EFFECTS OF ANTENNA BEAM CHROMATICITY ON REDSHIFTED 21 CM POWER SPECTRUM AND IMPLICATIONS FOR HYDROGEN EPOCH OF REIONIZATION ARRAY

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ABSTRACT

Unaccounted systematics from foregrounds and instruments prevent current experiments from detecting redshifted 21 cm signal from the Epoch of Reionization (EoR). We identify spectral structures (chromaticity) in the antenna power pattern as one such systematic that significantly affects all EoR measurements. Increase in chromaticity of the antenna beam causes the already bright foreground power to leak well beyond ideal limits and contaminate the otherwise clean EoR signal modes. A primary source of this chromaticity is reflections in the antenna-feed assembly and between structures in neighboring antennas. Using precise foreground simulations taking wide-field effects into account, we provide a framework to set cosmologically-motivated design specifications on these reflections to prevent further EoR signal degradation. We use the Hydrogen Epoch of Reionization Array (HERA) as an example. Using a simple and yet high dynamic range spectral weighting scheme, we demonstrate that EoR detection using HERA will not be impeded by such spectral systematics even in a conservative scenario that does not perform removal of foregrounds. We also show that all baselines in a 19-element HERA layout are capable of detecting EoR over a substantial observing window on the sky.

Keywords: cosmology: observations — dark ages, reionization, first stars — instrumentation: interferometers — large-scale structure of universe — radio continuum: galaxies — techniques: interferometric

1. INTRODUCTION

The Epoch of Reionization (EoR) is an important period of nonlinear growth of matter density perturbations and astrophysical evolution leading to the large scale structure observed currently in the Universe. The redshifted neutral hydrogen from the IGM in this epoch has been identified to be one of the most promising and direct probes of the EoR (Sunyaev & Zeldovich 1972; Scott & Rees 1990; Madau et al. 1997; Tozzi et al. 2000; Iliev et al. 2002).

Numerous experiments using low frequency radio telescopes targeting the redshifted 21 cm line from the spinflip transition of HI in this epoch have become operational such as the Murchison Widefield Array (MWA; Lonsdale et al. 2009; Bowman et al. 2013; Tingay et al. 2013), the Donald C. Backer Precision Array for Probing the Epoch of Reionization (PAPER; Parsons et al. 2010), the Low Frequency Array (LOFAR; van Haarlem et al. 2013) and the Giant Metrewave Radio Telescope EoR experiment (GMRT; Paciga et al. 2013). Many of these instruments have sufficient sensitivity for a statistical detection of the EoR signal by estimating the spatial power spectrum of the redshifted HI spin temperature fluctuations (Beardsley et al. 2013; Thyagarajan et al. 2013). These instruments are intended to be precursors and pathfinders to the next generation of low frequency radio observatories such as the Hydrogen Epoch of Reionization Array² (HERA; DeBoer et al. 2016) and the Square Kilometre Array³ (SKA). These next-generation instruments will advance the capability from a mere statistical detection of the signal to a direct three-dimensional tomographic imaging of HI from the EoR.

The most significant challenge to low frequency EoR observations arises from the extremely bright Galactic and extragalactic foreground synchrotron emission which are $\sim 10^4$ times stronger than the desired EoR signal (Di Matteo et al. 2002; Ali et al. 2008; Bernardi et al. 2009, 2010; Ghosh et al. 2012). However, there are inherent differences in spatial isotropy and spectral smoothness between the EoR signal and the foregrounds (see, e.g., Furlanetto & Briggs 2004; Morales & Hewitt 2004; Zaldarriaga et al. 2004; Santos et al. 2005; Furlanetto et al. 2006; McQuinn et al. 2006; Morales et al. 2006; Wang et al. 2006; Gleser et al. 2008).

When expressed in the coordinate system of power spectrum measurements described by the three-dimensional wavenumber (k), the foreground emission is restricted to a wedge-shaped region commonly referred to as the foreground wedge (Bowman et al. 2009; Liu et al. 2009, 2014a,b; Datta et al. 2010; Liu & Tegmark 2011; Ghosh et al. 2012; Morales et al. 2012; Parsons et al. 2012b; Trott et al. 2012; Vedantham et al. 2012; Dillon et al. 2013; Pober et al. 2013; Thyagarajan et al. 2013; Dillon et al. 2014) bounded by the horizon limits (Parsons et al. 2012b), whereas the EoR signal has spherical symmetry due to its isotropy. The region of k-space excluding the foreground wedge is commonly referred to as

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³ https://www.skatelescope.org/

the EoR window since it is expected to be relatively free of foreground contamination.

Despite attempts to exploit this knowledge about differences in spectral and spatial symmetry, first-generation experiments have at best only led to weak constraints on reionization models (Ali et al. 2015; Dillon et al. 2015; Pober et al. 2015). This is because their sensitivity is primarily limited by instrumental and foreground systematics. The extreme dynamic range required to suppress foreground and instrument systematics demands high precision modeling of foregrounds as observed by modern wide-field instruments.

In this paper, we explore a phenomenon that inherently extends foreground power beyond the *wedge*, namely, that arising from the chromaticity of the antenna power pattern. While highlighting the importance of such instrumental systematics on future EoR experiments, we demonstrate that the current HERA instrument design will exceed these specifications to detect the EoR signal with high significance. This will hold true when data is limited by foregrounds and systematics even in the most conservative scenario which involves neither foreground subtraction nor optimal analysis techniques but only relies on a simple spectral weighting scheme.

This paper is organized as follows. §2 describes the HERA instrument. A brief summary of the delay spectrum technique used extensively in this analysis and the recently confirmed wide-field instrument effects are presented in §3. §4 describes foreground simulations including antenna beam pattern, all-sky foreground models and two independent EoR models. §5 investigates the effects of chromaticity of antenna beam on the resulting delay power spectrum and the cosmologically motivated constraints it places on reflections in the instrument. EoR-foreground dynamic range of HERA under simple foreground avoidance criteria are demonstrated in §6. Our findings are summarized in §7.

2. THE HYDROGEN EPOCH OF REIONIZATION ARRAY

DeBoer et al. (2016) describe the HERA instrument in detail. Here, we provide a brief summary of the telescope currently under construction on the South African SKA site.

The primary science goal of HERA is to widen our understanding of the first stars, galaxies, and black holes, and their role in driving reionization. Through power-spectral measurements of the redshifted 21cm line of HI in the primordial IGM, HERA aims to directly constrain the topology and evolution of reionization, opening a unique window into the complex astrophysical interplay between the first luminous objects and their environments. HERA builds on the advances of first-generation 21cm EoR experiments, particularly PAPER, MWA, the MIT EoR experiment (MITEOR; Zheng et al. 2014) and the Experiment to Detect the Global EoR Step (EDGES; Bowman & Rogers 2010).

HERA will deploy 14 m fixed zenith-pointing parabolic dishes that strike an optimal balance between sensitivity and systematics. The large collecting area of a HERA element yields ≈ 5 times the sensitivity of an MWA tile and more than 20 times that of a PAPER element.

320 core elements of HERA will be arranged in a compact hexagonal grid, split into three displaced segments to cover the uv-plane with sub-element sampling density.

The core will be supplemented by 30 additional outrigger elements to tile the uv-plane with instantaneously complete sub-aperture sampling out to 250λ and complete aperture-scale sampling out to 350λ (at 150 MHz). The layout and its advantages are discussed in Dillon & Parsons (2016).

In this study, we use the HERA-19 hexagonal array layout, a small subset of the planned layout that are currently in use. Without loss of generality, the analysis and results in this paper will apply to the full proposed layout as well.

3. DELAY SPECTRUM

A brief description of the delay spectrum technique (Parsons et al. 2012a,b) is provided here. We borrow the notation used in Thyagarajan et al. (2015a).

Visibilities measured by an interferometer are given by (van Cittert 1934; Zernike 1938; Thompson et al. 2001):

$$V_b(f) = \iint_{\text{skv}} A(\hat{\boldsymbol{s}}, f) I(\hat{\boldsymbol{s}}, f) e^{-i2\pi f \frac{\boldsymbol{b} \cdot \hat{\boldsymbol{s}}}{c}} d\Omega, \qquad (1)$$

where, \boldsymbol{b} is the vector joining antenna pairs (commonly referred to as the baseline vector), $\hat{\boldsymbol{s}}$ is the unit vector denoting direction on the sky, f denotes frequency, c is the speed of light, $d\Omega$ is the solid angle element to which $\hat{\boldsymbol{s}}$ is the unit normal vector, $I(\hat{\boldsymbol{s}},f)$ and $A(\hat{\boldsymbol{s}},f)$ are the sky brightness and antenna's directional power pattern, respectively, as a function of $\hat{\boldsymbol{s}}$ and f. The delay spectrum, $\tilde{V}_b(\tau)$, is defined as the inverse Fourier transform of $V_b(f)$ along the frequency coordinate:

$$\tilde{V}_b(\tau) \equiv \int V_b(f) W(f) e^{i2\pi f \tau} df, \qquad (2)$$

where, W(f) is a spectral weighting function which can be chosen to control the quality of the delay spectrum (Vedantham et al. 2012; Thyagarajan et al. 2013), and τ represents the signal delay between antenna pairs:

$$\tau = \frac{\mathbf{b} \cdot \hat{\mathbf{s}}}{c}.\tag{3}$$

The delay spectrum has a close resemblance to cosmological H I spatial power spectrum and is defined as:

$$P_{\rm d}(\mathbf{k}_{\perp}, k_{\parallel}) \equiv |\tilde{V}_b(\tau)|^2 \left(\frac{1}{\Omega \Delta B}\right) \left(\frac{D^2 \Delta D}{\Delta B}\right) \left(\frac{\lambda^2}{2k_{\rm B}}\right)^2, \tag{4}$$

with

$$\mathbf{k}_{\perp} \equiv \frac{2\pi(\frac{\mathbf{b}}{\lambda})}{D},$$
 (5)

$$k_{\parallel} \equiv \frac{2\pi\tau \, f_{21} H_0 \, E(z)}{c(1+z)^2},$$
 (6)

where, ΔB is the bandwidth, λ is the wavelength of the band center, $k_{\rm B}$ is the Boltzmann constant, \mathbf{k}_{\perp} and k_{\parallel} are the transverse (on the sky) and line-of-sight (into the sky) wavenumbers respectively, f_{21} is the rest-frame frequency of the 21 cm spin-flip transition of H I, z is the redshift, $D \equiv D(z)$ is the transverse comoving distance, ΔD is the comoving depth along the line of sight corresponding to ΔB , and h, H_0 and $E(z) \equiv [\Omega_{\rm M}(1+z)^3 + \Omega_{\rm k}(1+z)^3]$

 $(z)^2 + \Omega_{\Lambda}^{-1/2}$ are standard terms in cosmology. Following Parsons et al. (2014),

$$\Omega \Delta B = \iint |A(\hat{\mathbf{s}}, f) W(f)|^2 d\Omega df, \qquad (7)$$

which is related to the cosmic volume probed by the instrument. In this paper, we use $\Omega_{\rm M}=0.27,\,\Omega_{\Lambda}=0.73,\,\Omega_{\rm K}=1-\Omega_{\rm M}-\Omega_{\Lambda},\,H_0=100\,{\rm km\,s^{-1}\,Mpc^{-1}},\,$ and $P_{\rm d}({\bf k_{\perp}},k_{\parallel})$ is in units of ${\rm K^2}(h^{-1}\,{\rm Mpc})^3$.

We note that these visibilities and delay power spectra are dependent on right ascension (RA) of the pointing as well as the frequency band. However, we defer expressing them explicitly as a function of pointing and center frequency (or redshift) to later sections where it becomes necessary.

It was recently discovered that in wide-field measurements diffuse foreground emission from wide off-axis angles appears enhanced in the delay spectrum near the edges of the foreground wedge even on wide antenna spacings (Thyagarajan et al. 2015a). Called the pitchfork effect, this arises due to severe foreshortening of baseline vectors towards the horizon along joining the antenna pairs thereby enhancing their sensitivity to large scale structures in these directions. Since delay spectrum maps directions on the sky to delay bins, the emission from large scales near the horizon appears enhanced in delay bins near the horizon limits of the foreground wedge. Since these delay modes lie adjacent to those considered sensitive to the EoR signal, they cause a significant contamination of line-of-sight modes critical for EoR signal detection. These findings were confirmed in MWA observations (Thyagarajan et al. 2015b).

It was also demonstrated in these studies that design of antenna power pattern, specifically its amplitude near the horizon, is an important tool in mitigating foreground contamination caused by these wide-field effects. A dish characterized by a nominal Airy pattern was found to mitigate this contamination by over four and two orders of magnitude relative to a dipole and a phased array of dipoles respectively. HERA has significantly based its antenna design principles on these findings in choosing its antenna geometry.

In this paper, we investigate the spectral properties of the proposed dish design through their effects on the resultant foreground delay power spectrum and the constraints they place on attenuation required to suppress reflections in the instrument.

4. SIMULATIONS

We simulate wide-field visibilities for 19-element HERA from all-sky antenna power pattern and fore-ground models using the $PRISim^4$ software package. The simulations cover 24 hr of observation in drift mode consisting of 80 accumulations spanning 1080 s each. The total bandwidth is 100 MHz centered on 150 MHz consisting of 256 channels with 390.625 kHz frequency resolution. The models used are described below.

4.1. Antenna Power Pattern

The High Frequency Structural Simulator (HFSS) was used to model the dish and its angular response used in

⁴ The Precision Radio Interferometry Simulator (PRISim) is publicly available at https://github.com/nithyanandan/PRISim

this study. The HFSS model used prime focus optics with a 14 m faceted parabola with a spar f/D ratio of 0.32. The model has a 1 m central hole in the aluminum surface which is filled with a dielectric material similar to dry soil. The feed used a full PAPER dipole inside of a cylindrical backplane, the backplane is modeled as an aluminum surface. For the metal parts of the dipole, the discs were modeled as aluminum at the actual size, and the arms and terminals were modeled as copper. Dielectric stand-offs and supporting members were included. For the calculations, one pair of arms was excited using a modal port. These models cover a frequency range of 90–210 MHz in intervals of 1 MHz (DeBoer et al. 2016).

For reference, we use two other models for the antenna power pattern. The first is a nominal Airy pattern corresponding to a uniformly illuminated circular aperture of 14 m diameter and the second is an achromatic model where the response of the design at 150 MHz of the HFSS model described above was fixed as the hypothetical response at all frequencies covering the entire band. This frequency independent model will be used to isolate the effects of spectral structures in the antenna power pattern (or beam chromaticity) on foreground delay power spectra. Hereafter, we refer to these three beams as 'simulated', 'Airy' and 'achromatic' models.

In a related series of papers, Neben et al. (2016) discuss the agreement of these simulated antenna beam patterns with actual measurements, Ewall-Wice et al. (2016) model the reflections and return loss expected in the proposed antenna-feed assembly, and Patra et al. (2016) present measurements quantifying the reflections. Our focus in this paper is to investigate chromaticity of antenna power patterns from the point of view of their impact on foreground contamination in delay power spectra.

4.2. Foreground Model

Our all-sky foreground model is the same as the one in Thyagarajan et al. (2015a). It consists of diffuse emission (de Oliveira-Costa et al. 2008) and point sources. The latter is obtained from a combination of the NRAO VLA Sky Survey (NVSS; Condon et al. 1998) at 1.4 GHz and the Sydney University Molonglo Sky Survey (SUMSS; Bock et al. 1999; Mauch et al. 2003) at 843 MHz with a mean spectral index of -0.83. The diffuse sky model has an angular resolution of 13'.74 and a spectral index estimated for every pixel.

$4.3. \ EoR \ Models$

We use two models of EoR. In the first, simulations of the HI signal were created using the publicly available $21 \mathrm{cmFAST^5}$ code described in Mesinger et al. (2011). The code uses the excursion set formalism of Furlanetto et al. (2004) to generate ionization and 21cm brightness fields for numerous redshifts. The model shown in this paper assumes the same fiducial values as in Ewall-Wice et al. (2016): $T_{\mathrm{vir}}^{\min} = 2 \times 10^4$ K (virial temperature of minimum mass of dark matter halos that host ionizing sources), $\zeta = 20$ (ionization efficiency), and $R_{\mathrm{mfp}} = 15$ Mpc (mean free path of UV photons) which predicts the redshift of 50% ionization (and hence a peak

⁵ http://homepage.sns.it/mesinger/DexM__21cmFAST.html

in the power spectrum signal) to be at z=8.5. The second EoR model is from the simulations described in detail in Lidz et al. (2008). Hereafter, we refer to these two as EoR models 1 and 2 respectively.

5. CHROMATICITY OF POWER PATTERN

The equation for delay spectrum describes the mapping between sky location of a foreground object and delay. The chromatic nature (variation with frequency) of the antenna power pattern appears multiplicatively in the frequency axis and thus results in convolving its delay response with that of the foregrounds and the geometric phases measured by the baseline vector. We discuss the resulting spillover of foreground power beyond the horizon delay limits.

5.1. Effect on Foreground Contamination

Since our aim in this paper is to quantify EoR-foreground power ratio without employing any sophisticated foreground removal techniques, we turn our attention to foreground avoidance strategy that employs spectral weighting technique. In such a scheme, specific choices for spectral weighting function, W(f), have been found to be effective in reducing foreground contamination by many orders of magnitude (Thyagarajan et al. 2013) and is regularly used in EoR data analysis (Parsons et al. 2012a). For instance, a Blackman-Harris function (Harris 1978) has a dynamic range of $\sim 100-120~\mathrm{dB}$ in delay power spectrum and a reduced effective bandwidth, with:

$$\epsilon = \frac{1}{B} \int_{-B/2}^{+B/2} |W(f)|^2 df,$$
 (8)

and,
$$B_{\text{eff}} = \epsilon B$$
, (9)

where, $1 - \epsilon$ is the loss in overall spectral sensitivity and $B_{\rm eff}$ is the effective bandwidth. For a *Blackman-Harris* window function denoted by $W_{\rm BH}(f)$, $\epsilon \approx 50\%$.

Considering that the dynamic range required to suppress foreground contamination in the *EoR window* may probably be even higher than that provided by a *Blackman-Harris* window function, we use a modified version given by the convolution of a *Blackman-Harris* window with itself:

$$W(f) = W_{\rm BH}(f) * W_{\rm BH}(f).$$
 (10)

Fig. 1 shows the *Blackman-Harris* window (gray) and the window in equation 10 (black) in frequency (top) and their power responses in delay (bottom). In its Fourier domain, this window has a response obtained by squaring the *Blackman-Harris* window response and thus increases the dynamic range further in the power response by another $100-120~\mathrm{dB}$ with $\epsilon \approx 42\%$.

This is an enormous gain in sidelobe characteristics for a small loss of sensitivity relative to a simple Blackman-Harris weighting. This will ensure that the contamination resulting from spillover of foregrounds along the line-of-sight k-modes are limited only by intrinsic spectral structures in the foregrounds or beam patterns and not by sidelobes from spectral weighting. In this paper, we apply this modified spectral weighting function defined in equation 10 whenever foregrounds are represented in the Fourier delay domain.

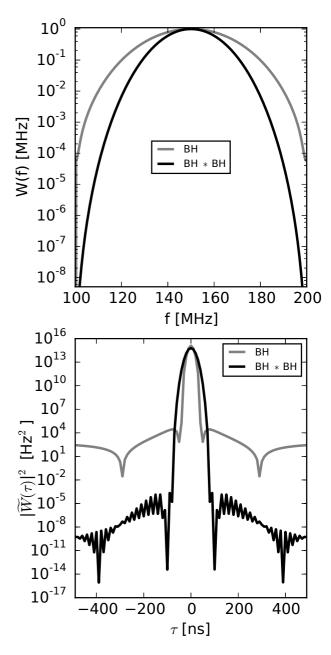


Figure 1. Choices for spectral weighting functions, W(f) (top) and their delay power spectrum responses, $|\widetilde{W}(\tau)|^2$ (bottom). The gray curves correspond to a Blackman-Harris window while those in black correspond to a Blackman-Harris window convolved with itself. The overall sensitivity of the former is $\epsilon \approx 50\%$ of a rectangular window while that of the latter is $\epsilon \approx 42\%$. As a result, the main lobe of the convolved window function response is slightly wider than that of a Blackman-Harris window. However, the sidelobes from the convolved window function are suppressed by more than ten orders of magnitude relative to that of a nominal Blackman-Harris window.

In HERA-19 array layout, there are 30 unique baseline vectors and 8 unique baseline lengths. Fig. 2 shows the delay power spectra of foregrounds on the 8 unique baseline lengths obtained with the aforementioned models for power pattern at arbitrary pointings on the sky. In all these panels, the full-band foreground delay power spectra obtained with achromatic, *Airy* and fully chromatic simulated beam patterns are shown in black, red, and

blue respectively. The brightening of foreground power near the horizon limits (vertical dotted lines) due to the pitchfork effect (Thyagarajan et al. 2015a,b) is prominently seen in all cases. A clear broadening of spilloverwings outside the horizon limits is seen with increasing chromaticity as the beam is changed from the achromatic to the Airy to the chromatic simulated model. For instance, the spillover from foreground delay power spectrum obtained with chromatic beam pattern is restricted to $|k_{\parallel}| \lesssim 0.2 \, h \, \mathrm{Mpc^{-1}}$, with the Airy pattern it is restricted to $|k_{\parallel}| \lesssim 0.15 \, h \, \mathrm{Mpc^{-1}}$, while with the achromatic beam it is restricted to $|k_{\parallel}| \lesssim 0.12 \, h \, \mathrm{Mpc^{-1}}$ even on longest baseline lengths. It is also noted that despite the extreme dynamic range of the spectral weighting function employed, the tail of the foreground spillover at $|k_{\parallel}| \gtrsim 0.2 \, h \, \mathrm{Mpc}^{-1}$ with an Airy beam pattern is many orders of magnitude higher than that using an achromatic beam while that from the simulated chromatic beam is even higher than from an Airy pattern by a few orders of magnitude. This signals that the foreground spillover shown are truly limited by intrinsic spectral features in the antenna beam patterns.

This clearly demonstrates that higher the beam chromaticity, the farther the foreground contamination inherently extends along k_{\parallel} . Thus, the chromaticity of antenna beam needs to be carefully controlled in EoR experiments in order to keep the foreground systematics sufficiently low.

Such a significant spillover is not bound by the horizon limits of the foreground wedge because this is caused by spectral structure in the antenna beam pattern which is independent of the position-dependent geometric delays. As a result delay-based complex deconvolution techniques such as CLEAN (Taylor et al. 1999; Parsons & Backer 2009; Parsons et al. 2012b) that rely on smoothness of foreground spectra and only spectral window shape will not have adequate information to accurately deconvolve intrinsic supra-horizon spillover arising from the chromaticity of the antenna beam. While delay power spectrum estimation using foreground removal strategy that accounts for direction- and beam chromaticity-dependent effects is possible, we leave it for future work.

5.2. Constraints on Reflections in the Instrument

One of the primary causes for spectral structure in antenna power patterns is reflections in the instrument. Patra et al. (2016) and Ewall-Wice et al. (2016) discuss the measured and simulated reflections respectively between a dish and its feed. Reflection between structures and signal paths from different antennas also causes chromaticity in the antenna beam. In this section, we provide cosmologically motivated design specifications on instrument systematics caused by these two types of reflections.

The effect of reflections it to shift the measured fore-ground power to higher modes in τ (or in k_{\parallel}) and thus cause further contamination in these higher k_{\parallel} -modes which are considered sensitive for EoR HI signal detection. These delay shifts introduce ripples in the spectrum. The net chromaticity in the measurements is the product of spectral structure arising out of the intrinsic nature of foreground emission, the baseline- and position-dependent frequency structure of the geometric phases,

the spectral features in the antenna power pattern besides any other spectral structures in the instrument unaccounted for. In the Fourier domain these factors have a convolving effect. In order to isolate the requirements on beam chromaticity from other sources of chromaticity, we start with an antenna beam in which those spectral structures are absent but the intrinsic chromaticity of foregrounds and the geometric phases of baselines are included

We define the required attenuation on the reflected foreground power as the ratio:

$$\Gamma_{k_{\mathrm{p}}}(\tau) \ge \max_{|k_{\parallel}| > k_{\mathrm{p}}} \left\{ \frac{P_{\mathrm{FG}}(k_{\parallel} - \frac{\mathrm{d}k_{\parallel}}{\mathrm{d}\tau} \tau)}{P_{\mathrm{HI}}(k_{\parallel})} \right\}^{1/2}, \tag{11}$$

where, $P_{\rm HI}(k_{\parallel})$ is the EoR HI power spectrum for the chosen antenna spacing, $P_{\rm FG}(k_{\parallel})$ is the foreground delay power spectrum obtained with the spectral weighting function applied over the full-band of the three uniquely oriented 14.6 m antenna spacings further averaged over a 0–12 hr local sidereal time (LST) range and over both positive and negative k_{\parallel} -modes, τ is the delay caused by reflections, and $dk_{\parallel}/d\tau$ is the *jacobian* in the transformation of τ to k_{\parallel} (see equation 6). Thus, $\Gamma_{k_{\rm p}}(\tau)$ is determined by the requirement that the reflected foreground power obtained by shifting in delay is below the EoR HI signal power in line-of-sight spatial scales of interest given by $|k_{\parallel}| > k_{\rm p}$.

Both EoR models were used separately in this analysis to reduce the dependence of design specifications for reflections on any single model. However, we found similar results except for minor differences caused by small amplitude differences between the two EoR models. Hence, we only use results from using EoR model 1 at 150 MHz $(z \approx 8.47)$.

5.2.1. Reflections in Dish-Feed Assembly

For reflections caused by dish-feed assembly, we use $P_{\rm FG}(k_{\parallel})$ obtained with the achromatic beam model on a 14.6 m baseline in equation 11. Fig. 3 shows $\Gamma_{k_{\rm p}}(\tau)$ (in dB) for $k_{\rm p}$ chosen to be 0.1 h Mpc⁻¹ (solid), 0.15 h Mpc⁻¹ (dashed), and 0.2 h Mpc⁻¹ (dotted). These curves set an upper limit for the reflected foreground power to lie below the EoR HI signal power as a function of delays. These reflections are primarily caused in the dish-feed assembly and to some extent in other subsystems not accounted for. It implies that if these reflections are attenuated to levels that lie in the regions below the different shaded regions, such spectral systematics in the instrument will not hinder detection of EoR in those corresponding k_{\parallel} -modes of interest.

The elbow-shaped turnover is a measure of the most severe requirement on attenuation of reflections. This depends sensitively on the chosen k_{\parallel} modes. For instance, the attenuation required is $\gtrsim 54$ dB at ~ 200 ns for $k_{\rm p} = 0.1\,h\,{\rm Mpc^{-1}}$, $\gtrsim 56$ dB at ~ 300 ns for $k_{\rm p} = 0.15\,h\,{\rm Mpc^{-1}}$ and $\gtrsim 58$ dB at ~ 400 ns for $k_{\rm p} = 0.2\,h\,{\rm Mpc^{-1}}$. Measurements by Patra et al. (2016) show that the return losses for HERA lie well within the regions excluded by the shaded regions thus implying that the attenuation is well above the lower limit and hence will not prevent EoR detection.

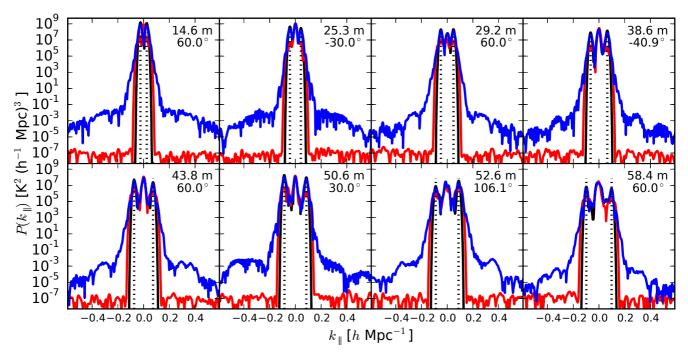


Figure 2. Foreground delay power spectra in units of $K^2(h^{-1} \text{ Mpc})^3$ on unique baseline lengths of HERA-19 at arbitrary sky pointings. The baseline length and orientation (anti-clockwise from East) are annotated at the top right corner of each panel. Black, red and blue curves correspond to delay power spectra obtained with achromatic, Airy and chromatic simulated antenna beams respectively. The achromatic beam has no spectral structure, the simulated chromatic beam has maximum chromaticity while a nominal Airy pattern has intermediate level of chromaticity. The pitchfork effect is clearly visible as peaks around the horizon limits. With increase in chromaticity of the antenna beam the foreground spillover beyond the foreground wedge becomes progressively worse - the extent of foreground-spillover wings beyond the horizon limits (vertical dotted lines) and the amplitude of spillover beyond $k_{\parallel} \gtrsim 0.2 h \text{ Mpc}^{-1}$ is most severe for the chromatic simulated beam, intermediate for an Airy pattern and negligible for an achromatic beam.

5.2.2. Antenna-to-Antenna Reflections

Similarly, for reflections arising out of structures and interfaces across different antennas, we use $P_{\rm FG}(k_{\parallel})$ obtained with the simulated chromatic and Airy antenna beams on 14.6 m baselines. These beams do not include spectral features from antenna-to-antenna reflections. Thus $\Gamma_{k_{\rm p}}(\tau)$ provides lower limit for attenuation of antenna-to-antenna reflections. Fig. 4 is similar to Fig. 3 with constraints for values of $k_{\rm p}$ chosen to be 0.1 h Mpc⁻¹ (left), 0.15 h Mpc⁻¹ (middle), and 0.2 h Mpc⁻¹ (right). Lower limits are estimated for Airy (dashed lines) and simulated chromatic beams (solid lines).

Increase in beam chromaticity makes the lower limits on attenuating reflections more severe relative to that from an achromatic beam. For instance, for $k_{\rm p}=0.1\,h$ $\rm Mpc^{-1}$ there is no delay at which the required attenuation is unconstrained to the left of the elbow-shaped turnover, including at $\tau=0$. This means that when additional chromaticity from antenna-to-antenna reflections is taken into account, the requirement that all k_{\parallel} -modes with $k_{\parallel}>0.1\,h$ $\rm Mpc^{-1}$ be accessible for EoR signal detection will not be satisfied with the currently simulated chromatic beam for HERA. For $k_{\rm p}=0.15\,h$ $\rm Mpc^{-1}$, there is a narrow range of allowed attenuation which is unconstrained for $\tau\lesssim50$ ns. However, for $k_{\parallel}>0.2\,h$ $\rm Mpc^{-1}$, the foreground power spectrum using simulated chromatic dish beam will have enough room to be effective for EoR signal detection despite additional chromaticity arising from antenna-to-antenna reflections.

We note here that designing a dish whose antenna beam closely resembles a nominal Airy pattern will have a significantly higher tolerance for allowing antenna-toantenna reflections and yet remain very effective for EoR signal detection. The HERA collaboration constantly pursues improvement of its dish design to minimize limitations from such chromatic systematics.

In both types of reflections discussed, similar design limits on reflections on various antenna spacings were also studied. With increase in baseline length, the amplitude of foreground power decreases but the foreground window also widens. This means the amplitude of reflections required to be suppressed is lower but there is lesser room along delay axis before the reflected foreground modes shift to and contaminate the k_{\parallel} -modes of interest. As a result, the elbow-shaped design constraints shift upward and leftward. For instance, in the presence of dish-feed reflections, it will still be feasible to probe $k_{\parallel} > 0.15 \, h \, \mathrm{Mpc^{-1}}$ with the 58.4 m baselines but not other larger scales.

6. EOR-FOREGROUND DYNAMIC RANGE

Here our goal is to estimate the EoR-foreground dynamic range (ratio of EoR signal power to foreground power) in the presence of antenna beam chromaticity, using HERA as an example. In order to avoid signal evolution across the entire bandwidth, we use subbands in which EoR signal evolution is not expected to be significant. These subbands with $B_{\rm eff}=10$ MHz are defined by spectral weights obtained by convolution of Blackman-Harris window with itself. These subbands are centered at 150 MHz and 170 MHz to estimate EoR-foreground dynamic range at $z\approx 8.47$ and $z\approx 7.36$ respectively. We use both EoR models 1 and 2 to reduce the dependence

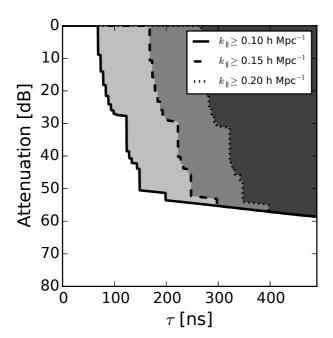


Figure 3. Minimum required attenuation (in dB) for internal dish-feed reflections required to keep the reflected foreground power below EoR HI signal power for all k_{\parallel} -modes greater than $0.1\,h\,{\rm Mpc^{-1}}$ (solid), $0.15\,h\,{\rm Mpc^{-1}}$ (dashed) and $0.2\,h\,{\rm Mpc^{-1}}$ (dotted). This is obtained on 14.6 m antenna spacing for EoR model 1 at 150 MHz ($z\approx 8.47$) and foreground power obtained with an achromatic antenna beam model. When the attenuation on dishfeed reflections is higher than these limits (outside the shaded regions), EoR will be detectable in respective k_{\parallel} -modes despite these reflections

of this analysis on any single EoR model.

6.1. Dependence on Baseline- k_{\parallel} Parameter Space

We estimate the ratio of EoR signal and foreground powers for HERA, where the latter is obtained with three antenna beams of different chromaticities. Fig. 5a and 5b show the EoR signal and foreground power in 150 MHz and 170 MHz subbands respectively. EoR models 1 and 2 are shown in cyan and gray respectively. The foreground delay power spectra obtained with achromatic, Airy and simulated chromatic antenna patterns are shown in black, red, and blue respectively. Each panel corresponds to a unique baseline vector, same as in Fig. 2.

Due to narrower subbands, the resolution of the foreground delay spectrum is coarser and the central region of foreground contamination extends to $|k_{\parallel}| \lesssim 0.2\,h$ Mpc⁻¹. The coarsening of delay resolution significantly absorbs the distinct differences caused by beams of different chromaticities as seen in the full-band foreground delay spectra outside the foreground wedge in Fig. 2. This means the foreground spillover wings that extend beyond the horizon even in the case of simulated chromatic beam are on spectral scales larger than the 10 MHz effective bandwidth of the subbands. Hence, this results in an EoR signal-foreground crossover at $|k_{\parallel}| \gtrsim 0.2\,h$ Mpc⁻¹ independent of different antenna beam chromaticities used in this analysis.

From Fig. 5, it is clearly demonstrated that across all baselines and subbands, HERA should detect EoR by more than two orders of magnitude above foreground

contamination obtained with any level of antenna beam chromaticity.

6.2. Dependence on Baseline-RA Parameter Space

We investigate the EoR-foreground dynamic range in two dimensional parameter space formed by baselines and pointings in Right Ascension (RA $\equiv \alpha$) to highlight capabilities of HERA and provide clues for the best observing window.

Due to the assumed isotropy of the redshifted HI power spectrum, it is independent of α . However, it is dependent on the center of the subband, f_0 , where $f_0 = f_{21}/(1+z)$. The foreground delay power spectra depends on both f_0 and α . Thus, we rewrite the EoR HI and foreground delay power spectra explicitly as a function of these quantities as $P_{\rm HI}(|\boldsymbol{b}|,k_{\parallel},f_0)$ and $P_{\rm FG}(\boldsymbol{b},k_{\parallel},f_0,\alpha)$ respectively.

 $P_{\mathrm{FG}}(\boldsymbol{b},k_{\parallel},f_{0},\alpha)$ respectively. We define baseline-dependent k_{\parallel} -modes of interest for foreground avoidance as $|k_{\parallel}|>k_{\parallel}^{\mathrm{FA}}(\boldsymbol{b})$, with:

$$k_{\parallel}^{\text{FA}}(\mathbf{b}) = \frac{2\pi f_{21} H_0 E(z)}{c(1+z)^2} \left(\frac{|\mathbf{b}|}{c} + \frac{\zeta}{B_{\text{eff}}}\right),$$
 (12)

where, the first term inside the parenthesis denotes the horizon limit, the second relates to the resolution due to subband bandwidth, B_{eff} , and ζ denotes a buffer to ensure the $k_{\parallel}^{\text{FA}}(|\boldsymbol{b}|)$ threshold "safely" avoids the main lobe of foreground power. In this study, we use $\zeta=3.5$.

We estimate the worst case EoR-foreground dynamic range in the $b-\alpha$ parameter space as:

$$\rho(\boldsymbol{b}, f_0, \alpha) = \min_{\|\boldsymbol{k}_{\parallel}\| > k_{\parallel}^{\text{FA}}(\|\boldsymbol{b}\|)} \left\{ \frac{P_{\text{HI}}(\|\boldsymbol{b}\|, k_{\parallel}, f_0)}{P_{\text{FG}}(\boldsymbol{b}, k_{\parallel}, f_0, \alpha)} \right\}.$$
(13)

This denotes the minimum EoR-foreground dynamic range in k_{\parallel} -modes of interest for foreground avoidance, $|k_{\parallel}| > k_{\parallel}^{\text{FA}}(\boldsymbol{b})$, for each baseline vector (\boldsymbol{b}) , subband (f_0) , and sky pointing (α) .

We consider the foreground power spectrum obtained with the simulated chromatic antenna beam, and EoR models 1 and 2, in each of the 150 MHz and 170 MHz subbands. Fig. 6 shows $\rho(\boldsymbol{b}, f_0, \alpha)$ for all 30 unique HERA baselines over 24 hours of α for the two EoR models and two subbands used in this study.

For the baselines considered, $\rho(\boldsymbol{b}, f_0, \alpha)$ increases with longer baselines. We attribute this to the much steeper dependence of foreground emission on baseline length than that of EoR HI power. This is also confirmed from Fig. 5 where the peak and sidelobe levels of foreground power obtained with the simulated chromatic antenna beam on the 14.6 m baseline, which is sensitive to diffuse emission, progressively drops by two orders of magnitude on the 58.4 m baseline where diffuse emission is not as dominant. Hence, from a foreground contamination standpoint, the shortest baselines are less sensitive than the longer ones in the HERA-19 layout.

However, in all four cases considered here, except when the Galactic center appears overhead in the RA range roughly in the range 16-19 hr, the worst case signalforeground ratio lies above unity in most of this parameter space. It demonstrates that HERA should detect the EoR signal with a very high signal-foreground ratio on all baselines in a vast majority of the pointings.

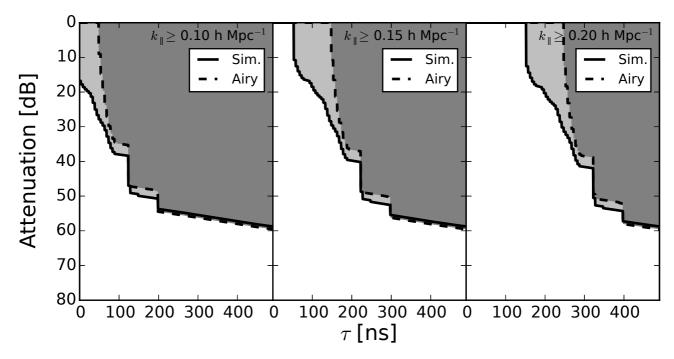


Figure 4. Minimum required attenuation (in dB) for antenna-to-antenna reflections to keep reflected foreground power below EoR HI signal power for all k_{\parallel} -modes greater than $0.1\,h$ Mpc⁻¹ (left), $0.15\,h$ Mpc⁻¹ (middle) and $0.2\,h$ Mpc⁻¹ (right). This is obtained on 14.6 m antenna spacing for EoR model 1 at 150 MHz ($z\approx8.47$) and foreground power obtained with an Airy (dashed) and simulated chromatic (solid) antenna beam models. Regions excluding shaded regions indicate EoR will be detectable in respective k_{\parallel} -modes despite these reflections. Increase in beam chromaticity makes the requirement on attenuation more severe. For instance, $k_{\parallel} > 0.1\,h$ Mpc⁻¹ modes will be inaccessible with the simulated chromatic beam if these reflections are taken into account. However, for the same beam the instrument will have much higher tolerance despite these reflections if the modes of interest are $k_{\parallel} > 0.2\,h$ Mpc⁻¹. Due to lower chromaticity, an Airy beam offers more tolerance to reflections than the simulated chromatic beam.

7. SUMMARY

First-generation EoR experiments such as the MWA, PAPER and LOFAR have made enormous progress in the field of 21 cm cosmology. However, they are currently limited by the systematics due to extremely bright foregrounds and the instrument. Hence, characterizing these to a very high level of precision is critical for the success of next-generation EoR experiments. In this paper, we highlight the importance of a key systematic feature of the instrument – the spectral structure of the antenna power pattern – and its impact on EoR signal contamination, using HERA as an example.

Using a new high dynamic range spectral weighting function obtained by convolving a *Blackman-Harris* window with itself, we isolate the effects of beam chromaticity on foreground delay power spectrum. We use three antenna beam models of varying chromaticity (achromatic, *Airy* and simulated chromatic) and show that increase in chromaticity extends the foreground spillover well beyond the horizon limits of the *foreground wedge* into the clean *EoR window* considered sensitive for EoR signal detection. The level of foreground spillover in the simulated chromatic beam is a few orders of magnitude worse than that from a nominal *Airy* disk pattern, which in turn is many orders of magnitude worse than that from an achromatic beam with no spectral structure.

We note that the inevitable reflections in the antennafeed assembly and between reflecting structures across multiple antennas are also significant factors that contaminate the cosmological signal in high k_{\parallel} -modes inside the $EoR\ window$. Using a novel approach, we provide

a formalism to set cosmologically-motivated design requirements directly on the level of suppression required on these reflections in the instrument. Ongoing reflectometry studies clearly indicate HERA will comfortably achieve the design limits prescribed here.

Taking into account the effects of these instrumental systematics, if data is not limited by thermal noise, we demonstrate that HERA should detect EoR with high significance with a simple spectral weighting even under a conservative analysis criterion which does not involve foreground removal strategies. All baselines of HERA-19 will not only detect but also help in filtering highly likely EoR models.

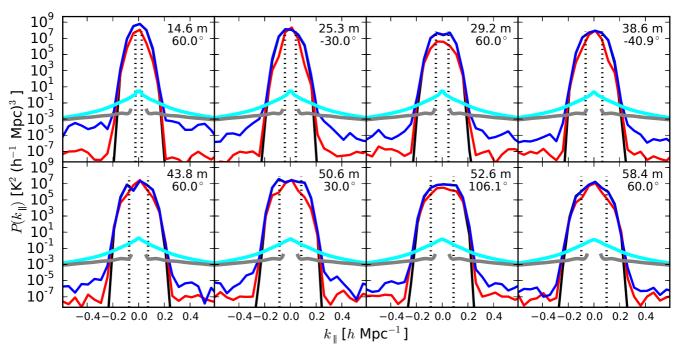
We are also investigating advanced strategies for foreground removal that will robustly eliminate these systematics further. More optimal analysis techniques and further design improvements will make HERA not only clear the obstacles limiting first-generation experiments but also become transformational for next-generation low frequency cosmology experiments.

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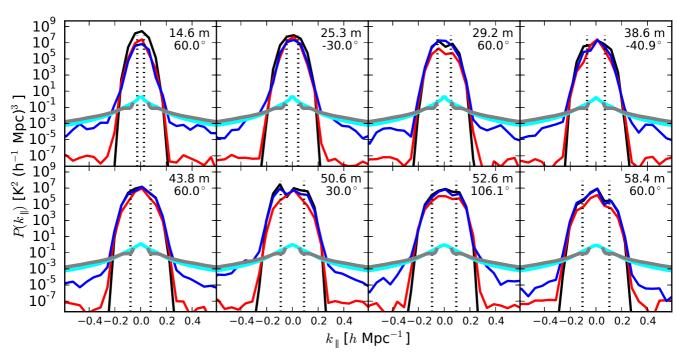
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(a) 150 MHz subband ($z \approx 8.47$)



(b) 170 MHz subband ($z \approx 7.36$)

Figure 5. EoR signal and foreground delay power spectrum in units of $K^2(h^{-1} \text{ Mpc})^3$ in 150 MHz (top) and 170 MHz (bottom) subbands $(B_{\text{eff}} = 10 \text{ MHz})$ on eight unique baseline lengths of HERA-19 at arbitrary sky pointings. The length and orientation of the baseline vector corresponding to each panel is annotated on the top right corner. EoR models 1 and 2 are shown in cyan and gray respectively. The foregrounds obtained with achromatic, Airy and simulated chromatic antenna beams are shown in black, red and blue respectively. EoR-foreground dynamic range is highest for antenna beam with least chromaticity and vice versa. Even for the simulated chromatic antenna beam pattern, which has the highest chromaticity among the antenna beam models considered, foreground power will be lower than signal power from the two independent EoR models by more than two orders of magnitude for $|k_{\parallel}| \gtrsim 0.2 \, h \, \text{Mpc}^{-1}$ on all HERA baselines.

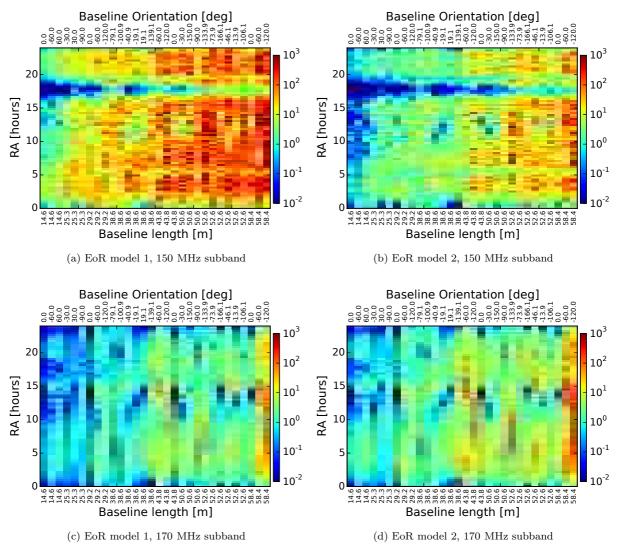


Figure 6. Worst case EoR-foreground dynamic range, $\rho(\boldsymbol{b}, f_0, \alpha)$, in foreground avoidance modes for different HERA-19 baselines as a function of RA (α) of pointing on the sky. Each panel corresponds to the EoR model and subband indicated. The baseline vector is specified by its length (in m) and orientation (in degrees) at the bottom and top of the x-axis respectively. The color scale is logarithmic. Even in the worst case, HERA will be able detect EoR drawn from independent models on all baselines for a large fraction of a full 24 hour sky transit cycle. $\rho(\boldsymbol{b}, f_0, \alpha)$ is seen to increase with increasing baseline length. This is because the loss in sensitivity to diffuse foreground power with increase in antenna spacings is faster than in the case of the EoR signal.

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