

Know The Complexities!

The Ultimate Cheat-Sheet for Design and Analysis of Computer Algorithms

Heaps

Heaps	Time Complexity						
	Heapify	Find Max	Extract Max	Increase Key	Insert	Delete	Merge
<a href="#">Linked List (sorted)</a>	-	$O(1)$	$O(1)$	$O(n)$	$O(n)$	$O(1)$	$O(m+n)$
<a href="#">Linked List (unsorted)</a>	-	$O(n)$	$O(n)$	$O(1)$	$O(1)$	$O(1)$	$O(1)$
<a href="#">Binary Heap</a>	$O(n)$	$O(1)$	$O(\log(n))$	$O(\log(n))$	$O(\log(n))$	$O(\log(n))$	$O(m+n)$
<a href="#">Binomial Heap</a>	-	$O(\log(n))$	$O(\log(n))$	$O(\log(n))$	$O(\log(n))$	$O(\log(n))$	$O(\log(n))$
<a href="#">Fibonacci Heap</a>	-	$O(1)$	$O(\log(n))^*$	$O(1)^*$	$O(1)$	$O(\log(n))^*$	$O(1)$

Graphs

Node / Edge Management	Storage	Add Vertex	Add Edge	Remove Vertex	Remove Edge	Query
<a href="#">Adjacency list</a>	$O( V + E )$	$O(1)$	$O(1)$	$O( V  +  E )$	$O( E )$	$O( V )$
<a href="#">Incidence list</a>	$O( V + E )$	$O(1)$	$O(1)$	$O( E )$	$O( E )$	$O( E )$
<a href="#">Adjacency matrix</a>	$O( V ^2)$	$O( V ^2)$	$O(1)$	$O( V ^2)$	$O(1)$	$O(1)$
<a href="#">Incidence matrix</a>	$O( V  \cdot  E )$	$O( V  \cdot  E )$	$O( V  \cdot  E )$	$O( V  \cdot  E )$	$O( V  \cdot  E )$	$O( E )$

Searching

Algorithm	Data Structure	Time Complexity		Space Complexity		
		Average	Worst	Worst		
<a href="#">Depth First Search (DFS)</a>	Graph of $ V $ vertices and $ E $ edges	-	$O( E  +  V )$	$O( V )$		
<a href="#">Breadth First Search (BFS)</a>	Graph of $ V $ vertices and $ E $ edges	-	$O( E  +  V )$	$O( V )$		
<a href="#">Binary search</a>	Sorted array of $n$ elements	$O(\log(n))$	$O(\log(n))$	$O(1)$		
<a href="#">Linear (Brute Force)</a>	Array	$O(n)$	$O(n)$	$O(1)$		
<a href="#">Shortest path by Dijkstra, using a Min-heap as priority queue</a>	Graph with $ V $ vertices and $ E $ edges	$O(( V  +  E ) \log  V )$	$O(( V  +  E ) \log  V )$	$O( V )$		
<a href="#">Shortest path by Dijkstra, using an unsorted array as priority queue</a>	Graph with $ V $ vertices and $ E $ edges	$O( V ^2)$	$O( V ^2)$	$O( V )$		
<a href="#">Shortest path by Bellman-Ford</a>	Graph with $ V $ vertices and $ E $ edges	$O( V   E )$	$O( V   E )$	$O( V )$		

# Sorting

Algorithm	Data Structure	Time Complexity			Worst Case Auxiliary Space Complexity
		Best	Average	Worst	Worst
<a href="#">Quicksort</a>	Array	$O(n \log(n))$	$O(n \log(n))$	$O(n^2)$	$O(n)$
<a href="#">Mergesort</a>	Array	$O(n \log(n))$	$O(n \log(n))$	$O(n \log(n))$	$O(n)$
<a href="#">Heapsort</a>	Array	$O(n \log(n))$	$O(n \log(n))$	$O(n \log(n))$	$O(1)$
<a href="#">Bubble Sort</a>	Array	$O(n)$	$O(n^2)$	$O(n^2)$	$O(1)$
<a href="#">Insertion Sort</a>	Array	$O(n)$	$O(n^2)$	$O(n^2)$	$O(1)$
<a href="#">Select Sort</a>	Array	$O(n^2)$	$O(n^2)$	$O(n^2)$	$O(1)$
<a href="#">Bucket Sort</a>	Array	$O(n+k)$	$O(n+k)$	$O(n^2)$	$O(nk)$
<a href="#">Radix Sort</a>	Array	$O(nk)$	$O(nk)$	$O(nk)$	$O(n+k)$

# Data Structures

Data Structure	Time Complexity								Space Complexity
	Average				Worst				Worst
	Indexing	Search	Insertion	Deletion	Indexing	Search	Insertion	Deletion	
<a href="#">Basic Array</a>	$O(1)$	$O(n)$	-	-	$O(1)$	$O(n)$	-	-	$O(n)$
<a href="#">Dynamic Array</a>	$O(1)$	$O(n)$	$O(n)$	$O(n)$	$O(1)$	$O(n)$	$O(n)$	$O(n)$	$O(n)$
<a href="#">Singly-Linked List</a>	$O(n)$	$O(n)$	$O(1)$	$O(1)$	$O(n)$	$O(n)$	$O(1)$	$O(1)$	$O(n)$
<a href="#">Doubly-Linked List</a>	$O(n)$	$O(n)$	$O(1)$	$O(1)$	$O(n)$	$O(n)$	$O(1)$	$O(1)$	$O(n)$
<a href="#">Skip List</a>	$O(\log(n))$	$O(\log(n))$	$O(\log(n))$	$O(\log(n))$	$O(n)$	$O(n)$	$O(n)$	$O(n)$	$O(n \log(n))$
<a href="#">Hash Table</a>	-	$O(1)$	$O(1)$	$O(1)$	-	$O(n)$	$O(n)$	$O(n)$	$O(n)$
<a href="#">Binary Search Tree</a>	$O(\log(n))$	$O(\log(n))$	$O(\log(n))$	$O(\log(n))$	$O(n)$	$O(n)$	$O(n)$	$O(n)$	$O(n)$
<a href="#">Cartresian Tree</a>	-	$O(\log(n))$	$O(\log(n))$	$O(\log(n))$	-	$O(n)$	$O(n)$	$O(n)$	$O(n)$
<a href="#">B-Tree</a>	$O(\log(n))$	$O(\log(n))$	$O(\log(n))$	$O(\log(n))$	$O(\log(n))$	$O(\log(n))$	$O(\log(n))$	$O(\log(n))$	$O(n)$
<a href="#">Red-Black Tree</a>	$O(\log(n))$	$O(\log(n))$	$O(\log(n))$	$O(\log(n))$	$O(\log(n))$	$O(\log(n))$	$O(\log(n))$	$O(\log(n))$	$O(n)$
<a href="#">Splay Tree</a>	-	$O(\log(n))$	$O(\log(n))$	$O(\log(n))$	-	$O(\log(n))$	$O(\log(n))$	$O(\log(n))$	$O(n)$
<a href="#">AVL Tree</a>	$O(\log(n))$	$O(\log(n))$	$O(\log(n))$	$O(\log(n))$	$O(\log(n))$	$O(\log(n))$	$O(\log(n))$	$O(\log(n))$	$O(n)$