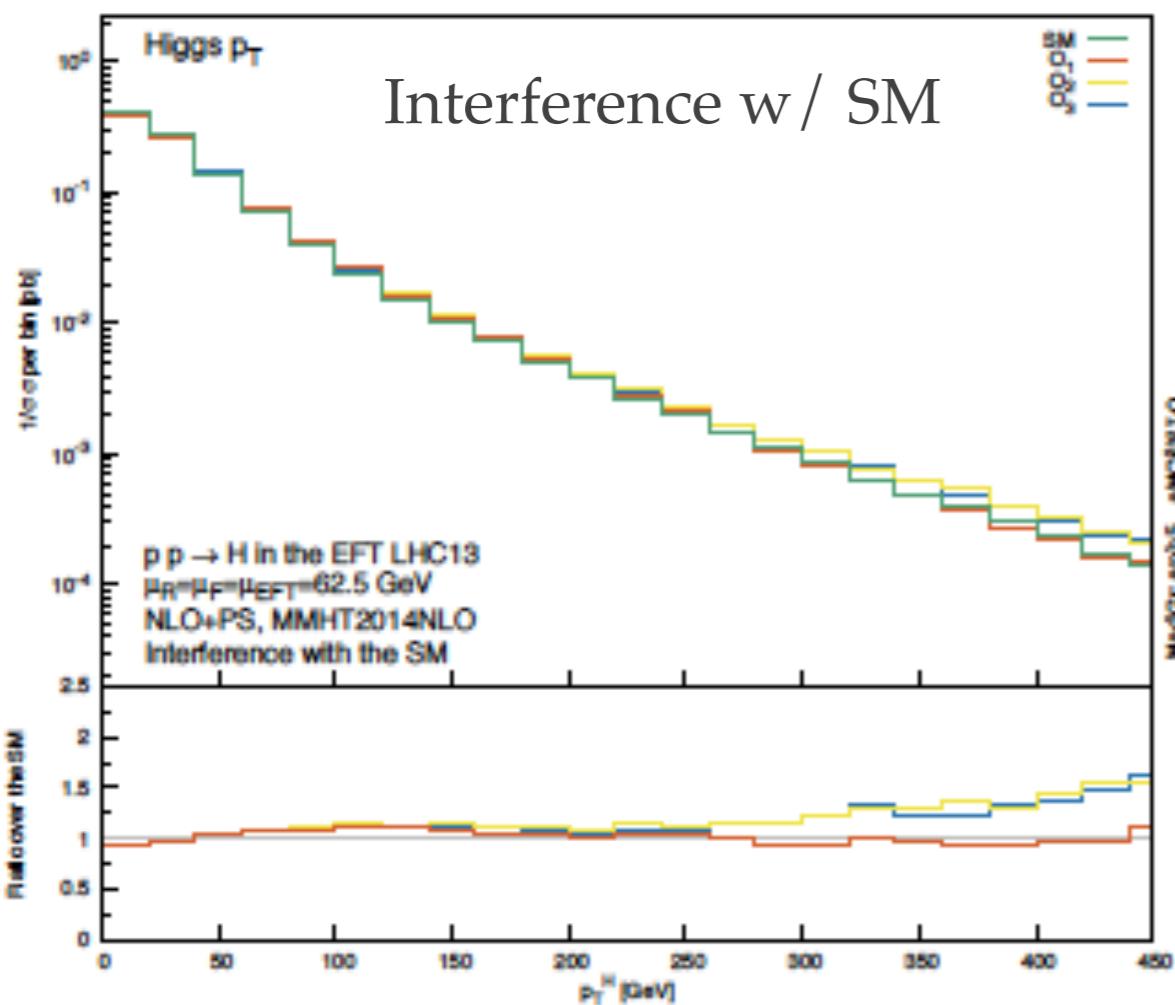
ggH at NLO



| | 13 TeV | σ LO | σ/σ_{SM} LO | σ NLO | σ/σ_{SM} NLO | K |
|---------------|--------|-------------------------------------|-------------------------|-------------------------------------|--------------------------|------|
| σ_{SM} | | $21.3^{+34.0+1.5\%}_{-25.0-1.5\%}$ | 1.0 | $36.6^{+26.4+1.9\%}_{-20.0-1.6\%}$ | 1.0 | 1.71 |
| σ_1 | | $-2.93^{+34.0+1.5\%}_{-25.0-1.5\%}$ | -0.138 | $-4.70^{+24.8+1.9\%}_{-20.0-1.6\%}$ | -0.127 | 1.61 |
| σ_2 | | $2660^{+34.0+1.5\%}_{-25.0-1.5\%}$ | 125 | $4130^{+23.9+1.9\%}_{-19.6-1.6\%}$ | 114 | 1.55 |
| σ_3 | | $50.5^{+34.0+1.5\%}_{-25.0-1.5\%}$ | 2.38 | $83.5^{+26.0+1.9\%}_{-20.6-1.6\%}$ | 2.28 | 1.65 |

$$\sigma = \sigma_{SM} + \sum_i \frac{1 \text{TeV}^2}{\Lambda^2} C_i \sigma_i + \sum_{i \leq j} \frac{1 \text{TeV}^4}{\Lambda^4} C_i C_j \sigma_{ij}$$

ggH at NLO



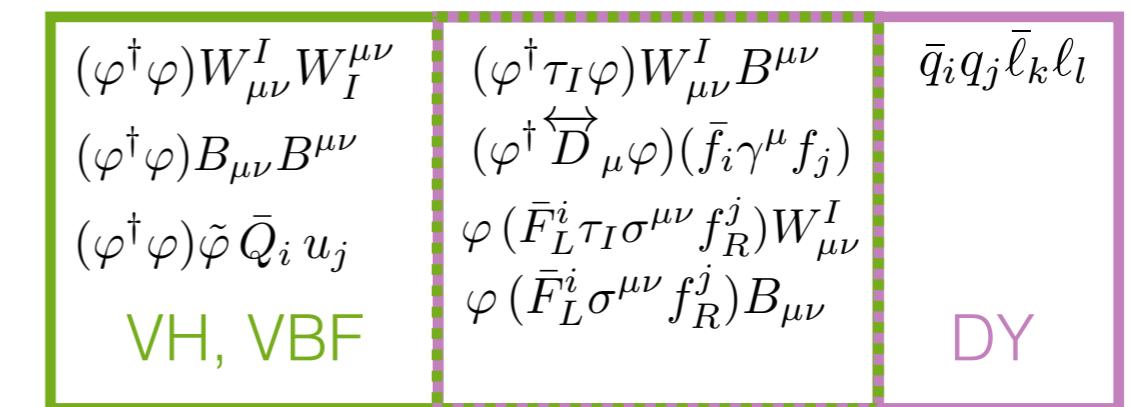
The effects of the chromo are “degenerate” with those of the $O_{\phi}G$ operator in the interference and diagonal squared terms.

VH, VBF, DY at NLO

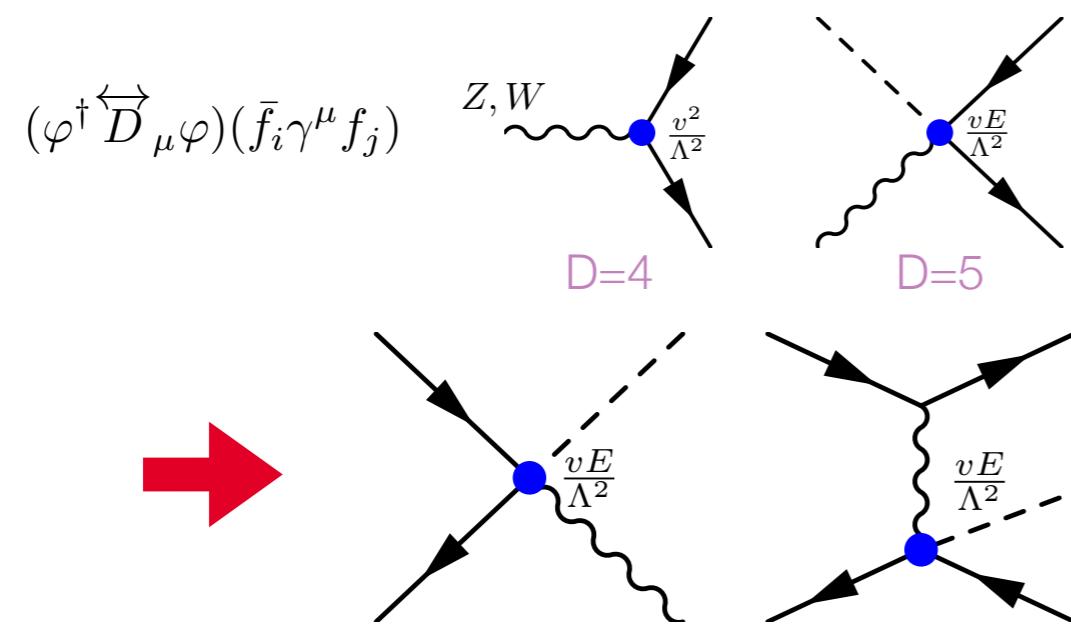
Most operators don't run under QCD

- Only Yukawa and scalar 4F
- Mostly SM counterterms

[Alioli et al.; JHEP 08 (2018) 205]
<http://powhegbox.mib.infn.it>



Current operators interesting



| | $pp \rightarrow \ell\nu$ | $pp \rightarrow \ell^+\ell^-, \nu\bar{\nu}$ | WH | ZH | VBF |
|---|--------------------------|---|----|----|-----|
| $C_{\varphi W}, C_{\varphi \bar{W}}$ | – | – | ✓ | ✓ | ✓ |
| $C_{\varphi B}, C_{\varphi \bar{B}}$ | – | – | – | ✓ | ✓ |
| $C_{\varphi WB}, C_{\varphi \bar{W} \bar{B}}$ | – | – | – | ✓ | ✓ |
| $\Gamma_{\gamma}^{u,d}$ | ✓ | ✓ | – | ✓ | ✓ |
| $\Gamma_W^{u,d}$ | ✓ | ✓ | ✓ | ✓ | ✓ |
| $\Gamma_{\gamma, W}^e$ | ✓ | ✓ | ✗ | ✗ | – |
| $c_{Q\varphi,U}, c_{Q\varphi,D}$ | ✓ | ✓ | ✓ | ✓ | ✓ |
| $c_{U\varphi}, c_{D\varphi}$ | – | ✓ | – | ✓ | ✓ |
| ξ | ✓ | – | ✓ | – | ✓ |
| $c_{L\varphi}^{(1,3)}, c_{e\varphi}$ | ✗ | ✗ | ✗ | ✗ | – |
| Y'_u, Y'_d | – | – | ✓ | ✓ | – |
| $C_{LQ,U}, C_{LQ,D}$ | ✓ | ✓ | – | – | – |
| C_{eu}, C_{ed} | – | ✓ | – | – | – |
| $C_{Lu}, C_{Ld,Qu}$ | – | ✓ | – | – | – |
| $C_{LeQd}, C_{LeQu}^{(1,3)}$ | ✓ | ✓ | – | – | – |

VH, VBF, DY at NLO

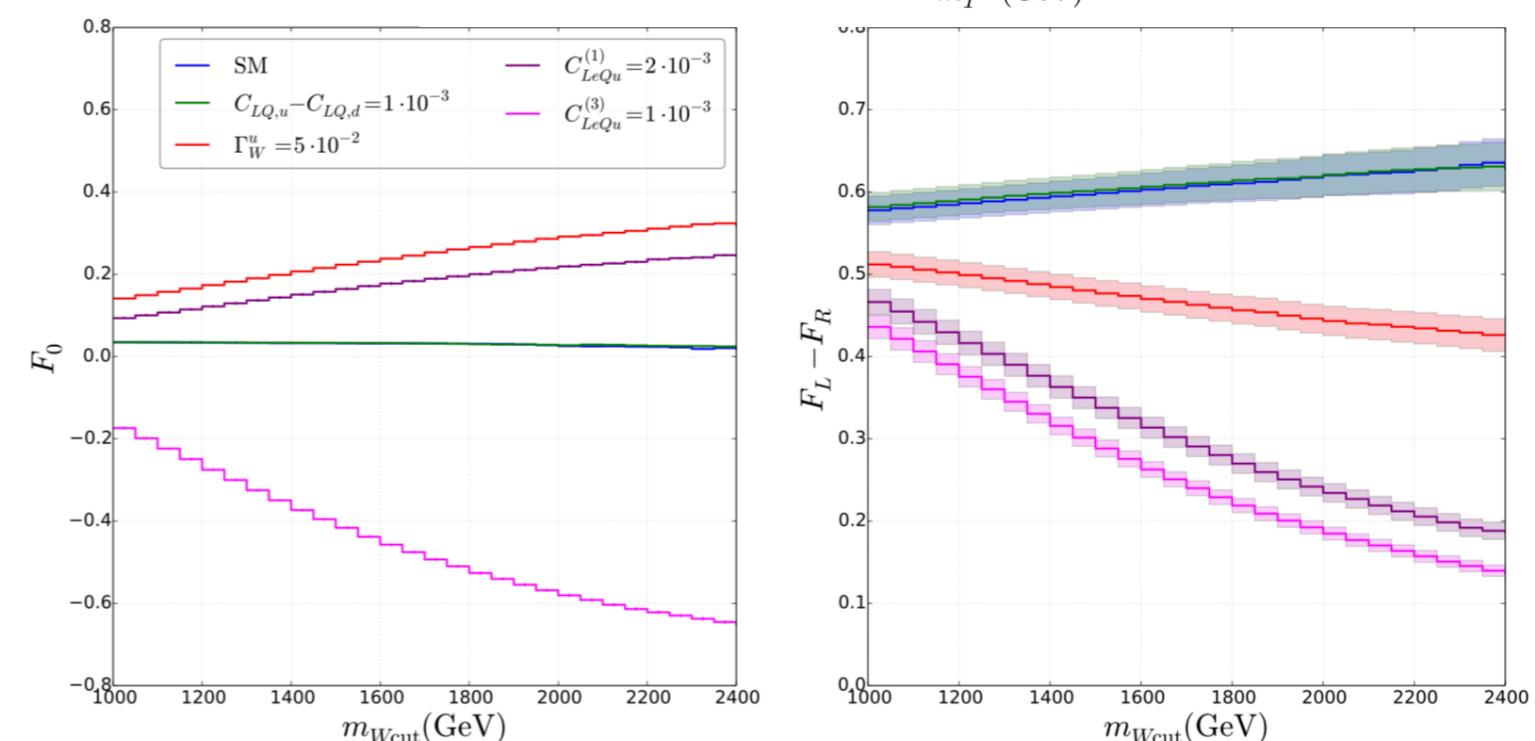
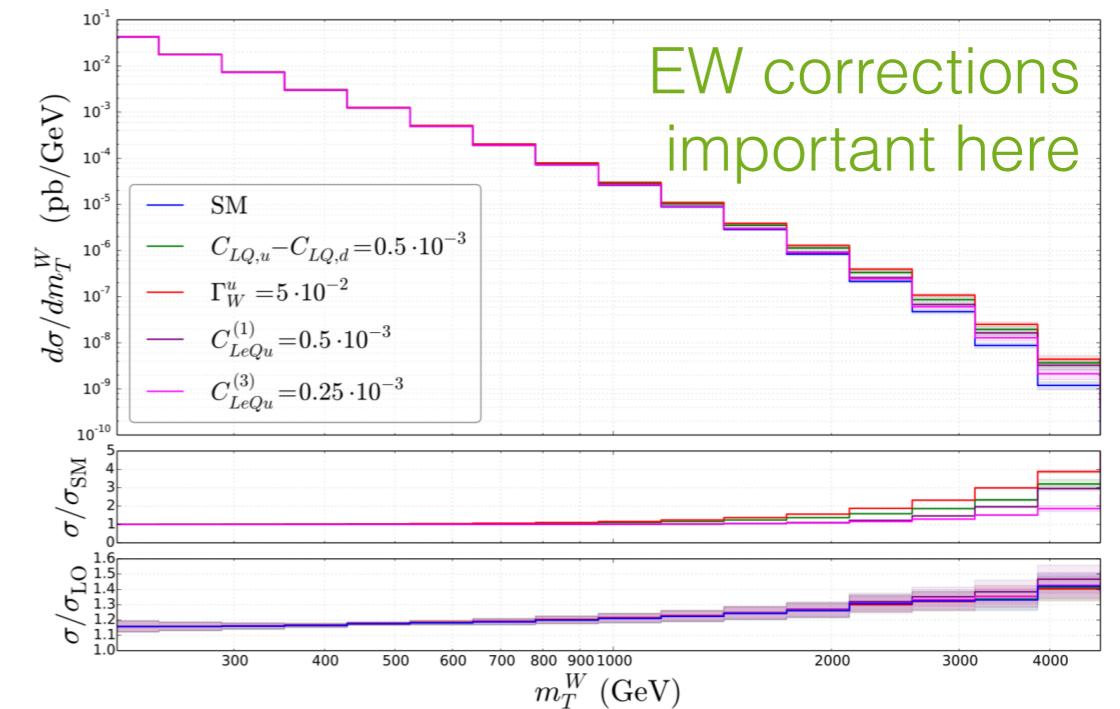
Drell-Yan

- Large effects in high energy tails, saturating existing limits
- K-factors increase with energy ~ 1.4
- Dominated by PDF uncertainty
- Set limits by recasting high mass NC & CC measurements

[ATLAS; EPJ C78 (2018) no.5 401
& JHEP 10 (2017) 182]

(pseudo)scalar & tensor 4F
limits competitive with pion &
 β -decays

W-helicity fractions
(challenging measurement)
can distinguish operators

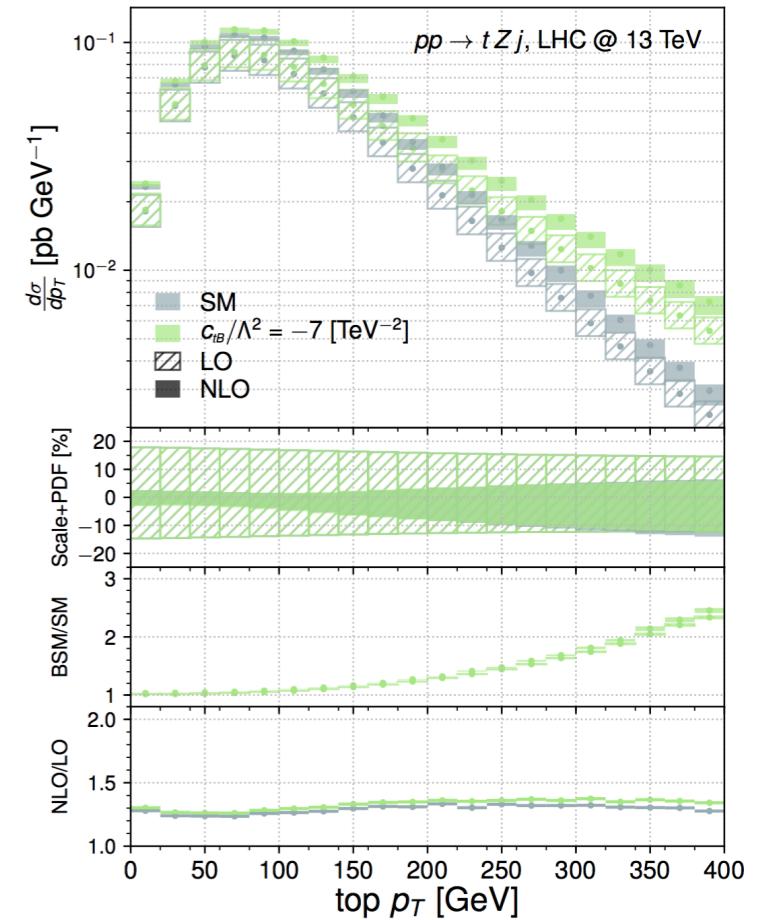
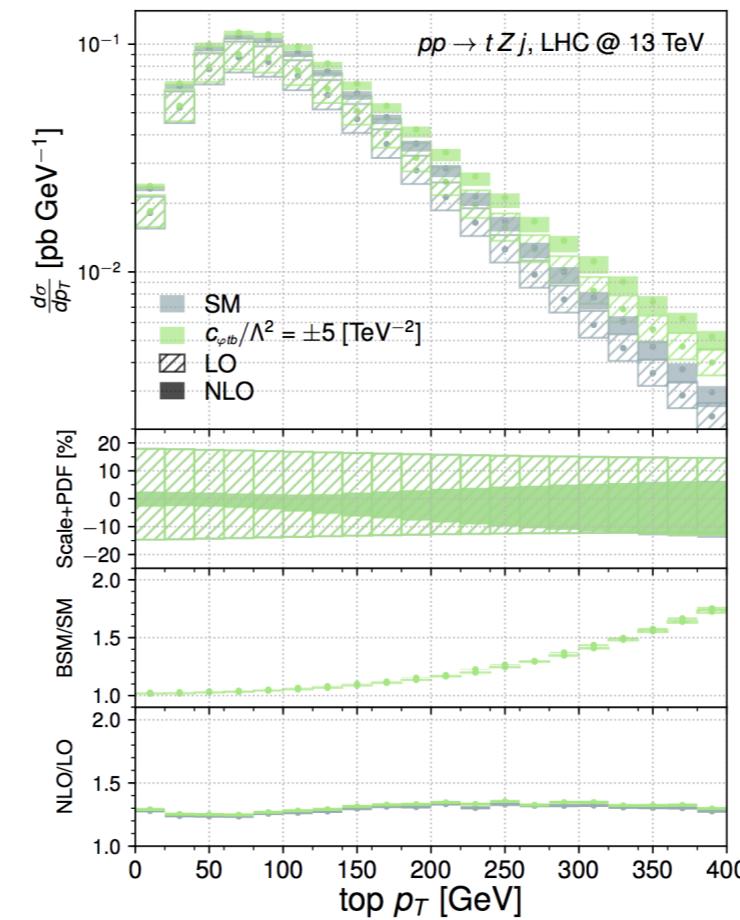
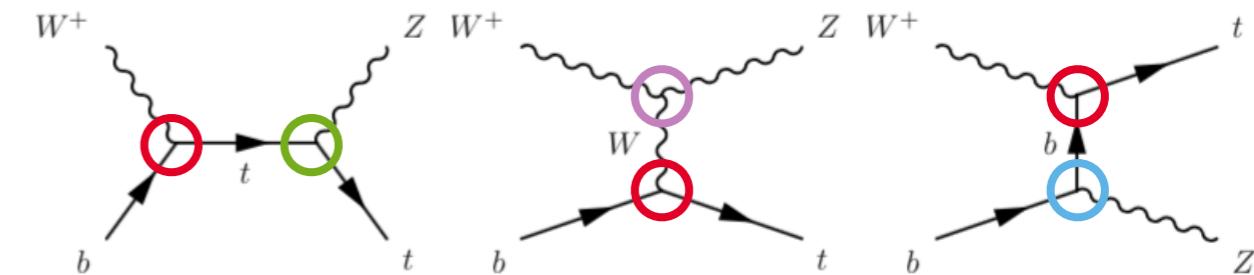


tZj/tHj

SMEFT@NLO

- tZj/tHj: case study of EW-top scattering
- Interplay of many top/higgs/EW couplings
- Energy growth from new Lorentz structures & unitarity **non-cancellations**

$$\begin{aligned}
 i(\tilde{\varphi} D_\mu \varphi)(\bar{t} \gamma^\mu b) + \text{h.c.} &\rightarrow G^0 \partial_\mu G^+ \bar{t}_R \gamma^\mu b_R \\
 i(\varphi^\dagger \overset{\leftrightarrow}{D}_\mu \tau_I \varphi)(\bar{Q} \gamma^\mu \tau^I Q) &\rightarrow G^0 \overset{\leftrightarrow}{\partial}_\mu G^+ \bar{t}_L \gamma^\mu b_L
 \end{aligned}$$



tZj/tHj

| σ [fb] | LO | NLO | K-factor |
|---|--|---|----------|
| σ_{SM} | $660.8(4)^{+13.7\%}_{-9.6\%} \pm 9.7\%$ | $839.1(5)^{+1.1\%}_{-5.1\%} \pm 1.0\%$ | 1.27 |
| σ_w | $-7.87(7)^{+8.4\%}_{-12.6\%} \pm 9.7\%$ | $-8.77(8)^{+8.5\%}_{-4.3\%} \pm 1.1\%$ | 1.12 |
| $\sigma_{w,w}$ | $34.58(3)^{+8.2\%}_{-3.9\%} \pm 13.0\%$ | $43.80(4)^{+6.6\%}_{-15.1\%} \pm 2.8\%$ | 1.27 |
| σ_{tB} | $2.23(2)^{+14.7[0.9]\%}_{-10.7[1.0]\%} \pm 9.4\%$ | $2.94(2)^{+2.3[0.4]\%}_{-3.0[0.7]\%} \pm 1.1\%$ | 1.32 |
| $\sigma_{tB,tB}$ | $2.833(2)^{+10.5[1.7]\%}_{-6.3[1.9]\%} \pm 11.1\%$ | $4.155(3)^{+4.7[0.9]\%}_{-10.1[1.4]\%} \pm 1.7\%$ | 1.47 |
| σ_{tW} | $2.66(4)^{+18.8[0.9]\%}_{-15.3[1.0]\%} \pm 11.4\%$ | $13.0(1)^{+15.8[2.1]\%}_{-22.8[0.0]\%} \pm 1.2\%$ | 4.90 |
| $\sigma_{tW,tW}$ | $48.16(4)^{+10.0[1.7]\%}_{-5.8[1.9]\%} \pm 11.3\%$ | $80.00(4)^{+7.9[1.3]\%}_{-14.7[1.6]\%} \pm 1.9\%$ | 1.66 |
| $\sigma_{\varphi dtR}$ | $4.20(1)^{+14.9\%}_{-10.9\%} \pm 9.3\%$ | $4.94(2)^{+3.4\%}_{-6.7\%} \pm 1.0\%$ | 1.18 |
| $\sigma_{\varphi dtR, \varphi dtR}$ | $0.3326(3)^{+13.6\%}_{-9.5\%} \pm 9.6\%$ | $0.4402(5)^{+3.7\%}_{-9.3\%} \pm 1.0\%$ | 1.32 |
| $\sigma_{\varphi Q}$ | $14.98(2)^{+14.5\%}_{-10.5\%} \pm 9.4\%$ | $18.07(3)^{+2.3\%}_{-1.6\%} \pm 1.0\%$ | 1.21 |
| $\sigma_{\varphi Q, \varphi Q}$ | $0.7442(7)^{+14.1\%}_{-10.0\%} \pm 9.5\%$ | $1.028(1)^{+2.8\%}_{-7.3\%} \pm 1.0\%$ | 1.38 |
| $\sigma_{\varphi Q^{(3)}}$ | $130.04(8)^{+13.8\%}_{-9.8\%} \pm 9.5\%$ | $161.4(1)^{+0.9\%}_{-4.8\%} \pm 1.0\%$ | 1.24 |
| $\sigma_{\varphi Q^{(3)}, \varphi Q^{(3)}}$ | $17.82(2)^{+11.7\%}_{-7.5\%} \pm 10.5\%$ | $23.98(2)^{+3.7\%}_{-9.3\%} \pm 1.4\%$ | 1.35 |
| $\sigma_{\varphi tb}$ | 0 | 0 | — |
| $\sigma_{\varphi tb, \varphi tb}$ | $2.949(2)^{+10.5\%}_{-6.2\%} \pm 11.1\%$ | $4.154(4)^{+5.1\%}_{-11.2\%} \pm 1.8\%$ | 1.41 |
| σ_{HW} | $-5.16(6)^{+7.8\%}_{-12.0\%} \pm 10.5\%$ | $-6.88(8)^{+6.4\%}_{-2.0\%} \pm 1.4\%$ | 1.33 |
| $\sigma_{HW,HW}$ | $0.912(2)^{+9.4\%}_{-5.2\%} \pm 12.0\%$ | $1.048(2)^{+5.2\%}_{-12.8\%} \pm 2.1\%$ | 1.15 |
| σ_{HB} | $-3.015(9)^{+9.9\%}_{-13.9\%} \pm 9.5\%$ | $-3.76(1)^{+5.2\%}_{-1.0\%} \pm 1.0\%$ | 1.25 |
| $\sigma_{HB,HB}$ | $0.02324(6)^{+12.7\%}_{-8.5\%} \pm 9.9\%$ | $0.02893(6)^{+2.3\%}_{-7.5\%} \pm 1.1\%$ | 1.24 |
| σ_{tG} | $0.45(2)^{+93.0\%}_{-148.8\%} \pm 4.9\%$ | — | |
| $\sigma_{tG,tG}$ | $2.251(4)^{+20.9\%}_{-30.0\%} \pm 2.5\%$ | — | |
| $\sigma_{Qq^{(3,1)}}$ | $-393.5(5)^{+8.1\%}_{-12.3\%} \pm 10.0\%$ | $-498(1)^{+8.9\%}_{-3.2\%} \pm 1.2\%$ | 1.26 |
| $\sigma_{Qq^{(3,1)}, Qq^{(3,1)}}$ | $462.25(3)^{+8.4\%}_{-4.1\%} \pm 12.7\%$ | $545.50(5)^{+7.4\%}_{-17.4\%} \pm 2.9\%$ | 1.18 |
| $\sigma_{Qq^{(3,8)}}$ | 0 | $-0.9(3)^{+23.3\%}_{-26.3\%} \pm 19.2\%$ | — |
| $\sigma_{Qq^{(3,8)}, Qq^{(3,8)}}$ | $102.73(5)^{+8.4\%}_{-4.1\%} \pm 12.7\%$ | $111.18(5)^{+9.3\%}_{-18.4\%} \pm 2.8\%$ | 1.08 |

← tZj

Useful inputs to global interpretations

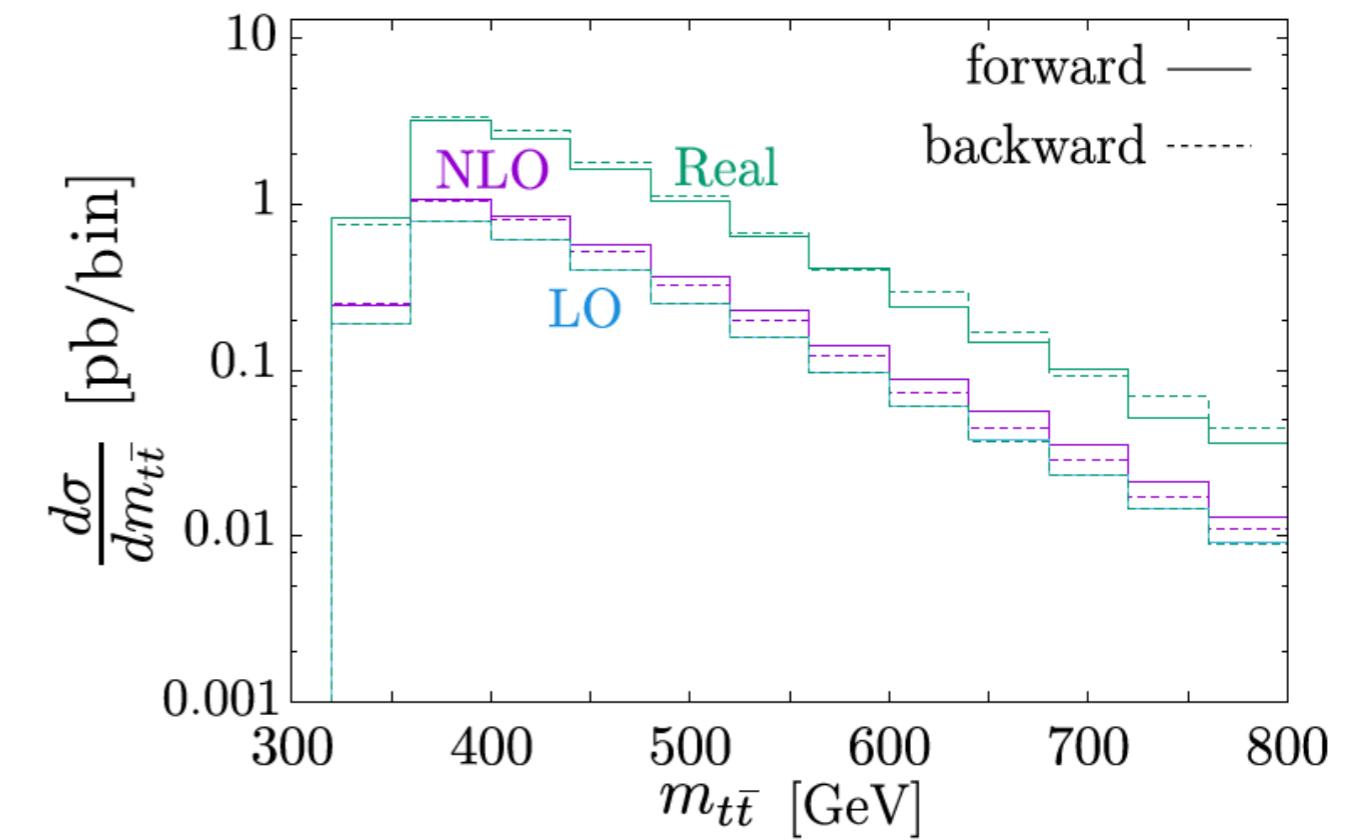
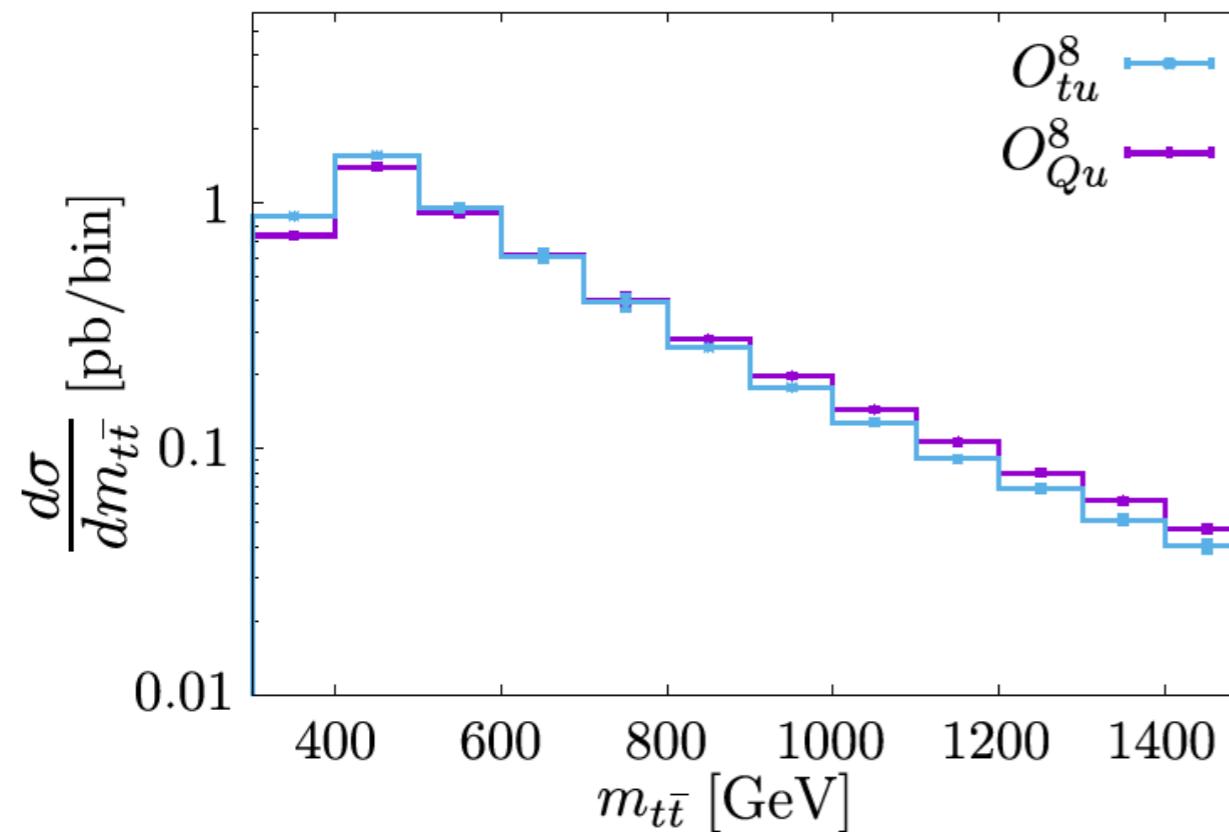
tHj ↓

| σ [fb] | LO | NLO | K-factor | |
|---|---|---|---|------|
| σ_{SM} | $57.56(4)^{+11.2\%}_{-7.4\%} \pm 10.2\%$ | $75.87(4)^{+2.2\%}_{-6.4\%} \pm 1.2\%$ | 1.32 | |
| $\sigma_{\varphi w}$ | $8.12(2)^{+13.1\%}_{-9.3\%} \pm 9.3\%$ | $7.76(2)^{+7.0\%}_{-6.3\%} \pm 1.0\%$ | 0.96 | |
| $\sigma_{\varphi w, \varphi w}$ | $5.212(7)^{+10.6\%}_{-6.8\%} \pm 10.2\%$ | $6.263(7)^{+2.6\%}_{-7.8\%} \pm 1.3\%$ | 1.20 | |
| $\sigma_{t\varphi}$ | $-1.203(6)^{+12.0\%}_{-15.6\%} \pm 8.9\%$ | $-0.246(6)^{+144.5[31.4]\%}_{-157.8[19.0]\%} \pm 2.1\%$ | 0.20 | |
| $\sigma_{t\varphi, t\varphi}$ | $0.6682(9)^{+12.7\%}_{-8.9\%} \pm 9.6\%$ | $0.7306(8)^{+4.6[0.6]\%}_{-7.3[0.2]\%} \pm 1.0\%$ | 1.09 | |
| σ_{tW} | $19.38(6)^{+13.0\%}_{-9.3\%} \pm 9.4\%$ | $22.18(6)^{+3.8[0.4]\%}_{-6.8[0.9]\%} \pm 1.0\%$ | 1.14 | |
| $\sigma_{tW, tW}$ | $46.40(8)^{+9.3\%}_{-5.5\%} \pm 11.1\%$ | $71.24(8)^{+7.4[1.5]\%}_{-14.0[6.9]\%} \pm 1.9\%$ | 1.54 | |
| $\sigma_{\varphi Q^{(3)}}$ | $-3.03(3)^{+0.0\%}_{-2.2\%} \pm 15.4\%$ | $-10.04(4)^{+11.1\%}_{-8.9\%} \pm 1.8\%$ | 3.31 | |
| $\sigma_{\varphi Q^{(3)}, \varphi Q^{(3)}}$ | $11.23(2)^{+9.4\%}_{-5.6\%} \pm 11.2\%$ | $15.28(2)^{+5.0\%}_{-10.9\%} \pm 1.8\%$ | 1.36 | |
| $\sigma_{\varphi tb}$ | 0 | 0 | — | |
| $\sigma_{\varphi tb, \varphi tb}$ | $2.752(4)^{+9.4\%}_{-5.5\%} \pm 11.3\%$ | $3.768(4)^{+5.0\%}_{-10.9\%} \pm 1.8\%$ | 1.54 | |
| σ_{HW} | $-3.526(4)^{+5.6\%}_{-9.5\%} \pm 10.9\%$ | $-5.27(1)^{+6.5\%}_{-2.9\%} \pm 1.5\%$ | 1.50 | |
| $\sigma_{HW,HW}$ | $0.9356(4)^{+7.9\%}_{-4.0\%} \pm 12.3\%$ | $1.058(1)^{+4.8\%}_{-11.9\%} \pm 2.3\%$ | 1.13 | |
| σ_{tG} | | $-0.418(5)^{+12.3\%}_{-9.8\%} \pm 1.1\%$ | — | |
| $\sigma_{tG, tG}$ | | $1.413(1)^{+21.3\%}_{-30.6\%} \pm 2.5\%$ | — | |
| $\sigma_{Qq^{(3,1)}}$ | | $-22.50(5)^{+8.0\%}_{-11.8\%} \pm 9.7\%$ | $-20.10(5)^{+13.8\%}_{-13.3\%} \pm 1.1\%$ | 0.89 |
| $\sigma_{Qq^{(3,1)}, Qq^{(3,1)}}$ | | $69.78(3)^{+8.0\%}_{-4.1\%} \pm 12.1\%$ | $62.20(3)^{+11.5\%}_{-15.9\%} \pm 2.3\%$ | 0.89 |
| $\sigma_{Qq^{(3,8)}}$ | — | $0.25(3)^{+25.4\%}_{-27.1\%} \pm 4.7\%$ | — | |
| $\sigma_{Qq^{(3,8)}, Qq^{(3,8)}}$ | | $15.53(2)^{+8.0\%}_{-4.1\%} \pm 12.1\%$ | $14.07(2)^{+11.0\%}_{-15.7\%} \pm 2.1\%$ | 0.91 |

Breaking degeneracies: tt+jet

[Brivio et al.; JHEP 2002 (2020) 131]

Many four-fermion operators enter in ttbar production.



$$\begin{aligned} \frac{d\sigma(u\bar{u} \rightarrow t\bar{t})}{d\cos\theta_t} &\propto (1 + 2\beta_{t\bar{t}} \cos\theta_t + 4\bar{m}^2 + \beta_{t\bar{t}}^2 \cos^2\theta_t) C_{tu}^8 \\ &+ (1 - 2\beta_{t\bar{t}} \cos\theta_t + 4\bar{m}^2 + \beta_{t\bar{t}}^2 \cos^2\theta_t) C_{Qu}^8 \end{aligned}$$

forward → forward
backward → backward

Plan for today's lecture

- SMEFT essentials
- The SMEFT precision frontier
- Example: Fitting in the Top (with Higgs/EW) sector
- Bringing the lesson home

Plan for today's lecture

- SMEFT essentials
- The SMEFT precision frontier
- Example: Fitting in the Top (with Higgs/EW) sector
- Bringing the lesson home

SMEFT global fit

- Measurements:
 - Total as well as differential, unfolded and / or fiducial, including uncertainties and correlations.
 - Reference SMEFT interpretations done by the experimental collaboration for best sensitivity targets.
- Theoretical predictions:
 - SM at the best possible accuracy
 - SMEFT at least at NLO in QCD
- Fitting:
 - Robust and scalable fitting technology
 - Combination with low / energy, flavour and LEP measurements

An application: A global top fit@NLO

Theory

(N)NLO QCD+ NLO EW for SM
NLO QCD for SMEFT
State-of-the-art PDFs without top data

Data

Top pair production and single top (differential)
Associated production with W,Z,H
W helicity fractions
Parton-level

Global SMEFT fit of the top-quark sector

Based on NNPDF
Faithful uncertainty estimate
Avoid under- and over-fitting
Validated on pseudo-data (closure test)

Fit results can be used to bound
specific UV complete models
New data can be straightforwardly added
Plan to extend to Higgs, gauge sector etc

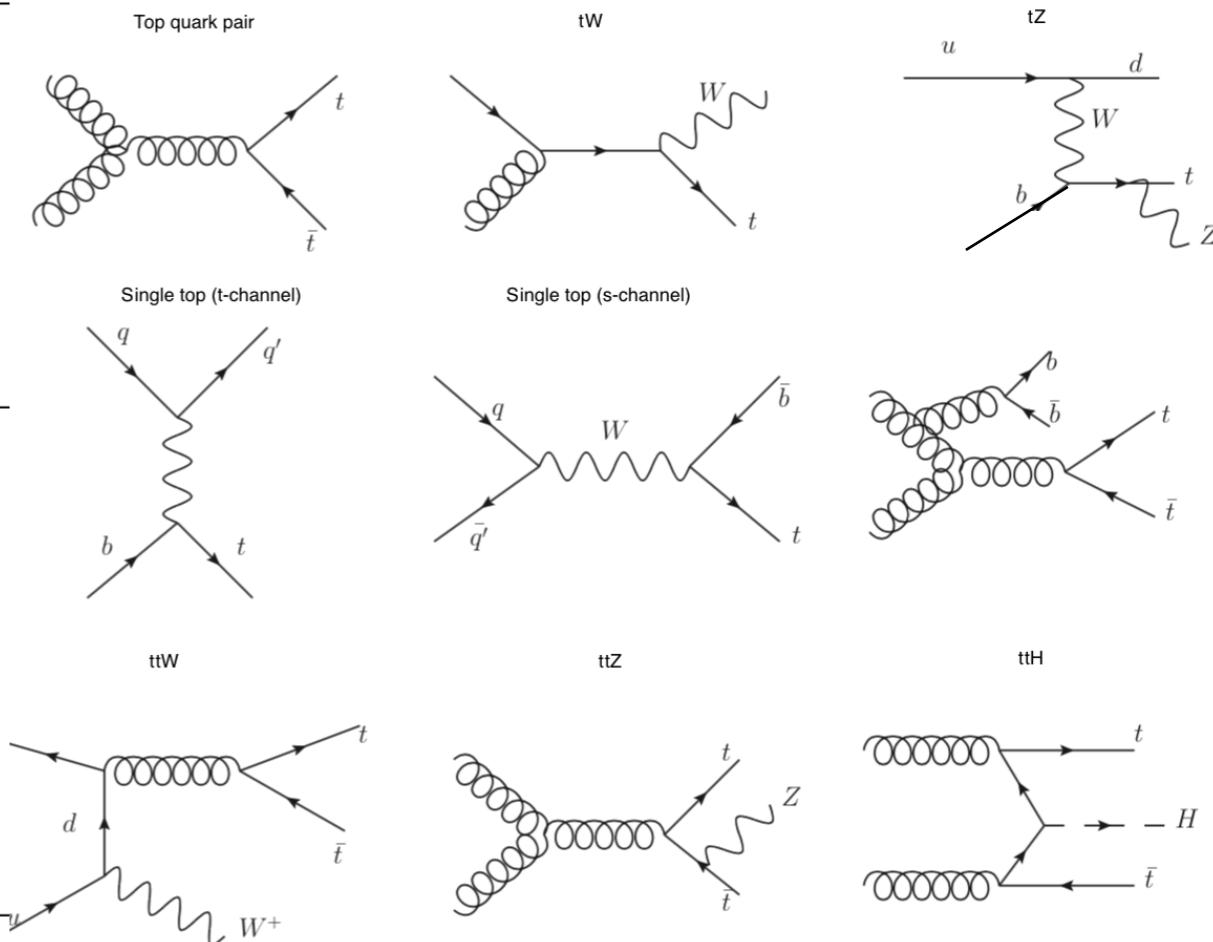
Methodology

Output

An application: A global top fit@NLO

| Class | Notation | Degree of Freedom | Operator Definition |
|----------------------|----------|-------------------|--|
| QQQQ | 0QQ1 | c_{QQ}^1 | $2C_{qq}^{1(3333)} - \frac{2}{3}C_{qq}^{3(3333)}$ |
| | 0QQ8 | c_{QQ}^8 | $8C_{qq}^{3(3333)}$ |
| | 0Qt1 | c_{Qt}^1 | $C_{qu}^{1(3333)}$ |
| | 0Qt8 | c_{Qt}^8 | $C_{qu}^{8(3333)}$ |
| | 0Qb1 | c_{Qb}^1 | $C_{qd}^{1(3333)}$ |
| | 0Qb8 | c_{Qb}^8 | $C_{qd}^{8(3333)}$ |
| | 0tt1 | c_{tt}^1 | $C_{uu}^{(3333)}$ |
| | 0tb1 | c_{tb}^1 | $C_{ud}^{1(3333)}$ |
| | 0tb8 | c_{tb}^8 | $C_{ud}^{8(3333)}$ |
| | 0QtQb1 | c_{QtQb}^1 | $C_{qud}^{1(3333)}$ |
| | 0QtQb8 | c_{QtQb}^8 | $C_{qud}^{8(3333)}$ |
| QQqq | 081qq | $c_{Qq}^{1,8}$ | $C_{qq}^{1(4334)} + 3C_{qq}^{3(4334)}$ |
| | 011qq | $c_{Qq}^{1,1}$ | $C_{qq}^{1(4334)} + \frac{1}{6}C_{qq}^{1(4334)} + \frac{1}{2}C_{qq}^{3(4334)}$ |
| | 083qq | $c_{Qq}^{3,8}$ | $C_{qq}^{1(4334)} - C_{qq}^{3(4334)}$ |
| | 013qq | $c_{Qq}^{3,1}$ | $C_{qq}^{3(4334)} + \frac{1}{6}(C_{qq}^{1(4334)} - C_{qq}^{3(4334)})$ |
| | 08qt | c_{tq}^8 | $C_{qu}^{8(4334)}$ |
| | 01qt | c_{tq}^1 | $C_{qu}^{1(4334)}$ |
| | 08ut | c_{tu}^8 | $2C_{uu}^{(4334)}$ |
| | 01ut | c_{tu}^1 | $C_{uu}^{(4334)} + \frac{1}{3}C_{uu}^{(4334)}$ |
| | 08qu | c_{Qu}^8 | $C_{qu}^{(4334)}$ |
| | 01qu | c_{Qu}^1 | $C_{qu}^{1(4334)}$ |
| | 08dt | c_{td}^8 | $C_{ud}^{(4334)}$ |
| | 01dt | c_{td}^1 | $C_{ud}^{1(4334)}$ |
| | 08qd | c_{Qd}^8 | $C_{qd}^{(4334)}$ |
| | 01qd | c_{Qd}^1 | $C_{qd}^{1(4334)}$ |
| QQ + V, G, φ | 0tG | c_{tG} | $\text{Re}\{C_{uG}^{(33)}\}$ |
| | 0tW | c_{tW} | $\text{Re}\{C_{uW}^{(33)}\}$ |
| | 0bW | c_{bW} | $\text{Re}\{C_{dW}^{(33)}\}$ |
| | 0tZ | c_{tZ} | $\text{Re}\{-s_W C_{uB}^{(33)} + c_W C_{uW}^{(33)}\}$ |
| | 0ff | c_{ptb} | $\text{Re}\{C_{\varphi ud}^{(33)}\}$ |
| | 0fq3 | $c_{\varphi Q}^3$ | $C_{\varphi Q}^{3(33)}$ |
| | 0pQM | $c_{\varphi Q}^-$ | $C_{\varphi Q}^{1(33)} - C_{\varphi Q}^{3(33)}$ |
| | 0pt | c_{pt} | $C_{\varphi u}^{(33)}$ |
| | 0tp | $c_{t\varphi}$ | $\text{Re}\{C_{u\varphi}^{(33)}\}$ |

| Sensitivity at $\mathcal{O}(\Lambda^{-2})$ ($\mathcal{O}(\Lambda^{-4})$) | | | | | | | | |
|--|------------|------|------|-------------|-------------|-------------|-------------|--------------------|
| $\bar{t}u$ | single-top | tW | tZ | $t\bar{t}W$ | $t\bar{t}Z$ | $t\bar{t}H$ | $t\bar{t}t$ | $t\bar{t}b\bar{b}$ |
| ✓ | | | | | | | ✓ | ✓ |



Rich phenomenology

Observables and theory predictions

Data

Top-pair production
W-helicities

4 tops, ttbb, top-pair
associated production

Single top
t-channel, s-channel,
tW, tZ

One distribution from each
dataset, to avoid double
counting

| Dataset | χ^2/n_{dat} (prior) | χ^2/n_{dat} (fit) | n_{dat} |
|---|---------------------------------|-------------------------------|------------------|
| ATLAS_tt_8TeV_1jets [$m_{t\bar{t}}$] | 1.51 | 1.25 | 7 |
| CMS_tt_8TeV_1jets [$y_{t\bar{t}}$] | 1.17 | 1.17 | 10 |
| CMS_tt2D_8TeV_dilep [$(m_{t\bar{t}}, y_t)$] | 1.38 | 1.38 | 16 |
| CMS_tt_13TeV_1jets2 [$m_{t\bar{t}}$] | 1.09 | 1.28 | 8 |
| CMS_tt_13TeV_dilep [$m_{t\bar{t}}$] | 1.34 | 1.42 | 6 |
| CMS_tt_13TeV_1jets_2016 [$m_{t\bar{t}}$] | 1.87 | 1.87 | 10 |
| ATLAS_WhelF_8TeV | 1.98 | 0.27 | 3 |
| CMS_WhelF_8TeV | 0.31 | 1.18 | 3 |
| | | | |
| CMS_ttbb_13TeV | 5.00 | 1.29 | 1 |
| CMS_tttt_13TeV | 0.05 | 0.02 | 1 |
| ATLAS_tth_13TeV | 1.61 | 0.55 | 1 |
| CMS_tth_13TeV | 0.34 | 0.01 | 1 |
| ATLAS_ttZ_8TeV | 1.32 | 5.29 | 1 |
| ATLAS_ttZ_13TeV | 0.01 | 1.06 | 1 |
| CMS_ttZ_8TeV | 0.04 | 0.06 | 1 |
| CMS_ttZ_13TeV | 0.90 | 0.67 | 1 |
| ATLAS_ttW_8TeV | 1.34 | 0.27 | 1 |
| ATLAS_ttW_13TeV | 0.82 | 0.65 | 1 |
| CMS_ttW_8TeV | 1.54 | 0.54 | 1 |
| CMS_ttW_13TeV | 0.03 | 0.09 | 1 |
| | | | |
| CMS_t_tch_8TeV_dif | 0.11 | 0.32 | 6 |
| ATLAS_t_tch_8TeV [y_t] | 0.91 | 0.43 | 4 |
| ATLAS_t_tch_8TeV [$y_{\bar{t}}$] | 0.39 | 0.45 | 4 |
| ATLAS_t_sch_8TeV | 0.08 | 1.92 | 1 |
| ATLAS_t_tch_13TeV | 0.02 | 0.09 | 2 |
| CMS_t_tch_13TeV_dif [y_t] | 0.46 | 0.49 | 4 |
| CMS_t_sch_8TeV | 1.26 | 0.76 | 1 |
| ATLAS_tW_inc_8TeV | 0.02 | 0.06 | 1 |
| CMS_tW_inc_8TeV | 0.00 | 0.07 | 1 |
| ATLAS_tW_inc_13TeV | 0.52 | 0.82 | 1 |
| CMS_tW_inc_13TeV | 4.29 | 1.68 | 1 |
| ATLAS_tZ_inc_13TeV | 0.00 | 0.00 | 1 |
| CMS_tZ_inc_13TeV | 0.66 | 0.34 | 1 |
| | | | |
| Total | 1.11 | 1.06 | 103 |

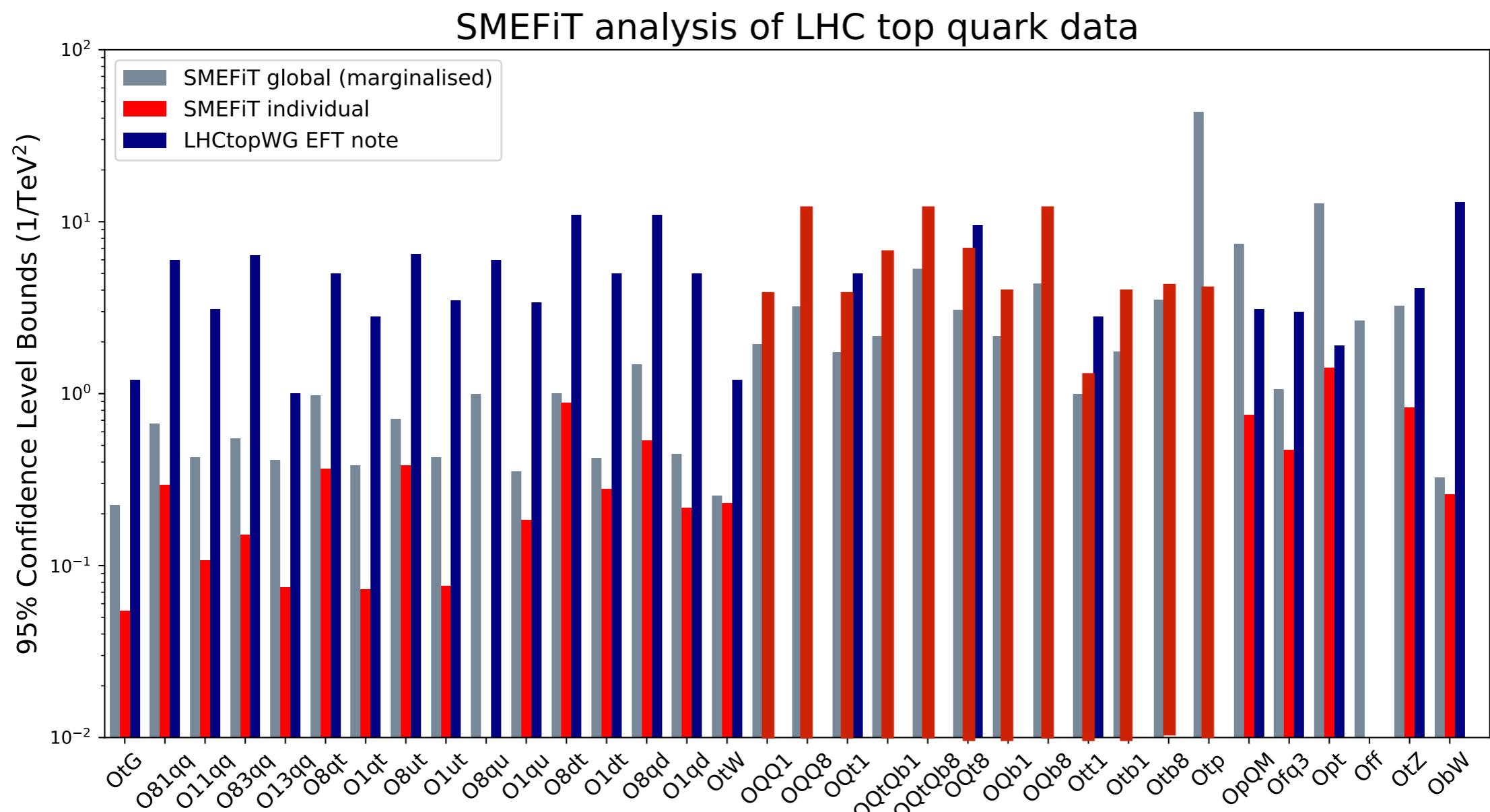
Theoretical predictions

| Process | SM | SMEFT |
|--------------------|----------|------------------------------|
| $t\bar{t}$ | NNLO QCD | NLO QCD |
| single-t (t-ch) | NNLO QCD | NLO QCD |
| single-t (s-ch) | NLO QCD | NLO QCD |
| tW | NLO QCD | NLO QCD |
| tZ | NLO QCD | LO QCD + NLO SM K-factors |
| $t\bar{t}W(Z)$ | NLO QCD | LO QCD + NLO SM K-factors |
| $t\bar{t}h$ | NLO QCD | LO QCD + NLO SM K-factors |
| $t\bar{t}t$ | NLO QCD | LO QCD + NLO SM K-factors |
| $t\bar{t}b\bar{b}$ | NLO QCD | LO QCD + NLO SM K-factors |

Baseline fit includes:

- Best available SM predictions
- NLO EFT predictions
- $O(1/\Lambda^4)$ terms

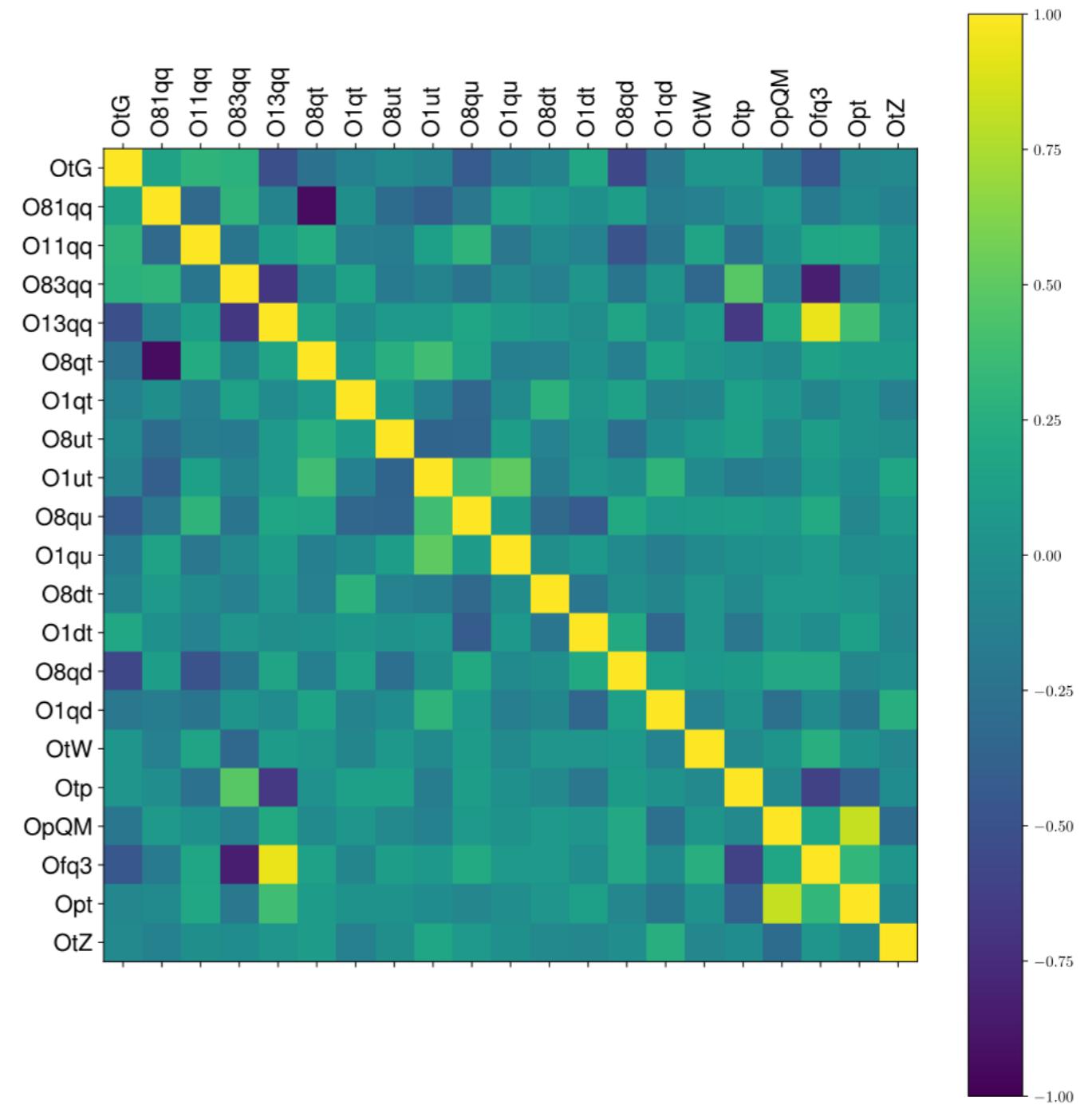
Results



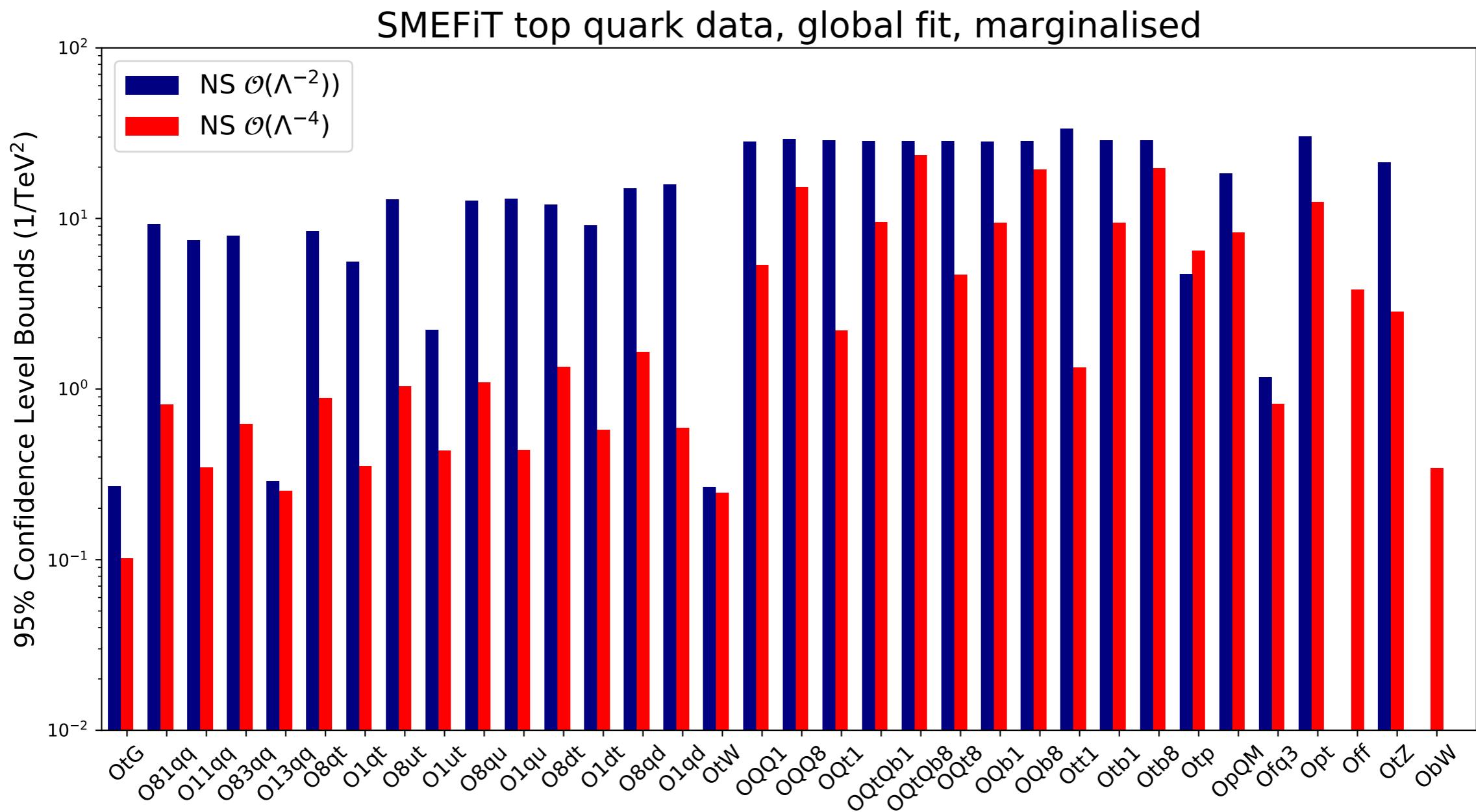
N. Hartland et. al. JHEP 1904 (2019) 100, updated

Results

- Correlations of fit parameters via color map
- Not all parameters completely independent!



Linear vs quadratic



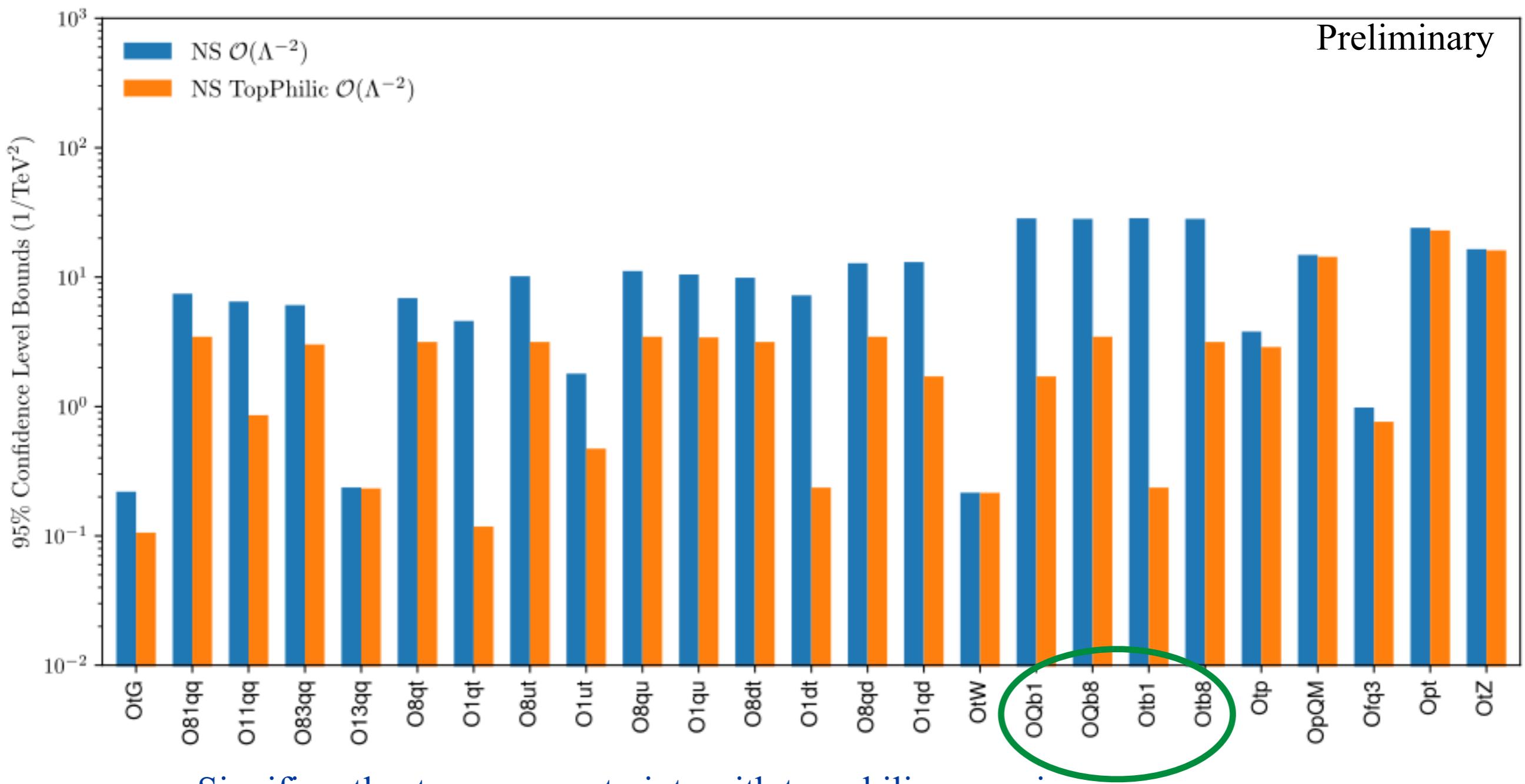
Top-philic scenario

- Same flavour symmetries as baseline scenario (MFV : $U(2)_q \times U(2)_u \times U(2)_d$)
- Assumes new physics couples more strongly to 3rd-generation LH doublet and RH up-type singlet (+ bosons)

$$\begin{aligned}
 & c_{t\varphi}^{[I]}, \quad c_{\varphi Q}^-, \quad c_{\varphi Q}^3, \quad c_{\varphi t}, \quad c_{tW}^{[I]}, \quad c_{tZ}^{[I]}, \quad c_{tG}^{[I]}, \\
 & c_{\varphi tb}^{[I]} \text{ and } c_{bW}^{[I]} \text{ appear proportional to } y_b \\
 & c_{QQ}^1, \quad c_{QQ}^8, \quad c_{Qt}^1, \quad c_{Qt}^8, \quad c_{tt}^1, \\
 & c_{QDW} = c_{Qq}^{3,1} = c_{Ql}^{3(\ell)}, \\
 & c_{QDB} = 6c_{Qq}^{1,1} = \frac{3}{2}c_{Qu}^1 = -3c_{Qd}^1 = -3c_{Qb}^1 = -2c_{Ql}^{1(\ell)} = -c_{Qe}^{(\ell)}, \\
 & c_{tDB} = 6c_{tq}^1 = \frac{3}{2}c_{tu}^1 = -3c_{td}^1 = -3c_{tb}^1 = -2c_{tl}^{(\ell)} = -c_{te}^{(\ell)}, \\
 & c_{QDG} = c_{Qq}^{1,8} = c_{Qu}^8 = c_{Qd}^8 = c_{Qb}^8, \\
 & c_{tDG} = c_{tq}^8 = c_{tu}^8 = c_{td}^8 = c_{tb}^8.
 \end{aligned}$$

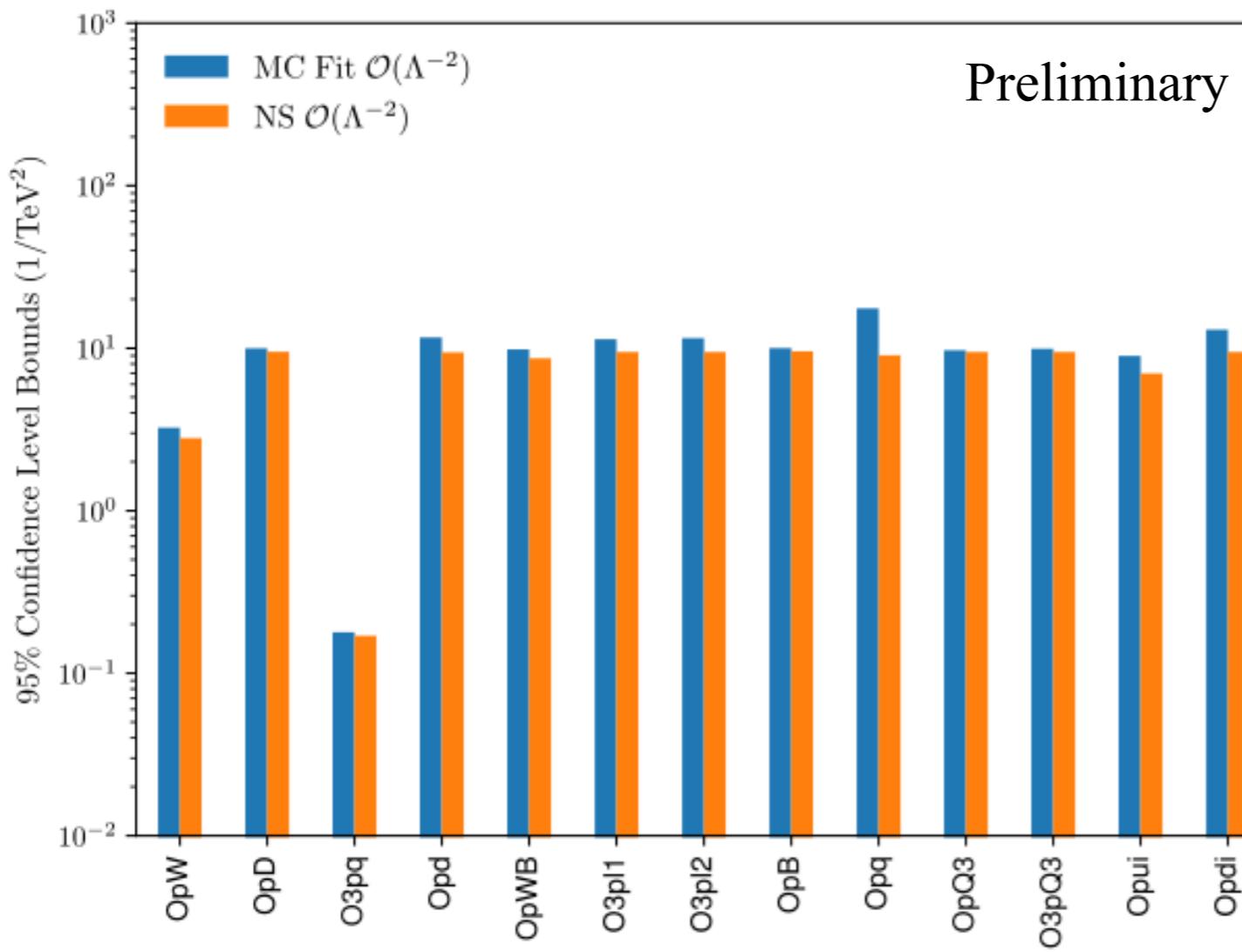
- 34 parameter basis reduced to 19 free parameters

Top-philic scenario



Adding the Higgs data

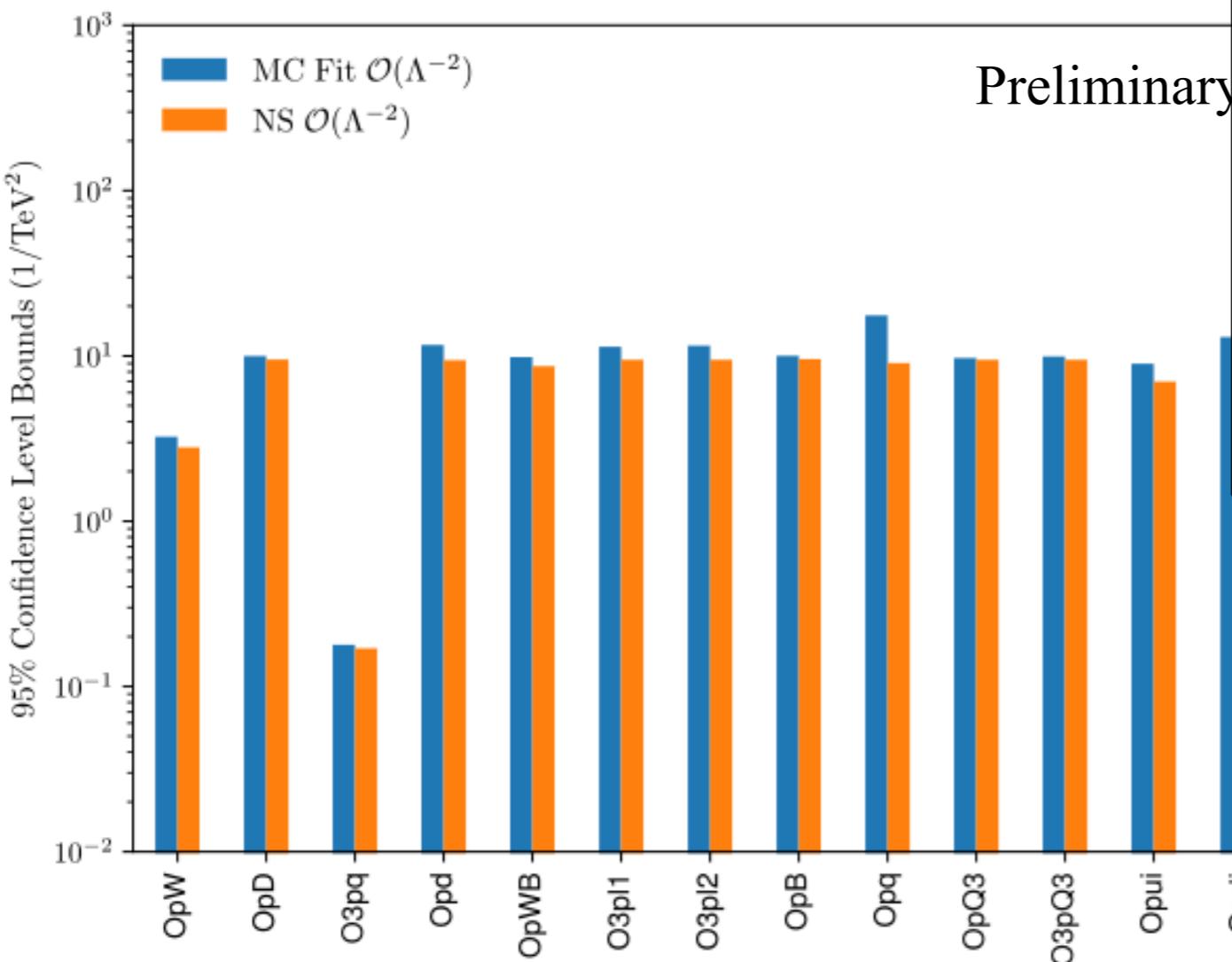
- Analysis of VH production data from ATLAS at 13 TeV
- Single dataset of 5 points
- Same SM prediction as ATLAS analysis



- No interference with top sector
- Total error dominated by statistical uncertainties – reflects in resulting coefficient bounds

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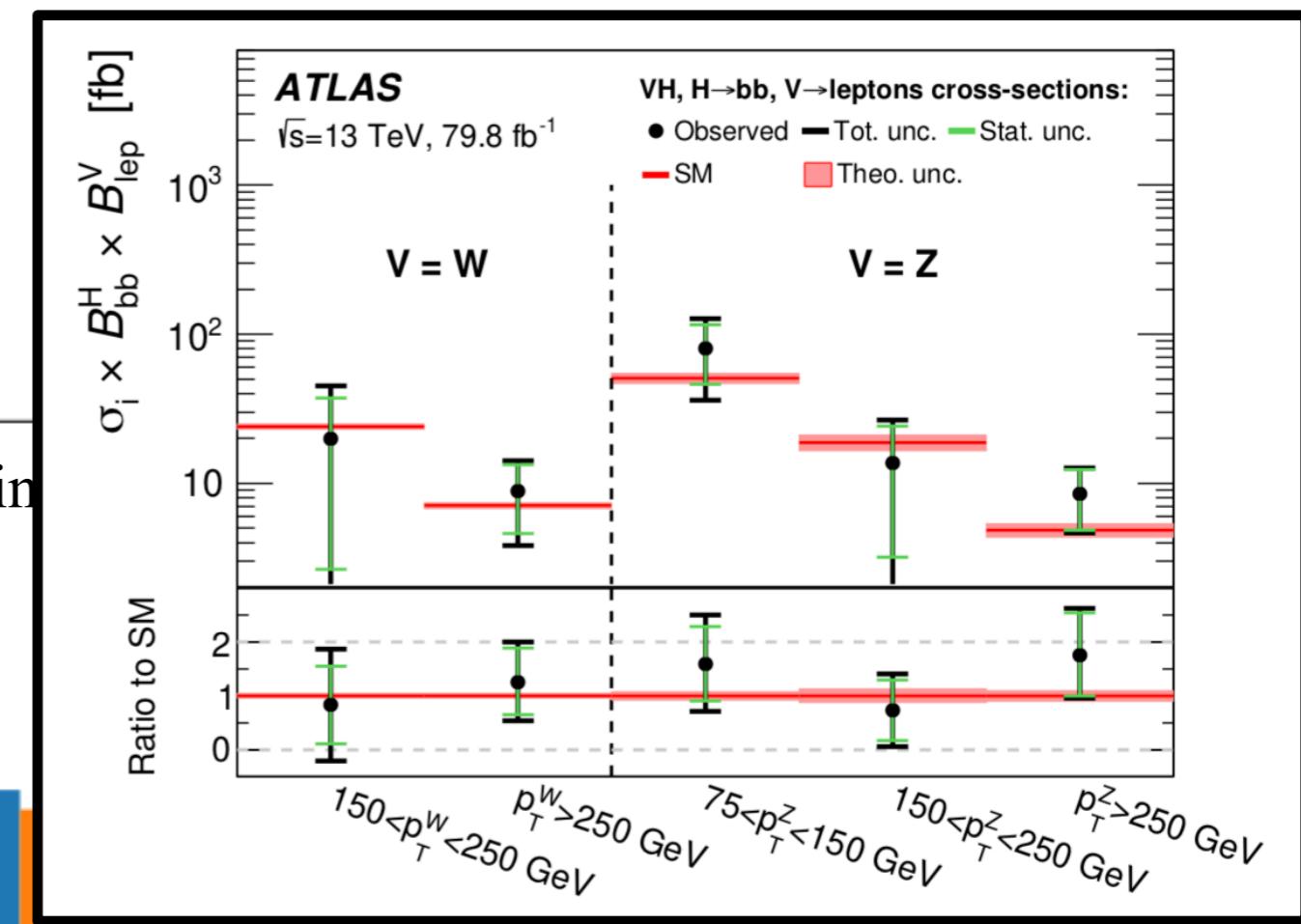
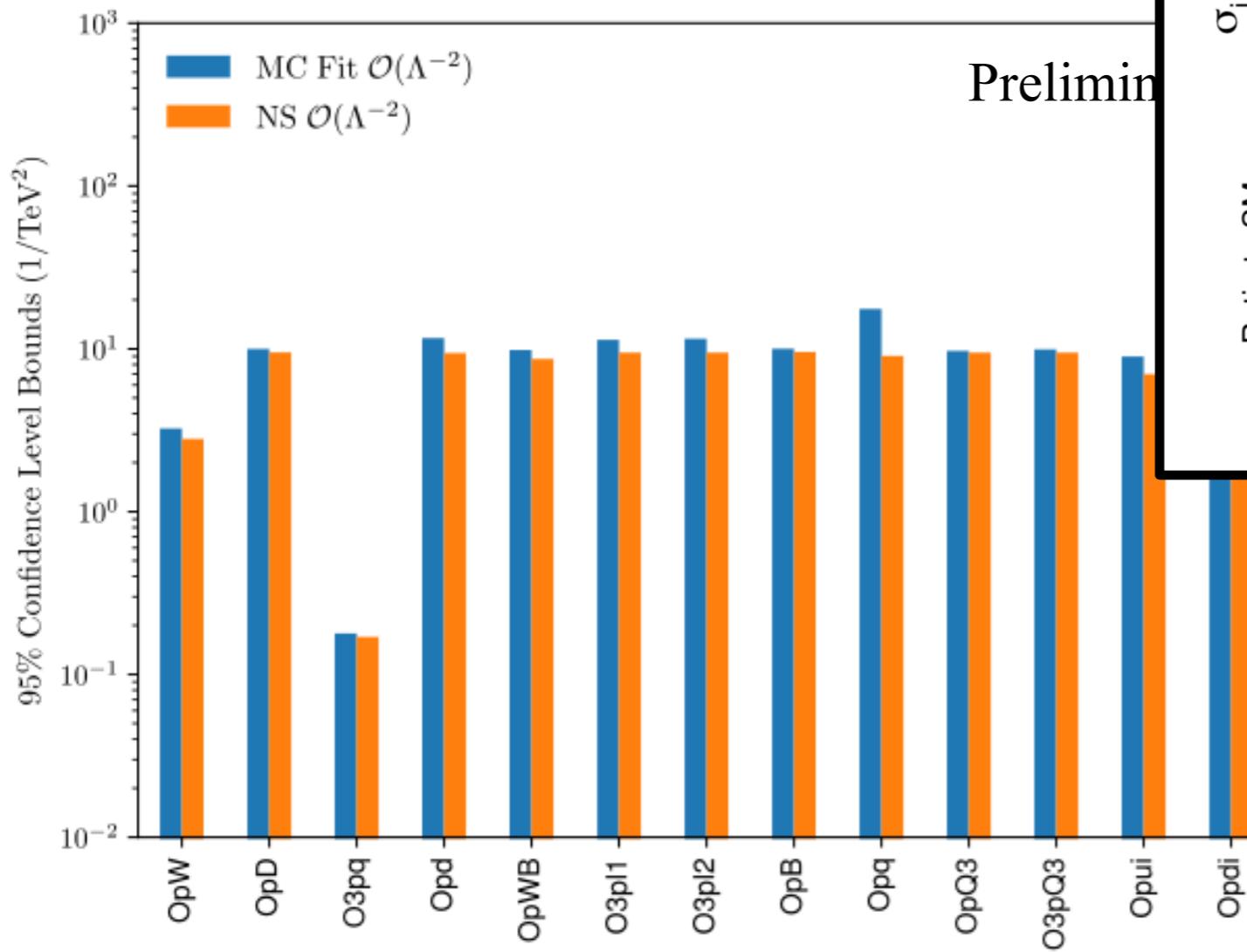


| Operator | Wilson Coefficient | Degree of Freedom | Operator Definition |
|----------|--------------------|-----------------------------------|---|
| OpW | cpW | $\mathcal{O}_{\varphi W}$ | $(\varphi^\dagger \varphi - \frac{v^2}{2}) W_I^{\mu\nu} W_{\mu\nu}^I$ |
| OpB | cpB | $\mathcal{O}_{\varphi B}$ | $(\varphi^\dagger \varphi - \frac{v^2}{2}) B^{\mu\nu} B_{\mu\nu}$ |
| OpWB | cpWB | $\mathcal{O}_{\varphi WB}$ | $(\varphi^\dagger \tau_I \varphi) B^{\mu\nu} W_{\mu\nu}^I$ |
| OpD | cpDC | $\mathcal{O}_{\varphi D}$ | $(\varphi^\dagger D^\mu \varphi)^\dagger (\varphi^\dagger D_\mu \varphi)$ |
| O3pq | cpqi | $\mathcal{O}_{\varphi q_i}^{(1)}$ | $\sum_{j=1,2} i (\varphi^\dagger \vec{D}_\mu \varphi) (\bar{q}_j \gamma^\mu q_j)$ |
| O3pQ3 | c3pqi | $\mathcal{O}_{\varphi q_i}^{(3)}$ | $\sum_{j=1,2} i (\varphi^\dagger \vec{D}_\mu \tau_I \varphi) (\bar{q}_j \gamma^\mu \tau^I q_j)$ |
| OpQ3 | cpQ3 | $\mathcal{O}_{\varphi Q}^{(1)}$ | $i (\varphi^\dagger \vec{D}_\mu \varphi) (\bar{Q} \gamma^\mu Q)$ |
| O3pQ3 | c3pQ3 | $\mathcal{O}_{\varphi Q}^{(3)}$ | $i (\varphi^\dagger \vec{D}_\mu \tau_I \varphi) (\bar{Q} \gamma^\mu \tau^I Q)$ |
| Opui | cpu | $\mathcal{O}_{\varphi u_i}$ | $\sum_{j=1,2} i (\varphi^\dagger \vec{D}_\mu \varphi) (\bar{u}_j \gamma^\mu u_j)$ |
| Opdi | cpd | $\mathcal{O}_{\varphi d_i}$ | $\sum_{j=1,2,3} i (\varphi^\dagger \vec{D}_\mu \varphi) (\bar{d}_j \gamma^\mu d_j)$ |
| Opd | cdp | $\mathcal{O}_{\varphi d}$ | $\partial_\mu (\varphi^\dagger \varphi) \partial^\mu (\varphi^\dagger \varphi)$ |
| O3pl1 | c3pl1 | $\mathcal{O}_{\varphi l_1}^{(3)}$ | $i (\varphi^\dagger \vec{D}_\mu \tau_I \varphi) (\bar{l}_1 \gamma^\mu \tau^I l_1)$ |
| O3pl2 | c3pl2 | $\mathcal{O}_{\varphi l_2}^{(3)}$ | $i (\varphi^\dagger \vec{D}_\mu \tau_I \varphi) (\bar{l}_2 \gamma^\mu \tau^I l_2)$ |

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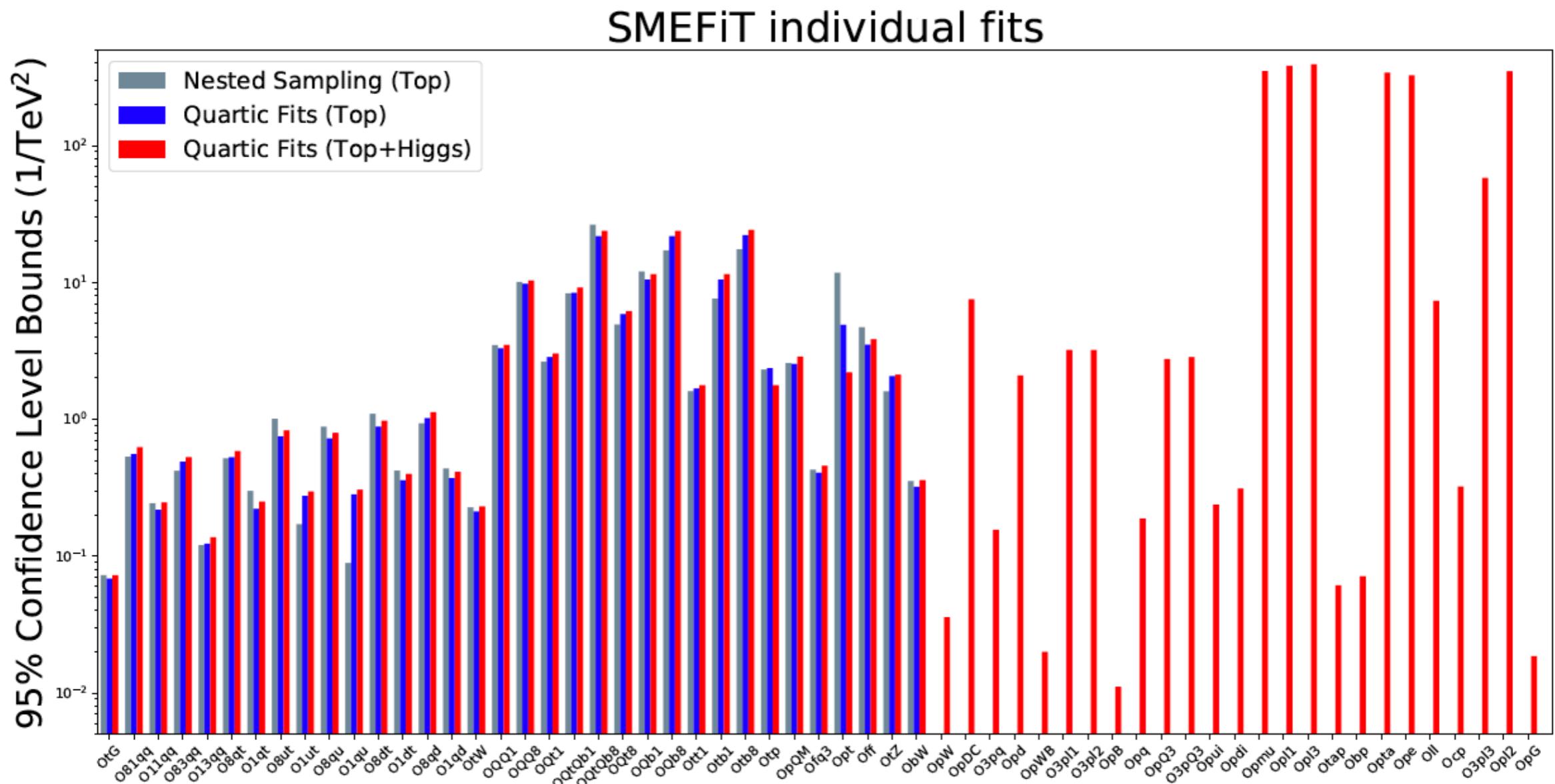
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Towards a global top/H/EW fit...



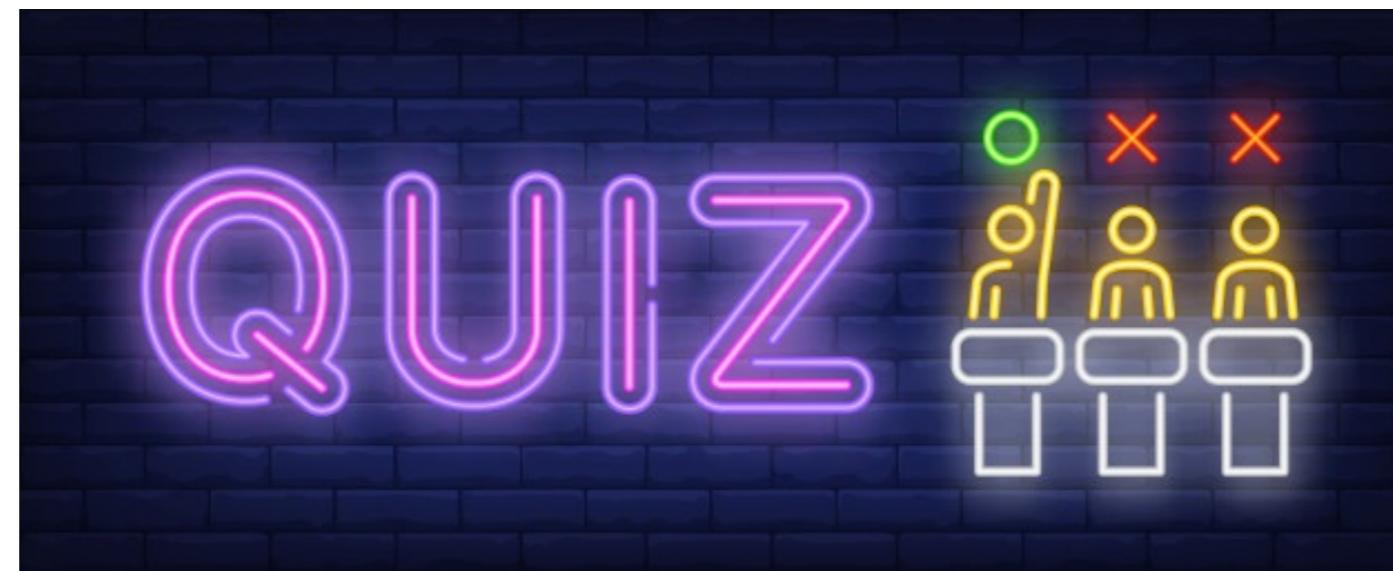
Plan for today's lecture

- SMEFT essentials
- The SMEFT precision frontier
- Example: Fitting in the Top (with Higgs/EW) sector
- Bringing the lesson home

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TRUE or FALSE?



10 questions you always wanted to know about
the SMEFT and never dared to ask

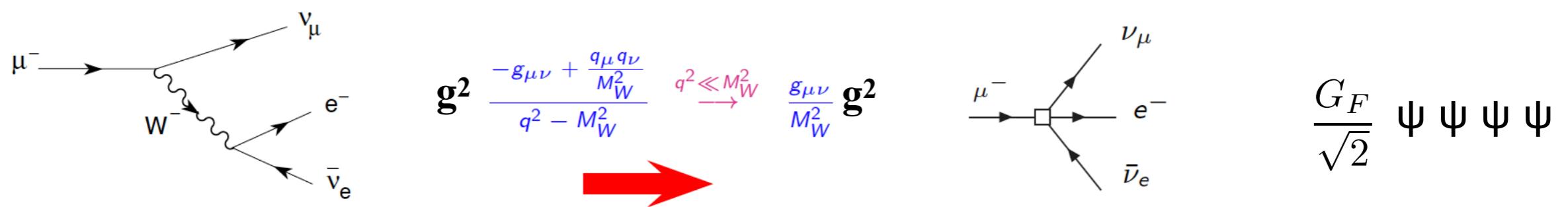
[Contino et al. , 1604.06444] [Aguilar-Saavedra ,1802.07237] [Many discussions...]

Λ is the scale of New Physics

1

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Consider the case of the Fermi theory of the muon decay:



From the measured value of the Fermi constant G_F

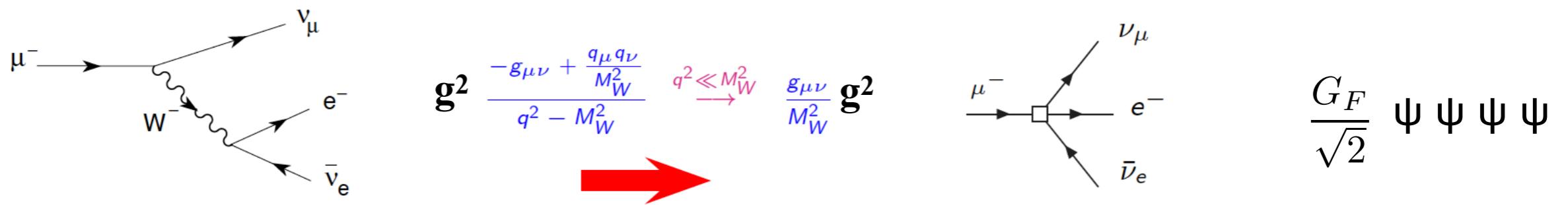
$$\frac{G_F}{\sqrt{2}} = \left(\frac{g}{2\sqrt{2}} \right)^2 \frac{1}{m_W^2} = \frac{1}{2v^2}$$

So $(4 \pi) v$ is the upper bound on the scale of New Physics. If the theory is weakly interacting the first massive state will have mass of the order $g v \ll v$. If the theory is strongly interacting, $g \sim 4 \pi$, $(4 \pi) v$ will coincide with the scale of NP.

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1

Note: Reinstating dimensions

$$\mathcal{L}_i^{\text{dim}=6} = \frac{g^{n_i-4}}{\Lambda^2} \mathcal{O}_i$$

$$\text{loop - factor} = \frac{g^2 \hbar}{(4\pi)^2}$$

$$M = g\Lambda = \text{GeV}$$

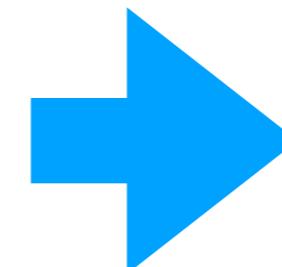
$$[G_{\mu\nu}] = \sqrt{\hbar} \text{ GeV}^2$$

$$[\phi] = [v] = [\Lambda] = \sqrt{\hbar} \text{ GeV}$$

$$[A_\mu] = \sqrt{\hbar} \text{ GeV}$$

$$[\psi] = \sqrt{\hbar} \text{ GeV}^{3/2}$$

$$[g] = [\sqrt{\lambda}] = 1/\sqrt{\hbar}$$



$$\mathcal{L} = \frac{g^2}{\Lambda^2} \phi^6 = \frac{g^4}{M^2} \phi^6$$

$$\mathcal{L} = \frac{g}{\Lambda^2} \phi \phi Q \phi u = \frac{g^3}{M^2} \phi \phi Q \phi u$$

$$\mathcal{L} = \frac{1}{\Lambda^2} \phi^2 G G = \frac{g^2}{M^2} \phi^2 G G$$

$$\mathcal{L} = \frac{1}{\Lambda^2} Q \phi u G = \frac{g^2}{M^2} Q \phi u G$$

$$\mathcal{L} = \frac{1}{\Lambda^2} \phi D \phi \psi \psi = \frac{g^2}{M^2} \phi D \phi \psi \psi$$

$$\mathcal{L} = \frac{1}{\Lambda^2} \psi \psi \psi \psi = \frac{g^2}{M^2} \psi \psi \psi \psi$$

$$\mathcal{L} = \frac{g^{-1}}{\Lambda^2} G G G = \frac{g}{M^2} G G G$$

The SMEFT is model independent

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The aim of an EFT is to reproduce the IR behaviour of (a possibly) wide set of UV theories. However, it always relies on (generic) assumptions on the UV dynamics. The SMEFT@dim6, for examples, assumes:

1. The upper bound on the scale of new physics is Λ .
2. The $SU(2) \times U(1)$ symmetry is linearly realised.
3. The expansion in $1/\Lambda$ is well-behaved, i.e. effects of dimension-8 operators are parametrically suppressed with respect to the dimension-6.

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Associating a “natural” normalisation to (class of) operators implies a UV bias, either some scaling rules and/or already an interpretation in mind. This is certainly legitimate, yet not necessary at the data analysis stage, if maximal flexibility/generality is desired.

At the SMEFT@dim6 one can work leaving the normalisation arbitrary (i.e. fixing the simplest convention) and just using data to constrain the coefficients. **At the end only relations between observables as implied by the model are physically meaningful.** And these do not depend on the normalisation.

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Order by order in the $1/\Lambda$ expansion, the SMEFT is renormalisable, i.e. higher-order contributions can be computed as perturbative series in the gauge couplings. For example, amplitudes with one operator insertion (at order $1/\Lambda^2$) can be renormalised using a finite number of counter-terms at all order in PT.

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4

Truncating the SMEFT at the $\text{dim}=6$ is always correct

5

Truncating the SMEFT at the dim=6 is always correct

The usefulness of the up to $1/\Lambda^2$ approximation will depend:

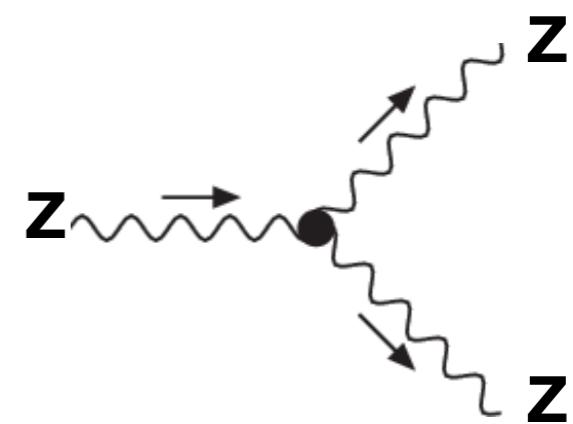
1. On the assumptions (explicit and implicit) on the UV model.
2. On the specific observables/interactions which might not be sensitive to dim=6 effects. For example a ZZZ vertex appears only at dim=8:

$$ie\Gamma_{ZZV}^{\alpha\beta\mu}(q_1, q_2, q_3) = \frac{-e(q_3^2 - m_V^2)}{M_Z^2} \left[f_4^V (q_3^\alpha g^{\mu\beta} + q_3^\beta g^{\mu\alpha}) - f_5^V \epsilon^{\mu\alpha\beta\rho} (q_1 - q_2)_\rho \right]$$

$$f_4^Z = \frac{M_Z^2 v^2 \left(c_w^2 \frac{C_{WW}}{\Lambda^4} + 2c_w s_w \frac{C_{BW}}{\Lambda^4} + 4s_w^2 \frac{C_{BB}}{\Lambda^4} \right)}{2c_w s_w}$$

$$f_4^\gamma = -\frac{M_Z^2 v^2 \left(-c_w s_w \frac{C_{WW}}{\Lambda^4} + \frac{C_{BW}}{\Lambda^4} (c_w^2 - s_w^2) + 4c_w s_w \frac{C_{BB}}{\Lambda^4} \right)}{4c_w s_w}$$

$$\begin{aligned} \mathcal{O}_{BW} &= i H^\dagger B_{\mu\nu} W^{\mu\rho} \{D_\rho, D^\nu\} H, \\ \mathcal{O}_{WW} &= i H^\dagger W_{\mu\nu} W^{\mu\rho} \{D_\rho, D^\nu\} H, \\ \mathcal{O}_{BB} &= i H^\dagger B_{\mu\nu} B^{\mu\rho} \{D_\rho, D^\nu\} H. \end{aligned}$$



5

[Degrande, 1308.6323]

Truncating the SMEFT at the dim=6 is always correct

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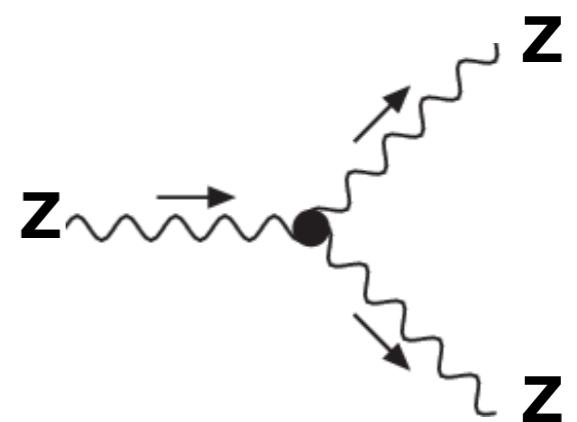
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5

[Degrande, 1308.6323]

The question on the validity/perturbativity of an EFT is moot

6

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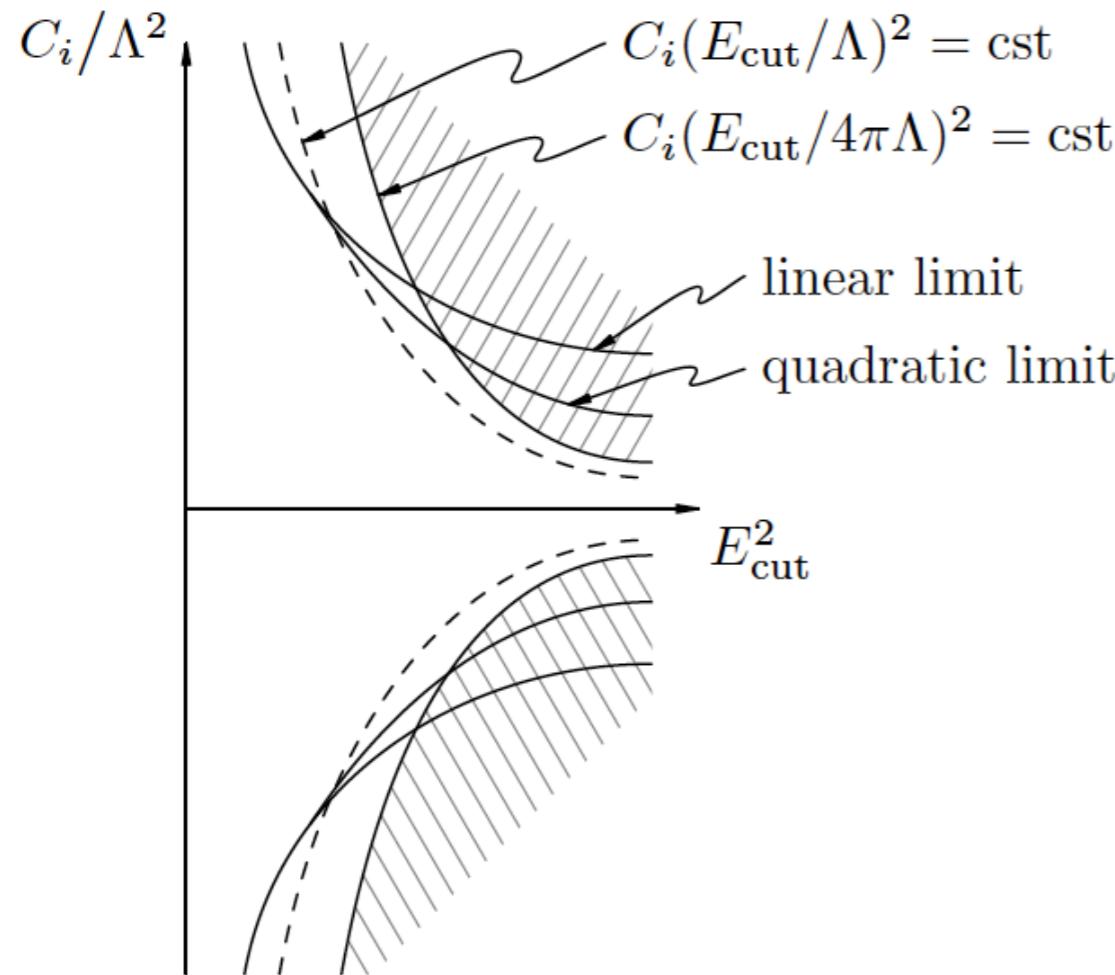


Figure 1: Illustration of the limit set on an EFT parameter as function of a cut on the characteristic energy scale of the process considered (see item 6). Qualitatively, one expects the limits to be progressively degraded as E_{cut} is pushed towards lower and lower values. At high cut values, beyond the energy directly accessible in the process considered, a plateau should be reached. The regions excluded when the dimension-six EFT is truncated to linear and quadratic orders are delimited by solid lines (see item 5c). The hatched regions indicate where the dimension-six EFT loses perturbativity (see item 7). In practice, curves will not be symmetric with respect to $C_i/\Lambda^2 = 0$.

* Provide information on the energy scales probed by the process *

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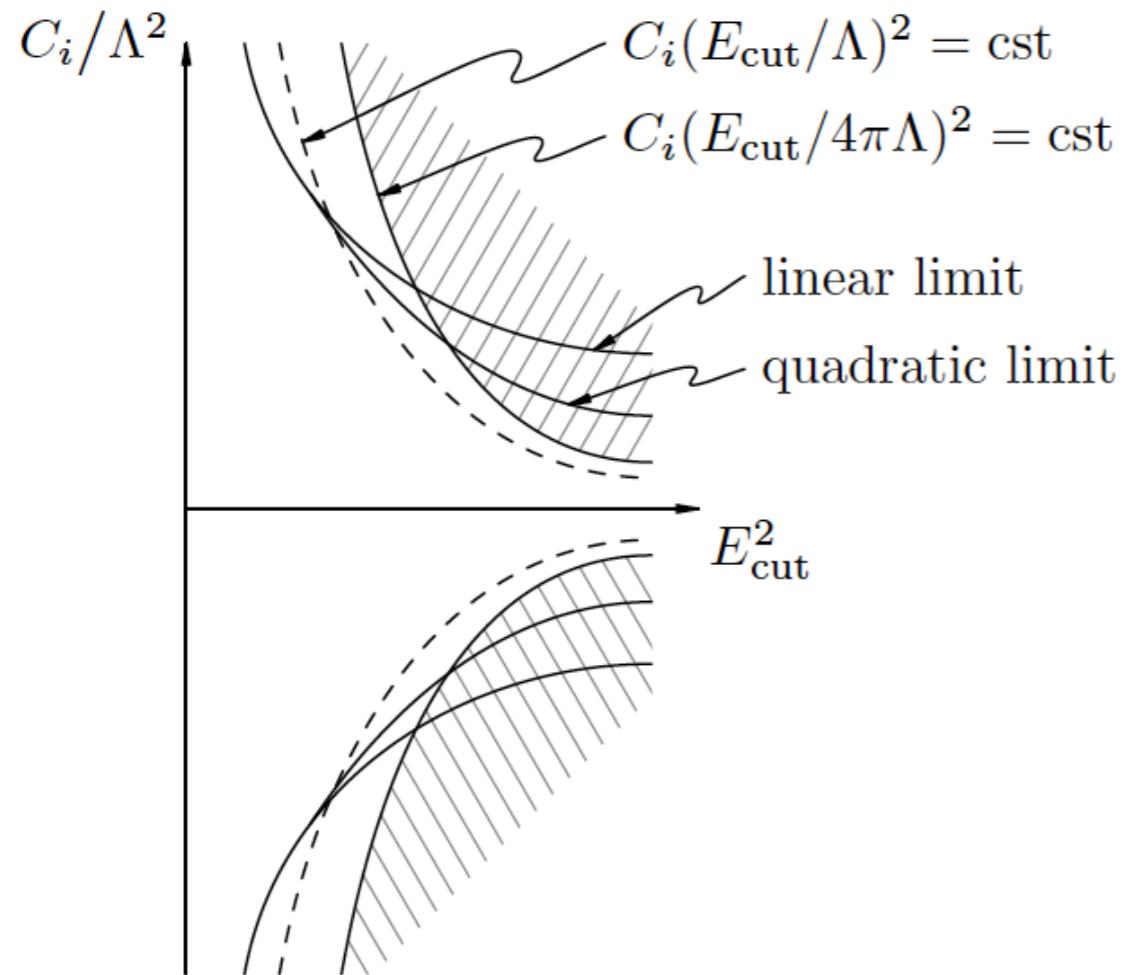


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Squared terms are not uniquely defined and should not be employed in pheno analyses

At the amplitude level:

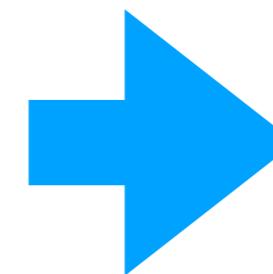
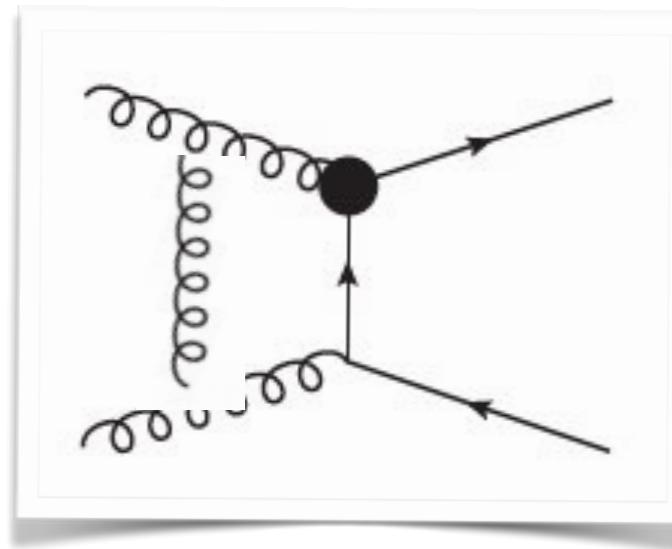
$$A = A_{\text{SM}} + \sum_i \tilde{c}_i^6 A_i^6 + \sum_k \tilde{c}_k^8 A_k^8 + \dots$$

At $1/\Lambda^2$ level, the $\text{dim}=6$ term is uniquely defined. One can change the basis, perform field redefinitions, use the EOM, yet the full blue sum remains the same, generating however, corrections of order $1/\Lambda^4$, feeding into the red term. This means that

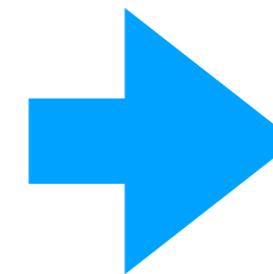
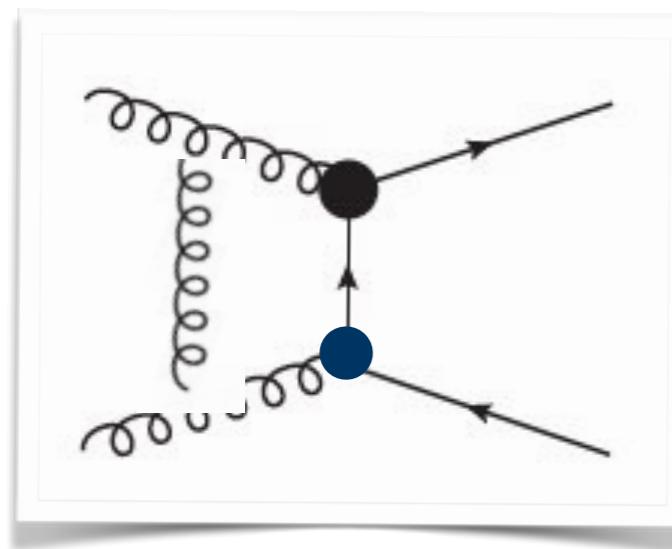
$$\begin{aligned} |A|^2 &= |A_{\text{SM}} + \sum_i \tilde{c}_i^6 A_i^6|^2 \\ &= |A_{\text{SM}}|^2 + 2 \sum_i^i \tilde{c}_i^6 \text{Re} [A_{\text{SM}}^* A_i^6] + \sum_{ij} \tilde{c}_i^6 \tilde{c}_j^{6*} A_i^{6*} A_j^6 \end{aligned}$$

is parametrisation invariant. The last term is order $1/\Lambda^4$, yet uniquely defined.

Squared terms are not uniquely defined and should not be employed in pheno analyses



This amplitude will need max dim=6 operators for renormalisation



This amplitude will generically need dim=8 operators for renormalisation

Squared terms are not uniquely defined and should not be employed in pheno analyses

In many cases the squared term should be included and in any case can be included:

- 1) If the interference term is highly suppressed because of symmetries (such as absence of FCNC at the tree-level in the SM) or selection rules (helicity selection for VV productions, i.e. the GGG operator in $gg \rightarrow gg$), the squared term is always the dominant contribution.
- 2) There are UV models, for which the squared terms are foreseen to be the dominant $1/\Lambda^4$ contributions:

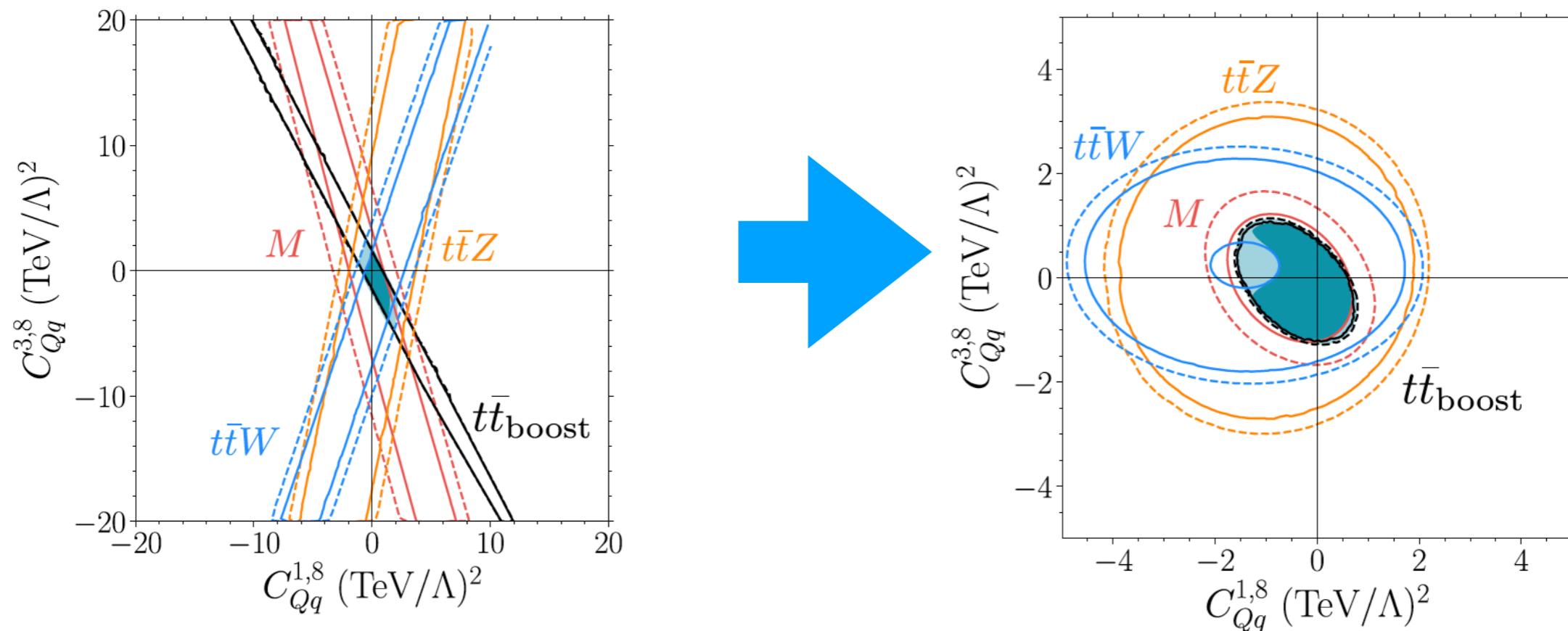
$$C_i^2 \frac{E^4}{\Lambda^4} > C_i \frac{E^2}{\Lambda^2} > 1 > \frac{E^2}{\Lambda^2}$$

EFT condition satisfied but $O(1/\Lambda^4)$ large for large operator coefficients

Squared terms are not uniquely defined and should not be employed in pheno analyses

At the fitting level the squared can have an important effect, as there are no flat directions in the fit with the squares:

[Brivio et al. , 1910.03606]



In general without knowing the effect of the squares one is left in the dark about meaning/reliability of the fit.

7

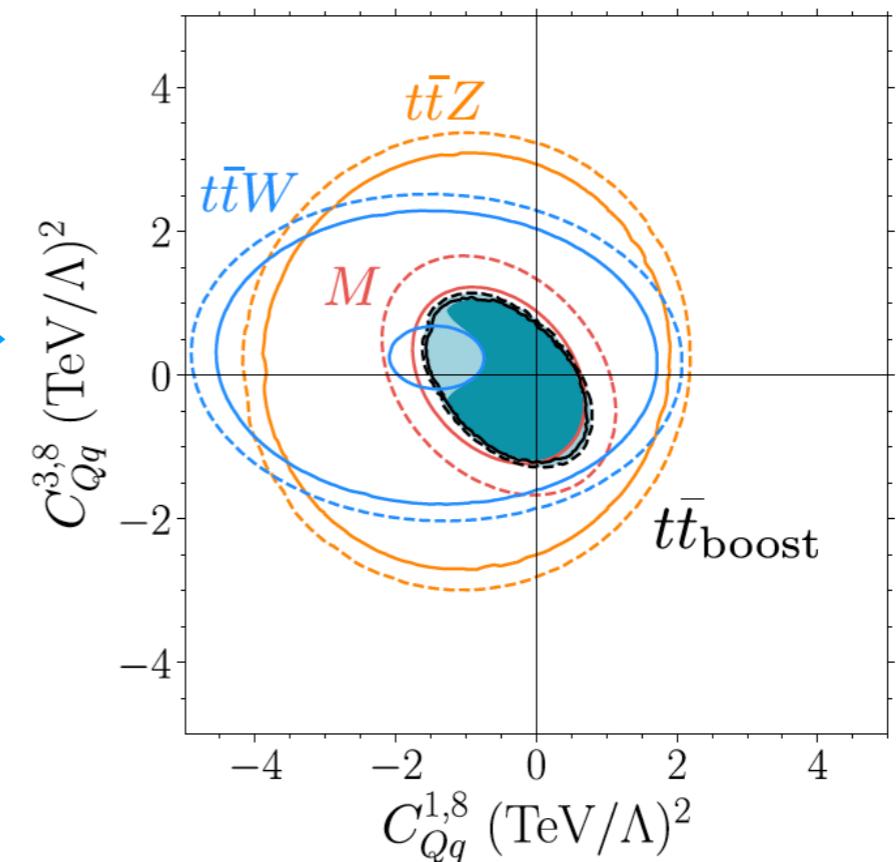
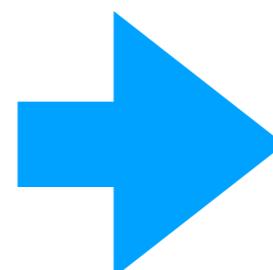
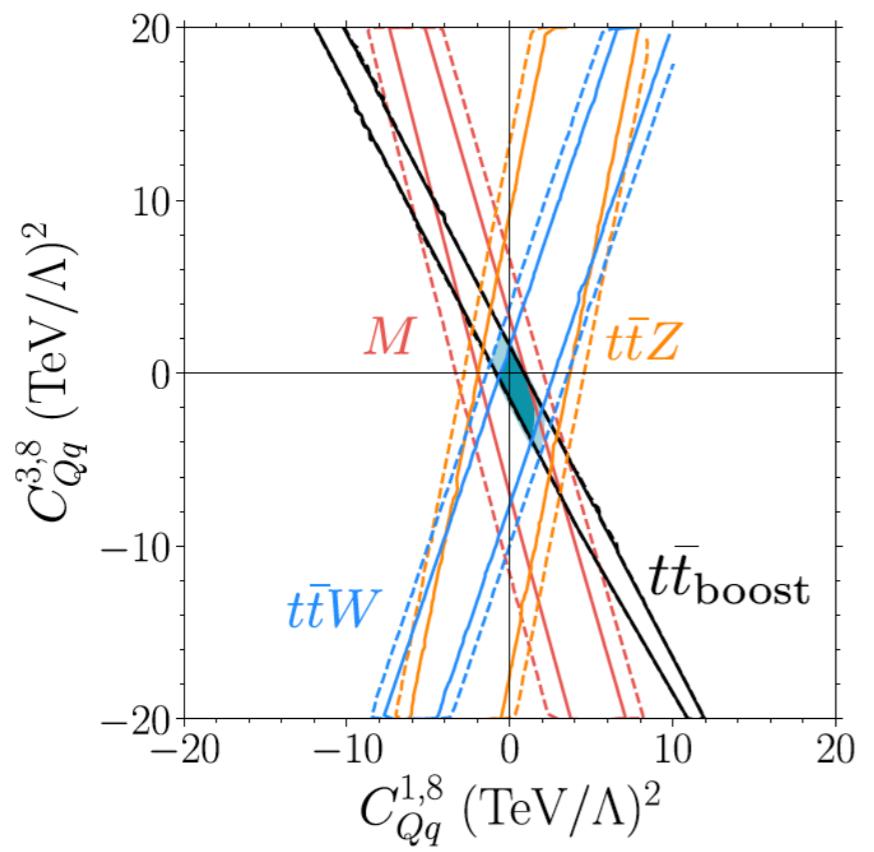
Provide constraints using i) linear and ii) linear+squared terms

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Provide constraints using i) linear and ii) linear+squared terms

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There are at least two cases where this will not be the case:

1. The new resonance is quite heavy with respect to the collider energy and no other states are found \Rightarrow it could be the first particle of a new heavy sector. EFT can include it and search for indirect effects of other states/phenomena.
2. The new resonance is light and very weakly interacting (like an axion) so that it does not impact collider phenomenology.



$v = 246 \text{ GeV}$, $f_a \sim 2 \times 10^{12} \text{ GeV}$, $v/f_a \sim 10^{-10}$, $m_a \sim 2 \mu\text{eV}$. Need

$$-\frac{g^2}{2M_W^2} + \frac{1}{f_a^2} \frac{q^2}{q^2 - m_a^2} = -\frac{2}{v^2} \left[1 + \frac{v^2}{2f_a^2} \frac{q^2/m_a^2}{q^2/m_a^2 - 1} \right]$$

$$\left| \frac{q^2}{m_a^2} - 1 \right| \sim \frac{v^2}{f_a^2} \sim 10^{-20} \Rightarrow \Delta q \sim 10^{-25} \text{ GeV}$$

Ex. by Manohar

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1. To understand which process is the most constraining one (comparing the impact of an operator on different processes is normalisation independent) **SENSITIVITY**.
2. Using pairs or triplets to understand the correlations and the flat directions and how to break them.
3. Technically, it might be complicated to include all operators in an analysis. However, having previous knowledge about where the sensitivity of an operator comes from, bounds from other processes/experiments, RGE information and, if desired, also UV model dependent information, one can establish a hierarchy and make maximal use of experimental information.

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Understanding and quantifying the higher order effects in the SMEFT is needed because of many reasons:

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2. NLO brings more accurate central values (k-factors) and reduction of the uncertainties (which can be gauged with the scale dependence, including EFT).
3. NLO QCD effects are important at the LHC, due to the nature of the collision. Not only rates can be greatly affected but also distributions.
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A quote

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Sun Tzu, The Art of War

A special thanks to
Ken Mimasu and Eleni Vryonidou
for providing material and insights for this lecture

General SMEFT Strategy

Courtesy of Ken Mimasu

General SMEFT Strategy

Basis

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General SMEFT Strategy

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Warsaw, SILH, HISZ, Higgs Basis

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General SMEFT Strategy

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Flavor assumptions

Universal, diagonal, 3rd gen, general?

Courtesy of Ken Mimasu

General SMEFT Strategy

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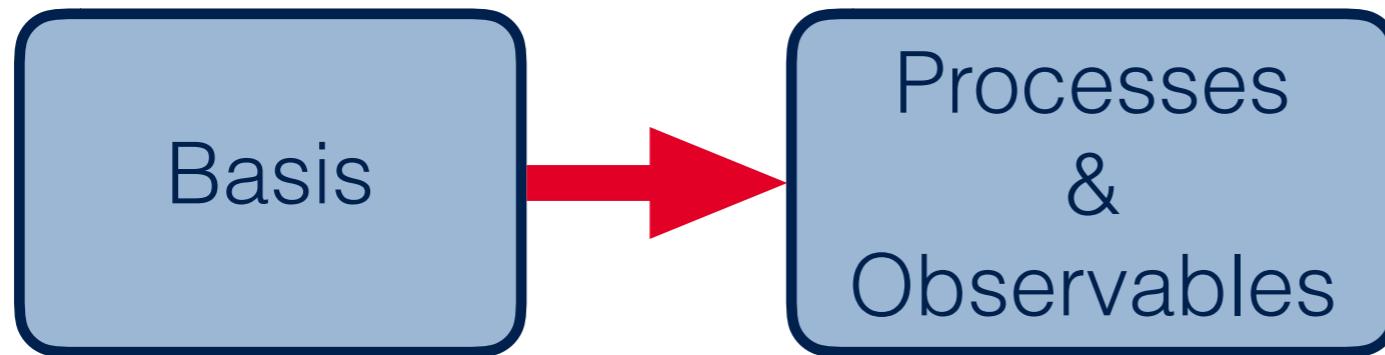
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CP, Baryon/Lepton number?

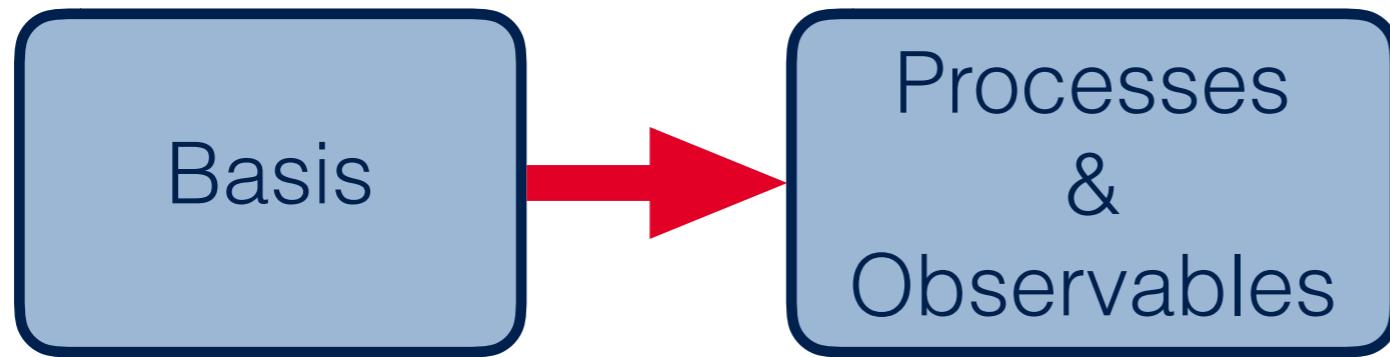
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General SMEFT Strategy



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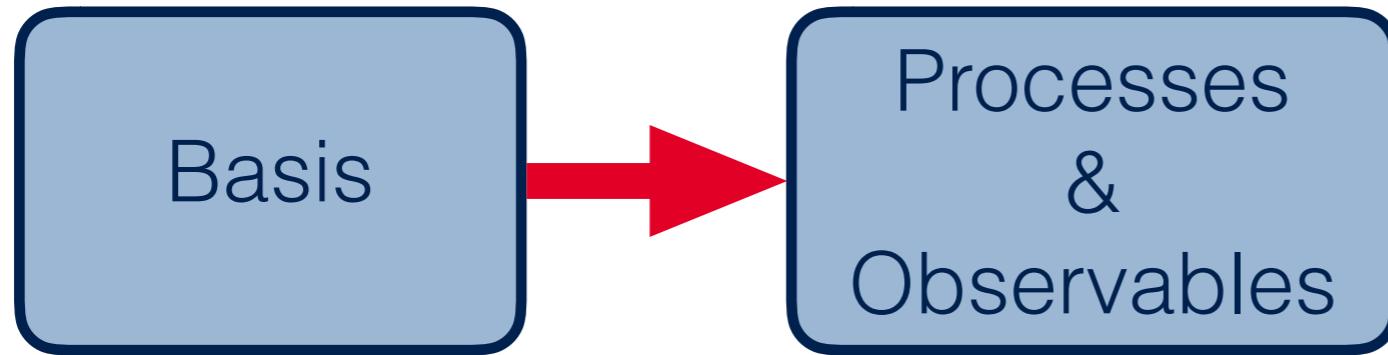
General SMEFT Strategy



$$\sigma_{\text{tot.}}, \quad \mu = \frac{\sigma}{\sigma_{\text{SM}}}$$

Courtesy of Ken Mimasu

General SMEFT Strategy

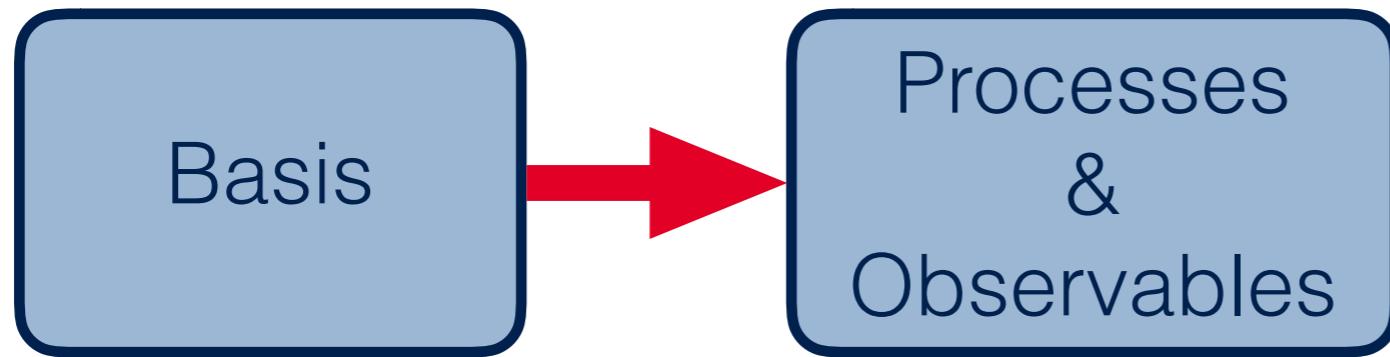


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Differential

Courtesy of Ken Mimasu

General SMEFT Strategy

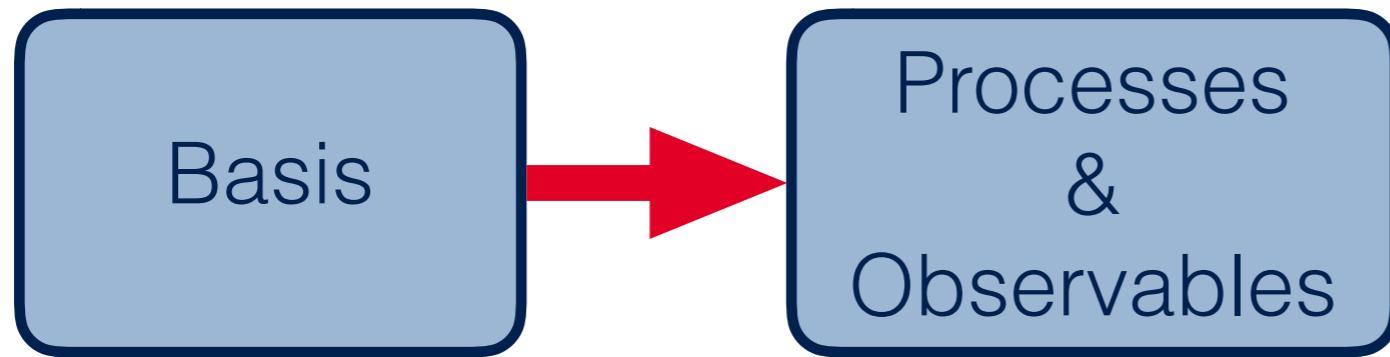


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General SMEFT Strategy

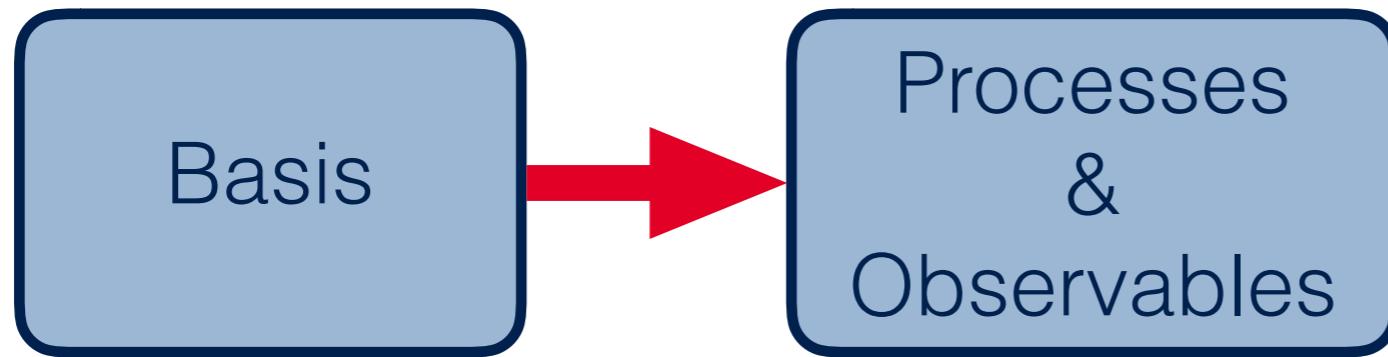


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General SMEFT Strategy



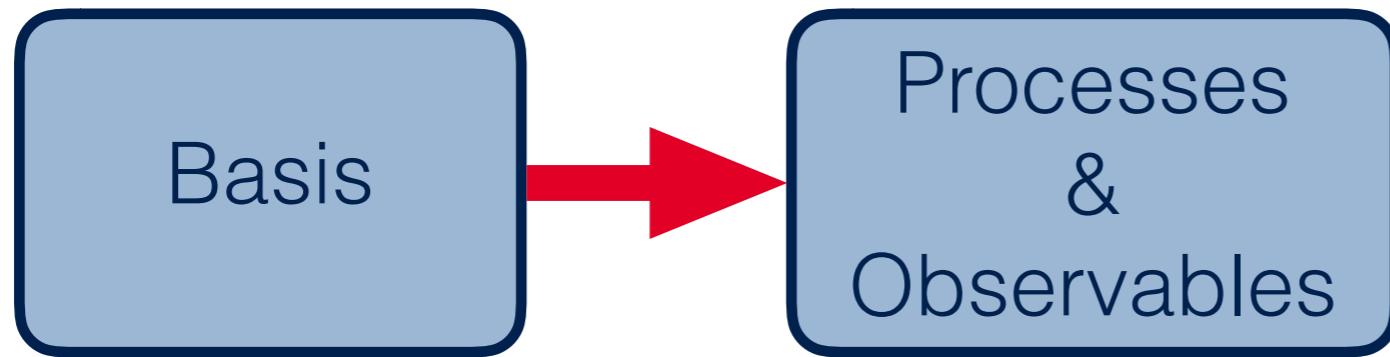
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High-level

Courtesy of Ken Mimasu

General SMEFT Strategy



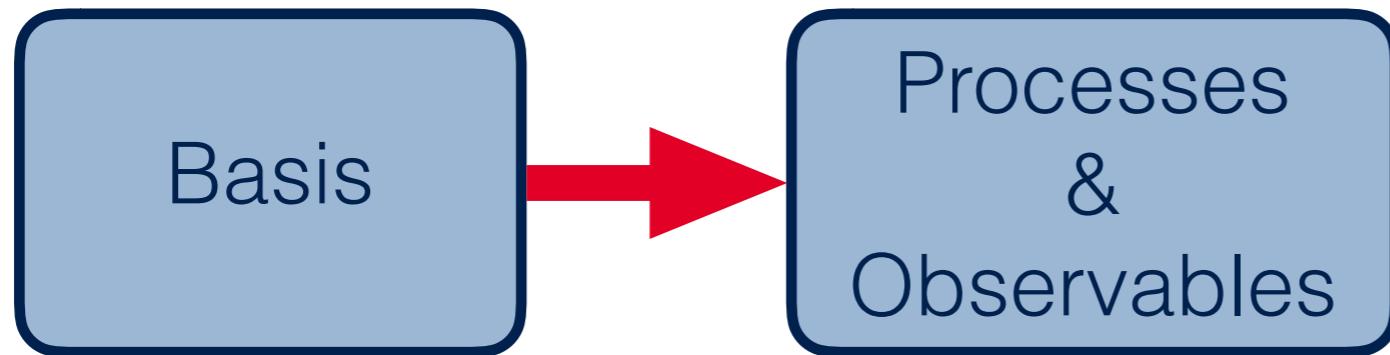
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Courtesy of Ken Mimasu

General SMEFT Strategy

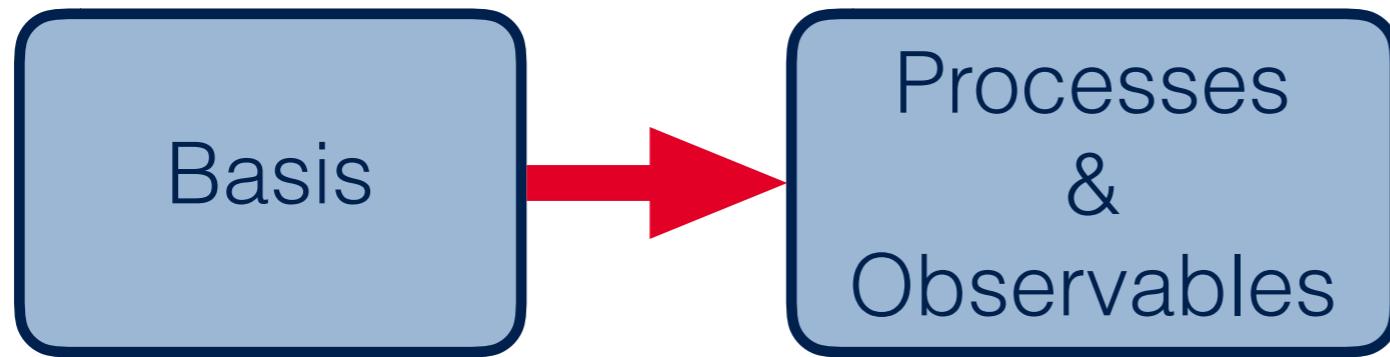


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| | | |
|--------------|---------------------------|--|
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| High-level | | <i>optimal observables</i> |

Courtesy of Ken Mimasu

General SMEFT Strategy



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Courtesy of Ken Mimasu

General SMEFT Strategy



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Determine dependence on
Wilson coefficients

Courtesy of Ken Mimasu

General SMEFT Strategy



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Courtesy of Ken Mimasu

General SMEFT Strategy



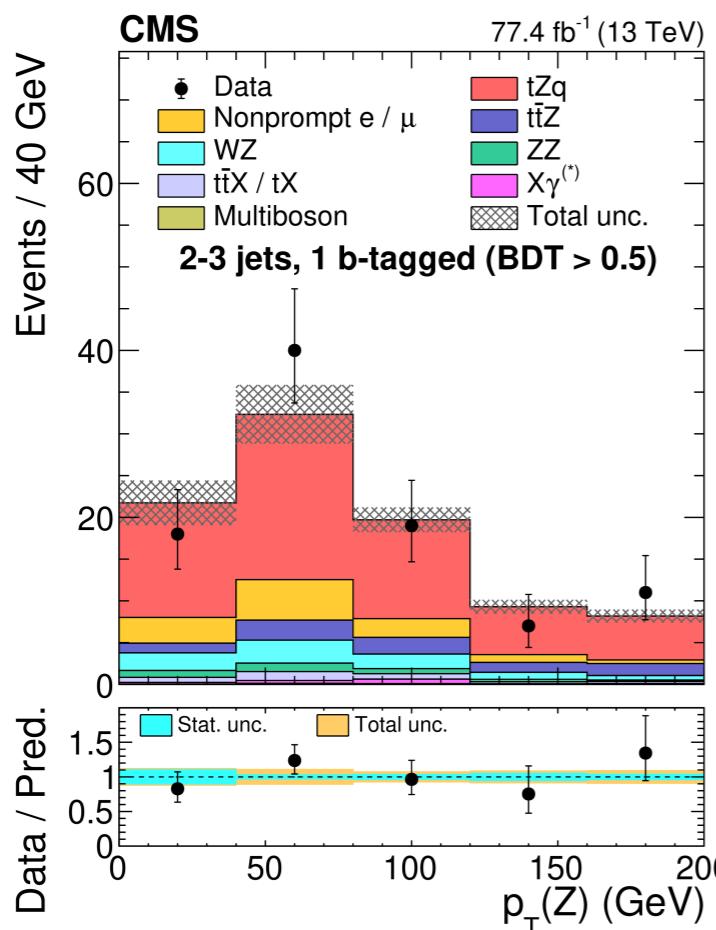
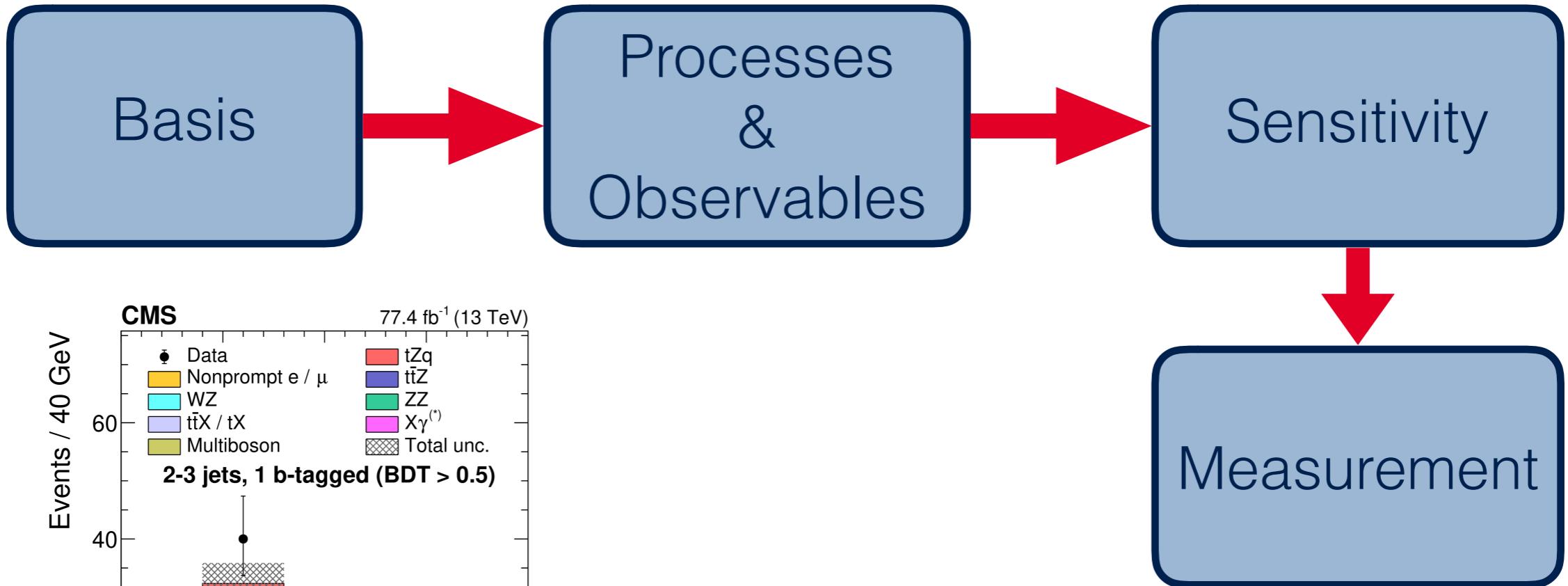
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Precise Monte Carlo tools

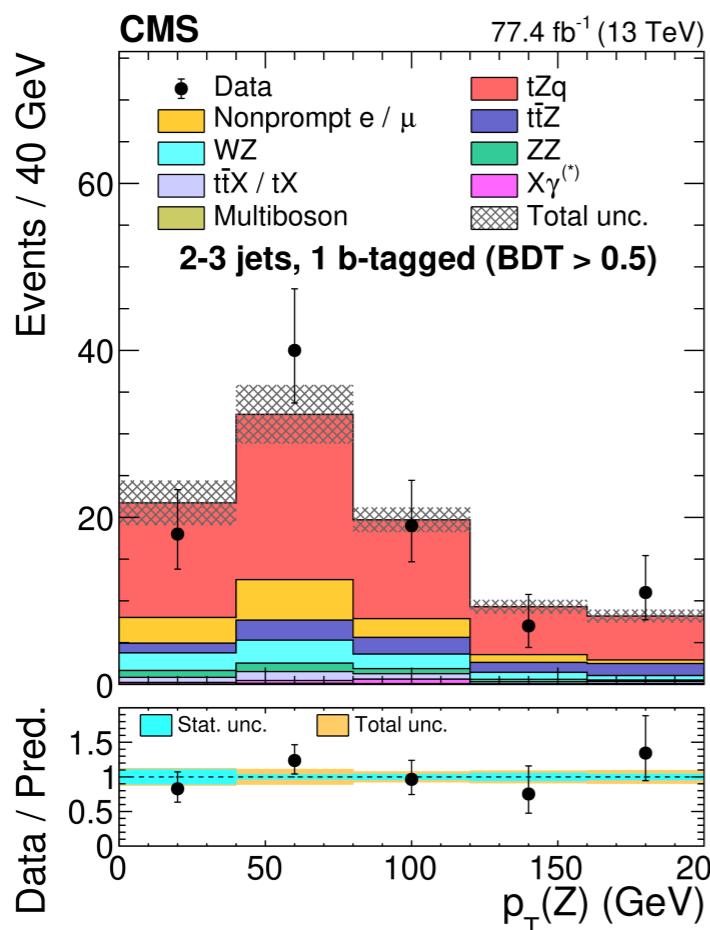
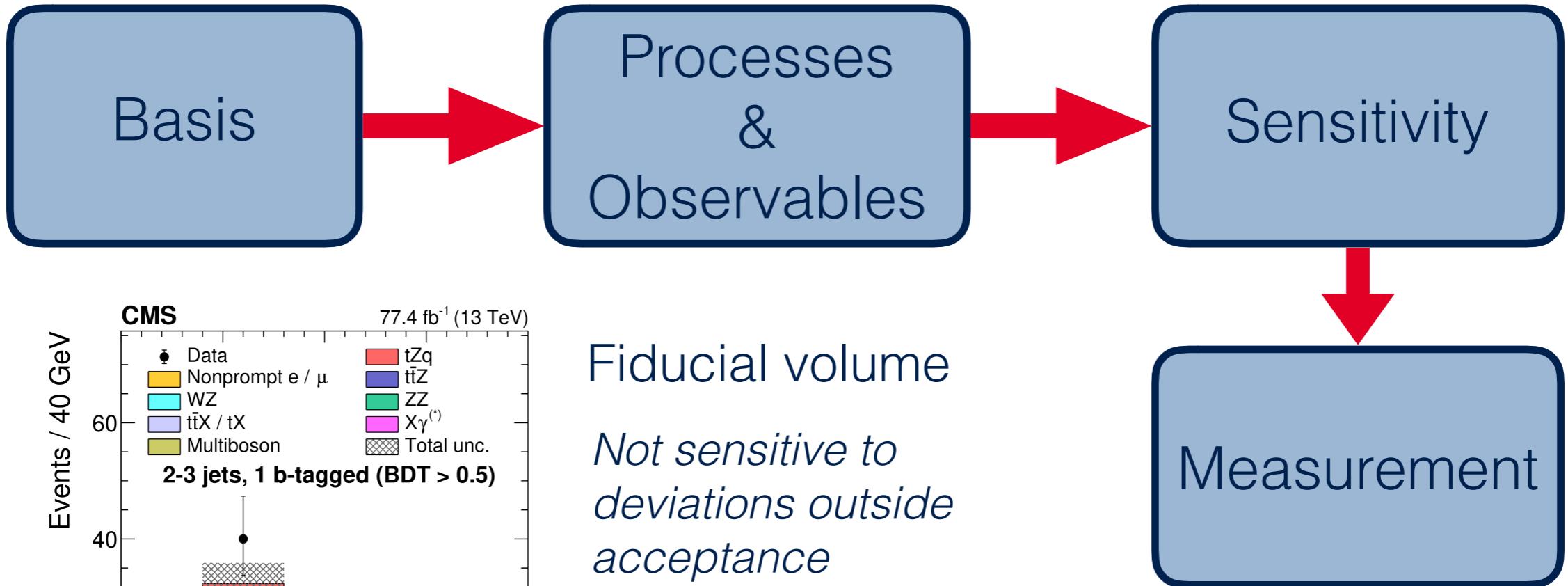
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Courtesy of [\[K. Mimasu \(2019\) 132003\]](#)

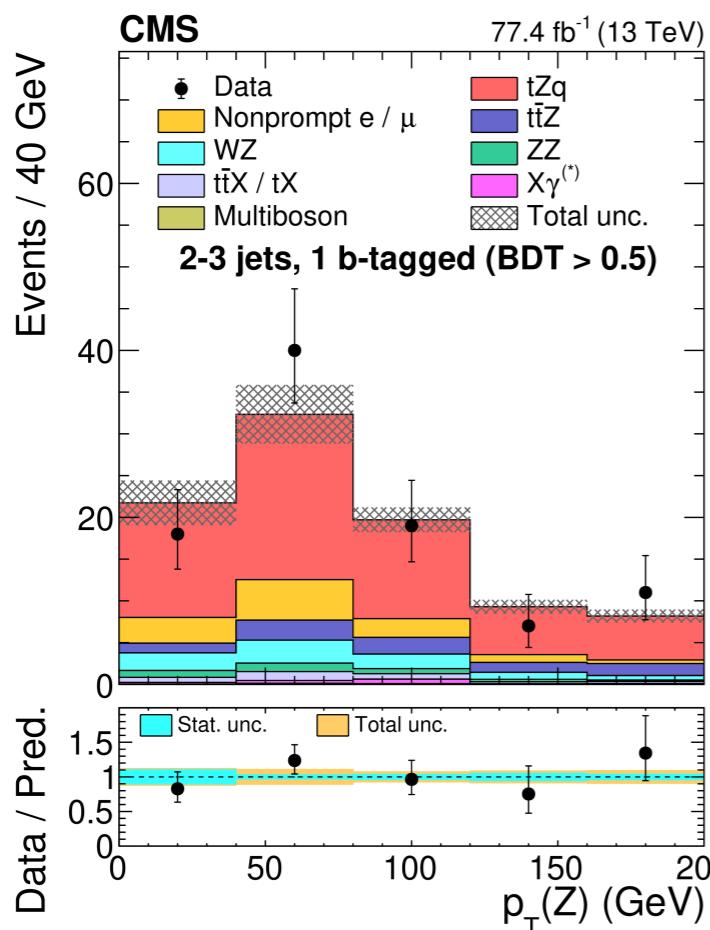
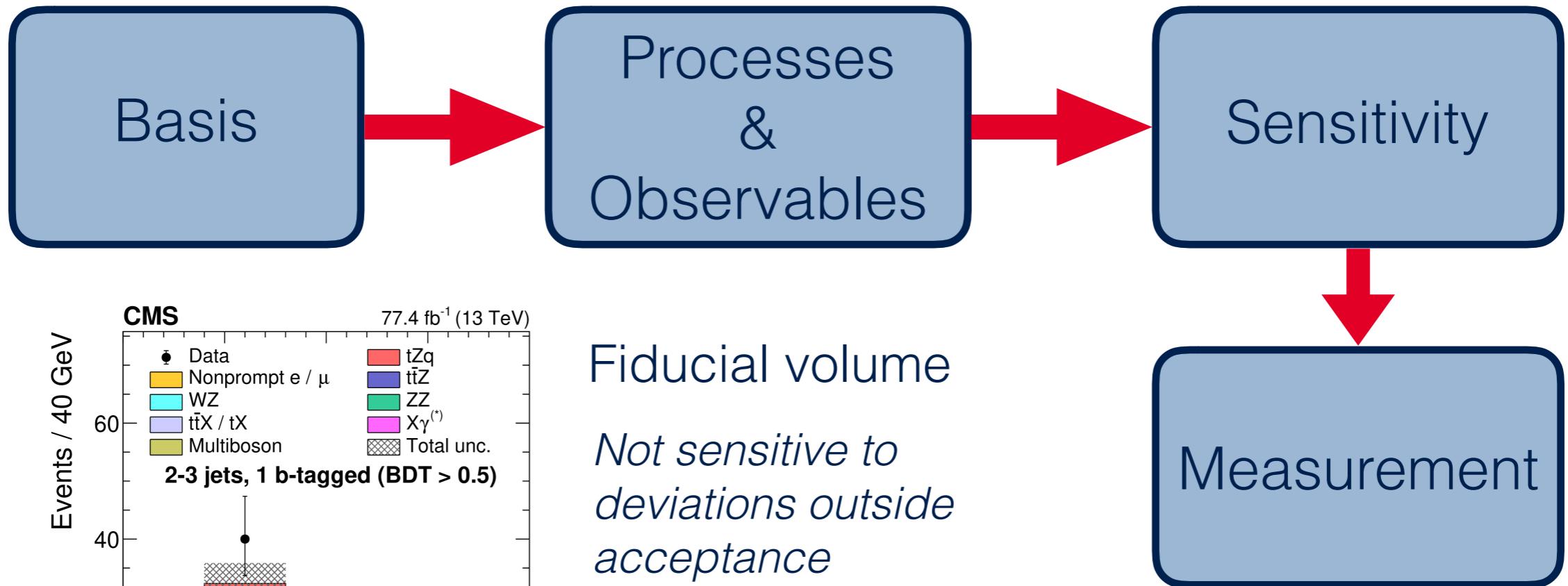
General SMEFT Strategy



Fiducial volume
*Not sensitive to
deviations outside
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Courtesy of [\[K.M. Mimasu \(2019\) 132003\]](#)

General SMEFT Strategy



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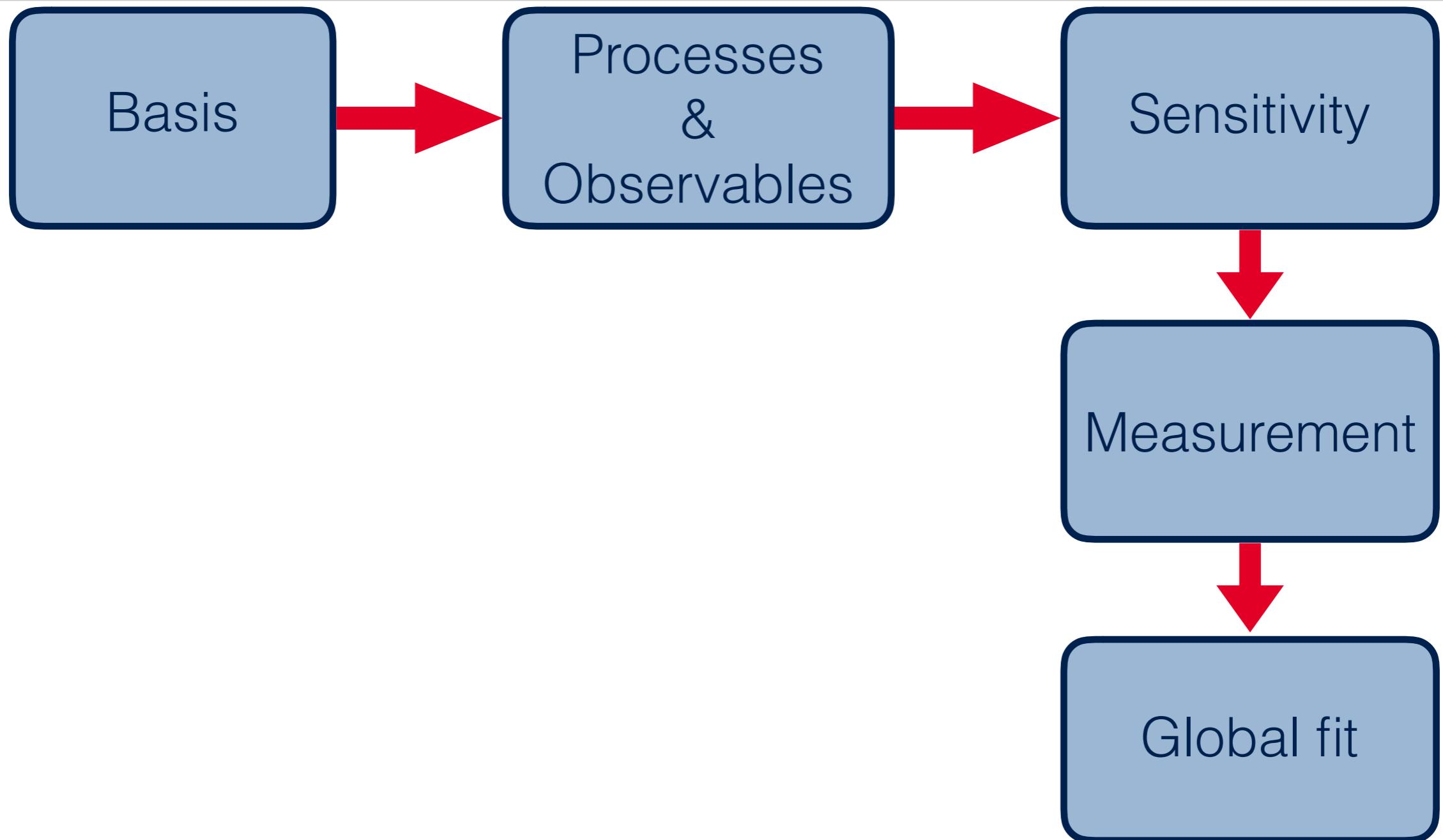
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Extract limits

$$c_i \subset [a, b] \quad [\text{TeV}^{-2}]$$

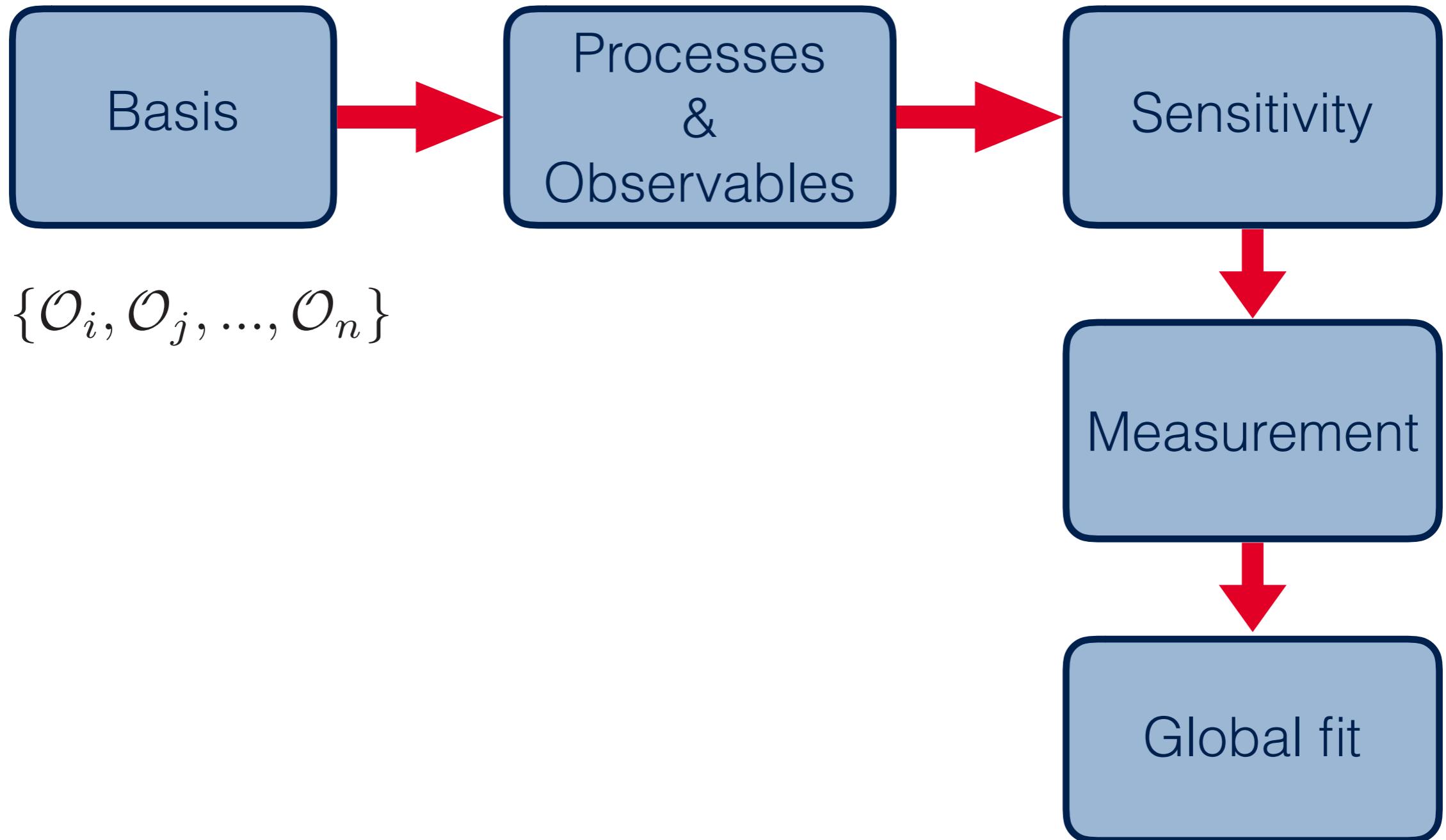
Courtesy of [Ken Mimasu (2019) 132003]

General SMEFT Strategy



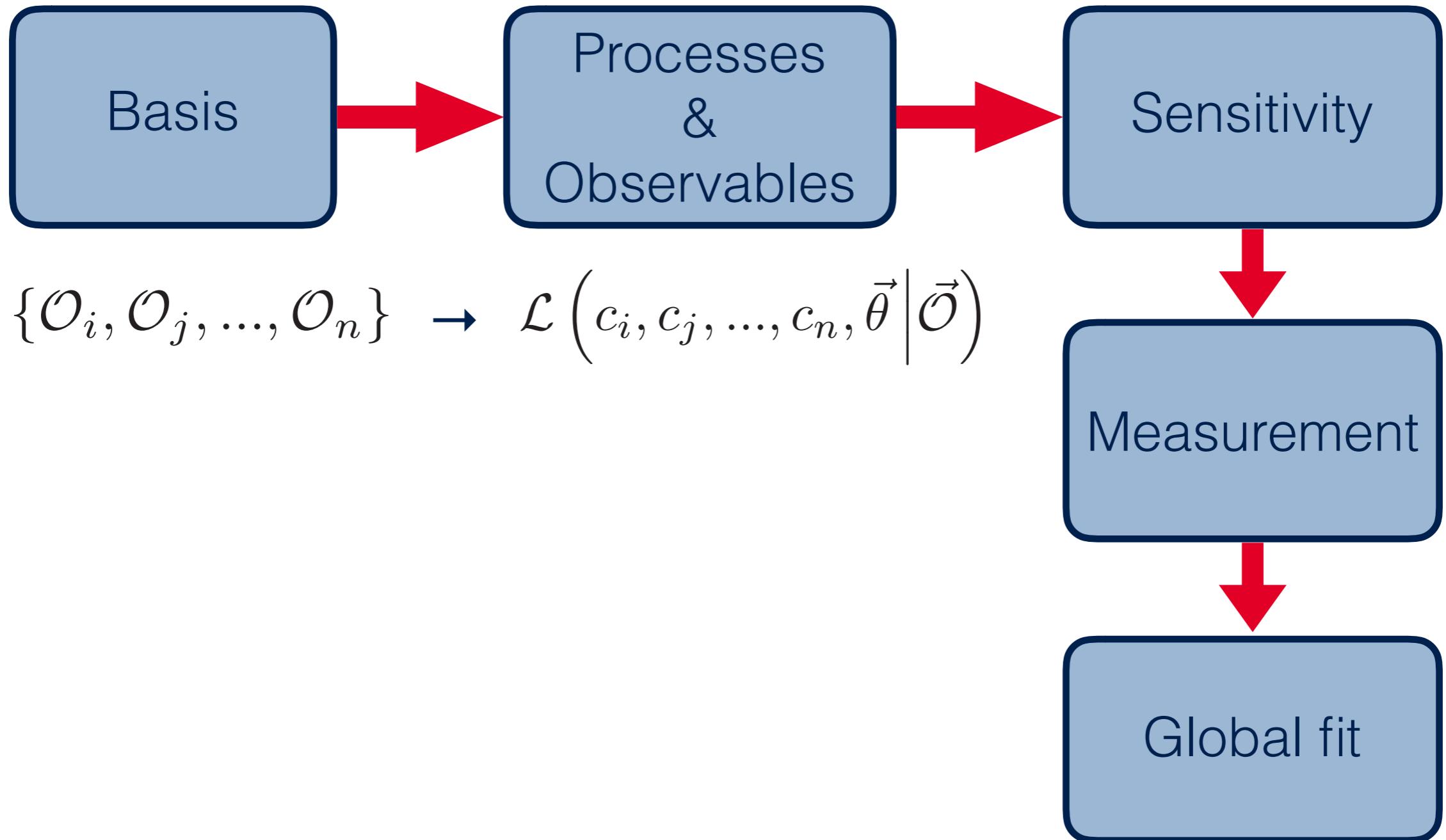
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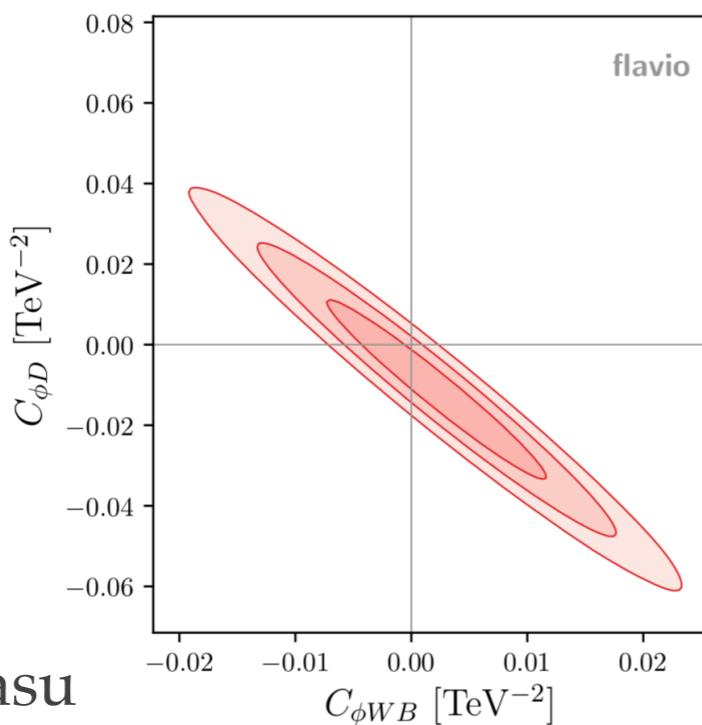
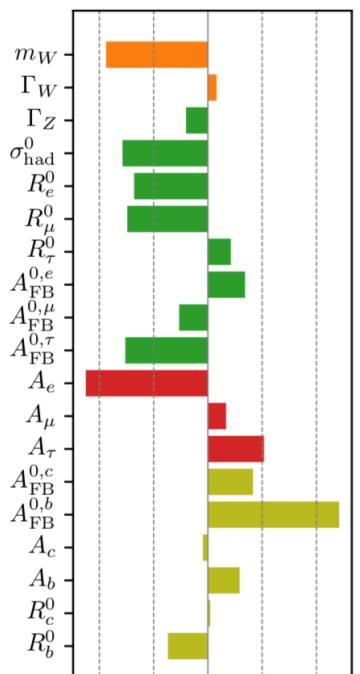
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General SMEFT Strategy

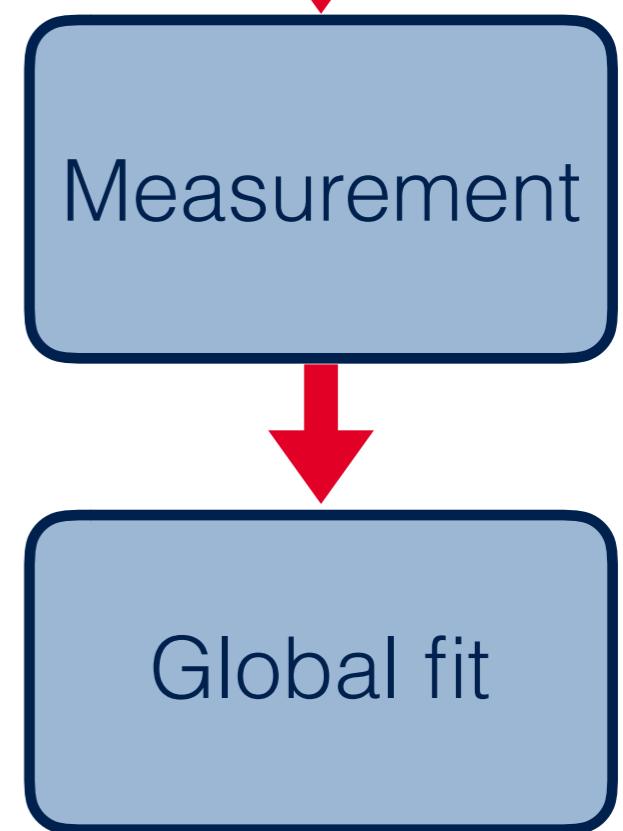


$$\{\mathcal{O}_i, \mathcal{O}_j, \dots, \mathcal{O}_n\} \rightarrow \mathcal{L}(c_i, c_j, \dots, c_n, \vec{\theta} \mid \vec{\mathcal{O}})$$

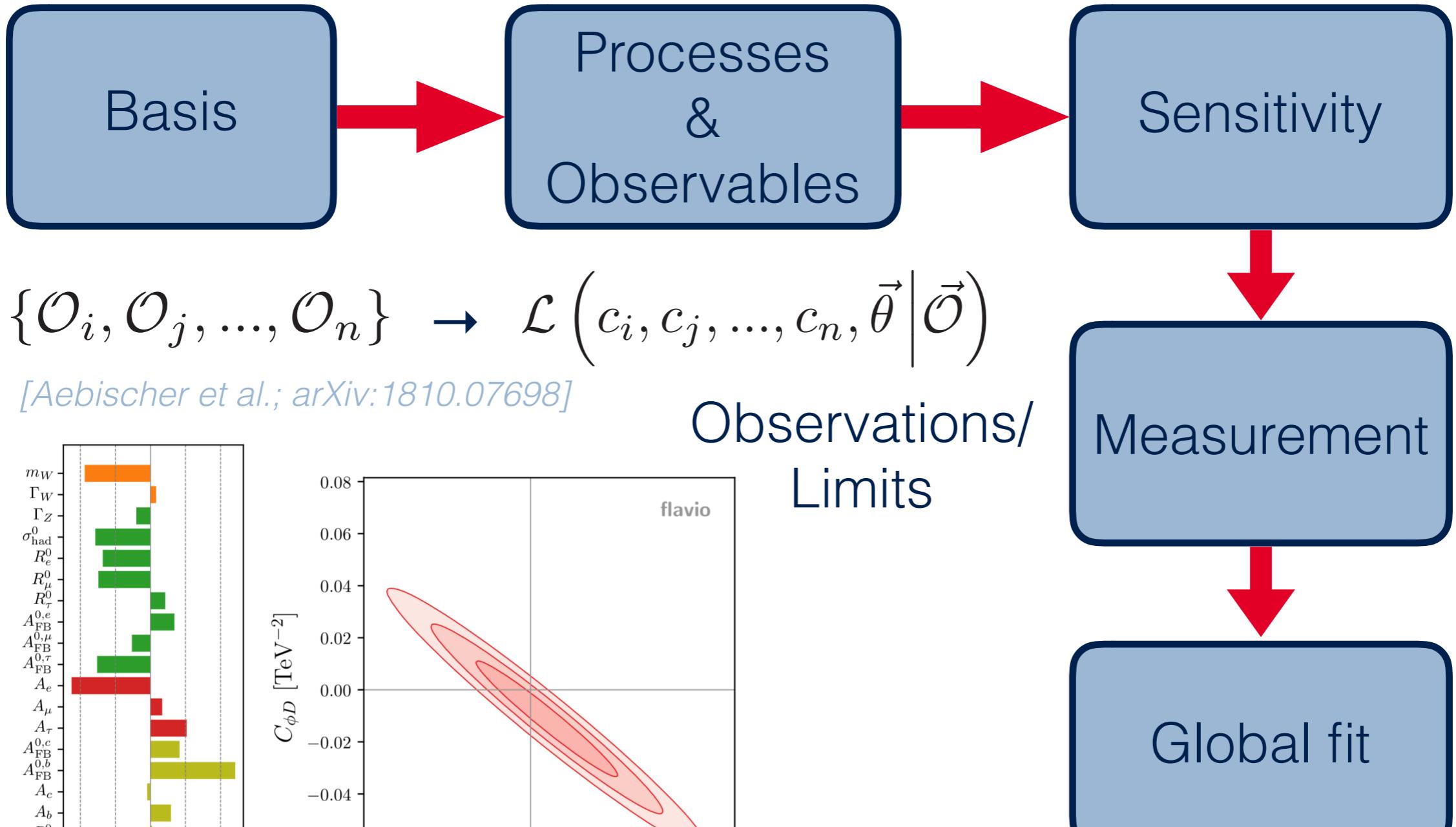
[Aebischer et al.; arXiv:1810.07698]



Courtesy of Ken Mimasu
pull (σ)

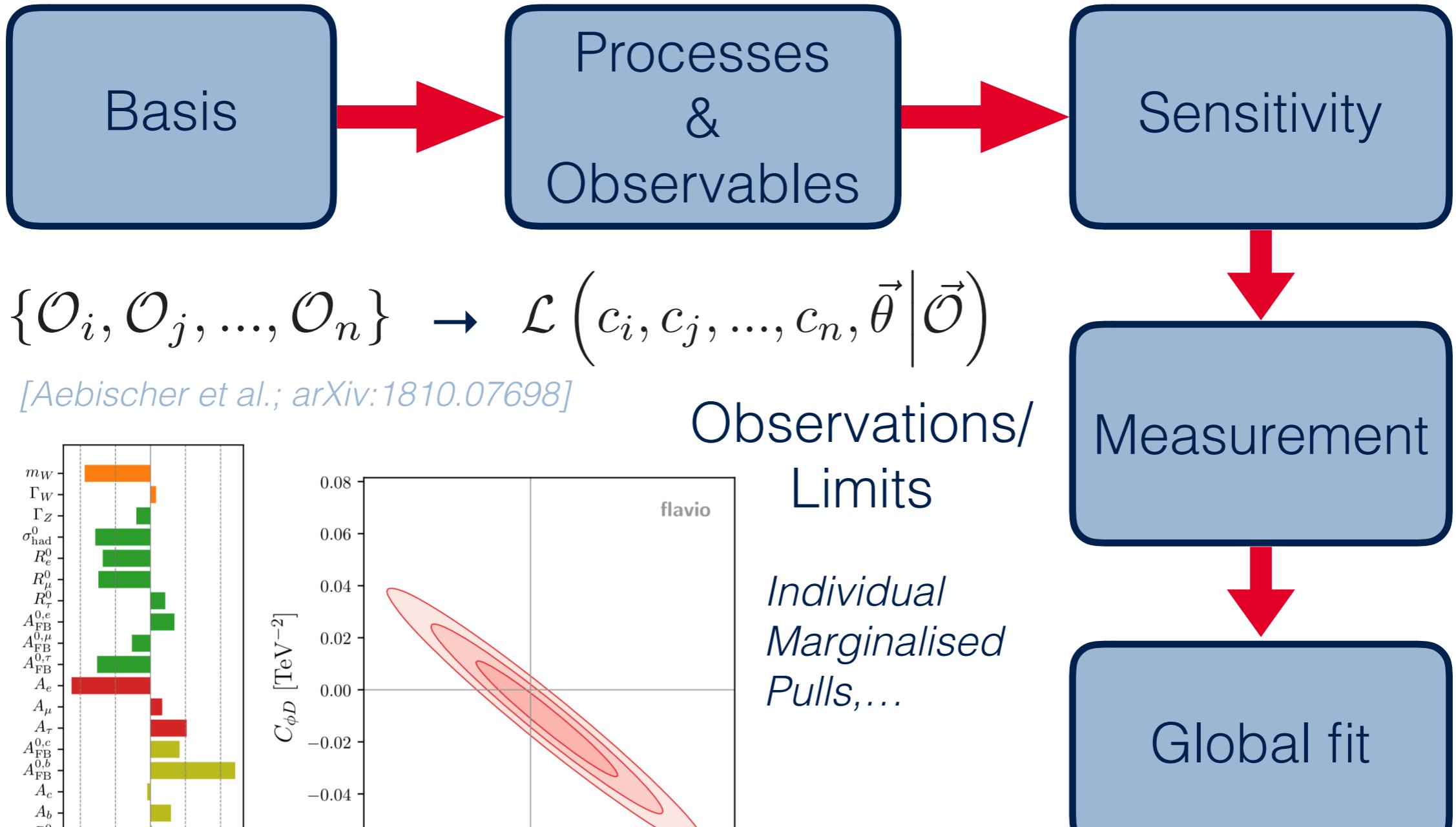


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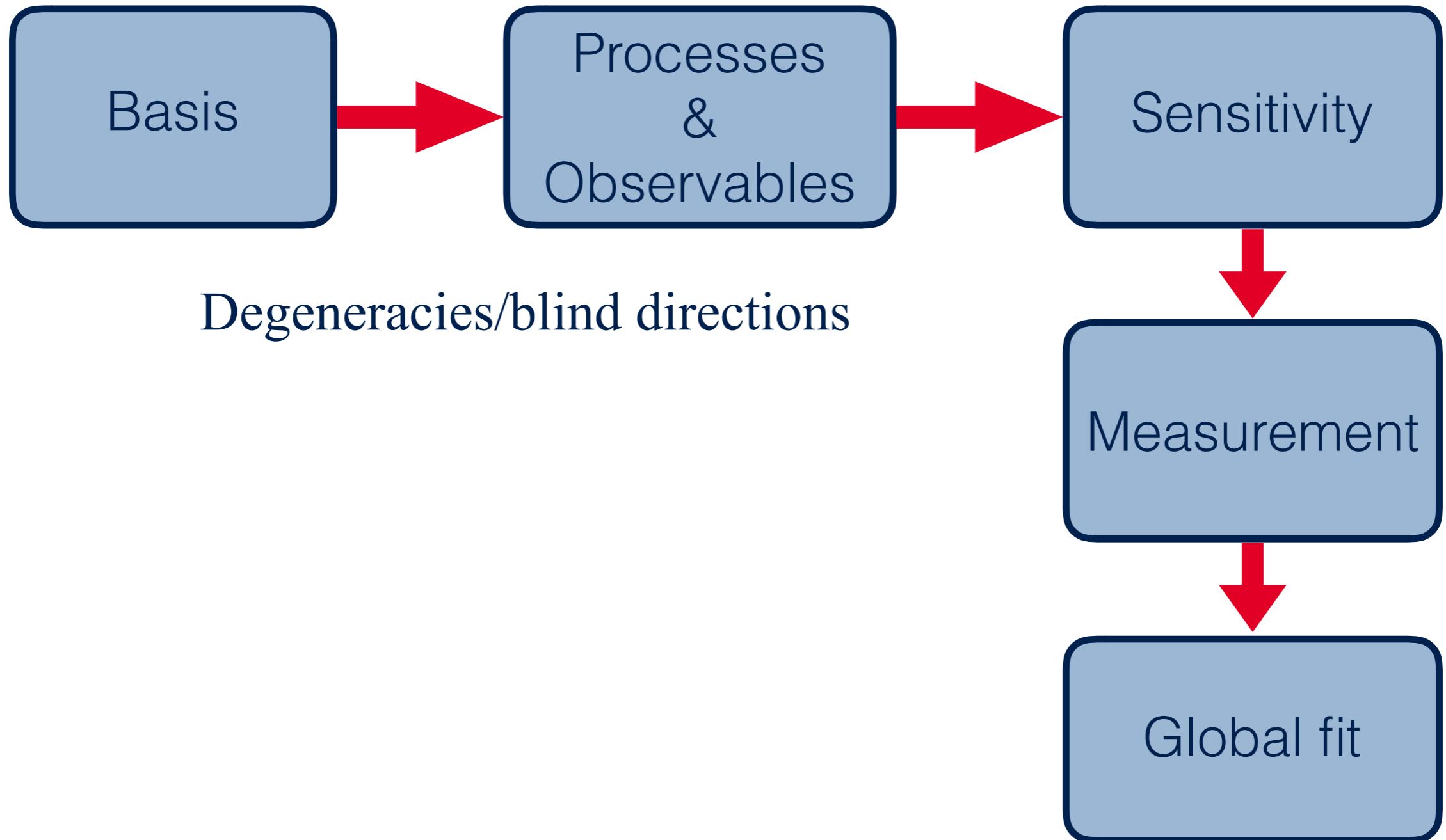
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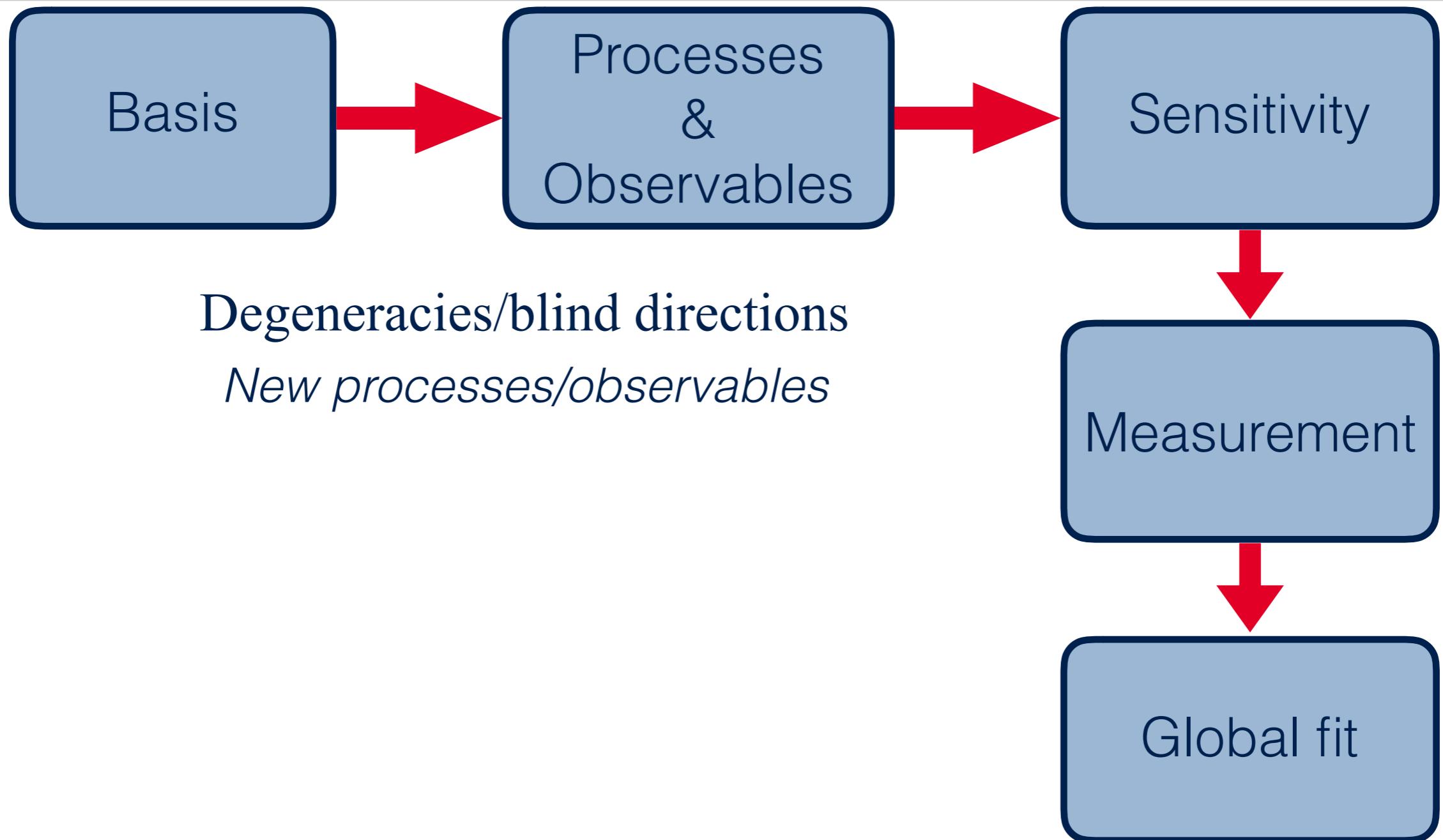
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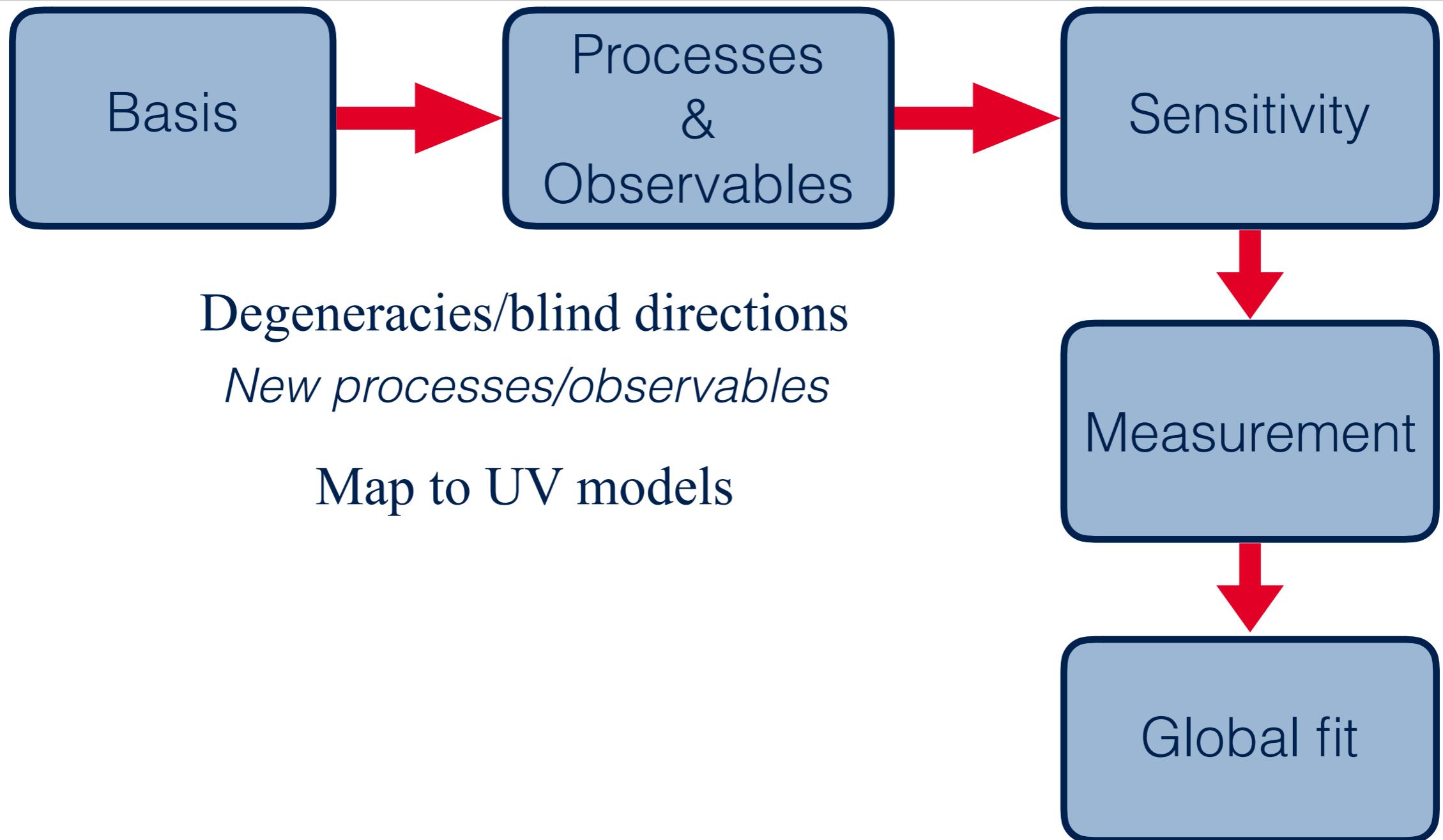
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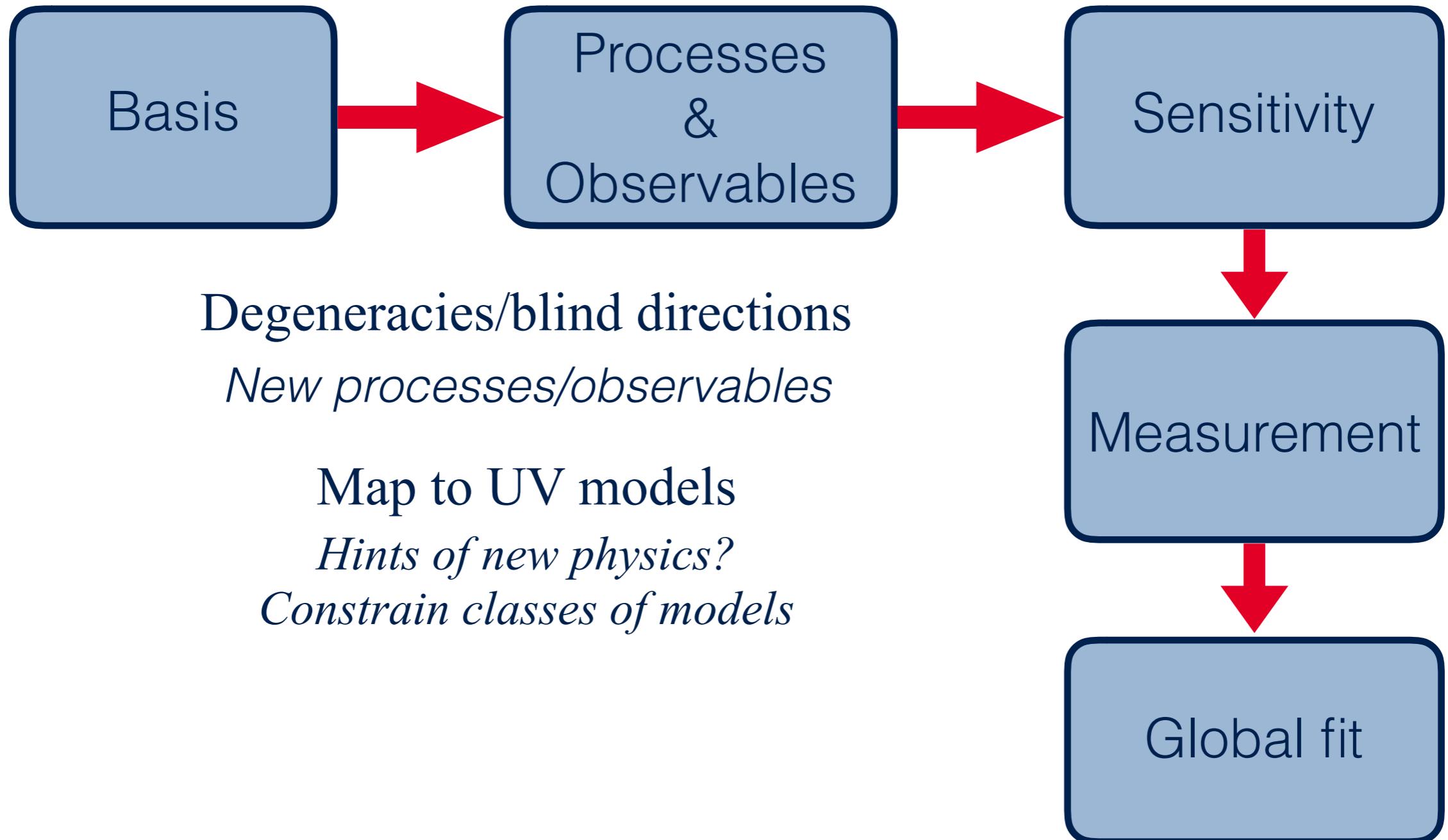
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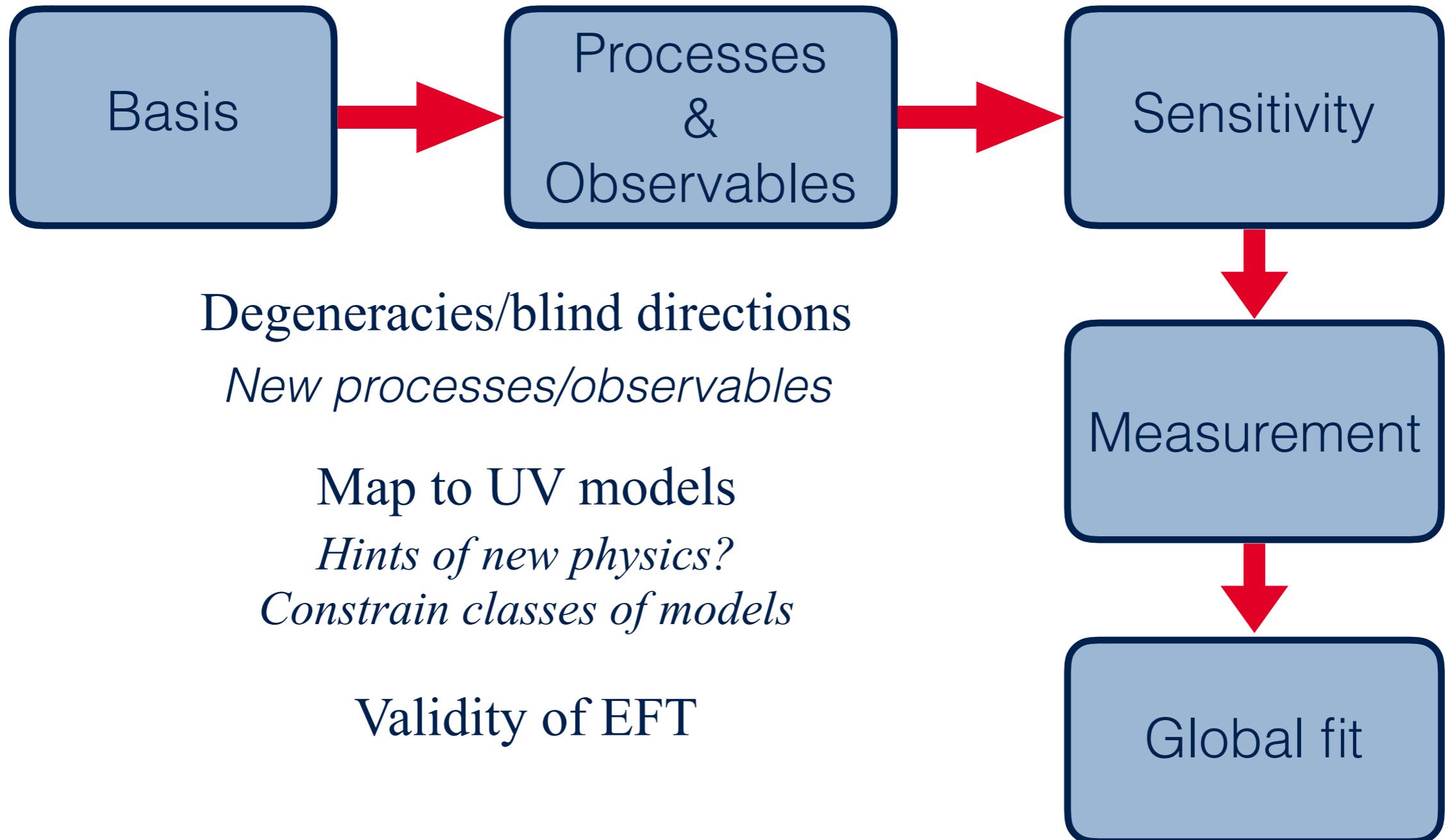
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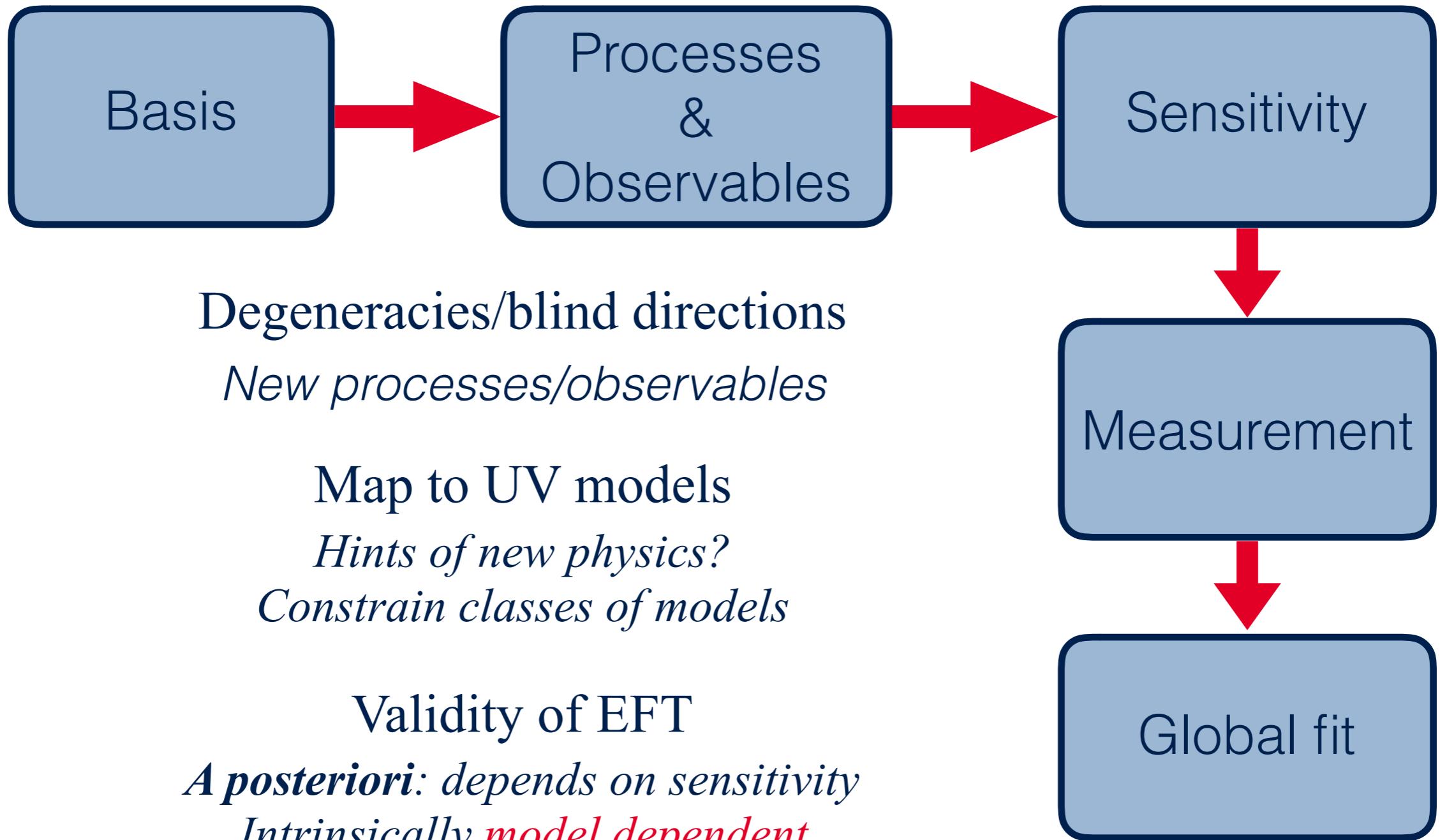
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Statistical tools

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 - ❖ Fit over a subset of coefficients \rightarrow confidence intervals on $\{g_i/M^2\}$

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- ❖ Global interpretation is the holy grail of SMEFT analysis
 - ❖ ‘individual’ constraints (setting other c ’s to 0) are **instructive** but **not robust**
 - ❖ Cancellations (blind directions) among different operators
 - ❖ A priori don’t know which operators will be generated by new physics
 - ❖ Operators **run & mix** under RGE $\rightarrow c=0$ is **scale dependent**
 - ❖ **Symmetries** are the safe way to restrict your parameter space
- ❖ Combine theoretical predictions & experimental data
 - ❖ Likelihood function in coefficient space \rightarrow confidence intervals on $\{c_i/\Lambda^2\}$
 - ❖ Model interpretation
 - ❖ Fit over a subset of coefficients \rightarrow confidence intervals on $\{g_i/M^2\}$
- ❖ Need flexible, open source tools to pool knowledge & effort

Rosetta

- ❖ Basis translation tool for SMEFT
- ❖ Underlines **basis independence**
 - ❖ No one basis is the ‘best’, all physically **equivalent**
 - ❖ Some may be more practical for a given study (Higgs, EWPO,...)
- ❖ Command line interface with SLHA input/output
 - ❖ User-defined basis implementations & translations (pure python)
 - ❖ Warsaw, SILH, Higgs Basis, HISZ, HiggsPO,...
- ❖ Provides interfaces to third party codes
 - ❖ Developed in specific bases → increase user base & validation
- ❖ Linked to anomalous couplings model: BSMCharacterisation
 - ❖ FeynRules/UFO for LO event generation

[Falkowski et al.; EPJ C75 (2015) no. 12, 583]

<https://rosetta.hepforge.org>

<http://feynrules.irmp.ucl.ac.be/wiki/BSMCharacterisation>

Rosetta

[Falkowski et al.; EPJ C75 (2015) no. 12, 583]
<https://rosetta.hepforge.org>

```
usage: rosetta [-h] [-s] [-v] [--force] INTERFACE ...  
  
Main Rosetta command-line executable.  
  
Global options:  
  -h, --help            show this help message and exit  
  -s, --silent          Suppress all warnings and take default answers to all  
                        questions  
  -v, --verbose          Activate verbose setting for program output  
  --force              Take default answers to all questions  
  
Arguments:  
  INTERFACE  
    translate      Translate an SLHA input card from one basis to another  
    signalstrengths  Standalone SignalStrengths interface  
    lilith        Standalone Lilith interface  
    defaultcard    Generate an SLHA parameter card for an implemented basis  
    ewpo          EWPO interface  
    ehdecay       Standalone eHDECAY interface  
    dihiggs       Double Higgs production at the LHC
```

```
bin/rosetta translate --flavor=universal -o my_output.dat my_input.dat
```

Smelli

[Aebischer *et al.*; *EPJ C79* (2019) no.6, 509]
<https://smelli.github.io>

Smelli

-
- ❖ Project for global, public SMEFT likelihood

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<https://smelli.github.io>

- ❖ Wrapper around flavio tool



[Straub; arXiv:1810:08132]

<https://flav-io.github.io>

- ❖ Initially developed for flavour physics observables

- ❖ EFT predictions for flavour, EWPO, LFV decays, lepton MDM, neutron EDM

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- ❖ Interface to Wilson tool



[Aebisher *et al.*; EPJ C78 (2018) no.12, 1026]

<https://wilson-eft.github.io>

- ❖ Running SMEFT coefficients down to EW scale

- ❖ Based on DsixTools implementation

[Celis *et al.*; EPJ C77 (2017) no.6, 405]

<https://dsixtools.github.io>

- ❖ Matching to Weak Effective Theory below EW scale + running

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- ❖ “Full stack” suite of global EFT analysis software

- ❖ Common interface: Wilson coefficient exchange format (WCxf)

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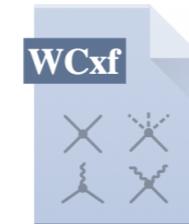
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- ❖ “Full stack” suite of global EFT analysis software

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❖



WCxf

[Aebischer et al.; *Comp. Phys. Comm.* 232 (2018) 71-83]
<https://wcxf.github.io>



WCxf

[Aebischer et al.; *Comp. Phys. Comm.* 232 (2018) 71-83]

<https://wclf.github.io>

Specifically for interfacing SMEFT tools

| Code | Import | Export |
|---------------------|--------|--------|
| DsixTools | ✓ | ✓ |
| EOS | ✓ | |
| flavio | ✓ | ✓ |
| FlavorKit | | ✓ |
| FormFlavor | ✓ | ✓ |
| wilson | ✓ | ✓ |
| SMEFT Feynman Rules | ✓ | ✓ |
| SMEFTsim | ✓ | |
| smelli | ✓ | ✓ |
| SPheNo | | ✓ |
| wclf-python | ✓ | ✓ |



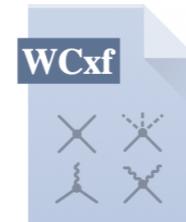
WCxf

[Aebischer et al.; *Comp. Phys. Comm.* 232 (2018) 71-83]
<https://wcxf.github.io>

Specifically for interfacing SMEFT tools

- yaml, json formats for basis definition
- Rosetta-inspired translation functionality
- Predefined Warsaw, WET

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| wilson | ✓ | ✓ |
| SMEFT Feynman Rules | ✓ | ✓ |
| SMEFTsim | ✓ | |
| smelli | ✓ | ✓ |
| SPheNo | | ✓ |
| wcxf-python | ✓ | ✓ |



WCxf

[Aebischer et al.; *Comp. Phys. Comm.* 232 (2018) 71-83]

<https://wclf.github.io>

Specifically for interfacing SMEFT tools

- yaml, json formats for basis definition
- Rosetta-inspired translation functionality
- Predefined Warsaw, WET

EFT file

```
eft: SMEFT
sectors:
  dB=dL=0:
  dB=dL=1:
  dL=2:
```

WC file

```
eft: SMEFT
basis: Warsaw
scale: 1e16
values:
  Gtilde: 3.1e-6
  uphi11:
    Re: 0
    Im: 0.0001
```

```
1  name: Warsaw
2  eft: SMEFT
3  sectors:
4    dB=dL=0:
5    G:
6      real: true
7    Gtilde:
8      real: true
9    W:
10      real: true
11    [...]
12    uphi_11:
13    uphi_12:
14    uphi_13:
15    [...]
```

Basis file

| Code | Import | Export |
|---------------------|--------|--------|
| DsixTools | ✓ | ✓ |
| EOS | ✓ | |
| flavio | ✓ | ✓ |
| FlavorKit | | ✓ |
| FormFlavor | ✓ | ✓ |
| wilson | ✓ | ✓ |
| SMEFT Feynman Rules | ✓ | ✓ |
| SMEFTsim | ✓ | |
| smelli | ✓ | ✓ |
| SPheNo | | ✓ |
| wclf-python | ✓ | ✓ |

Flavorful Higgs & EWPO

[Falkowski & Straub; arXiv:1911:07866, Falkowski & Riva; JHEP 1502 (2015) 039], Efrati et al.; JHEP 1507 (2015) 018]

Flavorful Higgs & EWPO

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- **Flavour general** description → 31 parameters

Flavorful Higgs & EWPO

[Falkowski & Straub; arXiv:1911:07866, Falkowski & Riva; JHEP 1502 (2015) 039], Efrati et al.; JHEP 1507 (2015) 018]

- **Flavour general** description → 31 parameters

| | | | | | |
|-----------------------|---|-----------------------|--|----------------|---|
| Q_G | $f^{ABC} G_\mu^{A\nu} G_\nu^{B\rho} G_\rho^{C\mu}$ | $Q_{\varphi l}^{(1)}$ | $(\varphi^\dagger i \overleftrightarrow{D}_\mu \varphi) (\bar{l} \gamma^\mu l)$ | $Q_{u\varphi}$ | $(\varphi^\dagger \varphi) (\bar{q} u \tilde{\varphi})$ |
| $Q_{\varphi G}$ | $\varphi^\dagger \varphi G_{\mu\nu}^A G^{A\mu\nu}$ | $Q_{\varphi l}^{(3)}$ | $(\varphi^\dagger i \overleftrightarrow{D}_\mu^I \varphi) (\bar{l} \tau^I \gamma^\mu l)$ | $Q_{d\varphi}$ | $(\varphi^\dagger \varphi) (\bar{q} d \varphi)$ |
| $Q_{\varphi B}$ | $\varphi^\dagger \varphi B_{\mu\nu} B^{\mu\nu}$ | $Q_{\varphi e}$ | $(\varphi^\dagger i \overleftrightarrow{D}_\mu \varphi) (\bar{e} \gamma^\mu e)$ | $Q_{e\varphi}$ | $(\varphi^\dagger \varphi) (\bar{l} e \varphi)$ |
| $Q_{\varphi W}$ | $\varphi^\dagger \varphi W_{\mu\nu}^I W^{I\mu\nu}$ | $Q_{\varphi q}^{(1)}$ | $(\varphi^\dagger i \overleftrightarrow{D}_\mu \varphi) (\bar{q} \gamma^\mu q)$ | Q_{ll} | $(\bar{l} \gamma_\mu l) (\bar{l} \gamma^\mu l)$ |
| $Q_{\varphi WB}$ | $\varphi^\dagger \tau^I \varphi W_{\mu\nu}^I B^{\mu\nu}$ | $Q_{\varphi q}^{(3)}$ | $(\varphi^\dagger i \overleftrightarrow{D}_\mu^I \varphi) (\bar{q} \tau^I \gamma^\mu q)$ | | |
| $Q_{\varphi \square}$ | $(\varphi^\dagger \varphi) \square (\varphi^\dagger \varphi)$ | $Q_{\varphi u}$ | $(\varphi^\dagger i \overleftrightarrow{D}_\mu \varphi) (\bar{u} \gamma^\mu u)$ | | |
| $Q_{\varphi D}$ | $(\varphi^\dagger D^\mu \varphi)^* (\varphi^\dagger D_\mu \varphi)$ | | | | |
| \mathcal{O}_W | $\varepsilon_{IJK} W_{\mu\nu}^I W^{J,\nu\rho} W^{K,\mu}_\rho$ | | | | |

Flavorful Higgs & EWPO

[Falkowski & Straub; arXiv:1911:07866, Falkowski & Riva; JHEP 1502 (2015) 039], Efrati et al.; JHEP 1507 (2015) 018]

- **Flavour general** description → 31 parameters

Higgs, EWPO
& diboson

| | | | | | |
|-----------------------|---|-----------------------|--|----------------|---|
| Q_G | $f^{ABC} G_\mu^{A\nu} G_\nu^{B\rho} G_\rho^{C\mu}$ | $Q_{\varphi l}^{(1)}$ | $(\varphi^\dagger i \overleftrightarrow{D}_\mu \varphi) (\bar{l} \gamma^\mu l)$ | $Q_{u\varphi}$ | $(\varphi^\dagger \varphi) (\bar{q} u \tilde{\varphi})$ |
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[Falkowski & Straub; arXiv:1911:07866, Falkowski & Riva; JHEP 1502 (2015) 039], Efrati et al.; JHEP 1507 (2015) 018]

- **Flavour general** description → 31 parameters

Constrained
by multijet

Higgs, EWPO
& diboson

| Q_G | $f^{ABC} G_\mu^{A\nu} G_\nu^{B\rho} G_\rho^{C\mu}$ | $Q_{\varphi l}^{(1)}$ | $(\varphi^\dagger i \overleftrightarrow{D}_\mu \varphi) (\bar{l} \gamma^\mu l)$ | $Q_{u\varphi}$ | $(\varphi^\dagger \varphi) (\bar{q} u \tilde{\varphi})$ |
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Flavorful Higgs & EWPO

[Falkowski & Straub; arXiv:1911:07866, Falkowski & Riva; JHEP 1502 (2015) 039], Efrati et al.; JHEP 1507 (2015) 018]

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Higgs, EWPO
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| $Q_{\varphi WB}$ | $\varphi^\dagger \tau^I \varphi W_{\mu\nu}^I B^{\mu\nu}$ | $Q_{\varphi q}^{(3)}$ | $(\varphi^\dagger i \overleftrightarrow{D}_\mu^I \varphi) (\bar{q} \tau^I \gamma^\mu q)$ | Independent f_i, f_j entries | | | |
| $Q_{\varphi \square}$ | $(\varphi^\dagger \varphi) \square (\varphi^\dagger \varphi)$ | $Q_{\varphi u}$ | $(\varphi^\dagger i \overleftrightarrow{D}_\mu \varphi) (\bar{u} \gamma^\mu u)$ | | | | |
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| | |
|----------------|---|
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3rd gen. only

Independent f_i, f_j entries

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3rd gen. only
1st,2nd gen.

Independent f_i, f_j entries

Flavorful Higgs & EWPO

[Falkowski & Straub; arXiv:1911:07866, Falkowski & Riva; JHEP 1502 (2015) 039], Efrati et al.; JHEP 1507 (2015) 018]

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Constrained
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Higgs, EWPO
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| $Q_{\varphi u}$ | $(\varphi^\dagger i \overleftrightarrow{D}_\mu \varphi) (\bar{u} \gamma^\mu u)$ |

| | |
|----------------|---|
| $Q_{u\varphi}$ | $(\varphi^\dagger \varphi) (\bar{q} u \tilde{\varphi})$ |
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3rd gen. only

1st,2nd gen.

Independent f_i, f_j entries

- Input data:
- Z, W pole observables
 - LEP 2 total and differential WW
 - Run 1 & 2 Higgs signal strengths

Results

Results

$$\begin{aligned}
\delta g_L^{W\ell} &= c_{\varphi l}^{(3)} + f(1/2, 0) - f(-1/2, -1), \\
\delta g_L^{Z\ell} &= -\frac{1}{2}c_{\varphi l}^{(3)} - \frac{1}{2}c_{\varphi l}^{(1)} + f(-1/2, -1), \\
\delta g_R^{Z\ell} &= -\frac{1}{2}c_{\varphi e}^{(1)} + f(0, -1), \\
\delta g_L^{Zu} &= \frac{1}{2}c_{\varphi q}^{(3)} - \frac{1}{2}c_{\varphi q}^{(1)} + f(1/2, 2/3), \\
\delta g_L^{Zd} &= -\frac{1}{2}c_{\varphi q}^{(3)} - \frac{1}{2}c_{\varphi q}^{(1)} + f(-1/2, -1/3), \\
\delta g_R^{Zu} &= -\frac{1}{2}c_{\varphi u} + f(0, 2/3), \\
\delta g_R^{Zd} &= -\frac{1}{2}c_{\varphi d} + f(0, -1/3), \\
\delta c_z &= c_{\varphi \square} - \frac{1}{4}c_{\varphi D} - \frac{3}{2}\Delta_{G_F}, \\
c_{z\square} &= \frac{1}{2g_L^2} (c_{\varphi D} + 2\Delta_{G_F}), \\
c_{gg} &= \frac{4}{g_s^2} c_{\varphi G}, \\
c_{\gamma\gamma} &= 4 \left(\frac{1}{g_L^2} c_{\varphi W} + \frac{1}{g_Y^2} c_{\varphi B} - \frac{1}{g_L g_Y} c_{\varphi WB} \right), \\
c_{zz} &= 4 \left(\frac{g_L^2 c_{\varphi W} + g_Y^2 c_{\varphi B} + g_L g_Y c_{\varphi WB}}{(g_L^2 + g_Y^2)^2} \right), \\
c_{z\gamma} &= 4 \left(\frac{c_{\varphi W} - c_{\varphi B} - \frac{g_L^2 - g_Y^2}{2g_L g_Y} c_{\varphi WB}}{g_L^2 + g_Y^2} \right). \\
f(T^3, Q) &\equiv \left\{ -Q \frac{g_L g_Y}{g_L^2 - g_Y^2} c_{\varphi WB} - \mathbf{1} \left(\frac{1}{4} c_{HD} + \frac{1}{2} \Delta_{G_F} \right) \left(T^3 + Q \frac{g_Y^2}{g_L^2 - g_Y^2} \right) \right\} \mathbf{1},
\end{aligned}$$

Results

$$\delta g_L^{W\ell} = c_{\varphi l}^{(3)} + f(1/2, 0) - f(-1/2, -1),$$

$$\delta g_L^{Z\ell} = -\frac{1}{2}c_{\varphi l}^{(3)} - \frac{1}{2}c_{\varphi l}^{(1)} + f(-1/2, -1),$$

$$\delta g_R^{Z\ell} = -\frac{1}{2}c_{\varphi e}^{(1)} + f(0, -1),$$

$$\delta g_L^{Zu} = \frac{1}{2}c_{\varphi q}^{(3)} - \frac{1}{2}c_{\varphi q}^{(1)} + f(1/2, 2/3),$$

$$\delta g_L^{Zd} = -\frac{1}{2}c_{\varphi q}^{(3)} - \frac{1}{2}c_{\varphi q}^{(1)} + f(-1/2, -1/3),$$

$$\delta g_R^{Zu} = -\frac{1}{2}c_{\varphi u} + f(0, 2/3),$$

$$\delta g_R^{Zd} = -\frac{1}{2}c_{\varphi d} + f(0, -1/3),$$

$$\delta c_z = c_{\varphi \square} - \frac{1}{4}c_{\varphi D} - \frac{3}{2}\Delta_{G_F},$$

$$c_{z\square} = \frac{1}{2g_L^2} (c_{\varphi D} + 2\Delta_{G_F}),$$

$$c_{gg} = \frac{4}{g_s^2} c_{\varphi G},$$

$$c_{\gamma\gamma} = 4 \left(\frac{1}{g_L^2} c_{\varphi W} + \frac{1}{g_Y^2} c_{\varphi B} - \frac{1}{g_L g_Y} c_{\varphi WB} \right),$$

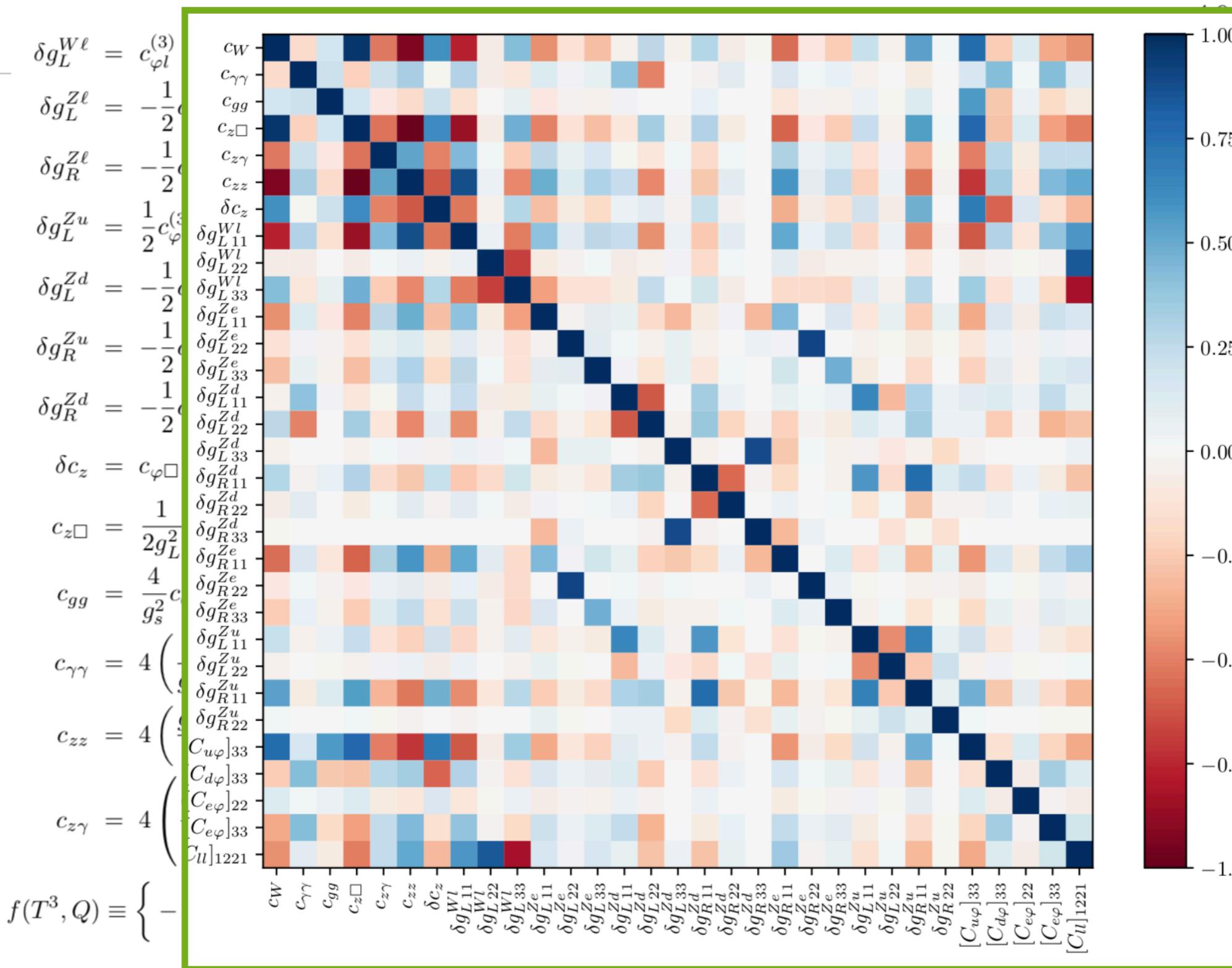
$$c_{zz} = 4 \left(\frac{g_L^2 c_{\varphi W} + g_Y^2 c_{\varphi B} + g_L g_Y c_{\varphi WB}}{(g_L^2 + g_Y^2)^2} \right),$$

$$c_{z\gamma} = 4 \left(\frac{c_{\varphi W} - c_{\varphi B} - \frac{g_L^2 - g_Y^2}{2g_L g_Y} c_{\varphi WB}}{g_L^2 + g_Y^2} \right).$$

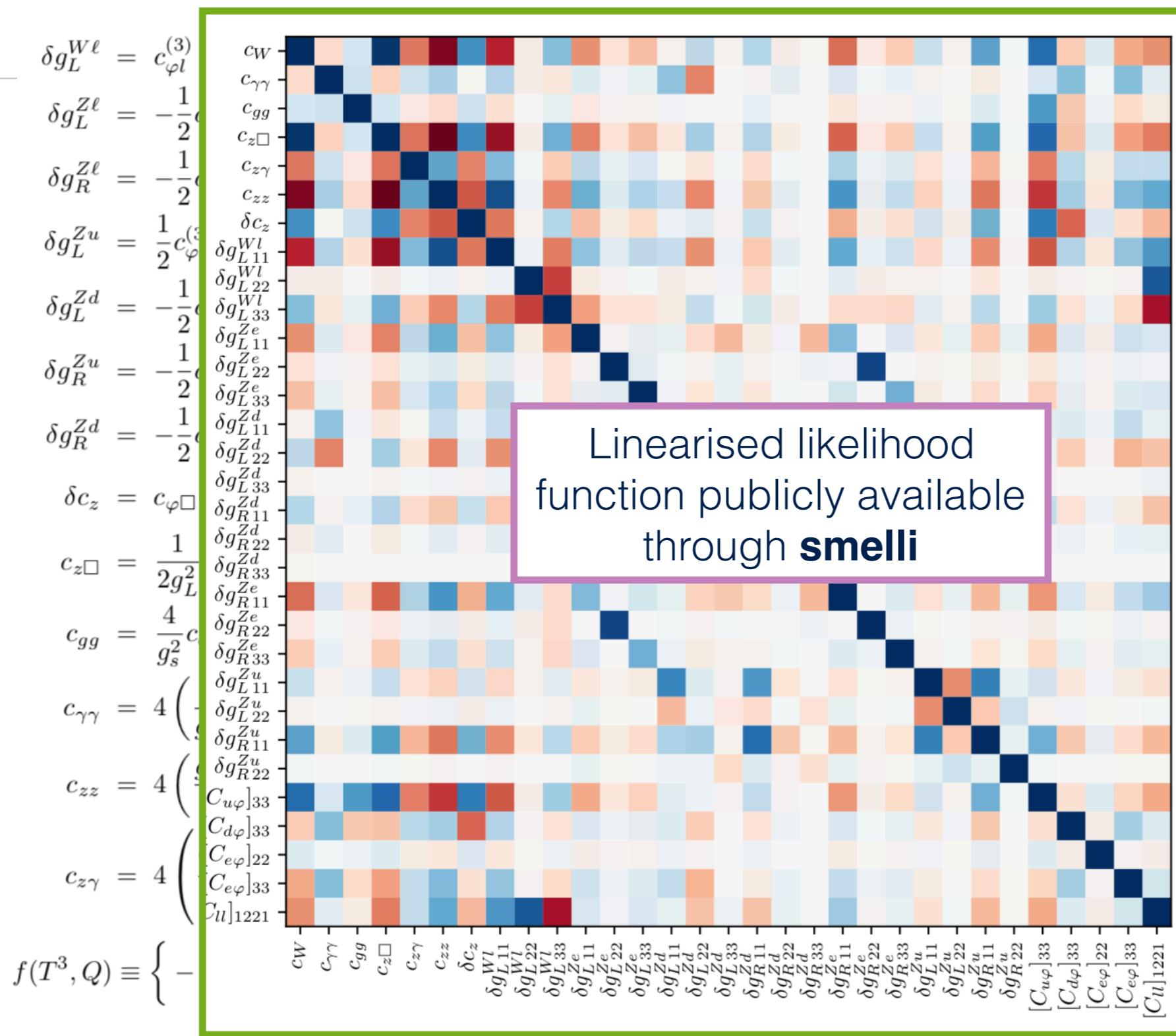
$$f(T^3, Q) \equiv \left\{ -Q \frac{g_L g_Y}{g_L^2 - g_Y^2} c_{\varphi WB} - \mathbf{1} \left(\frac{1}{4} c_{HD} + \frac{1}{2} \Delta_{G_F} \right) \left(T^3 + Q \frac{g_Y^2}{g_L^2 - g_Y^2} \right) \right\} \mathbf{1},$$

| Coeff. | central | unc. | pull [σ] |
|-----------------------|----------------------|------|-------------------|
| C_W | 0.19 ± 1.9 | 0.1 | |
| $c_{\gamma\gamma}$ | -0.056 ± 0.11 | 0.5 | |
| c_{gg} | -0.017 ± 0.014 | 1.2 | |
| $c_{z\square}$ | 4.9 ± 6.2 | 0.8 | |
| $c_{z\gamma}$ | -0.6 ± 0.63 | 1.0 | |
| c_{zz} | -12.0 ± 16.0 | 0.8 | |
| δc_z | 0.49 ± 1.5 | 0.3 | |
| δg_{L11}^{Wl} | -0.09 ± 0.053 | 1.7 | |
| δg_{L22}^{Wl} | -0.24 ± 0.083 | 2.9 | |
| δg_{L33}^{Wl} | 0.26 ± 0.1 | 2.6 | |
| δg_{L11}^{Ze} | -0.0074 ± 0.0052 | 1.4 | |
| δg_{L22}^{Ze} | -0.0014 ± 0.018 | 0.1 | |
| δg_{L33}^{Ze} | -0.0054 ± 0.01 | 0.5 | |
| δg_{L11}^{Zd} | -0.17 ± 0.66 | 0.3 | |
| δg_{L22}^{Zd} | 0.43 ± 0.57 | 0.8 | |
| δg_{L33}^{Zd} | 0.052 ± 0.027 | 1.9 | |
| δg_{R11}^{Zd} | 1.5 ± 1.0 | 1.4 | |
| δg_{R22}^{Zd} | 0.27 ± 0.73 | 0.4 | |
| δg_{R33}^{Zd} | 0.33 ± 0.11 | 3.1 | |
| δg_{R11}^{Ze} | -0.0086 ± 0.0056 | 1.5 | |
| δg_{R22}^{Ze} | -0.0018 ± 0.021 | 0.1 | |
| δg_{R33}^{Ze} | 0.0084 ± 0.01 | 0.8 | |
| δg_{L11}^{Zu} | 0.14 ± 0.5 | 0.3 | |
| δg_{L22}^{Zu} | -0.027 ± 0.072 | 0.4 | |
| δg_{R11}^{Zu} | 1.3 ± 0.85 | 1.5 | |
| δg_{R22}^{Zu} | -0.056 ± 0.084 | 0.7 | |
| $[C_{u\varphi}]_{33}$ | -0.18 ± 2.7 | 0.1 | |
| $[C_{d\varphi}]_{33}$ | 0.016 ± 0.049 | 0.3 | |
| $[C_{e\varphi}]_{22}$ | 0.004 ± 0.0054 | 0.8 | |
| $[C_{e\varphi}]_{33}$ | -0.0018 ± 0.019 | 0.1 | |
| $[C_{ll}]_{1221}$ | -0.68 ± 0.2 | 3.3 | |

Results



Results



| Coeff. | central | unc. | pull [σ] |
|-----------------------|--------------------|------|-------------------|
| C_W | 0.19 ± 1.9 | 0.1 | |
| $c_{\gamma\gamma}$ | -0.056 ± 0.11 | 0.5 | |
| c_{gg} | -0.017 ± 0.014 | 1.2 | |
| $[C_{e\varphi}]^{22}$ | 0.10 | 6.2 | 0.8 |
| $[C_{e\varphi}]^{33}$ | 0.63 | 1.0 | |
| $[C_{ll}]^{1221}$ | 16.0 | 0.8 | |
| $[C_{e\varphi}]^{22}$ | 1.5 | 0.3 | |
| $[C_{e\varphi}]^{33}$ | 0.053 | 1.7 | |
| $[C_{ll}]^{1221}$ | 0.083 | 2.9 | |
| $[C_{e\varphi}]^{22}$ | 0.1 | 2.6 | |
| $[C_{e\varphi}]^{33}$ | 0.0052 | 1.4 | |
| $[C_{ll}]^{1221}$ | 0.018 | 0.1 | |
| $[C_{e\varphi}]^{22}$ | 0.01 | 0.5 | |
| $[C_{e\varphi}]^{33}$ | 0.66 | 0.3 | |
| $[C_{ll}]^{1221}$ | 0.57 | 0.8 | |
| $[C_{e\varphi}]^{22}$ | 0.027 | 1.9 | |
| $[C_{e\varphi}]^{33}$ | 1.0 | 1.4 | |
| $[C_{ll}]^{1221}$ | 0.73 | 0.4 | |
| $[C_{e\varphi}]^{22}$ | 0.11 | 3.1 | |
| $[C_{e\varphi}]^{33}$ | 0.0056 | 1.5 | |
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| $[C_{e\varphi}]^{33}$ | 0.5 | 0.3 | |
| $[C_{ll}]^{1221}$ | 0.072 | 0.4 | |
| $[C_{e\varphi}]^{22}$ | 0.85 | 1.5 | |
| $[C_{e\varphi}]^{33}$ | 0.084 | 0.7 | |
| $[C_{ll}]^{1221}$ | 2.7 | 0.1 | |
| $[C_{e\varphi}]^{22}$ | 0.049 | 0.3 | |
| $[C_{e\varphi}]^{33}$ | 0.0054 | 0.8 | |
| $[C_{ll}]^{1221}$ | 0.019 | 0.1 | |
| $[C_{e\varphi}]^{22}$ | 0.2 | 3.3 | |



[*de Blas et al.*; *arXiv: 1910.14012*]
<http://hepfit.roma1.infn.it>



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- Standard model & extensions (specifically SMEFT)



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Bayesian statistical framework



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Bayesian statistical framework

- Markov-Chain Monte Carlo (MCMC) via Bayesian Analysis Toolkit

[*Caldwell et al.*; *Comp. Phys. Comm. 180 (2009) 2197*]



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Posterior distribution

$$P(\vec{\mathbf{x}}|D) = \frac{P(D|\vec{\mathbf{x}})P_0(\vec{\mathbf{x}})}{\int P(D|\vec{\mathbf{x}})P_0(\vec{\mathbf{x}})d\vec{\mathbf{x}}}$$

Likelihood, Prior &
Bayesian evidence



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Likelihood, Prior &
Bayesian evidence

- Metropolis-Hastings algorithm to sample parameter space from posterior

Observables

- Higgs signal strengths (LHC & Future lepton colliders incl. polarisation)
- EW precision data in (m_Z , α , G_F) scheme
- Flavour observables
- BSM model-specific (incl. theoretical constraints)

HEP

- Standard model

Bayesian statistics

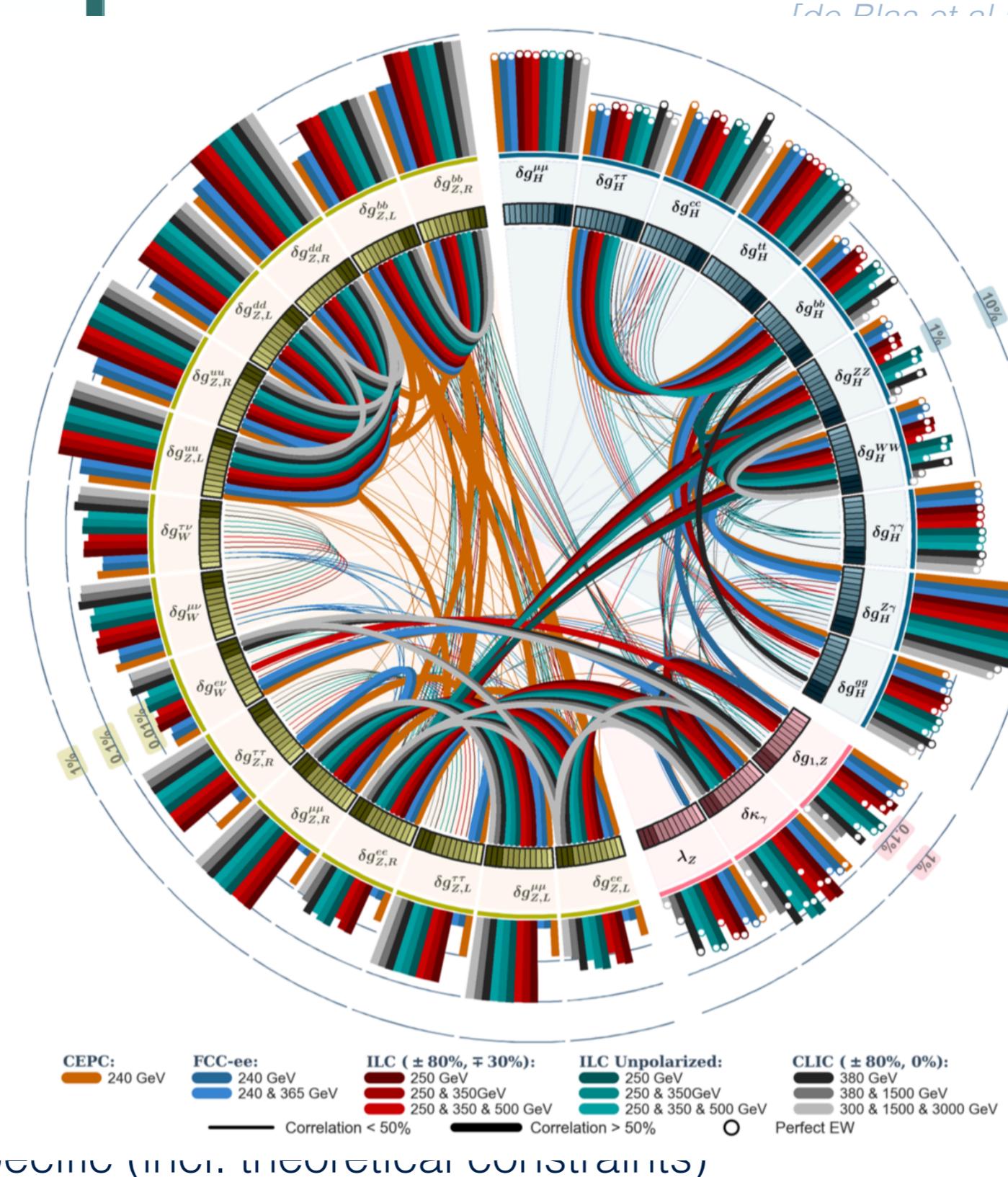
- Markov-Chain

Posterior distribution

- Metropolis-Hastings

Observables

- Higgs signal strength
- EW precision constraints
- Flavour observables
- BSM model-spectrum (from individual constraints)



[D. Blas et al. arXiv: 1910.14012]
pfit.roma1.infn.it

80 (2009) 2197]

d, Prior & evidence posterior