

## Lecture 16:-

## REPRESENTING

## RELATIONS.

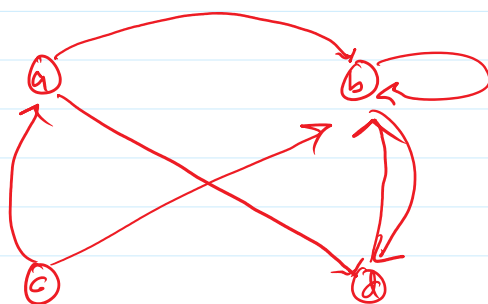
GRAPHS:-

Vertices  $\emptyset$  } Syntax.  
Edges / Arcs  $\rightarrow$  }

Set of Vertices. } Semantics.  
Set of Edges. }

Ex 7 :-  
479.

Set of Vertices =  $\{a, b, c, d\}$ .  
" " " " "  $= \{(a,b), (a,d), (b,b), (b,d), (c,a), (c,b), (d,b)\}$ .



## REPRESENTING RELATIONS USING GRAPHS

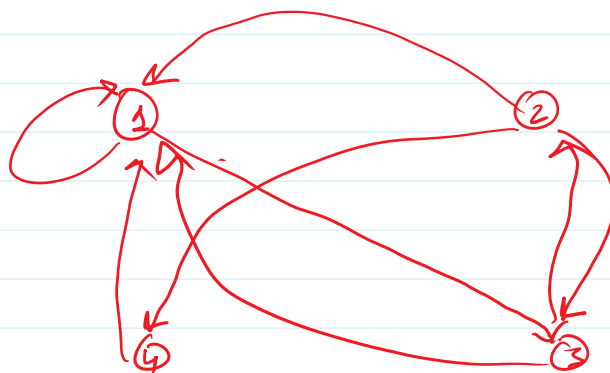
Ex 8 :-  
480

Set of Vertices = SET ON WHICH RELATION DEFINED.  
 $V = A$

Set of Edges =  $R$ .

$R = \{(1,1), (1,3), (2,1), (2,3), (2,4), (3,1), (3,2), (4,1)\}$ .

$A = \{1, 2, 3, 4\}$ .



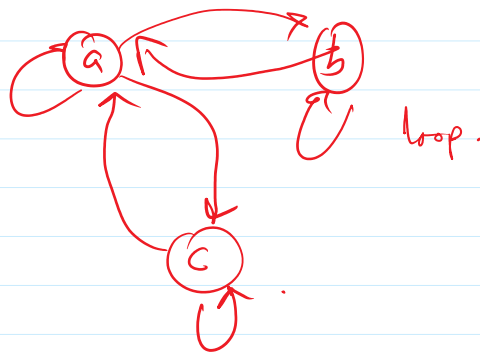
→ 3 Equivalent forms of Relations.

→ Relation on Set

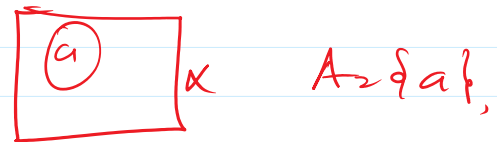
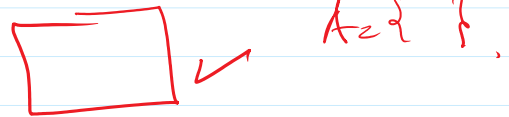
→ " " Matrix.

→ " " Graph.

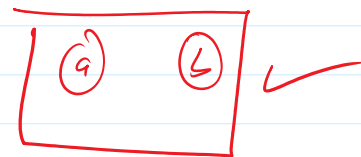
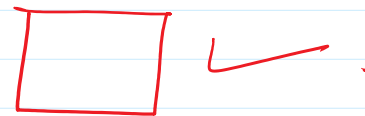
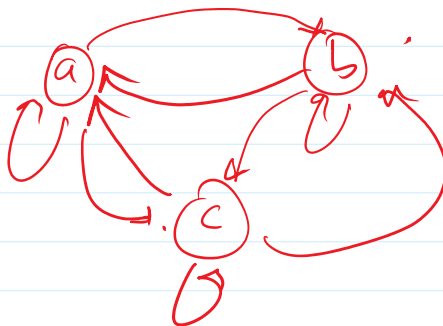
REFLEXIVE:  $\forall a \in A \quad (a,a) \in R$ .



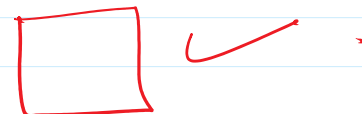
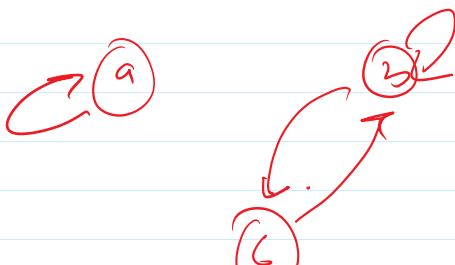
$A = \{a, b\}$

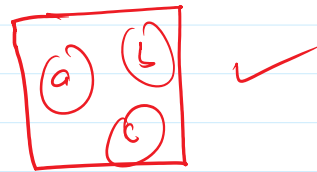
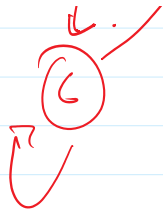


Symmetric:  $\forall a, b \in A \quad (a,b) \in R \rightarrow (b,a) \in R$ .



Anti Symmetric:  $\forall a, b \in A \quad \text{if } (a,b) \in R \wedge (b,a) \in R \rightarrow a=b$ .





Transitive:-  $\forall a, b, c \in A$  if  $(a, b) \in R \wedge (b, c) \in R \rightarrow (a, c) \in R$

