

This is an *individual* assignment: collaboration (such as discussing problems and brainstorming ideas for solving them) on this assignment is highly encouraged, but the work you submit must be your own. Give information only as a tutor would: ask questions so that your classmate is able to figure out the answer for themselves. It is unacceptable to share any artifacts, such as code and/or write-ups for this assignment. If you work with someone in close collaboration, you must mention your collaborator on your assignment.

Suggested practice problems, from CLRS: 22.1-1 through 22.1-5; 22.1-6 (challenge); 22.2-3; 22.2-6; 22.3-6; 22.3-8; 22.3-11; 22.4-2; 22.4-5; 22.5-3; 22.5-4

1. **(From problem set 5; previous exam question)** Let $A[1..n]$ be an array of non-integers taken from some set K of size $k > 1$. (*Note: For this problem, you are not given the set K or k ; this is only to illustrate that there are k distinct non-integer numbers. We only have access to elements through A . Further, note that k may be small or large: from constant to even larger than n .*)
 - (a) An algorithm that sorts A is described as a counting sort that iterates through the A , when a new key is found a node with a variable count is created and inserted in the binary search tree B . In the case of key we have already found we will increment the count value in the appropriate node. Going through the array will take n time. Then for k distinct keys we will create a mode which will take at most $\lg k$ time. So, the entire algorithm will take $O(n + k \lg(k))$.
 - (b) The worst-case running time for my algorithm would be $O(n \lg n)$. Since there would be at most n distinct keys where there are no repeated values.
2. Let $G = (V, E)$ be an n -vertex undirected graph consisting of *cops* and *robbers* as vertices. You are given two facts about the graph:
 - (a) G is connected, and
 - (b) each edge is incident to exactly one cop and one robber. (That is, no edge is incident to two cops, and no edge is incident to two robbers.)

Suppose we know that $\text{Dave} \in V$ is a cop. Give an efficient algorithm to distinguish all cops from all robbers.

We will find all cops and robbers by using a modified breadth-first search. Since $\text{Dave} \in V$ and is a cop, there will be a set of neighbors. Since each edge is incident to only one cop and one robber. All of Dave's neighbors would be robbers. Then each of the robber's neighbors that haven't been visited are cops and well. And the search will reach every node since the graph is connected.

3. Problem 22.2-5 from CLRS.
4. Problem 22.5-1 from CLRS. In addition to stating your answer, also (formally) prove its correctness.

When an edge is added the amount of strongly connected components can either stay the same if the edge is incident to two nodes in the same component or decrease by 1 if the edge is added between 2 components.

5. 1: **function** SEMICONNECTED-CHECK(G)
2: $G_R \leftarrow$ STRONGLY-CONNECTED-COMPONENTS(G)
3: $s \leftarrow G_R[0]$
4: DFS-VISIT(G_R, s)
5: **for all** $u \in G_R$ **do**
6: **if** $u.color == WHITE$ **then**
7: **return** false
8: **return** true
